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## Thermal expansion of lithiated silicon ( $\text{Li}_{13}\text{Si}_4$ and $\text{Li}_7\text{Si}_3$ ) anodes: a powder neutron diffraction study

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Whilst at room temperature structural changes on lithiation of the silicon electrode are hard to study due to formation of amorphous phases, at high temperatures, used in thermal batteries, clear phase changes linked to voltage plateaux are observed. Here we report results from a galvanostatic discharge of a  $\text{FeS}_2/\text{LiCl-KCl}/\text{Li}_{13}\text{Si}_4$  cell at 500 °C. The cell discharge showed a flat voltage plateau between  $\text{Li}_{13}\text{Si}_4$  and  $\text{Li}_7\text{Si}_3$  which indicates that both phases are in equilibrium and are line phases. *In situ* powder neutron diffraction study of two lithiated phases of silicon,  $\text{Li}_{13}\text{Si}_4$  and  $\text{Li}_7\text{Si}_3$ , was performed. The two phases were heated from room temperature to 500 °C. This showed the phases did not become amorphous and did not undergo phase changes, with both phases being remarkably stable. The variation with temperature of the unit cell parameters was linear. The volumetric thermal expansion coefficient of  $\text{Li}_{13}\text{Si}_4$  is  $99.3 \times 10^{-6} \text{ °C}^{-1}$  and  $\text{Li}_7\text{Si}_3$  is  $106 \times 10^{-6} \text{ °C}^{-1}$ . The volumetric thermal expansion of the two phases is significantly larger than that of silicon and closer to the thermal expansion of lithium metal. Thus, the  $\text{Li}_x\text{Si}$  electrode is mechanically closer to lithium than to silicon, and it can be considered as silicon clusters embedded within the lithium array rather than the silicon lattice hosting lithium.

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### Introduction

Silicon is a promising negative electrode material for lithium-ion batteries because of its high theoretical capacity that is ten times higher than graphite. Silicon suffers from large volume change of up to 400% (ref. 1) when lithium is inserted<sup>2</sup> at room temperature which leads to contact loss of electrode and capacity loss in the first cycle. Lithium reacts with silicon by forming an alloy which breaks the silicon matrix.<sup>3</sup> The lithiation mechanism of silicon at room temperature has been widely discussed in the literature; however, there is no clear consensus. Limthongkul *et al.* reported solid-state amorphisation occurs during lithiation, forming silicon and amorphous  $\text{Li}_x\text{Si}$  which are separated by a sharp reaction front with a thickness in the nanometre scale.<sup>4</sup>

At room temperature, the lithiation of silicon, during the cycling of a crystalline silicon electrode *vs.* a lithium electrode in a coin cell, results in one broad voltage plateau.<sup>5</sup> Approximately  $3500 \text{ mA h g}^{-1}$  is observed from the discharge of silicon at room temperature.<sup>5</sup> This is close to the theoretical capacity of silicon =  $3580 \text{ mA h g}^{-1}$  with a fully lithiated state of  $\text{Li}_{15}\text{Si}_4$ . Obrovac

and Christensen first reported that crystalline  $\text{Li}_{15}\text{Si}_4$  forms when the potential is less than 0.05 V *vs.* Li.<sup>5</sup> The study observed the voltage plateaux of coin cells containing crystalline silicon *vs.* lithium electrode that were stopped at various states of charge for *ex situ* X-ray diffraction studies.<sup>5</sup> From the X-ray diffraction data collected at room temperature, crystalline  $\text{Li}_{15}\text{Si}_4$  peaks were identified.<sup>5</sup>  $\text{Li}_{15}\text{Si}_4$  is a metastable phase.<sup>6</sup> The structure of  $\text{Li}_{15}\text{Si}_4$  was established using single-crystal X-ray diffraction at room temperature by Zeilinger *et al.* who synthesised the phase from equilibrated melts and isolated the phase using isothermal centrifugation.<sup>6</sup>

Because the cycling of a silicon electrode at room temperature involves the formation of amorphous phases, nuclear magnetic resonance (NMR) studies are available in the literature.<sup>7–10</sup> Key *et al.* did room temperature <sup>7</sup>Li and <sup>29</sup>Si NMR studies where silicon clusters were found as intermediate units during cycling of crystalline silicon *vs.* lithium in coin cells.<sup>7,8</sup>

The formation of amorphous phases during lithiation is difficult to study with X-ray diffraction. On the other hand, clear phase changes are observed at high temperature, in thermal batteries, linked to voltage plateaux. Thermal batteries are an established primary battery technology that are used for specialised applications such as aircraft emergency power supplies, space flights, and borehole drilling.<sup>11</sup> Thermal batteries are implemented when a constant power needs to be drawn over a period of time.  $\text{Li}_{13}\text{Si}_4$  is the most common anode material for thermal batteries whereas  $\text{Li}_7\text{Si}_3$  cannot provide the power

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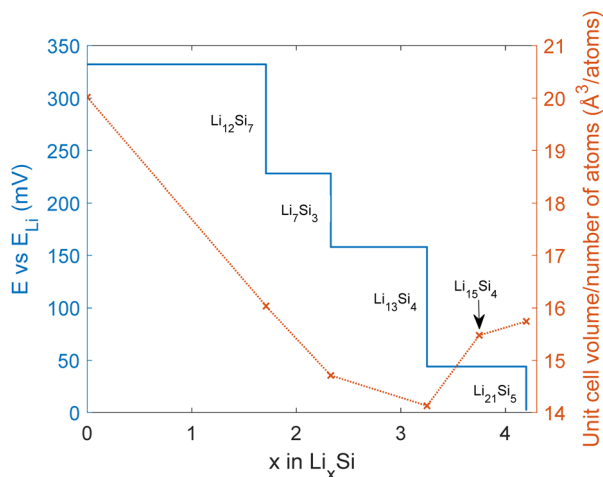


Fig. 1 Coulometric titration curve for lithium–silicon phases at 415 °C adapted from a study by Wen and Huggins.<sup>13</sup> The unit cell volume per total number of atoms of Li–Si phases, and Si are shown.

needed for high-rate pulsing due to a lower lithium diffusion in the phase.<sup>12</sup>

Wen and Huggins reported that the electrochemical alloying of lithium and silicon at high temperature (415 °C) follows the equilibrium Li–Si phase diagram with four distinct voltage plateaux, which corresponds to the formation of  $\text{Li}_{12}\text{Si}_7$ ,  $\text{Li}_7\text{Si}_3$ ,  $\text{Li}_{13}\text{Si}_4$ , and  $\text{Li}_{21}\text{Si}_5$ .<sup>13</sup>  $\text{Li}_{13}\text{Si}_4$  and  $\text{Li}_7\text{Si}_3$  are reported to be stable phases that congruently melt at 722 and 752 °C, respectively, whilst  $\text{Li}_{22}\text{Si}_5$  and  $\text{Li}_{12}\text{Si}_7$  incongruently melt at 628 and 648 °C, respectively.<sup>14,15</sup>

The transition from  $\text{Li}_{13}\text{Si}_4$  to  $\text{Li}_7\text{Si}_3$  has a voltage change of 44 mV to 158 mV with respect to lithium,<sup>13</sup> and the transition from  $\text{Li}_7\text{Si}_3$  to  $\text{Li}_{12}\text{Si}_7$  has a voltage change of 158 mV to 288 mV with respect to lithium.<sup>13</sup> The voltages and unit cell volumes divided by the total number of atoms of the Li–Si phases are shown in Fig. 1. Fig. 1 shows the unit cell volume decreases as silicon becomes more lithiated until the ratio is  $\text{Li}_{13}\text{Si}_4$  ( $\text{Li}_{3.25}\text{Si}$ ). The unit cell volume expands with further lithiation until the ratio is  $\text{Li}_{21}\text{Si}_5$  ( $\text{Li}_{4.2}\text{Si}$ ).

