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# Beryllium dinitride monolayer: a multifunctional direct bandgap anisotropic semiconductor containing polymeric nitrogen with oxygen reduction catalysis and potassium-ion storage capability†

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Searching for two-dimensional multifunctional polynitride materials with novel properties and practical applications presents an attractive challenge. The global energy minimum of the beryllium dinitride monolayer ( $\alpha$ -2D-BeN<sub>2</sub>) was predicted using a global structure search method and first-principles theory. With penta-, hexa-, and hepta-atomic rings and an N<sub>4</sub> tetramer in its planar anisotropic structure,  $\alpha$ -2D-BeN<sub>2</sub> monolayer exhibited lattice dynamic stability, excellent thermal stability, a direct bandgap of 1.82 eV, high carrier mobilities, visible light absorption, a large in-plane Poisson's ratio ranging from 0.228 to 0.368, promising oxygen reduction catalysis, and outstanding potassium storage capability with an ultrahigh specific capacity (2895 mA h g<sup>-1</sup>), a good voltage range (0.280–0.008 V), and a low migration barrier energy (0.109–0.146 eV). Therefore, the  $\alpha$ -2D-BeN<sub>2</sub> monolayer is expected to be an anisotropic multifunctional material with potential applications in various fields, such as semiconductors, visible-light detectors, donors in solar cells, ductile materials, iontronic devices, and potassium-ion anode materials, thereby expanding the possibilities for polynitride materials.

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## 1. Introduction

As an extension and frontier in structure and bonding, polynitride materials and polymeric nitrogen allotropes with polymeric N<sub>m</sub> substructure units ( $m > 2$ ) suffer an innate thermodynamic challenge due to the exceptionally high stability of the N≡N bond in nature. Through experimental methods involving conventional high temperature and high pressure, as well as new approaches, various forms have been identified, including an N<sub>3</sub> trimer in azides,<sup>1,2</sup> an N<sub>5</sub> pentatomic ring (CsN<sub>5</sub>),<sup>3</sup> an N<sub>6</sub> hexatomic ring (KN<sub>3</sub>)<sup>4</sup> and short chains (ScN<sub>3</sub>),<sup>5</sup> New methods have also led to the discovery of linear N<sub>5</sub><sup>+</sup> and N<sub>8</sub><sup>-</sup> chains,<sup>6,7</sup> infinite [N]<sub>n</sub> chains (MN<sub>4</sub>, M = Be, Zn, Mg,

Fe)<sup>8–12</sup> [N<sub>5</sub>]<sub>n</sub> rattan (TiN<sub>5</sub>),<sup>13</sup> polymeric two-dimensional (2D) networks (e.g. supernitride LaN<sub>8</sub>,<sup>14</sup> GaN<sub>5</sub>,<sup>15</sup> ScN<sub>5</sub>,<sup>5</sup> LP-N,<sup>16</sup> HLP-N,<sup>17</sup> bp-N),<sup>18,19</sup> and three-dimensional frameworks (cg-N, t-N).<sup>20,21</sup> Owing to theoretical methods, a more diverse range of polynitrides with intricate polymeric structures and extended properties<sup>9,22–30</sup> have been identified, such as MnN<sub>4</sub> (superconductivity and magnetism),<sup>31</sup> ZnN<sub>4</sub> (Dirac semimetal),<sup>10</sup> and WN<sub>6</sub> (superhardness).<sup>32</sup> Triggered by the high-energy state of their polymeric substructures, polynitrides often exhibit potential applications in energy storage, propellants, and explosives. However, this high-energy characteristic also poses a challenge for polynitrides in applications requiring high stability, high quality and low spillover. Thus, discovering new materials to expand and develop the polynitride family in terms of structure, properties, and applications remains an attractive challenge, with the aim of overcoming existing limits.

Today, a diverse range of 2D materials has been developed both experimentally and theoretically, such as graphene, phosphorene, borophene, h-BN, and MoS<sub>2</sub>,<sup>33–38</sup> possessing novel physical and chemical properties, especially their high specific surface areas with rich active sites for ion and molecular species absorption/loading in ion storage and catalysis. The exploration of 2D polynitrides is still in its early stages but shows great potential for extended properties and applications. Several 2D polynitride materials have been reported, including

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2D  $\text{KN}_3$  with an  $\text{N}_3$  trimer,<sup>39</sup>  $\text{h-MN}_2$  ( $\text{M} = \text{Be}, \text{Mg}$ ) with an  $\text{N}_4$  tetramer,<sup>40,41</sup>  $\text{h-MN}_3$  ( $\text{M} = \text{Be}, \text{Ge}$ )<sup>42</sup> with  $\text{N}_6$  hexa-atomic rings, and 2D  $\text{MN}_4$  ( $\text{M} = \text{Be}, \text{Mg}, \text{Ir}, \text{Rh}, \text{Ni}, \text{Cu}, \text{Au}, \text{Pd}, \text{and Pt}$ )<sup>43,44</sup> with infinite  $[\text{N}]_n$  chains. For instance, the 2D Be–N system, consisting of  $\text{BeN}$ ,  $\text{Be}_3\text{N}_4$ ,  $\text{Be}_2\text{N}_3$ ,  $\text{BeN}_2$ ,  $\text{BeN}_3$ , and  $\text{BeN}_4$ , has been explored *via* the global structure search method.<sup>34,42,45</sup> The investigations suggest that the polymerization degree of N atoms increases with the N atom ratio. Among them, the h- $\text{BeN}_2$  monolayer with isolated “Y”-shaped  $\text{N}_4$  tetramers in structure was predicted to exhibit a direct bandgap of 2.23 eV, excellent carrier mobilities, ultrahigh on-state current in transistors,<sup>46</sup> ferromagnetic half-metallicity *via* fluorination,<sup>47</sup> oxygen reduction catalytic ability<sup>48</sup> and water photocatalytic ability.<sup>41</sup> Recently, the experimental progress of the 2D  $\text{BeN}_4$  monolayer (beryllonitrene),<sup>8</sup> which feasibly could have exfoliated from the synthesized new layered material  $\text{BeN}_4$  *via* decompression technology, raises hope for practical 2D polynitrides with wide-ranging applications. Beryllonitrene is a planar monolayer with parallel armchair-like infinite  $[\text{N}]_n$  chains, possessing anisotropic structures with novel physical and chemical properties, such as anisotropic Dirac cone,<sup>8</sup> high lattice thermal conductivity,<sup>49</sup> layer-dependent electronic and optical properties,<sup>50</sup>  $\text{CO}_2$  capture,<sup>51</sup> hydrogen storage,<sup>52</sup> and Li/Na/Ca ion storage for ion batteries.<sup>44</sup> To date, practical 2D polynitride materials are still rare, waiting for new discovery and proposed candidates.

