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Statistics makes a difference: machine learning adsorption dynamics of functionalized cyclooctyne on Si(001) at DFT accuracy

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The interpretation of experiments on reactive semiconductor surfaces requires statistically significant sampling of configurational space by molecular dynamics, but conventional *ab initio* methods are limited due to prohibitive computational costs. Machine-learning interatomic potentials provide a promising solution, bridging the gap between the chemical accuracy of short *ab initio* molecular dynamics (AIMD) and the extensive sampling required to simulate experiment. Using ethynyl-functionalized cyclooctyne adsorption on Si(001) as a model system, we demonstrate that conventional AIMD undersamples the configurational space, resulting in discrepancies with scanning tunnelling microscopy and X-ray photoelectron spectroscopy data. To resolve these inconsistencies, we employ pre-trained equivariant message-passing neural networks, fine-tuned on only a few thousand AIMD snapshots, and integrate them into a “molecular-gun” workflow. This approach generates 10 000 independent trajectories more than 1000 times faster than AIMD. These simulations recover rare intermediates, clarify the competition between adsorption motifs, and reproduce the experimentally dominant on-top [2 + 2] cycloaddition structure. Our results show that fine-tuning of pre-trained foundational models enables statistically converged, chemically accurate simulations of bond-forming and bond-breaking events on complex surfaces, providing a scalable route to reconcile atomistic theory with experimental ensemble measurements in semiconductor functionalization.

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1 Introduction

The functionalization of semiconductor surfaces, particularly silicon, offers a versatile means to tailor electronic, chemical, and mechanical properties.^{1–4} Cyclooctynes, widely used in strain-promoted click chemistry,^{5–11} serve as selective and reactive agents for Si(001) functionalization, enabling mild, covalent attachment while minimizing side reactions.^{7–9,12–19} Surface-sensitive experimental techniques such as scanning tunneling microscopy (STM) or X-ray photoelectron spectroscopy (XPS) provide rich detail on adsorption structures, coverage, and side reactions,¹⁹ yet they lack the temporal and atomistic resolution needed to observe transient intermediates and adsorption pathways required to resolve reaction kinetics. Moreover, ensemble-averaged spectroscopies yield information on overall surface composition and functional group identity, but fail to resolve site-specific energetics or orientation distributions. As a result, critical details, including the relative

barriers for adsorption on the two non-equivalent dangling bonds of the Si(001) dimer (see Fig. 1), the influence of subsurface strain on cyclooctyne ring opening, and the lifetimes of metastable precursors, remain experimentally inaccessible.

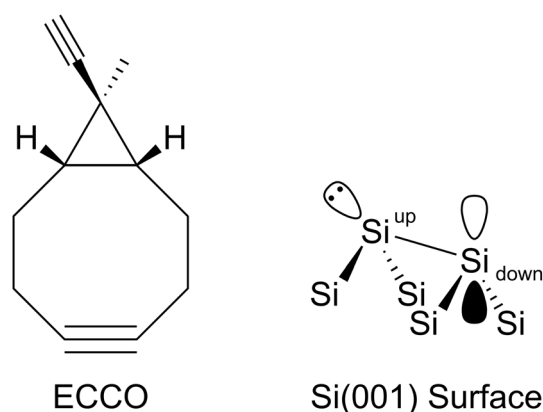


Fig. 1 Left: Lewis structure of 9-ethynyl-9-methylbicyclo[6.1.0]non-4-in (ECCO). Right: Reconstructed Si(001) surface, where Si-dimers are formed on the surface consisting of Si_{up} and Si_{down} atoms. The dimer can be described as a Si_{up} atom with a lone pair and a partial negative charge, whereas the Si_{down} can be described as carrying an empty p-orbital.

