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# Fast and scalable retrosynthetic planning with a transformer neural network and speculative beam search

Natalia Andronova,<sup>†e</sup> Mikhail Andronov,<sup>†\*a</sup> Jürgen Schmidhuber,<sup>ab</sup> Michael Wand<sup>ad</sup> and Djork-Arné Clevert<sup>c</sup>

AI-based computer-aided synthesis planning (CASP) systems are in demand as components of AI-driven drug discovery workflows. However, the high latency of such CASP systems limits their utility for high-throughput synthesizability screening in *de novo* drug design. We propose a transformer-based single-step retrosynthesis model with reduced inference latency based on speculative beam search combined with a scalable drafting strategy called Medusa. Replacing the standard transformer and beam search with our approach accelerates the expansion stage of the planning algorithm, leading to higher solvability in CASP when planning under stringent time limits, and saves hours of computation when synthesis is constrained by the number of iterations. Our method brings AI-based CASP systems closer to meeting the stringent latency requirements of high-throughput synthesizability screening and improving the overall user experience.

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## 1 Introduction

The modern pharmaceutical industry is heavily investing in Artificial Intelligence (AI) technologies to reduce the substantial time and financial costs associated with drug development.<sup>1</sup> Thus far, AI tools have been most impactful in the preclinical stage of drug discovery, becoming an integral part of the traditional Design-Make-Test-Analyze (DMTA) cycle. Numerous *de novo* drug design tools can generate virtually unlimited numbers of AI-designed molecular structures for the first stage of the DMTA cycle, already helping to identify potential drug candidates.<sup>2</sup> Naturally, the initially generated molecules must undergo extensive filtering, including the filtering for synthesizability.

Synthesizability, *i.e.*, the existence of a valid synthesis route from a given target molecule to available building blocks, depends on factors such as route length, yield, cost, the available stock of building blocks, and permitted reaction types.<sup>3</sup> Constructing a complete retrosynthetic tree with a Computer-Aided Synthesis Planning (CASP) system provides the most rigorous and flexible assessment of synthesizability. Often, in practical workflows,<sup>4,5</sup> full synthesis planning may be replaced

with filtering of generated molecules by molecular complexity scores such as SA score<sup>6</sup> or SYBA,<sup>7</sup> or by machine-learned retrosynthesis prediction scores such as RA score,<sup>8</sup> which estimate the likelihood that a CASP system will identify a synthetic route. However, these surrogate metrics provide only approximate assessments and do not replace explicit retrosynthetic tree construction; they may miss feasible routes or overestimate synthetic accessibility. Therefore, accelerating full retrosynthesis planning remains necessary for reliable synthesizability estimation of large amounts of novel molecules.

Like other areas of drug discovery, synthesis planning is also being transformed by AI, and AI-powered CASP systems are now in demand. Open-source AI-based CASP systems such as AiZynthFinder,<sup>9,10</sup> ASKCOS,<sup>11</sup> SynPlanner,<sup>12</sup> and Syntheseus<sup>13</sup> combine a single-step retrosynthesis model with a planning algorithm (*e.g.*, MCTS<sup>14</sup> or A\*<sup>15</sup>), implementing the design proposed by Segler *et al.*<sup>14</sup>

A major challenge limiting the integration of AI-based CASP systems into the DMTA cycle is the stringent latency requirements that a CASP tool must meet to keep up with the flood of structures produced by *de novo* generators. Current AI CASP systems are not fast enough for applications in the high-throughput setting, taking up to several hours to generate a synthesis plan for a molecule.<sup>16,17</sup> Therefore, AI CASP systems will greatly benefit from accelerated inference.

The single-step retrosynthesis models that enable state-of-the-art accuracy are template-free models based on a general sequence-modeling neural network architecture called the transformer.<sup>18–20</sup> Typically, single-step retrosynthesis is formulated as a conditional SMILES generation task in transformer

<sup>a</sup>SUPSI, IDSIA, Lugano, Switzerland. E-mail: mikhail.andronov@idsia.ch<sup>b</sup>Center of Excellence for Generative AI, KAUST, Thuwal, Saudi Arabia<sup>c</sup>Machine Learning Research, Pfizer Research and Development, Berlin, Germany<sup>d</sup>Institute for Digital Technologies for Personalized Healthcare, SUPSI, Lugano, Switzerland<sup>e</sup>Independent Researcher, Lugano, Switzerland

† These authors contributed equally to this work.



models: the model “translates” a query product SMILES into a set of candidate precursor SMILES using beam search in inference.<sup>21–23</sup> Since transformers also serve as the backbone for most Large Language Models (LLMs),<sup>24</sup> SMILES-to-SMILES transformers as single-step models provide unique opportunities for latency optimization inspired by advances in LLM inference acceleration.

In this work, we demonstrate the acceleration of multi-step retrosynthesis that relies on a SMILES-to-SMILES transformer as a single-step model using two complementary techniques. We accelerate the parallel decoding of single-step expansions using the recently proposed speculative beam search (SBS),<sup>25</sup> which extends speculative decoding<sup>26</sup> to beam search, in combination with a state-of-the-art drafting approach called Medusa. By integrating both techniques into AiZynthFinder,<sup>27</sup> we achieve substantial speed gains in multi-step retrosynthesis. Our method brings AI-based synthesis planning closer to the real-time performance required for integration into modern drug discovery pipelines.

## 2 Methods

### 2.1 Speculative decoding

Speculative decoding is a method of reducing the generation latency of autoregressive transformer models. It was originally introduced in the field of Large Language Models (LLMs), where inference speed is a critical issue. Autoregressive transformers are the foundation of both LLMs and template-free SMILES-to-SMILES synthesis prediction; they generate one text token per run, requiring multiple sequential runs to complete a text or a SMILES string. Each model run (forward pass) involves substantial computational overhead and processing time. Speculative decoding accelerates generation by reducing the number of model calls without sacrificing accuracy. It does so by accepting or rejecting entire subsequences that serve as guesses for potential sequence continuations, where these guesses, called “drafts”, may come from arbitrary sources. For example, they can be generated by a dedicated draft model or assembled based on heuristics.

