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# Strain engineering of optoelectronic and ferroelectric properties in *R3*-phase $\text{Zn}_3\text{TeO}_6$ : a first-principles study

 Xing-Yuan Chen,<sup>1</sup> Guo-Wei Lai,<sup>1</sup> Tu-Rong Ning,<sup>1</sup> Yan-Li Hu,<sup>1</sup> Xiao-Dong Yang,<sup>1</sup> Shuang-Rui Chen,<sup>2</sup> Yin Liu<sup>1</sup> and Hua-Kai Xu<sup>1\*</sup>

A systematic evaluation of the optoelectronic properties of ferroelectric ternary oxides under strain is essential for their integration into functional devices. In this study, the *R3*-phase ternary oxide  $\text{Zn}_3\text{TeO}_6$  was investigated using density functional theory to examine its stability, electronic structure, optical properties, ferroelectric behavior, and carrier mobility under both compressive and tensile strain. Calculations of elastic constants, molecular dynamics simulations, and phonon spectra confirm the stability of  $\text{Zn}_3\text{TeO}_6$  within a modest strain range. Compressive strain increases phonon frequencies, elastic constants, and bandgap, while enhancing ferroelectric polarization. In contrast, tensile strain decreases the bandgap and promotes visible-light absorption. Carrier transport analysis reveals pronounced n-type conduction, with electron mobility reaching  $\sim 150 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$ , further enhanced under compressive strain due to the suppression of polar optical phonon and piezoelectric scattering. These findings demonstrate that strain engineering offers an effective approach to tuning the multifunctional properties of *R3*- $\text{Zn}_3\text{TeO}_6$ , highlighting its potential for ferroelectric and photovoltaic applications.

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## 1. Introduction

$\text{X}_3\text{TeO}_6$  compounds (where X is a 3d transition metal) have attracted considerable attention due to their unique magnetic, electric, and dielectric properties.<sup>1–5</sup> Their complex magnetic behaviors and field-induced polarization effects, particularly the antiferromagnetic transitions and colossal magnetoelectric coupling observed in several members, highlight their great potential for multifunctional device applications.<sup>1,3,5</sup>  $\text{Zn}_3\text{TeO}_6$  crystallizes in an isostructural  $\beta\text{-Li}_3\text{VF}_6$ -type structure, similar to  $\text{X}_3\text{TeO}_6$ , and contains five distinct  $\text{Zn}^{2+}$  coordination environments, including distorted octahedral, tetrahedral, and square-pyramidal sites.<sup>6–8</sup> While the *C2/c* phases of  $\text{Co}_3\text{TeO}_6$  and  $\text{Zn}_3\text{TeO}_6$  are enthalpically favored below 10 GPa, the *R3* phase becomes energetically more stable above this pressure, resulting in a *C2/c*  $\rightarrow$  *R3* structural transition.<sup>9</sup> While the *R3* phase is a high-pressure phase in bulk materials, substrate-induced strain in epitaxial thin films can plausibly stabilize its polar structure as the energetic ground state, similar to the stabilization of polar *R3c*  $\text{MgSnO}_3$  films grown epitaxially or by pulsed laser deposition.<sup>10,11</sup> Fernández-Catalá *et al.* successfully

synthesized nanoscale  $\text{Ni}_3\text{TeO}_6$  (*R3*) and  $\text{Cu}_3\text{TeO}_6$  (*Ia3*) via an NaOH-assisted hydrothermal method, finding both materials exhibit semiconducting behavior (with respective band gaps of 2.44 eV and 2.56 eV) and pronounced photoconductivity.<sup>12</sup> A high-pressure phase,  $\text{Mg}_3\text{TeO}_6$  (space group *R3*), was obtained under 12.5 GPa and 1570 K, with an experimental band gap of 3.5 eV, confirming its wide-bandgap semiconducting nature.<sup>13</sup> Furthermore, crystallographic and optical investigations of  $\text{Co}_{3-x}\text{Zn}_x\text{TeO}_6$  revealed that Zn dopants preferentially occupy tetrahedral sites, enhancing local distortion, while the strong covalent character of Co–O bonds significantly affect the optical response.<sup>14</sup> Magnetic studies by Sarkar *et al.* demonstrated that Zn substitution shortens the  $\text{Co}^{2+}$ –O bond length and markedly suppresses the magnetic interactions in  $\text{Co}_3\text{TeO}_6$ .<sup>15</sup>  $\text{X}_3\text{TeO}_6$  compounds with the *R3* structure not only have potential applications in magnetism, photoconductivity, and as semiconductors, but this polar *R3* structure also suggests potential ferroelectric behavior, implying potential ferroelectric photovoltaic properties.<sup>16–18</sup>

By applying tensile strain, the structural stability, bandgap characteristics, and optical responses of various emerging two-dimensional materials (such as  $\text{Si}_2\text{C}$ ,  $\text{C}_3\text{B}$ , and  $\text{h-BC}_2\text{N}$ ) can be effectively tuned, enabling bandgap modulation and enhanced optical absorption, which highlights the crucial role of strain engineering in optimizing their optoelectronic performance.<sup>19–21</sup> Likewise, for three-dimensional ferroelectric materials, strain engineering has also become an indispensable

<sup>1</sup>Department of Physics, School of Science, Guangdong University of Petrochemical Technology, Maoming 525000, Guangdong, PR China. E-mail: chenxingyuan@gdpuet.edu.cn; xuhuakai@gdpuet.edu.cn; Fax: +86-668-2923567; Tel: +86-668-2923838

<sup>2</sup>Department of Architectural Engineering, Guangdong University of Petrochemical Technology, PR China



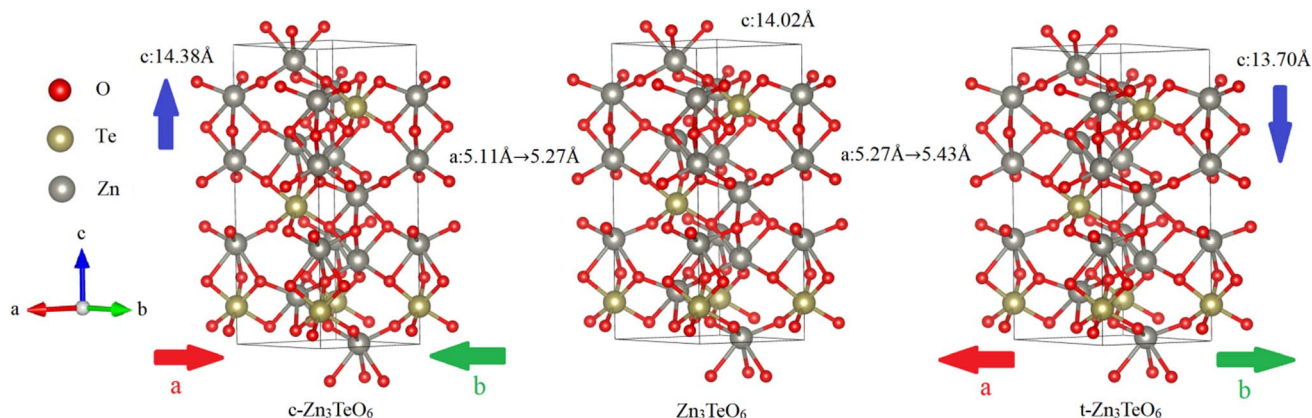


Fig. 1 The structure of  $R3\text{-Zn}_3\text{TeO}_6$ .

