

Cite this: *J. Mater. Chem. A*, 2025, **13**, 9292

Category-specific topological learning of metal–organic frameworks†

Dong Chen,^a Chun-Long Chen ^b and Guo-Wei Wei ^{*acd}

Metal–organic frameworks (MOFs) are porous, crystalline materials with high surface area, adjustable porosity, and structural tunability, making them ideal for diverse applications. However, traditional experimental and computational methods have limited scalability and interpretability, hindering effective exploration of MOF structure–property relationships. To address these challenges, we introduce, for the first time, a category-specific topological learning (CSTL), which combines algebraic topology with chemical insights for robust property prediction. The model represents MOF structures as simplicial complexes and incorporates elemental categorizations to enable balanced, interpretable machine learning study. By integrating category-specific persistent homology, CSTL captures both global and local structural characteristics, rendering multi-dimensional, category-specific descriptors that support a predictive model with high accuracy and robustness across eight MOF datasets, outperforming all previous results. This alignment of topological and chemical features enhances the predictive power and interpretability of CSTL, advancing understanding of structure–property relationships of MOFs and promoting efficient material discovery.

Received 14th December 2024
Accepted 24th February 2025

DOI: 10.1039/d4ta08877h

rsc.li/materials-a

1 Introduction

Metal–organic frameworks (MOFs) are a unique class of porous materials made up of metal ions or clusters connected to organic ligands, forming crystalline structures with remarkable tunability. Their customizable properties, including high surface area, adjustable porosity, and structural versatility, make MOFs highly suitable for a range of applications,^{1–4} such as gas storage,⁵ separation,⁶ catalysis,^{7,8} and sensing.⁹ Although the design possibilities for MOFs are vast, with potentially infinite structures that can be synthesized. A thorough understanding of the relationship between MOF structure and its properties is therefore crucial for designing MOFs tailored to specific applications.^{10,11} However, challenges remain. Traditional experimental methods, while valuable for providing insights into MOF behavior, can be labor-intensive, costly, and limited in scope, hindering the ability to explore the extensive chemical space that MOFs occupy. Computational methods, such as molecular dynamics (MD),¹² enable the simulation of

atomic motion over time and can be performed using either classical force fields¹³ or first-principles methods, *i.e.*, density functional theory (DFT).¹⁴ As a first-principles approach, DFT provides a quantum mechanical description of material properties and can be used in MD simulations. However, both classical and DFT-based MD often face scalability challenges,¹⁵ making simulations computationally prohibitive, particularly for large or complex MOF systems, due to the extensive calculations required.^{16–19}

Given the limitations of traditional experimental and computational approaches in studying MOF structure–property relationships, advanced data-driven techniques have become essential. Machine learning (ML) has become increasingly important in studying MOF structure–property relationships and offering a possible solutions to those limitations.^{20–23} And thanks to the high-throughput computational screening, in particular, has emerged as a valuable approach, has laid a solid foundation by generating extensive, high-quality MOF databases,^{24,25} such as the CoRE MOF²⁶ and hMOF datasets,²⁷ which enable ML applications in MOF research. Recently, ML models have leveraged geometric descriptors of MOF structures, such as void fraction and pore volume, to predict gas adsorption properties with notable accuracy.^{28,29} For instance, energy grid histograms have been used as descriptors in ML models to predict gas uptake,³⁰ while other models utilize geometric, atom-type, and chemical feature descriptors to forecast N₂/O₂ selectivity and diffusivity.²⁸ Despite these advances, prediction accuracy remains a challenge for certain properties. The deep learning (DL) models are introduced, including convolution

^aDepartment of Mathematics, Michigan State University, MI, 48824, USA. E-mail: weig@msu.edu^bPhysical Sciences Division, Pacific Northwest National Laboratory, Richland, Washington 99354, USA. E-mail: chunlong.chen@pnl.gov^cDepartment of Electrical and Computer Engineering, Michigan State University, MI 48824, USA^dDepartment of Biochemistry and Molecular Biology, Michigan State University, MI 48824, USA† Electronic supplementary information (ESI) available. See DOI: <https://doi.org/10.1039/d4ta08877h>

neural networks, graph neural networks^{31,32} and transformer-based architectures,^{33–36} have further enhanced the predictive power for various MOF properties by harnessing large datasets. However, these models come with certain limitations: they can be computationally demanding, often require substantial amounts of data, and sometimes function as ‘black-box’ systems, presenting challenges for interpretability. Addressing these considerations through continued refinement will help enhance the accessibility and interpretability of ML, particularly in advancing MOF discovery.

To address challenges in MOF research, incorporating mathematically derived, explainable features is essential. These features enhance interpretability and contribute to more robust predictive models for MOF properties. Instead of relying solely on conventional descriptors,^{28,29} advanced mathematical tools from fields like geometry and topology can be employed to extract insightful, high-level features. Techniques such as algebraic graph theory,^{37,38} persistent homology,³⁹ element-specific persistent homology,⁴⁰ path topology,⁴¹ and topological Laplacians⁴² are increasingly used in molecular and materials science, offering new methods to capture the structural and functional nuances of complex materials. Mathematics-based methods have already shown success in fields such as drug discovery,³⁸ biological sciences,⁴³ and materials science,⁴⁴ linking structural features to machine learning models for interpretable and detailed representations. For instance, persistent hyperdigraphs have enabled accurate predictions of protein–ligand interactions by capturing essential molecular details within a rigorous mathematical and transformer framework.⁴⁵ Mathematical deep learning was a top winner for pose and binding affinity prediction and ranking in D3R Grand Challenges, a worldwide competition series in computer-aided drug design.^{46,47}

In this work, we propose a category-specific topological leaning (CSTL) model for predicting the properties of MOFs. This model introduces a mathematically sound and chemically informed framework designed to analyze and predict MOF properties by integrating both structural complexity and elemental composition. Specifically, each MOF structure is represented as a simplicial complex, establishing a robust topological basis for capturing the unique geometric features of MOFs. To enhance structural analysis with chemical insights, the model incorporates category-specific representations by categorizing elements based on valence electron similarity and occurrence frequency. This categorization ensures a balanced representation across the diverse elemental distributions of MOFs. For each elemental category, the model constructs tailored topological representations and applies persistent homology analysis. This method captures both global and local structural features using topological invariants, while also preserving detailed geometric information—particularly beneficial for materials with complex pore networks and spatially organized atomic structures. The model generates multi-dimensional, category-specific descriptors to encapsulate these intricate structural characteristics, which then serve as input to a gradient boosting tree model for predictive analysis. This approach provides an interpretable, chemically informed

framework for predicting a broad range of MOF properties, including eight gas selectivity datasets, with the state-of-the-art performance and improved robustness. By aligning topological features with elemental distributions, CSTL addresses the limitations of conventional approaches, advancing the understanding and prediction of structure–property relationships in MOF materials.

2 Results

2.1 Workflow and schematic of a category-specific topological model

Fig. 1a presents the workflow of our proposed category-specific topological model, designed to analyze and predict properties of MOF structures. In this workflow, the model begins by constructing a simplicial complex representation, which provides a robust topological framework tailored to capture the complex geometry of MOF materials. However, persistent homology itself is not enough for molecular modeling.^{40,43} To enhance the structural analysis of MOFs with chemical insights, we introduce category-specific topological representations, denoted as categories C_0 through C_7 and C_{all} , where C_{all} represents the full structure. The necessity of this categorization arises from the fact that different elements play distinct roles in MOF functionality, influencing stability, reactivity, and porosity. Grouping elements into categories facilitates a more systematic understanding of their contributions and interactions within the framework. To establish these categories, an elemental distribution analysis is first conducted across the dataset, as illustrated in Fig. 1b, highlighting the frequency of elements and grouping them based on valence electron similarity and occurrence frequency. Elements with comparable properties are analyzed collectively, while highly prevalent elements such as carbon (C) and hydrogen (H), which play fundamental roles in MOF structures, are assigned distinct categories. This structured approach enables a more insightful analysis of elemental contributions, ultimately improving our ability to interpret and predict MOF properties. Table 1 further specifies these element categories. Notably, the dataset exhibits a broad range of elements, with particular diversity among metallic elements, though specific metallic elements appear less frequently. The categorization process addresses these distribution variances, ensuring that infrequent elements are adequately considered within the predictive model to prevent overemphasis on particular elements' influence.

