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ARTICLE

Optical frequency comb Fourier transform spectroscopy of the CH₂⁷⁹Br⁸¹Br, CH₂⁷⁹Br₂, and CH₂⁸¹Br₂ isotopologues in the 1180–1210 cm⁻¹ regionReceived,
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Quantitative spectroscopic detection of dibromomethane, CH₂Br₂, for environmental monitoring, workplace safety, and exoplanetary studies is limited by the lack of accurate absorption cross-section data and rigorous spectroscopic models. We report the first high-resolution (6.3 MHz point spacing) absorption cross-section of CH₂Br₂ in the 1180 – 1210 cm⁻¹ region, measured using optical frequency comb Fourier transform spectroscopy. This spectral region is dominated by the strong CH₂ wagging (ν₈) fundamental vibration, which is about 50 times stronger than the fundamental C–H stretch around 3077 cm⁻¹. The measurements resolve isotopologue-specific rovibrational features of CH₂⁷⁹Br⁸¹Br, CH₂⁷⁹Br₂, and CH₂⁸¹Br₂, and we assign rovibrational transitions of the ν₈ fundamental and the overlapping ν₄+ν₈–ν₄ hot bands using two methods. First, an empirical non-linear least square fit implemented in PGOPHER provides high-precision line assignment and spectroscopic constants, including accurate band origins, rotational constants, and quartic centrifugal distortion parameters, for the three isotopologues, covering rotational levels up to K_a = 25 and J = 144, with an average RMS residual of 0.00037 cm⁻¹ (11.1 MHz). Compared with previously reported band parameters retrieved from a fit to narrowband (1.78 cm⁻¹) supersonically cooled spectra (B. E. Brumfield *et al.*, *J. Mol. Spectrosc.*, 2011, **266**, 57–62), our fit provides much improved global agreement between measured and simulated spectra. In parallel, an ab initio-based effective Hamiltonian approach was used to model the complete rovibrational polyads, including weak hot-band transitions and polyad interactions inaccessible to purely empirical fits, and provided the first ab initio-based line intensities of CH₂Br₂ in the 8 μm spectral region.

1 Introduction

Dibromomethane, CH₂Br₂, is a naturally occurring halogenated volatile organic compound (HVOC) that is mainly emitted from the ocean.^{1–4} Its spectroscopic monitoring is important for modelling the natural cycling of climate relevant traces gases, as CH₂Br₂ acts as a source of reactive halogen atoms that contribute to ozone depletion, and as a contributor to the stratospheric bromine budget due to the fast vertical transportation by the tropical deep convection.^{3, 5} A potential anthropogenic source of brominated VOCs are treated ballast water systems,⁶ where they are formed as disinfection by-products (DBPs) at concentrations substantially higher

compared to their natural abundance.^{7–9} Beyond terrestrial applications, methylated halogen species such as CH₃I, CH₃Br, CH₃Cl have recently been proposed as potential capstone biosignatures in exoplanetary atmospheres, owing to their comparatively low false-positive potential when used to confirm primary biosignatures such as O₂.¹⁰ Dibromomethane may play a similar role, although this possibility remains unexplored.

Accurate spectroscopic models of CH₂Br₂ are therefore a prerequisite for (i) modelling the natural cycling of climate relevant traces gases, (ii) validating the existing models of the spread of ballast water discharge,¹¹ and assessing the ecotoxicological impact of DBPs on marine life and human health in harbour environments, and (iii) enabling the remote detection of halogenated biosignatures in Earth-like exoplanetary atmospheres.

Recent advances in optical frequency comb technology—combining high spectral resolution, broad spectral bandwidth, and absolute frequency accuracy—have enabled complete rovibrational band measurements with isotopologue specificity.^{12–17} Moreover, the recent availability of fully stabilised comb sources and comb-based spectrometers operating in the 8 μm region^{18–22} extends the reach of high-resolution, broadband precision spectroscopy into the long-wave mid-infrared (mid-IR) range.

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Electronic Supplementary Information (ESI) available: High-resolution absorption cross-section data of CH₂Br₂ in the region of 1180 to 1210 cm⁻¹, and input PGOPHER file for the empirical simulations of CH₂Br₂ in the range of 1180 to 1210 cm⁻¹. See DOI: 10.1039/x0xx00000x



Previously, we have reported the first frequency-comb-based high-resolution mid-IR spectra of CH_2Br_2 with isotopologue resolution in the region of 2960 to 3120 cm^{-1} , corresponding to the C–H stretching vibrations.¹⁵ In that study, we revisited an earlier assignment of the asymmetric C–H vibration, ν_6 , around 3076 cm^{-1} by Sadiek and Friedrichs,²³ which were based on continuous-wave cavity ring-down spectroscopy (CW-CRDS). We demonstrated that a cascade of hot-band transitions of the type $n\nu_4+\nu_6-n\nu_4$ (with $n \leq 3$) had been misassigned as isotopic shift of the three naturally abundant isotopologues: $\text{CH}_2^{79}\text{Br}^{81}\text{Br}$ (mixed), $\text{CH}_2^{79}\text{Br}_2$ (light), and $\text{CH}_2^{81}\text{Br}_2$ (heavy).

In the long-wave mid-IR region, particularly around 1197 cm^{-1} (or 8.35 μm), CH_2Br_2 exhibits absorption features that are nearly 50 times stronger than those in the C–H stretching region. These absorptions arise from the CH_2 wagging vibration associated with the ν_8 fundamental band and could offer a significantly enhanced sensitivity for spectroscopic detection, especially in workplace safety monitoring applications, and in astrophysics. Despite this advantage, no high-resolution absorption cross-section data are currently available for CH_2Br_2 in this spectral region. Previous room temperature spectra in the literature were acquired at low resolution using Fourier transform spectroscopy with incoherent light sources, which provided only overall band contours and lacked isotopic resolution and high-resolution cross-section data.²⁴ The only high-resolution study is a CW-CRDS measurement by Brumfield *et al.*,^{25, 26} using a quantum cascade laser coupled to a supersonic expansion source, with spectral coverage of 1.78 cm^{-1} around the ν_8 band centre. In that work, the assignment of the cold spectrum of the ν_8 band was straightforward, with three resolvable rovibrational progressions attributed to the $\text{CH}_2^{79}\text{Br}^{81}\text{Br}$, $\text{CH}_2^{79}\text{Br}_2$, and $\text{CH}_2^{81}\text{Br}_2$ isotopologues and the provided spectroscopic parameters precisely reproduced the jet-cooled spectrum. However, the limited spectral coverage around the band centre (i) restricted the fitted spectroscopic parameters to band origins, rotational constants, and a single quartic centrifugal constant, and (ii) limited the accuracy of these parameters for simulating room-temperature spectra. Consequently, reliable room-temperature cross-sections and comprehensive spectroscopic models for CH_2Br_2 in the ν_8 region remain unavailable.

A major challenge in modelling the room-temperature spectra of brominated molecules is the existence of energetically low-lying vibrational states that retain significant thermal population. This leads to congested hot-band structure that overlaps and interferes with nearby fundamental transitions, similar to the C–H stretch region.¹⁵ However, such anticipated behaviour in the ν_8 region has not yet been systematically investigated. Analogous hot-band progressions have been reported for other halomethanes, including iodomethane, CH_3I , where a single hot band near the fundamental C–H stretch bands has been observed,^{27, 28} and diiodomethane, CH_2I_2 , where up to 5 hot bands have been

observed.²⁹ Another challenge is the nearly equal natural abundances of ^{79}Br and ^{81}Br , resulting in a 2:1 population ratio of the mixed, light, and heavy isotopologues.

In this work, we present the first high-resolution room-temperature absorption cross-section of dibromomethane in the 1180 – 1210 cm^{-1} spectral range, measured using a comb-based Fourier transform spectrometer (FTS) in the long-wave mid-IR infrared region.²¹ These high-resolution spectra are used to develop a spectroscopic model that accounts for bromine isotopic abundances and the low-lying ν_4 vibrational band. The empirical model, implemented in PGOPHER, includes the ν_8 fundamental and the $\nu_4+\nu_8-\nu_4$ hot bands for the three isotopologues. This model is further benchmarked against *ab initio* line-list calculations based on a non-empirical effective Hamiltonian approach.³⁰ The combination of broadband, high-precision comb-based spectroscopy and the resulting global models provides a consistent and accurate description of the rovibrational structure of CH_2Br_2 in the 1180 – 1210 cm^{-1} spectral range.

2 Experimental and computational details

2.1 Experimental Methods

The setup of the comb-based FTS experiment has been described previously,^{21, 31, 32} and will only be briefly summarized here. It consists of a mid-IR frequency comb, a multi-pass absorption cell and an FTS. The mid-IR comb has a repetition rate, f_{rep} , of 125 MHz and spectral coverage of 1140 – 1280 cm^{-1} . It is produced by difference frequency generation (DFG) between pump and signal beams derived from the same Er: fiber oscillator¹⁹ and is therefore inherently free from carrier-envelope-offset, f_{ceo} . The f_{rep} was locked to the output of a tunable direct digital synthesizer locked to a GPS-referenced Rb clock.

The mid-IR beam passed through a Herriott multi-pass absorption cell (Thorlabs, HC10L/M-M02) with a path-length of 10.436(15) m. Analytical grade CH_2Br_2 sample (Acros organics – 99%) was contained in an Ace glass tube connected to the gas supply system and was allowed to evaporate into the cell under its vapour pressure. Prior to introducing CH_2Br_2 into the cell, the vacuum system was repeatedly purged with dry nitrogen gas and evacuated through a bypass valve to remove impurities. Afterwards the cell was filled to the desired pressure, measured using a pressure transducer (CERAVAC CTR 100 N, 1 Torr range) with a manufacturer stated measurement uncertainty of 0.2%; the practical resolution was approximately 0.1 μbar . All measurements were performed at room temperature ranging between 23.1 and 24.2 $^\circ\text{C}$ with variation during measurement of ~ 0.2 $^\circ\text{C}$.

After the absorption cell, the beam was coupled to a home-built fast-scanning FTS with a nominal resolution matched to the f_{rep} , and detected by two HgCdTe detectors in a balanced configuration. A beam of a narrow-linewidth CW diode laser with a wavelength of 1563 nm propagating on a path parallel to the comb beam in the FTS was used for calibrating the optical path difference (OPD).



We acquired two high-resolution spectra at 31 and 50.2 μbar using the sub-nominal resolution approach^{33,34}. The spectrum at 50.2 μbar was required to enable the assignments of weak transitions of hot bands of light and heavy isotopologues. We measured spectra at 20 f_{rep} steps separated by 21 Hz, corresponding to 6.3 MHz point spacing in the optical domain. We scanned the f_{rep} in alternating directions, and at each step we recorded a set of 20 interferograms. We repeated the scans 16 times, which gave a total of 320 interferograms at each f_{rep} step and a total acquisition time of 7.5 h for all steps. A background spectrum was obtained from the average of 400 interferograms recorded at the first f_{rep} step with the absorption cell evacuated. Half of the background interferograms were recorded before and half after the sample measurement. We normalized the averaged spectrum at each f_{rep} step to the average background spectrum linearly interpolated to the wavenumber scale of the sample spectrum. We then corrected the remaining baseline by masking out the CH_2Br_2 band in the range from 1178 to 1212 cm^{-1} and fitting a model of the baseline consisting of a 3rd order polynomial and a single sine function to account for an etalon appearing in the spectra. The baseline-corrected spectra measured at the different f_{rep} steps were interleaved to produce a final spectrum with 6.3 MHz spectral point spacing.

