Soft Matter

PAPER

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Cite this: *Soft Matter*, 2025, **21**, 2935

Received 9th December 2024, Accepted 15th March 2025

DOI: 10.1039/d4sm01463d

rsc.li/soft-matter-journal

1 Introduction

Bacteria spend most of their life attached to surfaces in structured colonies encased in a self-produced polymeric matrix, called biofilms, which are the prevalent form of life on earth.¹ The organisation in biofilms confers bacteria a selective advantage over the individual, e.g. by increasing resistance to mechanical damage and antibiotic agents. Biofilm formation requires bacteria to transition from a free-swimming, individual lifestyle, to a sessile cooperative one. Since the discovery of the multicellular tissue-like behaviour of bacteria about 100 years ago, research has focused on dissecting the environmental cues and biological pathways driving bacterial adhesion and biofilm formation: genetic changes, intracellular signalling, and cell-cell communication.² However, bacteria in their natural environments are continuously exposed to physical and physico-chemical forces, including mechanical stresses,³⁻⁸ osmotic pressure gradients,⁹⁻¹⁶ capillary¹⁷⁻¹⁹ and wetting forces^{20,21} and it remains often unclear how individuals or colonies integrate such physical cues. However, it is becoming increasingly known that many bacterial communities control and

The role of substrate mechanics in osmotic biofilm spreading[†]

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Bacteria invade surfaces by forming dense colonies encased in a polymer matrix. Successful settlement of founder bacteria, early microcolony development and later macroscopic spreading of these biofilms on surfaces rely on complex physical mechanisms. Recent data show that on soft hydrogels, substrate rigidity is an important determinant for biofilm initiation and spreading, through mostly unknown mechanisms. Using a thermodynamically consistent thin-film approach for suspensions on soft elastic surfaces supplemented with biomass production we investigate *in silico* the role of substrate softness in the osmotic spreading of biofilms. We show that on soft substrates with an imposed osmotic pressure spreading is considerably slowed down and may be completely halted depending on the biomass production rate. We find that the critical slowing down of biofilm spreading on soft surfaces is caused by a reduced osmotic influx of solvent into the biofilm at the edges, which results from the thermodynamic coupling between substrate deformation and interfacial forces. By linking substrate osmotic pressure and mechanical softness through scaling laws, our simple model semi-quantitatively captures a range of experimentally observed biofilm spreading dynamics on hydrogels with different architectures, underscoring the importance of inherent substrate properties in the spreading process.

use the mechanical and physico-chemical properties of their surrounding habitat to maximise their chances of survival and dissemination.²² It is now well understood that auto-produced matrix molecules act as osmolytes for biofilms grown on hydrogel substrates. The resulting flux of water with nutrients from the substrate into the biofilm can act as a driving force for lateral biofilm expansion. It has also been demonstrated that capillary, wetting and adhesion forces play a major role in the dynamics of the advancing edge of biofilms,^{20,23,24} and swarming colonies.^{17–19,25,26} Bacteria-produced surfactants allow the biofilm to overcome wetting-induced stalling of the biofilm edge^{20,27} and accelerate spreading in swarming colonies through Marangoni-flows, that may also trigger a fingering instability at the spreading front.^{19,27}

The influence of other material properties on biofilm spreading is less well explored. An example is the role of the mechanical substrate stiffness that represents an important parameter for the growth of biofilms on and in soft tissues. Over the past decade, only a few studies have specifically focused on the role of substrate rigidity on bacterial dynamics, both at the single cell and community level.^{5,7,28–40} Their results show that the rigidity of the underlying substrate does impact bacterial attachment and motility as well as colony morphology and dynamics. However, the observed trends are not consistent between different bacterial strains (*e.g. Pseudomonas aeruginosa, Escherichia coli*), different types of soft substrates (hydrogels, elastomers, layer-by-layer polymeric substrates) and different explored stiffness ranges (kPa–MPa). Thereby, one of the main experimental difficulties is the independent variation of physico-chemical properties (*e.g.* osmotic

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[†] Electronic supplementary information (ESI) available. See DOI: https://doi.org/ 10.1039/d4sm01463d

Paper

pressure) and mechanical rigidity of the substrate, which might explain opposing trends observed on different hydrogel architectures with identical mechanical properties (shear modulus). Within this context, the osmotic spreading of biofilms has been studied on various substrate architectures and chemical compositions.⁷ There it has been shown that at constant osmotic pressure, spreading is slower on soft than on rigid substrates, raising the question about the underlying coupling mechanism between the dynamics of the biofilm edge and the substrate rigidity.

Motivated by the aforementioned observations, here, we numerically study the effect of the rigidity of a soft elastic substrate on osmotic biofilm spreading. To that end we employ a minimal thinfilm model which naturally captures the effect of interfacial forces and elastic substrate deformations on the motion of the advancing biofilm edge. Briefly, we consider the biofilm as a shallow drop of viscous suspension whose lateral spreading is driven by bioactive growth and ensuing osmotic fluxes. The relevant evolution equations for the biofilm components and the substrate deformation are derived from a gradient dynamics approach^{41,42} supplemented by a bioactive growth term that mimics biological growth processes (cell division and matrix production).

Within this framework we investigate how substrate rigidity and biomass production rate affect the lateral spreading speed at the biofilm edge. We recover the experimentally observed behaviour of a slowing down of spreading with increasing substrate softness, *i.e.* with decreasing rigidity, at constant substrate osmotic pressure. Furthermore, we identify a growth regime, where the substrate softness leads to a complete arrest of the biofilm edge. We find that the reduced biofilm spreading speed on soft surfaces is not directly related to the visco-elastic braking observed for the spreading of droplets of passive liquid on soft solid surfaces^{42–45} but is rather caused by a reduced osmotic influx of solvent into the biofilm at its edges, which results from the thermodynamic coupling between substrate deformation and interfacial forces.