Based on these elemental categories, category-specific topological representations are constructed for each MOF structure using alpha complexes, which provide a categorized-level topology for these materials. The alpha complex is a type of simplicial complex that generalizes the concept of a graph. Unlike graphs, which capture only pairwise interactions, alpha complexes can represent higher-order interactions, making them well-suited for describing the structural complexity of MOFs. As illustrated in Fig. 5, the simplicial complex (Fig. 5a) can be decomposed into different dimensional components. The 0-simplices (Fig. 5b) correspond to individual points (atoms) in the structure. The 1-simplices, representing edges,



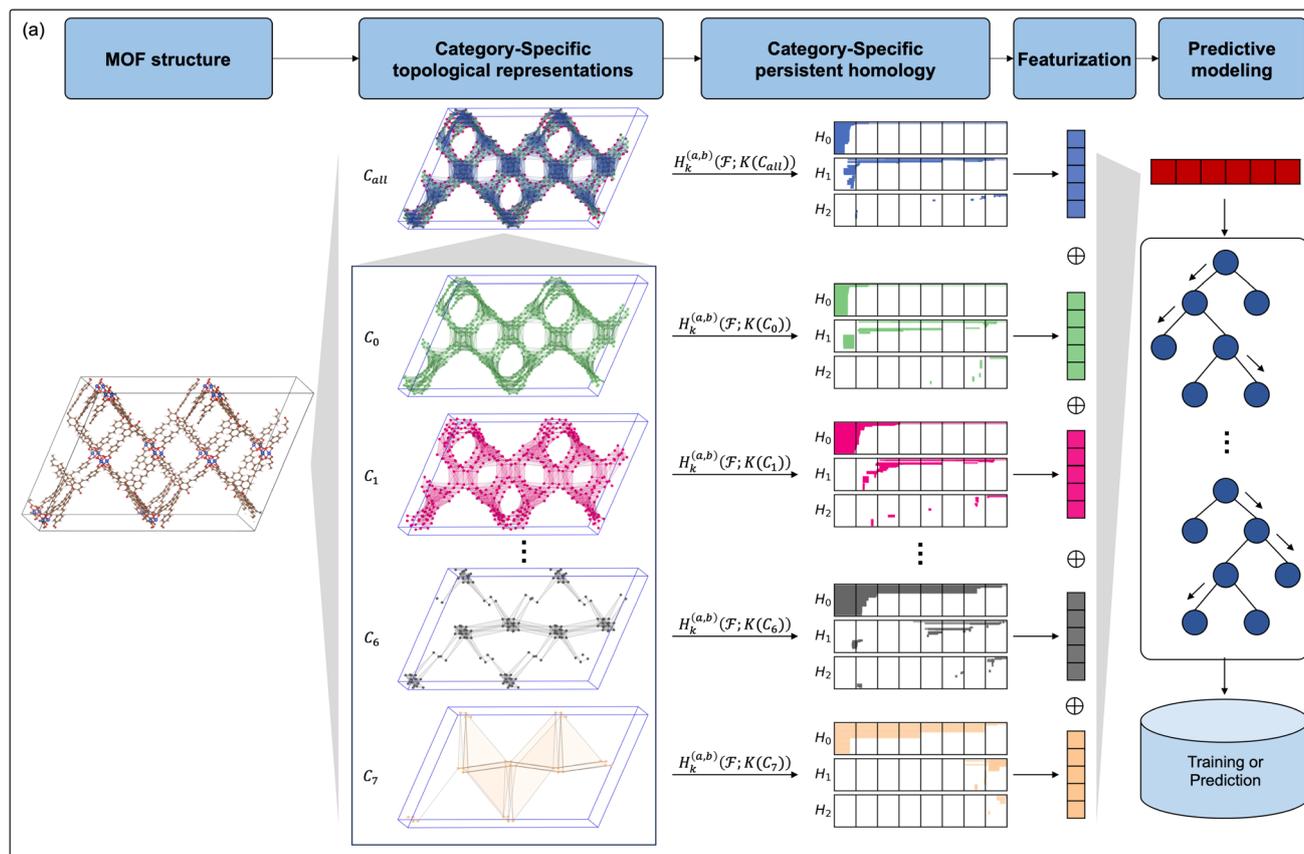


Fig. 1 Schematic for category-specific topological models in MOF property prediction. (a) Overview of the category-specific topological models used for predicting properties of MOFs. Given MOF structures (first column), category-specific topological representations are constructed, including a simplicial complex for all structures (C_{all}) and sub-complexes based on categories (C_0 to C_7). The persistent homology method is applied to each category to generate barcode representations. A featurization vector extracts features from these barcodes, which are then used to construct a gradient boosting tree model for predictions on specific datasets. (b) Element distribution across the CoRE MOF v2019 dataset. The y-axis indicates the number of MOFs present in the dataset, with elements categorized based on valence electron similarity and their frequencies in the dataset.

Table 1 Element categories for category-specific topological modeling of MOFs

Element category	Notation
Alkali metals, alkaline metals, and other metals	C_0
Transition metals, lanthanoids, actinoids	C_1
Metalloids	C_2
Halogens	C_3
Hydrogen (H)	C_4
Carbon (C)	C_5
Nitrogen (N), phosphorus (P)	C_6
Oxygen (O), sulfur (S), selenium (Se)	C_7
All	C_{all}

encode pairwise interactions, forming a molecular graph. The 2-simplices (Fig. 5c) capture three-body interactions, as they consist of triangles encompassing three points. Higher-order interactions are similarly represented by higher-dimensional simplices. To extract topological features from these complexes, we employ algebraic topology tools such as homology, which captures topological invariants of the structure. Specifically, in this work, we utilize rank of homology groups H_k for $k = 0, 1, 2$, corresponding to topological invariants in the first three dimensions, providing insights into connectivity, loops, and cavities within the MOF structures.

Subsequently, category-specific persistent homology analysis is applied, denoted as $H_k^{(a,b)}$, where $k = 0, 1, 2$ represents



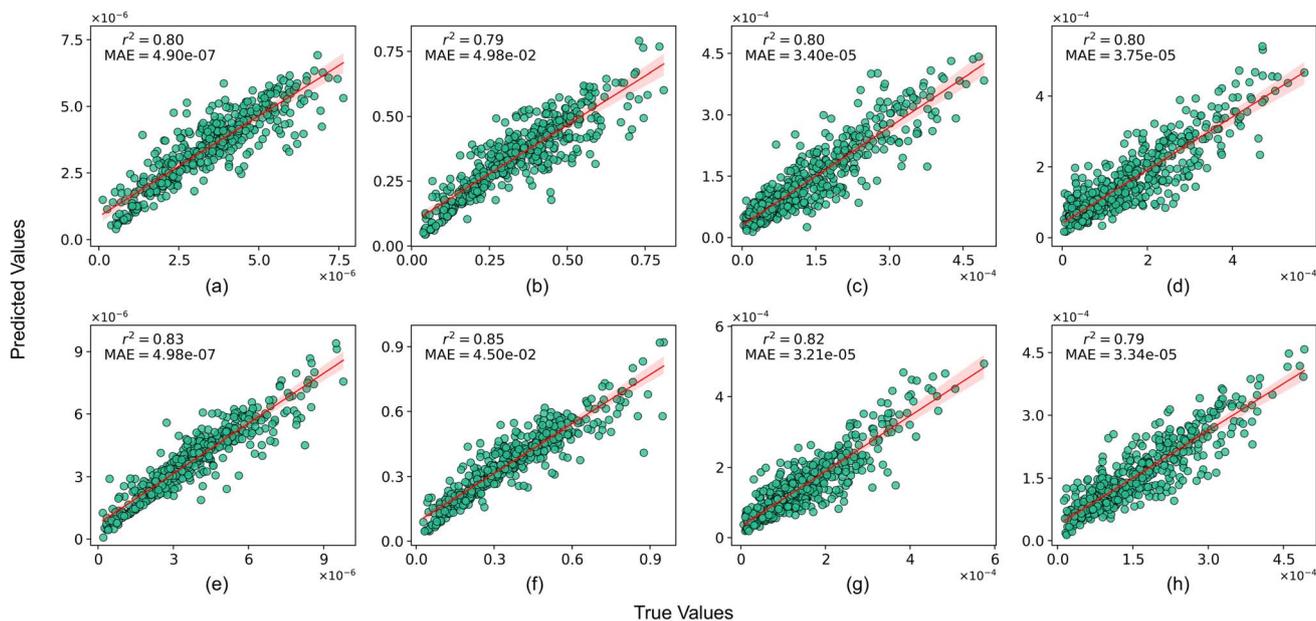


Fig. 2 Comparison between predicted and true values for eight datasets on O_2/N_2 selectivity properties in MOF materials. Panels (a–h) show prediction performance for different properties: Henry's constant for N_2/O_2 (a and e), N_2/O_2 uptake (mol kg^{-1}) (b and f), self-diffusivity of N_2/O_2 at 1 bar ($cm^2 s^{-1}$) (c and g), and self-diffusivity of N_2/O_2 at infinite dilution ($cm^2 s^{-1}$) (d and h). Each panel displays the r^2 and the MAE in the upper left corner. Each dataset was randomly split, with 80% used for training, with 10% reserved for testing.

