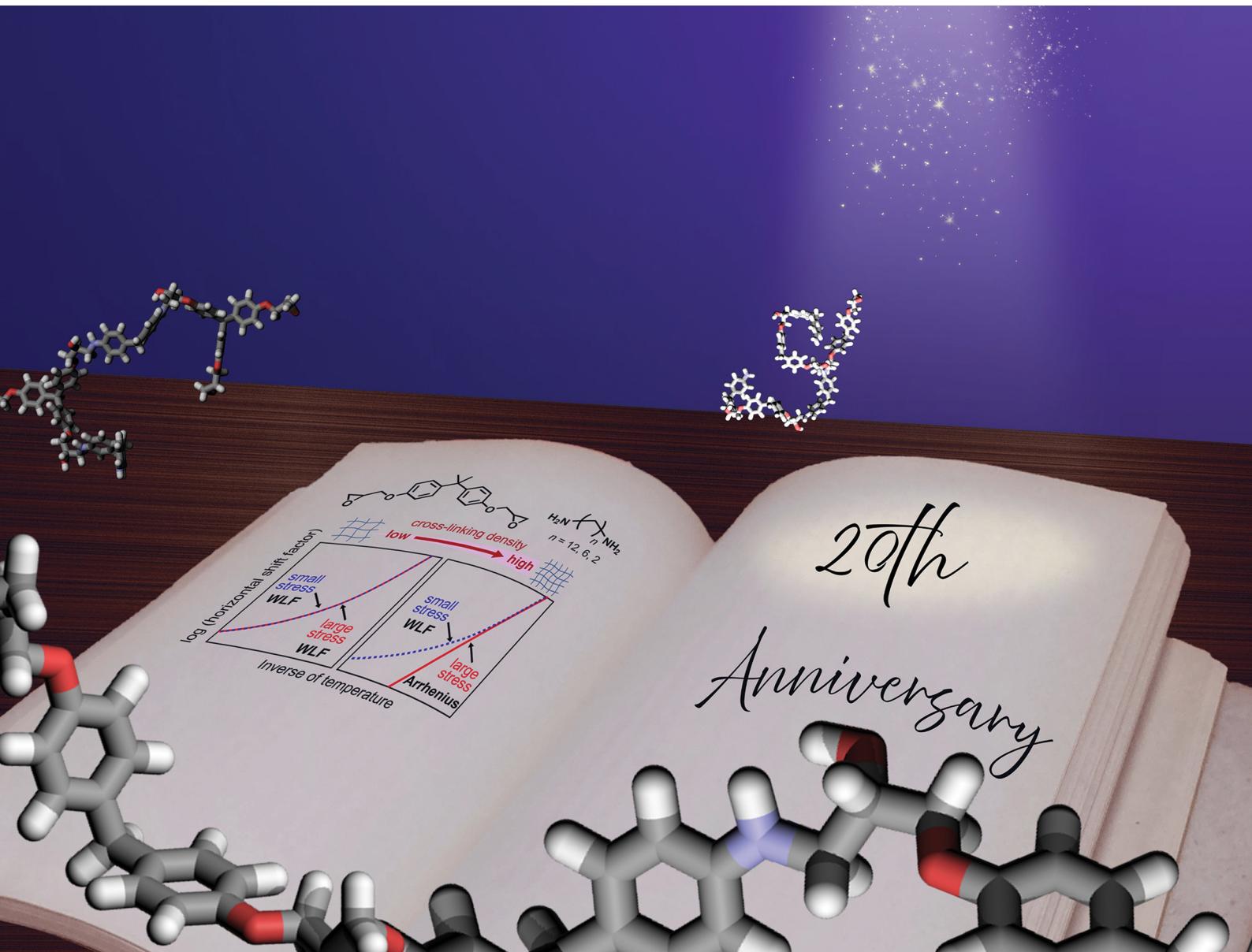


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## Impact of cross-linking on the time–temperature superposition of creep rupture in epoxy resins†

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Epoxy resins are an important class of thermosetting resins, and their network structure, formed by the curing reaction of epoxy and amine compounds, plays a crucial role in determining material properties, including creep behavior. We here applied the time–temperature superposition (TTS) principle to analyze the creep behavior of epoxy resins with well-defined network structures that were systematically varied based on the length of the *n*-alkyl diamine used. The superposition of isothermal creep curves under small stress was achieved through horizontal and vertical shifting, regardless of the length of the *n*-alkyl diamine. The temperature dependence of the horizontal shift factor was well described by the Williams–Landel–Ferry equation. Creep rupture measurements under large stress conditions revealed specimen rupture, and the time to rupture was plotted against the imposed stress. These plots, acquired at various temperatures, could be superimposed through horizontal shifting. As the diamine length decreased—namely, the distance between cross-linking points—the temperature dependence of the horizontal shift factors deviated from the WLF equation and exhibited Arrhenius-type behavior. The deviation was associated with differences in the fracture process involving chain scission, which became more pronounced as the diamine length decreased. The insights gained in this study should be valuable for controlling creep response and predicting the long-term durability of epoxy resins.