The structures of the four thermodynamically stable Li–Si phases at high temperature ( $\text{Li}_{21}\text{Si}_5$ ,  $\text{Li}_{13}\text{Si}_4$ ,  $\text{Li}_7\text{Si}_3$  and  $\text{Li}_{12}\text{Si}_7$ ) are shown in Fig. 2. The coulometric titration was measured using a three electrode cell (Al, “LiAl”/LiCl–KCl/Li<sub>x</sub>Si).<sup>13</sup> Al,

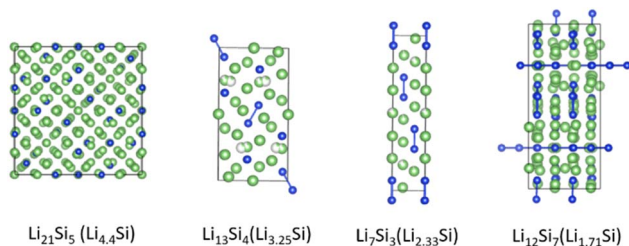


Fig. 2 Thermodynamically stable phases in the lithium–silicon system.<sup>13</sup> The green atoms are lithium, and the blue atoms are silicon. The phases have complex structures and are structurally different to elemental lithium or silicon. The structures were visualised on VESTA.<sup>16</sup>

“LiAl” represents a saturated solid solution of lithium in aluminium and an intermediate LiAl phase.  $\text{Li}_{15}\text{Si}_4$  was not observed at 415 °C, so it only exists in ambient conditions.

## $\text{Li}_{21}\text{Si}_5$

$\text{Li}_{21}\text{Si}_5$  (416 atoms per unit cell) is a lithium rich phase.  $\text{Li}_{21}\text{Si}_5$  has 12 Li sites and 4 Si sites.<sup>17</sup> It was previously thought to be  $\text{Li}_{22}\text{Si}_5$ , but a single crystal X-ray diffraction study showed it has a composition of  $\text{Li}_{21}\text{Si}_5$ .<sup>17</sup> The unit cell is shown in Fig. 3. The crystal data from Nesper *et al.*<sup>17</sup> is shown in Table 1. The synthesis of  $\text{Li}_{21}\text{Si}_5$  was described briefly in the literature. A stoichiometric mixture of lithium and silicon was sealed in a niobium ampoule. The ampoule was heated to 727 °C.<sup>17</sup> The crystals were collected after a slow cooling. The structure was determined by a least-squares refinement with 67 parameters and 356 reflections.<sup>17</sup>

## $\text{Li}_{13}\text{Si}_4$

$\text{Li}_{13}\text{Si}_4$  is a lithium rich phase.  $\text{Li}_{13}\text{Si}_4$  has 38 atoms per unit cell.  $\text{Li}_{13}\text{Si}_4$  has 8 Li and 2 Si sites.<sup>19</sup> The unit cell is shown in Fig. 4.

The single crystal X-ray diffraction data reported by Zeilinger *et al.*<sup>19</sup> is shown in Table 2. Zeilinger *et al.* synthesised  $\text{Li}_{13}\text{Si}_4$  from a mixture of lithium rods and silicon powder. The

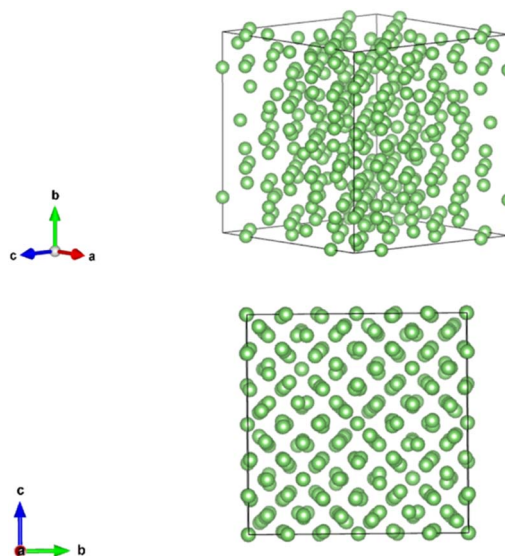


Fig. 3 Primitive unit cell of  $\text{Li}_{21}\text{Si}_5$ . The unit cell is cubic and made of 416 atoms. There are no partially occupied sites. The figure only shows the array of lithium atoms in green.

Table 1  $\text{Li}_{21}\text{Si}_5$  crystal data and information about data collection<sup>17,18</sup>

Space group	Cubic $F\bar{4}3m$
$a$ (Å)	18.7100(20)
$V$ (Å <sup>3</sup> )	6549.699
Radiation	Mo $K\alpha$
$T$ (K)	298
Diffractometer	P1 four circle
Theoretical specific capacity (mA h g <sup>-1</sup> )	4008



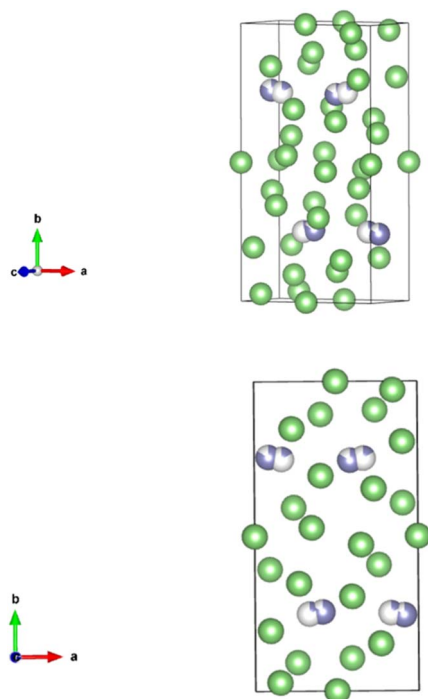


Fig. 4 The primitive unit cell of  $\text{Li}_{13}\text{Si}_4$ . The unit cell is orthorhombic and is made from 38 atoms. There are two partially occupied lithium sites, highlighted with purple in the figure, which are located next to each other and can be considered a split site. The partially occupied lithium sites have a 0.84/0.16 ratio. The figure only shows the array of lithium atoms.

synthesis was carried out in an argon glovebox. The mixture was placed into a tantalum ampoule which was arc welded inside the glovebox.<sup>20</sup> The tantalum ampoule was heated in a muffle furnace. The sample was heated to 750 °C for 30 minutes.<sup>5</sup> It was cooled to 500 °C for 1 hour.<sup>20</sup> The ampoule was transferred back into the glovebox and the final single crystals were collected. The single crystals were sealed in a 0.3 mm diameter glass capillary for X-ray diffraction.<sup>19</sup> The structure was determined by a least-squares refinement with 60 parameters and 2429 reflections.<sup>19</sup>