different topological dimensions, and $a = 0$ to $b = 25$ defines the distance interval, allowing a detailed examination of structure across multiple scales. Multi-dimensional category-specific barcodes are then computed to capture geometric and topological information specific to each elemental category. Following this, a featurization step was introduced. In a previous study, Krishnapriyan *et al.*⁴⁸ proposed a method that used persistent homology to extract 1D and 2D topological features of MOF pores and channels by computing birth–death pairs across spatial scales. The resulting persistence diagram was then transformed into a 2D vectorized representation using Gaussian kernels and grid discretization. In contrast, instead of generating a 2D vectorized representation, we introduced a featurization step that bins barcodes into fixed intervals ranging from 0 to 25 Å with a resolution of 0.1 Å. This approach captures more geometric details while maintaining a manageable feature dimensionality, making the subsequent machine learning model more effective with limited data. Finally, these features are concatenated to create a comprehensive and category-specific topological descriptor, which is fed into a gradient boosting tree model for predictive modeling across various MOF properties. This approach ensures a balanced representation of elements within the model, enhancing predictive robustness and capturing the nuanced impacts of elemental distribution on MOF properties.

2.2 Properties prediction for MOFs

In this study, we validated the proposed category-specific topological models by predicting key properties of MOF materials, including the Henry's constant for N_2 and O_2 (mol kg^{-1} Pa $^{-1}$), uptake values for N_2 and O_2 (mol kg^{-1}), self-diffusivity of

N_2 and O_2 at 1 bar ($cm^2 s^{-1}$), and self-diffusivity at infinite dilution ($cm^2 s^{-1}$). Table 3 and the datasets section provide detailed descriptions of these datasets. The prediction outcomes, shown in Fig. 2, demonstrate close alignment between predicted and actual values across all eight datasets, with an 80 : 10 : 10 random split for training, validation, and testing, respectively.^{33,34} Performance metrics, specifically r^2 and MAE, averaged over 100 repeated experiments, are presented in the top left corner of each dataset's plot, underscoring the model's accuracy and reliability.

To benchmark the model's performance, we compared it with state-of-the-art models, including MOFTransformer³³ and PMTransformer,³⁴ both of which were trained on over a million structures for MOF property prediction. As shown in Table 2, the category-specific topological model consistently outperforms these models across all datasets, achieving superior r^2 , MAE, and RMSE metrics. It is noted that a universal set of hyperparameters was applied across all eight datasets to ensure robustness and prevent overfitting; validation data was not specifically used. In practical applications, incorporating the validation data into the training set could further enhance model accuracy.

Additionally, we evaluated model robustness by testing on a 20% holdout set across all datasets, with results shown in Fig. S1 and Table S1,† where the proposed model continued to outperform previous models. To ensure the validation stability, we trained 100 models using 10 different seeds, each repeated across 10 randomly initialized predictive models. Heatmaps in Fig. S2–S4† illustrate that variations in seed selection have minimal impact on model performance, confirming the robustness and stability of the predictive model across both



Table 2 Comparison of CSTL performance with published models across various MOF datasets

Datasets	CSTL			Descriptor-based ²⁸		MOFTransformer ³³		PMTransformer ³⁴
	r^2	MAE	RMSE	r^2	RMSE	r^2	MAE	MAE
Henry's constant N ₂	0.80	4.90×10^{-7}	7.25×10^{-7}	0.70	8.94×10^{-7}			
Henry's constant O ₂	0.83	4.98×10^{-7}	7.63×10^{-7}	0.74	9.60×10^{-7}			
N ₂ uptake (mol kg ⁻¹)	0.79	4.98×10^{-2}	7.37×10^{-2}	0.71	8.62×10^{-2}	0.78	7.10×10^{-2}	6.90×10^{-2}
O ₂ uptake (mol kg ⁻¹)	0.85	4.50×10^{-2}	6.82×10^{-2}	0.74	9.28×10^{-2}	0.83	5.10×10^{-2}	5.30×10^{-2}
Self-diffusion of N ₂ at 1 bar (cm ² s ⁻¹)	0.80	3.40×10^{-5}	4.69×10^{-5}	0.76	5.00×10^{-5}	0.77	4.52×10^{-5}	4.53×10^{-5}
Self-diffusion of N ₂ at infinite dilution (cm ² s ⁻¹)	0.80	3.75×10^{-5}	5.15×10^{-5}	0.76	5.50×10^{-5}			
Self-diffusion of O ₂ at 1 bar (cm ² s ⁻¹)	0.82	3.21×10^{-5}	4.45×10^{-5}	0.78	4.98×10^{-5}	0.78	4.04×10^{-5}	3.99×10^{-5}
Self-diffusion of O ₂ at infinite dilution (cm ² s ⁻¹)	0.79	3.34×10^{-5}	4.53×10^{-5}	0.74	4.95×10^{-5}			

fixed and variable data splits. Furthermore, to demonstrate the improvement of CSTL with the categorized features, we apply C_{all} solely for the machine learning model. Under the same parameter settings, we found that CSTL outperforms the C_{all} -only model across all datasets and metrics. The detailed results are provided in Table S3.† This comparison highlights the importance of incorporating additional chemical information through the categorized method.

2.3 Feature analysis for the category-specific topological models

In this work, we propose a category-specific topological model to capture the distinctive characteristics of MOF materials. The model encodes each component's inherent structural and functional attributes by categorizing elements based on their chemical roles and applying persistent homology to analyze each category separately. This approach allows us to represent both the inorganic and organic building blocks of MOFs through distinct topological features, providing a nuanced view that goes beyond treating all atoms as identical.

MOFs are typically built from two primary types of components: inorganic metal nodes and organic linkers. Metal ions or clusters in the inorganic units serve as coordination centers and framework backbones, offering stability and structural rigidity while connecting to the organic linkers. Although metal nodes often appear in smaller quantities than organic atoms, they strongly influence the overall material properties.^{4,49} Because of the diversity among metal elements, it becomes challenging to systematically understand the effect of each metal across all samples—especially for rare metals like Rn, Bi, and Cs that appear infrequently. Organic linkers, composed mainly of carboxylates or nitrogen-containing ligands, bridge these metal nodes, defining the MOF's porosity and connectivity. These organic components typically make up the majority of the framework and play a critical role in establishing the intricate, symmetrical structures of MOFs.

To address these component-specific influences, we group metals into categorical types (C_0 , C_1 , C_2 , C_3) while non-metals are clustered into single element or few elements set (C_4 , C_5 , C_6 , and C_7) as shown in Table 1. This CSTL thus captures the functional contributions of distinct components within the

MOF without overemphasizing elemental diversity, allowing each category to reveal its unique structural influence through topological embedding.

Visualizing the 2D t-SNE reduction in Fig. 3, each green point represents a different MOF material, with distinct clusters reflecting the influence of the CSTL features. Here, key properties such as N₂ uptake, O₂ uptake, and self-diffusivity values are mapped, where materials with the maximum and minimum values for each property are highlighted. Even without predictive modeling, CSTL features differentiate structures with significant property variations, suggesting that the model inherently captures critical structure–property relationships. For example, the MOF material labeled ELOZEK_clean, which has the lowest N₂/O₂ uptake values (8.64×10^{-3} mol kg⁻¹ for both N₂ and O₂) and Henry's constants (8.64×10^{-3} mol kg⁻¹ Pa⁻¹ for both N₂ and O₂), reflects poor gas absorption. Similarly, COVPAG_clean demonstrates minimal self-diffusivity for N₂ (4.15×10^{-7} cm² s⁻¹), underscoring its limited diffusion capabilities. Such distinctions underscore the power of the CSTL approach to reveal essential structural variations directly through category-specific topological embeddings, distinguishing materials with extreme property values across the MOF dataset.

To quantify the significance of each feature within the proposed CSTL model, we analyzed the tree-based feature importance derived from trained predictive models, as illustrated in Fig. 4. The features with higher importance scores correspond to those that play a significant role in model predictions. This analysis highlights several key trends across different homology dimensions (H_0 , H_1 , and H_2) and categories, reflecting the structural and categorical influence on the model's predictions.

