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Experimental Demonstration of Enhanced Photon Recycling in Angle-Restricted GaAs Solar Cells

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Abstract

For cells near the radiative limit, optically limiting the angles of emitted light causes emitted photons to be recycled back to the cell, leading to enhancement in voltage and efficiency. While this has been understood theoretically for some time, only recently have GaAs cells reached sufficient quality for the effect to be experimentally observed. Here, as proof of concept, we demonstrate enhanced photon recycling and open-circuit voltage (Voc) experimentally using a narrow band dielectric multilayer angle restrictor on a high quality GaAs cell. With angle restriction we observe a clear decrease in the radiative dark current, which is consistent with the observed Voc increase. Furthermore, we observe larger Voc enhancements for cells that are closer to the radiative limit, and that more closely coupling the angle restrictor to the cell leads to greater Voc gains, emphasizing the optical nature of the effect.

1 Introduction

For ideal solar cells where all recombination is radiative, photons emitted from the cell are the sole source of carrier loss, as in the well-known Shockley-Queisser or detailed balance limit [1]. Cells approaching this radiative limit have significantly higher efficiencies, as evidenced by recent world record GaAs cells, and can also exhibit new effects owing to the significant number of radiatively emitted photons [2, 3, 4]. For example, optically limiting the angles of emitted light, as in figure 1a, causes emitted photons to be recycled back to the cell, leading to enhancement in voltage and efficiency. Despite this theoretical prediction, until recently even the highest efficiency solar cells were not close enough to the radiative limit for such an effect to be observed [5, 6, 7]. However, with the introduction of cells lifted off the growth substrate, GaAs cells have shown significant gains in efficiency due to Voc increases,
indicating an increase in the external radiative efficiency (ERE) of the cell [2, 3, 4]. In these lifted-off GaAs cells radiatively emitted photons are reflected from a metallized back surface instead of being absorbed in the substrate, resulting in a large increase in ERE and Voc [4, 8]. As radiative recombination is dominant in high quality GaAs, these lifted-off cells perform near the radiative limit and are therefore suitable for experimentally demonstrating enhanced photon recycling and Voc via angle restriction of emitted light. In fact, it was recently demonstrated that a voltage increase could be observed in such cells by placing a reflecting dome above the cell to recycle emitted photons [9].

Here, as proof of concept, we demonstrate enhanced photon recycling and open-circuit voltage (Voc) experimentally using an optical element with angle restriction only over the narrow wavelength range of emitted light in GaAs that is placed on a high quality GaAs cell. As in figure 1, we design a dielectric multilayer angle restrictor with excellent normal incidence transmission and high reflectivity at oblique angles for radiatively emitted wavelengths. Using this narrow band angle restrictor with a high quality GaAs cell, we observe enhanced photon recycling and a resulting voltage increase. In other words, simply placing an angle restrictor on the cell causes a voltage increase of 3.6mV without a change in current. In addition, we observe a 12% decrease in the radiative component of the dark current, which is consistent with the observed Voc increase. Considering a variety of cells, the largest Voc enhancements occur in cells that are closest to the radiative limit, with maximum ERE values of 15.7%. Finally, we see that more closely coupling the angle restrictor to the cell leads to greater Voc gains, emphasizing the optical nature of the enhancement.

The predicted voltage increase from angle restriction follows directly from the principles of detailed balance [1]. For a solar cell in the radiative limit at steady state and open circuit, detailed balance requires that the number of photons leaving the cell equal the number of photons entering the cell. Mathematically, we express this as

$$\int_{E_g}^{\infty} S(E) a(E) dE = \int_{\Omega_c} \int_{E_g}^{\infty} a(E) \frac{2}{\hbar^2 c^2} \frac{E^2}{e^{(E-q\text{Voc})/kT} - 1} dE \cos(\theta) d\Omega$$
where \(a(E)\) is the fraction of photons at energy \(E\) absorbed by the solar cell, \(\Omega_c\) is the solid angle the cell emits into, \(S(E)\) is the solar spectrum, and \(qV_{oc}\) equals the chemical potential of the cell [5]. The left-hand side of the equation gives the photon flux absorbed by the cell, and the right-hand side gives the emitted photon flux at open circuit.