## $\text{Li}_7\text{Si}_3$

$\text{Li}_7\text{Si}_3$  (21 atoms per unit cell) is a violet phase due to its distinct colour. The dark violet colour was also observed after

Table 2  $\text{Li}_{13}\text{Si}_4$  crystal data and information about data collection<sup>19</sup>

Space group	Orthorhombic <i>Pbam</i>
<i>a</i> (Å)	7.9488(4)
<i>b</i> (Å)	15.1248(8)
<i>c</i> (Å)	4.4661(2)
<i>V</i> (Å <sup>3</sup> )	536.932
Radiation	Mo K $\alpha$
<i>T</i> (K)	100
Diffractometer	Bruker APENXII CCD
Theoretical specific capacity (mA h g <sup>-1</sup> )	3101

synthesising  $\text{Li}_7\text{Si}_3$  in this work.  $\text{Li}_7\text{Si}_3$  has 3 Li and 1 Si sites.<sup>21</sup> The unit cell is shown in Fig. 5.

The ICSD database has only one study that determined the structure of  $\text{Li}_7\text{Si}_3$  or  $\text{Li}_{2.33}\text{Si}$ . The crystal data is shown in Table 3.

## $\text{Li}_{12}\text{Si}_7$

$\text{Li}_{12}\text{Si}_7$  (152 atoms per unit cell) is a silicon rich phase.  $\text{Li}_{12}\text{Si}_7$  has 13 Li and 9 Si sites.<sup>22</sup> The unit cell is shown in Fig. 6.

The synthesis of  $\text{Li}_{12}\text{Si}_7$  is described briefly in the literature. The sample was prepared by mixing lithium and silicon and placing the mixture in a sealed tantalum ampoule. The ampoule was heated to 997 °C.<sup>22</sup> The  $\text{Li}_{12}\text{Si}_7$  X-ray diffraction data is shown in Table 4.

This work explores if  $\text{Li}_{13}\text{Si}_4$  and  $\text{Li}_7\text{Si}_3$  undergo phase changes or become an amorphous phase on heating, and explores the thermal expansion of both phases which gives insights into the mechanical behaviour of the amorphous  $\text{Li}_x\text{Si}$  phase that forms during lithiation of silicon at room temperature. To the best of our knowledge, the current literature does not include a high-temperature neutron diffraction study of  $\text{Li}_x\text{Si}$  phases. Neutron diffraction is ideal for studying materials composed of lithium in the presence of heavier atoms because neutrons scatter from atomic nuclei, unlike X-ray scattering which depends on the number of electrons.<sup>23</sup> In this work, we

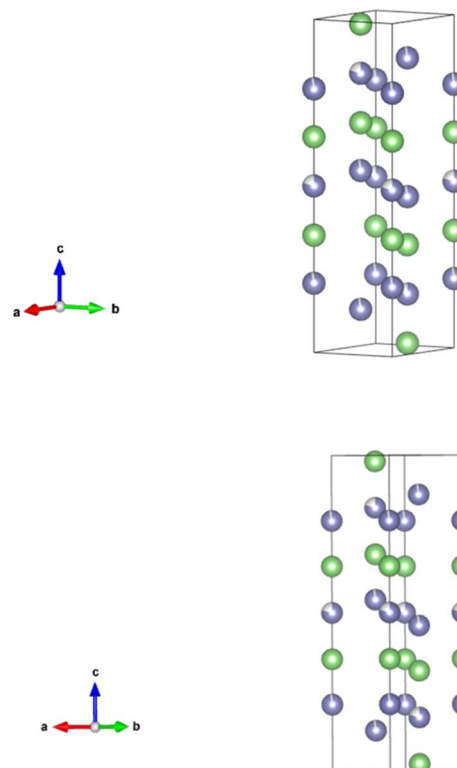


Fig. 5 The primitive unit cell of  $\text{Li}_7\text{Si}_3$ . The unit cell is trigonal and is made of 21 atoms. There are two partially occupied lithium sites, highlighted with purple in the figure, with 0.95 and 0.8 occupancy. The figure only shows the array of lithium atoms.



Table 3  $\text{Li}_7\text{Si}_3$  crystal data and information about data collection<sup>21</sup>

Space group	Trigonal $R\bar{3}m$
$a$ (Å)	4.4350(10)
$b$ (Å)	4.4350(10)
$c$ (Å)	18.1340(30)
$V$ (Å <sup>3</sup> )	308.895
Radiation	X-ray
$T$ (K)	293
Diffractometer	N/A
Theoretical specific capacity (mA h g <sup>-1</sup> )	2226

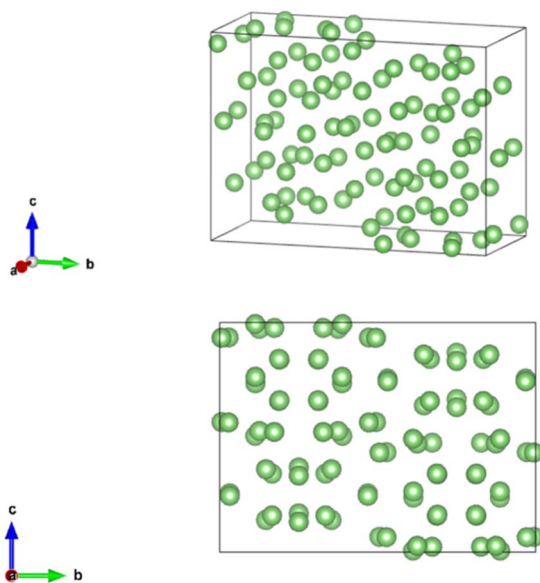


Fig. 6 The primitive unit cell of  $\text{Li}_{12}\text{Si}_7$ . The unit cell is orthorhombic and made of 152 atoms. There are no partially occupied sites. The figure only shows the array of lithium atoms in green.

Table 4  $\text{Li}_{12}\text{Si}_7$  crystal data and information about data collection<sup>22</sup>

Space group	Orthorhombic $Pnma$
$a$ (Å)	8.6100(20)
$b$ (Å)	19.7380(40)
$c$ (Å)	18.1340(30)
$V$ (Å <sup>3</sup> )	308.895
Radiation	X-ray
$T$ (K)	293
Diffractometer	N/A
Theoretical specific capacity (mA h g <sup>-1</sup> )	1636

report a galvanostatic cell discharge to identify voltage plateaux and high-temperature structural characterisation of  $\text{Li}_{13}\text{Si}_4$  and  $\text{Li}_7\text{Si}_3$  from time-of-flight (TOF) powder neutron diffraction data collected at the ISIS Neutron Source, Rutherford Appleton Laboratory, UK. The bonding environments are also discussed.

## Experimental

### *Ex situ* synthesis

The handling and storage of materials were carried out in an argon glovebox (PureLab HE, Ar atmosphere,  $\text{H}_2\text{O}$  less than

0.5 ppm and  $\text{O}_2$  levels less than 1 ppm). Starting materials were lithium metal (Li; granular 4–10 mesh 99%) and silicon powder (Si; 325 mesh 99%).  $\text{Li}_{13}\text{Si}_4$  was purchased from Albemarle.  $\text{Li}_7\text{Si}_3$  was synthesised *ex situ*.

