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## Machine-learning prediction of metal sulfide photocatalysts for sacrificial hydrogen evolution under visible light irradiation

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The development of promising inorganic semiconductor photocatalysts for water splitting to produce green H<sub>2</sub> is required to achieve a sustainable society. Machine learning is expected to accelerate the exploration of novel inorganic semiconductor photocatalysts. We applied machine learning to explore novel metal sulfide photocatalysts for sacrificial H<sub>2</sub> evolution under visible light irradiation. A machine-learning model that exhibited good accuracy was successfully constructed using our original in-house dataset (not openly shared data) of metal sulfide photocatalysts developed by our group. Then, data on materials in the Inorganic Crystal Structure Database (ICSD) were input into the constructed machine-learning model, resulting in the identification of various metal sulfide candidates with high activities for H<sub>2</sub> evolution in the first screening. We selected Ag<sub>2</sub>CdGeS<sub>4</sub> and Cu<sub>2</sub>CdMS<sub>4</sub> (M = Ge and Sn) among the candidates for the second screening because many photocatalysts containing Cu(I) and/or Ag(I) ions and corner-shared MS<sub>4</sub> tetrahedra have been reported as visible-light-responsive photocatalysts for sacrificial H<sub>2</sub> evolution. Ag<sub>2</sub>CdGeS<sub>4</sub> and Cu<sub>2</sub>CdMS<sub>4</sub> (M = Ge and Sn) photocatalysts, prepared by a solid-state reaction, showed activities for sacrificial H<sub>2</sub> evolution under visible light irradiation. Thus, we developed novel visible-light-responsive metal sulfide photocatalysts for sacrificial H<sub>2</sub> evolution by employing machine learning on our original dataset.

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## Introduction

Photocatalytic water splitting, as artificial photosynthesis, is a promising technology to produce low-cost green H<sub>2</sub> to solve resource, energy and environmental issues.<sup>1–8</sup> Since the report of the Honda–Fujishima effect of water splitting using a TiO<sub>2</sub> photoanode in the early 1970s,<sup>9</sup> various photocatalysts such as metal oxides,<sup>1,2</sup> metal (oxy)sulfides,<sup>10–13</sup> metal (oxy)nitrides<sup>14–21</sup> and polymeric materials<sup>22,23</sup> have been developed. In recent years, Domen and co-workers successfully developed a highly efficient Al-doped SrTiO<sub>3</sub> photocatalyst with a near-unity quantum yield, giving about 0.7% of a solar-to-hydrogen (STH) energy conversion efficiency.<sup>24,25</sup> In addition, they developed an efficient Z-schematic water splitting sheet composed of Rh and

La co-doped SrTiO<sub>3</sub> as an H<sub>2</sub>-evolving photocatalyst, Mo-doped BiVO<sub>4</sub> as an O<sub>2</sub>-evolving photocatalyst and Au as a solid electron mediator, giving about 1.1% STH efficiency.<sup>26</sup> However, the efficiencies are insufficient for practical solar water splitting. Therefore, the development of novel efficient photocatalysts is still a challenging topic. Among various photocatalytic material groups, metal sulfides are attractive because many of them respond to visible light due to the valence band consisting of S 3p orbitals being located at a relatively negative energy level. We have reported various metal sulfide photocatalysts, including Cu-doped,<sup>27</sup> Ni-doped,<sup>28</sup> Pb and A (A = Cl, Br, and I)-codoped ZnS,<sup>29</sup> AgInZn<sub>2</sub>S<sub>9</sub>,<sup>30</sup> NaInS<sub>2</sub>,<sup>31</sup> ZnS–AgInS<sub>2</sub>,<sup>32</sup> ZnS–CuInS<sub>2</sub>,<sup>33</sup> ZnS–CuInS<sub>2</sub>–AgInS<sub>2</sub>,<sup>34,35</sup> A<sup>I</sup>ZnA<sup>IV</sup>S<sub>4</sub> (A<sup>I</sup> = Cu and Ag; A<sup>IV</sup> = Sn and Ge),<sup>36</sup> AGa<sub>2</sub>In<sub>3</sub>S<sub>8</sub> (A = Cu and Ag),<sup>37</sup> Zn<sub>1–2x</sub>(CuGa)<sub>x</sub>Ga<sub>2</sub>S<sub>4</sub>,<sup>38</sup> ZnS–CuGaS<sub>2</sub>,<sup>39</sup> Ni-doped AgGaS<sub>2</sub>,<sup>40</sup> Cu<sub>1–x</sub>Ag<sub>x</sub>GaS<sub>2</sub>,<sup>41</sup> ZnS–CuCl,<sup>11</sup> BaLaCuS<sub>3</sub>,<sup>11</sup> ZnIn<sub>2</sub>S<sub>4</sub>,<sup>11</sup> ZnGa<sub>x</sub>In<sub>2–x</sub>S<sub>4</sub>,<sup>11</sup> MnGaInS<sub>4</sub>,<sup>11</sup> and Cu<sub>3</sub>MS<sub>4</sub> (M = V, Nb and Ta),<sup>11,42</sup> for H<sub>2</sub> evolution in aqueous solutions containing S<sup>2–</sup> and SO<sub>3</sub><sup>2–</sup> ions under visible light irradiation. However, metal sulfide photocatalysts cannot be employed for water splitting as a single particle because they are not chemically stable due to self-oxidation in an aqueous medium under light irradiation. This drawback can be solved by utilizing them as photocathodes and H<sub>2</sub>-evolving photocatalysts in photoelectrochemical and Z-schematic systems for artificial

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photosynthesis, respectively.<sup>43,44</sup> Various photoelectrochemical systems consisting of metal sulfide photocathodes have been constructed for water splitting under visible light irradiation.<sup>39,41,42,45–50</sup> Additionally, powdered Z-schematic water splitting under visible light irradiation has been achieved by using metal sulfides as a H<sub>2</sub>-evolving photocatalyst, metal oxides as an O<sub>2</sub>-evolving photocatalyst, and ionic or solid-state electron mediators such as Co complexes and a reduced graphene oxide.<sup>39,46,51,52</sup> Therefore, it is quite important to develop novel metal sulfide photocatalysts that are responsive to visible light.