Assuming the Voc does not closely approach the bandgap, we may approximate the Voc under illumination as

\[
V_{oc} \approx kT \ln \left( \frac{\int_{E_g}^{\infty} S(E) a(E) dE}{\int_{\Omega_c} \int_{E_g}^{\infty} a(E) \frac{2}{h^2c^2} \frac{E^2}{e^{(E/qV_{oc})/kT} - 1} dE \cos(\theta) d\Omega} \right) = kT \ln \left( \frac{J_{sc}}{J_0} \right) \tag{1}
\]

where \(J_{sc}\) is the short-circuit current and \(J_0\) is the dark current, which is solely due to radiatively emitted light. Restricting the emission angle causes photons generated by radiative recombination to be recycled and reabsorbed within the cell rather than emitted. Thus, enhanced photon recycling via angle restriction reduces \(J_0\) and increases Voc. For realistic cells, emitted light forms a larger fraction of \(J_0\) in cells closer to the radiative limit. Thus, high ERE cells, like the GaAs cells in these experiments, are required for \(J_0\) to be reduced sufficiently with angle restriction that a voltage increase may be observed. Furthermore, higher ERE cells should show larger voltage increases. For this reason, though the voltage increases in this proof-of-concept experiment are modest, further improvements in GaAs cell technology could significantly increase the performance benefits from angle restriction. In fact, for an Auger-limited GaAs cell, angle restriction is predicted to give cell efficiencies above 38% [6]. For terrestrial applications, we envision a flat plate, one sun, angle restricting system with high quality GaAs cells. While tracking may be beneficial, high accuracy tracking is not required as dielectric angle restrictors have a relatively large acceptance angle. Furthermore, for cells in the ERE range considered here, narrow angle restriction has limited benefit, as non-radiative recombination limits the possible voltage increase. (The supplemental includes a calculation with the angle dependence of Jsc.) Additionally, recent work has demonstrated the fabrication of high ERE cells in other III-V materials, notably
GaInP, suggesting that this approach will become more broadly applicable with continued cell development, and could easily be incorporated with multijunctions [10]. Use with these cell technologies also suggests early applications in military and space solar, where efficiency and weight are paramount.

While our previous work has considered broadband ray optical angle restrictors with light trapping cells, the cells in this experiment have high reflectivity specular back reflectors that are metallic, with reflectivity of 75.5%, or metallodielectric, with reflectivity of 99.7%. The calculated reflectivity values refer to band edge (873nm) emission angle-averaged within the GaAs. As the solar cells are planar and do not incorporate light trapping, we utilize a dielectric multilayer that provides angle restriction only over the narrow range of wavelengths at the semiconductor band edge where the GaAs cells emit light (see Fig. 1). This narrow-band angle restriction allows diffuse, non-normal incidence light to enter over most of the spectral range. (See SI.) Capturing this diffuse light gives significant current enhancements relative to a broadband concentrator or angle restrictor. In addition, potential losses due to tracking errors are greatly reduced, and simpler, cheaper trackers may be utilized. As in the supplemental, we envision depositing such an angle restrictor in place of a traditional AR coat, so the cost derives only from the added layers relative to a traditional AR coat.

As shown in figure 1b, the angle restrictor design consists of alternating high and low index layers with large refractive index contrast to increase the angular range of reflection [11, 12, 13]. While the design is not strictly periodic, the angular properties can be understood from the Bragg condition