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## 1. Introduction

Epoxy resins, obtained by the curing reaction of epoxies with amine compounds, are an important class of thermosetting polymers used in a wide range of applications, including adhesives,<sup>1–10</sup> coatings,<sup>11–15</sup> and composite materials.<sup>16–24</sup> They possess an internal three-dimensional network, where the segmental mobility is frozen in a glassy state at room temperature.<sup>25–30</sup> When polymeric materials in a glassy state are subjected to stress, such as tensile stress, they slowly elongate. This phenomenon, known as creep behavior, has been systematically studied in thermoplastic polymers.<sup>31–35</sup> In thermosetting resins, including epoxy resins, creep behavior is equally critical for applications requiring long-term shape stability.<sup>36–40</sup> Consequently, the relationship between the network structure, particularly cross-linking

density, and creep behavior in epoxy resins has been extensively investigated.<sup>41–50</sup>

From a practical application perspective, it is crucial to understand not only creep behavior but also material durability.<sup>51–53</sup> To address durability, establishing a method of predicting long-term behavior from short-term tests is highly desirable. The time–temperature superposition (TTS) principle is one of the most promising methods for this purpose.<sup>54–58</sup> A series of isothermal curves for creep compliance,  $J(t)$ , defined as the strain divided by the stress applied to a sample, can be obtained as a function of time. These curves can be superimposed onto one another through horizontal and/or vertical shifts. This operation generates a master curve that represents creep behavior over a wide time range, which cannot be achieved with individual isothermal measurements.<sup>31,59</sup> Consequently, the TTS principle has been widely used to predict the long-term response of material properties.<sup>60–64</sup> For instance, short-term (10 h) creep measurements at various temperatures make it possible to access a time scale of up to  $10^6$  h (more than 50 years).<sup>61</sup>

We recently studied the TTS principle based on the dynamic viscoelastic functions of epoxy resins, in which the network was well defined and systematically varied in terms of cross-linking density.<sup>65</sup> For these epoxy resins, an increase in cross-linking density led to a higher glass transition temperature ( $T_g$ ) with an associated reduction in the spatial size scale of the cooperative

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rearranging region (CRR).<sup>66</sup> The superimposition of isothermal curves in the frequency domain required not only horizontal, but also vertical shifts, regardless of the cross-linking density. The temperature dependence of the horizontal shift factor was well described by the Williams-Landel-Ferry (WLF) equation. Fitting analyses of the parameters  $C_1$  and  $C_2$ , combined with full-atomistic molecular dynamics (MD) simulations, revealed that an increase in cross-linking density resulted in a lower thermal expansion coefficient of free volume, accompanied by the suppression of entropic elasticity at high temperatures.<sup>65</sup> However, it is noteworthy that the shape of the master curve was slightly distorted for resins with higher cross-linking densities. This distortion is likely due to the increasing importance of cross-linking points, which cannot be ignored as the spatial length scale of the dynamics grows, even though the TTS principle assumes that the mode of dynamics remains unchanged with temperature variations.<sup>65,66</sup> These findings motivated us to apply the TTS principle to creep behaviors, which involve chain motions over longer timescales and larger spatial scales.

In this study, we examined how cross-linking density, which is related to all of the aforementioned factors, affects the horizontal and vertical shifts of the isothermal creep curves. Three different epoxy resins with varying cross-linking densities based on the length of *n*-alkyl diamine were studied. Creep tests were conducted under two distinct stress levels: small stress within the linear response regime and larger stress beyond it.

## 2. Experimental

### 2.1. Materials and preparation of epoxy resins

Panel (a) of Fig. 1 shows the chemical structures of diglycidyl ether of bisphenol A (DGEBA) with a purity greater than 99% and *n*-alkyl diamines with methylene group numbers (*n*) of 12, 6 and 2, each with a purity exceeding 99%. These compounds were purchased from New Japan Chemical Co., Ltd, Osaka, Japan, and Tokyo Chemical Industry Co., Ltd, Tokyo, Japan. DGEBA and *n*-alkyl diamines were mixed thoroughly at a molar ratio of 2:1, corresponding to the stoichiometric ratio of epoxy to amino groups. The mixture, heated to 353 K, was placed onto an aluminum substrate using a silicon rubber mold and pre-cured for 12 h. Subsequently, all samples underwent post-curing at 453 K for an additional 12 h, ensuring the apparent completion of the reactions, as confirmed by Fourier transform infrared (FT-IR) spectroscopy (FT/IR 6700 spectrometer, JASCO Co., Tokyo, Japan).<sup>67–69</sup> The resulting epoxy resins are hereafter

referred to as ER12, ER6 and ER2, where the number corresponds to the methylene group number of the *n*-alkyl diamines.