The transformer decoder accepts a sequence of  $N$  tokens as input and predicts the next token for each position. In standard autoregressive generation, we discard all predictions except the last one, append it to the input sequence, and re-run the transformer. However, in speculative decoding, we first concatenate the input sequence with a draft sequence of  $M$  tokens to leverage predictions for multiple positions simultaneously. If the prediction for the last input token matches the first token in the draft sequence, we accept the first draft token and check the prediction for the next position. We repeat this process until either a predicted token differs from the corresponding draft token or we reach the end of the draft sequence. This approach generates between 1 token in the worst case and  $M + 1$  tokens in the best case per transformer forward pass. The probability of accepting a token from the draft is called *acceptance rate*.<sup>26</sup> The empirical mean acceptance rate on the test set is the proportion of accepted speculative tokens to the total number of speculative tokens.

SMILES-to-SMILES generation is a task that is remarkably well-suited for speculative decoding. In chemical reactions, only some of the reactant atoms typically change their connectivity, while large fragments of the reactants remain unchanged and appear the same in the products. Therefore, instead of constructing the target SMILES token by token, the transformer can quickly assemble it from fragments of the query SMILES if they are presented as draft sequences. Extracting multiple fragments of a fixed length from a query sequence, trying them all as drafts at every generation step, and choosing the draft with the most accepted tokens is the essence of the heuristic drafting scheme for speculative decoding applied to SMILES-to-SMILES generation.<sup>25</sup>

### 2.2 Speculative beam search

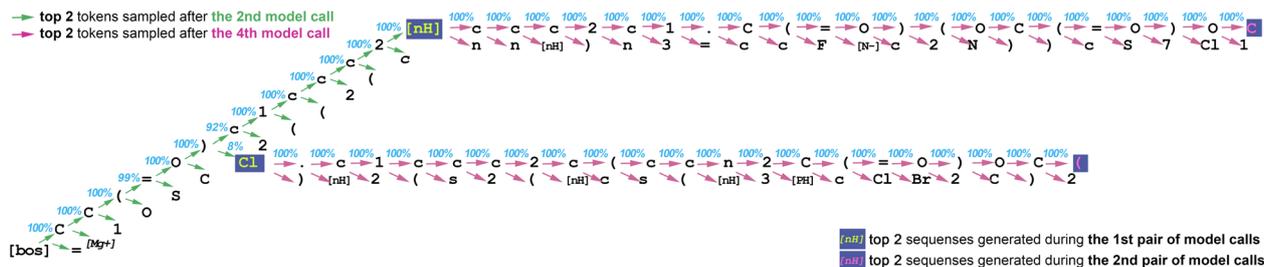
The limitation of basic speculative decoding is that it supports generating only one output sequence per input sequence. While sufficient for text generation in most cases, it poses a major obstacle to the potential of speculative decoding to accelerate template-free reaction prediction and single-step retrosynthesis models. When working as a component of a CASP system, a SMILES-to-SMILES transformer must produce multiple candidate predictions for every query, typically through beam search. We recently developed a method called “speculative beam search (SBS)”<sup>25</sup> in an attempt to introduce speculative decoding into CASP. SBS achieves up to  $3\times$  acceleration of Molecular Transformer<sup>21</sup> inference for reaction prediction and single-step retrosynthesis. The core idea of SBS is an extra step before appending the accepted draft tokens to the growing sequence. After selecting the accepted tokens, we determine the top- $K$  most probable next tokens for each accepted token using the model’s forward pass. With that, we obtain a set of candidate subsequences of different lengths, which we then sort by probabilities and extract the top- $K$  most probable continuations to use as beams. Both shorter and longer sequences may be the most probable. The drafts in SBS are generated by a heuristic drafting scheme that uses multiple fragments of the query SMILES as drafts.

### 2.3 Medusa

While SBS achieves good inference acceleration in reaction prediction and single-step retrosynthesis, the heuristic drafting strategy presents a scalability problem.<sup>25</sup> To achieve a high acceptance rate, multiple drafts should be used in parallel. It increases the effective batch size as  $O(BKN)$ , where  $B$  is the basic batch size,  $K$  is the number of beams, and  $N$  is the number of drafts. The latency of a forward pass of the model increases with batch size, and may quickly outweigh the benefits of the high throughput given by batching.

A recently proposed method, “Medusa”,<sup>28</sup> offers a simple solution for generating single drafts with a high acceptance rate. The fundamental idea of the method is to add extra subnetworks (decoding heads) to the transformer neural network that predict multiple tokens ahead of the next token in parallel. Instead of the usual transformer logits output of shape  $(B, L, V)$ , a Medusa model gives  $(B, L, M, V)$ , where  $B$  is the input





**Fig. 1** An example of the first two cycles of the sampling of candidate sequence trees in our Medusa speculative beam search with beam size 2. Each cycle takes 2 model calls. Here, we select the two best candidates at each cycle. The first model call produces 'CC(=O)c1ccc2ccccc2.C' as the draft of 20 tokens for 'CC(=O)c1ccc2c(ccn2C(=O)OC(C)(C)C)c1' as the encoder input and '[bos]' as the decoder input. Then this draft is concatenated to the decoder input, and another model call produces probabilities. The predicted probabilities of the main model head are used to make top-p (nucleus 99.75%) verification (12 draft tokens are accepted) and to produce candidates in top-k mode. The best sequences are CC(=O)c1ccc2 and CC(=O)Cl, and they become the "beams". In the next iteration, the draft for the first "beam" is ccc2c1.C(=O)(OC(=O)O (all 20 tokens are accepted), and for the second one it is .c1ccc2c(ccn2C(=O)OC (all 20 tokens are accepted). The fourth model call generates 44 sequences overall, which are all sorted by their probabilities. The most probable sequences in the second cycle are c1c[nH]c2ccc(C)C(= and c1c[nH]c2ccc(C)C(=, and they become the generated sequences for the next iteration. In this example, after 2 pairs of model calls, M-SBS generates 2 sequences of lengths 35 and 28, respectively, whereas the standard beam search would have generated 2 sequences of length 4.

batch size,  $L$  is the decoder input length,  $V$  is the vocabulary size, and  $M$  is the number of Medusa model heads. While the main prediction head generates the next token as usual, the additional Medusa heads predict the second next token, the third next token, and so on up to the  $M$ -th next token.