$$\cos \theta = \frac{m \lambda}{2 \Gamma}$$

where $\theta$ is the angle of maximum reflectivity, $\lambda$ is the wavelength, $\Gamma$ is the period of the multilayer, and $m$ is an integer [14]. For shorter wavelengths maximum reflectivity occurs away from normal incidence, providing angle restriction for emitted light and excellent transmission at normal incidence in both the designed and fabricated structures. We note that total internal reflection owing to the high index of GaAs already provides significant photon recy-
Figure 1: Narrowband Dielectric Angle Restrictor Design and Fabrication. a) Experimental set-up: a high quality GaAs cell is placed in optical contact with either a dielectric angle restrictor deposited on fused silica (left) or a bare fused silica control (right) using fused silica index matching fluid at the GaAs-fused silica interface. The emission angles for each optic are shown schematically in yellow. For the experiments in figures 2 and 3, the edges of the optics are coated with a gold reflector to minimize light loss. b) The refractive index at 800 nm as a function of depth for the dielectric angle restrictor multilayer design. (0 represents the air interface). c) Calculated reflectivity for the dielectric angle restrictor design as a function of angle and wavelength. Angles are denoted in air, as we are only concerned with light that is not totally internally reflected. Spectrum of photoluminescence available for photon recycling (white line) indicates the wavelengths where angle restriction is desired. d) Measured reflectivity for the dielectric angle restrictor as deposited with spectrum of photoluminescence available for photon recycling (white line). Reflections at the back surface of the substrate have been subtracted, see SI. Angles are again denoted in air. For both c and d, we plot only wavelengths greater than 600 nm, to correspond with the wavelengths of illumination in the experiment.
clinging within the cell, and despite this, there is still a substantial loss due to emitted light, as ERE estimates indicate [4]. As the measured reflectivity in air, see figure 1d, demonstrates, the dielectric structure provides photon recycling of light that would otherwise be emitted. This enhanced photon recycling occurs in addition to the photon recycling via total internal reflection, which is unaffected by the dielectric structure.

2 Results and Discussion

Theory clearly indicates that enhanced photon recycling via angle restriction will result in a reduction of the radiative dark current. We therefore measured the dark current characteristics of a single cell under both the angle restrictor and a bare fused silica control optic, as in figure 1a, with fused silica index matching fluid at the interface of the cell and the fused silica substrate to avoid extraneous reflections. In the high voltage region near Voc, where radiative emission contributes most significantly to the dark current, we see a clear decrease in dark current with angle restriction, as in figure 2a. To quantify this we fit the dark current, $J_0$, over the high voltage 0.6 to 1.1 V region, to the double diode equation

$$J_0 = J_{01}(e^{\frac{q[V - J_{dark}R_s]}{kT}} - 1) + J_{02}(e^{\frac{q[V - J_{dark}R_s]}{nkT}} - 1)$$

where $J_{01}$ is the high voltage dark current component, $J_{02}$ is the low voltage component, $R_s$ is the series resistance, and $n$ is the diode ideality factor [15, 16]. For both the control and angle restriction curves, the fit is excellent over several orders of magnitude. The fit deviates somewhat at very low currents, which we attribute to shunt resistance and has been previously observed in similar cells [2]. As figure 2b shows, $J_{02}$, $R_s$ and $n$ are unchanged with angle restriction and $n$ is very close to two, indicating that the double diode model is valid [15, 16]. In contrast, the $J_{01}$ term, which has the same voltage dependence as radiative recombination, shows a 12% decrease with angle restriction, well beyond the error of the fit. Thus, by simply changing the optic above the cell to an angle restrictor, we observe a
definite reduction in the dark current. Specifically, the reduction occurs in the high voltage dark current component attributable to radiative loss, indicating that angle restriction is enhancing photon recycling within the cell.

![Graph](image)

**Figure 2:** Dark Current Measurements and Fits. a) Representative dark current curves and double diode fits for both the angle restrictor and control cases. Inset: a clear reduction in dark current is evident near Voc for the angle restrictor case. b) Double diode fitted parameter results with each bar representing one of three trials on the same 15.7% ERE cell for both the angle restrictor and fused silica control. The error bars represent 95% confidence intervals derived from the fit. Consistent with reduced radiative loss, $J_{01}$ shows a marked decrease with angle restriction while all other parameters remain unchanged.