The manuscript is structured as follows. In Section 2 we introduce a minimal dynamic model for osmotic spreading on a soft elastic substrate and discuss the relevant parameters. In Sections 3-5the model behaviour is analysed using full numerical simulations. First, in Section 3 we investigate equilibrium biofilm shapes and substrate deformations for model biofilms with an imposed amount of biomass. Then, in Section 4 we analyse the dependence of the spreading dynamics of active model biofilms on the substrate softness and biomass growth rate. Finally, in Section 5, we establish a link between our theoretical results and the experiments of Asp *et al.*,⁷ and thereby propose a unifying description of the qualitatively different dependencies of the spreading velocity on the substrate stiffness on hydrogels of various architectures. We conclude in Section 6 by a thorough discussion of our theoretical results.

2 Model

We consider osmotic biofilm growth and spreading on a soft solid substrate within a mesoscopic modelling framework (Fig. 1) as previously introduced for rigid solid substrates.^{20,46}



Fig. 1 Osmotic spreading of a biofilm on a soft substrate. (a) Sketch of a biofilm illustrating the film height $h(\vec{r},t)$ biomass amount $\Psi(\vec{r},t)$ and vertical substrate displacement $\xi(\vec{r},t)$. Osmotic pressure gradients are generated as bacteria consume water and nutrients to produce biomass *via* bacterial proliferation and matrix secretion, which is described by the growth term $j_{\rm g}$. This causes an osmotic influx of nutrient-rich water $j_{\rm o}$ from the moist substrate into the biofilm. (b) Magnification showing the mesoscopic view of the leading edge of the biofilm, illustrating the physical influences (capillarity, wettability, elasticity) in the contact line region: a fluid adsorption layer of height $h_{\rm a}$ and devoid of biomass is in contact with the biofilm with the macroscopic contact angle θ_h . The vertical force balance at the contact line deforms the substrate (displacement ξ). γ_h and γ_{ξ} denote the surface tensions of the biofilm-gas and the substrate–biofilm interfaces, respectively. The wetting energy $f_w(h)$ describes the wettability of the substrate.

Here, we incorporate an underlying viscoelastic substrate in analogy to the approach introduced by Henkel *et al.*,^{42,47} namely, by considering a strain energy related to the vertical displacement of the solid–liquid interface in the fully compressible case. The biofilm itself is modelled as a thin liquid film of a suspension of biomass (bacteria and extracellular matrix) in a solvent (nutrient-rich water). The relevant field variables are the film thickness $h(\vec{r},t)$, the biomass $\Psi(\vec{r},t)$ and the vertical substrate displacement $\xi(\vec{r},t)$ where $\vec{r} = (x,y)^{T}$ are planar Cartesian coordinates. The biomass variable Ψ represents the effective biomass height, *i.e.* any spatial variations in the vertical direction within the biofilm are neglected. In addition, for convenience, we introduce the biomass volume fraction ϕ which is related to the effective biomass thickness Ψ by

$$\varphi = \frac{\Psi}{h}.$$
 (1)

For a thorough discussion of the usage of Ψ and ϕ see Trinschek *et al.*⁴⁶ The free energy functional \overline{F} (expressed in *h*, ξ , and ϕ) that determines the physico-chemical driving forces for all transport processes for the passive (non-bioactive) suspension is

$$\bar{F}[h,\xi,\varphi] = \int_{\Omega} \left[f_{\text{cap}}(h,\xi) + f_{\text{el}}(\xi) + f_{\text{w}}(h) + hf_{\text{m}}(h,\varphi) \right] \mathrm{d}\Omega \quad (2)$$

with the capillary energy (liquid–vapour surface tension γ_h , solid–liquid surface tension $\gamma_{\mathcal{E}}$)

$$f_{\rm cap} = \frac{\gamma_{\rm h}}{2} |\nabla(\xi + h)|^2 + \frac{\gamma_{\xi}}{2} |\nabla\xi|^2, \tag{3}$$

where $\nabla = (\partial \partial_{xy} \partial \partial_y)^T$ denotes the planar gradient operator. The elastic energy due to a vertical deformation of the substrate is modelled by a Winkler foundation model for a fully compressible substrate⁴²

$$f_{\rm el} = \frac{\kappa_{\rm v}}{2} \xi^2 \tag{4}$$

where κ_v is an elastic constant. We employ a simple wetting energy for a partially wetting liquid consisting of the sum of a short-range action48-50

$$f_{\rm w} = A \left(-\frac{1}{2h^2} + \frac{h_{\rm a}^3}{5h^5} \right) \tag{5}$$

where A is a Hamaker constant and h_a denotes the equilibrium thickness of a very thin adsorption layer at the substrate. The same form of the wetting energy has recently been employed in other thin-film models.^{19,20,41,42,51-53}

The entropy of mixing in the bulk of the liquid film is given by

$$f_{\rm m} = \frac{k_{\rm B}T}{a^3} [\varphi \ln \varphi + (1-\varphi)\ln(1-\varphi)],$$
 (6)

where a denotes an effective length scale characterising the biomass. $k_{\rm B}T$ denotes the thermal energy. Using the recently advanced gradient dynamics approach to thin film modelling^{41,42,53-57} we have derived the transport equations of the passive mixture supplemented by a bioactive growth term $j_o(h, \phi)$, which breaks the variational structure and renders the suspension bioactive. The resulting evolution equations for the thermodynamic variables h, Ψ, ξ are given by

$$\partial_t h = \nabla \cdot \left[Q_{hh} \nabla \frac{\delta F}{\delta h} + Q_{h\Psi} \nabla \frac{\delta F}{\delta \Psi} \right] + j_0 \tag{7}$$

$$\partial_t \Psi = \nabla \cdot \left[Q_{\Psi h} \nabla \frac{\delta F}{\delta h} + Q_{\Psi \Psi} \nabla \frac{\delta F}{\delta \Psi} \right] + j_g \tag{8}$$

$$\partial_t \xi = -\frac{1}{\zeta} \frac{\delta F}{\delta \xi} \tag{9}$$

Note, that here we employ the variation of the free energy $F[h,\xi,\Psi]$ which relates to the free energy $\overline{F}[h,\xi,\phi]$ in (2) as $\overline{F}[h,\xi,\phi] =$ $\overline{F}[h,\xi,\Psi/h] = F[h,\xi,\Psi]$. In the following ϕ should only be seen as a convenient short-hand notation for Ψ/h . The mobilities Q_{ij} form the symmetric and positive definite mobility matrix

$$\begin{pmatrix} Q_{hh} & Q_{h\Psi} \\ Q_{\Psi h} & Q_{\Psi \Psi} \end{pmatrix} = \frac{1}{3\eta} \begin{pmatrix} h^3 & h^2 \Psi \\ h^2 \Psi & h\Psi^2 \end{pmatrix} + \begin{pmatrix} 0 & 0 \\ 0 & D\Psi \end{pmatrix}.$$
(10)