strategy for tailoring their intrinsic properties. Compared with chemical doping or external fields, strain offers advantages such as reversibility, continuity, and high precision, enabling the modulation of structural stability as well as electronic, magnetic, and optical properties without introducing chemical complexity.<sup>22–24</sup> Epitaxial strain, for instance, can reconstruct band structures, leading to bandgap enlargement and corresponding modifications of the optical response in materials such as  $R3c\text{-BiFeO}_3$ .<sup>25</sup> Strain effects during synthesis are also critically important, as research has shown that the lattice strain introduced by reducing the heating rate during calcination can enhance the oxygen evolution reaction (OER) activity and stability of  $\text{Ni}_3\text{TeO}_6$  electrocatalysts.<sup>26</sup> It is reported in the literature that epitaxial strain can enhance ferroelectric properties while also favorably modifying the optical response of thin films, supporting their viability for optoelectronic device applications.<sup>27</sup>

Despite substantial advances in elucidating the magnetic properties of the  $\text{X}_3\text{TeO}_6$  system, its optoelectronic behavior—particularly the evolution of electronic structure and carrier dynamics of  $\text{Zn}_3\text{TeO}_6$  under different strain conditions—remains insufficiently explored. In this work, first-principles calculations combined with strain engineering are employed to investigate the structural stability, band modulation, carrier transport, and polarization response of  $R3\text{-Zn}_3\text{TeO}_6$  under both compressive and tensile strains. The aim is to uncover the mechanisms by which strain regulates its thermodynamic and mechanical stability as well as its coupled optoelectronic-ferroelectric properties, thereby providing theoretical guidance for the design and device integration of multifunctional tellurates.

## 2. Calculation model and method

All calculations in this work are mainly completed by the Vienna *Ab initio* Simulation Package (VASP) software package for first-principles calculations.<sup>28,29</sup> The interaction between electrons and atomic nuclei in the computational system is described using the projection additive wave (PAW) pseudo potential,<sup>30</sup> and the exchange correlation functional between electrons is processed using the generalized gradient approximation (GGA)

of Perdew–Burke–Ernzerhof (PBE).<sup>31</sup> The Heyd–Scuseria–Ernzerhof (HSE06) hybrid functional is used to calculate the bandgap values and optical properties, as it is usually closer to the experimental values.<sup>32,33</sup> A plane-wave cutoff energy of 520 eV was employed, and the Brillouin zone was sampled using a  $7 \times 7 \times 3$  gamma-centered  $k$ -point mesh. The electronic configurations of pseudo potential for Zn, Te, and O atoms are chosen as  $d^{10}p^2$ ,  $s^2p^4$ , and  $s^2p^4$ , respectively. The iterative convergence accuracy of the energy is set to  $10^{-6}$  eV, and the Hellman–Feynman forces are less than  $0.01 \text{ eV } \text{Å}^{-1}$ . The structural model of  $R3\text{-Zn}_3\text{TeO}_6$  is shown in Fig. 1, which contains 30 atoms.

The calculated lattice parameters are shown in Table 1. The calculated lattice parameters  $a$  and  $c$  of  $R3\text{-Zn}_3\text{TeO}_6$  by PBE method are 5.27 Å and 14.02 Å. As shown in Fig. 1, introducing a 3% compressive strain in the  $ab$  plane of  $R3\text{-Zn}_3\text{TeO}_6$  reduces the lattice parameter  $a$  from 5.27 Å to 5.11 Å. At the same time, the lattice parameter  $c$  of  $R3\text{-Zn}_3\text{TeO}_6$  under compression strain in the  $ab$  direction is changed to 14.38 Å, which is larger than the intrinsic  $R3\text{-Zn}_3\text{TeO}_6$ . When a similar tensile strain is introduced in the  $R3\text{-Zn}_3\text{TeO}_6$  along  $ab$  plane, the lattice parameters  $a$  and  $c$  of  $R3\text{-Zn}_3\text{TeO}_6$  are changed to 5.43 Å and 13.70 Å, respectively. When the compressive and tensile strains increase to 6%, the variation trends of the lattice parameters  $a$  and  $c$  remain essentially consistent with those observed under 3% strain. In all tables and pictures,  $c\text{-Zn}_3\text{TeO}_6$  and  $t\text{-Zn}_3\text{TeO}_6$  have been used to express as  $\text{Zn}_3\text{TeO}_6$  under compressive strain and tensile strain, respectively. The lattice  $a/c$  ratios of  $\text{Zn}_3\text{TeO}_6$  approach 0.37, closely matching those of  $\text{Co}_3\text{TeO}_6$ ,<sup>9</sup>  $\text{Ni}_3\text{TeO}_6$

Table 1 The calculated lattice parameters by PBE method

$R3$	$a$ (Å)	$c$ (Å)
$c\text{-Zn}_3\text{TeO}_6$ (−6%)	4.96	14.78
$c\text{-Zn}_3\text{TeO}_6$ (−3%)	5.11	14.38
$\text{Zn}_3\text{TeO}_6$	5.27	14.02
$t\text{-Zn}_3\text{TeO}_6$ (3%)	5.43	13.70
$t\text{-Zn}_3\text{TeO}_6$ (6%)	5.59	13.45
$\text{Co}_3\text{TeO}_6$ (ref. 9)	5.19	13.80
$\text{Ni}_3\text{TeO}_6$ (ref. 10)	5.11	13.75
$\text{Mg}_3\text{TeO}_6$ (ref. 11)	5.14	13.81