Furthermore, to check the linearity of the dependence of integrated absorption on sample density, we acquired spectra at five different sample pressures between 10 and 50 μbar at a single f_{rep} value (200 averages without interleaving). The sample cell was evacuated between each measurement. While these spectra are not fully resolved, the absorption integrated over the whole band can be compared across different pressures and to the same f_{rep} step of the interleaved spectra. For more effective baseline correction in the spectra taken at one f_{rep} step, we used a model of the CH_2Br_2 band based on the interleaved spectrum measured at 31 μbar , and fitted this band model together with the baseline model described above, instead of masking the CH_2Br_2 bands.

In the sub-nominal resolution method, the effective wavelength, λ_{ref} , of the reference laser used for OPD calibration is usually found by varying it in post processing to minimize instrumental line shape distortions of individual lines.³⁴ This optimization was not possible on the CH_2Br_2 spectrum due to spectral congestion and scarcity of isolated absorption lines. However, weak H_2O lines appeared away from the CH_2Br_2 bands, as a result of air leakage into the measurement cell during the measurement. Those H_2O lines were used for optimizing λ_{ref} by matching their positions in a preliminary measurement to a model simulated using parameters from the HITRAN2020 database.³⁵ We took the final λ_{ref} value as the mean of the optima found for four different H_2O lines located outside of the CH_2Br_2 band. For all measurements reported here, λ_{ref} was optimized by matching the CH_2Br_2 band contour to that in the optimized measurement. We estimate the frequency uncertainty of this procedure to be 2.4 MHz, which includes a 1.5 MHz uncertainty associated with line position determination arising from minimization of the instrumental line shape using water absorption lines, a ~ 1.8 MHz uncertainty in the HITRAN line centre positions of

the reference H_2O lines, and 0.2 MHz uncertainty from optimization of dibromomethane spectra shape to the reference measurement.

The aforementioned leak into the measurement cell led to the increase of the pressure to 214 μbar during the 31 μbar measurement and to 235 μbar during the 50.2 μbar measurement. We estimated the leak rate as an increase in pressure from the beginning of the measurement to its end to be 32 $\mu\text{bar}\cdot\text{L}/\text{h}$, assuming internal volume of the cell of 0.73 L, which corresponds to two thirds of the maximum leak rate of 10^{-5} Torr L/s stated by the manufacturer.

The peak absorption in the Q-branch region corresponds to transmission of 9%, while outside the Q-branch region the maximum absorption reaches values corresponding to transmission of 31% and 16% for measurements at 31 and 50.2 μbar , respectively. Therefore hereafter, the absorption is analysed in the range from 1178 cm^{-1} to 1212 cm^{-1} excluding the saturated Q-branch region at 1196–1197 cm^{-1} , unless stated otherwise. By comparing the spectra at each of the 16 f_{rep} scans, we observed a linear decrease in the absorption of CH_2Br_2 of about 7% during the whole measurement. This decrease in absorption can be attributed to adsorption of the sample to the cell walls. We quantified the decrease by fitting a model of the CH_2Br_2 absorption to the spectrum at the first f_{rep} step of each of the 16 f_{rep} scans, together with the model of the baseline. The absorption model was obtained from the fully interleaved and averaged spectra measured at 31 μbar and 50.2 μbar , respectively. Since the absorption change was linear, we scaled the absorption cross-section of the two measurements by half the percentual decrease, corresponding to 3.3% and 3.4% for the spectra at 31 μbar and 50.2 μbar , respectively. The spectra of the linearity measurement were acquired in 15 minutes per pressure and thus negligibly affected by the decrease in sample density.

2.2 Empirical PGOPHER simulations

The spectral simulations and empirical rovibrational fitting were first performed using the PGOPHER software developed by C. M. Western.³⁶ This is an empirical effective Hamiltonian approach, in which spectroscopic parameters are optimised through nonlinear least-squares fitting to the experimentally assigned transitions.

Dibromomethane was treated as a near-prolate asymmetric top, with the Ir representation. The light and heavy isotopologues were treated within the C_{2v} point group symmetry, whereas the mixed isotopologue was assigned C_s symmetry owing to the reduced molecular symmetry introduced by isotopic substitution. Nuclear spin statistical weights of 9:7:7:9 were included for the $\text{CH}_2^{79}\text{Br}_2$ and $\text{CH}_2^{81}\text{Br}_2$ isotopologues, while nuclear spin statistics were not applied to the mixed isotopologue.

Fig. 1 illustrates the molecular structure of CH_2Br_2 , including the principal axes of inertia and the symmetry planes of C_{2v} isotopologues. The H–C–H plane contains the hydrogen atoms and carbon, reflecting the identical bromines, while the Br–C–Br plane contains both bromine atoms and carbon, reflecting the hydrogen atoms. The spectrum of CH_2Br_2 in the 1180 – 1210 cm^{-1} range is dominated by the CH_2 wagging vibrations (ν_8 band), which induces a change in the dipole moment along the a -axis, resulting in an a -type parallel band structure.



Ground-state rotational and centrifugal distortion constants were fixed to values obtained from microwave spectroscopy, taken from Niide *et al.*³⁷ for the mixed isotopologue and from Davis and Gerry³⁸ for the light and heavy isotopologues. Initial excited-state parameters for the ν_8 fundamental band were taken from the narrowband cavity ring-down spectroscopy measurements of Brumfield *et al.*²⁶ and subsequently refined through fitting to the present broadband, room-temperature spectra. For the simulations of the $\nu_4 + \nu_8 - \nu_4$ hot bands, the band parameters of the low-lying lower state ν_4 were taken from our previous simulations of the C–H stretch region,¹⁵ and the upper state parameters were refined through fitting to the experimental spectrum. Overall, the empirical Hamiltonian model included the ν_8 fundamental and the $\nu_4 + \nu_8 - \nu_4$ hot bands for all three isotopologues, resulting in a total of six vibrational bands. The PGOPHER input file of the simulations and assignment is given in the Supplementary Information (S1).

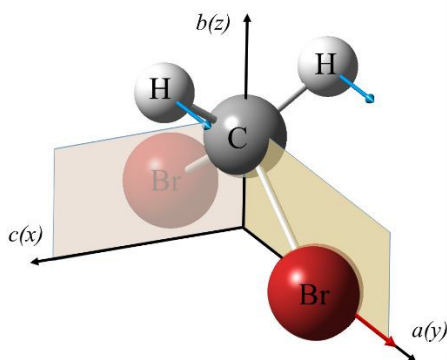


Fig. 1 Molecular structure of CH₂Br₂. The blue and red arrows represent the displacement vectors and the direction of the transition dipole moment for the ν_8 vibration. The principal axes of inertia and the two symmetry planes of the C_{2v} isotopologues are also shown.

2.3 Non-empirical (*ab initio*) effective Hamiltonian simulations

While PGOPHER provides efficient, band-specific simulations by fitting a number of spectroscopic parameters to experimental transitions, its applicability is limited to the bands exclusively included in the model, and to the spectral coverage of the experimental spectrum used to empirically fit rovibrational levels. It cannot easily be extrapolated to unobserved vibrational states or very high rotational levels, and it does not generate a global line list. Furthermore, it provides only relative intensities. To overcome these limitations, we use the *ab initio* based effective Hamiltonian methodology, proposed in Ref.³⁰ as a complementary approach. This method combines the simplicity of the traditional effective Hamiltonian approach, such as PGOPHER, with the completeness of pure variational calculations to provide globally accurate model for the construction of comprehensive line lists.

Following our previous *ab initio* works, in particular, ref.³⁹ and ⁴⁰, the potential energy surface (PES) and dipole moment surface (DMS) of CH₂Br₂ were both expressed as a polynomial expansion in terms of irreducible tensor operators (ITOs) built from internal coordinates and adapted to the C_{2v} and C_s point groups. Both the PES and the

DMS were then expanded as Taylor series in normal-mode coordinates up to sixth order, while the Eckart–Watson–Rimmet energy operator⁴¹, implemented in the TENSOR code^{42–45}, was employed. In order to determine the expansion coefficients, *ab initio* electronic structure calculations were performed on grids of reference nuclear configurations.

In the case of the PES, the RHF-CCSD(T)-F12b method implemented in the MOLPRO package^{46, 47} was employed in the first step in combination with the VQZ-PP-F12 and CVQZ-F12 basis sets for bromine, and for hydrogen and carbon, respectively. In the second step, corrections were included for: (i) scalar relativistic effects (within the Cowan-Griffin approach); (ii) the diagonal Born Oppenheimer correction (computed at the RHF-CCSD/cc-pVDZ level using the CFOUR package^{48, 49}); and (iii) high-order electron correlation effects (evaluated using the CCSDT(Q)/VDZ and CCSDTQ/VDZ methods within the MRCC package^{50, 51}). The resulting *ab initio* energies for the 5368 nuclear configurations were fitted using ITOs up to the sixth order, yielding 460 expansion coefficients. The root-mean-square deviation of the fit was 0.163 cm⁻¹.

The *ab initio* calculations of the electric dipole moment were made using the finite difference method as the first derivative of the potential energy of nuclei with respect to the electric field. The RHF-CCSD(T)-F12b/AVQZ level of theory, as implemented in MOLPRO, was employed to solve the electronic problem. The number of nuclear configurations was 5368 for the A₁ component, and 4444 for the B₁ and B₂ components. The root-mean-square (RMS) errors of the fit to the reference *ab initio* dipole moment values did not exceed 3.6 × 10⁻⁵ debye using 418, 351 and 397 expansion coefficients for the A₁, B₁, and B₂ components of the DMS, respectively.

The global effective approach begins with a full variational nuclear-motion Hamiltonian $H^{(J,C)}$ computed for a given symmetry block, defined by rotational quantum number J and symmetry C , in a primitive vibrational basis $|j,J,C\rangle$, where γ represents all other quantum numbers. This Hamiltonian includes all vibrational couplings and rotational interactions within the block, capturing the complete rovibrational structure. A unitary transformation $T^{(J,C)}$ is then applied to the Hamiltonian to obtain a block-diagonal effective Hamiltonian $H^{(J,C,P)}$, truncated to a chosen polyad P . This block-diagonalization ensures that strongly interacting states within a polyad are treated exactly, while weakly interacting states outside the polyad are effectively decoupled. The transformation also produces a set of effective eigenvectors $\tilde{U}(J,C)$ and eigenvalues E_{vT} corresponding to vibrational-rotational energy levels. In this work, the eigenpairs were computed up to $J = 20$. The variational energies E_{vT} can be replaced with experimental energies E_{vT}^{obs} , allowing refinement of the effective Hamiltonian with minimal computational effort. In case of CH₂Br₂, the empirically determined energy levels from PGOPHER simulations were used as E_{vT}^{obs} to refine the Hamiltonian. To this end, a small subset of so-called diagonal parameters was refined for the ground state and for the ν_4 , ν_8 and $\nu_4 + \nu_8$ vibrational bands. Here, 'diagonal' denotes that the powers of the creation and annihilation operators are equal.

The same transformation is applied to the dipole moment operators to compute line intensities to ensure that predicted



transition strengths are consistent with the effective Hamiltonian energy levels. This approach allows rapid calculation of high- J rotational levels while retaining global accuracy, and has been successfully applied to molecules such as CH_4 ⁵², and more recently for SiF_4 ³⁹ and CHF_3 .⁴⁰ However, CH_2Br_2 presents a more challenging case as highlighted earlier for several reasons: (i) As a heavy halogenated asymmetric top, it has a much denser rotational structure and more closely spaced energy levels than the relatively light and symmetric molecules mentioned above. (ii) The presence of two bromine atoms with the nearly equal natural isotopic abundance of ^{79}Br and ^{81}Br introduces multiple isotopologues with different symmetries. Note that the C_s isotopologue $^{12}\text{C}^{79}\text{Br}^{81}\text{Br}$ is the most abundant species. (iii) The coexistence of low-lying vibrational state which increase the density of state at room temperature, and hence requires careful treatment of rovibrational couplings. Such low-lying vibrational states result in a substantial number of hot bands, similar to CH_4 at high temperatures (>1000 K).