So far, photocatalysts have mainly been developed by an intuitive empirical approach. Hence, it is expected that employing machine learning with an objective approach by data-driven science utilizing specialized physicochemical parameters will accelerate the exploration of promising novel photocatalysts. Material development utilizing a machine-learning method is generally referred to as materials informatics (MI) and has been applied to various materials systems, such as catalysts,<sup>53,54</sup> adsorbents,<sup>55</sup> magnetics<sup>56</sup> and batteries.<sup>57,58</sup> Recently, various functional materials, such as alloys, metal oxides, zeolites, metal complexes, metal-organic frameworks and polyoxometalates, have been developed for applications in which the properties of either the surface or the bulk play an important role.<sup>54,59</sup> In contrast, it remains challenging to apply MI to the field of photocatalysts, especially inorganic semiconductor photocatalysts for water splitting, because the photocatalytic reaction involves complicated factors such as photoabsorption, mobility of carriers, recombination, surface reactions, and so on. Although there are some reports of MI application to inorganic semiconductor photocatalysts, these works focus on optimization of photocatalytic reactions rather than developing new photocatalyst materials.<sup>60</sup> Application of MI to develop novel inorganic photocatalysts faces a significant barrier because it is difficult to employ open data from publications, as the photocatalytic activities have not been evaluated under a common set of experimental conditions. This means that the data cannot be compared with each other. Therefore, a large dataset needs to be prepared, including photocatalytic activities evaluated with the same experimental system, photocatalytic compounds and crystal structures, to construct a machine-learning model for training.

We have developed many photocatalysts of metal oxides and metal sulfides that are active for water splitting and sacrificial H<sub>2</sub> and O<sub>2</sub> evolutions.<sup>2,61,62</sup> We possess a large in-house dataset consisting of many photocatalyst compounds, crystal structures, preparation conditions, activities for water splitting, and sacrificial H<sub>2</sub> and O<sub>2</sub> evolutions evaluated under the same experimental conditions. Our dataset contains photocatalyst materials with not only high but also low activities, which is a great advantage for constructing an accurate predictive model. Recently, we have preliminarily demonstrated that a machine-learning model with acceptable accuracy was successfully constructed by employing our original dataset.<sup>63,64</sup> These reports are significant in terms of the effectiveness of our dataset.

In the present study, we constructed a machine-learning model based on our in-house dataset, which was then used to

predict the activities for sacrificial H<sub>2</sub> evolution of metal sulfides listed in the Inorganic Crystal Structure Database (ICSD, a commercially licensed database). Then, we experimentally synthesized Ag<sub>2</sub>CdGeS<sub>4</sub> and Cu<sub>2</sub>CdMS<sub>4</sub> (M = Ge and Sn) from the candidates identified by machine learning and evaluated the activities for H<sub>2</sub> evolution under visible light irradiation.

## Experimental

### Machine-learning methods

We retrieved 8975 data entries of metal sulfide compounds from the ICSD<sup>65,66</sup> in order to confirm the material that had been experimentally identified. In addition, we used an in-house dataset of metal sulfide photocatalysts, including 357 experimental data points developed by our group, as the training data. A representative sample of the original dataset is included as a csv file named 'Example\_of\_original\_dataset' in the SI. Each record in our dataset contains a material variable of chemical composition, 16 variables related to preparation conditions, dopants and cocatalysts, and an objective variable of activities for sacrificial H<sub>2</sub> evolution. The material variable of the chemical compositions in the in-house dataset of metal sulfide photocatalysts developed by our group was converted into numerical features by using XenonPy (version 0.6.5)<sup>67</sup> in order to process machine-learning algorithms. First, chemical compositions were converted into comp\_dict, which is a dictionary of proportions by element, using Pymatgen.<sup>68</sup> Then, after normalization of the proportions, 232 compositional features on the basis of comp\_dict were calculated, such as 58 features (atomic number, bond radius, van der Waals radius, electronegativity, and so on) of weighted average, weighted variance, and the minimum and maximum for each element.<sup>69</sup> The calculated features with high dimensions were projected to the figure with 2 dimensions by principal component analysis (PCA). The figure with axes called principal components shows the diversity of the data features.<sup>70,71</sup> Subsequently, LightGBM,<sup>72</sup> based on a gradient-boosting algorithm, was employed to construct the prediction model of sacrificial H<sub>2</sub> activities of metal sulfide photocatalysts because we focused on understanding the trend of the activities of metal sulfide photocatalysts in order to perform the rough material screening. Logarithmic transformations for the objective variables were used when constructing the machine-learning model. Double-cross-validation and evaluation metrics were carried out by Scikit-learn.<sup>73</sup> A 5-fold double cross-validation was used in this study.

### Preparation of photocatalysts

Ag<sub>2</sub>CdGeS<sub>4</sub> and Cu<sub>2</sub>CdMS<sub>4</sub> (M = Ge and Sn), which were predicted as new photocatalyst candidates by machine learning, were prepared by a solid-state reaction in evacuated quartz ampule tubes. Ag<sub>2</sub>S (Kojundo Chemical, 99%), Cu<sub>2</sub>S (Kojundo Chemical, 99%), CdS (Kojundo Chemical, 99.99%), SnS<sub>2</sub> (Kojundo Chemical, 99.9%) and GeS<sub>2</sub> (Kojundo Chemical, 99.99%) were used as starting materials. They were mixed in an agate mortar with 20% excess Ge for Ag<sub>2</sub>CdGeS<sub>4</sub>, 40% excess Ge



for  $\text{Cu}_2\text{CdGeS}_4$ , and 10% excess Cd and Sn for  $\text{Cu}_2\text{CdSnS}_4$ . The mixtures were heated under vacuum for 12 h at 923, 923 and 823 K for  $\text{Ag}_2\text{CdGeS}_4$ ,  $\text{Cu}_2\text{CdGeS}_4$  and  $\text{Cu}_2\text{CdSnS}_4$ , respectively.

### Characterization of photocatalysts

X-ray diffraction (XRD; Rigaku; MiniFlex600) with  $\text{Cu K}\alpha$  radiation was used to identify the crystal structures of the obtained samples. Diffuse reflectance spectra were measured by using a UV-vis-NIR spectrometer (JASCO; UbeatV-570) with an integrating sphere and were converted to absorbance by the Kubelka-Munk method. Scanning electron microscopy (SEM; JEOL; JSM-6700F) was used to observe the morphologies of the particles. Photoelectron yield spectroscopy (PYS; Bunkoukeiki; BIP-KV100) was conducted under vacuum to determine the ionization potential of the samples.