Given the light mass of Be and N elements, the high specific surface areas with rich active sites for 2D Be–N structures, and the isoelectronic formula of  $\text{BeN}_2$  to h-BN (both are 4e per atom) with high strength and stability, in this study, a novel single-atom-thick anisotropic 2D polynitride with 5-, 6-, 7-membered rings and isolated “U”-shaped  $\text{N}_4$  tetramers in its planar structure, beryllium dinitride monolayer ( $\alpha$ -2D- $\text{BeN}_2$ ), is predicted as a global energy minimum by a 2D global structure search method. The thermodynamics, lattice dynamics, and thermal stability results indicate its good synthesizability and high structural stability. The new structure exhibits a direct bandgap, good visible light absorption, a relatively large Poisson's ratio, promising oxygen reduction catalysis ability, and excellent potassium storage ability. The  $\alpha$ -2D- $\text{BeN}_2$  monolayer is expected to be a highly structurally stable multifunctional material with promising properties for wide-ranging applications in various fields.

## 2. Computational details

The simulation of structural optimization, energy and electronic structure was based on the first-principles density functional theory (DFT) code with the projector augmented wave (PAW)<sup>53</sup> method. An energy cutoff of 520 eV was adopted. The electron exchange–correlation potential was powered by the Perdew–Burke–Ernzerhof (PBE) functional.<sup>54</sup> The Brillouin zone was sampled with an  $8 \times 12 \times 1$  G-centered  $K$ -point grid for geometry optimization and electronic properties. The convergence criteria for energy and forces were set to  $10^{-6}$  eV and  $0.01 \text{ eV } \text{\AA}^{-1}$ , respectively. To gain more accurate results, the Heyd–Scuseria–Ernzerhof (HSE06) functional was adopted for electronic properties.<sup>55</sup> The DFT-D3 method<sup>56</sup> was applied to

describe the adsorption of species during the oxygen reduction reaction (ORR) and potassium atoms. The finite displacement method was used to investigate the lattice dynamic stability *via* phonon calculation.<sup>57</sup> The *ab initio* molecular dynamics (AIMD) simulations at constant temperature and volume (NVT) were carried out to check the thermal stability *via* setting the time step at 1 fs and the total simulation time at 5 ps. The climbing image nudged elastic band (CI-NEB) method<sup>58</sup> was used to obtain the migration paths and barriers of potassium ions.

## 3. Results and discussion

### 3.1 Structure and stability

The global structure search was carried out using the artificial bee colony (ABC) algorithm in the 2D structure search mode implemented in the CALYPSO code.<sup>59</sup> The structural unit cell with various atom numbers (Be : N atom = 2 : 4, 3 : 6, and 4 : 8) was considered in computations. The searching population and generation are 20 and 30, respectively. As displayed in Fig. 1a and b, the minimum energy structure for the structural unit cell with an atom number of Be : N = 2 : 4 is graphene-like  $\beta$ -2D- $\text{BeN}_2$  (or h- $\text{BeN}_2$ ), while it is  $\alpha$ -2D- $\text{BeN}_2$  for the structural unit cell with a larger atom number of Be : N = 4 : 8. Remarkably, the  $\alpha$ -2D- $\text{BeN}_2$  monolayer is thermodynamically more stable than the graphene-like h- $\text{BeN}_2$  monolayer predicted previously with a decrease of  $-34 \text{ meV}$  per atom in total energy. Based on the energy sequence, the global energy minimum structure in all searches is  $\alpha$ -2D- $\text{BeN}_2$  (Fig. S1 and S2 in the ESI†).  $\alpha$ -2D- $\text{BeN}_2$  is a planar monolayer with penta-, hexa-, and hepta-atomic rings (noted as R5, R6, R7, respectively) in structure, different from the h- $\text{BeN}_2$  monolayer with only hexa-atomic rings. The  $\alpha$ -2D- $\text{BeN}_2$  monolayer has a symmetry of PMC21 (space group of No. 26) with lattice constants of  $a = 7.264 \text{ \AA}$  and  $b = 5.134 \text{ \AA}$ . There are two types of Be atoms with identical positions of Be\_1(0.931, 0.360, 0.500) and Be\_2(0.389, 0.500, 0.500) in the structure, and four types of N atoms of N\_1(0.717, 0.271, 0.500), N\_2(0.616, 0.491, 0.500), N\_3(0.716, 0.710, 0.500), and N\_4(0.896, 0.668, 0.500), respectively.  $\alpha$ -2D- $\text{BeN}_2$  can be regarded as a framework composed of two units, a ‘U’-shaped chain segment  $\text{N}_4$  tetramer and a Be atom, as shown in Fig. 1b. The bond length of Be–N ( $d_{\text{Be-N}}$ ) is from 1.589 to 1.672  $\text{\AA}$ , while that of N–N bonds is  $d_{\text{N-N}} = 1.324\text{--}1.346 \text{ \AA}$ , as shown in Fig. 1f. As comparison, the bond length in the h- $\text{BeN}_2$  monolayer is quite similar to  $d_{\text{Be-N}} = 1.616 \text{ \AA}$  and  $d_{\text{N-N}} = 1.324 \text{ \AA}$  with the same calculation method (Fig. 1g).