The tokens predicted by the additional heads are the draft sequences for the main head to verify. The first Medusa call is used to generate a draft. In our experiments, the model has 20 heads, so the draft length is 20. We use greedy decoding to create only one draft per given input sequence to avoid inflating the effective batch size. The second Medusa call uses only the main head's output data to verify draft tokens. At least one draft token will always be approved (since it was generated by the main model head in greedy mode), so the worst case is 2 tokens generated across 2 model calls. Of course, the worst-case scenario is still undesirable, as additional heads necessitate additional weights in the model architecture, which may result in a slightly slower forward pass. In our architecture, adding extra heads increased the number of weights by 7.5%. Thus, a high acceptance rate for draft tokens is important. In the best case, the Medusa model with 20 heads (1 main head and 19 extra heads) produces 21 tokens in 2 model calls.

As a verification procedure, we use one similar to top-p sampling. We sort the predicted probabilities for every token in the vocabulary in descending order and calculate the cumulative

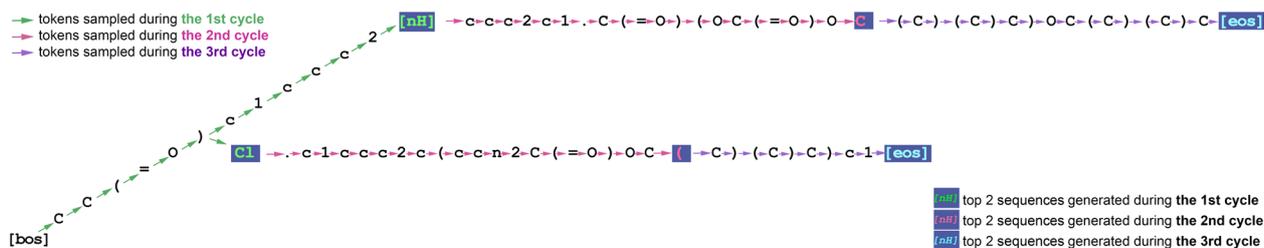
probabilities for every token. If the cumulative probability for a given draft token is less than the nucleus parameter (99.75%), then that token is considered probable enough and approved. Additionally, the highest probability token among all vocabulary tokens is always approved. Fig. 1 and 2 provide an example.

To train the model, we select the "joint training, combined loss" recipe from the original Medusa paper.<sup>28</sup> To give priority to the accuracy of the main head, we divide each head's contribution to the loss function by the number of that head.

When we replace the heuristic drafting in the Molecular Transformer with the Medusa approach, we observe a significant improvement in SBS scalability at larger batch sizes, expanding the potential of speculative decoding and transformer models for fast synthesis planning.

## 2.4 Multi-step synthesis planning

Since the ultimate goal of building accelerated template-free SMILES-to-SMILES prediction models is to enable fast AI-powered CASP, we evaluate our single-step retrosynthesis model as a component of a multi-step synthesis planning system. We choose AiZynthFinder 4.0 (ref. 9 and 27) because of its straightforward support for arbitrary template-free models and to maintain continuity with prior work that benchmarked various single-step retrosynthesis models as the components of



**Fig. 2** A simplified illustration of building top 2 sequences with M-SBS algorithm for the source molecule CC(=O)c1ccc2c(ccn2C(=O)OC(C)(C)C)c1. It requires 6 model calls instead of 52 in classic beam search. M-SBS generates CC(=O)c1ccc2[nH]ccc2c1.C(=O)(OC(=O)OC(C)(C)C)OC(C)(C)C (coincides with the target) and CC(=O)Cl.c1ccc2c(ccn2C(=O)OC(C)(C)C)c1 as the result.



AiZynthFinder.<sup>16</sup> We mostly focus on Retro\* (ref. 15) as the search algorithm for building the synthesis tree. We use only the reactant probability from the single-step model as the guiding probability in tree search, as done by Torren-Peraire *et al.*<sup>16</sup> AiZynthFinder allows constraining the planning by both total time and the maximum number of iterations, and these must be set simultaneously. Therefore, those constraints should be chosen carefully, because ultimately, the strictest of the two is the limiting constraint. In our experiments, we chose either a time limit (assigning a very large maximum number of iterations) or an iteration limit (assigning a very large maximum time). This made it easier to analyze the experiments. AiZynthFinder also features two search modes: either the search stops when at least one route is found, or it continues until the iteration or time limit is reached. When planning is set to build multiple routes until the time limit is reached, the acceleration of the single-step model does not save time; instead, it enables a more thorough exploration of the route space.

It is important to note that AiZynthFinder runs all single-step expansions with a batch size of 1 by design. Therefore, in our multi-step synthesis experiments, the comparison between single-step models is limited to performance at a batch size of 1. Currently, all ML-based open source CASP systems (AiZynthFinder,<sup>27</sup> SynPlanner,<sup>12</sup> Syntheseus,<sup>13</sup> and ASKCOS<sup>11</sup>) support single-step expansions with only a batch size of 1.