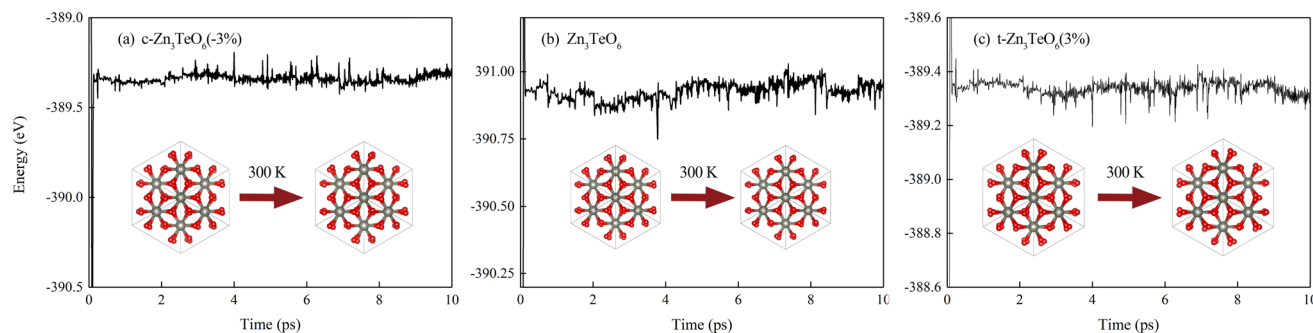


Fig. 2 AIMD energy evolution of  $\text{Zn}_3\text{TeO}_6$  under (a)  $-3\%$  compressive strain, (b) the unstrained structure, and (c)  $+3\%$  tensile strain.

(ref. 12) and  $\text{Mg}_3\text{TeO}_6$ ,<sup>13</sup> indicating a highly similar crystal structure. The stability and photoelectric properties of  $R3\text{-Zn}_3\text{TeO}_6$  under compressive and tensile strain have been analyzed by elastic properties, phonon spectrum and electronic structure.

### 3. Results and discussion

#### 3.1 Stability and mechanical properties

*Ab initio* molecular dynamics (AIMD) simulations were performed at 300 K within the *NVT* ensemble using the Nosé-Hoover thermostat, with a time step of 2 fs and a total simulation duration of 10 ps. Fig. 2 presents the evolution of the total energy of  $\text{Zn}_3\text{TeO}_6$  under various strain conditions. As shown in Fig. 2, the compressive ( $-3\%$ ), unstrained, and tensile ( $+3\%$ ) configurations exhibit only minor fluctuations in total energy throughout the simulation, with no abrupt changes or indications of structural collapse. The atomic configurations after the AIMD run remain essentially identical to their initial structures, with no bond breaking or noticeable lattice distortion observed. These results confirm that  $R3\text{-Zn}_3\text{TeO}_6$  retains good thermal and dynamic stability within the investigated strain range. In addition to the  $\pm 3\%$  strain discussed in the main text, AIMD

simulations under larger biaxial strains of  $-6\%$  and  $+6\%$  were included in the SI to provide a more comprehensive assessment of the strain-dependent thermal stability of  $R3\text{-Zn}_3\text{TeO}_6$ . As shown in Fig. S1 (SI), the system under  $-6\%$  compressive strain exhibits an upward trend in total energy during the 300 K, 10 ps simulation, suggesting potential instability despite the absence of structural collapse or bond breaking. In contrast, the  $+6\%$  tensile configuration shows relatively stable energy fluctuations and remains structurally intact, indicating that it still maintains dynamic stability. Overall, the stability of  $\text{Zn}_3\text{TeO}_6$  deteriorates under such large strain conditions.

The phonon spectra of  $R3\text{-Zn}_3\text{TeO}_6$  under compressive and tensile strain were calculated using the VASP + PHONOPY package.<sup>34</sup> As displayed in Fig. 3, all phonon frequencies are positive with no imaginary modes, demonstrating that the material satisfies the dynamic stability criteria within this strain range. Furthermore, compressive strain increases phonon frequencies, whereas tensile strain reduces them, indicating that compressive strain enhances the dynamic stability of  $R3\text{-Zn}_3\text{TeO}_6$  while tensile strain slightly weakens it. Phonon calculations under larger biaxial strains of  $-6\%$  and  $+6\%$  were also provided in the SI. As shown in Fig. S2 (SI, imaginary phonon modes appear under both strain conditions,

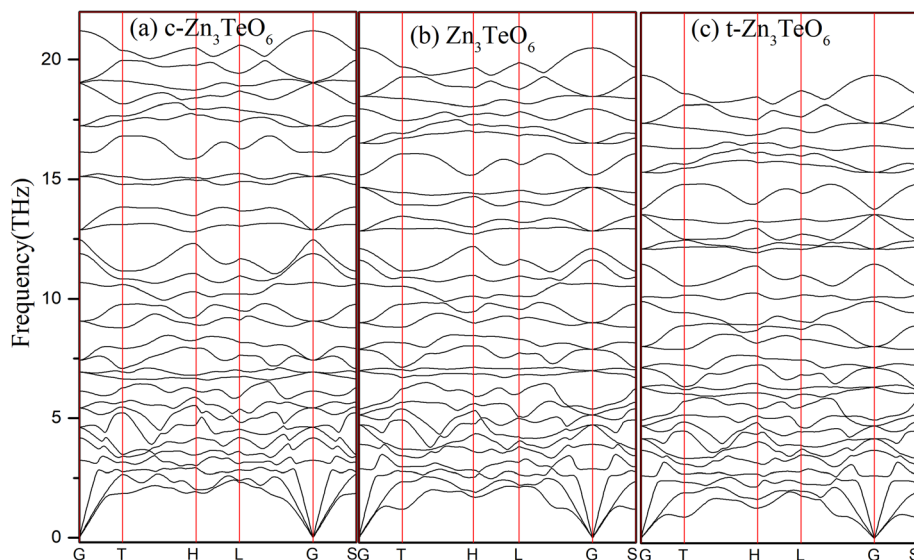


Fig. 3 The calculated phonon frequency of (a)  $c\text{-Zn}_3\text{TeO}_6$ , (b)  $\text{Zn}_3\text{TeO}_6$  and (c)  $t\text{-Zn}_3\text{TeO}_6$ .



Table 2 The calculated elastic constants and the unit is given in GPa

R3	$C_{11}$	$C_{12}$	$C_{13}$	$C_{14}$	$C_{15}$	$C_{33}$	$C_{44}$
c-Zn <sub>3</sub> TeO <sub>6</sub> (-6%)	290.948	177.480	127.568	14.680	1.569	285.218	32.349
c-Zn <sub>3</sub> TeO <sub>6</sub> (-3%)	270.858	151.487	104.092	16.212	2.533	244.507	34.758
Zn <sub>3</sub> TeO <sub>6</sub>	238.136	130.239	79.997	17.669	8.430	202.499	26.784
t-Zn <sub>3</sub> TeO <sub>6</sub> (3%)	207.301	121.390	62.335	19.075	14.730	174.200	19.133
t-Zn <sub>3</sub> TeO <sub>6</sub> (6%)	141.795	114.394	34.617	20.679	19.190	139.421	16.947

Table 3 The calculated Bulk modulus  $B$ , Shear modulus  $G$  and Young's modulus  $E$ 

R3	$B$ (GPa)	$G$ (GPa)	$E$ (GPa)
c-Zn <sub>3</sub> TeO <sub>6</sub> (-6%)	192.957	52.858	145.307
c-Zn <sub>3</sub> TeO <sub>6</sub> (-3%)	166.064	48.519	132.638
Zn <sub>3</sub> TeO <sub>6</sub>	138.108	38.794	106.417
t-Zn <sub>3</sub> TeO <sub>6</sub> (3%)	117.896	24.267	68.126
t-Zn <sub>3</sub> TeO <sub>6</sub> (6%)	93.096	14.764	46.763

confirming that the dynamic stability of Zn<sub>3</sub>TeO<sub>6</sub> deteriorates significantly when subjected to such large strains.