In addition to a reduction in dark current, we also expect a direct Voc enhancement under illumination. Furthermore, this voltage enhancement should be larger for cells with
higher ERE, as more photons are available to be recycled via angle restriction. We therefore measured light current-voltage curves for a set of four cells with differing back reflector and material quality leading to significant variations in ERE across the cells, as determined from the Jsc and Voc characteristics under the control optic. (See SI for further model details.) Owing to a reflecting band in the optical coupler around 550 nm, we limited the spectrum in this proof-of-concept experiment to wavelengths longer than 605 nm. (As in the supplemental, this reflecting band can be eliminated with a rugate filter optical design, but for the initial coupler we did not pursue these structures as they are more difficult to fabricate [17, 18].) As shown in figure 3a, when we directly compare the control and angle restrictor on the same cell, current losses of 3.5% to 5.3% are observed with angle restriction, consistent with the measured normal incidence reflectivity of the angle restrictor. Without a change in the dark current, a reduction in Jsc would normally produce a corresponding reduction in Voc, as in equation (1). However, Voc increases of up to 2.5 mV are observed under angle restriction for the highest ERE cells, as dark current reduction is the dominant effect. Thus, angle restriction increases cell voltage without any change in the illumination, and despite a reduction in Jsc. Furthermore, as we expect for photon recycling, the voltage change tracks the cell ERE.

Fortunately, these current losses are not intrinsic, and result from the simplicity of our initial angle restrictor design [17, 18]. (See SI.) To isolate the photon recycling effect, we adjust the solar simulator to equalize the currents between the control and angle restrictor, as in figure 3b. Once Jsc values are matched for the angle restrictor and control, voltage increases ranging from 1.2mV to 3.6 mV are seen for all cells, with higher ERE cells showing larger voltage increases. As the 15.7% ERE cell was also used for dark current measurements, we can compare the change in $J_{01}$ to the observed change in Voc. Since $V_{oc} = kT \ln(J_{sc}/J_0)$ and the $J_{01}$ term is dominant near Voc, the change in Voc should be approximately $kT \ln(J_{01}/J'_{01})$, where $J'_{01}$ indicates the average fitted value with the angle restrictor. Using this approach, we predict from the dark current fits that the Voc increase
Figure 3: Voltage Increase as a Function of Radiative Efficiency. Measured changes in open-circuit voltage (dark blue line) and short-circuit current (green line) with angle restriction. The set of four cells is plotted as a function of external radiative efficiency (ERE) determined from Jsc and Voc under the control optic. Variations in ERE occur between cells owing to differences in back reflectors and material quality. The error bars are calculated from standard deviation of five measured trials. The dotted white line indicates the expected voltage increase based on a modified detailed balance calculation. The light blue area shows the expected range of the model based on uncertainty in Jsc, Voc, and temperature. a) No solar simulator adjustment. Cells with high external radiative efficiency show a voltage increase despite a reduction in current. b) The solar simulator was adjusted so that currents were equalized with the angle restrictor and control. With this current equalization, all cells see a voltage increase, with high ERE cells seeing a larger voltage increase.
should be 3.0 mV, which is reasonably consistent with the measured value of 3.6 mV for this cell. Thus, we observe a clear Voc increase with angle restriction that is consistent with our dark current measurements, and an ERE trend that indicates enhanced photon recycling as the mechanism.

We also develop a model that directly relates the voltage increase to the optical characteristics of the angle restrictor. While detailed balance is traditionally considered an idealized model, we have developed a more realistic detailed balance model that includes the cell thickness, anti-reflective coating, back reflectors, and Auger and surface recombination. (Further details are provided in the SI.) To account for the optical environment, we calculate the angle-averaged emissivity for both the control and the angle restrictor based on measured reflectivity data as in figure 1d. For each cell, we use the values for Jsc and Voc measured under the control optic to determine the cell’s ERE. (See SI.) We then predict the Voc under angle restriction based on the previously determined ERE and measured Jsc. Finally, the observed temperature fluctuations of 0.1 °C and uncertainty estimates for Jsc and Voc are used to determine the range of the prediction, as in figure 3. These calculations agree quite well with the experimental results, indicating that the reduction in emissivity with angle restriction and the resulting photon recycling enhancement fully explain the observed differences in Voc.