A more complete description of the *ab initio* based effective Hamiltonian model for CH_2Br_2 isotopologues will be published in a separate paper.

3 Results and discussion

3.1 High-resolution absorption cross-section

Figure 2(a) presents the high-resolution absorption cross-section of CH_2Br_2 in the region from 1178 cm^{-1} to 1212 cm^{-1} retrieved from the spectrum measured at $31\text{ }\mu\text{bar}$ with a point spacing of 6.3 MHz (black), compared to the cross-section from the Pacific Northwest

spectrum from PNNL, which does not resolve the rotational structures at all. For comparison, the frequency comb data is also plotted convolved with a *sinc* function with a zero-crossing spacing of 3.4 GHz (green) to mimic the resolution of the PNNL spectra. Fig. 2(b) shows the relative difference in cross-section between the convolved spectrum and the PNNL spectrum. The comb spectrum agrees with PNNL to within a few percent throughout most of the CH_2Br_2 bands, deviating significantly only on the wings where the absorption is small and slight differences in baseline between the two measurements would have a large impact on the relative discrepancy. The experimental cross-section is provided in the Supplementary Information (S2).

Figure 3 shows the pressure dependence of the integrated absorption measured to evaluate the linearity and uncertainty of the absorption cross-section. The absorption coefficient, α , of the linearity series measurement integrated from 1178 cm^{-1} to 1212 cm^{-1} excluding the saturated Q-branch at $1196\text{--}1197\text{ cm}^{-1}$ is shown as black dots. The inset of Fig. 3 shows a CH_2Br_2 spectrum with spectral range used for absorption coefficient integration highlighted in black. The dotted line shows a linear fit to the linearity measurement data. The fit included an intercept as a free parameter to evaluate any potential offset in the pressure measurement, but it was not statistically significant. The plot also includes the integrated absorption coefficient of the two interleaved measurements (red crosses) where the data point at $31\text{ }\mu\text{bar}$ corresponds to the spectrum shown in Fig. 2.

The standard deviation of all data points in lower panel of Fig. 3 is 2%, which is comparable to the difference of 2.3% in the cross-sections of the comb-FTS and PNNL spectra integrated over the same

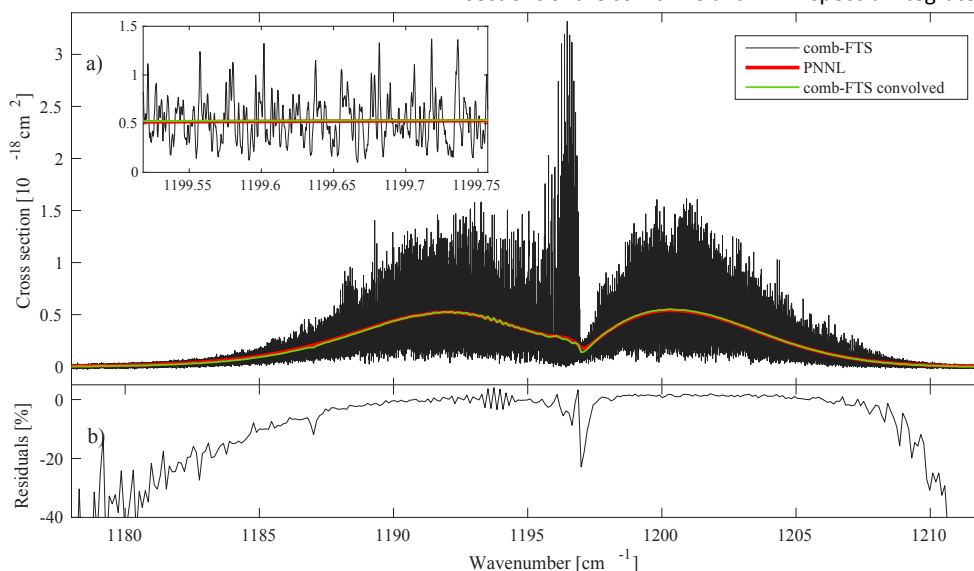


Fig. 2 (a) Absorption cross-section of CH_2Br_2 measured in this work at $31\text{ }\mu\text{bar}$ using the comb-based FTS (black) compared to the PNNL data²⁴ (red). The green trace shows the cross section from this work convolved with the *sinc* function to mimic the resolution of PNNL spectra. The inset shows a zoomed spectral window around 1199.65 cm^{-1} . (b) The relative discrepancy between the convolved comb-FTS measurement and the PNNL data.

National Laboratory (PNNL) database (red),²⁴ which has a resolution of 3.4 GHz . The inset shows a zoomed spectral window around 1199.65 cm^{-1} demonstrating the dramatic improvement in spectral resolution compared to the Fourier transform infrared (FT-IR)

range as for the linearity measurement. However, despite this very good agreement, comparison of the integrated absorption of the spectra in the linearity series — using either the band shape model described in Section 2.1 or masking the band region during baseline



correction —indicates that baseline correction can contribute up to 10% uncertainty to the slope in Fig. 3 and to the cross-section in Fig. . The band shape model is used for the results presented here, as it allows a simultaneous fit of both the baseline and absorption feature across the full spectral range, whereas masking the band region constrains the baseline fit only to the surrounding spectral regions and therefore increases its sensitivity to chosen etalon frequencies and polynomial order.

Beyond the comparison with PNNL, we estimated a minimum detectable absorption coefficient from the standard deviation of the noise in the baseline of the spectrum at 31 μbar to be α_{min} of $4.6 \times 10^{-6} \text{ cm}^{-1}$ in total acquisition time of $t = 7.5 \text{ h}$. This corresponds to a noise equivalent absorption sensitivity, $\text{NEAS} = \alpha_{\text{min}} \cdot t^{1/2} = 7.5 \times 10^{-4} \text{ cm}^{-1} \text{ Hz}^{-1/2}$. Taking into account the spectral coverage of the comb with $M = 2.4 \times 10^5$ spectral elements in the interleaved spectra, we also report the figure of merit $\text{FoM} = \text{NEAS} \cdot M^{-1/2} = 1.5 \times 10^{-6} \text{ cm}^{-1} \text{ Hz}^{-1/2}$ per spectral element.

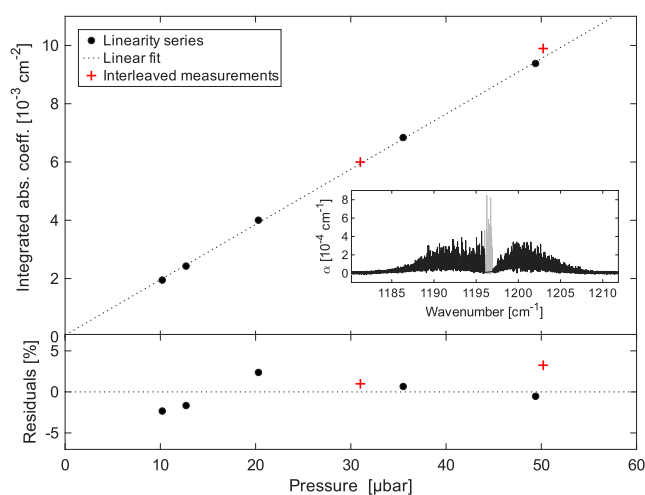


Fig. 3 The pressure dependence of the absorption coefficient integrated from 1178 cm^{-1} to 1212 cm^{-1} excluding the Q-branch (see black trace in the inset where grey data points were excluded) in the linearity series (black dots) and the two interleaved measurements (red crosses). The dotted line shows a linear fit to the linearity series. The bottom panel shows the fit residuals expressed as a percentage of the absorption.

3.2 Spectral simulations and analysis

In this section, the rovibrational spectra of CH_2Br_2 in the 1180–1210 cm^{-1} range are analysed for all three isotopologues: $\text{CH}_2^{79}\text{Br}^{81}\text{Br}$, $\text{CH}_2^{79}\text{Br}_2$, and $\text{CH}_2^{81}\text{Br}_2$. The analysis combines empirical effective Hamiltonian simulations implemented in PGOPHER with benchmark comparisons to non-empirical *ab initio*-based effective Hamiltonian line lists.

3.2.1 Empirical effective Hamiltonian simulations

The parallel nature of the ν_8 band might suggest a straightforward assignment, however, as mentioned earlier the presence of the low-lying ν_4 vibration ($\sim 172 \text{ cm}^{-1}$) and the nearly equal abundance of the two bromine isotopes significantly complicates the spectra at room temperature. For an equilibrated sample, the first hot band ($\nu_4 + \nu_8 - \nu_4$) is predicted to appear near the fundamental band with a population ratio of 0.44, based on the Boltzmann distribution. Consequently, each isotopologue exhibits both cold and hot parallel

bands, all of which must be simulated to reproduce the room-temperature spectra of CH_2Br_2 with naturally abundant Br and Br.

Figure 4 shows the measured high-resolution absorption coefficient spectrum at 31 μbar of CH_2Br_2 together with simulations of the fundamental ν_8 and the hot $\nu_4 - \nu_8 + \nu_4$ bands of each isotopologue: $\text{CH}_2^{79}\text{Br}^{81}\text{Br}$ (green), $\text{CH}_2^{79}\text{Br}_2$ (red), and $\text{CH}_2^{81}\text{Br}_2$ (blue). The spectra were simulated using Gaussian line shapes with Doppler full width at half maximum (FWHM) of 0.0011 cm^{-1} . The simulations of each isotopologue are offset for clarity, and for each isotopologue the hot and the fundamental band simulations are also offset relative to one another. The strong rovibrational features at the band centre of the measured spectra are saturated due to the strong absorption of CH_2Br_2 (vide supra). The assignment was enabled through the measurements at a lower pressure of 31 μbar for the strong fundamental band transitions, and at a higher pressure of 50.2 μbar for the weak transitions of the light and heavy isotopologues and for the hot bands. The predicted 2:1:1 intensity ratio of $\text{CH}_2^{79}\text{Br}^{81}\text{Br}$, $\text{CH}_2^{79}\text{Br}_2$, and $\text{CH}_2^{81}\text{Br}_2$ isotopologues, explained by the isotope abundance, can be seen in Fig. 4. In addition, the intensities of the hot bands roughly match the predictions from Boltzmann statistics for each isotopologues. It should be noted again that PGOPHER provides only relative intensities, particularly for hot bands, unless a proper partition function is specified; absolute line strengths or absorption cross-sections require additional scaling and proper treatment of coupling between vibrational states. These limitations can be addressed in the complementary *ab initio*-based non-empirical simulations (vide infra).

Initial simulation of the ν_8 spectra utilized band origins and rotational constants from the CRDS measurements of Brumfield *et al.*,²⁶ which were obtained from a fit to a narrow spectral coverage of 1.78 cm^{-1} around the band centre, measured in the jet-cooled sample. These parameters provide a good initial match with the Q-subcluster rovibrational features near the band centres of the measured comb spectra at room temperature. However, the agreement deteriorated far from the band centre, and the parameters were lacking for the hot band transitions.