### 2.2. Characterizations

The mass density ( $\rho$ ) of the cured epoxy resins was examined using a gas pycnometer (ULTRAPYC 1200e, Anton Paar QuantaTec Inc., Florida, USA) with helium as the probing gas. The helium pressure was set at 117 kPa, and measurements were taken 100 times to obtain an average value. Dynamic mechanical analysis (DMA) was conducted using a Rheovibron DDV-01FP (A&D Co., Ltd, Tokyo, Japan) on samples with a thickness of 300  $\mu$ m, width of 3 mm, and length of 30 mm. A sinusoidal strain of 0.3%, within the linear response regime, was applied. Measurements were taken under a dry nitrogen purge with a heating rate of 2 K min<sup>-1</sup> at a frequency of 1 Hz. The average cross-linking density ( $\nu$ ) of the network was estimated based on the storage modulus ( $E'$ ) in the rubbery plateau region.<sup>66</sup>

Before conducting creep and rupture tests, the mechanical properties of the epoxy resins were characterized through tensile testing using a TENSILON RTF-1310 (A&D Co., Ltd, Tokyo, Japan). The specimens were prepared according to Japanese Industrial Standards (JIS) K6251-7, with a gauge length of 12 mm and a width of 2 mm. Tensile tests were conducted at various temperatures ranging from 358 to 438 K, controlled by a thermostatic chamber (TKC-R3-C, A&D Co., Ltd, Tokyo, Japan). The crosshead speed was set at 1 mm min<sup>-1</sup>.

Creep and rupture tests were performed using the same instrument as the tensile testing setup. For the creep tests, a stress ( $\sigma$ ) in the range of 0.7–1.3 MPa, within the linear response regime, was applied to the specimen at a specified temperature ( $T$ ).  $J(t)$ , defined as the strain divided by  $\sigma$ , was recorded as a function of time ( $t$ ). Measurements were taken at different  $T$ s within the range of 358–473 K, at 5 K intervals. For the creep rupture tests, higher  $\sigma$ s in the range of 2–25 MPa were applied to the specimens at given  $T$ s, and the time to macroscopic rupture ( $t_{rp}$ ) was recorded. These measurements were taken at various  $T$  values within the range of 358–473 K, also at 5 K intervals, to establish the relationship between  $t_{rp}$  and  $\sigma$ .

After the creep rupture tests, changes in the  $\nu$  of the specimens were assessed using a swelling test. Specimens were weighed ( $W_0$ ) and immersed in THF at 313 K for 12 days. The equilibrium weight ( $W_{eq}$ ) was recorded after collecting the fractured pieces and gently blotting THF from the sample surface. The swelling ratio was calculated as  $(W_{eq} - W_0)/W_0$ .

## 3. Results and discussion

### 3.1. Creep behavior under small strain

Table 1 summarizes the characterization data for  $\nu$ ,  $\rho$  and  $T_g$  for ER12, 6 and 2, as reported in our previous study.<sup>65</sup> The  $\nu$  value was estimated based on the rubbery plateau modulus using the equation of  $\nu = E'/3RT$ , where  $R$  is the gas constant.<sup>65,66,70,71</sup> The  $T_g$  value was dynamically defined at an  $\alpha$ -relaxation time ( $\tau$ ) of 100 s, determined through the DMA measurements.<sup>65,66</sup> The  $\nu$ ,  $\rho$  and  $T_g$  values were higher in the order of ER2, 6 and 12.

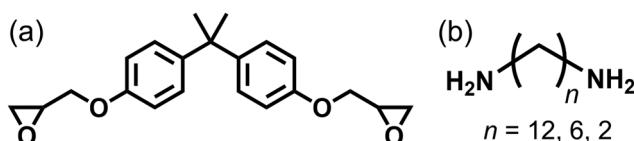


Fig. 1 Chemical structures of (a) DGEBA and (b) *n*-alkyl diamines with varying numbers of methylene groups (*n*), where *n* = 12, 6, and 2.