Here, η denotes the composition-dependent biofilm viscosity

$$\eta = \eta_0 [(1 - \phi) + \mu \phi], \tag{11}$$

and μ represents the ratio $\mu = \eta_b/\eta_0$ of the viscosities of the pure biomass η_b and the pure solvent η_0 . Further, $D = a^2/(6\pi\eta)$ denotes the biomass diffusivity consistent with the diffusion constant $D_{\text{diff}} = k_{\text{B}}T/(6\pi\eta a)$ with a being the typical biomass length scale as introduced in eqn (6). Finally, ζ denotes the viscosity of the solid viscoelastic substrate.

The non-conserved fluxes j_0 and j_g correspond to the osmotic flux of solvent between the moist substrate and the biofilm and the active growth of biomass in the biofilm, respectively. Thereby, the osmotic flux is thermodynamically driven by the difference between the osmotic pressures in the biofilm Π and in the substrate Π_s , *i.e.*

$$j_{\rm o} = Q_{\rm o}(\Pi - \Pi_{\rm s}),\tag{12}$$

stabilising and a long-range destabilising van-der-Waals inter- where the former is given as variation of the energy functional

$$\Pi = -\frac{\delta F}{\delta h} \tag{13}$$

and the latter is imposed as

$$\Pi_{\rm s} = -\frac{k_{\rm B}T}{a^3} \ln\Big(1 - \varphi_{\rm eq}\Big). \tag{14}$$

Eqn (14) implies that a thick biofilm of uniform height $h \gg h_{\rm a}$ and biomass concentration $\phi_{\rm eq}$ is in thermodynamic equilibrium with the substrate. Note, that we treat the substrate as an infinite solvent reservoir at fixed uniform osmotic pressure Π_s (*i.e.* a chemostat). In other words, we neglect any effect a substrate deformation might have on Π_s . Finally, Q_0 denotes a mobility.

The active biomass growth $j_{\rm g}$ is modelled as logistic growth with limited resources

$$j_{g}(h,\varphi) = gh\varphi(1-\varphi) \left(1 - \frac{h\varphi}{h^{*}\varphi_{eq}}\right) f_{mod}(h,\varphi)$$
(15)

where g is a rate constant, $\Psi^* = \phi_{eq}h^*$ gives the upper limit for the biomass layer thickness that can be sustained on a substrate, *i.e.* neglecting spatial gradients, the biofilm will reach a stationary state of uniform height h* and biomass concentration ϕ_{eq} . Thereby, Ψ^* is related to the thickness for which nutrient diffusion and consumption of nutrients by the bacteria throughout the vertical profile of the film equilibrate.^{12,58} The function $f_{\rm mod}$ which governs the onset of biomass growth is given by

$$f_{\rm mod}(h,\varphi) = \left(1 - \frac{h_{\rm u}\varphi_{\rm eq}}{h\varphi}\right) \left[1 - \exp\left(\frac{h_{\rm a}\varphi_{\rm eq} - h\varphi}{h_{\rm a}}\right)\right]$$
(16)

and ensures that growth only starts if the biomass Ψ exceeds a (small) critical value $\Psi_u = \phi_{eq} h_u$, such that no biomass is produced spontaneously in the adsorption layer of thickness $h_a < h_u$, and the biomass in the adsorption layer equilibrates at a small value $\Psi_{\rm a} = h_{\rm a}\phi_{\rm eq}$. For effective biomass thickness $\Psi \gg \Psi_{\rm u}$ we have $f_{\rm mod}$ = 1 and the function does not affect the biomass growth.

A core feature of the employed simple gradient dynamicsbased modelling for thin films of mixtures is the approximation that vertical concentration gradients are small.^{41,46} Note that another class of models takes vertical concentration gradients into account.^{24,58} However, Tam et al.²⁴ also show that such vertical dependencies are small for biologically realistic parameters further confirming our chosen modelling approach.

To facilitate the model analysis we introduce the vertical length scale

$$\mathscr{H} = h_{\mathrm{a}},$$
 (17)

the horizontal length scale

$$\mathscr{L} = \sqrt{\frac{\gamma_h}{A}} h_{\rm a}^{\ 2}, \tag{18}$$

and the time scale

$$\mathscr{T} = 3 \frac{\eta_0 \gamma_h h_a^5}{A^2}.$$
 (19)

The scaling of space and time results in a nondimensional parameter, the substrate softness $s \sim 1/\kappa_v$ (*i.e.* the inverse of the substrate rigidity)

$$s = \frac{\mathscr{L}_{cc}^2}{\mathscr{L}^2} \tag{20}$$

where the elastocapillary length $\mathscr{L}_{\rm ec} = \sqrt{\frac{\gamma_h}{\kappa_v}}$ enters naturally, which characterises the typical elastic deformation induced by surface tension.

In the remainder of the manuscript all dimensional quantities will be expressed tacitly in the scales \mathscr{H} , \mathscr{L} and \mathscr{T} , *e.g.* the biomass growth rate constant g in units of $1/\mathcal{T}$, the biofilm height h and biomass layer thickness Ψ in units of \mathcal{H} , the horizontal distance x in units of \mathcal{L} , etc. The nondimensional model equations and nondimensional parameters are summarised in Table S1 in Section S1 of the ESI.[†] The above system of eqn (2)-(16) is numerically integrated using the finite element method (FEM) implemented in the software package oomphlib.^{59,60} This package enables efficient direct time simulations, incorporating adaptive time stepping based on a second-order backward differentiation method. The software's spatial adaptivity makes it suitable for handling large-scale systems and sharp geometric features like wetting ridges. Simulations of eqn (2)-(16) were performed on one-dimensional domains of size L = 2000 with Neumann boundary conditions.