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Computational approaches can complement experiment, but rely on computationally costly quantum-chemical calculations. As a consequence, studies are often limited to static analyses using density functional theory (DFT), which is usually the workhorse of such simulations.^{20,21} However, for capturing reaction kinetics and dynamical processes, molecular dynamics (MD) simulations are needed. Classical force fields, which offer a computationally viable solution, lack the ability to describe covalent bond formation and breaking. For some specific systems, reactive Force Fields (ReaxFF^{22,23}) have been used in surface chemical studies. However, for statistically relevant sampling, these methods are also too demanding.^{24–27} *Ab initio* molecular dynamics (AIMD), in principle, offers both reactivity and accuracy, yet its computational cost severely limits accessible timescales and statistical sampling.^{13,28–31} Recent work on ethynyl-functionalized cyclooctyne (ECCO, see Fig. 1) adsorption at Si(001) surfaces revealed a bottleneck: AIMD trajectories, even tens of picoseconds in length, can miss key binding modes observed experimentally, leading to discrepancies in predicted *versus* measured dominant adsorption geometries.^{19,32} Whether such mismatches stem from methodological limitations or from simple undersampling remains an open and critical question.

To address this question, we leverage machine learning (ML) to vastly accelerate surface MD simulations without compromising *ab initio* accuracy. Specifically, we fine-tune the foundational equivariant, message-passing atomic cluster expansion (MACE) model,^{33,34} MACE-MP-0, using our previous AIMD data for ECCO/Si(001),³² deploying a “molecular gun” strategy that generates thousands of statistically independent trajectories in a black-box fashion to simulate ultra-high-vacuum experiments (UHV) (for details see 2.1).

Therefore, simulations at near-DFT accuracy become accessible, while being multiple orders of magnitude faster.³⁵ While the MACE-MP-0 architecture is widely adopted across molecular and materials applications,^{36–58} its suitability for surface fine-tuning with limited data,^{59–67} as demonstrated here, presents a practical solution to statistical convergence issues in surface chemistry.^{68–70}

By fine-tuning a pre-trained MACE-MP-0 model³⁴ with targeted ECCO/Si(001) AIMD snapshots,³² we remove the sampling bottleneck, enabling large-scale, chemically accurate simulations at affordable computational cost. Our machine learning molecular gun allows for detailed analysis of binding-site populations, desorption barriers, and ring-opening dynamics, placing the atomistic mechanism of ECCO adsorption in direct, quantitative correspondence with STM and XPS data.¹⁹

2 Computational details

To conduct ML-accelerated AIMD, we use the foundational MACE model for materials, MACE-MP-0,³⁴ and fine-tune it on data obtained by some of us in a recent study.³² We therefore only briefly summarise the quantum-chemical reference simulations and the model architecture, referring to the cited publications for full details.

2.1 AIMD reference simulations

The *ab initio* data for training were taken from previous work^{32,71} using DFT-based MD. Trajectories were generated using VASP 5.4.4,^{72–76} using the exchange–correlation functional by Perdew, Burke, and Ernzerhof (PBE)^{77,78} with the DFT-D3(BJ) dispersion correction scheme.^{79,80} The simulations were designed to model UHV deposition experiments, in which evaporated molecules impinge on a surface with finite kinetic energy. We therefore refer to this approach as the “molecular gun”. In this protocol, the Si(001) slab (Table S3 and Fig. S10) and the ECCO molecule were first equilibrated separately for 40 ps at 300 K in the NVT ensemble. From these trajectories, a configuration (coordinates and velocities) was extracted every 1 ps to sample thermally excited states of both subsystems. Ten such configurations served as initial states for subsequent MD runs, in which the molecule was accelerated towards the surface by adding a random downward and random $\pm x$ and $\pm y$ velocity component, mimicking the conditions of UHV deposition. The x and y contribution accounts for incoming angles in a randomised fashion. The velocity is rescaled to match 300 K before adding it to the molecule. We use this same strategy in our work to generate additional initial conditions and improve statistical sampling.

In the reference data, dynamics were simulated in the NVT ensemble using a Nosé–Hoover thermostat^{81–83} at 300 K with a Nosé mass of 1.8.³²

The complete AIMD dataset comprises approximately 327k frames: formed from ~ 199 k frames of the ECCO molecule and ~ 128 k frames of molecular gun runs (ECCO + Si(001)).⁷¹ All frames in which unphysical C–H bond fission occurred were removed, which was concluded to be the result of a too large time step in the underlying DFT data, surpassing the barrier that would be expected for the C–H fission. This was the case in two of the 10 AIMD trajectories.³² After randomising the remaining frames, every 25th configuration was selected to form the production machine learning dataset (coordinates, velocities, and energies), resulting in ~ 13 000 data points of ECCO on Si(001). As shown previously, only a fraction of all trajectories is enough to achieve good training results.^{84,85}