**Table 1**  $\nu$ ,  $\rho$  and  $T_g$  values for ER12, ER6 and ER2. (The data are reproduced from ref. 65 with permission. Copyright 2021 American Chemical Society)

	$\nu \cdot 10^{-3}/\text{mol m}^{-3}$	$\rho/\text{g cm}^{-3}$	$T_g/\text{K}$
ER12	$1.70 \pm 0.04$	$1.120 \pm 0.008$	357
ER6	$2.14 \pm 0.05$	$1.159 \pm 0.004$	379
ER2	$2.39 \pm 0.04$	$1.180 \pm 0.013$	395

This indicates that the cross-linking density of the products increased as the length of *n*-alkyl diamine decreased, resulting in a glassy state with higher mass density, which effectively suppressed the segmental motion in between the cross-linking points.<sup>72</sup> Notably, the  $T_g$  values for ER12, ER6, and ER2 remained unchanged even after a heating and cooling cycle in the range of 293–453 K, suggesting thermal stability during the subsequent creep (rupture) tests.

The creep test was conducted on the three epoxy resins by applying  $\sigma$ , which was within the linear response regime, as confirmed by the tensile test (see Fig. S1 in the ESI†). This resulted in the time dependence of  $J(t)$  being examined at various  $T$ s ranging from  $T_g$  to  $T_g + 35$  K (see Fig. S2 in the ESI†). When the TTS principle is applied to the creep tests, the horizontal and vertical shift factors ( $a_T$  and  $b_T$ ) are expressed as follows:<sup>31,54</sup>

$$J(t, T_r) = \frac{J(t \cdot a_T^{-1}, T)}{b_T} \quad (1)$$

where  $t$  and  $T$  represent time and temperature, respectively, and  $T_r$  is the reference temperature ( $T_g$ ). Typically, the master curve for  $J(t)$  is constructed by horizontally shifting the time-domain data at a given  $T$  to align with  $T_r$  using  $a_T$ .<sup>31,54</sup> In some cases, a vertical shift, dividing the data by  $b_T$ , is also required.<sup>31,42,43,54,73</sup> The  $b_T$  value is often correlated with temperature and mass density.<sup>31,54</sup> While  $b_T$  is generally assumed to be unity, this is not always the case.<sup>42,43,73</sup> In a previous study on the same epoxy resin, we applied TTS to their dynamic viscoelastic functions ( $E'$  and  $E''$ ) obtained via DMA.<sup>65</sup> It was observed that the  $b_T$  value increased with temperature, and the increase was smaller for shorter diamine lengths.<sup>65</sup> This trend was attributed to entropic elasticity, which became less pronounced as the diamine length decreased.<sup>65</sup> Based on these findings, the  $b_T$  values derived from the master curve constructions of the frequency-domain data of  $E'$  and  $E''$ , as reported in ref. 65, were incorporated into this study and used here to construct the master curves for  $J(t)$ . The time-domain data of  $J(t)$  were first vertically shifted using  $b_T$ , followed by horizontal shifting with  $a_T$ , to achieve optimal superimposition.

Fig. 2 shows the master curves for ER12, ER6 and ER2, with  $T_r$  set to their respective  $T_g$  values listed in Table 1. For all epoxy resins, the value of  $J(t)$  scaled with  $b_T^{-1}$  ( $J(t) \cdot b_T^{-1}$ ) increased with increasing scaled time ( $t \cdot a_T^{-1}$ ) before reaching a plateau. However, notable differences were observed in the master curves among the three samples. The speed of increase in  $J(t) \cdot b_T^{-1}$  was slower in the order of ER2, ER6 and ER12. Consequently, the  $t \cdot a_T^{-1}$  value at which  $J(t) \cdot b_T^{-1}$  reached the plateau was longer in the same order, indicating that deformation occurs more slowly as the diamine length decreases. Also, the

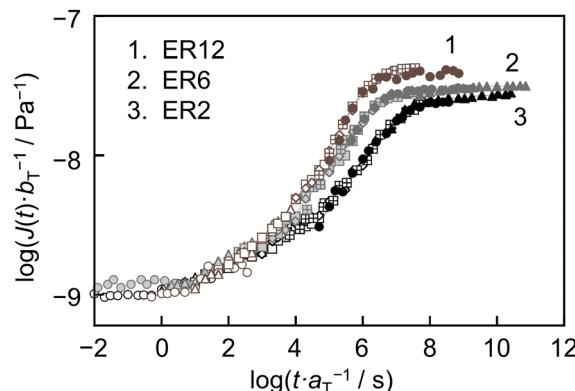


Fig. 2 Master curves of  $J(t)$  for ER12, ER6 and ER2, constructed through vertical and subsequent horizontal shifting. The reference temperature was set to  $T_g$ .

plateau  $J(t) \cdot b_T^{-1}$  values were lower in the order of ER2, ER6 and ER12. This indicates that the magnitude of the deformation over long timescales decreases as the diamine length decreases. Assuming that cross-linking points in the network suppress deformation,<sup>45,48</sup> the observed differences in the master curves based on diamine length can be reasonably explained.