Lastly, we perform a series of experiments where we gradually increase the photon recycling and Voc by coupling the angle restrictor more closely to the cell. As shown in figure 4, we begin by placing a large, uncoated fused silica cylinder above the cell which allows light to escape unimpeded from both the sides and the top of the cylinder. In essence, this fused silica spacer facilitates the outcoupling of light emitted from the solar cell to free space, similar to the glass sphere often used with light-emitting diodes. As before, index matching fluid is used at the fused silica-GaAs cell interface. Then, the angle restrictor is placed on a series of fused silica spacers with non-reflecting, uncoated sides that allow light to escape, with index matching fluid between the spacer and the angle restrictor substrate. As the height
Figure 4: Voltage Increase as a Function Angle Restrictor Coupling. Measured open-circuit voltage (dark blue line) and short-circuit current (green line) as angle restriction is increased by coupling the angle restrictor more closely to the 15.7% ERE cell. The x-axis labels indicate the height of the fused silica spacer below the dielectric angle restrictor, or bare fused silica control, as on the far left. For all but the rightmost optical configuration, the sides of the fused silica spacers are uncoated to allow emitted light may escape. Thus, a taller spacer allows more light to escape from the sides, reducing photon recycling to the 1 cm² cell. In the rightmost configuration, the sides of the fused silica substrate are coated with a reflector to avoid side loss and maximize photon recycling by the dielectric angle restrictor. The error bars are calculated from standard deviation of five measured trials. The dotted white line indicates the expected Voc based on a modified detailed balance calculation. The light blue area shows the expected range of the model based on uncertainty in Jsc, Voc, and temperature. The solar simulator was adjusted as necessary to equalize the currents across the various optical configurations.
of the spacer is reduced, less light escapes through the transparent sides of the spacers and more light is recycled back to the cell by the dielectric angle restrictor. Finally, we use an angle restrictor with reflecting sides to prevent light escape from the sides of the fused silica substrate and maximize the photon recycling. As figure 4 illustrates, more closely coupling the angle restrictor to the solar cell increases the observed Voc, demonstrating that more effective angle restriction leads to enhanced photon recycling and Voc. We also find close agreement between the experiment and realistic detailed balance calculations, indicating that the coupling of the angle restrictor explains the observed changes in Voc.

3 Conclusion

We have performed a series of experiments that clearly demonstrate enhanced photon recycling and resulting Voc increases of up to 3.6mV via angle restriction with a narrowband dielectric multilayer angle restrictor. Dark current measurements show a 12% decrease in the radiative component of the dark current consistent with the observed voltage enhancement. In addition, measurements of the voltage increase on several cells illustrate that cells closer to the radiative limit show larger voltage enhancements, as we expect for photon recycling. These measurements also show good agreement with calculations based on the measured reflectivity of the angle restrictor. Finally, we have shown that more closely coupling the angle restrictor to the cell leads to predictable increases in voltage for several configurations, emphasizing that this voltage increase is due to a purely optical photon recycling effect.

Thus, we have demonstrated as a proof of concept that angle restriction with a narrowband dielectric multilayer leads to enhanced photon recycling and a corresponding voltage increase in high quality GaAs cells. The narrowband angle restrictor approach has significant advantages in admitting diffuse light and in the relatively simple design that can replace an existing anti-reflective coating. While the voltage enhancements shown here are relatively small, the effect becomes much larger as ERE increases and cells approach the radiative
limit. High ERE cells are already being developed for III-V materials to achieve the highest possible voltage and efficiency, and these cells are ideal candidates for a broader applicability of the angle restriction approach [10]. As further improvements are made in III-V cell technology and other materials reach the high ERE regime, this approach holds promise for significantly increasing cell efficiencies in a flat plate geometry.

References


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