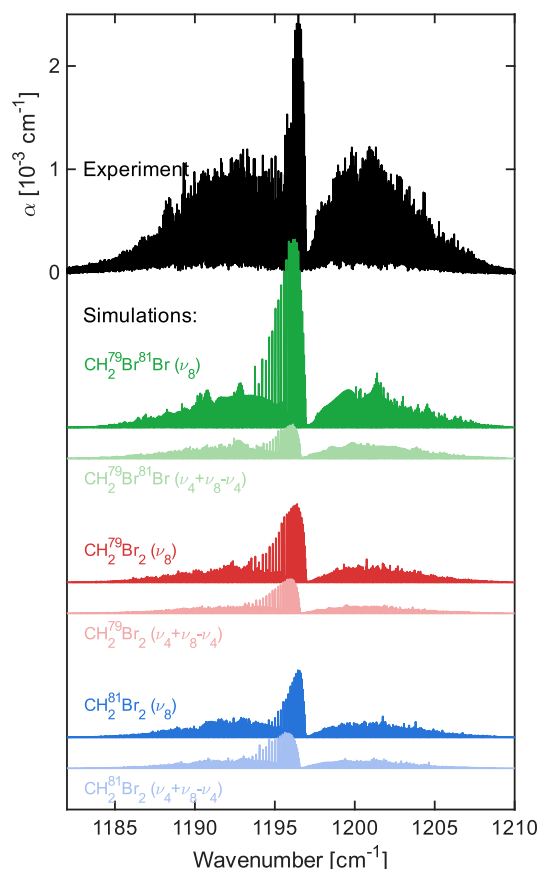


Fig. 4 High resolution absorption coefficient (α , in cm^{-1}) measured at 31 μbar using the comb-based FTS together with the GOPHER simulations of the fundamental ν_8 and the $\nu_4+\nu_8-\nu_4$ hot bands of $\text{CH}_2^{79}\text{Br}^{81}\text{Br}$ (green), $\text{CH}_2^{79}\text{Br}_2$ (red), and $\text{CH}_2^{81}\text{Br}_2$ (blue). The overall simulations involve the sum of all six vibrational bands.

Band parameters from line fit. The first set of assignments involved the progression of the strong, sharp spectral features at the centre of the ν_8 bands for all the three isotopologues, shown in Fig. 4. For each isotopologue, these features represent a series of Q-subcluster progressions characteristic of a-type parallel vibrations. Each single feature is composed of a series of tightly packed transitions sharing the same K_a for the lower and upper states: $Q(J'', K_a'', K_c'') : (\nu', J' = J'', K_a' = K_a'', K_c' = K_c'' \pm 1) \leftarrow (\nu'', J'', K_a'', K_c'')$. The assignment of these Q-subclusters was possible up to K_a values of 22 – 25, thanks to the broad spectral coverage of the frequency comb. This broad coverage of the full band directly impacts the accuracy of the obtained band parameters and the ‘global’ match of the experimental spectra to the simulations (vide infra).

After fitting the assigned Q-subclusters, partially resolved transitions in the P and R branches could be assigned. Similarly, for the $\nu_4+\nu_8-\nu_4$ hot bands, the assignment started with the Q-subclusters, first for the mixed isotopologue and subsequently for the light and heavy isotopologues. For these bands, the fit was mostly limited to the Q-subcluster progressions, as unambiguous assignments of P- and R- branch transitions was hindered by the cross-interfering absorption of fundamental band transitions. It should be noted that higher-order hot bands, $2\nu_4+\nu_8-2\nu_4$ and $3\nu_4+\nu_8-3\nu_4$, are predicted to reach population ratios of ~ 0.19 and ~ 0.08 at room temperature, respectively. However, assignment of

their Q-subcluster progressions was challenging due to the overlap with other strong bands. Overall, 6298 transitions were assigned among all simulated bands. These assigned transitions were used in non-linear least square fit to provide effective band parameters for the ν_8 and $\nu_4+\nu_8-\nu_4$ bands of the three isotopologues. In addition, they were used to refine the effective Hamiltonian of the non-empirical *ab initio*-based calculations as described earlier.

Figure 5 (a) shows the overall simulated spectrum (inverted for clarity) after fitting the assigned transitions, together with the experimental spectrum measured at CH_2Br_2 pressure of 50.2 μbar . The simulated spectrum is scaled to have the same integrated absorption as the experimental spectrum at 50.2 μbar , excluding the Q-branch region between 1196 to 1197 cm^{-1} . The data for the simulated spectrum is provided in the Supplementary Information (S3). Blue vertical bars at the top of panel (a) indicate the 297 transitions assigned by Brumfield *et al.*²⁶ within the 1.78 cm^{-1} measurements window. As shown in this figure, an overall very good match in the band structure between the experiment and simulation is observed. The lower panels present zoomed-in spectral windows, marked in panel (a), highlighting the quality of the match near the band centre [panel (e)], the Q-subcluster progressions for both the ν_8 and $\nu_4+\nu_8-\nu_4$ bands show excellent agreement with the experiment for the three isotopologues, as indicated by the faithful reproduction of all strong and weak absorption peaks. Close to the band centre, but apart from these Q-subclusters [panel (d)], still a very good match is obtained. Even farther from the band centre, panels (b) and (g), several sharp rovibrational transitions could be identified.

Table 1 summarizes the fitted band parameters of the fundamental ν_8 and the hot $\nu_4+\nu_8-\nu_4$ bands for the $\text{CH}_2^{79}\text{Br}^{81}\text{Br}$ isotopologue, together with the ν_8 band parameters reported by Brumfield *et al.*²⁶ For the ν_8 band, the band origin and rotational constants obtained in the present work agree with those of Brumfield *et al.* within $\approx 1\sigma$ of the combined uncertainty, with the band origins differing by only 2.1×10^{-5} (~ 0.6 MHz). The uncertainty of the ν_8 band origin in the present work is about four times smaller than that reported by Brumfield *et al.*, while the uncertainties of the rotational constants are lower by more than one order of magnitude. In addition, higher order centrifugal distortion constants could be floated in the present fit, while in the work of Brumfield *et al.* these parameters were fixed to their ground state values. Also listed in this table are the number of assigned K_a values, $N(K_a)$, the maximum assigned rotational levels, J_{max} , and the total number of transitions. Since dibromomethane is a near-prolate asymmetric top with a Ray’s asymmetry parameter of approximately -0.996 , the rotational energies depend strongly on K_a but only weakly on K_c , leading to very similar frequencies for many distinct rovibrational transitions that differ only in K_c . Several transitions satisfying $E(J, K_a, K_c \pm 1) \approx E(J, K_a, K_c)$ may become coincident within the Doppler width of the profiles and experimentally unresolved. These coincident transitions are not restricted to the Q-subclusters near the band centre but also occur for several transitions in the P and R branches. In the present analysis, these coincident transitions, together with the Q-subclusters, are treated as single effective transitions in the fitting



procedure. Table 1 additionally reports the number of unique frequencies assigned, N_{uniq} , corresponding to the number of experimentally distinguishable line positions used in the fit.

Table 1 The band parameters of the fundamental ν_8 and the $\nu_4+\nu_8-\nu_4$ hot band for the $\text{CH}_2^{79}\text{Br}^{81}\text{Br}$ isotopologue (all in cm^{-1}), number of K_a and J_{max} assignments, the number of assigned transitions, $N(\text{trans})$, number of unique frequencies assigned to the experiment N_{uniq} , and their root-mean-square (RMS) errors (in cm^{-1}). Values in parentheses are 1σ uncertainties.

	ν_0	ν_8		$\nu_4+\nu_8$
	Niide et al. ³⁷	This work	Brumfield et al. ^{26,a}	This work ^a
Origin		1196.957031(14)	1196.957052(52)	1367.727286(37)
A	0.8675192	0.86265314(19)	0.8626518(25)	0.86629162(46)
B	0.0408047	0.04082189(2)	0.0408228(16)	0.04076770(20)
C	0.0392537	0.03923653(2)	0.0392382(14)	0.03924246(20)
$\Delta D_k \times 10^7$ ^b		-1.956(5)	-2.17(22)	-2.064(9)
$D_k \times 10^7$	-3.810	-3.813(2)		
$D_j \times 10^9$	7.749	7.8032(3)		
$d_1 \times 10^{10}$	-6.44	-6.531(7)		
$d_2 \times 10^9$	-1.03	-1.0507(4)		
$N(K_a)$		24	12	25
J_{max}		144	13	80
$N(\text{trans})$		3549	123	386
N_{uniq}		1512	86	97
RMS		0.00036	0.00023	0.00043

^a: Values of D_k , D_j , d_1 , and d_2 were fixed to their ground state constants based on microwave measurements of Niide et al.³⁷

^b: $\Delta D_k = D'_k - D''_k$, with $D'_k(\nu_8) = 1.290 \times 10^{-5} \text{ cm}^{-1}$ and $D''_k(\nu_4) = 1.240 \times 10^{-5} \text{ cm}^{-1}$.

The RMS error of the fit is defined as³⁶

$$\text{RMS} = \sqrt{\frac{\sum_i^{n_{\text{obs}}} (\text{Obs}_i - \text{Calc}_i)^2}{n_{\text{obs}} - n_{\text{par}}}}$$

where n_{obs} is the total number of assigned transitions, Obs_i and Calc_i are the observed and calculated frequencies of the i^{th} transition, respectively, and n_{par} is the number of floated parameters in the least squares fitting.

For the ν_8 fundamental band of $\text{CH}_2^{79}\text{Br}^{81}\text{Br}$, an RMS value of 0.00036 cm^{-1} (or 10.8 MHz) was obtained. This value is ~ 1.6 larger than the value of 0.00023 cm^{-1} reported by Brumfield *et al.*²⁶ However, the present spectroscopic model provides a more global description of the rovibrational structure, as it includes assignments up to $K_a = 24$ and $J_{\text{max}} = 144$, compared to $K_a = 12$ and $J_{\text{max}} = 13$ in the earlier study.²⁶ Actually, the RMS value reported by Brumfield *et al.* should be interpreted with consideration of the N_{uniq} contributing to the fit. While Q-subclusters were treated as single observed frequencies in their analysis, several coincident pairs of P- and R-

branch transitions with identical J and K_a and $\Delta K_c = \pm 1$ were counted as separate observed transitions, despite corresponding to the same experimentally unresolved line position. As discussed above, such coincidences arise naturally from the near-prolate asymmetric-top structure of CH_2Br_2 . When the RMS is evaluated using the N_{uniq} rather than the total number of assigned transitions, their RMS values would increase by $\sim 20\%$ on average for all isotopologues. It should also be noted that at room temperature the Q-subclusters assigned in the present work consist of substantially larger number of tightly packed transitions compared to those observed under supersonic jet conditions (with temperatures of $\sim 20 \text{ K}$).²⁶ As a result, the transitions contributing to each cluster span a broader Obs–Calc distribution at room temperature than the few transitions forming each cluster at low temperature (*vide infra*). Consequently, RMS values should be interpreted in the context of spectral congestion, and the extent of rovibrational state coverage.

Finally, the RMS value of 10.8 MHz for the ν_8 band obtained here corresponds to only $\sim 1/3$ of the Doppler full width of CH_2Br_2 at room temperature (33 MHz), demonstrating the high precision of comb-based FTS even at ambient conditions. By comparison, the RMS of $\sim 8 \text{ MHz}$ reported for the jet-cooled cw-CRDS spectrum corresponds to roughly 60% of the linewidth (of 13.5 MHz) of the narrow transitions measured in the jet. These comparisons further illustrate that, despite the broader Doppler-limited conditions and substantially larger rovibrational state coverage considered in the present work, the achieved fit precision remains competitive with that obtained in jet-cooled measurements. Combining such broadband comb measurements with supersonic sources or buffer gas cooling methods,^{20, 22} will provide an unambiguous assignment with ultimate accuracy and precision.

For the $\nu_4+\nu_8-\nu_4$ hot band, an RMS value of 0.00043 cm^{-1} (or 12.9 MHz) was obtained from 97 unique frequencies, with assignments extending up to $K_a = 25$ and $J_{\text{max}} = 80$ (see Table 1). The fit involved five floated parameters ($n_{\text{par}} = 5$), limited to the band origin, the rotational constants, and the quartic centrifugal constant D_k , while the remaining parameters listed in Table 1 were fixed to their ν_0 values in both lower and upper states.