The stability of the  $\alpha$ -2D- $\text{BeN}_2$  monolayer structure was examined in different aspects. First, it has a large binding energy of  $-5.013 \text{ eV}$  per atom. Compared with the experimental 2D structures with purely 3-fold atoms, it is lower than that of graphene ( $-7.974 \text{ eV}$  per atom) and h-BN ( $-7.098 \text{ eV}$  per atom), but higher than that of phosphorene ( $-3.477 \text{ eV}$  per atom) and silicene ( $-3.974 \text{ eV}$  per atom), indicating the high-strength Be–N and N–N bonds in  $\alpha$ -2D- $\text{BeN}_2$ . More importantly, the formation energy of  $\alpha$ -2D- $\text{BeN}_2$  ( $E_{\text{f-BeN}_2}$  vs. Be metal and  $\text{N}_2$  molecule, eqn (S1)†) is  $-0.308 \text{ eV}$  per atom, suggesting its good formation feasibility from the Be metal bulk and  $\text{N}_2$  molecule in thermodynamics. Notably, the interlayer binding energy of bilayer  $\alpha$ -



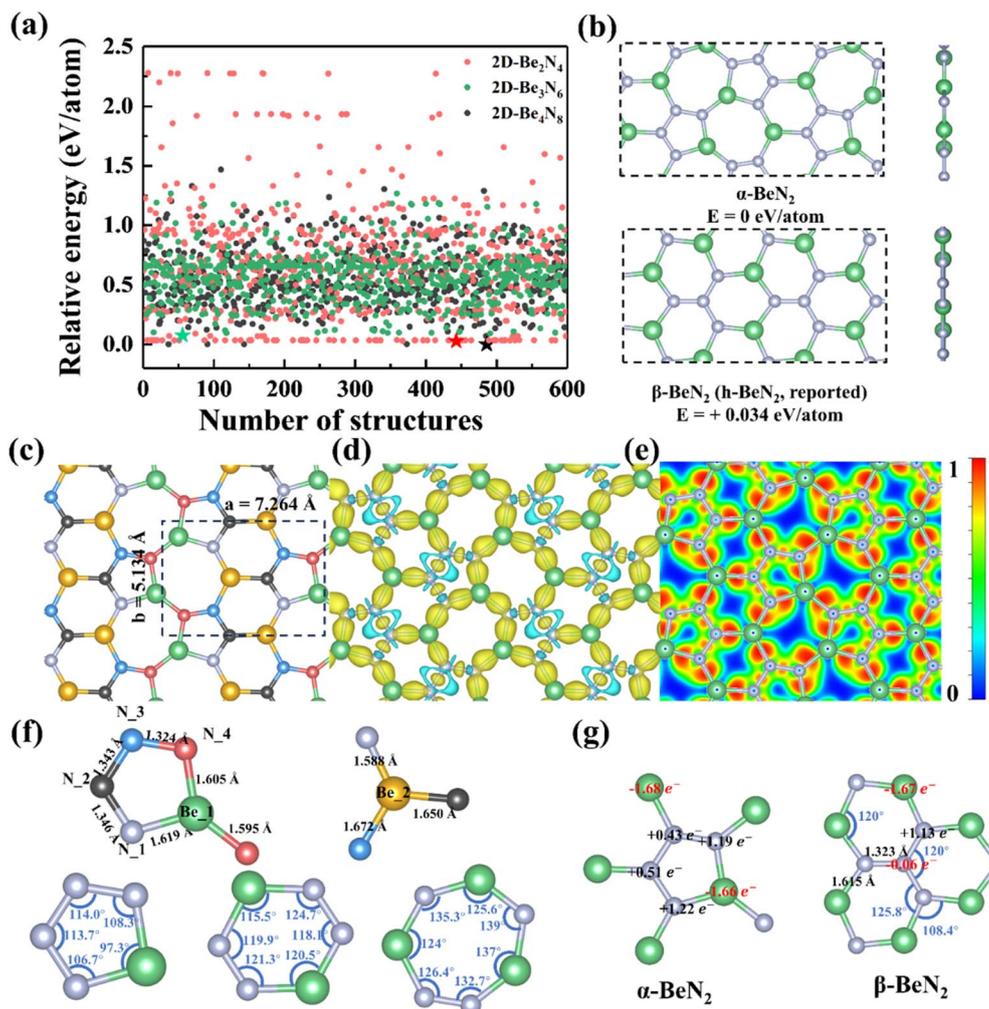


Fig. 1 (a) Energy distribution of  $\text{BeN}_2$  structures determined *via* global structure searches using the CALYPSO method. The red, green, and black dots represent systems with Be : N atom ratios of 2 : 4, 3 : 6, and 4 : 8, respectively. The pentagrams mark the lowest-energy structures in each system. (b) Structural representations of  $\alpha\text{-BeN}_2$  and  $\beta\text{-BeN}_2$  (h- $\text{BeN}_2$ ). (c) Schematic diagram of  $\alpha\text{-BeN}_2$ , with different colors used to distinguish non-equivalent but identical atoms. (d) Deformation electron density and (e) electron localization function of  $\alpha\text{-2D-BeN}_2$ . (f) Structural information of  $\alpha\text{-2D-BeN}_2$ . (g) Charge transfer analysis of  $\alpha\text{-BeN}_2$  and  $\beta\text{-BeN}_2$ .

$2\text{D-BeN}_2$  is merely  $-20 \text{ meV } \text{\AA}^{-2}$  (eqn S2<sup>†</sup>) with a large interlayer distance of  $2.92 \text{ \AA}$ , comparable to that of graphene ( $-19 \text{ meV } \text{\AA}^{-2}$ ) and h-BN ( $-17 \text{ meV } \text{\AA}^{-2}$ ), but significantly smaller than that of borophene ( $-192 \text{ meV } \text{\AA}^{-2}$ ) and silicene ( $-61 \text{ meV } \text{\AA}^{-2}$ ), confirming that the  $\alpha\text{-2D-BeN}_2$  layers are mainly stabilized by weak vdW interactions without any interlayered chemical bonds. Combining the results of AIMD simulation (Fig. S3<sup>†</sup>), the  $\alpha\text{-2D-BeN}_2$  monolayer should not dimerize under ambient condition. Then, according to the calculated phonon dispersion (PhonBand) and density of states (PhonDOS) (Fig. 2a), the  $\alpha\text{-2D-BeN}_2$  monolayer has no imaginary frequency in the whole Brillouin zone. Therefore, the  $\alpha\text{-2D-BeN}_2$  monolayer is lattice dynamical stable. Finally, the thermal stability of the new structure was confirmed using AIMD simulations. A  $2 \times 3$  supercell was employed in the simulations at temperatures ranging from 500 to 3000 K with an interval of 500 K. The snapshots of the geometrical structure after 5 ps simulation indicate that the monolayer can maintain its structural integrity

up to about 2500 K (Fig. 2b and S4<sup>†</sup>), and it will melt at 3000 K, suggesting the high thermal stability of  $\alpha\text{-2D-BeN}_2$  for applications.