2.2 Machine learning MD

All MD simulations in this work were performed using the MD driver implemented in the atomic simulation environment (ASE).⁸⁶ As initial configurations, we used the ten starting structures from the reference AIMD simulations,³² providing pre-equilibrated systems (see also Subsection 2.1). For each run, the position of the ECCO molecule in the x – y plane (parallel to the surface) was randomised. The distance between the surface atom plane and the ECCO centre of mass was fixed at 20 Å, corresponding to an approximate shortest atom–surface separation of 13 Å. To initiate motion towards the slab, a random velocity component was added to the initial DFT velocities of the ECCO molecule along the z -axis. The velocities of the slab atoms were kept unchanged from the AIMD frames. The simulations were propagated with a time



step of 0.5 fs for 20 000 iterations, corresponding to a total simulation time of 10 ps. An NVE ensemble was employed,⁸⁷ as the systems were pre-equilibrated at the target temperature in the DFT stage and the experimental surface-deposition process is intrinsically non-equilibrium.

2.3 Machine learning

For machine learning, we employ the foundational messaging passing atomic cluster expansion (MACE)³³ model, MACE-MP-0,³⁴ which was originally trained on the Materials Project Trajectory (MPtrj) dataset.⁸⁸ This dataset contains approximately 1.5 million configurations, primarily small periodic unit cells representing inorganic crystals with some molecular components.³⁴ Notably, the MPtrj dataset contains limited surface-chemistry data, motivating the fine-tuning of MACE-MP-0 for improved data efficiency. Our fine-tuning approach assumes that knowledge gained from a large and diverse dataset of materials facilitates learning for new systems. Accordingly, the parameters of MACE-MP-0 were used to initialise the training of fine-tuned models. The model representation comprises of 128 scalar and 128 vectorial components. Fine-tuning was performed with a learning rate of 0.001 for 100 epochs to prevent overfitting, re-initialising the readout layers.⁸⁹ Training employed a batch size of 16 across 8 NVIDIA A100-SXM4GPUs. A weighting factor of 1 : 100 between energies and forces was applied during training in the loss function, where both contributions were computed using the mean squared error (MSE). The MSE of the energies was weighted by 1, and the MSE of the forces was weighted by 100, reflecting the greater importance of forces for MD simulations. Because of this weighting, the energies are considered less reliable in this work and only the forces are used to represent the correct dynamic behavior. Five percent of the 13k points are used for validation and 10k randomly selected structures from the total data points (excluding the 13k points used for training) are used for testing. All other architectural parameters were kept at their default values, matching those of the foundational MACE-MP-0 model.⁸⁹ A fixed random seed of 24 was used for reproducibility. For comparison, we also trained MACE models from scratch using the same setup as the fine-tuned models, except for an increased training length of 1000 epochs.

2.4 MD analysis

Trajectory analysis was performed using ASE modules.^{86,90} We further used an automated detection method for adsorption sites and modes. Structure visualizations were rendered using Blender⁹¹ *via* our ASE-Blender interface.⁹² To evaluate the sampling density of the space above the Si(001) surface, a binning approach was conducted using NumPy v2.3.⁹³ An *xy*-grid was created and, for each *xy* bin in the unit cell, the lowest occurring *z*-value of the centre of the cyclooctyne triple bond was stored for the respective set of trajectories. The spacing of the *xy* bins was set to one thousandth of the unit cell, corresponding to an area of 0.0015 Å² per bin.

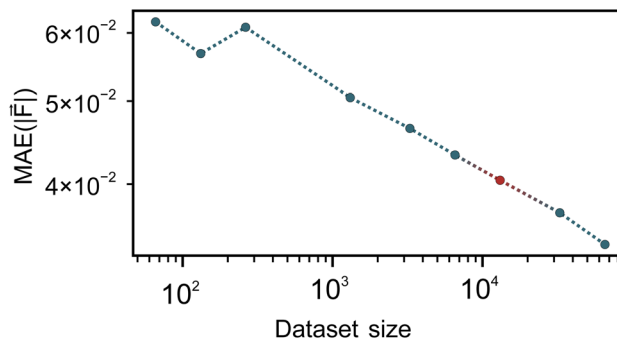


Fig. 2 Learning curve of the fine-tuned models showing the mean absolute error (MAE) of forces (\bar{F}) plotted against the dataset size in logarithmic scale. The production dataset is marked in red, at 13 000 data points.