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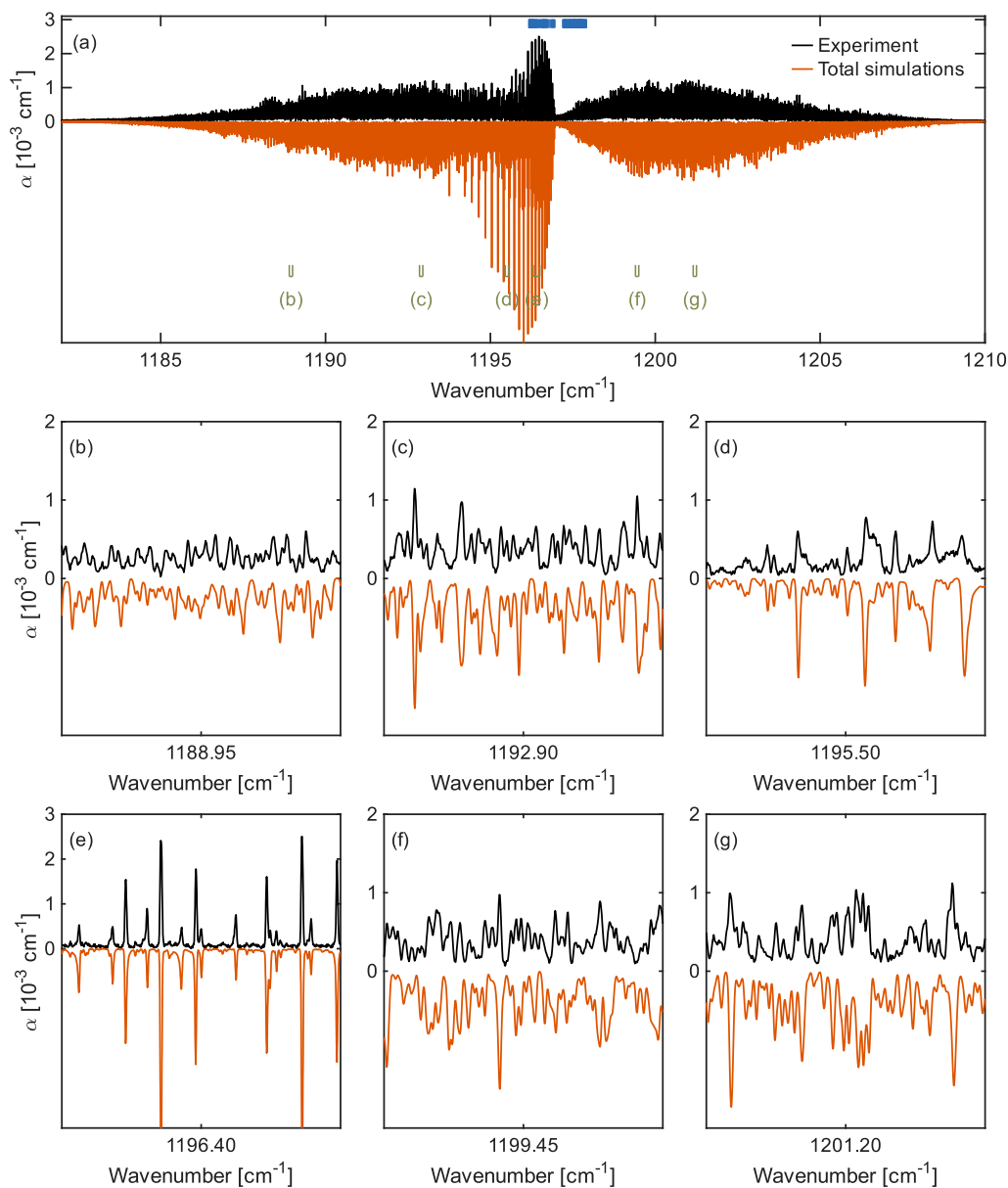


Fig. 5 (a) Comparison of the absorption coefficient of CH_2Br_2 measured at 50.2 μbar (black) with the overall PGOPHER simulations (orange). The PGOPHER simulations were performed for a Doppler FWHM of 0.0011 cm^{-1} and no Lorentzian contribution. The central part of the fundamental band is saturated because of the strong absorption signal. The blue vertical bars in the top panel indicate the 297 transitions ($N_{\text{uniq}} = 213$ unique frequencies) for the ν_3 band of the three isotopologues assigned by Brumfield *et al.*²⁶ from CRDS measurements combined with a supersonic jet. (b) – (g) Zoomed-in spectral windows at different parts of the spectrum.



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Table 2 The band parameters of the fundamental ν_8 and the hot $\nu_4+\nu_8-\nu_4$ bands for the $\text{CH}_2^{79}\text{Br}_2$ and $\text{CH}_2^{81}\text{Br}_2$ isotopologues (all in cm^{-1}), the number of K_a and J_{max} assignments, the number of assigned transitions, $N(\text{trans})$, the number of unique frequencies assigned to the experiment (N_{uniq}) and their root-mean-square (RMS) values (in cm^{-1}). Values in parentheses are 1σ uncertainties.

	$\text{CH}_2^{79}\text{Br}_2$				$\text{CH}_2^{81}\text{Br}_2$			
	ν_0	ν_8		$\nu_4+\nu_8$	ν_0	ν_8		$\nu_4+\nu_8$
	Davis & Gerry ³⁸	This work ^a	Brumfield <i>et al.</i> ^{26, a}	This work ^a	Davis & Gerry ³⁸	This work	Brumfield <i>et al.</i> ^{26, a}	This work ^a
Origin		1196.982451(22)	1196.982565(56)	1368.679265(46)		1196.931404(21)	1196.931350(46)	1366.713846(45)
A	0.8683441	0.86347446(33)	0.8634374(31)	0.86696106(47)	0.8667564	0.86189101(29)	0.8618897(32)	0.86545019(52)
B	0.0413131	0.04132770(8)	0.0413299(24)	0.04129157(90)	0.0402973	0.040306916(80)	0.0403157(14)	0.03997084(68)
C	0.0397255	0.03971131(7)	0.0397103(22)	0.03973530(97)	0.0387823	0.038772105(82)	0.0387663(13)	0.03845840(79)
$\Delta_K \times 10^5$	1.2922	1.27231(6)	1.2676(22)	1.24040(8)	1.2879	1.26860(6)	1.2667(33)	1.2071(1)
$\Delta_{JK} \times 10^7$	-3.8403	-3.8388(7)			-3.7483	-3.8186(6)		
$\Delta_J \times 10^9$	7.9321	8.139(2)			7.5662	7.596(2)		
$\delta_J \times 10^{10}$	5.2279	4.699(56)			4.8773	6.06(8)		
$\delta_K \times 10^8$	3.93	3.9247(2)			3.782	3.7726(4)		
$N(K_a)$		25	13	25		24	11	22
J_{max}		71	13	42		101	12	31
$N(\text{trans})$		663	92	254		1257	82	189
N_{uniq}		265	67	42		575	60	24
RMS		0.00037	0.00027	0.00040		0.00037	0.00022	0.00028

^a: Values of Δ_{JK} , Δ_J , δ_J , and δ_K were fixed to their ground state constants based on microwave measurements of Davis and Gerry.³⁸

Table 2 summarizes the band parameters of the fundamental ν_8 band for the light and heavy isotopologues obtained from the present room-temperature comb measurements and those reported by Brumfield *et al.*²⁶ from CRDS at supersonic temperature. Also included in this table are the band parameters of the $\nu_4+\nu_8-\nu_4$ hot bands obtained from the present work. Similar to the mixed isotopologue, the uncertainties of the ν_8 band origins of the light and heavy isotopologues obtained here are about a factor of two smaller than those reported by Brumfield *et al.*²⁶ while for the rotational constants they are lower by about one order of magnitude. For $\text{CH}_2^{79}\text{Br}_2$, the difference in the ν_8 band origin between the two studies is $1.14 \times 10^{-4} \text{ cm}^{-1}$, which is within $\sim 2\sigma$ of the combined uncertainties. The rotational constants A, B, and C differ by $3.7 \times 10^{-5} \text{ cm}^{-1}$, $-2.2 \times 10^{-6} \text{ cm}^{-1}$, and $1.0 \times 10^{-6} \text{ cm}^{-1}$, corresponding to $\approx 80\sigma$, 9σ , and 5σ of the combined uncertainties, respectively, and have a very large impact on the residuals of the assigned high J transitions (see below). Similarly, for the ν_8 band of $\text{CH}_2^{81}\text{Br}_2$, the band origins obtained in the two studies differ by only $5.4 \times 10^{-5} \text{ cm}^{-1}$ ($\sim 1.6 \text{ MHz}$), corresponding to about 1σ of the combined uncertainty. In contrast, the rotational constant A, B, and C differ by several σ , and again this difference is significant, and it reflects the impact of extended J and K_a coverage of the present assignment.

By comparing the RMS values for the ν_8 band of the light and heavy isotopologues with those from Brumfield *et al.*²⁶ the same arguments as for the mixed isotopologue apply. After accounting for the number of unique frequencies used in the fits, the RMS values obtained here are approximately 1.4 times larger for both $\text{CH}_2^{79}\text{Br}_2$ and $\text{CH}_2^{81}\text{Br}_2$ than those reported by Brumfield *et al.* Importantly, the present results are based on substantially broader rovibrational

coverage, extending up to $K_a = 25$ and $J_{\text{max}} = 71$ for $\text{CH}_2^{79}\text{Br}_2$ (compared to $K_a = 13$ and $J_{\text{max}} = 13$), and up to $K_a = 24$ and $J_{\text{max}} = 101$ for $\text{CH}_2^{81}\text{Br}_2$ (compared to $K_a = 11$ and 12). As a result, the derived parameters represent global effective values that provide an improved description of the rovibrational structure, as reflected in the fit residuals.

Fit residuals. Fig. 6 shows the residuals of the least squares fit to wavenumbers of a total of 2515 uniquely assigned transitions in the ν_8 band as a function of J and K_a quantum numbers for the $\text{CH}_2^{79}\text{Br}^{81}\text{Br}$ (green), $\text{CH}_2^{79}\text{Br}_2$ (red), and $\text{CH}_2^{81}\text{Br}_2$ (blue) [panel (a)]. The residuals are randomly scattered around zero for transitions with quantum numbers up to $J = J_{\text{max}}$ and $K_a = N(K_a)$ for each isotopologue – see Tables 1 and 2. As can be seen in Fig. 6, the assignment of clustered $Q(J, K_a, K_c)$ transitions to a single observed peak results in larger residual spread for these transitions. For example, at the highest $K_a = 24$ of $\text{CH}_2^{81}\text{Br}_2$ in Fig. 6(a), this large vertical spread of residuals comes from the multiple $Q(24)$ sub-cluster transitions being assigned to the same frequency. Such spread adds to the overall RMS error budget.

Applying the band parameters reported by Brumfield *et al.*²⁶ to the broadband dataset assigned here results in systematic deviations at higher J values, as shown in panel (b) (note the different vertical scale). In contrast, simulations based on the present parameters exhibit significantly reduced deviations across the full range of J and K_a . The large residuals observed at high J and K_a when using band parameters from earlier work are attributed to small difference in rotational constants (A , B , and C) and to the use of ground state centrifugal distortion constants (D_J , D_{JK} , D_K) for the excited state, as the limited number of transitions did not allow for floating these parameters. Such high sensitivity of the fit residuals to small



differences in spectroscopic parameters is enabled by the broadband coverage and high frequency precision of the comb-based Fourier transform spectrometer.