Generally, we observe that feature importance is concentrated at the beginning of each dimensional homology (H_0 , H_1 , and H_2) across all categories. This is due to the intentionally large end value set for the intervals (25 Å), ensuring the model's robustness across a broader range of structures, including potential extreme cases beyond the current dataset. Consequently, topological features in the later portion of the interval largely default to zero, explaining the higher importance of features at the beginning of each homology dimension. For



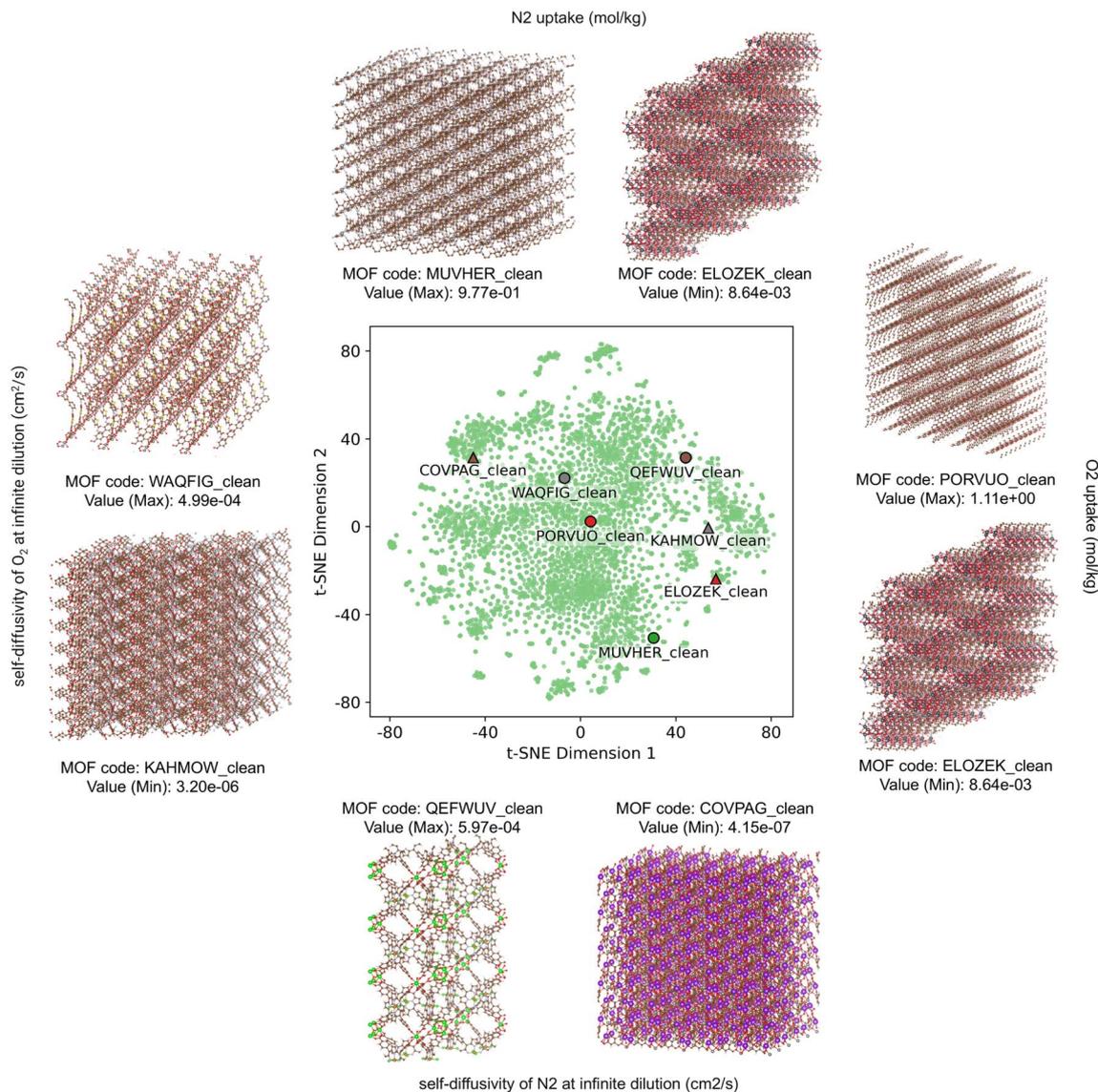


Fig. 3 t-SNE feature reduction for category-specific topological features of MOF materials, where each green point represents a distinct MOF material. Highlighted circles and triangles indicate materials with maximum and minimum values, respectively, for four key properties: N_2 uptake (mol kg^{-1}), O_2 uptake (mol kg^{-1}), self-diffusivity of N_2 at infinite dilution ($\text{cm}^2 \text{s}^{-1}$), and self-diffusivity of O_2 at infinite dilution ($\text{cm}^2 \text{s}^{-1}$). 3D structures of the materials with minimum and maximum values for each property are shown around the t-SNE plot.

category C_2 , which includes metalloids like B, Si, Ge, As, Sb, Te, Po, and At, the feature importance appears limited. Since these elements have valence electron configurations similar to carbon, and their occurrence within the dataset is low (as shown in Fig. 1b), their influence is often overshadowed by the predominant presence of carbon. This results in carbon having a stronger impact within this category, affecting the overall model importance distribution.

Focusing on Henry's constant, shown in the green-highlighted section of Fig. 4a, we see distinct variations in feature importance between different gases (N_2 in blue and O_2 in orange). Categories C_5 and C_7 , representing carbon and oxides respectively, exhibit substantial shifts in importance, indicating that carbon-based structures and strongly oxidizing elements influence the selectivity of MOF materials towards

these gases. In particular, H_2 in C_5 suggests that carbon-based cavities strongly affect gas selectivity, while H_0 in C_7 highlights the role of oxidizing element spacing on selectivity. A similar trend is observed for N_2 and O_2 uptake properties, as shown in Fig. 4b. For self-diffusivity of N_2/O_2 , whether at 1 bar or infinite dilution, Fig. 4c and d indicate that cycles and cavities within the overall MOF structure, particularly within H_1 and H_2 of the C_{all} category, are the primary factors influencing diffusion properties. This suggests that the model effectively captures the topological elements critical to gas diffusion across MOF structures.

Furthermore, when comparing properties related to gas absorption (Fig. 4a and b) and diffusivity (Fig. 4c and d), we note that C_1 shows significant variations in importance. This implies that metal atoms have a pronounced effect on gas absorptivity,