3 Passive behaviour of a biofilm on a soft elastic substrate

In a first set of simulations, we characterise the passive spreading dynamics of biofilm droplets of fixed constant biomass $\int \Psi dx$, *i.e.* without biomass growth (g = 0), depending on the substrate softness *s*. In this scenario droplets may exchange solvent with the substrate which acts as an osmotic chemostat. The equilibrium state is characterised by a vanishing of all fluxes, a stationary droplet shape and a stationary substrate deformation.

We initialise all droplets with the identical parabolic film profile $h_0(x)$ with the Young–Dupré contact angle^{42,61} on an undeformed substrate and an initial profile for the biomass height $\Psi_0(x) = h_0(x)\phi_{eq}$ (for more details refer to Section S2 of the ESI†). Droplets then evolve towards their equilibrium shapes according to eqn (2)–(16). Fig. 2(a)–(c) illustrates the resulting equilibrium drop shapes and substrate deformations as a function of substrate softness *s*. On a rigid substrate the droplet does not deform the substrate (Fig. 2(a)). As softness increases, wetting and capillary forces increasingly deform the substrate, impacting in turn the drop shape. The first apparent signature of elastocapillary forces is the deformation of the substrate in the contact line region: with increasing softness a so-called wetting ridge is increasingly pulled out of the



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Fig. 2 Equilibrium shapes of passive biofilms with a fixed biomass $\int \Psi dx$ on soft substrates. (a)–(c) Typical equilibrium droplet shapes and substrate deformations in (a) the nearly rigid limit s < 10, (b) the moderately soft regime $10 < s < 10^5$ regime and (c) the very soft (liquid) limit $s > 10^5$. Panel (d) shows the scaling behaviour of the wetting ridge height $\Delta \xi$ that distinguishes the three regimes. The two vertical dashed lines in (d) indicate the transitions from the rigid to the soft regime and from the soft to the liquid regime.

substrate in the vertical direction (Fig. 2(b)). For very soft substrates, the distinguished wetting ridge shrinks again as the droplet rather sinks into the substrate forming a liquid lens (Fig. 2(c)). Note that the resulting equilibrium droplet volume V only depends very weakly on the substrate softness s (see Fig. S1 in Section S3 of the ESI†).

As characterised for drops of simple passive liquids on soft elastic substrates,^{42,45} three different regimes of elastocapillarity can be identified. The three regimes can formally be distinguished by the scaling of the height of the wetting ridge‡ $\Delta \xi_{\rm max}$ with the substrate softness⁴² (Fig. 2(d)). The transitions between the three regimes are associated with the interplay of three length scales, namely, the elastocapillary length $\mathscr{L}_{\rm ec}$, the mesoscopic scale \mathscr{L} , *i.e.* the interface width which is governed by capillarity and wetting forces, and the macroscopic scale, *i.e.* the typical drop size r.^{42,45,62}

Briefly, we identify a nearly rigid regime $(\mathcal{L}_{ec}/\mathcal{L} = \sqrt{s} \leq 1)$, where the drop barely 'feels' the substrate softness as elastic forces completely dominate. In consequence, the substrate barely deforms in the mesoscopic contact line region, and the droplet shape is governed by the Young–Dupré equation (Fig. 2(a)). The wetting ridge height scales linearly with softness, *i.e.* $\Delta \xi_{\max} \sim s$. This can be intuitively understood by expressing the vertical force balance at the contact line as $\kappa_v \xi_r \mathcal{L} = \gamma_h \sin \theta_h$ where ξ_r denotes the substrate displacement at the contact line. This results in the scaling $\Delta \xi_{\max} = \xi_r \sim \kappa_v^{-1} \sim s$ (using $\kappa_v \sim s^{-1}$ from eqn (20)).

In the moderately soft regime $(10 < s < 10^5; \mathcal{L} < \mathcal{L}_{ec} < r)$ a wetting ridge with a height smaller but comparable to the

[‡] Here we define the wetting ridge height as the difference $\Delta \xi_{\max} = \xi_{\max} - \xi(L)$, where ξ_{\max} denotes the maximal vertical substrate displacement in the contact line region and $\xi(L)$ indicates the substrate displacement in the adhesion layer far away from the biofilm edge.

drop size is pulled out (Fig. 2(b)). Its height scales with softness as $\Delta \xi_{\rm max} \sim s^{1/2}$.

In the very soft regime, where the droplet sinks into the substrate the wetting ridge height decreases as $\Delta\xi_{\rm max} \sim s^{-1}$ (Fig. 2(c)). In this regime $\mathscr{L}_{\rm ec} > r$, capillarity and wetting forces dominate while elastic forces can be neglected. The scaling in the moderately and very soft regimes can be understood by considering the macroscopic vertical force balance at the contact line for a liquid ridge in the small slope approximation, *i.e.* $\sqrt{1 + (\partial_x \xi)^2} \approx 1 + \frac{1}{2}(\partial_x \xi)^2$ and $\sqrt{1 + (\partial_x h + \partial_x \xi)^2} \approx 1 + \frac{1}{2}(\partial_x h + \partial_x \xi)^2$. In this case the vertical force balance reads (see Section S4 of the ESI† for details)

$$0 = [\gamma_h \partial_x (h + \xi) + \gamma_s \partial_x \xi]_{x=r_-} - [\gamma_{sv} \partial_x \xi]_{x=r_+}, \qquad (21)$$

where γ_{sv} denotes the surface tension of the solid–vapour interface which relates to the wetting energy (eqn (5)) by $\gamma_{sv} = f_w(h_a) + \gamma_s + \gamma_h$.⁶¹ The positions $x = r_-$ and $x = r_+$ indicate a respective evaluation directly to the left (liquid covered region) and directly to the right (bare substrate) of the contact line situated at x = r.