Fig. 3 shows the  $a_T$  data as a function of inverse temperature for ER12, 6 and 2. Closed symbols represent the  $a_T$  data obtained from the superposition of  $J(t)$  curves in the creep test. The temperature dependence of  $a_T$  can be well described by the Williams–Landel–Ferry (WLF) equation;<sup>31,54,74–76</sup>

$$\log a_T = \frac{-C_1(T - T_r)}{C_2 + T - T_r} \quad (2)$$

where  $C_1$  and  $C_2$  are empirical constants adjusted to fit the  $a_T$  values. This relationship was indeed confirmed for the  $a_T$  values obtained through the master curve construction of  $E'$  and  $E''$  using DMA (open symbols), as reported in our

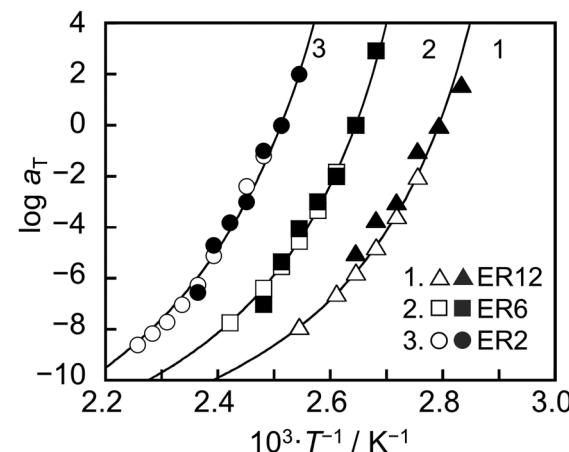


Fig. 3 Temperature dependence of  $a_T$  for ER12, ER6 and ER2. Closed symbols represent experimental data obtained from the creep test, while open symbols correspond to data from DMA measurements. Solid curves indicate the best fit of the WLF equation to the DMA data. (The DMA data are reproduced from ref. 65 with permission. Copyright 2021 American Chemical Society).



previous study.<sup>65</sup> Solid curves indicate the best-fits of the WLF equation to the DMA data. The alignment between the  $\alpha_T$  values derived from the creep test and the corresponding fitted curves demonstrates the consistency between the two methods. These results emphasize that both the creep test and DMA provide reliable and consistent temperature dependencies of  $\alpha_T$ , which are well captured by the WLF equation.

### 3.2. Creep rupture behavior under large strain

For the creep rupture test,  $\sigma$  larger than the stress levels used previously was applied to the specimen at a constant  $T$ . Fig. 4 shows the time dependence of  $J(t)$  for a representative sample, ER12, under  $\sigma$  values of 14, 15 and 16 MPa at 368 K. Regardless of the applied  $\sigma$ , the  $J(t)$  value increased over time, eventually reaching a plateau. After a certain period, the specimens ruptured. The time required for rupture ( $t_{rp}$ ) decreased as  $\sigma$  increased. To construct master curves, the relationship between  $t_{rp}$  and  $\sigma$  was obtained at various  $T$  values ranging from  $T_g$  to  $T_g + 35$  K (see Fig. S3 in the ESI†). The  $t_{rp}-\sigma$  plots at different  $T$  were horizontally shifted to align with the data at  $T_g$ , using a horizontal shift factor ( $\alpha_{Trp}$ ). Assuming that vertical shifting in the creep rupture test is negligible,<sup>77–81</sup> the value of vertical shift factor was set to unity. Fig. 5 shows the master curves for ER12, ER6 and ER2. All samples exhibited the trend where  $t_{rp} \cdot \alpha_{Trp}^{-1}$  was inversely proportional to  $\sigma$ , indicating that the specimen ruptured more easily as the stress increased. Notably, the shapes of the master curves for ER12, ER6 and ER2 differed around  $\sigma = 10$  MPa. Specifically, the  $t_{rp} \cdot \alpha_{Trp}^{-1}$  values were shorter in the order of ER2, ER6 and ER12. This suggests that the temperature dependence of  $\alpha_{Trp}$  varies with the methylene group number of the diamine. It is also interesting to consider the differences in behavior before and after the threshold  $\sigma$  of 10 MPa. A possible explanation is a transition in the failure mode around this stress level, for  $\sigma > 10$  MPa, the fracture behavior resembles brittle fracture, whereas for  $\sigma < 10$  MPa, it appears more ductile-like. However, to draw a definitive conclusion, direct observations of the fracture surfaces would be necessary.