## 2.5 Model

We train a custom variant of the Molecular Transformer,<sup>21</sup> an encoder-decoder transformer for SMILES-to-SMILES translation. Our model consists of six encoder and decoder layers, eight heads in the multi-head attention mechanism, an embedding dimensionality of 256, a feedforward dimensionality of 2048, and 20 additional Medusa heads to predict tokens 1–20 positions ahead of the next token. All Medusa heads are implemented as a single MLP with a hidden layer of dimension  $20 \times 50 = 1000$ , followed by a residual connection and layer normalization. The base transformer has 17.4 million parameters, and the Medusa heads have 1.3 million, for a total of 18.7 million. We train a transformer for product prediction to evaluate the round-trip accuracy of the retrosynthesis models. We use the same hyperparameters as in Schwaller *et al.*, with four encoder and decoder layers, eight heads, an embedding dimensionality of 256, and a feedforward dimensionality of 2048, resulting in 11.4 million parameters. We use the Adam<sup>29</sup> optimizer for training. We train and test our models on one NVIDIA Tesla V100 GPU with 32 GB of memory.

## 2.6 Data

For training the single-step retrosynthesis model and its isolated evaluation, we employ the standard USPTO 50K dataset with the same train/validation/test splits as in GLN (ref. 30) (40 008/5001/5007 reactions). We apply the 20-fold R-SMILES augmentation<sup>31</sup> to the USPTO 50K training subset. The test set comprises 5007 reactions; we do not augment it. We follow the standard atomwise tokenization procedure<sup>21</sup> to tokenize SMILES.

For multi-step synthesis planning experiments, we used two sets of building blocks: PaRoutes and ZINC. PaRoutes stock

contains 13 414 molecules designated as purchasable in the PaRoutes-n1 dataset.<sup>10,16</sup> ZINC stock contains 17 422 831 molecules and is available for download through the AiZynthFinder codebase.<sup>32</sup>

# 3 Results and discussion

## 3.1 Single-step retrosynthesis

We first test our models in a single-step retrosynthesis setting using the USPTO 50K dataset. We compare the base transformer with beam search decoding, the base transformer with speculative beam search decoding in a “smart” heuristic drafting variant,<sup>25</sup> and the Medusa variant of the transformer with speculative beam search that relies on draft tokens predicted by the Medusa heads. We denote the first model as T-BS (Transformer + Beam Search), the second as T-HSBS (Transformer + Heuristic Speculative Beam Search), and the latter as M-SBS (Medusa + Speculative Beam Search). We also include a separate “optimized” beam search that does not call the model to predict the pad token after the EOS token. This optimization of the beam search does not affect the accuracy or the number of model calls. However, it reduces the effective batch size, thereby reducing calculation time at larger batch sizes. Since T-HSBS and M-SBS do not call their models to produce the pad token after the EOS token, we outline T-BSO (Transformer + Beam Search (Optimized)) as a separate position to ensure a more accurate comparison. Table 1A provides a schematic that describes the difference between the four decoding variants.

As Table 1B shows, M-SBS significantly outperforms T-BS and T-HSBS at various batch sizes in terms of inference speed. T-HSBS outperforms T-BS and T-BSO at smaller batch sizes but suffers from scalability limitations. Due to the *throughput-latency tradeoff* inherent to processing multiple draft sequences simultaneously, the heuristic drafting scheme requires careful tuning of draft number and length to achieve optimal performance. At larger batch sizes, the computational overhead of processing multiple drafts negates the acceleration benefits, and the optimal number of drafts becomes 1, making T-HSBS similar to M-SBS, as it also uses only one draft. At the same time, M-SBS achieves a higher acceptance rate (Table 1E) through its integrated architecture, maintaining consistent acceleration even at batch size 32, which establishes M-SBS as the superior acceleration approach for single-step retrosynthesis with transformers. M-SBS requires fewer forward passes of the model to complete generation (Table 1C) and achieves an acceptance rate of 91%, leaving T-HSBS far behind.

In terms of accuracy and prediction validity, all three methods demonstrate nearly identical performance (Table 2). While our speculative beam search approach does not guarantee output distributions identical to those of standard beam search, the practical differences are negligible. A slightly larger difference in accuracy and SMILES validity between M-SBS and T-HSBS stems from marginal performance differences across model checkpoints rather than algorithmic effects. M-SBS implies a custom transformer architecture and requires training a separate model, whereas T-HSBS is a drop-in replacement for beam search.



**Table 1** Comparison between the inference algorithms for the single-step retrosynthesis model on the USPTO 50k test set (5K reactions). T-BS is the transformer with beam search, and T-BSO is the transformer with the optimized beam search. "Optimized beam search" means that the finished sequences in a batch are put aside, and the transformer is not called to generate pad tokens after the EOS token (it reduces the average effective batch size). T-HSBS is the transformer with speculative beam search relying on heuristic drafting (source substrings); M-SBS is the Medusa model with speculative beam search. "B" stands for batch size. The number of drafts and the draft length in T-HSBS are individual for every B: 10 drafts of length 10 for B = 1; 3 drafts of length 10 for B = 4; and 1 draft of length 20 for other B (8, 16, 32). Medusa heads always generate 1 draft of length 20. The average time and the standard deviation are estimated based on 5 runs

Beam size 10					
(A) Model description	Architecture	Inference	Drafts	[PAD] generation optimized	
T-BS	Transformer	Beam search	—	No	
T-BSO	Transformer	Beam search	—	Yes	
T-HSBS	Transformer	Speculative beam search	Src. SMILES substrings	Yes	
M-SBS	Medusa	Speculative beam search	One learnable draft	Yes	
(B) Decoding wall time, min	B = 1	B = 4	B = 8	B = 16	B = 32
T-BS	50.0 ± 3.8	26.9 ± 3.5	18.7 ± 1.2	14.9 ± 0.1	16.2 ± 0.1
T-BSO	50.0 ± 2.2	16.2 ± 0.3	9.4 ± 0.2	7.3 ± 0.1	5.5 ± 0.1
T-HSBS	22.7 ± 1.3	10.1 ± 0.2	7.4 ± 0.2	6.1 ± 0.1	5.2 ± 0.0
M-SBS	11.4 ± 0.4	4.0 ± 0.2	2.4 ± 0.2	2.1 ± 0.1	1.5 ± 0.1
(C) Model calls	B = 1	B = 4	B = 8	B = 16	B = 32
T-BS	295 947	99 030	54 934	29 941	16 170
T-BSO	295 947	99 030	54 934	29 941	16 170
T-HSBS	92 538	36 960	28 056	15 807	8817
M-SBS	59 502	19 240	10 730	5906	3224
(D) Average effective batch size	B = 1	B = 4	B = 8	B = 16	B = 32
T-BS	10	40	80	160	320
T-BSO	8	25	45	82	151
T-HSBS	23	40	29	52	93
M-SBS	6	18	32	58	105
(E) Acceptance rate, %	B = 1	B = 4	B = 8	B = 16	B = 32
T-HSBS	74	70	64	64	64
M-SBS	91	91	91	91	91