The fit residuals of the $\nu_4+\nu_8-\nu_4$ hot band transitions for all three isotopologues are shown in panel (c) of Fig. 6. No systematic trends are observed as a function of J or K_a , although systematic deviations may appear at $J > J_{\max}$ assigned here.

Finally, it should be noted that the average (from all isotopologues) RMS error of $\sim 0.00037 \text{ cm}^{-1}$ ($\sim 11.1 \text{ MHz}$) is about 4 times larger than the experimental frequency uncertainty (2.4 MHz – see Experimental Section). This clearly indicates that the average error is limited by the spectroscopic model rather than the experimental precision. This is not unexpected given the complexity of the room-temperature spectra and the existence of several other additional unassigned absorption peaks, most likely due to higher-order hot bands (e.g., $2\nu_4+\nu_8-2\nu_4$ and $3\nu_4+\nu_8-3\nu_4$). In addition, the natural isotopic composition of bromine leads to overlapping contributions from multiple isotopologues, further increasing the spectral congestion. These challenges limit the band-by-band empirical analysis and motivate the use of a more global spectroscopic description capable of accounting for interactions between multiple vibrational states simultaneously.

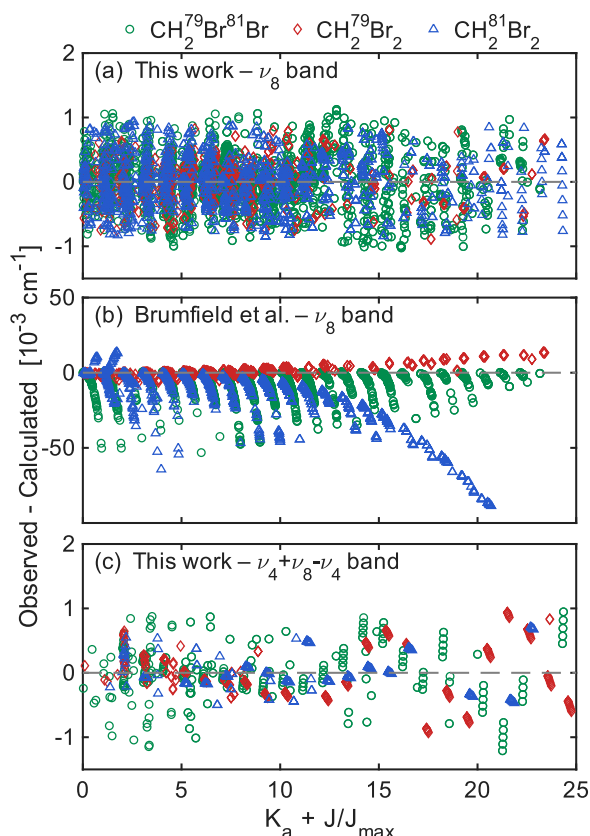


Fig. 6 Residuals between the observed transition wavenumbers and those from a PGOPHER fit (Obs - Calc) as a function of the upper state K and J quantum numbers of the ν_8 band for (a) our work and (b) using the band parameters of Brumfield *et al.*,²⁶ and (c) of the $\nu_4+\nu_8-\nu_4$ band for the three isotopologues: $\text{CH}_2^{79}\text{Br}^{81}\text{Br}$ (green), $\text{CH}_2^{79}\text{Br}_2$ (red), and $\text{CH}_2^{81}\text{Br}_2$ (blue) from our work.

3.2.2 Non-empirical (*ab initio*-based) spectral calculations

In contrast to the band-by-band analysis performed with PGOPHER, the simulations based on the *ab initio*-based effective Hamiltonian formalism³⁰ follow a more global description of the rovibrational structure. In this approach, vibrational states that are connected through anharmonic resonances are grouped into polyads and described by a common effective Hamiltonian that incorporates the relevant coupling interactions. In the polyad-based treatment, fundamental bands and associated hot bands can therefore be handled within the same theoretical framework, allowing resonance interactions between the contributing states to be naturally accounted for. Such a global description is particularly advantageous as it allows to: (i) simulate broadband spectra of polyatomic molecules, where overlapping bands and vibrational couplings can significantly complicate the measured spectra, (ii) compute absolute line strengths of rovibrational transitions, whereas the empirical PGOPHER approach typically provides relative intensities.

Figure 7 shows the calculated rovibrational line strengths of the fundamental ν_8 transition polyad ($P_0 \rightarrow P_7$) and the corresponding hot band $\nu_4+\nu_8-\nu_4$ polyad transitions ($P_1 \rightarrow P_8$) for the three isotopologues. The intensities shown in this figure already account for the natural isotopic abundances of ^{79}Br and ^{81}Br (0.5069 and 0.4931, respectively).³⁵ Here, the nuclear spin statistical weight of the C_{2v} and C_s species are 9:7 and 16:16 for the $A:B$ and $A':A''$ symmetries, respectively. They were used to compute the values of the partition functions given by 2243730 and 4557407 for the C_{2v} and C_s species, respectively. For the mixed isotopologue, the peak intensity is $4.54 \times 10^{-21} \text{ cm}^{-1}/(\text{molecule}\cdot\text{cm}^{-2})$, which is almost twice as large as the light and heavy isotopologues, with maxima of 2.65×10^{-21} and $2.47 \times 10^{-21} \text{ cm}^{-1}/(\text{molecule}\cdot\text{cm}^{-2})$, respectively. The corresponding $P_1 \rightarrow P_8$ hot band intensities are 1.97×10^{-21} , 1.15×10^{-21} , and $1.1 \times 10^{-21} \text{ cm}^{-1}/(\text{molecule}\cdot\text{cm}^{-2})$ for the mixed, light, and heavy isotopologues, respectively, representing $\sim 43\%$ (on average) of the fundamental band intensities. This is in a good agreement with the simple Boltzmann prediction of $\sim 44\%$ of population distributions at room temperature. This also indicates the significance of polyad interactions in the *ab initio* effective Hamiltonian approach, which captures couplings and predicts the intensities of the different vibrational bands accurately.



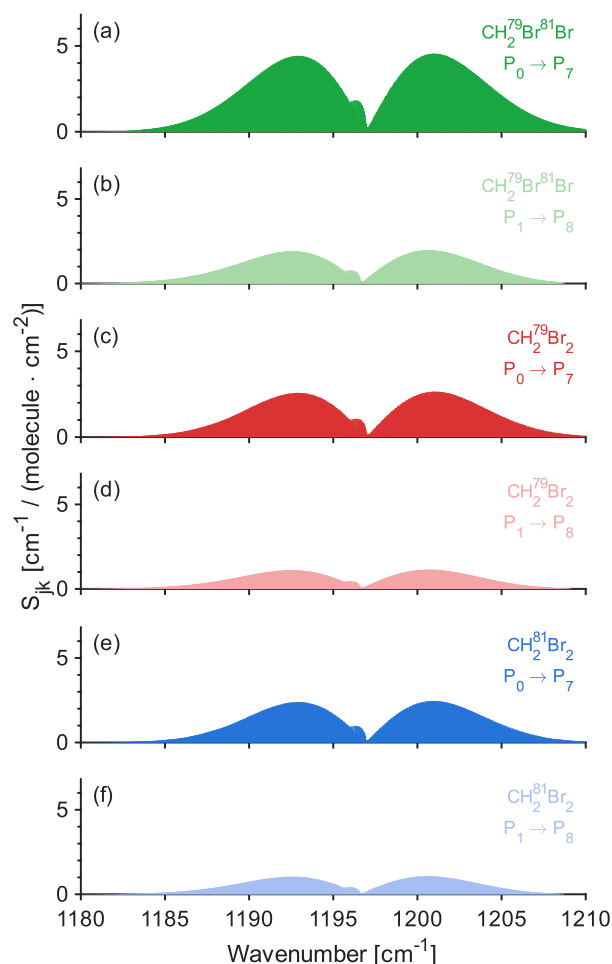


Fig. 7 Calculated *ab initio*-based intensities of the fundamental ($P_0 \rightarrow P_7$) polyad rovibrational transitions and the hot band ($P_1 \rightarrow P_8$) transitions in the 1180 to 1210 cm^{-1} spectral region for the three isotopologues of dibromomethane: $\text{CH}_2^{79}\text{Br}^{81}\text{Br}$ [green – panels (a) and (b)], $\text{CH}_2^{79}\text{Br}_2$ [red – panels (c) and (d)], and $\text{CH}_2^{81}\text{Br}_2$ [blue – panels (e) and (f)].

Figure 8 presents the differences in line positions between empirically assigned transitions (Obs) and the *ab initio*-based effective Hamiltonian calculations (Calc) for the ν_8 and $\nu_4 + \nu_8 - \nu_4$ bands of the mixed isotopologue. The majority of transitions are reproduced with small residuals, resulting in RMS values of 0.008 cm^{-1} for the 2007 ν_8 transitions up to $J_{\text{max}} = 80$ in panel (a), and 0.007 cm^{-1} for the 365 transitions of $\nu_4 + \nu_8 - \nu_4$ shown in panel (b). These values are, however, about 22 times larger than those obtained from empirical fit (see Table 1).

A distinct ‘anomaly’ is observed around $K_a = 16$ and 17, where residuals reach 0.07 and 0.05 cm^{-1} , respectively. This anomaly was not observed in the empirical fit (see Fig. 6(a)), as it is likely absorbed by the floating of rotational and centrifugal distortion constants in PGOPHER analysis. However, for high- J transitions of $K_a = 16$ and 17 that were not included in the empirical fit, this anomaly can become visible, as it can no longer be compensated by the fitted parameters. Excluding transitions with $|\text{Obs} - \text{Calc}| > 0.02 \text{ cm}^{-1}$ in Fig. 8(a) results in an RMS value of 0.003 cm^{-1} .

Such anomaly in Fig. 8(a) could be possibly attributed to the fact that the *ab initio* model incorporates numerous diagonal and non-

diagonal parameters associated with vibrational bands that are not experimentally observed. These parameters were therefore fixed to their *ab initio* values, which are likely not sufficiently accurate. For example, the trend observed in Fig. 8 appears correlated with the Coriolis coupling between the ν_8 and $\nu_3 + \nu_9$ bands. The maximum contribution of this coupling to the $\nu_8 = 1$ energy levels is $\sim 0.5 \text{ cm}^{-1}$, at $K_a = 16$. This incomplete refinement is also expected to influence the line strength of coupled vibrations, such effects cannot be resolved unambiguously using the present room temperature, highly congested spectrum. One possible route to improve the quality of the *ab initio* effective coupling parameters is to enhance the accuracy of the PES by optimizing certain force constants. In Fig. 8(b), several outliers in the $\nu_4 + \nu_8 - \nu_4$ hot band do not follow the overall trend and may reflect misassignments of these weak transitions.

This behaviour reflects the distinct treatment of molecular interactions in the two approaches. In the empirical PGOPHER analysis, the experimental spectrum is reproduced by adjusting rotational constants and centrifugal distortion parameters, resulting in effective spectroscopic constants that implicitly account for weak perturbations between interacting states. In contrast, the *ab initio*-based effective Hamiltonian explicitly treats such interactions within the polyad framework, providing a more detailed picture of the molecular interactions. Therefore these large residuals around $K_a = 16$ and 17 may also indicate a local coupling that is not yet accounted for in the *ab initio*-based effective Hamiltonian.