### Density functional theory calculations

Density functional theory (DFT) calculations were carried out using the CASTEP code.<sup>74</sup> ICSD #152753, #26150 and #619773 were employed for  $\text{Ag}_2\text{CdGeS}_4$ ,  $\text{Cu}_2\text{CdGeS}_4$  and  $\text{Cu}_2\text{CdSnS}_4$ , respectively. In geometric optimization, the Vanderbilt-type ultrasoft pseudopotentials,<sup>75</sup> the generalized gradient approximation (GGA)<sup>76</sup> and the Perdew-Burke-Ernzerhof (PBE)<sup>77</sup> as exchange-correlation functional were used under periodic boundary conditions. 600 eV of cutoff energy and a  $k$ -point mesh with a typical spacing of  $0.07\text{ \AA}^{-1}$  given by the Monkhorst-Pack method<sup>78</sup> were used. The limited-memory Broyden-Fletcher-Goldfarb-Shanno (LBFGS) algorithm<sup>79</sup> was employed for geometric optimization of the supercells. Details of the conditions of the convergence criteria are summarized in the SI (Table S1). The Heyd-Scuseria-Ernzerhof (HSE03)<sup>80</sup> hybrid functional was used to analyze the density of states and the band structures of the optimized crystal structures. The valence electronic configurations for Cu, Ag, Cd, Ge, Sn and S were  $3d^{10}4s^1$ ,  $4d^{10}5s^1$ ,  $4d^{10}5s^2$ ,  $4s^24p^2$ ,  $5s^25p^2$  and  $3s^23p^4$ , respectively. The number of electrons in the primitive unit cell were 156 and 124 for  $[\text{Ag}_2\text{CdGeS}_4]$  and  $[\text{Cu}_2\text{CdMS}_4$  ( $\text{M} = \text{Ge}$  and  $\text{Sn}$ )], respectively.

### Photocatalytic reactions

Photocatalytic  $\text{H}_2$  evolution was carried out using a top-irradiation cell with a Pyrex window in a gas-closed circulation system. The sample was dispersed in an aqueous solution (150 mL) of  $0.1\text{ mol L}^{-1}$   $\text{Na}_2\text{S}$  ( $\text{Na}_2\text{S}\cdot 9\text{H}_2\text{O}$ ; Kanto Chemical, 98%) and  $0.5\text{ mol L}^{-1}$   $\text{K}_2\text{SO}_3$  (Kanto Chemical; 95%) as sacrificial reagents. The pH of the aqueous solution containing  $\text{S}^{2-}$  and  $\text{SO}_3^{2-}$  ions was 13. A Ru cocatalyst as an  $\text{H}_2$ -evolving site<sup>36</sup> was loaded on the prepared sulfide photocatalysts by *in situ* photodeposition in an aqueous solution of  $\text{RuCl}_3\cdot n\text{H}_2\text{O}$  (Tanaka Kikinzoku; 39% as Ru in  $\text{RuCl}_3\cdot n\text{H}_2\text{O}$ ) as a source of a cocatalyst. A 300 W Xe-arc lamp (PerkinElmer; Cermax PE300BF) was used as a light source. The wavelength of light irradiation was controlled by using a cut-off filter (HOYA; L42,  $\lambda > 420\text{ nm}$ ). The amount of evolved  $\text{H}_2$  was quantified using an online gas chromatograph (Shimadzu; GC-8A, MS-5A column, TCD, Ar carrier).

Apparent quantum yields (AQY) were measured using a 300 W Xe-arc lamp (PerkinElmer; Cermax PE300BF) and a 100 W Xe-arc lamp (Asahi Spectra; LAX 102) with band pass filters (Asahi Spectra). The photon flux of monochromatic light was measured using a silicon diode head (OPHIR; PD300-UV head) with a NOVA display. AQY was calculated by the following eqn (1).

$$[\text{AQY \%}] = 100 \times [\text{the number of reacted electrons}]/[\text{the number of incident photons}] = 100 \times [\text{the number of evolved H}_2 \text{ molecules} \times 2]/[\text{the number of incident photons}] \quad (1)$$

## Results and discussion

### Machine-learning-based prediction of metal sulfide photocatalyst candidates for sacrificial $\text{H}_2$ evolution under visible light irradiation

A flowchart for screening of metal sulfide photocatalysts for sacrificial  $\text{H}_2$  evolution under visible light irradiation ( $\lambda > 420\text{ nm}$ ) by machine learning is shown in Fig. 1. First, the prediction model of activities for  $\text{H}_2$  evolution was constructed by machine learning on the basis of our original in-house dataset, as shown in Fig. 1(1). Fig. 2 shows a plot of the predicted *versus* experimental activities, which was used to evaluate the constructed machine-learning model using double cross-validation. The coefficient of determination ( $R^2$ ) was more than 0.5, indicating that the model was constructed with acceptable accuracy for the initial (first/rough) materials screening, as shown in Fig. 1(1)–(3). The acceptable accuracy described here means that the constructed machine-learning model is suitable for understanding the trend of activities for  $\text{H}_2$  evolution of metal sulfide photocatalysts, which leads to a subsequent (second/refined) screening based on chemical insights, as shown in Fig. 1(4). Next, we selected candidate materials for screening from the ICSD of metal sulfide compounds based on their similarity in the feature space to our in-house dataset of metal sulfide photocatalysts, as shown in Fig. 1(2). Fig. 3 shows the material space of metal sulfides in the ICSD and our in-house original dataset as red and blue dots, respectively. Then, we selected 765 metal sulfide compounds, located within the blue square in Fig. 3, as candidate materials for screening. This region was selected because it included many in-house experimental data that were used as training data, given that it was difficult to predict the activities of materials outside the range of the training data. Subsequently, the activities of the candidate sulfides for sacrificial  $\text{H}_2$  evolution were predicted by using the constructed machine-learning model, as shown in Fig. 1(3) and 2. The selected metal sulfide candidate materials with their predicted activities are shown in Fig. 4. The 200 material sulfide candidates with their predicted activities were obtained, as shown in the ‘list\_of\_candidates’ csv file (SI). Thus, the metal sulfide photocatalyst candidates were identified in the first stage of screening by MI. As shown in Fig. 1(4), we selected three metal sulfides,  $\text{Ag}_2\text{CdGeS}_4$  and  $\text{Cu}_2\text{CdMS}_4$  ( $\text{M} = \text{Ge}$  and  $\text{Sn}$ ), for the second stage of screening based on empirical insights, given that a number of metal sulfides containing Cu(i) and/or Ag(i)