**Table 2** The top-N accuracy of our model in single-step retrosynthesis on USPTO 50K and the proportion of invalid SMILES in the N-th prediction with different decoding strategies: beam search (T-BS/T-BSO), speculative beam search with heuristic drafting strategy (T-HSBS), speculative beam search with Medusa heads for drafting (M-SBS). The difference in accuracy between all decoding methods is negligible

Single-step retrosynthesis		Top-1	Top-3	Top-5	Top-10
Accuracy, %	T-BS/T-BSO	52.08	75.16	82.97	89.08
	T-HSBS	52.08	75.16	82.07	89.12
	M-SBS	54.06	75.95	82.90	89.20
Invalid SMILES, %		<b>Pred. 1</b>	<b>Pred. 3</b>	<b>Pred. 5</b>	<b>Pred. 10</b>
	T-BS/T-BSO	0.8	1.8	3.5	8.1
	T-HSBS	0.8	1.8	3.5	8.2
	M-SBS	0.5	1.7	3.1	9.3



### 3.2 Multi-step retrosynthesis

We incorporated our single-step retrosynthesis models into AiZynthFinder to test their performance in multi-step synthesis planning. Since M-SBS consistently outperforms T-HSBS in terms of the speed of single-step prediction generation, we decided to compare M-SBS only with the standard Transformer + Optimized Beam Search (T-BSO) in multi-step synthesis planning. We will further refer to M-SBS as “Medusa” and to T-BSO as “Transformer”. We selected Caspyrus10k as the benchmark dataset for multi-step synthesis planning, drawing inspiration from the experiments of Torren-Peraire *et al.*<sup>16</sup>

**3.2.1 Synthesis planning constrained by time.** To compare Transformer and Medusa in synthesis planning on Caspyrus10k, we adjusted the original methodology of Torren-Peraire *et al.* to prioritize inference speed, assuming that chemists would not wait for hours for computation to complete, and constrained the multi-step synthesis to either solve a query molecule within several seconds or consider it unsolved. Solving a molecule means building a synthesis tree in which all leaf nodes are building blocks, *i.e.*, molecules that are assumed to be available. Here, we use the PaRoutes stock (13 414 molecules) or the ZINC stock (17 422 831 molecules). We set the models to generate 10 candidate precursor sets with every call of a single-step model, constrained the maximum route length to 5 or 7, and the maximum number of algorithm iterations to 35 000 (enough to ensure the priority of the time constraint). When the algorithm identifies the first route from a query molecule to the building blocks, it stops, and the molecule is considered solved. Table 3 summarizes the results of our multi-step retrosynthesis experiments under the time constraints of 5 and 15 seconds for solving a molecule. The results reveal that Medusa consistently outperforms Transformer across all experimental conditions, with improvements in both the number of solved molecules and computational efficiency.

The iteration of the planning algorithm (Retro\* or DFPN search) is accelerated with Medusa by approximately 3 times, which results from the acceleration of the single-step model by approximately 4 times (Table 1B). Due to the different number of the planning algorithm iterations, the first route is identified by Medusa approximately 2 times faster. It leads to the increase of success rate under the stringent time limit. When using DFPN search with a 5 second limit, Medusa solves 2080 molecules out of 10 000, which is 86% more compared to the 1117 solved by Transformer. For the 1017 molecules that both methods successfully solve, Medusa requires on average less than half the time (0.86 seconds *vs.* 1.88 seconds) (Table 3A). With the Retro\* algorithm, Medusa maintains its advantage, solving 36% more molecules than Transformer within 5 seconds (5287 *vs.* 3890, Table 3B) and 26% more within 15 seconds (6715 *vs.* 5341, Table 3C). When using the ZINC stock with a depth limit of 5 and a 15 second time limit (Table 3D), Medusa solves 8343 molecules compared to 7708 for the Transformer, while also reducing the average solution time (1.73 s *vs.* 3.21 s). Finally, with ZINC and the depth limit increased to 7 (Table 3E), Medusa solves 8608 molecules *versus* 7888 for the Transformer and maintains a lower average

solution time (1.89 s *vs.* 3.37 s). Across all conditions, Medusa consistently achieves faster average solution times while solving substantially more molecules.

Interestingly, Medusa required more algorithm iterations per commonly solved molecule than Transformer. This likely reflects differences in probability distributions: Transformer tends to concentrate probability mass on the top candidate, while Medusa produces more smooth distributions across candidates, leading to more exploratory search behavior. Fig. 3 shows that the top-1 probability of Medusa is lower than that of the Transformer. The effect is small, but it is noticeable. Similarly, the number of commonly solved molecules under different parameter settings (Table 3) never coincides with the Transformer's number of solved molecules, indicating that Medusa produces a slightly different probability distribution.