To reveal the chemical bonding nature, the deformation electron density (DED, Fig. 1d), electron localization function (ELF, Fig. 1e), and the Bader charge analysis (Fig. 1g)<sup>60</sup> were calculated. The DED result indicates that the electrons are mainly distributed at the bridge site between N atoms and the nearest neighbor Be atoms but with partially between each two neighbor N atoms of  $\text{N}_4$  chain segment, suggesting significantly covalent hybridizations between Be and N atoms, and inside  $\text{N}_4$  chain segment. The ELF shows similar distribution characters, that electrons tend to mostly concentrate on the bridge site between N and Be atoms with considerable delocalization in  $\text{N}_4$  chain segment. The Bader charge analysis demonstrates that there is dominant charge transfer of  $1.66/1.68 e^-$  from  $\text{Be}_{-1}/\text{Be}_{-2}$  atoms to the  $\text{N}_4$  chain segment, less than  $2 e^-$  (the typical valence of  $\text{Be}^{2+}$ ), and the N atoms gain electrons of  $0.43\text{--}1.22 e^-$



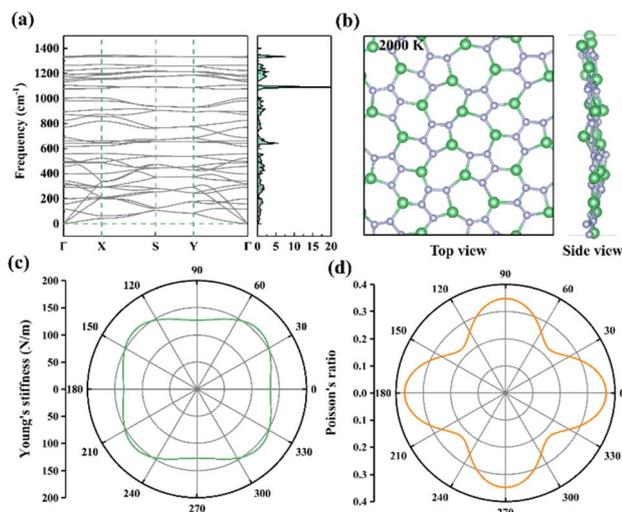


Fig. 2 (a) Phonon spectrum and phonon density of states of  $\alpha$ -2D-BeN<sub>2</sub>. (b) Snapshot of the  $\alpha$ -2D-BeN<sub>2</sub> structure after the AIMD simulation at 2000 K for 5 ps. (c) In-plane Young's stiffness and (d) Poisson's ratio of  $\alpha$ -2D-BeN<sub>2</sub>.

symmetrically but unequally with charge distribution of ( $N^{-1.19}N^{-0.43}N^{-0.51}N^{-1.22}$ ), different from those in h-BeN<sub>2</sub> of ( $N^{+0.06}N_3^{-1.13}$ ) (Fig. 1g). These results coherently indicate the ionic-covalent bonding feature of Be-N and the covalent bonding of N-N in the  $\alpha$ -2D-BeN<sub>2</sub> monolayer, in agreement with its isoelectronicity to h-BN (both are 4e and 3 folds per atom on average) with high strength bonds.

### 3.2 Mechanical, electronic, and optical properties

In mechanical properties, the  $\alpha$ -2D-BeN<sub>2</sub> monolayer was investigated by examining its elastic constants. The elastic constants were calculated to be  $C_{11} = 153.8 \text{ N m}^{-1}$ ,  $C_{22} = 145.4 \text{ N m}^{-1}$ ,  $C_{12} = C_{21} = 53.5 \text{ N m}^{-1}$ , and  $C_{66} = 63.8 \text{ N m}^{-1}$ , in compliance with the mechanical stability criteria for the 2D structure ( $C_{11} > 0$ ,  $C_{22} > 0$ ,  $C_{11}C_{22} - C_{12}^2 > 0$ ,  $C_{66} > 0$ ),<sup>61</sup> suggesting that the  $\alpha$ -2D-BeN<sub>2</sub> monolayer is mechanically stable. As shown in Fig. 2c and d, in-plane Young's stiffness ( $Y(\theta)$ , eqn (S3)<sup>†</sup> and Poisson's ratio ( $\nu(\theta)$ , eqn (S4)<sup>†</sup>) at a rotation angle of  $\theta$  are directionally varied, showing a certain degree of anisotropy in mechanical properties. For Young's stiffness, the  $\alpha$ -2D-BeN<sub>2</sub> monolayer has a value of  $Y(\theta)$  from 127 to 157  $\text{N m}^{-1}$  for all rotation angles,  $\theta$ , with an anisotropy of  $Y_{\text{max}}/Y_{\text{min}} = 1.24$ . The  $Y$  are  $Y_{11} = 134$  and  $Y_{22} = 127 \text{ N m}^{-1}$  along the direction- $a$  and - $b$ , respectively. Therefore, the  $\alpha$ -2D-Be<sub>3</sub>N<sub>2</sub> monolayer exhibits moderate and anisotropic rigidity for all directions with an observable difference of 30  $\text{N m}^{-1}$ . Compared with other 2D structure monolayers, it is comparable to that of MoS<sub>2</sub> (121  $\text{N m}^{-1}$ ),<sup>62</sup> and larger than that of silicene (62  $\text{N m}^{-1}$ )<sup>63</sup> and phosphorene (21–91  $\text{N m}^{-1}$ ),<sup>64</sup> but much smaller than that of graphene (330  $\text{N m}^{-1}$ )<sup>62</sup> and h-BN ( $\sim 279 \text{ N m}^{-1}$ ).<sup>65</sup> Interestingly, the  $\alpha$ -2D-BeN<sub>2</sub> monolayer has a large in-plane Poisson's ratio, ranging from 0.228 to 0.368 for all rotation angle,  $\theta$ , with a considerable anisotropy of  $\nu_{\text{max}}/\nu_{\text{min}} = 1.61$ . Therefore, the  $\alpha$ -2D-BeN<sub>2</sub> monolayer is a ductile

material in most directions (Poisson's ratio  $> 0.25$ ) with a relatively strong rigidity.