3 Results and discussion

3.1 Machine learning

To ensure accurate machine learning interatomic potentials, we analysed the learning and training data distribution using learning curves and dimensionality reduction techniques, respectively.

The learning curves for our fine-tuned models (Fig. 2) plot the force mean absolute error (MAE) on an independent test set, with respect to the DFT reference, against the number of training geometries on a log-log scale. The observed decay of the MAE is clearly linear, demonstrating that the fine-tuned model continues to benefit systematically from additional data. The energy and force errors for varying training set sizes are presented in detail for all models in Table S1 of the SI. Fine-tuning generally requires fewer epochs and, consequently, less training time than training models from scratch on the ECCO on Si(001) system (see also Table 1). Both models achieve lower errors than the non-fine-tuned foundational model. This is expected as the foundational model does not have knowledge on the data and is also trained on another reference method. Additionally, we find that models trained from scratch on our AIMD data achieve lower errors than the fine-tuned versions from the foundational model (1.75×10^{-3} eV and 2.97×10^{-2} eV Å⁻¹ for energies and forces, respectively, compared to MAEs of 2.73×10^{-3} eV and 4.04×10^{-2} eV Å⁻¹ for the fine-

Table 1 Computational time comparison of DFT and machine learning MDs. DFT values are extrapolated from one trajectory. One MD run consists of 20 000 time steps. All timings in CPUh/GPUh, respectively. Training was performed on 8 GPUs and takes 1.1 h for fine-tuned models and 6.6 h for models trained from scratch

Method	Full MD ^a	1 MD step	1000 MDs
DFT ^b	7.1×10^4	3.6	7.1×10^7
ML ^c	4.3	2.2×10^{-4}	4.4×10^3
ML ^d	1.0×10^{-1}	5.0×10^{-6}	1.0×10^2

^a 20,000 steps, extrapolated from 14 933 steps for DFT-MD. ^b CPU: 20 Intel Haswell E5-2680v3 = 240 cores total. ^c CPU: 1 AMD EPYC CPU 9334 = 1 core. ^d GPU: NVIDIA H100-SXM5.



tuned models). This counter-intuitive result likely stems from differences between the MPtrj data and our target domain. The MPtrj dataset spans a much broader chemical space, containing bonding motifs and structures not directly relevant to our system. Fine-tuning adapts the model to our trajectories, but it begins from parameter values optimized for generalization across the MPtrj dataset. These values turn out to be less suitable for the narrower Si–C–H surface chemistry under study, compared with random initialization when training from scratch. Using a larger learning rate with a decay schedule may help the fine-tuned model escape the local minima associated with the pre-training, potentially achieving errors comparable to the model trained from scratch. In practice, this involves starting with a relatively high initial learning rate followed by exponential decay, where the learning rate is reduced after several epochs without improvement. However, this may come at the cost of losing much of the information gained from the MPtrj dataset. That said, it is important to note that a direct comparison of error metrics is not a good measure for evaluating performance in MD simulations. Machine learning potentials are, in essence, interpolators, and because the test set is drawn from the same underlying DFT trajectories as the training set, it contains very similar configurations. These metrics therefore do not reflect how the model behaves on new trajectories that sample regions of configuration space not well represented in the training data. For test set error metrics to more accurately reflect MD performance, a much more comprehensive set of reference configurations would be required, ideally covering the full space of potential trajectories. However, obtaining such coverage would require many expensive DFT trajectories and is therefore not practical. Nevertheless, the key advantage of fine-tuned models is that they retain knowledge from their pre-training, enabling broader transferability across chemical space. In our case, the strength lies in generalizing to unforeseen configurations not present in the training set that might be seen in a potential MD trajectory, making the model more suitable when generalizability and accurate observables are preferred over minimizing the error over a selection of predefined configurations. To support this, we compared MD simulations of unfunctionalized cyclooctyne at the Si(001) surface using both models, applying the same protocol. Remarkably, the fine-tuned model outperformed the model trained from scratch, resulting in a negligible number of unphysical cyclooctyne structures (see Section S4 of the SI for details). However, the foundational model used, MACE-MP-0, may not be an ideal starting point since it contains a large amount of inorganic bulk crystals not directly related to surface chemistry. Other models, such as the MACE-OMAT,⁹⁴ which were trained on a vastly larger and more chemically diverse dataset, are expected to extrapolate better to surface systems; however, the underlying dataset still lacks explicit surface configurations. Future work in this area will likely focus on developing foundational models trained directly on surface and adsorbate data to improve transferability and reduce the data needed for task-specific fine-tuning.