**3.2.2 Synthesis planning constrained by iteration number.** To compare our model's performance within AiZynthFinder's planning system with the single-step models compared by Torren-Peraire *et al.*, namely LocalRetro,<sup>35</sup> Chemformer<sup>23</sup> and the default template-based single-step model available in AiZynthFinder, we set the same parameters for the multi-step retrosynthesis search: the maximum route depth of 7, the beam size of 50, ZINC stock (consisting of 17 422 831 molecules) of building blocks, Retro\* as a search algorithm, and the maximum number of algorithm iterations per molecule of 200. Since we conducted our experiments on a GPU (Tesla V100 32 GB), we set the time limit to 3 minutes instead of the original 480 minutes, which is enough for Transformer and Medusa to be limited only by the iteration limit, and not the time limit, in the case of a complex input molecule. We also use the setting in which the search is stopped as soon as at least one route for a given molecule is found. It does not affect the success rate (the number of molecules for which a full synthesis route is found), but it speeds up experiments by avoiding the calculation of all 200 Retro\* iterations. According to Table 6, Transformer, a model of 17 million parameters, is sufficient to achieve a high percentage of successfully solved molecules, approaching 100%. With the limit of 200 iterations, Transformer reaches 97.13% of solved molecules, spending 0.67 seconds per Retro\* iteration, while Medusa achieves 95.90% of solved molecules, spending 2 times less, only 0.31 seconds per iteration. This means that if Transformer ran for all 200 iterations, as in the experiments of Torren-Peraire *et al.*,<sup>16</sup> it would spend about 134 seconds per molecule and about 372 hours on the entire dataset. Meanwhile, for Medusa, these values would be 62 seconds and 172 hours, respectively. Thus, Medusa would save approximately 200 hours of GPU calculations while maintaining a 95.9% solved-molecule rate.

We compared the multistep success rate of the models with their round-trip accuracy, diversity, and percentage of invalid SMILES (Table 4). Instead of the relative round-trip accuracy, we calculated the number of round-trip feasible reactions, *i.e.*, predicted reactions that lead to the initial target molecule when evaluated with the Molecular Transformer forward model in top-10 mode. Diversity is measured as the number of unique reaction names, assigned by Rxn-INSIGHT.<sup>34</sup> For comparison, we took the default template-based single-step model from AiZynthFinder 4.0. Despite the template-based model (42 554



**Table 3** The comparison between the Transformer and Medusa as a single-step retrosynthesis models within AiZynthFinder on Caspyrus10k under different search algorithms and time limits per molecule. Beam size is 10. Depth-First Proof-Number<sup>33</sup> (DFPN) (A) and Retro\* (B–E) are search algorithms (referred as “alg.”) that build the synthesis tree. PaRoutes stock (13 414 molecules) (A–C) or ZINC stock (D and E) is used as a building block set. The maximum synthesis route length is 5 (A–C and D) or 7 (E). The search is stopped when at least one route for a given molecule is found

(A) DFPN, PaRoutes stock, depth 5; time limit 5 seconds	Transformer	Medusa
Solved molecules	1117	2080
Common solved molecules		1017
Avg. time per solved molecule, sec	2.01	1.85
Statistics on common solved molecules:		
Avg. time per molecule, sec	1.88	0.86 (×2.)
Avg. alg. iterations per molecule	6.52	9.51
Avg. alg. iteration time, sec per iteration	0.34	0.10 (×3.)
(B) Retro*, PaRoutes stock, depth 5; time limit 5 seconds	Transformer	Medusa
Solved molecules	3890	5287
Common solved molecules		3628
Avg. time per solved molecule, sec	2.14	1.41
Statistics on common solved molecules:		
Avg. time per molecule, sec	2.06	0.99 (×2.)
Avg. alg. iterations per molecule	5.51	7.38
Avg. alg. iteration time, sec per iteration	0.43	0.16 (×3.)
(C) Retro*, PaRoutes stock, depth 5; time limit 15 seconds	Transformer	Medusa
Solved molecules	5341	6715
Common solved molecules		5050
Avg. time per solved molecule, sec	4.25	2.86
Statistics on common solved molecules:		
Avg. time per molecule, sec	4.00	1.84 (×2.)
Avg. alg. iterations per molecule	12.44	18.99
Avg. alg. iteration time, sec per iteration	0.44	0.14 (×3.)
(D) Retro*, ZINC stock, depth 5; time limit 15 seconds	Transformer	Medusa
Solved molecules	7708	8343
Common solved molecules		7439
Avg. time per solved molecule, sec	3.21	1.73
Statistics on common solved molecules:		
Avg. time per molecule, sec	3.06	1.26 (×2.)
Avg. alg. iterations per molecule	6.15	10.13
Avg. alg. iteration time, sec/iteration	0.60	0.16 (×4.)
(E) Retro*, ZINC stock, depth 7; time limit 15 seconds	Transformer	Medusa
Solved molecules	7888	8608
Common solved molecules		7666
Avg. time per solved molecule, sec	3.37	1.89
Statistics on common solved molecules:		
Avg. time per molecule, sec	3.23	1.41 (×2.)
Avg. alg. iterations per molecule	6.5	9.5
Avg. alg. iteration time, sec/iteration	0.61	0.19 (×3.)

templates in total) offering 50 templates at a time, some templates cannot be applied, some predictions are filtered out by the default neural filter, and duplicate predictions also occur. As a result, the model, on average, offers only 15 reactions per target molecule during testing. The model runs on a CPU. We assigned it a longer time limit of 5 hours per molecule to ensure the programs' running times would be comparable. It increased the success rate from 72.6% to 82.6%.