To assess the mechanical stability of R3-Zn<sub>3</sub>TeO<sub>6</sub> under compressive and tensile strain, the elastic constants were calculated using the VASP package, as summarized in Table 2. Owing to the symmetry of the trigonal/rhombohedral system (R3 space group), seven independent elastic constants were obtained. According to the stability criteria proposed by Mouhat and Coudert,<sup>35</sup> R3-Zn<sub>3</sub>TeO<sub>6</sub> is mechanically stable when the following inequalities are satisfied:

- (i)  $C_{11} > |C_{12}|$
- (ii)  $C_{13}^2 < 0.5 \times C_{33} \times (C_{11} + C_{12})$
- (iii)  $C_{14}^2 + C_{15}^2 < 0.5C_{44} \times (C_{11} - C_{12})$
- (iv)  $C_{44} > 0$

Our results show that under +6% tensile strain, the elastic constants fail to satisfy these inequalities, indicating mechanical instability. In contrast, the unstrained configuration and all other strain states meet the criteria and thus remain mechanically stable. Notably, compressive strain increases the elastic constants, implying enhanced mechanical strength, whereas

tensile strain reduces them, leading to weakened stability. This trend is consistent with our previous findings.<sup>36</sup> We further evaluated the bulk modulus  $B$ , shear modulus  $G$ , and Young's modulus  $E$  using the Voigt-Reuss-Hill (VRH) approximation.<sup>37</sup> The explicit formulas are:

$$B_V = \frac{1}{9}[2(C_{11} + C_{12}) + C_{33} + 4C_{13}]$$

$$G_V = \frac{1}{30}(C_{11} + C_{12} + 2C_{33} - 4C_{13} + 12C_{44} + 12C_{66})$$

$$B_R = \frac{(C_{11} + C_{12})C_{33} - 2C_{13}^2}{C_{11} + C_{12} + 2C_{33} - 4C_{13}}$$

$$G_R = \frac{5}{2} \frac{[(C_{11} + C_{12})C_{33} - 2C_{13}^2]C_{44}C_{66}}{3B_V C_{44}C_{66} + [(C_{11} + C_{12})C_{33} - 2C_{13}^2](C_{44} + C_{66})}$$

$$C_{66} = \frac{1}{2}(C_{11} - C_{12})$$

$$B = \frac{1}{2}(B_V + B_R)$$

$$G = \frac{1}{2}(G_V + G_R)$$

$$E = \frac{9BG}{3B + G}$$

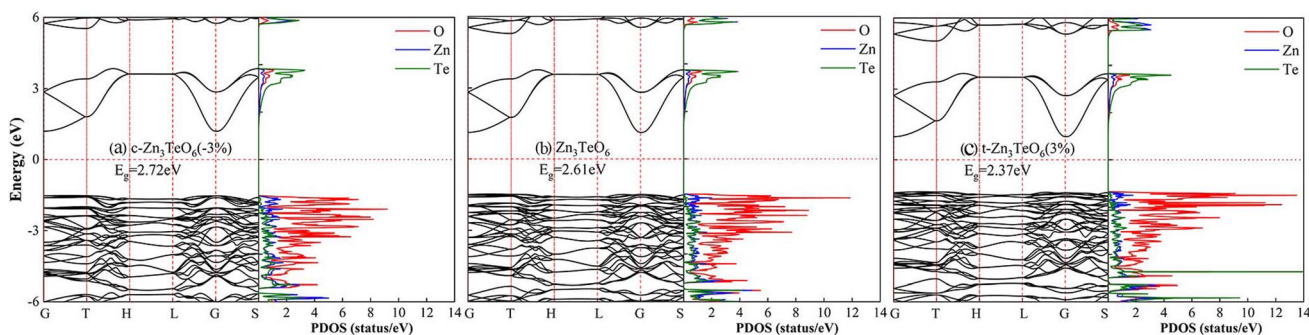
Fig. 4 The calculated band structure and density of states of (a) c-Zn<sub>3</sub>TeO<sub>6</sub>, (b) Zn<sub>3</sub>TeO<sub>6</sub> and (c) t-Zn<sub>3</sub>TeO<sub>6</sub>.

Table 4 The calculated bond length of Zn–O and Te–O. The unit is given in Å

	Zn1–O1	Zn1–O2	Zn2–O1	Zn2–O2	Zn3–O1	Zn3–O2	Te–O1	Te–O2
c-Zn <sub>3</sub> TeO <sub>6</sub> (–6%)	2.25	2.00	2.00	2.18	1.95	2.18	1.96	1.92
c-Zn <sub>3</sub> TeO <sub>6</sub> (–3%)	2.30	2.02	1.99	2.23	2.02	2.23	1.97	1.94
Zn <sub>3</sub> TeO <sub>6</sub>	2.33	2.04	2.03	2.27	2.05	2.29	1.98	1.95
t-Zn <sub>3</sub> TeO <sub>6</sub> (3%)	2.36	2.07	2.08	2.32	2.08	2.35	2.00	1.97
t-Zn <sub>3</sub> TeO <sub>6</sub> (6%)	2.37	2.10	2.09	2.45	2.14	2.30	2.01	1.98

As summarized in Table 3, compressive strain leads to an increase in Young's modulus, whereas tensile strain reduces it, consistent with trends reported in previous literature.<sup>36</sup> Integrating the results from molecular dynamics, phonon spectra, and elasticity-based stability analyses, we conclude that R3-Zn<sub>3</sub>TeO<sub>6</sub> remains stable under small strains ( $\pm 3\%$ ), while larger strains ( $\pm 6\%$ ) are prone to inducing instability. This is in agreement with experimental observations: during the fabrication of three-dimensional polar films *via* pulsed laser deposition (PLD) or molecular beam epitaxy (MBE), substrates with closely matched lattice parameters are typically required.<sup>10,11</sup> Therefore, in the following discussions on electronic structure, band dispersion, optical properties, ferroelectric polarization, and carrier transport behavior, we primarily focus on configurations under small strain ( $\pm 3\%$ ).