A solid-state synthesis method was adapted from literature.<sup>7,17,24–26</sup> In this work, 0.5 g of stoichiometric ratio of lithium and silicon were mixed by hand with a mortar and pestle in the glovebox for 15 minutes. The mixture was placed in a tantalum crucible (melting point = 3017 °C) and transferred into a silica glass test tube attached to a valve fitting with an O-ring. The silica glass test tube had dimensions of 9 mm inner diameter and 12 mm outer diameter.

The silica tube was connected to a vacuum pump. The tube was evacuated (gauge pressure =  $10^{-5}$  mbar) and sealed into a silica glass ampoule using a high-temperature flame. Prior to use, the silica glass and tantalum were wiped clean with ethanol and dried in an oven at 80 °C.

The ampoule was placed in a tube furnace. The temperature was increased at a rate of 5 °C per minute and kept at 190 °C for 2 hours to allow the lithium to melt close to its melting point. The temperature slowly increased to 500 °C at a rate of 2 °C min<sup>-1</sup>. The sample remained at this temperature for 12 hours. The reaction was stopped, and the temperature decreased at a rate of 5 °C per minute to below 180.5 °C and the ampoule was moved away from the hot zone of the furnace. Once cooled, the ampoule was cut open in the glovebox to obtain the final powder. The alloying of lithium and silicon is complex due to the inert conditions required for synthesis.

### Powder X-ray diffraction

X-ray diffraction patterns were obtained at room temperature from the diffractometer (PANalytical Empyrean). The Bragg–Brentano focusing geometry was used. The diffractometer has  $\text{CuK}\alpha 1$  radiation with wavelength of  $\lambda = 1.54$  Å. The diffractometer has a X'celerator RTMS detector. Moisture sensitive samples were placed in a zero-background silicon substrate holder and had a protective Kapton film covering the holder. The diffraction range was 5 to 90°  $2\theta$  and the data was collected for 60 minutes. The resulting diffraction pattern shows the peak positions ( $x$ -axis) and relative peak intensities ( $y$ -axis) of the sample.

The phases were identified by comparing the experimental diffraction pattern with a reference pattern from a database. In this work, the Inorganic Crystal Structure Database (ICSD) was used to find reference patterns from crystallographic information files (CIF). The experimental and reference patterns were compared by superimposing them on the same plot in CrystalDiffract. The X-ray diffraction patterns were indexed and refined using WinXPOW to determine phase purity.

### Soft X-ray emission spectroscopy

Soft X-ray emission spectroscopy was performed on the JEOL JSM-IT800 FEG-SEM. Soft X-ray emission spectroscopy allows the mapping of lighter elements such as lithium ions because



the X-rays of lighter elements have lower energies. Soft X-ray emissions are produced from the electronic transitions inside the sample.<sup>27</sup> It is a characterisation technique that probes the energy state of bonding electrons<sup>27</sup> by measuring the difference in the peak shape.<sup>27</sup> The acceleration voltage was 5 kV and beam current was 60 nA. The nominal energy resolution was 0.3 eV.

### Electrochemical discharge

A cell was made from 0.15 g of  $\text{Li}_{13}\text{Si}_4$ , 0.05 g  $\text{LiCl-KCl-MgO}$  (anode); 0.2 g  $\text{LiCl-KCl}$  (electrolyte) mixed with 35% wt.  $\text{MgO}$  (separator); and 0.15 g  $\text{FeS}_2$ , 0.05 g  $\text{LiCl-KCl-MgO}$  (cathode) were pressed into three different pellets. The two electrode pellets were 13 mm in diameter. The electrolyte/separator pellet was 15 mm in diameter. The pellets were loaded into a Swagelok type cell which allowed electrochemical testing to be performed at 500 °C *ex situ* inside the argon glovebox. The testing rig consists of a vertical tube furnace with a platform to hold the cell. Solartron analytical software was used to collect the data. The raw data was plotted on XM Studio ECS software. The cell was tested galvanostatically with slow discharge (current = 10 mA) to identify the voltage plateaus.

### Powder neutron diffraction

Powder neutron diffraction data were collected on the Polaris high flux, medium resolution diffractometer at the ISIS Neutron and Muon Source, UK. The high intensity of the incident neutron beam and a large solid angle of detector coverage enables it to collect good quality data in short periods of time from small samples.

Polaris's multiple detector banks allow the collection of diffraction patterns of varying  $\Delta d/d$  Bragg peak resolutions over a series of partially overlapping  $d$ -spacings. The banks at lower  $2\theta$  angles access the longest  $d$ -spacings but have lower resolution. The banks at higher  $2\theta$  angles have the best resolution but measure to progressively smaller maximum  $d$ -spacings.

For this study, the best compromise between required  $d$ -spacing range and peak resolution was achieved in detector bank 3 (average  $2\theta$  angle = 52°). The dimensions of the incident beam were decreased to 10 mm wide × 14 mm high to prevent the beam scattering from the steel and ceramic components in the sample holder. This would contaminate the diffraction patterns with unwanted Bragg reflections.

A thin pair of vanadium plates held the sample in place in the neutron beam. Vanadium has a low neutron scattering length ( $b = -0.39$  fm). This means the intensities of its Bragg reflections are low relative to those from the samples, so they make a negligible contribution to the overall diffraction pattern.

2g of  $\text{Li}_{13}\text{Si}_4$  and  $\text{Li}_7\text{Si}_3$  were weighed. The samples were pressed into pellets of 20 mm diameter in an argon glovebox using an electronically controlled uniaxial hydraulic press. The pellets were made using a pressure of 3 tonnes for 3 minutes. The pellets were sealed, under argon, in aluminium bags and transported to the ISIS Neutron and Muon Source.

The pellets were placed into an electrochemical testing rig designed by the University of St. Andrews.<sup>28</sup> The furnace

temperature was monitored using a thermocouple located close to the sample.

### Neutron data analysis

Rietveld Refinement was carried out on the neutron diffraction patterns using known unit cell parameters and atom positions from the ICSD database. The CIF files from the database provide initial approximations to fit the calculated pattern with the experimental pattern. The objective of the refinement is to find the unit cell parameters at different temperatures and to find trends in the parameters which may indicate phase transitions. The General Structure Analysis System (GSAS) II<sup>29</sup> and EXPGUI graphical interface were used for refinement.<sup>30</sup>

## Results and discussion

### Phase identification

$\text{Li}_{13}\text{Si}_4$  and  $\text{Li}_7\text{Si}_3$  powder were characterised by X-ray diffraction. Fig. 7 shows that the  $\text{Li}_{13}\text{Si}_4$  and  $\text{Li}_7\text{Si}_3$  patterns agree with the reference patterns by Zeilinger *et al.*<sup>19</sup> and von Schnering *et al.*,<sup>21</sup> respectively. The amorphous broad peaks around  $20^\circ 2\theta$  are due to the Kapton film covering the samples during the measurements. The synthesised  $\text{Li}_7\text{Si}_3$  had unreacted silicon in the first batch, and this is likely because a small quantity of silicon powder fell outside of the tantalum foil during loading.