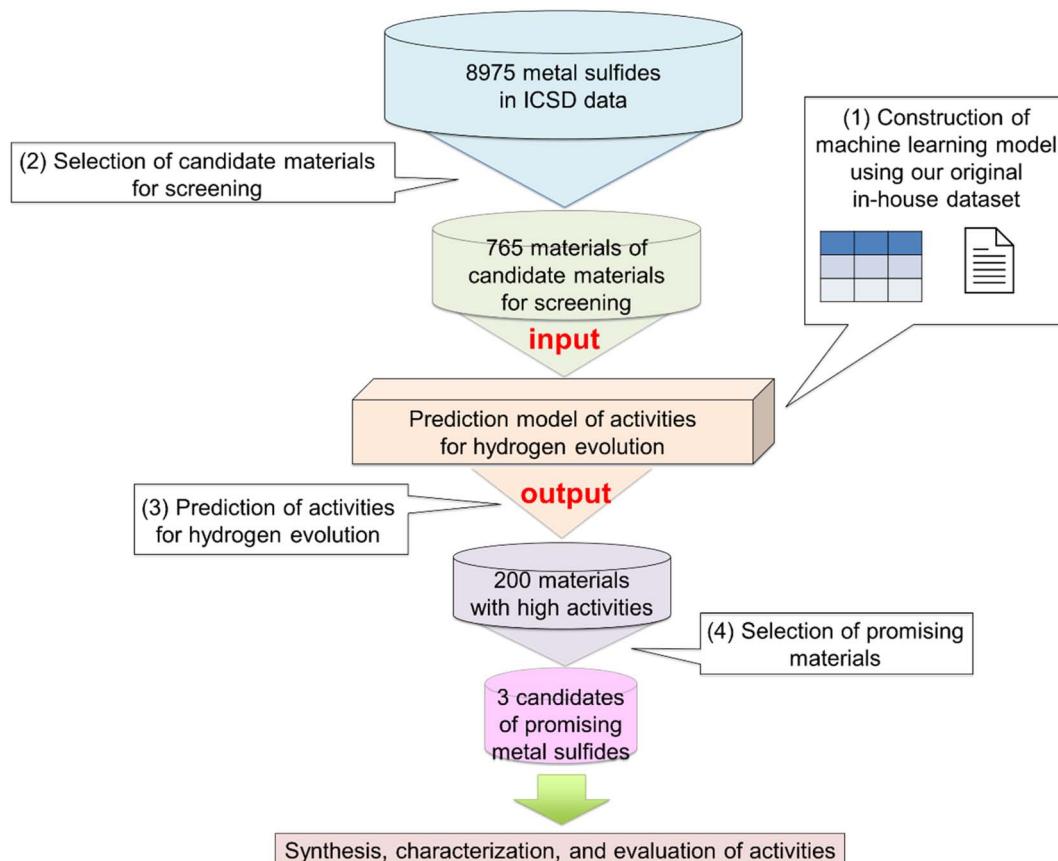


Fig. 1 Flowchart of exploring metal sulfides for  $\text{H}_2$  evolution by machine-learning.

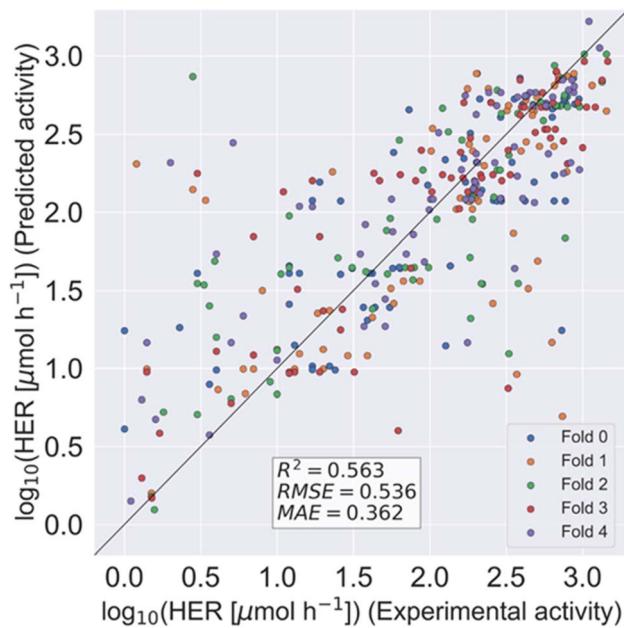


Fig. 2 Comparison between predicted activities obtained by the machine-learning model and experimental activities for sacrificial  $\text{H}_2$  evolution under visible light irradiation ( $\lambda > 420 \text{ nm}$ ) on the basis of our original experimental dataset. In the 5-fold double cross-validation, the validation results from fold 0 to fold 4 are shown as blue, orange, green, red and purple circles, respectively.

ions and corner-shared  $\text{MS}_4$  tetrahedra have been reported as promising visible-light-responsive photocatalysts for sacrificial  $\text{H}_2$  evolution.<sup>36,39,41</sup>

#### Preparation and characterization of $\text{Ag}_2\text{CdGeS}_4$ and $\text{Cu}_2\text{CdMS}_4$ ( $\text{M} = \text{Ge and Sn}$ ) photocatalysts

$\text{Ag}_2\text{CdGeS}_4$  and  $\text{Cu}_2\text{CdMS}_4$  ( $\text{M} = \text{Ge and Sn}$ ) were synthesized by a conventional solid-state reaction. XRD patterns revealed that orthorhombic  $\text{Ag}_2\text{CdGeS}_4$ , with the enargite structure, and tetragonal  $\text{Cu}_2\text{CdSnS}_4$ , with the stannite structure, were obtained in a single phase (Fig. S1). Orthorhombic  $\text{Cu}_2\text{CdGeS}_4$ , with the enargite structure in an almost single phase, was also obtained with a negligible amount of  $\text{Cd}_4\text{GeS}_6$ . We optimized the excess amount of  $\text{GeS}_2$  (0–50 mol% ex.) with the aim of obtaining a single phase of  $\text{Cu}_2\text{CdGeS}_4$ . It was revealed that the lowest amount of  $\text{Gd}_4\text{GeS}_6$  in the sample was achieved when a 40 mol% excess amount of  $\text{GeS}_2$  was used, although the single phase of  $\text{Cu}_2\text{CdGeS}_4$  was not obtained. Particulate morphologies were observed in the SEM images (Fig. S2). Sintered large particles with a size of several tens of micrometers were observed on  $\text{Ag}_2\text{CdGeS}_4$ , and aggregations of primary particles with a size of several micrometers were observed on  $\text{Cu}_2\text{CdMS}_4$  ( $\text{M} = \text{Ge and Sn}$ ). Diffuse reflectance spectra of the obtained samples are shown in Fig. 5(a). The band gaps of  $\text{Ag}_2\text{CdGeS}_4$ ,  $\text{Cu}_2\text{CdGeS}_4$  and  $\text{Cu}_2\text{CdSnS}_4$  were estimated to be 2.21, 1.86 and