### 3.2 Optoelectronic property

The energy band structure and densities of states (DOS) for R3-Zn<sub>3</sub>TeO<sub>6</sub> under unstrained, compressive, and tensile conditions were calculated using the HSE06 hybrid functional. As shown in Fig. 4, the unstrained R3-Zn<sub>3</sub>TeO<sub>6</sub> exhibits a calculated band gap of 2.60 eV. This value modulates under applied strain, widening to 2.72 eV under compressive strain (c-Zn<sub>3</sub>TeO<sub>6</sub>) and narrowing to 2.36 eV under tensile strain (t-Zn<sub>3</sub>TeO<sub>6</sub>). These calculated band gaps are considerably smaller than that of HP-Mg<sub>3</sub>TeO<sub>6</sub> (3.5 eV), suggesting potential for absorption over a broader portion of the visible spectrum and potentially enhanced photoelectric conversion efficiency.<sup>13</sup> Specifically, the band gap narrowing under tensile strain suggests enhanced

visible light absorption, whereas the band gap widening under compression is expected to shift the absorption onset toward the ultraviolet region, reducing responsiveness to visible light. Analysis of the projected densities of states (PDOS) in Fig. 4 indicates that considerable hybridization between O 2p and Zn 3d orbitals occurs within the valence band (*ca.* –3.5 to –2.0 eV). This hybridization likely plays a significant role in determining the material's primary electronic properties. The states near the valence band maximum (VBM) are predominantly composed of hybridized O–Zn orbitals, while the states near the conduction band minimum (CBM) are mainly derived from O–Te hybrid orbitals. For both the VBM and CBM, O 2p states provide the most significant contribution. Compared to the unstrained structure, c-Zn<sub>3</sub>TeO<sub>6</sub> exhibits a lower density of O-derived states at the VBM, whereas t-Zn<sub>3</sub>TeO<sub>6</sub> shows a higher density. Simultaneously, the CBM energy level shifts upward for c-Zn<sub>3</sub>TeO<sub>6</sub> and downward for t-Zn<sub>3</sub>TeO<sub>6</sub> relative to the unstrained case. The mechanism for this band gap widening under compression is consistent with the findings of Liu H. L. *et al.*<sup>23</sup> and can be attributed to the shortening of O–Zn and O–Te bond lengths Table 4, which enhances orbital overlap. The band structures of Zn<sub>3</sub>TeO<sub>6</sub> under  $\pm 6\%$  compressive and tensile strain were also calculated, and the results are provided in the SI (Fig. S3). The bandgaps obtained under 6% compressive and 6% tensile strain are 2.68 eV and 2.03 eV, respectively. Relative to the unstrained state, the compressive strain results in an increased bandgap, whereas the tensile strain leads to a reduced bandgap.

The absorption coefficient  $\alpha(\omega)$  can be obtained from the real part  $\epsilon_1(\omega)$  and imaginary part  $\epsilon_2(\omega)$  of the dielectric function *via*

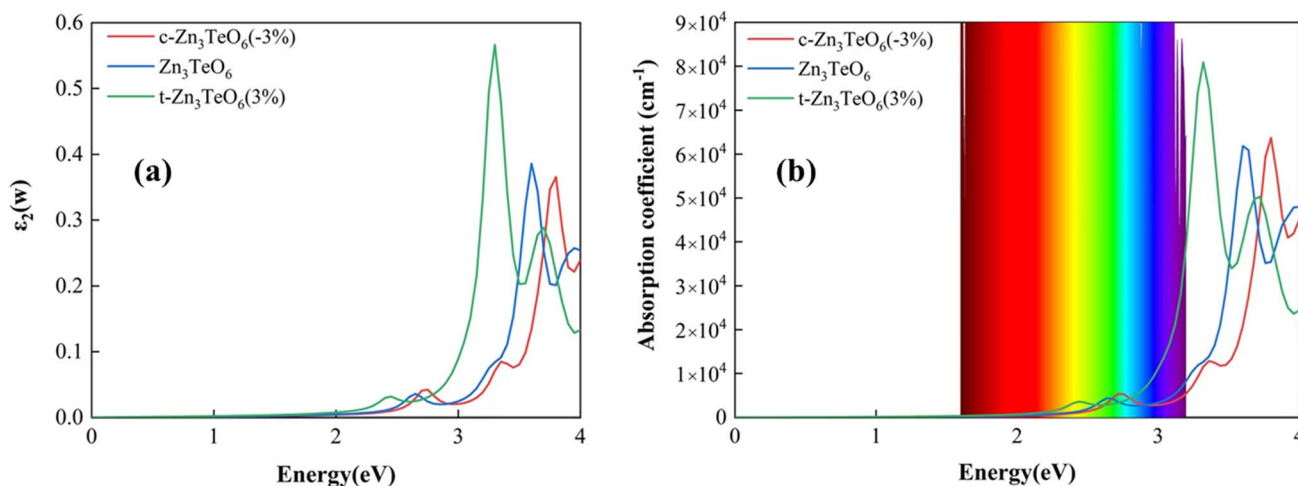


Fig. 5 (a) Imaginary component of the dielectric function ( $\epsilon_2$ ) and (b) optical absorption coefficient ( $\alpha$ ) of Zn<sub>3</sub>TeO<sub>6</sub>.