The peaks in Fig. 7 were indexed using WinXPOW. A peak list for each diffraction pattern was made. All peaks above 10% relative intensity were indexed for  $\text{Li}_{13}\text{Si}_4$  which indicates the phase had no significant impurities. The unit cell was determined to have  $a = 7.985(6)$  Å,  $b = 15.168(7)$  Å,  $c = 4.4771(21)$  Å and  $V = 542.2(7)$  Å<sup>3</sup> after refinement.

In Fig. 7, all peaks above 10% relative intensity for the second batch of  $\text{Li}_7\text{Si}_3$  (orange graph) were indexed which indicates this phase did not have significant impurities. The unit cell was determined to have  $a = 4.438(3)$  Å,  $c = 18.140(13)$  Å, and  $V = 309.42(24)$  Å<sup>3</sup> after refinement.

In Fig. 7, the first batch of  $\text{Li}_7\text{Si}_3$  (blue graph) had impurities of Si and  $\text{Li}_{13}\text{Si}_4$  after indexing peaks with 10% relative intensity on WinXPOW. 7 Peaks remained unindexed which indicates impurities. The two batches from Fig. 7 were mixed to make a 2 g pellet for the neutron diffraction study.

### Cell discharge

The galvanostatic discharge at 500 °C shows two distinct voltage plateaux (Fig. 8). The voltage plateaux show  $\text{Li}_{13}\text{Si}_4$  is an ideal negative electrode for high-capacity thermal batteries. The  $\text{Li}_{13}\text{Si}_4/\text{Li}_7\text{Si}_3$  plateau is flat with a constant voltage which means  $\text{Li}_{13}\text{Si}_4$  and  $\text{Li}_7\text{Si}_3$  are in equilibrium and both phases are line phases. The change in voltage is determined by the transitions in the  $\text{FeS}_2$  positive electrode.

Fig. 8 shows the cell gives a voltage of 1.9 V which is close to the 1.8 V reported by Guidotti and Masset.<sup>11</sup> The two voltage plateaux shown in Fig. 9 also align with the voltage plateaux reported by Guidotti and Masset.<sup>11</sup>

As the transition of  $\text{Li}_{13}\text{Si}_4$  to  $\text{Li}_7\text{Si}_3$  occurs, the emf of the electrode is  $-0.15$  V vs.  $\text{Li-Al}$  at 415 °C.<sup>13</sup> The transition from



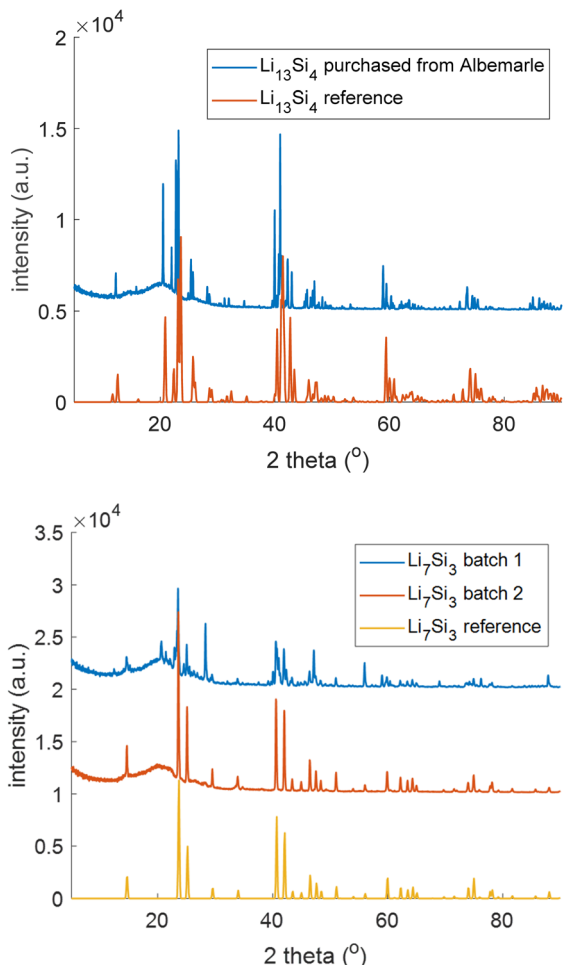


Fig. 7 *Ex situ* X-ray diffraction patterns of  $\text{Li}_{13}\text{Si}_4$  and  $\text{Li}_7\text{Si}_3$  recorded from 5 to  $90^\circ$   $2\theta$  at room temperature. The experimental patterns are compared with the reference patterns of  $\text{Li}_{13}\text{Si}_4$  and  $\text{Li}_7\text{Si}_3$ , respectively.

$\text{FeS}_2$  to  $\text{Li}_3\text{Fe}_2\text{S}_4$  has an emf of +1.75 V vs. Li–Al at 415 °C.<sup>31</sup> The full cell potential is  $E_{\text{cell}} = E_{\text{cathode}} - E_{\text{anode}} = +1.75 \text{ V} - (-0.15 \text{ V}) = +1.90 \text{ V}$ . The positive cell potential indicates that the overall redox reaction is spontaneous.

### Bonding environments

Fig. 9 presents the results of the soft X-ray emission spectra where a lithium K-emission (2s to 1s shell) occurs, and a silicon L-emission (3p to 2p shell) occurs. Fig. 9 shows the background subtracted spectra that were normalised by the maximum intensity of the lithium K peak. Lithium has a single asymmetric spectral peak. This is because of the electronic transition from the p states of the valence bands to the 1s state of the atom.<sup>32</sup> Crystalline silicon gives three peaks. This is because of the electronic transition from the valence bands to the 2p vacancy of the atom.<sup>32</sup>

The lithium and silicon peak shapes are different due to the different bonding environments in the phases. From Fig. 9, the lithium peak in  $\text{Li}_{13}\text{Si}_4$  and  $\text{Li}_7\text{Si}_3$  occurs at lower energies than pure lithium because Si clusters are embedded in Li arrays.

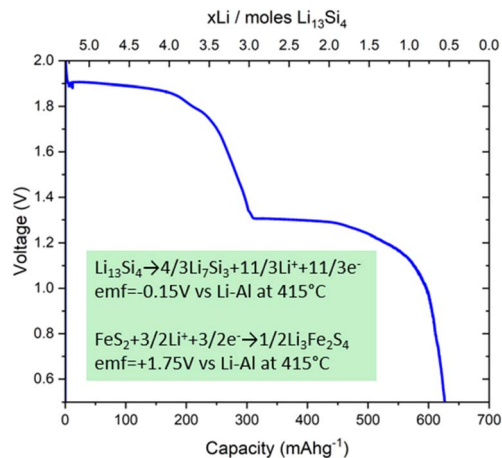


Fig. 8 Battery discharge profile for a  $\text{FeS}_2/\text{LiCl-KCl}/\text{Li}_{13}\text{Si}_4$  cell discharged galvanostatically at 500 °C using a current of 10 mA. The voltage changes are associated with phase transitions in  $\text{FeS}_2$ .