Panel (a) of Fig. 6 shows the temperature dependence of  $\alpha_{Trp}$  for ER12, ER6, and ER2. Closed symbols denote experimental

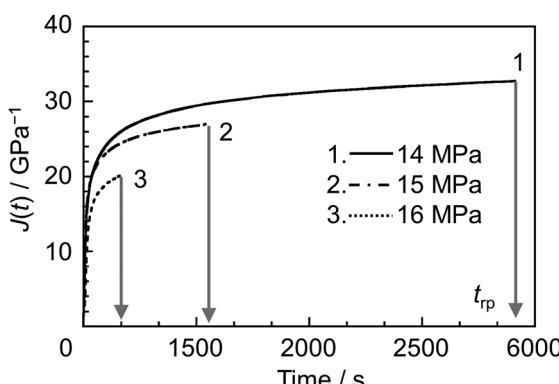


Fig. 4 Representative time dependence of  $J(t)$  for ER12 under  $\sigma$  values of 14, 15, and 16 MPa at 368 K.

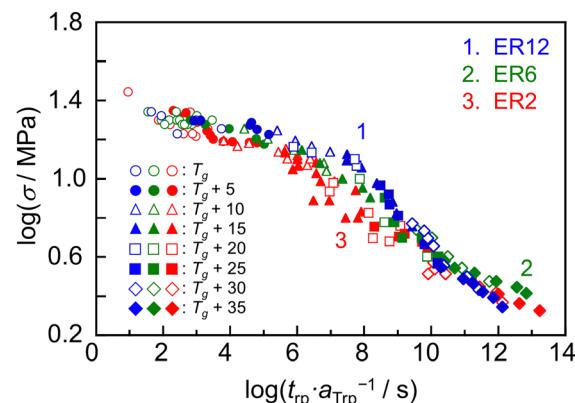


Fig. 5 Master curves of the  $t_{rp}-\sigma$  plots for ER12, ER6 and ER2 after horizontal shifting. Blue, green, and red-colored symbols denote the data for ER12, ER6, and ER2, respectively. The reference temperature was set to  $T_g$ .

data, while solid curves indicate the best-fit results using the WLF equation applied to the  $\alpha_T-T^{-1}$  relationship from the creep test under small strain (Fig. 3). For all samples, the  $\alpha_{Trp}$  values were close to their respective WLF curves in the low-temperature region. However, as the temperature increased, the  $\alpha_{Trp}$  values began to deviate from the WLF curves. This deviation can be quantified as the difference between  $\alpha_{Trp}$  and the WLF curve ( $\Delta\alpha_{Trp}$ ). Panel (b) of Fig. 6 shows the correlation between  $\Delta\alpha_{Trp}$  and  $T-T_r$  ( $\Delta T$ ) for ER12, ER6, and ER2. For ER12,  $\Delta\alpha_{Trp}$  values remained near zero at all  $\Delta T$ , indicating that the temperature dependence of  $\alpha_{Trp}$  was well described by the WLF equation. In contrast, for ER6 and ER2,  $\Delta\alpha_{Trp}$  increased with increasing  $\Delta T$ , reflecting greater deviations from the WLF curve in the high-temperature region. Here, it should be noted that the increase in  $\Delta\alpha_{Trp}$  was more pronounced in the order of ER2, ER6, and ER12. Thus, it is most likely that, as the diamine length decreases, the temperature dependence of  $\alpha_{Trp}$  transitions from WLF-type behavior to Arrhenius-type behavior, where the logarithm of  $\alpha_{Trp}$  scales linearly with the inverse temperature. The potential reasons for this transition will be discussed in the following section.

### 3.3. Cross-linking density effect on rupture behavior

To explore the reason for the differences in the temperature dependence of  $\alpha_{Trp}$  among the three resins, we examined rupture strain ( $\epsilon_{rp}$ ) as an alternative to  $t_{rp}$  in the creep rupture test. Fig. 7 shows double logarithmic plots of  $\sigma$  against  $\epsilon_{rp}$  for ER12, ER6, and ER2. For each sample, the rupture points obtained at the different temperatures were superimposed, resulting in a master curve. As temperature increased, the points moved clockwise around the curve and eventually passed through the maximum. This behavior is consistent with the failure envelope observed in tensile tests, where failure strain is plotted against failure stress while varying temperature and tensile rate.<sup>77,78,82–84</sup> It indicates that, for a given applied stress, rupture occurs when the strain exceeds a certain limit. Similarly, in experiments where strain is fixed, the material ruptures when subjected to stress beyond a specific threshold. A particular