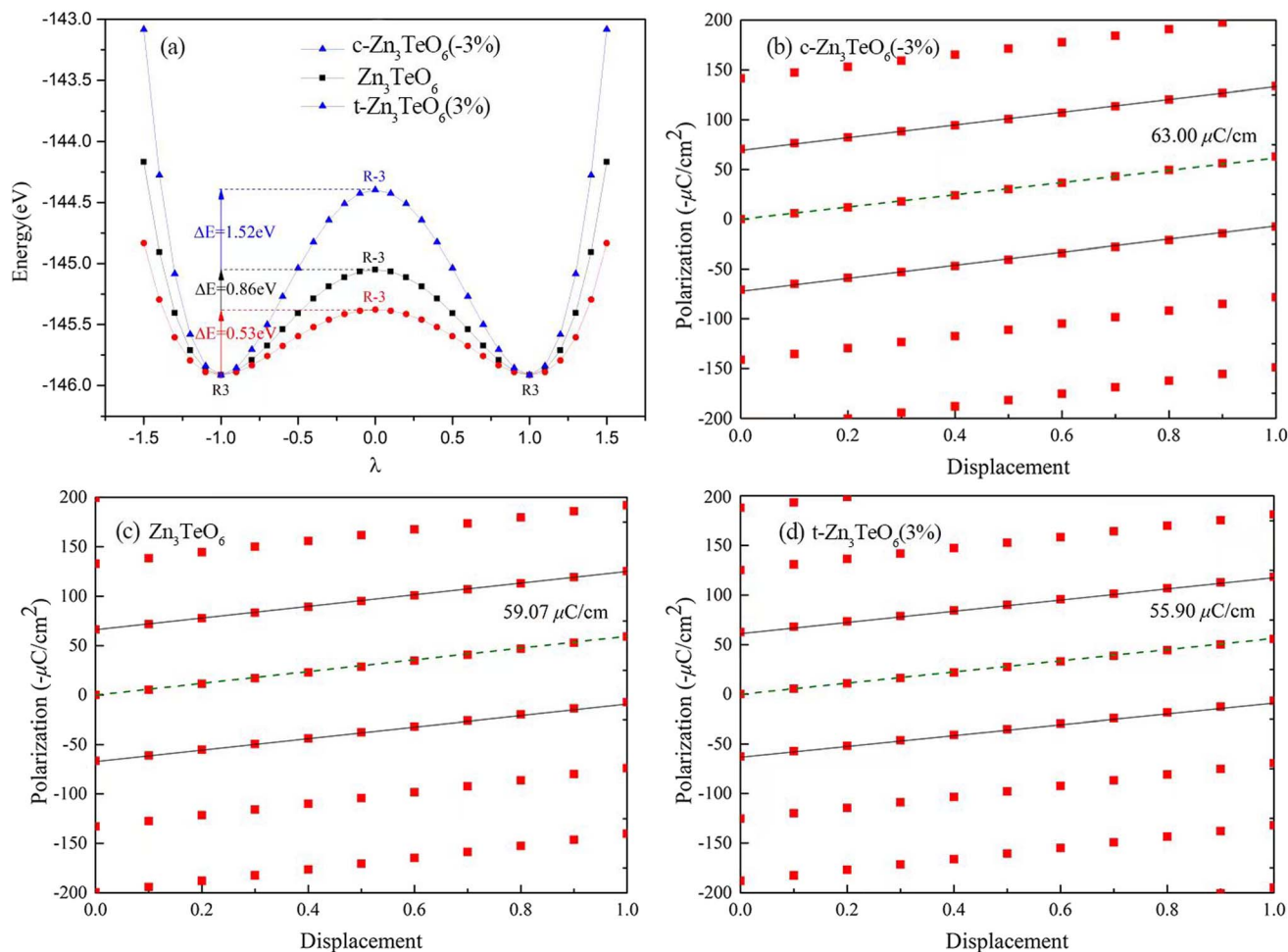


Fig. 6 (a) Potential energy curves and ferroelectric polarization as a function of structural distortion for (b)  $-3\%$  compressive strain, (c) the unstrained structure, and (d)  $+3\%$  tensile strain.

the formula  $\alpha(\omega) = \frac{\sqrt{2}\omega}{c} \left[ \sqrt{\varepsilon_1(\omega)^2 + \varepsilon_2(\omega)^2} - \varepsilon_1(\omega) \right]^{1/2}$ . As shown in Fig. 5, pristine  $\text{Zn}_3\text{TeO}_6$  and its strained counterparts exhibit consistent optical-response trends in both  $\varepsilon_2(\omega)$  and  $\alpha(\omega)$ : negligible absorption is found in the low-energy region ( $< \sim 2.2$  eV), indicating weak intrinsic absorption in the visible range, whereas a sharp rise emerges near the band edge, giving rise to pronounced peaks. Consequently, all three structures show strong ultraviolet absorption above  $\sim 3$  eV, with maximum absorption coefficients on the order of  $10^4 \text{ cm}^{-1}$ . A clear divergence appears under tensile *versus* compressive strain. The  $3\%$  tensile strain narrows the band gap, causing a red shift of the absorption edge for  $t\text{-Zn}_3\text{TeO}_6$  to  $\sim 2.8$  eV and producing a stronger main peak around  $3.1\text{--}3.3$  eV (maximum  $\varepsilon_2 \approx 0.55$  with a corresponding absorption peak of  $\sim 8 \times 10^4 \text{ cm}^{-1}$ ), thereby enabling enhanced near-UV and lower-energy photon absorption. In contrast,  $-3\%$  compressive strain widens the band gap, shifting the absorption edge of  $c\text{-Zn}_3\text{TeO}_6$  to higher energy ( $\sim 3.1$  eV) and slightly moving the main peak toward  $\sim 3.7\text{--}3.8$  eV with reduced intensity, confining its dominant response to the ultraviolet region. These results confirm that strain engineering is an effective approach for tuning band-edge

optical transitions and optimizing the electronic and optical properties of  $R3\text{-Zn}_3\text{TeO}_6$ .

### 3.3 Ferroelectric property

The ferroelectric polarization of unstrained, compressively strained, and tensile-strained  $R3\text{-Zn}_3\text{TeO}_6$  was calculated using the Berry-phase method.<sup>38,39</sup> Following this approach, a centrosymmetric  $R3$  reference structure was constructed, and the energy and polarization were obtained through linear interpolation between the polar  $R3$  phase ( $\lambda = 1$ ) and the centrosymmetric phase ( $\lambda = 0$ ). As shown in Fig. 6(a), the structural distortion energy curves of  $R3\text{-Zn}_3\text{TeO}_6$  under all strain conditions exhibit a double-well potential, indicating robust ferroelectricity. The ferroelectric well depths are  $0.86$  eV (unstrained),  $1.52$  eV (compressive strain), and  $0.53$  eV (tensile strain). Because the calculations correspond to three formula units, the averaged well depths per  $\text{Zn}_3\text{TeO}_6$  formula unit are  $0.29$  eV,  $0.51$  eV, and  $0.18$  eV, respectively. Under compressive strain, the well depth ( $0.51 \text{ eV f.u.}^{-1}$ ) becomes comparable to that of the classical ferroelectric  $\text{BiFeO}_3$  ( $0.43 \text{ eV f.u.}^{-1}$ ),<sup>40</sup> demonstrating that compressive strain enhances the stability of the ferroelectric phase. The calculated spontaneous polarization of  $R3\text{-Zn}_3\text{TeO}_6$