As shown in Fig. 3a,  $\alpha$ -2D-BeN<sub>2</sub> has a direct bandgap of 1.10 eV in the energy band structure for  $\alpha$ -2D-BeN<sub>2</sub> with the PBE functional. Both the valence band maximum (VBM) and the conduction band minimum (CBM) are positioned at the  $Y(1/2, 0, 0)$  point. The calculated projected density of states (PDOS, Fig. 3b) indicated that the VBM was dominantly contributed by N<sub>2p<sub>z</sub></sub> (especially N<sub>1</sub> and N<sub>4</sub>), while the CBM was mainly contributed by the p<sub>z</sub> orbital of all N atoms and Be<sub>2</sub> atoms (Fig. 3c). The HSE06 method provides that the more accurate bandgap is 1.82 eV with a work function of 4.93 eV. The bandgap of  $\alpha$ -2D-Be<sub>3</sub>N<sub>2</sub> is slightly larger than that of phosphorene (1.58 eV),<sup>64</sup> but smaller than that of h-BeN<sub>2</sub> (2.23 eV) and h-BN (5.66 eV)<sup>66</sup> with the HSE06 functional.

Furthermore, the carrier mobilities of the  $\alpha$ -2D-BeN<sub>2</sub> monolayer were calculated using the deformation potential (DP) theory.<sup>67</sup> For electron carriers, the effective mass is 0.96/0.61  $m_e$  with a high mobility of  $0.55/6.6 \times 10^4 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$  along the direction- $a/b$ , respectively. In comparison, the hole carrier has a close effective mass of  $-0.60/-0.81 m_e$  with a relatively small mobility of  $1.3/8.3 \times 10^3 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$ , along the direction- $a/b$ , respectively. The highest value is lower than that of graphene ( $3.4 \times 10^5 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$ )<sup>68</sup> and h-BeN<sub>2</sub> ( $3.4 \times 10^5 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$ ),<sup>40</sup> but higher than that of the BP monolayer ( $2.6 \times 10^4 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$ ),<sup>69</sup> offering potential applications of the  $\alpha$ -2D-BeN<sub>2</sub> monolayer in semiconductor electronics. See more calculation details in the ESI.<sup>†</sup>

The optical properties of  $\alpha$ -2D-BeN<sub>2</sub> were computed using the HSE06 method. Due to the anisotropy in structure, the dielectric constant of  $\alpha$ -2D-BeN<sub>2</sub> is expressed as  $\epsilon_{xx} \neq \epsilon_{yy} \neq \epsilon_{zz}$ . As shown in Fig. 3d, the absorption coefficients are different

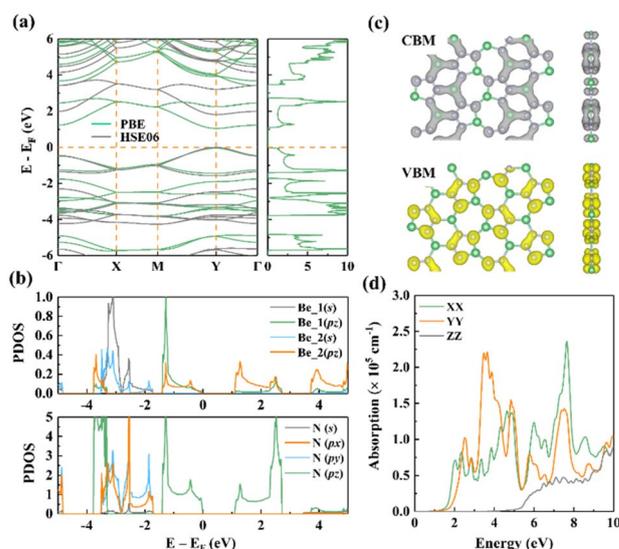


Fig. 3 (a) Band structure of  $\alpha$ -2D-BeN<sub>2</sub> (green: PBE level, gray: HSE06 level) and total density of states (PBE level). (b) Projected density of states (PDOS) of  $\alpha$ -2D-BeN<sub>2</sub>, with the Fermi level set to 0 eV. (c) Partial charge density of the CBM and VBM of  $\alpha$ -2D-BeN<sub>2</sub>. (d) Optical absorption coefficient of  $\alpha$ -2D-BeN<sub>2</sub>.



along the direction-*a* (axial *a*), -*b* (axial *b*) and -*c* (out-of-plane). Possessing a direct bandgap of 1.82 eV,  $\alpha$ -2D-Be<sub>3</sub>N<sub>2</sub> displays an anisotropic optical absorption spectrum with abundant absorbance in the visible range. The high intensity region started from about 1.9 eV with peaks up to  $2.4 \times 10^5 \text{ cm}^{-1}$  at 4.8, 6.0, and 8.0 eV for the direction-*a*, at 3.7 and 7.5 eV for the direction-*b*, and the intensity along the out-of-plane direction is quite slight until about 5.1 eV in the optical absorption spectrum. The in-plane absorption coefficient rapidly stepped up to a high intensity interval of  $1.0\text{--}2.4 \times 10^5 \text{ cm}^{-1}$  in the visible light region. With high-strength chemical bonds, high thermal stability, and high-density optical absorption in the visible light region,  $\alpha$ -2D-BeN<sub>2</sub> should be a promising candidate as a visible light detector and a donor in solar cells. See more calculation details in the ESI.†