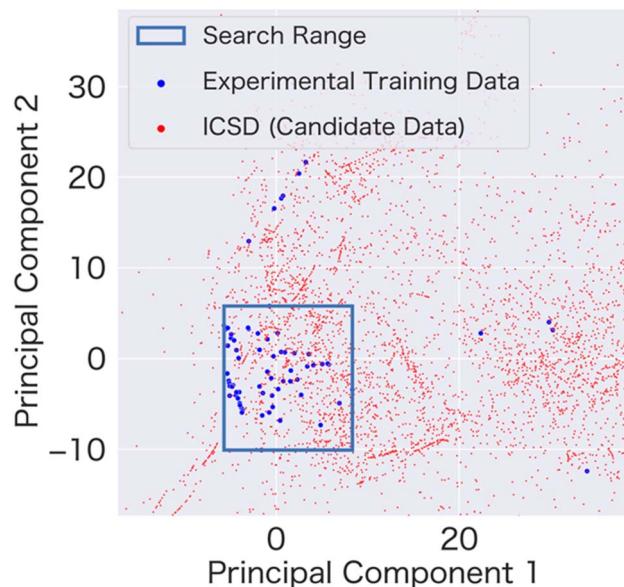


Fig. 3 Material space of metal sulfides in the ICSD and our original dataset by PCA. Principal components 1 and 2 (with no units), which form the axes, are new coordinate axes constructed by performing linear combinations of the original variables.

1.28 eV, respectively, from the absorption edges. It is notable that  $\text{Cu}_2\text{CdSnS}_4$  absorbs over the whole range of visible light. PYS spectra were measured under vacuum to determine the ionization potentials, which can generally be assigned to the top of the valence band level of the samples. As shown in Fig. 5(b), the potentials were estimated to be  $-5.79$  eV (vs. vacuum level) for  $\text{Ag}_2\text{CdGeS}_4$  and  $-5.18$  eV (vs. vacuum level) for  $\text{Cu}_2\text{CdMS}_4$  ( $\text{M} = \text{Ge}$  and  $\text{Sn}$ ), indicating that the valence band of  $\text{Ag}_2\text{CdGeS}_4$  formed at a more positive potential than those of  $\text{Cu}_2\text{CdMS}_4$  ( $\text{M} = \text{Ge}$  and  $\text{Sn}$ ). This result is reasonable because the Ag 4d orbitals generally form the valence band at a more positive level than Cu 3d orbitals, as observed for other metal sulfide photocatalysts containing Cu(i) and Ag(i) ions.<sup>41</sup> DFT calculations were also performed to investigate the band structures of  $\text{Ag}_2\text{CdGeS}_4$  and  $\text{Cu}_2\text{CdMS}_4$  ( $\text{M} = \text{Ge}$  and  $\text{Sn}$ ), as shown in Fig. 6 and 7. All samples showed the direct transition property, and the calculated band gaps for  $\text{Ag}_2\text{CdGeS}_4$ ,  $\text{Cu}_2\text{CdGeS}_4$  and  $\text{Cu}_2\text{CdSnS}_4$  were  $1.89$ ,  $1.65$  and  $0.95$  eV, respectively. The order of the band gaps agreed well with the experimental data estimated from absorption edges of diffuse reflectance spectra, as shown in Fig. 5(a). The partial density of states (PDOS) of  $\text{Ag}_2\text{CdGeS}_4$  and  $\text{Cu}_2\text{CdMS}_4$  ( $\text{M} = \text{Ge}$  and  $\text{Sn}$ ) are shown in Fig. 7. The valence band maxima mainly consisted of Ag 4d + S 3p hybrid orbitals for  $\text{Ag}_2\text{CdGeS}_4$  and Cu 3d + S 3p hybrid orbitals for  $\text{Cu}_2\text{CdMS}_4$  ( $\text{M} = \text{Ge}$  and  $\text{Sn}$ ), while the conduction band minima mainly consisted of Cd 5s5p + Ge 4s4p hybrid orbitals for  $\text{Ag}_2\text{CdGeS}_4$  and  $\text{Cu}_2\text{CdGeS}_4$ . We previously reported DFT calculations for a  $\text{Cu}_2\text{ZnGeS}_4$  photocatalyst with the stannite structure that was active for sacrificial  $\text{H}_2$  evolution under visible light irradiation.<sup>36</sup> The results showed that Zn 4s4p orbitals were located at a higher energy than Ge 4s4p orbitals, indicating that the contribution of Zn 4s4p to the conduction band of  $\text{Cu}_2\text{ZnGeS}_4$

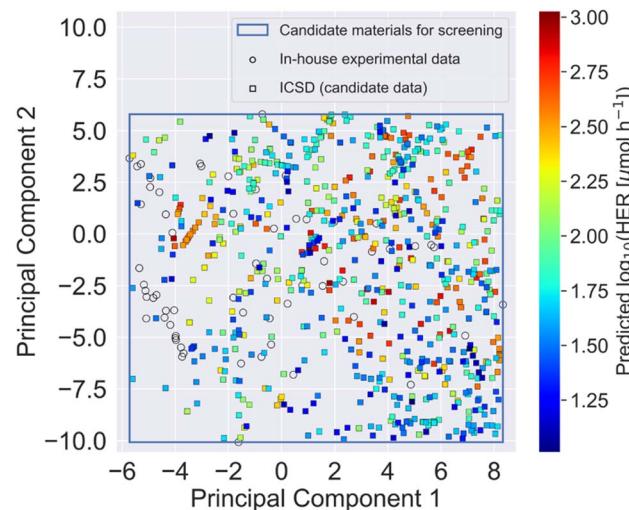


Fig. 4 Material space of metal sulfides in the ICSD and our original dataset with predicted activities for sacrificial  $\text{H}_2$  evolution under visible light irradiation ( $\lambda > 420$  nm) by PCA. Principal components 1 and 2 (with no units), which form the axes, are new coordinate axes constructed by performing linear combinations of original variables. Open circles are in-house experimental data. Squares are the data from the ICSD, and the color indicates a predicted activity corresponding to the right vertical axis.

was small. In contrast, the contribution of Cd 5s5p to the conduction band was relatively large for  $\text{Ag}_2\text{CdGeS}_4$  and  $\text{Cu}_2\text{CdGeS}_4$ . The conduction band minima mainly consisted of Cd 5s5p + Sn 5s5p hybrid orbitals for  $\text{Cu}_2\text{CdSnS}_4$ , which were located at a lower energy than the Cd 5s5p + Ge 4s4p hybrid orbitals, leading to the narrow band gap of  $\text{Cu}_2\text{CdSnS}_4$ . Fig. 8 shows the band structures determined by diffuse reflectance spectra, the ionization potentials by PYS measurements, and the DFT calculations. The order of driving forces for the reduction of water was  $\text{Cu}_2\text{CdGeS}_4 > \text{Ag}_2\text{CdGeS}_4 \gg \text{Cu}_2\text{CdSnS}_4$ . The DRS, PYS and PDOS results suggest that Sn 5s5p orbitals contribute to the formation of the conduction band of  $\text{Cu}_2\text{CdSnS}_4$  at a more positive level than for  $\text{Ag}_2\text{CdGeS}_4$  and  $\text{Cu}_2\text{CdGeS}_4$ , leading to the decreased driving force for water reduction.