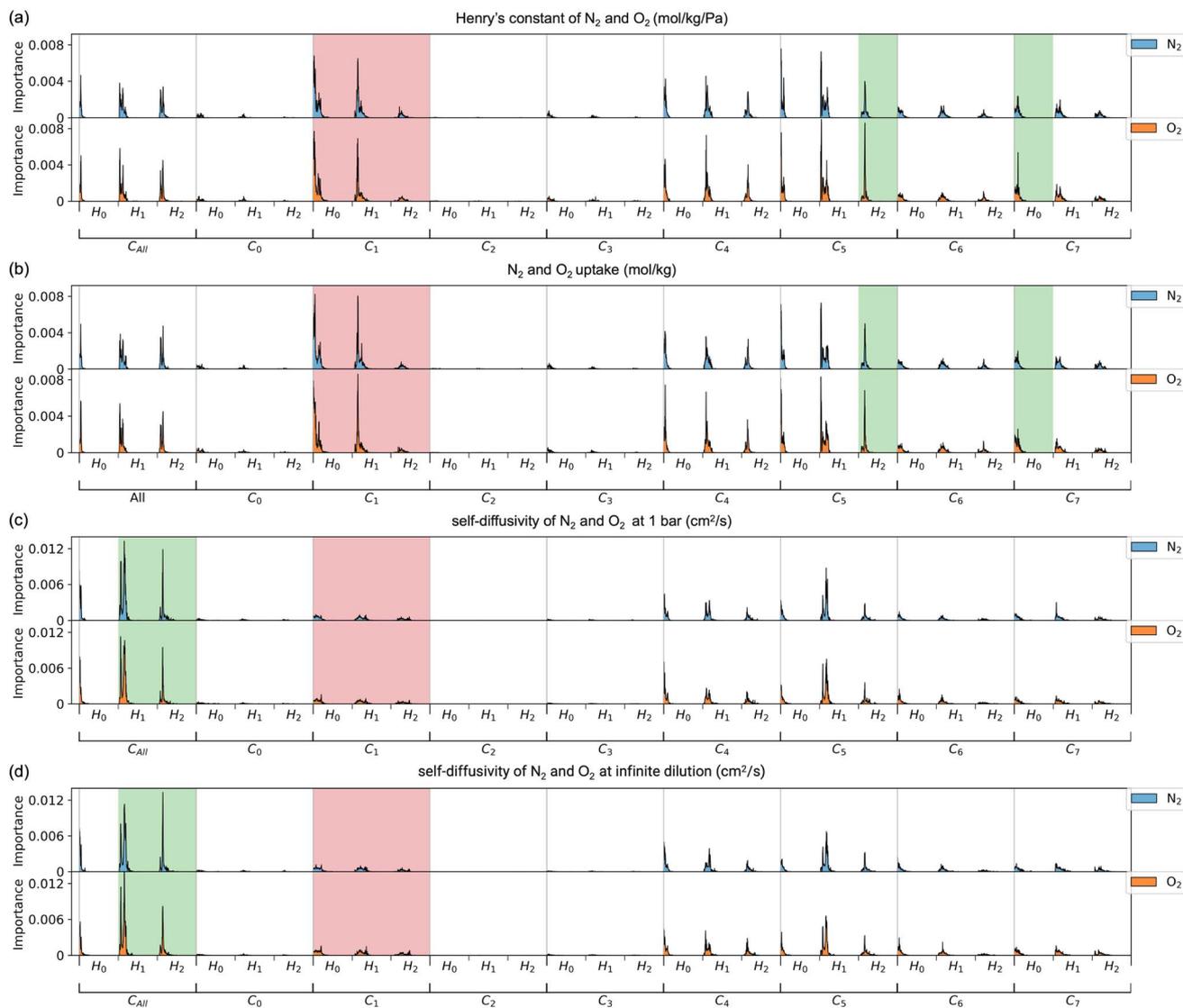


Fig. 4 Feature importance analysis for predictive models of eight properties in MOF materials using gradient boosting tree model-based importance. Panels (a)–(d) show the importance of topological features for predicting (a) Henry's constant of N₂ and O₂ (mol kg⁻¹ Pa⁻¹), (b) N₂ and O₂ uptake (mol kg⁻¹), (c) self-diffusivity of N₂ and O₂ at 1 bar (cm² s⁻¹), and (d) self-diffusivity of N₂ and O₂ at infinite dilution (cm² s⁻¹). Each panel presents separate importance values for N₂ (blue) and O₂ (orange) predictions. The bars highlight feature groups by topological dimensions H₀, H₁, and H₂ across different topological categories (C₀ to C₇), with green-shaded regions indicating particularly influential features for different gases (N₂ and O₂) and red-shaded regions indicating particularly influential features across different properties.

in contrast to their relatively lower impact on diffusivity properties. In conclusion, this feature analysis demonstrates the versatility and precision of the proposed CSTL model, which adeptly balances generalization and prediction accuracy across diverse property predictions. By integrating both structural and elemental distinctions, the model captures the nuanced interactions within MOF materials, offering a robust framework for predicting many functional properties.

3 Conclusion

The unique properties of MOFs stem from the combination of metal clusters and organic linkers, which endow them with high surface area, adjustable porosity, and the ability to finely

tune their structures. Despite these advantageous characteristics, traditional experimental and computational methods face significant challenges when scaling to the vast chemical and structural diversity of MOFs, as well as in interpreting the complex structure–property relationships.

In this work, we introduce the Category-Specific Topological Learning (CSTL) model, a novel and efficient approach for predicting MOF properties. CSTL combines advanced topological techniques with chemically informed categorization to overcome the limitations of conventional methods. By representing MOF structures as topological objects, *i.e.*, simplicial complexes, CSTL captures both global and local geometric features, while persistent homology facilitates the extraction of topological invariants that provide unique insights into the



material's structural properties. Furthermore, the integration of category-specific representations based on valence electron similarity and occurrence frequency ensures a more balanced and nuanced understanding of elemental distributions in various MOFs. This approach enhances the accuracy and interpretability of predictions related to gas selectivity, adsorption, and other key properties. The multi-dimensional, category-specific descriptors generated by CSTL serve as inputs to a gradient boosting tree model, which demonstrates state-of-the-art performance in predicting a broad range of MOF properties with increased robustness and accuracy.

Additionally, our analysis of the trained model reveals that specific categories, particularly those including transition metals, lanthanoids, and actinoids, exert a more significant influence on adsorption-related properties such as Henry's constant and gas uptake than on self-diffusivity properties. The proposed CSTL model offers a scalable, interpretable, and chemically informed framework that advances our understanding of MOF structure–property relationships. This method provides a powerful tool for the rational design of MOFs with targeted properties, accelerating the discovery of new materials for diverse applications, including energy storage, environmental remediation, and beyond. By bridging the gap between structural complexity and chemical composition, CSTL represents a significant advancement in the computational modeling of advanced materials.

4 Method

4.1 Datasets

All datasets used in this study originate from the CoRE MOFs 2019 database.²⁶ The properties of interest, such as O₂ and N₂ selectivity, were simulated in earlier studies.²⁶ Certain entries, identified as outliers, were found to lie at the extreme upper end of the distribution, significantly distant from the majority of data points.²⁸ To enhance the robustness and reliability of the models, these outliers were excluded. Additionally, the data used for validating property predictions was further refined by applying upper-limit threshold values, as outlined in the work of Orhan *et al.*²⁸ This filtering process removed the outliers, resulting in a more uniform and comprehensive distribution, ensuring a well-represented target-variable space. The filtering methodology follows that of Orhan *et al.*²⁸ To ensure a clear and transparent comparison, we compiled the data information for all methods compared in this study, as summarized in Table

S1† In this study, the input features were derived solely from MOF structural data stored in CIF files, without the use of any additional descriptors. Detailed information about the datasets, including the filtered properties and prediction performance, is provided in Table 3.

4.2 Category-specific topology

4.2.1 Simplicial complex representations. In classical MOF research, topology is typically represented using graphs, where atoms or clusters serve as nodes and bonds as edges, capturing only pairwise relationships. However, this graph-based approach is inherently limited, as it fails to account for higher-order interactions that play a crucial role in MOF properties such as porosity, adsorption, and diffusion. To address this limitation, simplicial complexes are introduced as a more generalized framework that extends graphs to higher dimensions, allowing for a richer structural representation. A graph is a special case of a simplicial complex, consisting only of 1-simplices (edges), whereas a simplicial complex incorporates higher-order simplices—such as 2-simplices (triangles) that encode three-body interactions and 3-simplices (tetrahedra) that capture four-body interactions. As illustrated in Fig. 5, a k -simplex is defined as the convex hull of $k + 1$ independent points, encompassing points (0-simplex, Fig. 5b), line segments (1-simplex, Fig. 5c), triangles (2-simplex, Fig. 5d), and tetrahedra (3-simplex, Fig. 5e). This hierarchical structure enables a more comprehensive characterization of MOF architectures, capturing not only connectivity but also loops, voids, and cavities. Formally, a k -simplex is the k -dimensional analog of these shapes, defined as the convex hull of $k + 1$ affinely independent points, and can be expressed as

$$\sigma^k = \left\{ v \mid v = \sum_{i=0}^k \lambda_i v_i, \sum_{i=0}^k \lambda_i = 1, 0 \leq \lambda_i \leq 1, i = 0, 1, \dots, k \right\}. \quad (1)$$

A simplicial complex K is a collection of simplices such that (1) every face of a simplex in K is also in K , and (2) the intersection of any two simplices is either empty or a common face.

In this work, we represent MOF structures using simplicial complexes, where atoms are 0-simplices (vertices), bonds are 1-simplices (edges), and higher-order interactions, such as atomic rings and cavities, are captured as higher-dimensional simplices. This approach allows us to model not only the

Table 3 Summary of datasets for N₂ and O₂ selectivity of MOFs

Datasets (properties)	Sizes	Train : valide : test	Splitting method
Henry's constant of N ₂ (mol kg ⁻¹ Pa ⁻¹)	4744	80 : 10 : 10	Random split
Henry's constant of O ₂ (mol kg ⁻¹ Pa ⁻¹)	5036	80 : 10 : 10	Random split
N ₂ uptake (mol kg ⁻¹)	5132	80 : 10 : 10	Random split
O ₂ uptake (mol kg ⁻¹)	5241	80 : 10 : 10	Random split
Self-diffusivity of N ₂ at 1 bar (cm ² s ⁻¹)	5056	80 : 10 : 10	Random split
Self-diffusivity of N ₂ at infinite dilution (cm ² s ⁻¹)	5192	80 : 10 : 10	Random split
Self-diffusivity of O ₂ at 1 bar (cm ² s ⁻¹)	5223	80 : 10 : 10	Random split
Self-diffusivity of O ₂ at infinite dilution (cm ² s ⁻¹)	5097	80 : 10 : 10	Random split