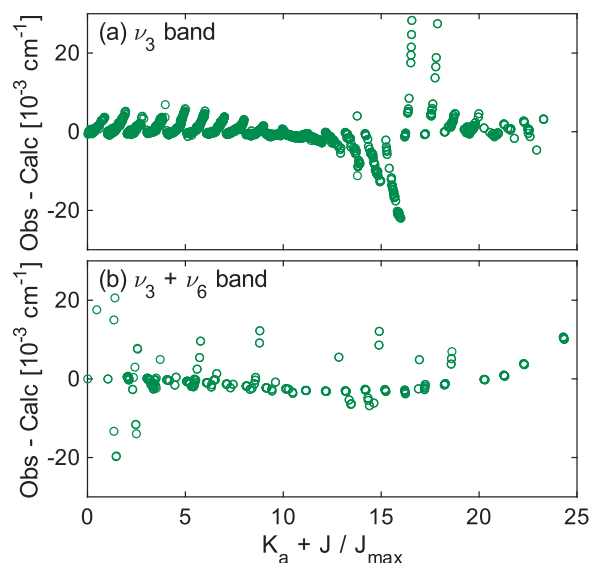


Fig. 8 (a) Residuals of the transition wavenumber ($\text{Obs} - \text{Calc}$) of $\text{CH}_2^{79}\text{Br}^{81}\text{Br}$ from *ab initio*-based effective Hamiltonian calculations as a function of the upper state K_a and J quantum numbers: (a) the ν_8 band, comprising 2007 transitions up to $J_{\text{max}} = 80$; (b) the $\nu_4 + \nu_8 - \nu_4$ band, comprising 365 transitions up to $J_{\text{max}} = 80$.

The calculated *ab initio*-based line intensities were subsequently used to determine the absorption cross-sections and compared with the experimental data. Fig. 9(a) shows the simulated absorption cross-sections together with PNNL reference spectrum (black). The *ab initio* spectra were simulated using a Voigt line-shape function, with the self-pressure broadening being almost negligible at the measurement pressure of $31 \mu\text{bar}$, and set to a value of 0.2 cm^{-1}



1-atm^{-1} , typical for halogenated molecules.³⁵ The spectra were then convolved with a *sinc* function to reproduce the resolution of the PNNL spectrum.

The contributions of the different polyads are also shown. In this spectral region, the dominant contribution arises from the $P_0 \rightarrow P_7$ polyad (cyan), mainly associated with the fundamental ν_8 band, accounting for $\sim 50\%$ of the total cross-section. Inclusion of higher polyads, dominated by hot-band transitions originating from the low-lying ν_4 mode, gradually improves the agreement with experiment. Specifically, adding the $P_1 \rightarrow P_8$ polyad (green), dominated by the $\nu_4 + \nu_8 - \nu_4$ hot band, increases the agreement to 72%. Further inclusion of the $P_2 \rightarrow P_9$ (blue) and $P_3 \rightarrow P_{10}$ (red) polyads, dominated by $2\nu_4 + \nu_8 - 2\nu_4$ and $3\nu_4 + \nu_8 - 3\nu_4$ transitions, respectively, improves the agreement to 83%.

The remaining discrepancy (17%) is attributed to contributions from higher polyads, e.g., $P_4 \rightarrow P_{11}$, involving transitions such as $\nu_9 + \nu_8 - \nu_9$ and $(\nu_3 + \nu_4) + \nu_8 - (\nu_3 + \nu_4)$, which are not included due to insufficient accuracy of their band centres. Inclusion of these bands without further refinement leads to distortions in the simulated spectral contour.

Figure 9(b) shows the relative difference in cross-section ($\Delta\sigma$, in %) between the simulated and PNNL spectra. The largest discrepancies are observed in the band wings, indicating missing contributions from higher-order hot bands and limitations in the current model, particularly at high- J values.

Apart from the remaining higher polyads, several factors may contribute to the remaining discrepancies. (i) Uncertainties in the PNNL reference data; according to the metadata, a small rescaling of 1.016 was applied to account for impurities. (ii) The existence of a nearby weak bands in the lower wavenumber range that is not included in the present simulations of Fig. 9. (iii) Limitations of the theoretical model; the dipole moment surface used here was constructed for the $\text{CH}_2^{79}\text{Br}_2$ isotopologue, whereas the mixed isotopologue dominates experimentally, and the treatment of isotopic effects on transition frequencies and intensities remain a challenge for *ab initio* calculations. Finally, (iv) the completeness of the line list is limited by the convergence with respect to rotational excitation and hot-band contributions. For a heavy molecule such as CH_2Br_2 , the density of states increases rapidly with energy, making it computationally demanding to include all relevant transitions. The combined variational-effective Hamiltonian approach employed here provides a practical solution, but the polyad formalism becomes less reliable at high- J , where interactions between states become increasingly complex. A more complete treatment will be presented in an accompanying theoretical study, aiming to provide *ab initio*-based line positions and intensities up to 2000 cm^{-1} .

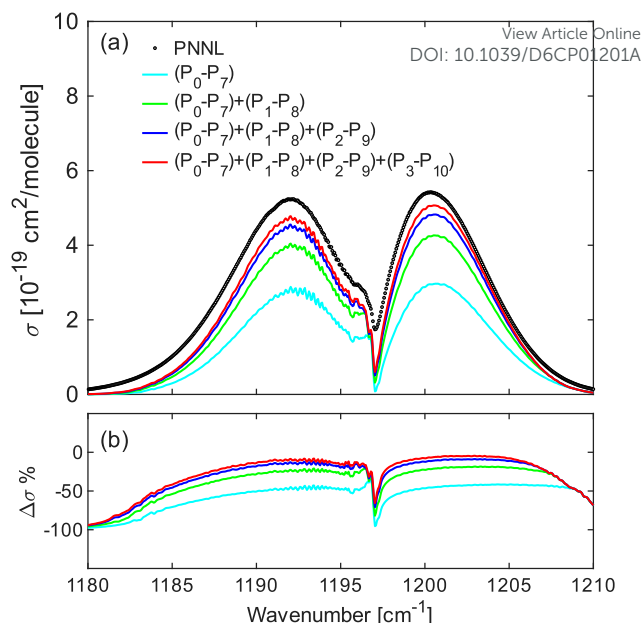


Fig. 9 (a) Absorption cross-section, σ , of CH_2Br_2 at room temperature simulated from *ab initio*-based effective Hamiltonian model, including successive contribution from $(P_0 \rightarrow P_7)$, $(P_0 \rightarrow P_7) + (P_1 \rightarrow P_8)$, $(P_0 \rightarrow P_7) + (P_1 \rightarrow P_8) + (P_2 \rightarrow P_9)$, and $(P_0 \rightarrow P_7) + (P_1 \rightarrow P_8) + (P_2 \rightarrow P_9) + (P_3 \rightarrow P_{10})$, compared with the PNNL database. (b) Relative differences in cross-section ($\Delta\sigma$, %) between the simulated and PNNL spectra.

Conclusions

We report the first high-resolution absorption cross-section of CH_2Br_2 in the long-wave mid-infrared region from 1180 to 1210 cm^{-1} . This spectral range is dominated by the intense CH_2 wagging vibration (ν_8 band), which is ~ 50 stronger than the C–H stretch vibrations in the $3.3\text{ }\mu\text{m}$ region. This makes it particularly suitable for spectroscopic detection of CH_2Br_2 in applications such as workplace safety monitoring, where it can occur as a by-product in treated ballast water, as well as in environmental sensing. The reported cross-section shows an overall good agreement across the entire ν_8 band region with the low-resolution FT-IR measurements of the PNNL database.²⁴

A spectroscopic model of the measured spectrum is developed for this asymmetric top molecule based on an empirical fitting, as implemented in GOPHER. The model explicitly accounts for the natural isotopic abundances of ^{79}Br and ^{81}Br , and for the presence of $\nu_4 + \nu_8 - \nu_4$ hot bands cross-interfering with the fundamental ν_8 bands. Band parameters (origin, rotational constants, and centrifugal distortion constants) of both the ν_8 fundamental and the $\nu_4 + \nu_8 - \nu_4$ hot bands were determined for all three isotopologues. Compared to previously reported band parameters retrieved from a fit to narrowband (1.78 cm^{-1}) supersonically cooled spectra,^{25, 26} the present broadband analysis provides global agreement between measured and simulated spectra across a wide range of rotational quantum numbers. A least squares fit of 2515 unique frequency assignments yields a root-mean-square error of 0.00037 cm^{-1} (or 11.1 MHz – average of the six bands). These assigned transitions were used to refine a non-empirical, *ab initio* based effective Hamiltonian for calculating a first complete line list of CH_2Br_2 isotopologues. Successive inclusion



of the dominant polyads – $P_0 \rightarrow P_7$, $P_1 \rightarrow P_8$, $P_2 \rightarrow P_9$, and $P_3 \rightarrow P_{10}$ – corresponding mainly to the ν_8 , the $\nu_4 + \nu_8 - \nu_4$, $2\nu_4 + \nu_8 - 2\nu_4$ and $3\nu_4 + \nu_8 - 3\nu_4$ bands, respectively, yields agreement with PNNL cross-section at the ~83% level. The remaining discrepancy is attributed primarily to the higher order polyads, e.g., $P_4 \rightarrow P_{11}$ involving bands such as $\nu_9 + \nu_8 - \nu_9$ and $(\nu_3 + \nu_4) + \nu_8 - (\nu_3 + \nu_4)$, which are not yet included due to insufficient accuracy of their band centres.

Overall, this study provides accurate high-resolution absorption cross-section data in the 8.35 μm spectral region, together with spectroscopic models for all three isotopologues of CH_2Br_2 in the CH_2 wagging vibrational region. The reliability of these models at high- J values still needs to be validated against cooled samples through broadband measurements, ideally at variable temperatures. Nevertheless, these results provide the necessary spectroscopic data (when relying on the strong peaks around the band centres) for optical monitoring of CH_2Br_2 in workplace and some environmental settings, particularly in harbour and ballast-water treatment contexts. In addition, it could enable quantitative assessments of the detectability of CH_2Br_2 in planetary atmospheres.

Author Contributions

Ibrahim Sadiék: Conceptualization, Formal analysis, Visualization, Project administration, Writing - Original draft preparation; **Aleksandr Balashov:** Investigation, Formal analysis, Software, Visualization, Writing - Review & Editing; **Adrian Hjältén:** Investigation, Formal analysis, Visualization, Writing - Original draft preparation; **Michael Rey:** Formal analysis, Software, Validation, Writing - Review & Editing; **Oleg Egorov:** Formal analysis, Writing - Review & Editing; **Aleksandra Foltynowicz:** Conceptualization, Supervision, Funding acquisition, Resources, Writing - Review & Editing.

Conflicts of interest

There are no conflicts to declare.

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References

1. J. H. Butler, D. B. King, J. M. Lobert, S. A. Montzka, S. A. Yvon-Lewis, B. D. Hall, N. J. Warwick, D. J. Mondeel, M. Aydin and J. W. Elkins, *Glob. Biogeochem. Cycles*, 2007, **21**, GB1023.
2. L. J. Carpenter, C. E. Jones, R. M. Dunk, K. E. Hornsby and J. Woeltjen, *Atmos. Chem. Phys.*, 2009, **9**, 1805-1816.