#### Photocatalytic $\text{H}_2$ evolution over $\text{Ag}_2\text{CdGeS}_4$ and $\text{Cu}_2\text{CdMS}_4$ ( $\text{M} = \text{Ge}$ and $\text{Sn}$ ) photocatalysts in the presence of sacrificial reagents under visible light irradiation

Photocatalytic  $\text{H}_2$  evolution over  $\text{Ag}_2\text{CdGeS}_4$  and  $\text{Cu}_2\text{CdMS}_4$  ( $\text{M} = \text{Ge}$  and  $\text{Sn}$ ) photocatalysts from an aqueous solution containing  $\text{S}^{2-}$  and  $\text{SO}_3^{2-}$  ions as sacrificial reagents, was investigated under visible light irradiation.  $\text{H}_2$  continuously evolved for all samples for 3 h, without a noticeable deactivation, as shown in Fig. 9. As mentioned in the previous section,  $\text{Cu}_2\text{CdGeS}_4$  contained a small amount of  $\text{Cd}_4\text{GeS}_6$  as an impurity. However, the single  $\text{Cd}_4\text{GeS}_6$  showed very low activity ( $16 \mu\text{mol h}^{-1}$ ) compared to  $\text{Cu}_2\text{CdGeS}_4$  ( $369 \mu\text{mol h}^{-1}$ ). Therefore, the obtained  $\text{Ag}_2\text{CdGeS}_4$  and  $\text{Cu}_2\text{CdMS}_4$  ( $\text{M} = \text{Ge}$  and  $\text{Sn}$ ) represent new visible-light-responsive metal sulfide photocatalysts for  $\text{H}_2$  evolution. The  $\text{Cu}_2\text{CdSnS}_4$  photocatalyst continuously evolved



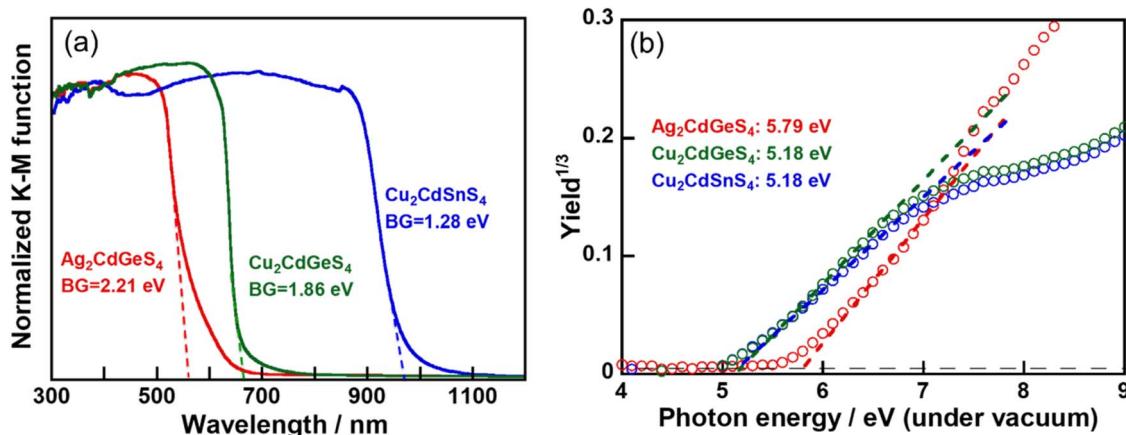


Fig. 5 (a) Diffuse reflectance spectra and (b) PYS spectra of  $\text{Ag}_2\text{CdGeS}_4$  and  $\text{Cu}_2\text{CdMS}_4$  ( $\text{M} = \text{Ge}$  and  $\text{Sn}$ ) prepared by a solid-state reaction.

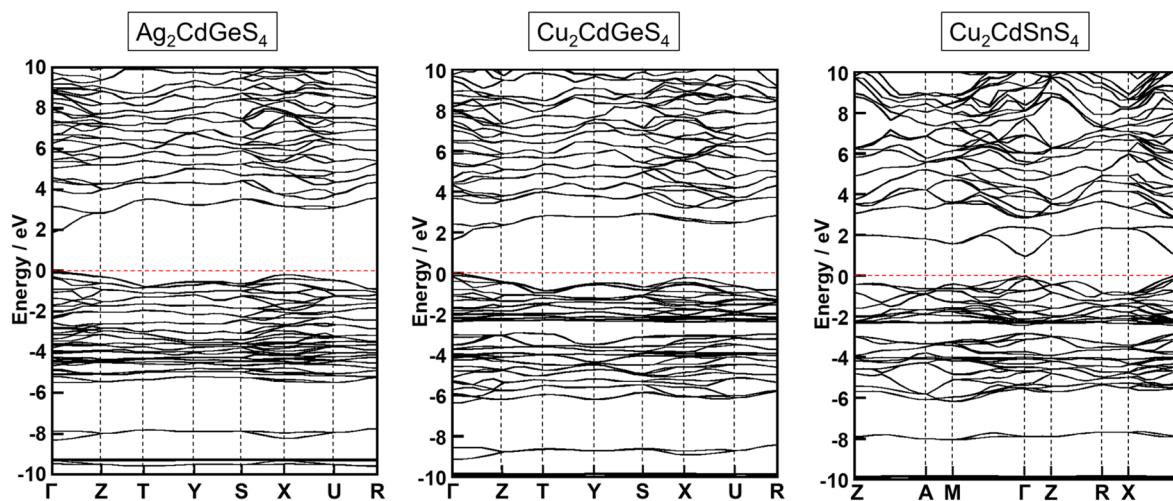


Fig. 6 Band structures of  $\text{Ag}_2\text{CdGeS}_4$  and  $\text{Cu}_2\text{CdMS}_4$  ( $\text{M} = \text{Ge}$  and  $\text{Sn}$ ).