### 3.3 Oxygen reduction/evolution reaction catalytic ability

There are rich electronic states around the relatively shallow Fermi level and many bare 3-fold Be atoms in the  $\alpha$ -2D-BeN<sub>2</sub> structure, which suggests the potential electrocatalytic activity to oxygen reduction reactions. For O<sub>2</sub> approach to and adsorption on the surface of  $\alpha$ -2D-BeN<sub>2</sub>, it prefers a side-on configuration on Be<sub>2</sub> with an adsorption free energy of  $-0.10 \text{ eV}$  among the different pathways, and the O–O bond is pronouncedly elongated to 1.24 and 1.36 Å, confirming the O<sub>2</sub> activation ability of the  $\alpha$ -2D-BeN<sub>2</sub> structure. The spatially constrained associative mechanism of ORR catalysis is mainly focused here (Fig. 4a). Specifically, the possible structures of each intermediate (O<sub>2</sub><sup>\*</sup>, OOH<sup>\*</sup>, O<sup>\*</sup>, and OH<sup>\*</sup>) in the four-electron pathway are considered across all active sites, with the assumption that adjacent reactions can only occur on the same or neighboring active sites. The free energy diagrams in Fig. 4a show that all electrochemical steps of the ORR are exothermic at an electrode potential (*U*) of 0 V. The hydrogenation of O<sub>2</sub><sup>\*</sup> to OOH<sup>\*</sup> at the Be<sub>2</sub> site was determined to be the potential-limiting step, as it possesses the least negative  $\Delta G$  of  $-0.43$  to  $-0.53 \text{ eV}$  for different pathways. As a result, the limiting

potential of the ORR ( $U_{L,ORR}$ ) was calculated to be 0.43–0.53 V for  $\alpha$ -2D-BeN<sub>2</sub>, higher than that of h-BeN<sub>2</sub> (0.40 V)<sup>48</sup> and smaller than that of the electrode of 2D biphenylenes ( $U_{L,ORR} = 0.69\text{--}0.73 \text{ V}$ )<sup>70,71</sup> and Pt metal (0.79 V).<sup>72</sup>

The reversible process of ORR, the oxygen evolution reaction (OER), was investigated for the electrocatalytic OER. The dehydrogenation of O<sup>\*</sup> to OOH<sup>\*</sup> at the Be<sub>2</sub> site was determined to be the potential-limiting step, as it has the largest positive  $\Delta G$  of 2.05 eV (Fig. 4b). Therefore, the limiting potential of the OER ( $U_{L,OER}$ ) was calculated to be 0.82 V for  $\alpha$ -2D-BeN<sub>2</sub>, smaller than that of other 2D structures, such as h-BN (0.93 V),<sup>73</sup> and graphene ( $U_{L,OER} = 1.37 \text{ V}$ ),<sup>74</sup> but higher than that of graphene (0.46 V)<sup>75</sup> and RuO<sub>2</sub> (0.42 V).<sup>76</sup> The calculation details of the ORR and OER are shown in the ESI.†

### 3.4 K ion adsorption and migration

The adsorption, migration and storage ability of potassium ions on  $\alpha$ -2D-BeN<sub>2</sub> monolayer were investigated. The adsorption of single K ions on the  $\alpha$ -2D-BeN<sub>2</sub> monolayer was studied based on a  $2 \times 3$  supercell structure model. As shown in Fig. 5a, three adsorption sites were examined, including R5, R6 and R7 sites. After the structural optimization, the adsorption energy based on eqn (S10)† ( $E_{\text{ads}}$ , vs. corresponding K metal) is  $-0.149$ ,  $-0.050$ , and  $-0.268 \text{ eV}$  for R5, R6 and R7 sites, respectively. Therefore, the R7 site is the most stable adsorption site. The Bader charge analysis indicates that the K ion on the R7 site loses 0.87 electrons, indicating the high-degree ionic state of K ions (+0.87).

The migration behavior of K ions is shown in Fig. 5b using the CI-NEB method.<sup>58</sup> Eight in-plane migration paths were simulated to cover the periodicity in the structure, including R7 → R7' (Path-1, labelled as P-1), R7 → R5 (P-2), R7 → R5' (P-3), R7 → R5'' (P-4), R7 → R6 (P-5), R5 → R6 (P-6), and R5 → R6' (P-7), R6 → R6' site (P-8, unstable), as shown in Fig. 5a. The calculated energy barrier ( $E_b$ ) of all paths ranges from 0.108 to 0.248 eV (Fig. 5b). The combination of “Path-2, -6, -5” along the direction-*a* is the most favorable migration path with

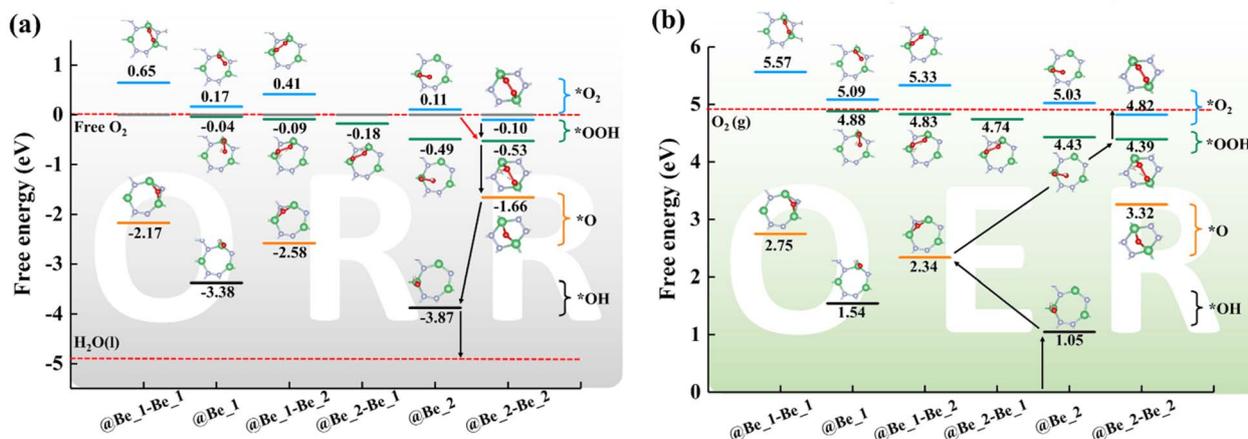


Fig. 4 Free energy diagrams with spatial considerations of the (a) ORR and (b) OER processes on  $\alpha$ -2D-BeN<sub>2</sub>. The x-axis represents different adsorption sites, with the assumption that each step of the ORR and OER reactions occurs at the same or adjacent sites.