For final models, we use every 25th AIMD frame, resulting in 13 000 data points for training. To ensure that these ~13 000

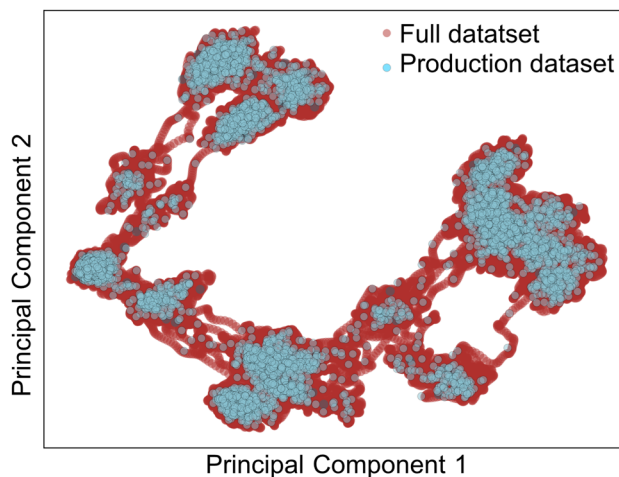


Fig. 3 PCA of the full (red) and the production AIMD-datasets (blue). Equivariant features are used for the descriptors as inputs for PCA.

configurations adequately span relevant reaction pathways and surface environments, we embedded both training and reference AIMD geometries into a low-dimensional manifold using principal component analysis (PCA) based on equivariant geometrical descriptors (Fig. 3). As shown, both datasets cover approximately the same space, demonstrating the completeness of our training dataset using only every 25th AIMD frame for training. Energy-scaled PCAs for all relevant parts of the dataset are presented in Fig. S6 (SI), indicating that reducing the production dataset size does not significantly reduce the chemical space or energy ranges covered.

3.2 ML driven MD simulations

To assess the role of statistics in MD simulations and to enable meaningful comparison with experiments, we performed 100, 1000, and 10 000 trajectories using machine learning interatomic potentials, in contrast to the 10 trajectories feasible with full DFT-based AIMD. Both machine learning models were tested for their ability to reproduce relevant chemical events in the MD runs. As shown in Table 1, using machine learning models results in a dramatic reduction in computational time over AIMD of several orders of magnitude. At the same time, the training time of the fine-tuned model training is only 1.1 h on eight GPUs. For the model trained from scratch, increasing the number of epochs by a factor of 10 in comparison to the fine-tuned model, increases the training time by a factor of six to 6.6 h.

To analyse whether improved statistics lead to larger sampling of configuration space during dynamics and new structures not observed in the 10 DFT-based AIMD, we analyse representative adsorption structures. These are illustrated in Fig. 4. Nine representative adsorption structures arise in our molecular gun simulations: 1 – on-top cyclooctyne (OT-CY), 2 – bridge cyclooctyne (BR-CY), 3 – on-top ethynyl (OT-ET), 4 – bridge ethynyl (BR-ET), 5 – double (DB), 6 – precursor (PC), 7 – sublayer (SL), 8 – sublayer double (SL-DB), and 9 – other.