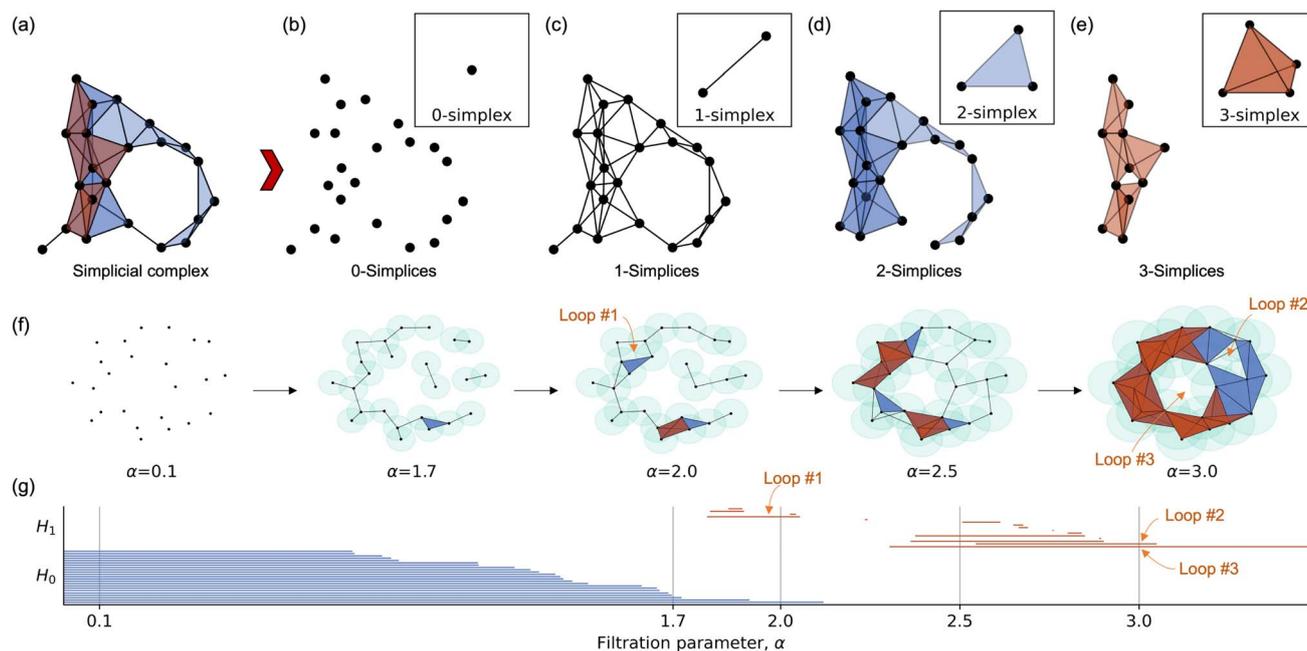


Fig. 5 Illustration of concepts in persistent homology. (a) An example of a simplicial complex. (b)–(e) Expansion of the simplicial complex in (a) into different simplex dimensions: (b) 0-simplices (vertices), with the 0-simplex as a building block shown in the upper right; (c) 1-simplices (edges), with the 1-simplex in the upper right; (d) 2-simplices (triangles), with the 2-simplex in the upper right; and (e) 2-simplices, with the 3-simplex (tetrahedron) in the upper right. (f) A nested simplicial complex with an increasing parameter α , exemplifying an alpha complex. (g) Barcode representation of H_0 and H_1 for the complex in (f), with specific values of $\alpha = 0.1, 1.6, 2.0, 2.5$, and 3.0 corresponding to the simplicial complex states shown in (f). For the $\alpha = 2.0$, and 3.0 , the highlighted loops in (f) are pointed out.

pairwise connections but also the higher-order geometric and topological features essential for understanding the physical and chemical properties of MOFs. In the category-specific representation framework for MOF structures, all atoms are grouped into distinct sets based on the categories listed in Table 1, denoted as C_0 to C_7 . Additionally, C_{all} represents the set containing all atoms. For each category-specific set, topological representations are constructed to capture the interactions among atoms across different categories.

4.2.2 Homology and persistence. To analyze the topological properties of MOF structures represented by simplicial complexes, homology is used as an algebraic tool. By employing concepts such as chains, chain groups, and boundary operators, homology groups capture features like connected components, loops, and cavities within the material. For a given dimension k , the k -chain group C_k is formed by k -simplices with coefficients from a specified field (*e.g.*, \mathbb{Z}_2). The boundary operator ∂_k maps k -chains to $(k - 1)$ -chains, defined as:

$$\partial_k[v_0, v_1, \dots, v_k] = \sum_{i=0}^k (-1)^i [v_0, \dots, \hat{v}_i, \dots, v_k], \quad (2)$$

where \hat{v}_i indicates the omission of vertex v_i . This operation helps identify cycles (chains with no boundary) and boundaries (chains that are boundaries of higher-dimensional simplices). The k -th homology group H_k is then defined as:

$$H_k = \ker(\partial_k) / \text{im}(\partial_{k+1}), \quad (3)$$

which represents k -dimensional holes, such as connected components (H_0), loops (H_1), and voids (H_2) in the MOF structure. The homology group (H) allows for the measurement of topological features, such as Betti numbers (β), which count the number of independent k -dimensional cycles, reflecting the number of k -dimensional holes. They can be calculated by, $\beta_k = \text{rank}(H_k) = \text{rank}(Z_k) - \text{rank}(B_k)$, where the $Z_k = \ker \partial_k$ means the kernel of the boundary ∂_k , and the $B_k = \text{im} \partial_{k+1}$ represents the image of the boundary ∂_{k+1} .

To capture how these topological features vary with the spatial scale, persistent homology is introduced.^{39,50,51} It tracks the evolution of homological features as a parameter (*e.g.*, bond length or distance threshold) changes. This is achieved through a filtration, a sequence of nested subcomplexes $\{K_i\}$ where $K_0 \subseteq K_1 \subseteq \dots \subseteq K_n$. There are some common used filtration methods, such as Vietoris–Rips complex,⁵² Čech complex,⁵³ and alpha complex.⁵⁴ In this work, we employ the alpha complex for analyzing MOF structures. The alpha complex is constructed based on the Delaunay triangulation of the atomic positions. For a given parameter α , a simplex (*e.g.*, an edge, triangle, or tetrahedron) is included in the complex if the radius of the smallest empty circumsphere that encloses it is less than or equal to α . As α increases, the alpha complex grows, progressively capturing larger topological features in the MOF structure, such as rings, tunnels, and cavities, an example is shown Fig. 5f.

Persistent homology quantifies the persistence of these features across different scales, revealing stable patterns that



correspond to critical geometric and chemical properties of the MOF. Each k -th homology group is tracked across the filtration, providing insights into how certain features (e.g., porosity or connectivity) appear, merge, and disappear as the structure evolves. These persistent patterns are typically visualized using barcodes,⁵⁵ where the length of each bar represents the lifespan of a particular topological feature. An example of barcodes corresponding to the alpha complex is shown in Fig. 5g, and the loops represented in Fig. 5f are highlighted at filtration parameters $\alpha = 2$ and 3.

4.2.3 Category-specific topological embedding. Persistent homology does not distinguish different element types and thus gives a poor representation for chemical and biological systems. Element-specific persistent homology was introduced to better capture chemical and biological properties.⁴⁰ In this work, we propose a category-specific topological embedding approach to preserve the chemical and physical information inherent in MOF structures. Elements in the periodic table are categorized into eight distinct groups based on their chemical similarities and structural roles (see Table 1). Before constructing the embeddings, the supercell of each material is scaled uniformly to approximately $64 \text{ \AA} \times 64 \text{ \AA} \times 64 \text{ \AA}$ to ensure that the topological analysis is performed consistently across different structures.

Our method involves two main stages: (1) for a given MOF structure, category-specific topological representations are constructed based on the elemental types of atoms, categorized as C_0 to C_7 , along with an additional set C_{all} containing all atoms. (2) The persistent homology of each category from stage (1) is computed to capture global and category-level topological patterns, characterized by their Betti numbers in the H_0 , H_1 , and H_2 homology spaces. This approach allows the topological analysis to incorporate both structural and chemical information. For each category and each homology dimension, we employ a grid-based method to generate the topological embeddings. Specifically, we construct a grid ranging from 0 to 25 Å with a step size of 0.1 Å and record the Betti numbers (*i.e.*, the number of topological features that persist at each scale). This process yields a feature vector of length 750 (250 steps \times 3 homology dimensions: H_0 , H_1 , and H_2) for each element category. Here, each 250 features are denoted as one feature group. By concatenating these feature vectors across all eight categories, we obtain a 6000-dimensional representation. When combined with the features derived from the entire MOF structure, the final topological embedding results in a 6750-dimensional vector that integrates both global structural patterns and category-specific chemical information.