According to all the single-step metrics, Transformer and Medusa are very similar. As we trained our models on data without reagents, they achieved relatively low round-trip accuracies of 62.8% and 63.0%, respectively (considering beam size 10 mode). These numbers are close to the template-based model's round-trip accuracy of 62.3%. One can see that in the 3 minutes per molecule time constraint, Medusa speeds up the program by 1.4×. In the iteration constraint, the 4.4×



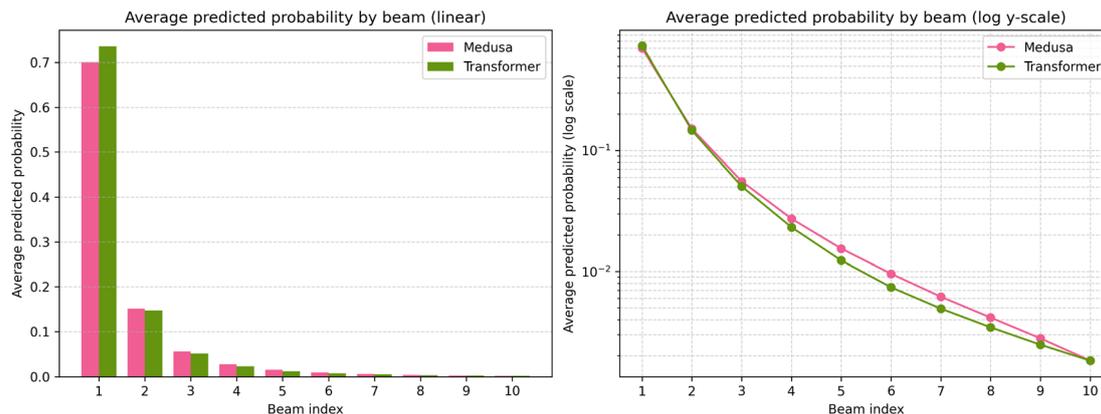


Fig. 3 Average predicted probabilities of the top-10 sequences generated by Transformer (T-BSO) and Medusa (M-SBS) for every input in the USPTO 50k test set. The probabilities of Medusa outputs are slightly smoother than those of the Transformer.

acceleration of the single-step model and, as a result, faster multi-step iteration, leads to  $1.7\times$  and  $2.9\times$  acceleration of the entire program.

**3.2.3 PaRoutes-n1 evaluation.** To evaluate the multi-step retrosynthesis performance of our models, we used the PaRoutes-n1 (ref. 10) benchmark, which is designed to assess the ability of retrosynthesis planners to recover predefined reference routes given a fixed stock of building blocks.

The PaRoutes-n1 dataset contains 10 000 target molecules, each associated with a single reference synthesis route and a predefined stock of building blocks. From this dataset, we randomly selected 1000 target molecules for evaluation. The search configuration provided with the PaRoutes benchmark was used without modification. Both models successfully completed the full 500-iteration search procedure for all evaluated targets.

The results of this experiment are summarized in Table 5. During the search, we collected up to 50 solved synthesis routes per target molecule. Both models demonstrated a high overall solvability, defined as the fraction of targets for which at least one valid synthesis route was found. Medusa solved 937 molecules (93.7%), while the Transformer solved 941 molecules (94.1%). To assess the models' ability to reproduce the reference routes provided in PaRoutes, we evaluated route accuracy, defined as the fraction of targets for which the exact reference route appears among the top-50 predicted synthesis routes. Medusa successfully recovered the reference route for 276 molecules (27.6%) and completed the evaluation in 10 hours. The Transformer recovered the reference route for 286 molecules (28.6%) and required 24 hours of computation. Again, Medusa maintains the Transformer's performance while being significantly faster.

Table 4 Connection between number of beams, multistep success rate of transformer-like models, and their single-step metrics, namely round-trip accuracy, diversity, and percentage of invalid SMILES. The multistep experiments are conducted using AiZynthFinder on Caspyrus10k with the Retro\* search algorithm; ZINC stock (17 422 831 molecules) is used as building blocks; the search is stopped when at least one route for a given molecule is found. Maximum synthesis route length is 7. Transformer stands for transformer with beam search, which produces pad-token after EOS-token automatically without extra calls. Medusa is a Transformer-like model that uses speculative beam search with Medusa heads as draft source. These models run on a GPU. AZF stands for the AiZynthFinder 4.0 default single-step model with a cumulative probability of 99.5% in combination with top-50; it runs on 55 CPU processes in parallel. The multi-step experiments are conducted with a limit of 200 iterations of the planning algorithm and a time limit of 3 minutes (in the case of AZF model, 5 hours per molecule, due to its fast operation). The single-step metrics are measured on the USPTO 50k test set. Eff. N stands for the number of valid reaction SMILES without repetitions. R.-t. (round-trip) feasible reactions stands for the number of reactions that lead to the initial target molecule when evaluated with the Molecular Transformer forward model in top-10 mode. The diversity counts the number of unique reaction names, classified by Rxn-INSIGHT.<sup>34</sup>

Model	Multistep				Single-step, average per target molecule			
	Top N	Limit	Success rate, %	Total time, h	Invalid SMILES, %	Eff. N	R.-t. feasible reactions	Diversity, classes
Transformer	10	200 it	89.49	29.57	4.03	9.2	5.8	5.77
		180 s	94.08	58.27				
Transformer	50	200 it	97.13	26.42	13.98	39.6	18.5	13.57
		180 s	94.90	41.32				
Medusa	10	200 it	87.90	10.32	4.07	9.4	5.9	5.80
		180 s	94.90	41.32				
Medusa	50	200 it	95.90	15.42	15.22	39.9	18.5	13.43
		180 s	94.90	41.32				
AZF (template-based)	50	200 it	72.63	2.73	0	15.1	9.4	7.87
		5 h	82.60	24.01				



**Table 5** Evaluation performed on 1000 randomly selected targets from the PaRoutes-n1 dataset. For each target, up to 50 synthesis routes were collected during 500 search iterations. Route accuracy is expressed as the absolute number of targets for which the corresponding model retrieved the reference route among the top-50 predicted routes. Building-block accuracy is calculated for molecules solved only by the rival model using the route accuracy metric and is expressed as the number of molecules for which the corresponding model predicted the reference set of building blocks

Model	Success rate, %	Route accuracy	Route accuracy overlap	Building block accuracy on unsolved molecules	Runtime, h
Transformer	94.1	286	248	8/28	24
Medusa	93.7	276		22/38	10

The sets of molecules solved by both Transformer and Medusa do not fully overlap. Among the molecules for which the reference route was recovered, 248 targets were common to both models. Therefore, Transformer solved 38 molecules that Medusa did not solve, while Medusa solved 28 molecules that Transformer did not solve. This observation is consistent with our earlier results (e.g., Table 3) and indicates that the two models explore different regions of the retrosynthetic solution space, despite achieving similar overall performance. For the 38 molecules solved only by the Transformer, Medusa generated routes with exactly matching reference building block sets for 22 molecules, indicating that it was often close to recovering the correct route topology. Conversely, among the 28 molecules solved only by Medusa, the Transformer produced routes with matching building block sets for 8 molecules.