Configurations 1–4 involve the molecule spanning two adjacent surface atoms, either *via* the cyclooctyne ring's triple



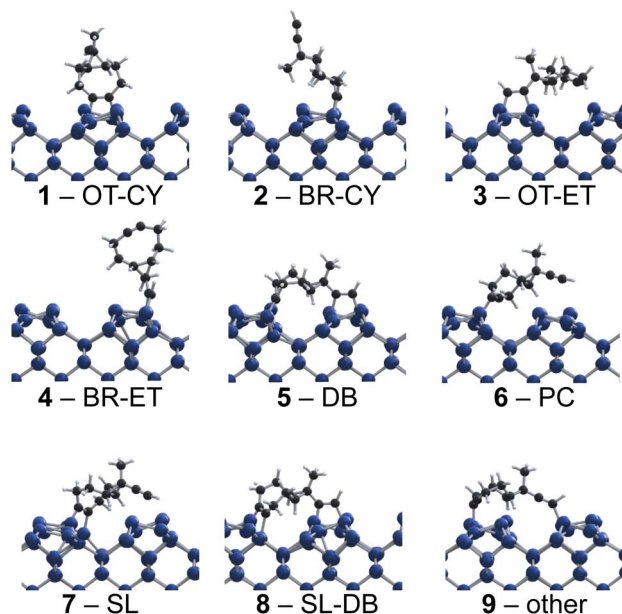


Fig. 4 Binding modes as detected using ML-MD and (partially) AIMD (1–9). Si atoms blue, C black and H white. ECCO binds either via the triple bond of the cyclooctyne (CY) or ethynyl (ET) group. The Si(001) surface offers two distinct binding sites on-top (OT) and bridge (BR). As each ECCO can bind via the two functional groups, also doubly bound ECCO molecules can be observed (DB). During reactions of ECCO with the surface, ECCO molecules that bind to a single Si atom can be observed (precursor states, PC). When Si atoms of the second Si atom layer are involved in bonding, structures are labeled as sublayer (SL). These binding modes can also occur with doubly bound ECCO molecules (sublayer-double, SL-DB). For the top view and available DFT binding energies see Fig. S6.

bond (CY; 1 and 2) or the ethynyl group (ET; 3 and 4). The two surface atoms can be on the same Si dimer (on-top, OT; 1 and 3) or on neighboring dimers (bridge, BR; 2 and 4). Configuration 5 comprises states where both triple bonds react with the surface to form doubly bonded ECCO (DB). The precursor state (PC; 6) describes ECCO datively bound to a single Si atom. This state is observed in DFT data, where it is an important reaction intermediate.³² In sublayer (SL; 7) and sublayer-double (SL-DB; 8) structures, ECCO binds to a Si atom beneath the top layer, either singly or doubly. All other configurations (mainly both triple bonds in a datively bonded state) are grouped as other (9).

Fig. 5 shows the distribution of final ECCO adsorption sites on Si(001) for the fine-tuned model and the AIMD reference. The distributions obtained for the other discussed models are shown in Fig. S1. The main experimental adsorption mode corresponds to the on-top cyclooctyne (1), shown in yellow.¹⁹ The 10 DFT-based AIMDs fail to capture the experimentally dominant motif 1, while instead over-emphasizing the doubly bonded mode 5. The 1000 trajectories obtained using the fine-tuned MACE-MP-0 model are able to capture the experimental motif much better, recovering the statistics of the adsorption. Additionally, several adsorption configurations are found which correspond to intermediate states in the DFT trajectories. Notably, most of these structures are not observed

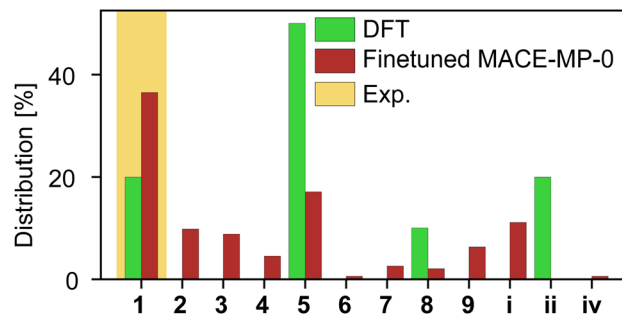


Fig. 5 Distribution of the binding modes at the end of each MD simulation for the fine-tuned MACE-MP-0 model and the AIMD reference. The binding mode distribution of the fine-tuned model is given in red and the AIMD reference in green. The “single adsorption configuration”¹⁹ observed in STM is highlighted in yellow.¹⁹

experimentally since they are not stable enough to be observed under experimental conditions.