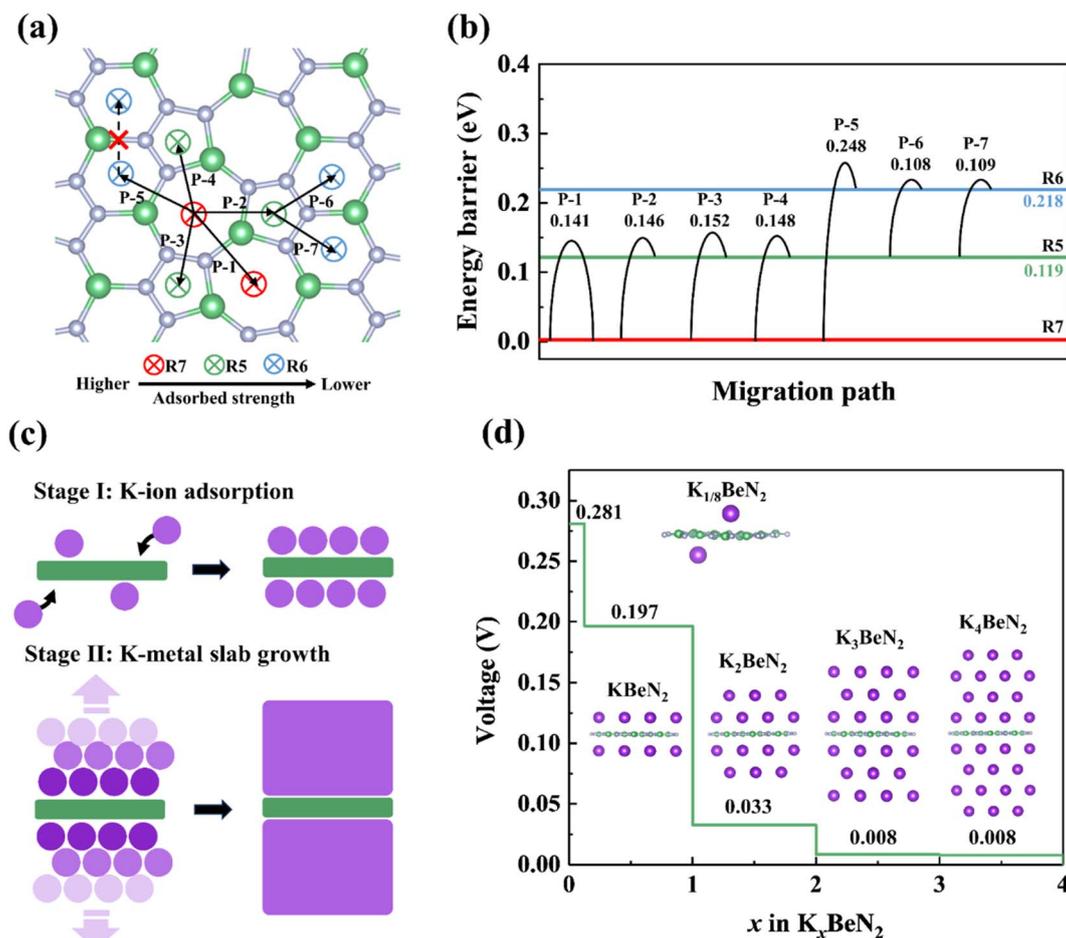


Fig. 5 (a) Adsorption sites and migration pathways of K on the surface of  $\alpha$ -2D-BeN<sub>2</sub>. (b) Migration energy barriers for K along different pathways, with the red, green, and blue lines representing the initial and final positions of K and their relative energies. (c) Schematic of the K-ion adsorption stage and K-metal slab growth on the surface of  $\alpha$ -2D-BeN<sub>2</sub>. (d) Voltage profiles corresponding to different K adsorption concentrations and side views of the structures.

a minimum  $E_b$  value of 0.146 eV, while the most favorable migration path is the combination of “Path-6, -7” ( $E_b = 0.109$  eV) along the direction- $b$  to migrate across the whole surface in periodicity, endowing the high K ion conduction ability at room temperature. In general, the K ion possesses the lowest migration energy barrier of only  $E_b = 0.109$ – $0.146$  eV, lower than that in graphite (0.19 eV),<sup>77</sup> comparable to that on graphene (0.09 eV),<sup>55</sup> but larger than that on MoS<sub>2</sub> (0.06 eV).<sup>78</sup> Therefore,  $\alpha$ -2D-BeN<sub>2</sub> monolayer should exhibit excellent K ion adsorption and conduction ability to be applied in iontronic devices *via* K ion-dominated bandgap change, and anode materials in PIBs through ion capture and transport.

### 3.5 K ion storage performances

To achieve the reusable K ion storage, the transition between potassiation and depotassiation needs to be a reversible process. The half-cell reaction on  $\alpha$ -2D-BeN<sub>2</sub> associated with K and K<sup>+</sup> is as follows:  $\text{BeN}_2 + x\text{K}^+ + xe^- \leftrightarrow \text{K}_x\text{BeN}_2$ . The thermodynamically stable structures of K<sub>x</sub>@ $\alpha$ -2D-BeN<sub>2</sub> (K<sub>x</sub>BeN<sub>2</sub>) at different K ion adsorption concentrations were determined by the formation

energy ( $E_f$ ) of K<sub>x</sub>BeN<sub>2</sub> based on eqn (S11).<sup>†</sup> As shown in Fig. S5,<sup>†</sup> the convex hull diagrams of the relationship between the calculated  $E_f$  and the K ion proportion in K<sub>x</sub>BeN<sub>2</sub> displays five stable K ion concentration points, which lies on the convex hull, according to thermodynamics stability criteria.