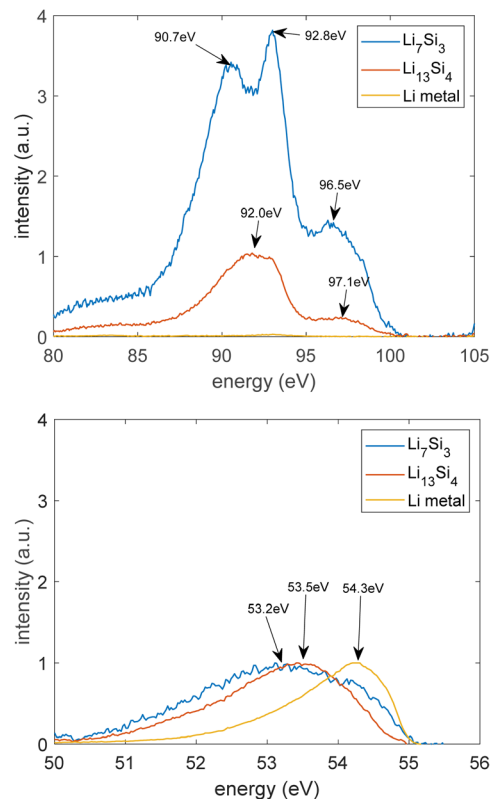


Fig. 9 Lithium K-emission and silicon L-emission spectra obtained from lithium–silicon phases.

$\text{Li}_7\text{Si}_3$  gives three silicon peaks, like crystalline Si, whereas  $\text{Li}_{13}\text{Si}_4$  gives two silicon peaks because  $\text{Li}_7\text{Si}_3$  is a more silicon rich phase and contains more Si dimers.

Lin *et al.* reported that the Li peak shifted to a lower energy from 53.6 to 53.3 eV after lithiation of a single crystal silicon.<sup>33</sup> They also reported that after lithiation of silicon, two Si peaks disappear and one Si peak shifts to a higher energy from 91.5 to



91.7 eV.<sup>33</sup> These changes indicate a transition from amorphous  $\text{Li}_{13}\text{Si}_4$  to crystalline  $\text{Li}_{15}\text{Si}_4$ .<sup>33</sup> The energies shown in Fig. 9 are within the range of energies reported by Lin *et al.*<sup>33</sup> These results suggest the similarity of  $\text{Li}_{13}\text{Si}_4$  and  $\text{Li}_7\text{Si}_3$  to crystalline  $\text{Li}_{15}\text{Si}_4$  which forms during lithiation of the silicon electrode at room temperature.

### Unit cell size on heating

The neutron diffraction patterns of  $\text{Li}_{13}\text{Si}_4$  and  $\text{Li}_7\text{Si}_3$  are shown in Fig. 10. Fig. 10 shows neither phase becomes amorphous as the temperature increases to 500 °C. The phases are stable at high temperature compared to the lithium electrode which melts at 180.5 °C and the lithiated silicon electrode that becomes electrochemically amorphous at room temperature.<sup>4</sup> Lithium and silicon bond well with each other because the phases do not lose crystallinity at high temperature. The complex structured background in the diffraction patterns arises from scattering by the amorphous silica glass tube of the rig. The background was modelled by Chebyshev polynomials with ten coefficients. The structure models of  $\text{Li}_{13}\text{Si}_4$  and  $\text{Li}_7\text{Si}_3$  were refined to obtain the best fit to the data collected in the low angle detector bank (number 3) over the TOF region of 2500 to 15000 ms (0.75 to 4.45 Å). The isotropic atomic displacement parameters ( $U_{\text{iso}}$ ), unit cell parameters, background parameters, instrument parameters and sample parameters were refined. From Rietveld refinement of the structure models, the unit cell parameters were obtained for  $\text{Li}_{13}\text{Si}_4$  and  $\text{Li}_7\text{Si}_3$ .

As a starting point for Rietveld refinement, atomic coordinates and unit cell parameters were taken from Zeilinger *et al.*<sup>19</sup> for  $\text{Li}_{13}\text{Si}_4$  and von Schnering *et al.*<sup>21</sup> for  $\text{Li}_7\text{Si}_3$ . The initial structure refinements were carried out using multiple data sets collected at 500 °C summed into single diffraction patterns to improve counting statistics on the data points and give a more stable refinement. After convergence, the resulting structures were used as starting models for sequential refinements of the structures at lower temperatures (450 °C to room temperature), which were single run data sets. Sequential refinement involves refining the background, hydrostatic strain parameters and isotropic atomic displacement parameters. Fig. 11 and 12 show

the unit cell parameters as a function of temperature for  $\text{Li}_{13}\text{Si}_4$  and  $\text{Li}_7\text{Si}_3$ , respectively.

The neutron data indicates that there are no phase changes between room temperature and 500 °C. Both phases did not become amorphous at 500 °C. The unit cells for both phases expand as the temperature increases.

The lattice parameters for  $\text{Li}_{13}\text{Si}_4$  in the literature by Zeilinger *et al.*<sup>19</sup> are smaller ( $a = 7.9488$  Å,  $b = 15.1248$  Å,  $c = 4.4661$  Å and  $V = 536.93$  Å<sup>3</sup>) than that observed in this work once the extrapolated lattice parameters were calculated at 100 K/−173.15 °C ( $a = 7.9922$  Å,  $b = 15.2433$  Å,  $c = 4.4763$  Å and  $V = 545.09$  Å<sup>3</sup>). The structural model of  $\text{Li}_{13}\text{Si}_4$  reported by Zeilinger *et al.* was from a single crystal X-ray diffraction study at 100 K/−173.15 °C.<sup>19</sup> On the other hand, the lattice parameters for  $\text{Li}_7\text{Si}_3$  by von Schnering *et al.*<sup>21</sup> are larger ( $a = 4.435$  Å,  $c = 18.134$  Å and  $V = 308.9$  Å<sup>3</sup>) than that observed in this work, although the lattice parameter  $a$  at room temperature matches very well with that measured by von Schnering *et al.* Once again, the structural model of  $\text{Li}_7\text{Si}_3$  was from an X-ray diffraction study at room temperature which explains the differences observed after Rietveld refinement. The differences in unit cell parameters between this work and that of literature is likely because of instrumental differences or disordering caused by the unit cells expanding.

The expansion of the unit cells is significant.  $\text{Li}_{13}\text{Si}_4$  has 1.8% expansion in  $a$ , 0.95% expansion in  $b$ , and 1.9% expansion in  $c$ . The unit cell volume expands by 4.7%.  $\text{Li}_7\text{Si}_3$  has 1.8% expansion in  $a$ , and 1.4% expansion in  $c$ . The unit cell volume for  $\text{Li}_7\text{Si}_3$  expands by 5.1%.