Not all MD trajectories yield covalent binding – non-productive outcomes are labelled: intact but floating ECCO (i), H-abstraction (ii), broken C–C bonds (iii, see Fig. S5, SI), and “explosions”, corresponding to total disintegration of the molecule due to insufficient training data in this region, (iv). As shown in Fig. S1a, the fine-tuned model best matches experiment. From-scratch models produce a high fraction (>30%) of desorbed intact ECCO (i), while MACE-MP-0 often breaks the C–C bond (~20%; iii). The tendency of the MACE-MP-0 and from-scratch model yield unphysical or unproductive events, despite low MAEs, underscores that the fine-tuned model generalizes better and predicts realistic dynamics at scale. The increasing fraction of desorbed molecules predicted by the from-scratch model are considered unrealistic due to the experimental sticking coefficient of approximately one for the unfunctionalized cyclooctyne meaning that almost all molecules are expected to adsorb when hitting the surface.¹⁹ We do concede though that the models results may be less reliable once the dynamics moves too far outside of the training domain. Uncertainty measurements during key binding events could help increase the models trustworthiness.

Fig. S1b illustrates convergence of binding mode populations with increasing number of MD trajectories. Moving from 100 to 1000 machine learning based MD trajectories, there is a marked shift in the observed binding mode distribution and covered configurational space, as supported by PCA descriptor plots (see Fig. S7). The difference between 1000 and 10 000 trajectories, however, is minor, indicating statistical convergence is reached after around 1000 independent simulations. The precise proportions of binding modes for 1000 and 10 000 runs are summarized in Table S2. In order to show the statistically unconverged results, four sets of 10 ML-trajectories are run (Fig. S12). This results in a varying distribution for each of the sets, showing the low number of trajectories to be a main contributor of the previous disagreement between experiment and theory.³²

Examining surface sampling, Fig. 6 displays the minimum distance between the cyclooctyne triple bond and the surface for



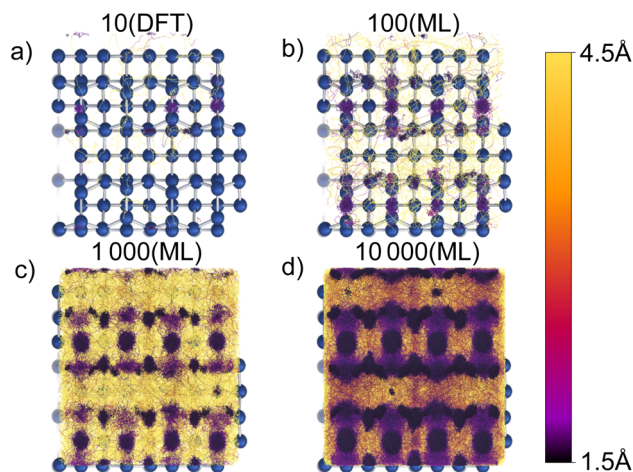


Fig. 6 Representation of the sampling (top view). Utilizing a binning approach on the center of the cyclooctyne triple bond over all simulation runs for (a) 10 DFT, (b) 100, (c) 1000, and (d) 10 000 trajectories obtained using the fine-tuned MACE-MP-0 model. The bins are created with a size of 0.0015 \AA^2 and colored corresponding to the lowest occurring z -value (surface normal). The height information is relative to the topmost surface atoms.

all trajectories. DFT-based trajectories reach only a limited set of surface sites, reflecting the small sample. With 100 machine learning-driven simulations using the fine-tuned model, coverage expands, but many regions remain unsampled. For both 1000 and 10 000 trajectories, all surface regions are visited, supporting the conclusion from Fig. S1b that 1000 runs suffice for statistical convergence (see Fig. S3 for mode-colored sampling, and Fig. S4 for a side view.)

3.3 Preferred binding mode

The statistical convergence of binding mode distributions demonstrates that AIMD simulations based on only 10 DFT trajectories are insufficient to provide a realistic depiction of ECCO adsorption behavior. Notably, the most prominent double-adsorption structure (5) appears primarily because the PBE functional underestimates the ethynyl reaction barrier by approximately 0.1 to 0.2 eV, as previously shown.⁹⁵ This underestimation, and the consequent increased likelihood for the ethynyl group to react with the surface, are therefore also inherited by our ML models.