These observations suggest that even when the exact reference route is not recovered, the models frequently identify chemically consistent precursor sets, reflecting partial convergence toward the reference synthesis strategy.

### 3.3 Limitations

Similar to the paper by Torren-Peraire *et al.*,<sup>16</sup> we focus here solely on the speed of building the retrosynthetic graph. However, Aizynthfinder also spends a significant amount of

time splitting the tree into separate routes. The more model calls are made within the time limit, the more nodes are added to the retrosynthesis tree, and the more complex the tree becomes for splitting. We alleviated this problem by allowing AiZynthFinder to extract only the successful routes in which all leaves are building blocks. This approach requires only a small fraction of the time required for the exhaustive process of extracting all retrosynthetic routes in AiZynthFinder. In cases where unsolved routes are required, the tree-splitting algorithm can be easily optimized by first extracting the most probable reactions rather than making a random choice of unsolved reactions, and by decreasing the maximum route number limit.

Table 4 shows that the round-trip accuracy of Transformer rapidly decreases from 63%  $\left(\frac{5.8}{9.2}\right)$  to 47%  $\left(\frac{18.5}{39.6}\right)$  when going from top-10 to top-50, although the success rate is noticeably improved from 90% to 97% (with Medusa showing similar behavior). We attribute this to the fact that the quality of the beams decreases with an increase in their number, and the template-free models sometimes return short answers, *i.e.*, SMILES that are valid but meaningless, for instance, “Cl” as a single precursor for “ClC1csc(-c2ccccc2)n1”. At the same time, the metrics show that after the tenth beam, valuable predictions are generated (the absolute number of round-trip feasible reactions is larger in the top-50 than in the top-10), but they are mixed with low-quality predictions that need to be filtered out. Although it is easy to filter out invalid reactions or those that contain the product itself among the reactants, short answers are more difficult to filter out. The default neural filter of AizynthFinder 4.0 defines “Cl  $\gg$  ClC1csc(-c2ccccc2)n1” as a feasible reaction with 99.95% probability. The round-trip filter successfully recognizes this case, but it is heavy and also may erroneously filter out reactions written with missing reagents. Generating reactions with reagents would, in turn, reduce the diversity of autoregressively generated reactions and, consequently, the diversity of routes. Thus, it is necessary to find an elusive balance between all these factors. It may be useful to combine heuristic filters of nonsensical reactions with transformer models in order to avoid formally solved, but in fact incomplete routes.

Currently, AiZynthFinder and its alternatives do not readily support batch sizes other than one for single-step retrosynthesis models in multi-step synthesis planning. Our future work will focus on generalizing multi-step synthesis planning algorithms

**Table 6** The comparison between different single-step inference methods within AiZynthFinder on Caspyrus10k under the Retro\* search algorithm with iteration limit 200 per molecule. ZINC stock (17 422 831 molecules) is used as building blocks. Beam size is 50. Maximum synthesis route length is 7. Transformer stands for transformer with beam search, which produces pad-token after EOS-token automatically without extra calls. Medusa is a Transformer-like model that uses speculative beam search with Medusa heads as draft source. AZF stands for AiZynthFinder single-step model. Av. Retro\* iter. time represents the average time of a single Retro\* iteration. GPU stands for Tesla V100 32 GB. CPU experiments data is taken from ref. 16

Model	Time limit per molecule, min	Success rate, %	Av. Retro* iter. time, s	Device
Transformer	3	97.1	0.67	GPU
Medusa		95.9	<b>0.31</b>	
Local Retro <sup>16</sup>	480	74.1	0.81	CPU
Chemformer <sup>16</sup>		62.4	107.63	
AZF <sup>16</sup>		41.1	0.80	



to support larger batch sizes, which should further reduce the latency in CASP systems, considering the significant speed benefits of Medusa at larger batch sizes.

## 4 Conclusions

We demonstrate that a Medusa variant of the Transformer combined with speculative beam search offers significant speed advantage in multi-step synthesis planning in AiZynthFinder compared to the usual combination of SMILES-to-SMILES Transformer and beam search while retaining the same level of accuracy. In isolated single-step retrosynthesis experiments, Medusa and SBS accelerate the generation of 10 expansions per query by approximately 4 times across batch sizes from 1 to 32 without compromising the accuracy of the baseline Transformer. When Transformer is compared against Medusa in multi-step synthesis planning in AiZynthFinder under stringent time constraints, Medusa allows a single iteration of the planning algorithm to run approximately 3 times faster across varying time limits, search algorithms, and building blocks, enabling AiZynthFinder to solve significantly more molecules under the same time constraints compared to the Transformer. When the multi-step search is constrained by a maximum number of iterations instead of maximum time, the search with Medusa completes much faster than with Transformer, saving dozens of hours of compute while demonstrating negligible discrepancy in solvability and route accuracy. Our approach presents a promising alternative for SMILES-to-SMILES transformers in synthesis planning when planning speed is critical and brings the speed of AI-based CASP closer to the level required for high-throughput synthesizability screening in pharmaceutical research.

## Author contributions

MA and NA conceptualized the paper idea. NA and MA wrote the code and conducted the experiments. MA and NA wrote the manuscript with inputs from all co-authors. JS, DC, and MW acquired the research funding, administered the project, and provided supervision.

## Conflicts of interest

There are no conflicts to declare.

## Data availability

The instructions for downloading the data and running the code to replicate the results are at <https://github.com/Academich/faster-ml-casp> and <https://doi.org/10.5281/zenodo.18002214>.

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