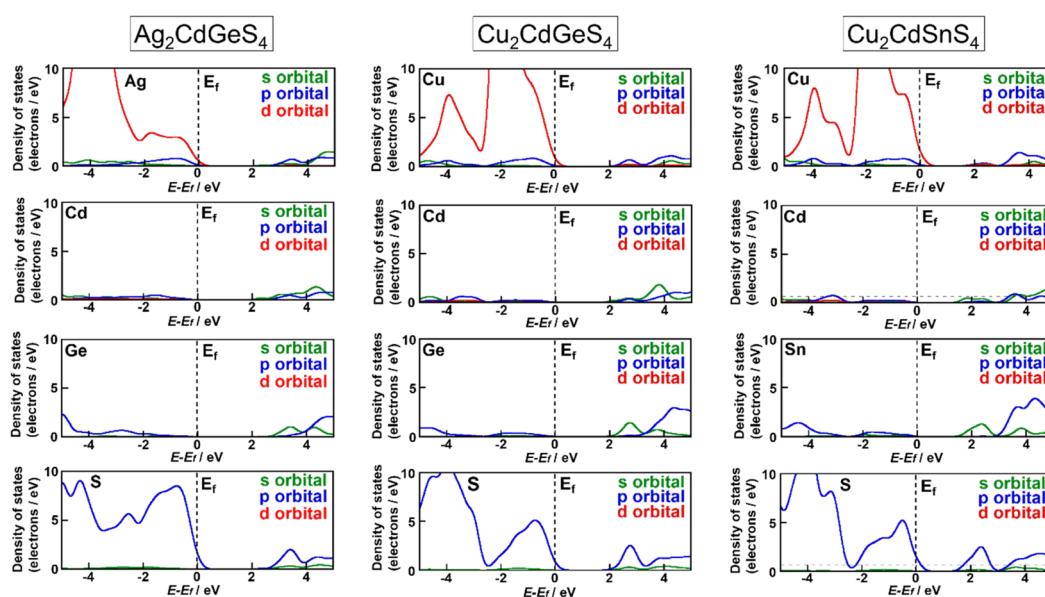


Fig. 7 Density of states of  $\text{Ag}_2\text{CdGeS}_4$  and  $\text{Cu}_2\text{CdMS}_4$  ( $\text{M} = \text{Ge}$  and  $\text{Sn}$ ).



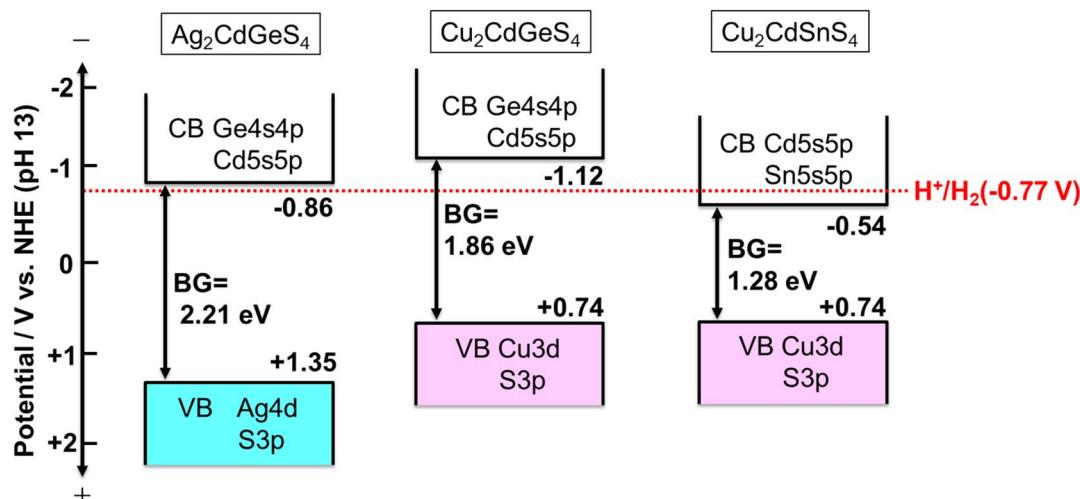


Fig. 8 Band structures of  $\text{Ag}_2\text{CdGeS}_4$  and  $\text{Cu}_2\text{CdMS}_4$  ( $\text{M} = \text{Ge}$  and  $\text{Sn}$ ).

$\text{H}_2$  for 22 h (Fig. S3). The turnover numbers of the molar quantity of reacted electrons for  $\text{H}_2$  evolution to that of the photocatalyst host were 1.8 at 3 h, 3.1 at 3 h and 1.2 at 22 h for  $\text{Ag}_2\text{CdGeS}_4$ ,  $\text{Cu}_2\text{CdGeS}_4$  and  $\text{Cu}_2\text{CdSnS}_4$ , respectively. The turnover numbers were larger than unity, indicating that  $\text{H}_2$  evolution proceeded photocatalytically.  $\text{Cu}_2\text{CdGeS}_4$  showed the highest activity among the samples. Fig. 10 shows action spectra of sacrificial  $\text{H}_2$  evolution over the Ru (0.5 wt%)-loaded  $\text{Ag}_2\text{CdGeS}_4$ ,  $\text{Cu}_2\text{CdGeS}_4$  and  $\text{Cu}_2\text{CdSnS}_4$  photocatalysts.  $\text{Ag}_2\text{CdGeS}_4$  and  $\text{Cu}_2\text{CdGeS}_4$  responded to 570 and 780 nm, respectively. The onsets of the action spectra of  $\text{Ag}_2\text{CdGeS}_4$  and  $\text{Cu}_2\text{CdGeS}_4$  agreed well with those of the diffuse reflectance spectra, indicating that  $\text{H}_2$  evolution proceeded by band gap excitation. Notably,  $\text{Cu}_2\text{CdSnS}_4$  responded to near-infrared light at 900 nm. AQYs were 2.6% at 470 nm for  $\text{Ag}_2\text{CdGeS}_4$ , 3.4% at

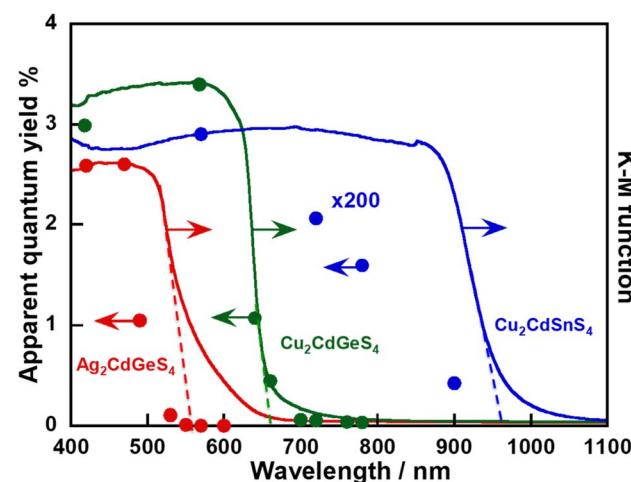


Fig. 10 Action spectra of sacrificial  $\text{H}_2$  evolution over the Ru (0.5 wt%)-loaded  $\text{Ag}_2\text{CdGeS}_4$ ,  $\text{Cu}_2\text{CdMS}_4$  ( $\text{M} = \text{Ge}$  and  $\text{Sn}$ ) photocatalysts. Photocatalyst: 0.3 g, cocatalyst: PD *in situ*, reactant solution: 0.5 mol per L  $\text{K}_2\text{SO}_3$  and 0.1 mol per L  $\text{Na}_2\text{S}$  aqueous solution (120 mL), cell: top-irradiation cell with a Pyrex window, light source: 300 W Xe lamp with band-pass filters.