4 Conclusion

We have demonstrated that large-scale molecular dynamics sampling is essential to accurately reproduce experimental adsorption statistics for large molecules adsorbing on a surface at the example of ethynyl-functionalized cyclooctyne on Si(001). By leveraging equivariant message-passing neural network potentials, comparing models trained from scratch and fine-tuned models based on parameters of foundational models, we achieved over 10^3 -fold speed-ups compared to conventional DFT-based molecular dynamics, enabling 10^3 – 10^4 trajectories to be run with moderate computational resources. Fine-tuning

on a few thousand AIMD snapshots is critical to adapt foundational models for specific surface chemistry: without this step, important adsorption modes are missing in subsequent machine learning-driven MD. Moreover, fine-tuning requires only a handful of epochs, reducing both training times and data requirements, while also minimizing the risk of catastrophic forgetting compared to training from scratch.

Our high-throughput based MDs uncover numerous new final states, such as mixed on-top/sublayer motifs, which are rare or completely absent in the few DFT-based runs. This comprehensive sampling shifts theoretical predictions towards the experimentally dominant on-top adsorption mode. Nevertheless, certain DFT-induced biases persist, in particular the tendency for the double-adsorption motif to appear due to the PBE underestimation of the ethynyl reaction barrier, which is inherited by the machine learning models. As the number of trajectories increases, surface sampling rapidly improves: at 100 runs, significant regions remain unsampled; at 1000, all key binding motifs are visited; at 10 000, near-complete coverage of the surface is achieved.

The statistical convergence of site populations between 1000 and 10 000 trajectories is minor, clearly indicating that poor statistical sampling – rather than deficiencies in *ab initio* theory – explains discrepancies between previous AIMD and experimental studies. Future work could further improve accuracy by employing Δ -learning, fine-tuning against higher-level quantum data, or selectively incorporating experimental observables to address residual DFT errors. Overall, our “machine-learning molecular gun” workflow provides a robust and scalable means to connect atomistic mechanisms with ensemble-level experiments, thereby guiding the rational design of surface-functionalized semiconductor devices. Due to the small fine-tuning required, this model can easily be extended to other surfaces and adsorbates with the potential to significantly increase the impact of modeling in computational surface dynamics.

5 Outlook

This work is a mere first step into the combination of quantum-chemical surface chemistry with machine learning targeting a single molecule on a surface. In the future, this approach can be extended to include molecule–molecule interactions. However, on a DFT level, this is not possible at large scales because of the many possible arrangements of the molecules. Nevertheless, they can play a fundamental role in coverage dynamics, *e.g.*, *via* reactivity reduction^{96,97} or a long-range steering effect,¹⁵ which has been investigated in a static fashion.

The ability to obtain statistics in DFT-quality MD will enable completely new avenues in surface chemistry, functionalization, catalysis, thin-film growth, and related fields, enabling us to get the chemistry right and provide statistically relevant answers to experimental questions.

Author contributions

Hendrik Weiske: data curation, formal analysis, investigation, methodology, software, validation, visualization, writing –



review & editing; Rhyan Barrett: ML methodology, writing – editing; Ralf Tonner-Zech: conceptualization, funding acquisition, project administration, resources, supervision, writing – review & editing; Patrick Melix: data curation, formal analysis, methodology, project administration, software, supervision, writing – original draft preparation, review & editing; Julia Westermayr: funding acquisition, project administration, resources, supervision, writing – original draft preparation, review & editing.

Conflicts of interest

There are no conflicts to declare.

Data availability

The data used to train ML models is freely available under the following link: <https://doi.org/10.17172/NOMAD/2021.09.28-2>.

Supplementary information (SI): PDF and raw data. See DOI: <https://doi.org/10.1039/d5dd00420a>.

Code availability: The code used to conduct molecular dynamics with the MACE model is freely available *via* the ASE package. Instructions to train MACE models and foundational models using fine-tuning processes can be found in the corresponding manual. All scripts and outputs (excluding ML-MD trajectories due to size) produced in this project are available in the published raw data on zenodo: <https://doi.org/10.5281/zenodo.17523493>.

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