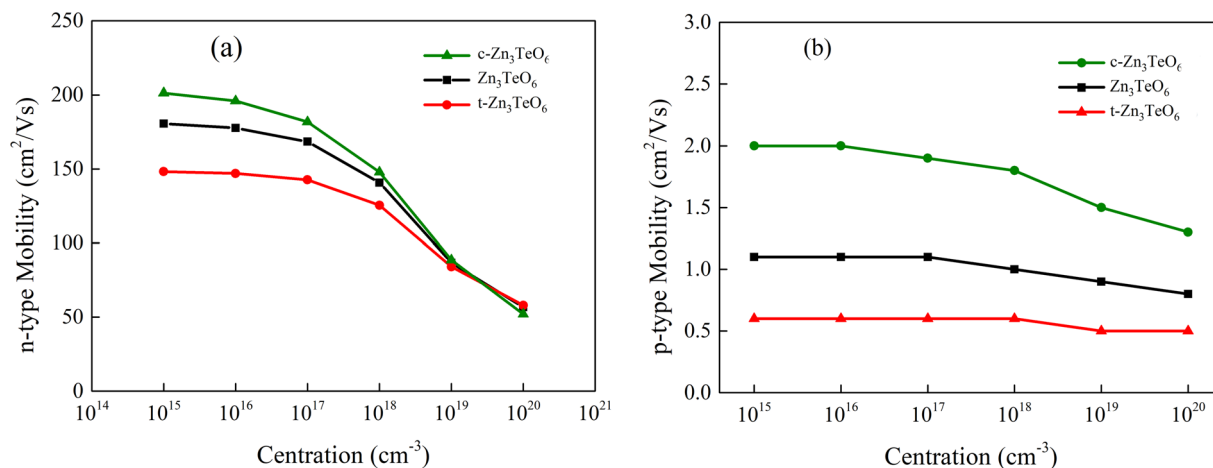


Fig. 7 The (a) electron and (b) hole mobility as a function of concentration for semiconductor  $\text{Zn}_3\text{TeO}_6$  by AMSET code.

increases from  $59.07 \mu\text{C cm}^{-2}$  (unstrained) to  $63.00 \mu\text{C cm}^{-2}$  under compressive strain, approaching the reported value of  $72 \mu\text{C cm}^{-2}$  for  $\text{Ni}_3\text{TeO}_6$ .<sup>9</sup> This enhancement originates from the reduced interatomic distances and strengthened polar phonon instability induced by compressive strain. Under 3% tensile strain, the polarization decreases to  $55.90 \mu\text{C cm}^{-2}$ , which is consistent with the behavior observed in  $R3c\text{-BiFeO}_3$ .<sup>41</sup> Fig. 6(b–d) show that at the polarization endpoints ( $\lambda = \pm 1$ ), compressive strain significantly increases the slope of the polarization curve, indicating a stronger and faster lattice-distortion-induced polarization response. In contrast, tensile strain reduces both polarization and potential-well depth, thereby weakening ferroelectric stability. As shown in Fig. S4, the potential-energy curves under 0%,  $\pm 3\%$ , and  $\pm 6\%$  strain confirm these trends. Tensile strain gradually shallows the double-well potential and reduces the energy difference between the ferroelectric and paraelectric phases. At 6% tensile strain, the two wells nearly merge, and the interpolation-based Berry-phase method fails to converge. Conversely, 6% compressive strain deepens the ferroelectric–paraelectric potential well and increases the spontaneous polarization to  $67.94 \mu\text{C cm}^{-2}$ .

### 3.4 Mobility

The carrier mobility of semiconductors governs the electrical conductivity and switching performance of devices and is

therefore critical for many applications. Fig. 7 presents the electron and hole mobilities of the three structures as a function of n-type and p-type carrier concentrations, calculated using the AMSET code within the momentum relaxation time approximation (MRTA) framework.<sup>42</sup> In these calculations, four dominant scattering mechanisms are explicitly considered: acoustic deformation potential (ADP) scattering, piezoelectric (PIE) scattering, polar optical phonon (POP) scattering, and ionized impurity (IMP) scattering. The total mobility is obtained by combining the contributions from these scattering processes, and all relevant parameters are derived from first-principles calculations. For ADP scattering, small uniaxial (or isotropic) strains are applied to the crystal, and the band structures are recalculated for each strain value. The deformation potential constant  $E_1$  is then obtained by linearly fitting the variation of the conduction-band minimum (CBM) or valence-band maximum (VBM) energy with respect to strain, as summarized in Table 5, while the corresponding elastic constants are taken from Table 2. For PIE scattering, the piezoelectric tensor is evaluated using density functional perturbation theory (DFPT) under small strains by computing the change in polarization and is subsequently combined with the elastic constants and piezoelectric tensor for transport calculations Tables 2 and 6. For POP scattering, the longitudinal optical (LO) phonon frequency at the  $\Gamma$  point, together with the static and high-frequency dielectric constants ( $\epsilon_0$  and  $\epsilon_\infty$ ), is obtained from

Table 5 The calculated the deformation potential calculations (eV)

		VBM			CBM		
		$D_{XX}$	$D_{YY}$	$D_{ZZ}$	$D_{XX}$	$D_{YY}$	$D_{ZZ}$
c- $\text{Zn}_3\text{TeO}_6$ (−3%)	$D_{XX}$	0.20	0.92	0.11	5.56	0.18	0.03
	$D_{YY}$	0.92	0.22	0.03	0.18	5.57	0.08
	$D_{ZZ}$	0.11	0.03	2.32	0.03	0.08	7.87
$\text{Zn}_3\text{TeO}_6$	$D_{XX}$	0.72	0.56	0.22	5.64	0.05	0.12
	$D_{YY}$	0.56	0.71	0.21	0.05	5.64	0.11
	$D_{ZZ}$	0.22	0.21	1.83	0.12	0.11	5.83
t- $\text{Zn}_3\text{TeO}_6$ (3%)	$D_{XX}$	1.61	0.22	0.31	5.67	0.09	0.1
	$D_{YY}$	0.22	1.62	0.32	0.09	5.66	0.1
	$D_{ZZ}$	0.31	0.32	0.95	0.1	0.1	4.16

Table 6 The calculated piezoelectric tensor ( $\text{C/m}^{-2}$ )

		XX	YY	ZZ	XY	YZ	ZX
c- $\text{Zn}_3\text{TeO}_6$	X	0.30	−0.30	0.00	0.12	0.00	−0.06
	Y	0.12	−0.12	0.00	−0.30	−0.06	0.00
	Z	−0.08	−0.08	−0.63	−0.01	0.00	0.00
$\text{Zn}_3\text{TeO}_6$	X	0.34	−0.34	0.00	0.25	0.05	−0.07
	Y	0.25	−0.25	0.00	−0.34	−0.06	−0.05
	Z	−0.56	−0.56	−1.10	−0.01	0.00	0.00
t- $\text{Zn}_3\text{TeO}_6$	X	0.45	−0.45	0.00	0.37	0.05	−0.15
	Y	0.37	−0.37	0.00	−0.45	−0.14	−0.05
	Z	−0.66	−0.66	−1.47	0.00	0.00	0.00