In the moderately soft regime ($\mathcal{L}_{ec} < r$) eqn (21) reads

$$pr = \xi_r \sqrt{\kappa_v} \left(\sqrt{\gamma_h} + \sqrt{\gamma_{sv}} \right) = \kappa_v \xi_r \left(\mathscr{L}_{ec,1} + \mathscr{L}_{ec,2} \right), \tag{22}$$

where the Laplace pressure *p* and the droplet radius *r* are assumed to be constant and identical to the rigid regime. The force balance (22) can be interpreted as a constant force (the liquid-vapor interfacial tension) pulling at the substrate which is deformed over the lengths $\mathscr{L}_{\rm ec,1} = \sqrt{\gamma_{\rm s}/\kappa_{\rm v}}$ and $\mathscr{L}_{\rm ec,2} = \sqrt{\gamma_{\rm sv}/\kappa_{\rm v}}$ to the left and the right of the contact line, respectively. This results in the scaling $\Delta\xi_{\rm max} \approx \xi_r \sim \kappa_{\rm v}^{-1/2} \sim \sqrt{s}$.

In the very soft regime ($\mathscr{L}_{ec} > r$) the liquid–vapour surface tension drives the droplet into the substrate *via* the curvature of the liquid–vapour interface $(\int_0^r [p + \kappa_v \xi(x)] dx)$ and exerts an upward directed point force on the surface at the contact line (*pr*). The force balance (eqn (21)) can be rewritten in the intuitive formulation

$$pr = \kappa_{v}\xi_{r}\mathscr{L}_{\mathrm{ec},2} + \int_{0}^{r} [p + \kappa_{v}\xi(x)]\mathrm{d}x, \qquad (23)$$

which simplifies to

$$0 = \kappa_{\rm v}\xi_r \mathscr{L}_{\rm ec,2} + \int_0^r \kappa_{\rm v}\xi(x)\mathrm{d}x, \qquad (24)$$

and results up to leading order in the scaling $\xi_r = \frac{pr^3}{3\gamma_{\rm sl}\sqrt{\gamma_{\rm sv}}} \sqrt{\kappa} \sim s^{-1/2}$ (see Section S4 of the ESI† for the detailed calculation) and $\Delta\xi_{\rm max} = \xi(r) - \xi(L) \approx \xi_r(L-r)/\mathscr{L}_{\rm ec,2} \sim \xi_r\sqrt{\kappa_v} \sim s^{-1}$. Note, that the slow decay of the displacement of the bare substrate contributes to the scaling of $\Delta\xi_{\rm max}$. Note also, that we assume here that the Laplace pressure and radius of the droplet are constant and correspond to the liquid regime with vanishing κ_v , where the wetting ridge vanishes and the droplet floats with a lens-like shape at the substrate–vapour interface.

In the examples of Fig. 2, the droplet size r is of order $100 \mathscr{L}$, situating the transition from the moderately soft to the very soft regime at $s \approx 10^4$, which well agrees with our simulations. Having studied the case of passive drops as a reference case, next we consider the bioactive case.

4 Spreading of active biofilms on soft substrates

Here we focus on an investigation of the spreading behaviour of bioactive films on moderately soft and very soft substrates (*i.e.* s > 10, g > 0). Note that the osmotic spreading of biofilms on rigid solid substrates has been extensively characterised by Trinschek *et al.*^{20,46} Simulations of biofilm growth are started from a small biofilm droplet (parabolic film profile h_0 with biomass profile $\Psi_0 = h_0\phi_{eq}$, see Section S2 of the ESI† for details), which then develops according to eqn (2)–(16) with a biomass growth rate constant g > 0. Fig. 3 exemplarily characterises the spreading behaviour at fixed substrate softness $s = 10^4$ for two different biomass growth rates (for numerical details see Section S5 of the ESI†).

At low biomass growth rate ($g = 1.3 \times 10^{-6}$, Fig. 3(a)) the biofilm swells until reaching a stationary state where drop, biomass and substrate deformation profiles do not change any more. This parallels the state of arrested growth already described in Trinschek et al.,20 with the addition, that the substrate is deformed and a stationary wetting ridge develops at the biofilm edge. Strikingly, at an increased biomass growth rate constant ($g = 5.3 \times 10^{-6}$, Fig. 3(b)), the spreading behaviour dramatically changes. After a transient phase of combined vertical and horizontal swelling, similar to the transient in the arrested case, the biofilm enters a continuous lateral spreading regime. Then the biofilm edge advances with a constant shape and speed. This behaviour mirrors the continuous growth state described in Trinschek et al.20 with the additional feature that the biofilm edge deforms the substrate and a wetting ridge continuously advances with the biofilm edge.

Fig. 3(c) and (d) further characterise the arrested and continuous spreading regimes at long times in terms of the evolution of the biofilm volume and total biomass (V, blue and green curves, respectively), the maximal film height h_{max} and wetting ridge height $\Delta \xi$, the contact angle of the biofilm edge θ_h , and the lateral biofilm extension r. The short-time behaviour is shown in more detail in Fig. S2 in Section S6 of the ESI.[†] In the arrested case, at large times, the film volume, biomass and lateral biofilm extension reach plateau values whereas in the continuous growth case they increase linearly with time. In both cases, the maximal value of the film height reaches a constant value close to the imposed maximal film height h^* , where the net biomass increase stops [eqn (15)]. In the case of continuous spreading the growth restriction leads to a pronounced pancake-like shape of the biofilm, whereas in the arrested case, the biofilm adopts a spherical cap-like shape. Furthermore, in both cases, the wetting ridge height converges to the value found in the passive limiting Paper



Fig. 3 Spreading of active biofilms on soft substrates. (a) and (b) Snapshots of biofilm profiles (blue shading) and substrate deformation profiles (brown shading) at (a) low biomass growth rate constant ($g = 1.3 \times 10^{-6}$) and (b) high biomass growth rate constant ($g = 5.3 \times 10^{-6}$). The colour gradient in the biofilm profile indicates the progression of time: darker colours represent initial evolution steps and lighter colours indicate later stages. The profiles correspond to times $t \in \{0, 5.49 \times 10^{6}, 1.37 \times 10^{7}, 3.16 \times 10^{7}, 4.44 \times 10^{8}\}$ in (a) and $t \in \{0, 1.3 \times 10^{6}, 1.1 \times 10^{7}, 3 \times 10^{7}, 5 \times 10^{7}, 7 \times 10^{7}, 9 \times 10^{7}\}$ in (b). Note that the colour scale is logarithmic in (a) and linear in (b). In (a) the film, biomass and substrate deformation profile evolve towards a stationary state (arrest of spreading). In (b), after an initial swelling phase, the biofilm edge advances at constant shape and speed (continuous spreading). (c) and (d) Time evolution of biofilm and biomass volume (V, blue and green, respectively), maximal biofilm (h_{max} , blue) and wetting ridge ($\Delta\xi$, red) heights, macroscopic contact angle θ_h (for details of measurement see Section S5 of ESI†) and biofilm extension (r). The dashed vertical line in (d) denotes the onset of the continuous spreading regime. The substrate softness is $s = 10^{4}$ and remaining parameters are as given in Table S1 in the ESI.†

case (for a detailed analysis see Fig. 4). Also, the contact angle is evolving in both cases in a similar manner.