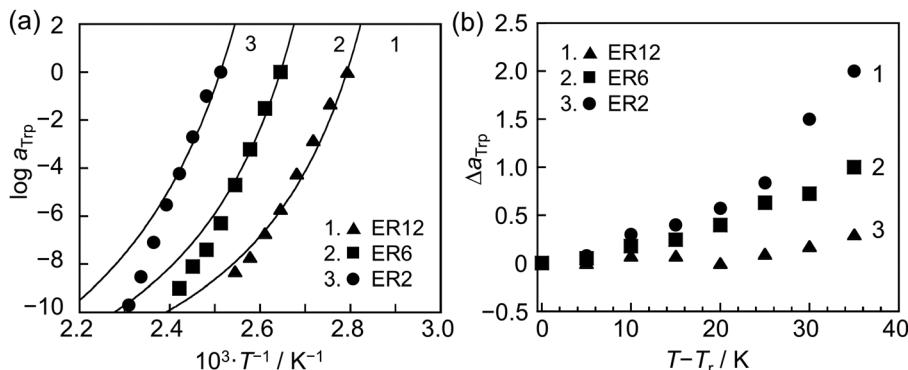


Fig. 6 (a) Temperature dependence of  $a_{T_{rp}}$  for ER2, ER6, and ER12. Closed symbols denote experimental data, and solid curves indicate the best-fit WLF equation applied to the  $a_T - T$  relationship from the creep test. (b) Correlation between  $\Delta a_{T_{rp}}$  and  $\Delta T$  ( $T - T_r$ ).

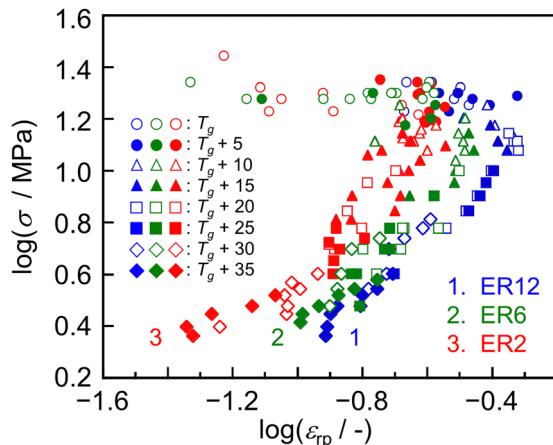


Fig. 7 Double logarithmic plots of  $\sigma$  against  $\epsilon_{rp}$  for ER12, ER6, and ER2. Blue, green, and red-colored symbols denote data for ER12, ER6, and ER2, respectively.

interesting aspect is that, when failure is analyzed at a fixed strain, two distinct stress limits emerge. These correspond to brittle and ductile failure modes, as mentioned earlier. The data associated with higher failure stress correspond to brittle fracture, whereas those at lower failure stress correspond to ductile fracture. At relatively low temperatures, brittle failure dominates, placing the

corresponding data points in the upper region of the plot. Notably, the shapes of the master curves differed markedly among the three resins, particularly at relatively low  $\sigma$ , corresponding to high  $T$ . In this region,  $\epsilon_{rp}$  was smaller in the order of ER2, ER6, and ER12. Thus, it is obvious that the macroscopic rupture occurred more easily as the diamine length decreased. This effect became more pronounced at higher  $T$ , suggesting that the fracture mechanism depends on the diamine length, and consequently, the cross-linking density.

In general, the rupture behavior of polymer materials, including epoxy resins, involves crazing and/or void formation, which lead to crack generation and propagation.<sup>85–88</sup> These processes are often accompanied by chain scissions.<sup>89–93</sup> If chain scission occurs in epoxy resins, the cross-linking density of the network structure should decrease. To verify this, we examined changes in cross-linking density during the creep rupture test using a swelling test.<sup>94–96</sup> Epoxy resin specimens were subjected to a  $\sigma$  of 2.5 MPa at  $T_g + 35$  K and left undisturbed until just before rupture. The stretched portion of each specimen was immersed in a good solvent, THF, for a specific period, and the swelling ratio ( $\phi$ ) was obtained based on weight changes. For comparison, neat specimens without creep treatment were also tested.