4.3 Predictive modeling

In this work, a Gradient Boosting Tree (GBT) model was constructed to perform regression analysis using the proposed category-specific topological embedding as input features. Gradient boosting is an ensemble learning method that builds multiple weak learners (typically decision trees) sequentially, where each tree is trained to correct the errors made by the previous ones, thereby producing a more accurate model. We

implemented the gradient boosting regressor from Scikit-learn,⁵⁶ optimizing the squared error loss function. The model parameters were set as follows: $\text{max_depth} = 7$, $\text{max_features} = \text{'sqrt'}$, $\text{min_samples_leaf} = 1$, $\text{min_samples_split} = 2$, $n_estimators = 10\ 000$, and $\text{subsample} = 0.5$. These settings were not fine-tuned, as we aimed to demonstrate the robustness of the proposed predictive model with a single set of hyperparameters.

All input features were normalized using standard scaling, and the target properties were standardized to facilitate regression analysis. For model evaluation, we split the dataset into train, validation, and test sets using an 80%, 10%, and 10% ratio, respectively.^{28,33} Since we used a universal set of hyperparameters, the validation set was not employed for model selection. Instead, 80% of the data was used for training to establish a fair comparison with previous works. The results for the test set (10%) and for both the test and validation sets combined (20%) are reported to assess the model's performance comprehensively.

To ensure robust evaluation, we repeated the random data split 10 times, and for each split, 10 models were trained with different random seeds, resulting in a total of 100 models per dataset. The performance metrics, including root mean square error (RMSE), mean absolute error (MAE), and r^2 correlation, were averaged over these 100 models and reported as the final results (as seen in ESI Section †). This approach of using a single set of hyperparameters and a consistent evaluation protocol highlights the robustness of the predictive model, making the results reliable and comparable to existing methods in the literature.

Data availability

The datasets utilized in this work are derived from the structures available in the CoRE MOFs 2019 database.²⁶ The properties for each dataset were obtained using the methods outlined in Orhan *et al.*²⁸

Conflicts of interest

There are no conflicts to declare.

Acknowledgements

This work was supported in part by NIH grants R01GM126189, R01AI164266, and R35GM148196, National Science Foundation Grants DMS2052983 and IIS-1900473, Michigan State University Research Foundation, and Bristol-Myers Squibb 65109. D. C. was supported in part by the AMS-Simons Travel Grant. C.-L. C. gratefully acknowledges financial support from the Defense Threat Reduction Agency (Project CB11141), and the Department of Energy (DOE), Office of Science, Office of Basic Energy Sciences (BES) under an award FWP 80124 at Pacific Northwest National Laboratory (PNNL). PNNL is a multiprogram national laboratory operated for the Department of Energy by Battelle under Contract DE-AC05-76RL01830.



References

- 1 R. Freund, O. Zaremba, G. Arnauts, R. Ameloot, G. Skorupskii, M. Dincă, A. Bavykina, J. Gascon, A. Ejsmont, J. Goscińska, *et al.*, The current status of mof and cof applications, *Angew. Chem., Int. Ed.*, 2021, **60**(45), 23975–24001.
- 2 S. Kumar, S. Jain, M. Nehra, N. Dilbaghi, G. Marrazza and Ki-H. Kim, Green synthesis of metal–organic frameworks: A state-of-the-art review of potential environmental and medical applications, *Coord. Chem. Rev.*, 2020, **420**, 213407.
- 3 C.-L. Chen and A. M. Beatty, Guest inclusion and structural dynamics in 2-d hydrogen-bonded metal–organic frameworks, *J. Am. Chem. Soc.*, 2008, **130**(51), 17222–17223.
- 4 C.-L. Chen, A. M. Goforth, M. D. Smith, C.-Y. Su and H.-C. z. Loye, [co₂ (ppca) 2 (h₂o)(v₄o₁₂) 0.5]: a framework material exhibiting reversible shrinkage and expansion through a single-crystal-to-single-crystal transformation involving a change in the cobalt coordination environment, *Angew. Chem., Int. Ed.*, 2005, **44**(41), 6673–6677.
- 5 S. Ma and H.-C. Zhou, Gas storage in porous metal–organic frameworks for clean energy applications, *Chem. Commun.*, 2010, **46**(1), 44–53.
- 6 Q. Qian, P. A. Asinger, M. J. Lee, G. Han, K. Mizrahi Rodriguez, S. Lin, F. M. Benedetti, A. X. Wu, W. S. Chi and Z. P. Smith, Mof-based membranes for gas separations, *Chem. Rev.*, 2020, **120**(16), 8161–8266.
- 7 J. Y. Lee, O. K. Farha, J. Roberts, K. A. Scheidt, S. B. T. Nguyen and J. T. Hupp, Metal–organic framework materials as catalysts, *Chem. Soc. Rev.*, 2009, **38**(5), 1450–1459.
- 8 K. O. Kirlikovali, Z. Chen, T. Islamoglu, J. T. Hupp and O. K. Farha, Zirconium-based metal–organic frameworks for the catalytic hydrolysis of organophosphorus nerve agents, *ACS Appl. Mater. Interfaces*, 2020, **12**(13), 14702–14720.
- 9 L. E. Kreno, K. Leong, O. K. Farha, M. Allendorf, R. P. V. Duyne and J. T. Hupp, Metal–organic framework materials as chemical sensors, *Chem. Rev.*, 2012, **112**(2), 1105–1125.
- 10 Y. J. Colón and R. Q. Snurr, High-throughput computational screening of metal–organic frameworks, *Chem. Soc. Rev.*, 2014, **43**(16), 5735–5749.
- 11 S. Lee, B. Kim, H. Cho, H. Lee, S. Y. Lee, E. S. Cho and J. Kim, Computational screening of trillions of metal–organic frameworks for high-performance methane storage, *ACS Appl. Mater. Interfaces*, 2021, **13**(20), 23647–23654.
- 12 M. Karplus and G. A. Petsko, Molecular dynamics simulations in biology, *Nature*, 1990, **347**(6294), 631–639.
- 13 W. D. Cornell, P. Cieplak, C. I. Bayly, I. R. Gould, K. M. Merz, D. M. Ferguson, D. C. Spellmeyer, T. Fox, J. W. Caldwell and P. A. Kollman, A second generation force field for the simulation of proteins, nucleic acids, and organic molecules, *J. Am. Chem. Soc.*, 1995, **117**(19), 5179–5197.
- 14 W. Kohn, A. D. Becke and R. G. Parr, Density functional theory of electronic structure, *J. Phys. Chem.*, 1996, **100**(31), 12974–12980.
- 15 L. Shao, J. Ma, J. L. Prelesnik, Y. Zhou, M. Nguyen, M. Zhao, S. A. Jenekhe, S. V. Kalinin, A. L. Ferguson, J. Pfaendtner, *et al.*, Hierarchical materials from high information content macromolecular building blocks: construction, dynamic interventions, and prediction, *Chem. Rev.*, 2022, **122**(24), 17397–17478.
- 16 H. Daglar and S. Keskin, Recent advances, opportunities, and challenges in high-throughput computational screening of mofs for gas separations, *Coord. Chem. Rev.*, 2020, **422**, 213470.
- 17 K. Torkelson, N. Y. Naser, X. Qi, Z. Li, W. Yang, K. Pushpavanam, C.-L. Chen, F. Baneyx and J. Pfaendtner, Rational design of novel biomimetic sequence-defined polymers for mineralization applications, *Chem. Mater.*, 2024, **36**(2), 786–794.
- 18 M. Zhao, S. Zhang, R. Zheng, S. Alamdari, C. J. Mundy, J. Pfaendtner, L. D. Pozzo, C.-L. Chen, J. J. De Yoreo and A. L. Ferguson, Computational and experimental determination of the properties, structure, and stability of peptoid nanosheets and nanotubes, *Biomacromolecules*, 2023, **24**(6), 2618–2632.
- 19 S. Yadav Schmid, M. Xiang, J. A. Hammons, S. T. Mergelsberg, B. S. Harris, T. Ferron, W. Yang, W. Zhou, R. Zheng, S. Zhang, *et al.*, Influence of peptoid sequence on the mechanisms and kinetics of 2d assembly, *ACS Nano*, 2024, **18**(4), 3497–3508.
- 20 J. Wei, X. Chu, X.-Y. Sun, K. Xu, H.-X. Deng, J. Chen, Z. Wei and M. Lei, Machine learning in materials science, *InfoMat*, 2019, **1**(3), 338–358.
- 21 Y. Luo, S. Bag, O. Zaremba, A. Cierpka, J. Andreo, S. Wuttke, P. Friederich and M. Tsotsalas, Mof synthesis prediction enabled by automatic data mining and machine learning, *Angew. Chem., Int. Ed.*, 2022, **61**(19), e202200242.
- 22 S. Chong, S. Lee, B. Kim and J. Kim, Applications of machine learning in metal–organic frameworks, *Coord. Chem. Rev.*, 2020, **423**, 213487.
- 23 Z. Han, Y. Yang, J. Rushlow, J. Huo, Z. Liu, Yu-C. Hsu, R. Yin, M. Wang, R. Liang, K.-Y. Wang, *et al.*, Development of the design and synthesis of metal–organic frameworks (mofs)–from large scale attempts, functional oriented modifications, to artificial intelligence (ai) predictions, *Chem. Soc. Rev.*, 2025, **54**(1), 367–395.
- 24 D. Banerjee, C. M. Simon, A. M. Plonka, R. K. Motkuri, J. Liu, X. Chen, B. Smit, J. B. Parise, M. Haranczyk and P. K. Thallapally, Metal–organic framework with optimally selective xenon adsorption and separation, *Nat. Commun.*, 2016, **7**(1), 1–7.
- 25 P. Z. Moghadam, Y. G. Chung and R. Q. Snurr, Progress toward the computational discovery of new metal–organic framework adsorbents for energy applications, *Nat. Energy*, 2024, **9**(2), 121–133.
- 26 Y. G. Chung, E. Haldoupis, B. J. Bucior, M. Haranczyk, S. Lee, H. Zhang, K. D. Vogiatzis, M. Milisavljevic, S. Ling, J. S. Camp, *et al.*, Advances, updates, and analytics for the computation-ready, experimental metal–organic framework database: Core mof 2019, *J. Chem. Eng. Data*, 2019, **64**(12), 5985–5998.