We next investigate the robustness of the above described transition between arrested and continuous biofilm growth by varying the substrate softness s. Fig. 4(a)-(f) show exemplary biofilm profiles for various growth rate constants and substrate softnesses s while Fig. 4(g) presents a nonequilibrium phase diagram that gives the spreading speed in the parameter plane spanned by the biomass-growth rate g and the substrate softness s. For completeness the effect of the biomass growth on the wetting ridge height is shown in Fig. S3 of Section S7 of the ESI.[†] In general, biofilm spreading is favoured on rigid substrates. In contrast, soft substrates are unfavourable for biofilm spreading and may completely stop biofilm evolution. At very low growth rates, continuous spreading can not be achieved, independent of the substrate softness. Importantly, in the intermediate regime, spanning one order of magnitude for the growth rate constant g (5 \times 10⁻⁷ < g < 5 \times 10⁻⁶), the biofilm spreading velocity is controlled by substrate softness in a parameter region spanning nearly 3 orders of magnitude, *i.e.* $10^2 < s < 10^5$ (Fig. 4(g) and (h)). At large growth rates $(g > 5 \times 10^{-6})$, continuous spreading occurs across all three softness regimes such that even on very soft substrates spreading is continuous, albeit with a low velocity (blue curve in Fig. 4(h)). Note, that at high growth rates the velocity does not drop monotonically with increasing substrate softness, but slightly increases with increasing softness before dropping sharply (blue and red curves in Fig. 4(h)). For rigid substrates Trinschek *et al.*²⁰ find that the transition from arrested to continuous spreading occurs when reducing the influence of surface forces as compared to entropic forces. Here, a similar transition is observed when varying the substrate elasticity. This shows that substrate softness represents another important passive material property, which fundamentally alters biofilm spreading behaviour.

To gain a better understanding of the physical mechanism underlying the arrest of spreading on very soft substrates we next investigate the hypothesis, that the osmotic solvent exchange between the substrate and the biofilm is altered in spreading biofilms as compared to arrested biofilms. Fig. 4(i) shows exemplary spatial profiles of the osmotic exchange flux $j_0(x)$ between the substrate and the biofilm for a spreading (s = 300) and an arrested (s = 9000) biofilm. In the spreading biofilm, the flux vanishes in the central region of the biofilm ($x \approx 0$). Close to the biofilm edge, where biomass is produced, the osmotic flux is directed from the substrate into the biofilm. Interestingly, in a region between the biofilm edge and the biofilm centre, the osmotic flux is directed from the biofilm into the substrate. However, the osmotic outflow in this region is weak compared to the massive osmotic influx at the advancing biofilm edge. In the arrested case, osmotic fluxes are still present. Although the spatial profiles (film height h, biomass Ψ , substrate deformation ξ) are stationary, and conserved and nonconserved fluxes are balanced, they do not vanish. This is a signature of active, *i.e.*,



Fig. 4 Dynamical phase behaviour of biofilm spreading in dependence of biomass growth and substrate softness. (a)–(c) Drop and substrate deformation profiles for continuously spreading biofilms at a biomass growth rate constant $g = 6 \times 10^{-6}$. The softness is (a) $s = 10^{-2}$ (nearly rigid case), (b) $s = 10^3$ (moderately soft case), and (c) $s = 10^7$ (very soft case). (d)–(f) Drop and substrate deformation profiles for arrested spreading showing the resulting stationary biofilms at a biomass growth rate constant $g = 2 \times 10^{-7}$. The softness is (d) $s = 10^{-2}$, (e) $s = 10^3$, and (f) $s = 10^7$. (g) Morphological phase diagram in the plane spanned by substrate softness s and the biomass growth rate constant g. The lateral spreading velocity in the continuously spreading regime is indicated by the blue shading (see colour bar on the right). In the white region the biofilm spreading is arrested. (h) Examples of the dependence of the lateral spreading speed on softness for various biomass growth rate constants g as indicated in the legend. (i) Examples of somotic solvent flux profiles $j_0(x)$ for a continuously spreading biofilm at s = 300 and an arrested biofilm at s = 9000 at fixed $g = 1.3 \times 10^{-6}$ (corresponding to the green curve in panel (h)). The vertical dotted lines indicate the position of the wetting ridge.

out-of-equilibrium, behaviour and is a direct result of the gradient dynamics structure being broken by biomass growth j_g in eqn (8). The osmotic flux is directed into the substrate at the centre of the biofilm and into the biofilm close to the edge of the biofilm, where it drops to zero as the wetting ridge is approached. From the inspection of the osmotic flux profiles on the macroscale it does not yet become clear, what feature causes the spreading arrest, since the observed osmotic influx close to the biofilm edge should favour spreading in both cases.