Fig. 8 shows  $\phi$  as a function of immersion time for ER12, ER6, and ER2, with and without creep treatment. For all samples,

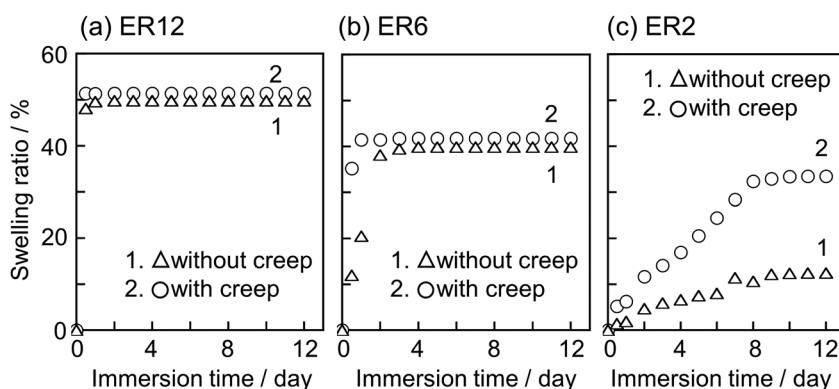


Fig. 8 Time dependence of the swelling ratio ( $\phi$ ) for (a) ER12, (b) ER6, and (c) ER2 at 313 K.

$\phi$  increased over time and reached equilibrium, regardless of the creep treatment. However, specimens subjected to creep exhibited steeper slopes and higher equilibrium  $\phi$  values, with the effect being most pronounced for ER2. The equilibrium  $\phi$  for ER2 increased markedly upon creep treatment. Given that equilibrium  $\phi$  is inversely proportional to cross-linking density,<sup>94–96</sup> it can be claimed that the cross-linking density of ER2 decreased due to chain scission during the creep test. As the cross-linking density increases, that is, as the distance between cross-linking points decreases, the proportion of chains in an extended state increases. This is equivalent to our previous finding that a shorter distance between cross-linking points results in a smaller entropic elasticity contribution to  $b_T$ . Consequently, these chains become more susceptible to scission.<sup>89,91</sup> This scenario explains why the temperature dependence of  $a_{Trp}$  transitions from the WLF-type to Arrhenius-type behavior as cross-linking density increases (Fig. 6). That is, a two-state approximation, representing the states before and after chain scission, likely underpins the observed Arrhenius-type behavior.

Finally, we discuss the applicability of the TTS principle, which assumes that a molecular motion mode remains unchanged with temperature, allowing for the horizontal (time-axis) shifting of viscoelastic data. However, as molecular motion becomes increasingly active at higher temperatures, localized network disruptions occur, leading to a breakdown in cooperative segmental motion. This shift alters the dominant relaxation mechanism, transitioning to one governed by activation energy, characteristic of Arrhenius-type behavior. Thus, when applying the TTS principle to cross-linked polymer networks, including thermosetting polymers, it is crucial to consider these fundamental limitations and recognize the potential transition in temperature dependence as the system undergoes structural changes at elevated temperatures.

## 4. Conclusions

We examined how cross-linking points affect the time-temperature scaling of creep (rupture) behavior in epoxy resins, obtained from the curing reaction of a DGEBA epoxy base with *n*-alkyl diamine hardeners containing varying numbers of methylene groups. In creep tests under relatively small  $\sigma$ s, time-domain curves of  $J(t)$  were successfully superimposed within the temperature region from  $T_g$  to at least  $T_g + 35$  K by horizontally and vertically shifting the curves. The resulting master curves indicated that, as the diamine length—namely, the distance between cross-linking points—decreased, deformation became slower and more suppressed. The temperature dependence of  $a_T$  was well described by the WLF equation, consistent with our previous results obtained by DMA. For creep rupture behavior under relatively large  $\sigma$ ,  $t_{rp}$ - $\sigma$  plots obtained at various temperatures could also be superimposed through horizontal shifting. However, as the diamine length decreased, the temperature dependence of  $a_{Trp}$  deviated from the WLF equation, resulting in Arrhenius-type behavior. This deviation was likely linked to differences in the fracture

process, depending on the diamine length, particularly at higher temperatures, as suggested by variations in the master curves of the  $\epsilon_{rp}$ - $\sigma$  plots. Solvent swelling tests further revealed that cross-linking density decreased due to chain scission, which became more marked as the diamine length decreased. These findings highlight the impact of cross-linking density on the fracture mechanism and provide valuable insights for the improved design and development of thermosetting polymer materials. In particular, the insights gained from this study is useful for predicting the long-term durability for structural adhesives and composites, which are subjected to a constant stress during their usage leading to the failure *via* the creep deformation.

## Author contributions

A. S. conducted the data analysis and drafted the original manuscript. M. A. performed the experiments and contributed to the data analysis. S. Y. provided insights into the deformation mechanism, and K. T. supervised the entire study, reviewed and edited the manuscript, and oversaw its finalization.

## Data availability

The data that support the findings of this study are available from the corresponding author upon request.

## Conflicts of interest

There are no conflicts to declare.

## Acknowledgements

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