- 27 C. E. Wilmer, M. Leaf, C. Y. Lee, K. F. Omar, B. G. Hauser, J. T. Hupp and R. Q. Snurr, Large-scale screening of hypothetical metal-organic frameworks, *Nat. Chem.*, 2012, **4**(2), 83–89.
- 28 I. B. Orhan, H. Daglar, S. Keskin, Tu C. Le and R. Babarao, Prediction of o₂/n₂ selectivity in metal-organic frameworks via high-throughput computational screening and machine learning, *ACS Appl. Mater. Interfaces*, 2021, **14**(1), 736–749.
- 29 A. Nandy, C. Duan and H. J. Kulik, Using machine learning and data mining to leverage community knowledge for the engineering of stable metal-organic frameworks, *J. Am. Chem. Soc.*, 2021, **143**(42), 17535–17547.
- 30 B. J. Bucior, N. Scott Bobbitt, T. Islamoglu, S. Goswami, A. Gopalan, T. Yildirim, K. F. Omar, N. Bagheri and R. Q. Snurr, Energy-based descriptors to rapidly predict hydrogen storage in metal-organic frameworks, *Mol. Syst. Des. Eng.*, 2019, **4**(1), 162–174.
- 31 A. S. Rosen, S. M. Iyer, D. Ray, Z. Yao, A. Aspuru-Guzik, L. Gagliardi, J. M. Notestein and R. Q. Snurr, Machine learning the quantum-chemical properties of metal-organic frameworks for accelerated materials discovery, *Matter*, 2021, **4**(5), 1578–1597.
- 32 T. Xie and J. C. Grossman, Crystal graph convolutional neural networks for an accurate and interpretable prediction of material properties, *Phys. Rev. Lett.*, 2018, **120**(14), 145301.
- 33 Y. Kang, H. Park, B. Smit and J. Kim, A multi-modal pre-training transformer for universal transfer learning in metal-organic frameworks, *Nat. Mach. Intell.*, 2023, **5**(3), 309–318.
- 34 H. Park, Y. Kang and J. Kim, Enhancing structure–property relationships in porous materials through transfer learning and cross-material few-shot learning, *ACS Appl. Mater. Interfaces*, 2023, **15**(48), 56375–56385.
- 35 Z. Cao, R. Magar, Y. Wang and A. B. Farimani, Moformer: self-supervised transformer model for metal-organic framework property prediction, *J. Am. Chem. Soc.*, 2023, **145**(5), 2958–2967.
- 36 P. Chen, R. Jiao, J. Liu, Y. Liu and Y. Lu, Interpretable graph transformer network for predicting adsorption isotherms of metal-organic frameworks, *J. Chem. Inf. Model.*, 2022, **62**(22), 5446–5456.
- 37 D. D. Nguyen and G.-W. Wei, Agl-score: algebraic graph learning score for protein–ligand binding scoring, ranking, docking, and screening, *J. Chem. Inf. Model.*, 2019, **59**(7), 3291–3304.
- 38 D. Chen, K. Gao, D. D. Nguyen, X. Chen, Y. Jiang, G.-W. Wei and F. Pan, Algebraic graph-assisted bidirectional transformers for molecular property prediction, *Nat. Commun.*, 2021, **12**(1), 3521.
- 39 A. Zomorodian and G. Carlsson, Computing persistent homology, in *Proceedings of the Twentieth Annual Symposium on Computational Geometry*, 2004, pp. 347–356.
- 40 Z. Cang and G.-W. Wei, Integration of element specific persistent homology and machine learning for protein–ligand binding affinity prediction, *Int. J. Numer. Method. Biomed. Eng.*, 2018, **34**(2), e2914.
- 41 D. Chen, J. Liu, J. Wu, G.-W. Wei, F. Pan and S.-T. Yau, Path topology in molecular and materials sciences, *J. Phys. Chem. Lett.*, 2023, **14**(4), 954–964.
- 42 R. Wang, D. D. Nguyen and G.-W. Wei, Persistent spectral graph, *Int. J. Numer. Method. Biomed. Eng.*, 2020, **36**(9), e3376.
- 43 Z. Cang and G.-W. Wei, Topologynet: Topology based deep convolutional and multi-task neural networks for biomolecular property predictions, *PLoS Comput. Biol.*, 2017, **13**(7), e1005690.
- 44 Y. Jiang, D. Chen, X. Chen, T. Li, G.-W. Wei and F. Pan, Topological representations of crystalline compounds for the machine-learning prediction of materials properties, *npj Comput. Mater.*, 2021, **7**(1), 28.
- 45 D. Chen, J. Liu and G.-W. Wei, Multiscale topology-enabled structure-to-sequence transformer for protein–ligand interaction predictions, *Nat. Mach. Intell.*, 2024, **6**(7), 799–810.
- 46 D. D. Nguyen, Z. Cang, K. Wu, M. Wang, Y. Cao and G.-W. Wei, Mathematical deep learning for pose and binding affinity prediction and ranking in d3r grand challenges, *J. Comput.-Aided Mol. Des.*, 2019, **33**, 71–82.
- 47 D. D. Nguyen, K. Gao, M. Wang and G.-W. Wei, Mathdl: mathematical deep learning for d3r grand challenge 4, *J. Comput.-Aided Mol. Des.*, 2020, **34**, 131–147.
- 48 A. S. Krishnapriyan, J. Montoya, M. Haranczyk, J. Hummelshøj and D. Morozov, Machine learning with persistent homology and chemical word embeddings improves prediction accuracy and interpretability in metal-organic frameworks, *Sci. Rep.*, 2021, **11**(1), 8888.
- 49 R. C. Rohde, K. M. Carsch, M. N. Dods, H. Z. H. Jiang, A. R. McIsaac, R. A. Klein, H. Kwon, S. L. Karstens, Y. Wang, A. J. Huang, *et al.*, High-temperature carbon dioxide capture in a porous material with terminal zinc hydride sites, *Science*, 2024, **386**(6723), 814–819.
- 50 H. Edelsbrunner, *Geometry and Topology for Mesh Generation*, Cambridge University Press, 2001.
- 51 J. Z. Afra, *Topology for Computing*, Cambridge University Press, 2005, vol. 16.
- 52 J.-C. Hausmann, *et al.*, On the Vietoris-Rips complexes and a cohomology theory for metric spaces, *Université de Genève-Section de Mathématiques*, 1994.
- 53 R. W. Ghrist, *Elementary Applied Topology*, Createspace, Seattle, 2014, vol. 1.
- 54 H. Edelsbrunner, Smooth surfaces for multi-scale shape representation, in *International Conference on Foundations of Software Technology and Theoretical Computer Science*, Springer, 1995, pp. 391–412.
- 55 R. Ghrist, Barcodes: the persistent topology of data, *Bull. Am. Math. Soc.*, 2008, **45**(1), 61–75.
- 56 F. Pedregosa, G. Varoquaux, A. Gramfort, M. Vincent, T. Bertrand, O. Grisel, M. Blondel, P. Prettenhofer, R. Weiss, D. Vincent, *et al.*, Scikit-learn: Machine learning in python, *J. Mach. Learn. Res.*, 2011, **12**, 2825–2830.