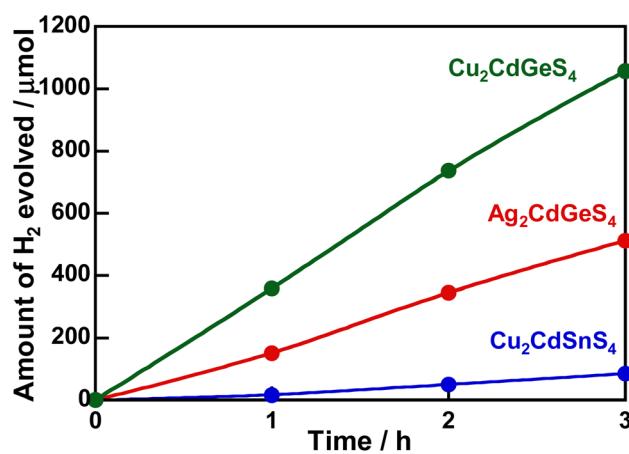


Fig. 9  $\text{H}_2$  evolution over Ru-loaded  $\text{Ag}_2\text{CdGeS}_4$  and  $\text{Cu}_2\text{CdMS}_4$  ( $\text{M} = \text{Ge}$  and  $\text{Sn}$ ) photocatalysts prepared by a solid-state reaction from an aqueous solution containing sacrificial reagents under visible light irradiation. Photocatalyst: 0.3 g, cocatalyst: photodeposition *in situ*, reactant solution: 0.5 mol per L  $\text{K}_2\text{SO}_3$  and 0.1 mol per L  $\text{Na}_2\text{S}$  aqueous solution (120 mL), cell: top-irradiation cell with a Pyrex window, light source: 300 W Xe lamp with a cut-off filter (HOYA: L42).

570 nm for  $\text{Cu}_2\text{CdGeS}_4$  and 0.015% at 570 nm for  $\text{Cu}_2\text{CdSnS}_4$ . The order of AQYs was  $\text{Cu}_2\text{CdGeS}_4 > \text{Ag}_2\text{CdGeS}_4 \gg \text{Cu}_2\text{CdSnS}_4$ . Here, the order of the driving force of reduction of water was  $\text{Cu}_2\text{CdGeS}_4 > \text{Ag}_2\text{CdGeS}_4 \gg \text{Cu}_2\text{CdSnS}_4$ , judging from the position of the conduction band minima, as shown in Fig. 8. Therefore,  $\text{Cu}_2\text{CdGeS}_4$ , with the largest driving force for reduction of water, showed the highest activity among the samples.

## Conclusions

We have successfully developed  $\text{Ag}_2\text{CdGeS}_4$  and  $\text{Cu}_2\text{CdMS}_4$  ( $\text{M} = \text{Ge}$  and  $\text{Sn}$ ) as new visible-light-responsive metal sulfide photocatalysts for sacrificial  $\text{H}_2$  evolution by utilizing machine



learning. The machine-learning model with acceptable accuracy was constructed by utilizing our original dataset of metal sulfide photocatalysts developed by our group. The features of material sulfides in the ICSD and our original dataset were plotted in a material space with two dimensions by using XenonPy and principal component analysis. We predicted the activities of 765 metal sulfides in the ICSD inside the material space (where many experimental data used as the training data existed) using the constructed machine-learning model, resulting in the identification of metal sulfide candidates for H<sub>2</sub> evolution. We experimentally synthesized Ag<sub>2</sub>CdGeS<sub>4</sub> and Cu<sub>2</sub>CdMS<sub>4</sub> (M = Ge and Sn) from the candidates because metal sulfides containing Cu(i) and/or Ag(i) ions and corner-shared MS<sub>4</sub> tetrahedra have been reported as promising photocatalysts for sacrificial H<sub>2</sub> evolution under visible light irradiation. The band gaps of Ag<sub>2</sub>CdGeS<sub>4</sub>, Cu<sub>2</sub>CdGeS<sub>4</sub> and Cu<sub>2</sub>CdSnS<sub>4</sub> were estimated to be 2.21, 1.86 and 1.28 eV, respectively, from the diffuse reflectance spectra. DFT calculations indicated that the conduction band minima of Ag<sub>2</sub>CdGeS<sub>4</sub> and Cu<sub>2</sub>CdGeS<sub>4</sub> mainly consisted of Cd 5s5p + Ge 4s4p hybrid orbitals, and Cu<sub>2</sub>CdSnS<sub>4</sub> were mainly composed of Cd 5s5p + Sn 5s5p hybrid orbitals. Ag<sub>2</sub>CdGeS<sub>4</sub>, Cu<sub>2</sub>CdGeS<sub>4</sub> and Cu<sub>2</sub>CdSnS<sub>4</sub>, prepared by a solid-state reaction, showed activities for sacrificial H<sub>2</sub> evolution under visible light irradiation up to 570, 780 and 900 nm, respectively. Among the prepared photocatalysts, Cu<sub>2</sub>CdGeS<sub>4</sub> gave the highest AQY, possibly because it possessed a larger driving force for the reduction of water compared to Ag<sub>2</sub>CdGeS<sub>4</sub> and Cu<sub>2</sub>CdSnS<sub>4</sub>. In this study, exploration of novel visible-light-responsive metal sulfides for sacrificial H<sub>2</sub> evolution by machine learning has been achieved. It is expected that this study will contribute to the accelerated exploration of novel metal semiconductor photocatalysts not only in the metal sulfide group but also in other material groups, such as metal oxides.

## Author contributions

A. K. and M. F. designed and supervised the research. F. K. carried out the preparation, characterization and evaluation of the H<sub>2</sub>-evolving activity of metal sulfide photocatalysts. R. B. and W. T. provided the candidates of metal sulfide photocatalysts for H<sub>2</sub> evolution by machine learning. Y. Y., F. K. and T. T. performed the DFT calculation. Y. Y. wrote the manuscript. Y. Y., F. K., R. B., W. T., Y. H., T. T., M. F. and A. K. discussed and reviewed the content of the research.

## Conflicts of interest

There are no conflicts to declare.

## Data availability

The data supporting this article have been included as part of the supplementary information (SI). Supplementary information is available. See DOI: <https://doi.org/10.1039/d5ta06041a>.

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