However, a close inspection of the osmotic pressure profile in the biofilm on the mesoscopic scale in the contact line region reveals important differences between arrested and spreading biofilms. Fig. 5(a) shows the spatial profile of the osmotic pressure difference $\Delta \Pi$ between the biofilm and the substrate in the contact line region for spreading and arrested biofilms. All profiles were laterally shifted such that the wetting ridge is located at x = 0. The osmotic pressure difference $\Delta \Pi$ for the advancing biofilm fronts (s < 9000) is positive and shows a local maximum in the contact line region $x \approx 0$ indicating solvent influx into the biofilm. However, for the arrested biofilm front at s = 9000 the osmotic pressure difference $\Delta \Pi \approx 0$. The osmotic pressure difference contains two contributions: one results from the entropy of mixing of biomass $\Delta \Pi_{\text{entropic}}$ and another one results from interfacial forces (capillarity and wettability) $\Delta \Pi_{\text{interface}}$. Using expression (14) for the constant osmotic pressure $\Pi_s = -\frac{k_B T}{a^3} \ln \left(1 - \varphi_{eq}\right)$



Fig. 5 Role of the osmotic flux between the substrate and the biofilm in spreading on soft substrates. (a) Osmotic pressure difference $\Delta \Pi$ between biofilm and substrate in the contact line region for various agar softnesses *s* as indicated in the legend. The growth rate constant is $g = 1.3 \times 10^{-6}$. At a softness of s = 9000 the contact line is stationary. All other curves (s < 9000) belong to spreading biofilm fronts. (b) Entropic $\Delta \Pi_{entropic}$, see eqn (25), and (c) interfacial $\Delta \Pi_{interface}$, see eqn (26), contributions to the osmotic pressure difference. The legends are as in (a). The grey dashed lines in (a)–(c) indicate the location of the wetting ridge for all profiles. Remaining parameters are given in Table S1 in the ESI.†

in the substrate, the two contributions can be expressed as (see eqn (12) and (13))

$$\Delta \Pi_{\text{entropic}} = \frac{k_{\text{B}}T}{a^3} \Big[\ln \Big(1 - \varphi_{\text{eq}} \Big) - \ln (1 - \varphi) \Big], \tag{25}$$

$$\Delta \Pi_{\text{interface}} = \gamma_h \Delta (h + \xi) - \frac{\partial f_w}{\partial h}$$
(26)

The decomposition of the osmotic pressure difference $\Delta \Pi$ into entropic and interfacial contributions (Fig. 5(b) and (c)) reveals that for advancing biofilm edges ($s \leq 3000$) at the contact line the entropic contribution favours osmotic outflux ($\Delta \Pi_{\text{entropic}} < 0$) since the biomass concentration is below the equilibrium value ($\phi < \phi_{\text{eq}}$). However, the interfacial contribution favours osmotic influx ($\Delta \Pi_{\text{interface}} > 0$). The resulting net flux is small (10^{-4} , compared to the magnitude of 10^{-2} for each individual flux) but positive, driving the advancement of the biofilm edge. In contrast, for arrested fronts (s = 9000 in Fig. 5(b) and (c)) the biomass concentration in the biofilm ϕ favours solvent influx, whereas the interfacial forces are inducing a negative osmotic pressure difference, such that outflux is favoured. Importantly, the net solvent flux between substrate

and biofilm vanishes at the contact line. Note, that a fully developed advancing biofilm front (that has developed on a rigid substrate) will initially recede until the biofilm adopts the stationary droplet shape on a soft substrate.

In conclusion, arrested and spreading case differ qualitatively w.r.t. the forces which drive osmotic fluxes. The transition between the two regimes results from a subtle equilibration of these forces in the contact line region. It emerges that direction and magnitude of osmotic solvent fluxes are decisive for biofilm spreading. Viscoelastic braking observed in droplet spreading of passive fluids is certainly present in biofilms as well, but not the major determinant for a decreased spreading speed on moderately soft to very soft substrates.

5 Comparison with experiments

Up to now, we have treated the osmotic pressure in the substrate (determined by the hydrogel concentration ϕ_{eq}) and the substrate softness s as independent parameters, and have obtained results as discussed at Fig. 3 and 4 at fixed $\phi_{
m eq}$. This ideal assumption of independent parameters only approximately holds for specific experimental protocols of substrate fabrication. Typically, the hydrogel substrate rigidity is varied, e.g. by increasing the crosslinker concentration at constant hydrogel concentration or by changing the hydrogel concentration at constant cross-linker concentration. When the latter method is used both parameters, osmotic pressure and elastic modulus of the substrate, are impacted in a way specific for each hydrogel. To be able to discuss such scenarios, we study the influence of the osmotic pressure of the substrate (via the equilibrium biomass concentration $\phi_{eq}^{63,64}$). Fig. 6(a) shows the resulting morphological phase diagram in the plane spanned by s and ϕ_{eq} at fixed biomass growth rate $g = 5.3 \times 10^{-6}$. Generally speaking, rigid substrates and a low substrate osmotic pressure favour a rapid biofilm expansion. An increase in the biofilm osmotic pressure reduces the propagation speed of the biofilm edge, since a larger amount of biomass has to be produced in the biofilm to draw water from the substrate into the biofilm.

To establish at least a semi-quantitive link between theory and experiment based on the obtained phase diagram, we introduce (i) appropriate scales to relate the nondimensional softness and the elastic modulus as well as the nondimensional spreading speed to the dimensional one and (ii) we relate substrate osmotic pressure and elastic modulus for a given experimentally employed substrate architecture.

Regarding (i), the shear modulus G' scales as $G' \sim \kappa_v d$, with κ_v denoting the model elastic constant of the substrate and d denoting the substrate thickness.⁴² Using the definitions of softness *s* (20) and elastocapillary length $\mathscr{L}_{ec} = \sqrt{\gamma_h/\kappa_v}$ we find a scaling between the linear shear modulus G' and the softness *s*

$$G' \sim \frac{\gamma_h d}{\mathscr{L}^2 s}.$$
 (27)

The velocity scale is given by \mathscr{L}/\mathscr{T} with the length scale \mathscr{L} and time scale \mathscr{T} defined in eqn (18) and (19).



Fig. 6 (a) and (b) Phase diagrams characterising the biofilm spreading velocity in the plane spanned by the equilibrium biomass concentration ϕ_{eq} and (a) on the one hand the softness *s* and (b) on the other hand the elastic shear modulus *G'*. Thereby, the colour (scales given on the right of each panel) indicates the lateral (adimensional (a), dimensional (b)) spreading velocity within the continuous spreading regime. (c)–(e) Biofilm spreading velocity depending on the substrate shear modulus *G'* for three exemplary scenarios $G'(\phi_{eq})$ as indicated by matching coloured lines in (b), see main text. Lines represent theoretically calculated spreading velocities; symbols correspond to the experimental data of Asp *et al.*⁷ on three different substrate architectures, namely, (c) PAA substrate with fixed PAA concentration and varying cross-linker (bis-acrylamide) concentration, (d) PAA substrate with varying PAA concentration and constant cross-linker (bis-acrylamide) concentration. The (nondimensional) growth rate constant is $g = 5.3 \times 10^{-6}$. The dimensional velocity and the shear modulus are determined as described in the main text.