3. S. R. S.A. Montzka, S. O'Doherty, A. Engel, A.K. Kruger, W.T. Sturges, D. Blake, M. Dorf, P. Fraser, L. Froidevaux et al., *Scientific assessment of ozone depletion: 2010*, World Meteorological Organization, Geneva Switzerland, 2011.
4. H. Hepach, B. Quack, F. Ziska, S. Fuhlbrügge, E. L. Atlas, K. Krüger, I. Peeken and D. W. R. Wallace, *Atmos. Chem. Phys.*, 2014, **14**, 1255-1275.
5. B. Quack, E. Atlas, G. Petrick and D. W. R. Wallace, *J. Geophys. Res. Atmos.*, 2007, **112**, D09312.
6. IMO, International Convention for the Control and Management of Ships' Ballast Water and Sediments (BWM), 2017, pp. 1–38.
7. A. D. Shah, Z.-Q. Liu, E. Salhi, T. Höfer, B. Werschkun and U. von Gunten, *Environ. Sci.: Water Res. Technol.*, 2015, **1**, 465-480.
8. R. Xue, H. Shi, Y. Ma, J. Yang, B. Hua, E. C. Inniss, C. D. Adams and T. Eichholz, *Chemosphere*, 2017, **189**, 349-356.
9. G. Ziegler, M. Gonsior, D. J. Fisher, P. Schmitt-Kopplin and M. N. Tamburri, *Environ Sci Technol*, 2019, **53**, 8006-8016.
10. M. Leung, E. W. Schwieterman, M. N. Parenteau and T. J. Fauchez, *Astrophys. J.*, 2022, **938**, 6.
11. J. Maas, S. Tegmeier, B. Quack, A. Biastoch, J. V. Durgadoo, S. Rüks, S. Gollasch and M. David, *Ocean Sci.*, 2019, **15**, 891-904.
12. S. K. Scholten, C. Perrella, J. D. Anstie, R. T. White and A. N. Luiten, *Phys. Rev. Appl.*, 2019, **12**, 034045.
13. D. M. Bailey, G. Zhao and A. J. Fleisher, *Anal. Chem.*, 2020, **92**, 13759-13766.
14. A. Parriaux, K. Hammani, C. Thomazo, O. Musset and G. Millot, *Phys. Rev. Res.*, 2022, **4**, 023098.
15. I. Sadiék, A. Hjältén, F. C. Roberts, J. H. Lehman and A. Foltynowicz, *Phys. Chem. Chem. Phys.*, 2023, **25**, 8743-8754.
16. A. Hjältén, I. Sadiék and A. Foltynowicz, *J. Quant. Spectrosc. Radiat. Transfer*, 2025, **340**, 109452.
17. I. Sadiék, A. Hjältén, G. Friedrichs and A. Foltynowicz, *J. Am. Chem. Soc.*, 2025, **147**, 38110-38127.
18. H. Timmers, A. Kowligy, A. Lind, F. C. Cruz, N. Nader, M. Silfies, G. Ycas, T. K. Allison, P. G. Schunemann, S. B. Papp and S. A. Diddams, *Optica*, 2018, **5**, 727-732.
19. K. Krzempek, D. Tomaszewska, A. Gluszek, T. Martynkien, P. Mergo, J. Sotor, A. Foltynowicz and G. Soboń, *Opt. Express*, 2019, **27**, 37435-37445.
20. P. B. Changala, M. L. Weichman, K. F. Lee, M. E. Fermann and J. Ye, *Science*, 2019, **363**, 49-54.
21. A. Hjältén, M. Germann, K. Krzempek, A. Hudzikowski, A. Gluszek, D. Tomaszewska, G. Soboń and A. Foltynowicz, *J. Quant. Spectrosc. Radiat. Transfer*, 2021, **271**, 107734.
22. N. Baradaran, D. Charczun, T. Nambiar, M. Zou, K. F. Lee, M. E. Fermann and M. L. Weichman, *Opt. Express*, 2026, **34**, 6751-6767.
23. I. Sadiék and G. Friedrichs, *Spectrochim. Acta A Mol. Biomol. Spectrosc.*, 2017, **181**, 180-191.
24. S. W. Sharpe, T. J. Johnson, R. L. Sams, P. M. Chu, G. C. Rhoderick and P. A. Johnson, *Appl. Spectrosc.*, 2004, **58**, 1452-1461.
25. B. E. Brumfield, J. T. Stewart, S. L. W. Weaver, M. D. Escarra, S. S. Howard, C. F. Gmachl and B. J. McCall, *Rev. Sci. Instrum.*, 2010, **81**, 063102.
26. B. E. Brumfield, J. T. Stewart and B. J. McCall, *J. Mol. Spectrosc.*, 2011, **266**, 57-62.



27. I. Sadiek, A. Hjältén, F. Senna Vieira, C. Lu, M. Stuhr and A. Foltynowicz, *J. Quant. Spectrosc. Radiat. Transfer*, 2020, **255**, 107263.
28. A. Hjältén, A. Foltynowicz and I. Sadiek, *J. Quant. Spectrosc. Radiat. Transfer*, 2023, **306**, 108646.
29. F. C. Roberts and J. H. Lehman, *J. Chem. Phys.*, 2022, **156**, 114301.
30. M. Rey, *J. Chem. Phys.*, 2022, **156**, 224103.
31. M. Germann, A. Hjältén, V. Boudon, C. Richard, K. Krzempek, A. Hudzikowski, A. Głuszek, G. Soboń and A. Foltynowicz, *J. Quant. Spectrosc. Radiat. Transfer*, 2022, **288**, 108252.
32. M. Germann, A. Hjältén, J. Tennyson, S. N. Yurchenko, I. E. Gordon, C. Pett, I. Silander, K. Krzempek, A. Hudzikowski, A. Głuszek, G. Soboń and A. Foltynowicz, *J. Quant. Spectrosc. Radiat. Transfer*, 2024, **312**, 108782.
33. P. Maslowski, K. F. Lee, A. C. Johansson, A. Khodabakhsh, G. Kowzan, L. Rutkowski, A. A. Mills, C. Mohr, J. Jiang, M. E. Fermann and A. Foltynowicz, *Phys. Rev. A*, 2016, **93**, 021802(R).
34. L. Rutkowski, P. Maslowski, A. C. Johansson, A. Khodabakhsh and A. Foltynowicz, *J. Quant. Spectrosc. Radiat. Transfer*, 2018, **204**, 63-73.
35. I. E. Gordon, L. S. Rothman, R. J. Hargreaves, R. Hashemi, E. V. Karlovets, F. M. Skinner, E. K. Conway, C. Hill, R. V. Kochanov, Y. Tan, P. Wcisło, A. A. Finenko, K. Nelson, P. F. Bernath, M. Birk, V. Boudon, A. Campargue, K. V. Chance, A. Coustenis, B. J. Drouin, J. M. Flaud, R. R. Gamache, J. T. Hodges, D. Jacquemart, E. J. Mlawer, A. V. Nikitin, V. I. Perevalov, M. Rotger, J. Tennyson, G. C. Toon, H. Tran, V. G. Tyuterev, E. M. Adkins, A. Baker, A. Barbe, E. Canè, A. G. Császár, A. Dudaryonok, O. Egorov, A. J. Fleisher, H. Fleurbaey, A. Foltynowicz, T. Furtenbacher, J. J. Harrison, J. M. Hartmann, V. M. Horneman, X. Huang, T. Karman, J. Karns, S. Kassi, I. Kleiner, V. Kofman, F. Kwabia-Tchana, N. N. Lavrentieva, T. J. Lee, D. A. Long, A. A. Lukashetskaya, O. M. Lyulin, V. Y. Makhnev, W. Matt, S. T. Massie, M. Melosso, S. N. Mikhailenko, D. Mondelain, H. S. P. Müller, O. V. Naumenko, A. Perrin, O. L. Polyansky, E. Raddaoui, P. L. Raston, Z. D. Reed, M. Rey, C. Richard, R. Tóbiás, I. Sadiek, D. W. Schwenke, E. Starikova, K. Sung, F. Tamassia, S. A. Tashkun, J. Vander Auwera, I. A. Vasilenko, A. A. Viganin, G. L. Villanueva, B. Vispoel, G. Wagner, A. Yachmenev and S. N. Yurchenko, *J. Quant. Spectrosc. Radiat. Transfer*, 2022, **277**, 107949.
36. C. Western, PGOPHER version 10.1. <http://pgopher.chm.bris.ac.uk>, 2018.
37. Y. Niide, H. Tanaka and I. Ohkoshi, *J. Mol. Spectrosc.*, 1990, **139**, 11-29.
38. R. W. Davis and M. C. L. Gerry, *J. Mol. Spectrosc.*, 1985, **109**, 269-282.
39. O. Egorov and M. Rey, *Molecules*, 2025, **30**, 4239.
40. O. Egorov and M. Rey, *Phys Chem Chem Phys*, 2026, **28**, 9536.
41. J. K. G. Watson, *Mol. Phys.*, 1968, **15**, 479-490.
42. M. Rey, A. V. Nikitin and V. G. Tyuterev, *Mol. Phys.*, 2010, **108**, 2121-2135.
43. M. Rey, A. V. Nikitin and V. G. Tyuterev, *J Chem Phys*, 2012, **136**, 244106.
44. M. Rey, *J Chem Phys*, 2019, **151**, 024101.
45. M. Rey and T. Carrington, Jr., *J Chem Phys*, 2024, **161**, 044102.
46. H.-J. Werner, P. J. Knowles, F. R. Manby, J. A. Black, K. Doll, A. Heßelmann, D. Kats, A. Köhn, T. Korona, D. A. Kreplin, Q. Ma, T. F. Miller, III, A. Mitrushchenkov, K. A. Peterson, I. Polyak, G. Rauhut and M. Sibaev, *J Chem Phys*, 2020, **152**, 144107.
47. H.-J. Werner, P. J. Knowles, G. Knizia, F. R. Manby, M. Schütz, P. Celani, T. Korona, R. Lindh, A. Mitrushchenkov and G. Rauhut, MOLPRO, version 2021.3, a package of ab initio programs. See <https://www.molpro.net>, 2021.
48. D. Mester, P. R. Nagy, J. Csóka, L. Gyevi-Nagy, P. B. Szabó, R. A. Horváth, K. Petrov, B. Hégyel, B. Ladóczki, G. Samu, B. D. Lőrincz and M. Kállay, *J Phys Chem A*, 2025, **129**, 2086-2107.
49. M. Kállay, P. R. Nagy, D. Mester, L. Gyevi-Nagy, J. Csóka, P. B. Szabó, Z. Rolik, G. Samu, B. Hégyel, B. Ladóczki, K. Petrov, J. Csontos, Á. Ganyecz, I. Ladjánszki, L. Szegedy, M. Farkas, P. D. Mezei, R. A. Horváth and B. D. Lőrincz, MRCC, a quantum chemical program suite 2019.
50. D. A. Matthews, L. Cheng, M. E. Harding, F. Lipparini, S. Stopkowicz, T.-C. Jagau, P. G. Szalay, J. Gauss and J. F. Stanton, *J Chem Phys*, 2020, **152**, 214108.
51. J. F. Stanton, J. Gauss, L. Cheng, M. E. Harding, D. A. Matthews, P. G. Szalay, A. A. Auer, R. J. Bartlett, U. Benedikt and C. Berger, CFOUR, a quantum chemical program package (Version 2.00beta). <http://www.cfour.de>.
52. A. Hjältén, V. Silva de Oliveira, I. Silander, A. Rosina, M. Rey, L. Rutkowski, G. Soboń, K. K. Lehmann and A. Foltynowicz, *J. Chem. Phys.*, 2024, **161**, 124311.



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“Optical frequency comb Fourier transform spectroscopy of the $\text{CH}_2^{79}\text{Br}^{81}\text{Br}$, $\text{CH}_2^{79}\text{Br}_2$ and $\text{CH}_2^{81}\text{Br}_2$ isotopologues in the 1180–1210 cm^{-1} region” by I. Sadiq, A. Balashov, A. Hjältén, M. Rey, O. Egorov, and A. Foltynowicz

The data supporting the findings of this study are available in the Supplementary Information of this article. This includes the experimentally measured absorption cross-section (S2), the PGOPHER input files used for the empirical spectroscopic analysis (S1), and the absorption cross-section simulated using PGOPHER (S3). Additional data related to this work are available from the corresponding author upon reasonable request.