**Table 7** Parameters and results of mobility calculation.  $\omega_0$  is polar-optical phonon frequency (THz),  $\epsilon_0$  and  $\epsilon_\infty$  are static dielectric constant and high-frequency dielectric constant and  $m^*$  is effective mass ( $m_e$ ).  $S$  is the scattering rate of the material at a doping concentration of  $10^{-18} \text{ cm}^{-3}$  ( $10^{12} \text{ S}^{-1}$ )

		$\omega_0$	$\epsilon_0$	$\epsilon_\infty$	$m^*$	$S$			
						ADP	IMP	PIE	POP
c-Zn <sub>3</sub> TeO <sub>6</sub>	Electron	10.82	14.82	4.72	0.23	6.6	13.9	19.5	252
	Hole				6.88	6.6	12.7	19.5	252
Zn <sub>3</sub> TeO <sub>6</sub>	Electron	10.04	17.3	4.85	0.21	9.1	15.9	58.5	271
	Hole				8.01	9.1	14.4	58.5	271
t-Zn <sub>3</sub> TeO <sub>6</sub>	Electron	9.23	21.09	5.09	0.18	20.8	14.4	195	295
	Hole				8.46	20.8	12.9	195	295

DFPT Table 7, and these quantities are used to construct a Fröhlich-type electron–LO phonon coupling model. For IMP scattering, all dopants are assumed to be fully ionized, and the ionized impurity concentration is set equal to the carrier concentration specified in the transport calculations. The impurity charge number  $Z$  is chosen according to the assumed dopant valence, while the dielectric constant obtained from first-principles calculations is used to describe the screening of the coulomb interaction.

Within AMSET, the carrier mobility at different n-type and p-type doping levels is computed consistently under the MRTA framework. In this approach, doping is not modeled by explicit atomic substitution; instead, the target carrier concentration is provided as an input parameter. For a given electron or hole concentration, AMSET self-consistently determines the corresponding Fermi level and evaluates the scattering rates arising from ADP, POP, IMP, and other relevant mechanisms, and then solves the Boltzmann transport equation to obtain mobility. In this way, the dependence of electron and hole mobilities on n-type and p-type carrier concentrations is systematically established without modifying the underlying crystal structure.

The results show that at a moderate doping concentration of  $10^{18} \text{ cm}^{-3}$ , the electron mobility for all three structures exceeds  $150 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$ , approaching that of conventional semiconductor ZnO.<sup>43</sup> The hole mobility is two orders of magnitude lower than the electron mobility, indicating that Zn<sub>3</sub>TeO<sub>6</sub> is characterized by strong n-type behavior. From the input parameters Table 7, the hole effective mass is significantly larger than the electron effective mass, consistent with the relatively flat band structure near the VBM. This results in substantially lower hole transport capability compared to electrons. Among the scattering mechanisms, POP scattering dominates, reaching an order of magnitude of approximately  $10^{14} \text{ s}^{-1}$ , which critically determines the carrier relaxation time.

Notably, among the three structures c-Zn<sub>3</sub>TeO<sub>6</sub> exhibits the highest electron mobility value. Although compressive strain slightly increases the effective mass of Zn<sub>3</sub>TeO<sub>6</sub>, it concurrently elevates the characteristic frequency  $\omega_0$  of the polar optical phonons. As evident in the phonon dispersion spectra Fig. 3, c-Zn<sub>3</sub>TeO<sub>6</sub> possesses higher optical phonon frequencies. A higher

$\omega_0$  implies that greater energy is required for electrons to exchange energy with optical phonons, thereby significantly reducing POP scattering intensity. Furthermore, as strain transitions from tensile to compressive, the high-frequency dielectric constant  $\epsilon_\infty$  and the static dielectric constant  $\epsilon_0$  decrease slightly. Since the polar coupling strength is proportional to  $\frac{1}{\epsilon_\infty} - \frac{1}{\epsilon_0}$ , which equals 0.149, 0.148, and 0.144 for the t-Zn<sub>3</sub>TeO<sub>6</sub>, Zn<sub>3</sub>TeO<sub>6</sub>, and c-Zn<sub>3</sub>TeO<sub>6</sub> structures respectively, compressive strain weakens polar coupling, further suppressing POP scattering. For PIE scattering, under tensile strain, the scattering rate can reach the order of  $10^{14} \text{ s}^{-1}$ , highlighting its significant contribution to carrier scattering. However, as shown in Table 6, under compressive strain, the tensor components of the piezoelectric coefficients are notably reduced due to decreased lattice dimensions and restricted atomic displacements. This reduction stems from the smaller lattice dimensions and constrained atomic displacements within the unit cell, leading to diminished piezoelectric response and consequently reduced PIE scattering intensity. Overall, the analysis shows that compressive strain helps suppress the dominant scattering mechanisms POP and PIE, thereby enhancing the electron mobility in Zn<sub>3</sub>TeO<sub>6</sub>.

## 4. Conclusion

Using density functional theory, the elastic constants, phonon spectra, and molecular dynamics of R3-Zn<sub>3</sub>TeO<sub>6</sub> under compressive and tensile strain were systematically investigated to assess its structural stability. Electronic structure analyses reveal that the valence band is predominantly determined by Zn–O interactions, while the conduction band mainly arises from Te–O hybridization. Under compressive strain, the O orbital contribution near the valence band maximum decreases and the conduction band minimum shifts upward, resulting in a bandgap widening from 2.60 eV to 2.72 eV. Conversely, tensile strain enhances the O orbital contribution and lowers the conduction band minimum, narrowing the bandgap to 2.36 eV—favorable for visible-light absorption. Compressive strain significantly enhances the ferroelectric polarization of Zn<sub>3</sub>TeO<sub>6</sub>, conferring excellent ferroelectric performance and structural robustness. In terms of charge transport, Zn<sub>3</sub>TeO<sub>6</sub> exhibits high electron mobility ( $>150 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$ ) and hole mobility two orders of magnitude lower, indicative of a strong n-type character. Notably, compressive strain further promotes electron mobility through increased optical phonon frequencies and reduced piezoelectric coefficients, effectively suppressing carrier scattering. These results provide theoretical insight into the potential of R3-Zn<sub>3</sub>TeO<sub>6</sub> for stable, high-performance ferroelectric and optoelectronic applications.

## Conflicts of interest

The authors declared that they have no conflicts of interest to this work. We declare that we do not have any commercial or associative interest that represents a conflict of interest in connection with the work submitted.



## Data availability

The data that support the findings of this study are available from the corresponding author upon reasonable request.

Supplementary information (SI) is available. See DOI: <https://doi.org/10.1039/d5ra08570e>.

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