### Thermal expansion

The variation with temperature of the lattice parameters is linear for  $\text{Li}_{13}\text{Si}_4$  and  $\text{Li}_7\text{Si}_3$ . Therefore, constant values of the thermal expansion coefficients of  $a$ ,  $b$  and  $c$  were determined. Linear thermal expansion coefficient is calculated using<sup>34</sup>  $\alpha = (1/L_0) \times (dL/dT)$ .  $L_0$  is the initial value of  $a$ ,  $b$ , or  $c$  in Å and  $dL = dT$  is the rate of change in  $a$ ,  $b$ , or  $c$  with respect to the change in temperature (the gradient of the straight line). The unit of

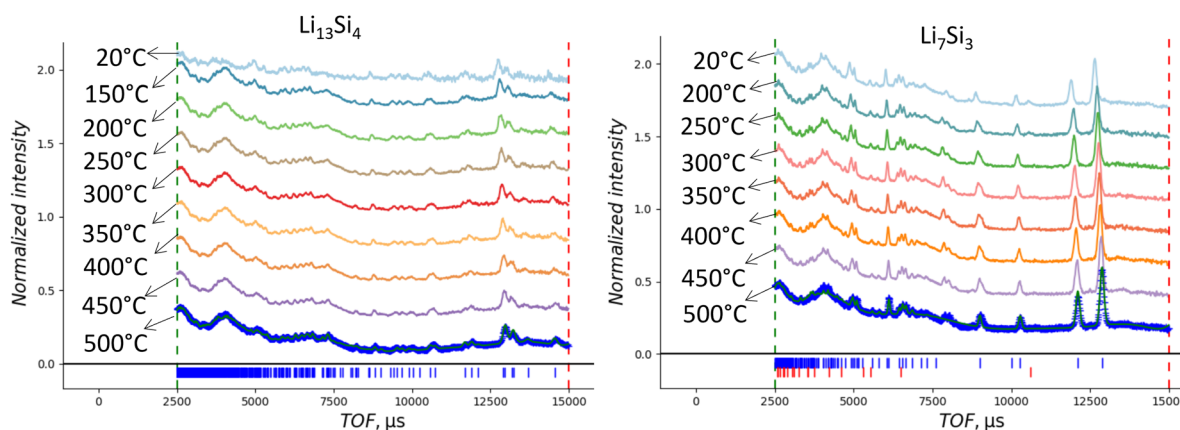


Fig. 10 Neutron diffraction data recorded between room temperature and 500 °C. The x-axis shows time-of-flight (TOF).



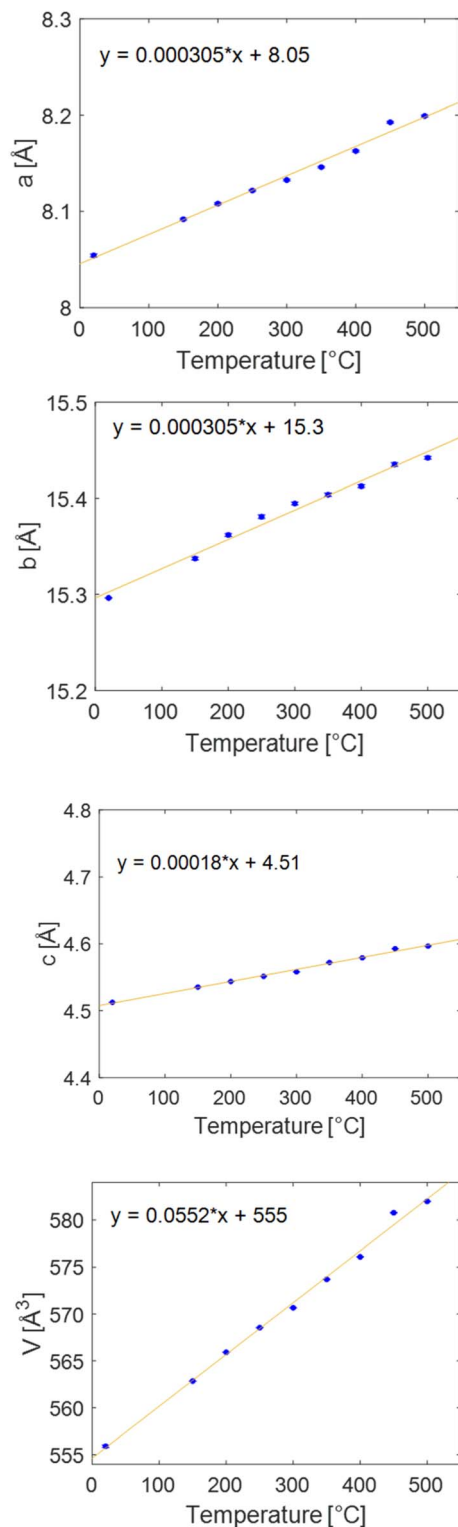


Fig. 11 Unit cell parameters  $a$ ,  $b$ ,  $c$  and cell volume,  $V$ , derived from the neutron diffraction data as  $\text{Li}_{13}\text{Si}_4$  was heated from room temperature to 500 °C. The error bars are shown on the measured (blue) points.

thermal expansion coefficient is  $^{\circ}\text{C}^{-1}$  or  $\text{K}^{-1}$ . Table 5 presents the thermal expansion coefficients of  $\text{Li}_{13}\text{Si}_4$  and  $\text{Li}_7\text{Si}_3$ .

The linear thermal expansion coefficient of silicon at room temperature is reported to be approximately  $2.6 \times 10^{-6} \text{ }^{\circ}\text{C}^{-1}$ .<sup>35</sup> At

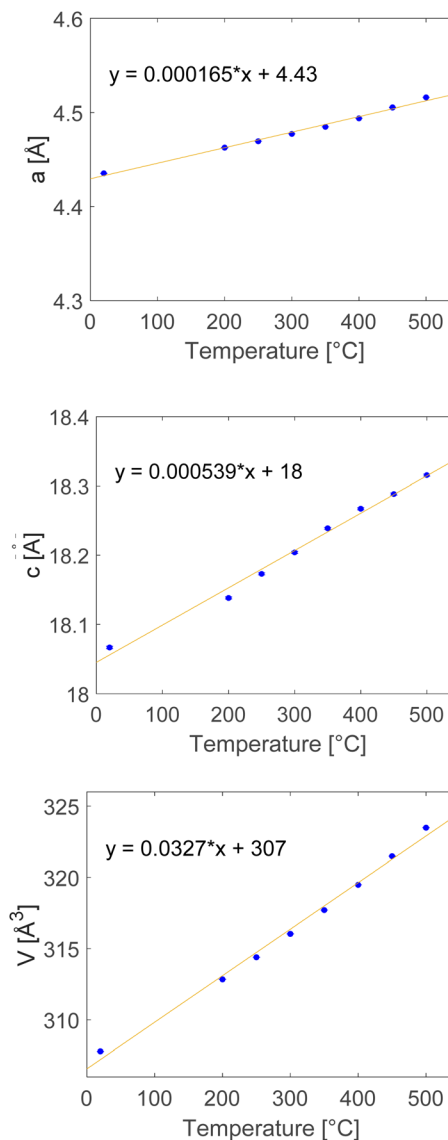


Fig. 12 Unit cell parameter  $a$ ,  $b$ ,  $c$  and cell volume,  $V$ , derived from the neutron diffraction data as  $\text{Li}_7\text{Si}_3$  was heated from room temperature to 500 °C. The error bars are shown on the measured (blue) points.