The adsorption of K ions includes two stages, namely the ion adsorption stage and the layered potassium metal slab growth stage, which is similar to that on the Ca<sub>2</sub>Si monolayer.<sup>79</sup> The storage of K ion is *via* ionic interactions between K and the  $\alpha$ -2D-BeN<sub>2</sub> surface for the first stage ( $\text{BeN}_2 + \text{K}^+ + e^- \leftrightarrow \text{KBeN}_2$ ). During the first stage, K ions first adsorbed at the R7 site on the surfaces, but with a placement transition to the R5 sites. For the second stage, the formation of K metal layers *via* K–K metal bonds dominates the process ( $\text{KBeN}_2 + 3\text{K}^+ + 3e^- \leftrightarrow \text{K}_4\text{BeN}_2$ , Fig. 5c). It should be noted that, due to the similar storage mechanism to K on the Ca<sub>2</sub>Si monolayer, only four K layers on each side of  $\alpha$ -2D-BeN<sub>2</sub> were examined here. For a layer number >5 for K ion adsorption, the process should be an unlimited K metal growth process, which is helpful to form a novel K metal phase and achieve safely ultrahigh capacity storage of K ions, similar to that occurring on the Ca<sub>2</sub>Si monolayer.<sup>79</sup>



Based on eqn (S12),<sup>†</sup> the average stepwise adsorption energy ( $E_{\text{step}}$ , vs. K metal bulk) of K ions in the first stage is  $-0.280$ ,  $-0.197$  eV per K atom for stable concentrations of  $x = 0.125$  and  $1$  in  $K_x\text{BeN}_2$ , and it is  $-0.033$ ,  $-0.008$ , and  $-0.008$  eV per K atom for  $x = 2, 3$ , and  $4$  in  $K_x\text{BeN}_2$  in the second stage, respectively. The maximum specific capacities ( $C_M$ ) of K ions on  $\alpha$ -2D- $\text{BeN}_2$  were calculated using eqn (S13).<sup>†</sup> The specific capacity ( $C_M$ ) of K ions is  $724 \text{ mA h g}^{-1}$  for the ionic state of K ions, and at least  $2895 \text{ mA h g}^{-1}$  for potassium storage with high-degree low valence K ions. Both of these two specific capacities are significantly higher than that of the experimental graphite anode ( $279 \text{ mA h g}^{-1}$ ),<sup>80</sup>  $\text{K}_2\text{C}_6\text{O}_6$  ( $218 \text{ mA h g}^{-1}$ ).<sup>81</sup> Considering multi-layer adsorption of K ions, the specific capacity is higher than most other 2D structures, graphene ( $558 \text{ mA h g}^{-1}$ ),<sup>70</sup> thgraphene ( $744 \text{ mA h g}^{-1}$ ),<sup>75</sup>  $\text{C}_{57}$  ( $1117 \text{ mA h g}^{-1}$ ),<sup>82</sup>  $\text{C}_{36}\text{H}_8$  ( $1278 \text{ mA h g}^{-1}$ ),<sup>83</sup>  $\text{C}_{18}\text{H}_6$  ( $1449 \text{ mA h g}^{-1}$ ),<sup>84</sup> biphenylene-based carbon allotropes ( $1116$ – $1489 \text{ mA h g}^{-1}$ ),<sup>70</sup> but smaller than  $\text{Ca}_2\text{Si}$  ( $5459 \text{ mA h g}^{-1}$ ).<sup>79</sup>

Based on the formation convex hull result, the open-circuit voltage ( $V_{\text{OC}}$ ) profile was calculated using eqn (S14).<sup>†</sup> As shown in Fig. 5d, there are four voltage plateaus at different K ion adsorption concentrations, displaying the profile of voltage plateaus with the  $K$  concentration range of  $0.280$  ( $K_{x=0-0.125}\text{C}_6$ )  $\rightarrow 0.197$  ( $x = 0.125-1$ )  $\rightarrow 0.033$  ( $x = 1-2$ )  $\rightarrow 0.008$  ( $x = 2-3$ )  $\rightarrow 0.008$  ( $x = 3-4$ ) V. Therefore,  $\alpha$ -2D- $\text{BeN}_2$  exhibits a voltage  $V_{\text{OC}}$  ranging from  $0.280$  to  $0.008$  V in K ion storage, indicating its promising voltage performance as a PIB anode material.

## 4. Conclusions

In summary, we have investigated the structural stability, mechanical properties, electronic properties, optical absorption, oxygen reduction/evolution catalysis and potassium storage ability of the  $\alpha$ -2D- $\text{BeN}_2$  monolayer (with an iso-electronicity to h-BN, and there are  $4e$  and  $3$  folds per atom on average for both structures) based on the first-principles theory. The monolayer has good lattice dynamics and excellent thermal stability to maintain its basic structural framework up to about  $2500$  K. With a moderate direct bandgap of  $1.82$  eV, it displays a high carrier mobility (up to  $6.6 \times 10^4 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$ ) and high-intensity photon absorption in the visible region. It exhibits a relatively large Poisson's ratio ranging from  $0.228$  to  $0.368$ , oxygen reduction/evolution catalysis ability, outstanding potassium storage ability with an ultrahigh specific capacity of  $2895 \text{ mA h g}^{-1}$ , a good voltage ranging from  $0.280$  to  $0.008$  V, and a low migration barrier energy of  $0.109$ – $0.146$  eV. Owing to the novel nature and significant properties, the  $\alpha$ -2D- $\text{BeN}_2$  monolayer is expected to be an anisotropic multifunctional material for wide-ranging applications in various fields such as semiconductor electronics, visible-light detectors, donors in solar cells, ductile materials, iontronic devices, and potassium ion anode materials.

## Data availability

The data supporting this article have been included as part of the ESI.<sup>†</sup>

## Author contributions

S. N.: computation executing, methodology, investigation, data curation, writing – original draft. J. J.: computation executing, investigation, formal analysis, data analysis, visualization, writing – original draft. W. W.: discussion of the research scheme, manuscript review, funding acquisition. X. W.: manuscript review, funding acquisition. Z. Z., Z. W.: conceptualization, methodology, data analysis, writing – review & editing, supervision.

## Conflicts of interest

The authors declare no competing financial interest.

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