500 °C, it is reported to be approximately  $4 \times 10^{-6} \text{ }^{\circ}\text{C}^{-1}$ .<sup>35</sup> The thermal expansion of  $\text{Li}_{13}\text{Si}_4$  and  $\text{Li}_7\text{Si}_3$  is significantly larger than that of silicon. The volumetric thermal expansion coefficient of silicon at 500 °C, assuming isotropic expansion,<sup>36</sup> is  $\alpha_V = 3(4 \times 10^{-6} \text{ }^{\circ}\text{C}^{-1}) = 12 \times 10^{-6} \text{ }^{\circ}\text{C}^{-1}$ . The volumetric expansion of  $\text{Li}_{13}\text{Si}_4$  is  $\alpha_V = (1/V_0) (\Delta V/\Delta T) = 0.0552/555.912 = 99.3 \times 10^{-6} \text{ }^{\circ}\text{C}^{-1}$ . The volumetric expansion of  $\text{Li}_7\text{Si}_3$  is  $\alpha_V = 0.0327/307.786 = 106 \times 10^{-6} \text{ }^{\circ}\text{C}^{-1}$ . The volumetric expansion of both phases is

Table 5 Linear thermal expansion coefficients of  $\text{Li}_{13}\text{Si}_4$  and  $\text{Li}_7\text{Si}_3$  unit cell parameters

Phase	$\alpha_a 10^{-6} (\text{K}^{-1})$	$\alpha_b 10^{-6} (\text{K}^{-1})$	$\alpha_c 10^{-6} (\text{K}^{-1})$
$\text{Li}_{13}\text{Si}_4$	37.9	19.9	39.9
$\text{Li}_7\text{Si}_3$	37.2	37.2	29.8



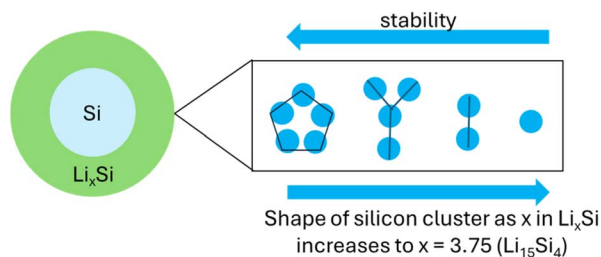


Fig. 13 The lithiation of silicon, adapted from the work of Limthongkul *et al.*<sup>4</sup> Planar Si<sub>5</sub>, Si<sub>4</sub> stars and Si<sub>2</sub> dimers stabilise the structure more than isolated Si atoms found in Li<sub>15</sub>Si<sub>4</sub>.

significant compared to that of silicon. The volumetric thermal expansion coefficient of lithium is approximately  $47 \times 10^{-6} \text{ }^\circ\text{C}^{-1}$  at room temperature.<sup>37</sup> This means Li<sub>13</sub>Si<sub>4</sub> and Li<sub>7</sub>Si<sub>3</sub> are mechanically closer to lithium metal than silicon. Lithium metal is highly ductile, and ductility can mitigate fracturing. Basu *et al.* reported the stress–strain curves of an amorphous silicon electrode at room temperature using Grand Canonical Monte Carlo and molecular dynamic simulations.<sup>38</sup> The authors reported that Li<sub>x</sub>Si with  $x = 2.5$  to  $3.5$ , which are similar compositions to Li<sub>7</sub>Si<sub>3</sub> and Li<sub>13</sub>Si<sub>4</sub>, is ductile during lithiation.<sup>38</sup>

Li<sub>13</sub>Si<sub>4</sub> and Li<sub>7</sub>Si<sub>3</sub> can be considered as Li arrays with Si clusters embedded (Si<sub>5</sub> rings, Si<sub>4</sub> stars and Si<sub>2</sub> dimers). Li<sub>13</sub>Si<sub>4</sub> and Li<sub>7</sub>Si<sub>3</sub> are both Zintl-like phases with Si<sub>*n*</sub><sup>*m*-</sup> polyanions called Zintl ions. Zintl phases have delocalised bonding in clusters.<sup>39</sup> All Zintl phases show remarkable stability because of closed shells.<sup>39</sup> There is covalent interactions in the anionic part (Si clusters) of the compound and ionic interaction between the cation and anion species (Si clusters and Li array).<sup>39</sup> Planar Si<sub>5</sub> rings, Si<sub>4</sub> stars and Si<sub>2</sub> dimers stabilise the structure more than isolated Si atoms found in Li<sub>15</sub>Si<sub>4</sub>. This is summarised in Fig. 13.

The findings of this work are also connected to the discharge mechanisms in thermal batteries. It is recommended to carry out simultaneous electrochemical and neutron diffraction measurements of thermal battery cells with Li<sub>13</sub>Si<sub>4</sub> and Li<sub>7</sub>Si<sub>3</sub> as the anode active materials. The Polaris diffractometer together with the St Andrews conductivity rig can provide simultaneous data collection from neutron diffraction and electrochemical potentiostatic discharge at 500 °C. This may lead to new discharge mechanisms at the anode side which will advance the understanding of processes occurring inside a thermal battery. Previous work by the St Andrews research group studied NiS<sub>2</sub> and CoS<sub>2</sub> cathodes and new discharge mechanisms were proposed.<sup>40,41</sup>

## Conclusions

Li<sub>13</sub>Si<sub>4</sub> and Li<sub>7</sub>Si<sub>3</sub> can be made from solid state synthesis. The galvanostatic cell discharge showed a flat voltage plateau indicating that Li<sub>13</sub>Si<sub>4</sub> and Li<sub>7</sub>Si<sub>3</sub> are in equilibrium and both phases are line phases. The powder neutron diffraction study of Li<sub>13</sub>Si<sub>4</sub> and Li<sub>7</sub>Si<sub>3</sub> was performed for the first time. Li<sub>13</sub>Si<sub>4</sub> and Li<sub>7</sub>Si<sub>3</sub> neutron diffraction data confirmed that within the temperature

range of 20 °C and 500 °C, there were no phase changes and no amorphous phase formed. The volumetric thermal expansion of Li<sub>13</sub>Si<sub>4</sub> and Li<sub>7</sub>Si<sub>3</sub> is significant and closer to lithium metal than to silicon which suggests the Li<sub>x</sub>Si electrode is mechanically closer to lithium metal and can be considered as having silicon clusters within a lithium array rather than the silicon lattice hosting lithium.

## Data availability

Data for this article, including X-ray diffraction, cell discharge, and scanning electron microscopy are available at the University of St Andrews repository at <https://doi.org/10.17630/e44eae73-ca6e-4562-a9f6-0e06865174c1>. Data files collected at the ISIS Neutron and Muon Source may be obtained from <https://doi.org/10.5286/ISIS.E.RB1910457-1>.

## Author contributions

Atia Azad: conceptualisation, data curation, formal analysis, investigation, methodology, validation, visualisation, writing – original draft. Katherine Bateman: investigation, data curation, formal analysis, validation, visualisation. Matthew Irvine: investigation, methodology. Aaron B. Naden: resources, visualisation. Stewart A. M. Dickson: conceptualisation, investigation, methodology. Ronald I. Smith: data curation, resources, writing – review & editing. Richard K. B. Gover: conceptualisation, funding acquisition, supervision. John T. S. Irvine: conceptualisation, funding acquisition, supervision, writing – review & editing.

## Conflicts of interest

There are no conflicts to declare.

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