With this scaling we now compare our results with the experimental observations reported by Asp *et al.*⁷ (see their Fig. 4). They investigate biofilm spreading on hydrogel substrates of various chemical compositions and architectures (agar substrate, bisacrylamide (Bis) cross-linked polyacrylamide (PAA)). Thereby, they influence the elastic modulus by varying either the polymer concentration (agar, PAA) or the cross-linker concentration (Bis). Osmotic spreading on agar substrates with varying concentrations has also been studied, *e.g.* by Ziege *et al.*³⁶ Kochanowski *et al.*⁶³ with similar observed trends as reported in Asp *et al.*⁷

To proceed we assume a (nondimensional) growth rate constant $g = 5.3 \times 10^{-6}$ and visually compare our Fig. 4(h) with Fig. 4 of Asp et al.⁷ In this way, we are able to establish the relation $sG' = \gamma_h d/\mathscr{L}^2 = 2 \times 10^7$ Pa between s and G' and to determine the velocity scale to be $\mathcal{L}/\mathcal{T} = 2.8 \text{ mm s}^{-1}$. Using the gel thickness $d = 1 \text{ mm}^7$ and the surface tension and viscosity of water ($\gamma_h = 70 \times 10^{-3} \text{ N m}^{-1}$, $\eta_0 = 10^{-3} \text{ Pa s}$), we obtain the lateral length scale \mathscr{L} = 1.9 μ m, the vertical length scale $\mathscr{H} = 0.1 \ \mu\text{m}$, and the time scale $\mathscr{T} = 7 \times 10^{-4}$ s. These scales are consistent with a Hamaker constant $A = 10^{-18}$ N m and a dimensional biomass (extracellular matrix, bacteria) growth rate constant $g = 0.5 \text{ min}^{-1}$. The scaling procedure above results in Fig. 6(b) that gives the rescaled representation of the biofilm spreading speed in the plane spanned by the equilibrium biomass concentration ϕ_{eq} and the elastic shear modulus G'. Also here we see that more rigid substrates with low osmotic pressure favour a rapid biofilm expansion.

Finally, we come back to point (ii) from above, regarding the relation between parameters that we have treated as independent up to now. Identifying the experimental parameter of hydrogel concentration with our ϕ_{eq} , we consider three example scenarios for the dependence of hydrogel stiffness G' on ϕ_{eq} that correspond to the experimental conditions reported by Asp *et al.*⁷ in their Fig. 4: in scenario one, G' is increased *via* an increase of the cross-linker concentration at fixed PAA concentration (*i.e.* ϕ_{eq} remains constant, red solid line in Fig. 6(b) and (c)). In scenario two, $G' \sim \phi_{eq}$ scales linearly with the hydrogel concentration (PAA, constant cross-linker concentration, measured by Asp *et al.*⁷ blue dot-dashed line in Fig. 6(b) and (d)). In scenario three, $G' \sim \phi_{eq}^{\nu}$ scales with an exponent $\nu \geq 2$ (agarose,^{65,66} green dashed line in Fig. 6(b) and (e)).

The mentioned Fig. 6(c)–(e) compare the resulting dependence of spreading velocity on shear modulus G' as experimentally measured by Asp *et al.*⁷ and as obtained here when following the three trajectories in the (ϕ_{eq} ,G')-plane (Fig. 6(b)). Interestingly, depending on the hydrogel substrate and the implied specific functional dependence $G'(\phi_{eq})$, biofilm spreading can be enhanced with increasing substrate stiffness (Fig. 6(c)), can show a nonmonotonic behaviour (Fig. 6(d)), or can be slowed down with increasing substrate stiffness (Fig. 6(e)). The obtained coherent explanation of seemingly contradictory results for the dependencies on G' underscores the importance of understanding the relation between the hydrogel parameters elasticity and osmotic pressure.

6 Conclusion

We have demonstrated that biofilm spreading on soft substrates is critically slowed down compared to rigid substrates and that substrate softness can even lead to the complete arrest of the biofilm edge. This result holds for the case where mechanical (rigidity) and physico-chemical (osmotic pressure) substrate properties can be independently controlled. Furthermore, we find that the reduction of the biofilm spreading speed on soft substrates is not directly related to the viscoelastic braking observed for the hydrodynamic spreading of liquid droplets on soft solid substrates⁴²⁻⁴⁵ but is rather caused by a reduced osmotic influx of solvent into the biofilm at its edges, which results from the thermodynamic coupling between substrate deformation and interfacial forces. However, for practically used hydrogel substrates often the mechanical softness and the osmotic pressure cannot be independently controlled, i.e. they cannot be treated as independent parameters. Typically, an increase in substrate softness which slows down spreading is also associated with a reduced osmotic pressure in the substrate, which in turn accelerates spreading. This effect is clearly illustrated by Asp et al.7 where they show that the biofilm spreading velocity on hydrogels strongly depends on substrate architecture. The spreading velocity may increase or decrease with increasing substrate rigidity or may even show nonmonotonic behaviour. Coupling substrate rigidity and substrate osmotic pressure via scaling laws, our minimal theory coherently captures these seemingly contradictory experimental results and clearly underscores the importance of substrate deformations and osmotic fluxes in the dynamics of the advancing biofilm edge.

While the here proposed minimalistic model applies to biofilm growth on abiotic surfaces under air, other more physiological settings may be considered within a slightly modified modelling framework: biofilm growth on biotic surfaces (*e.g.* airway epithelia, airway mucus; relevant for biofilm development in cystic fibrosis patients due to *Pseudomonas aeruginosa*^{67,68}) or growth of immersed biofilms on soft abiotic and biotic surfaces.^{5,69} In the latter case, the coupling between osmotic substrate pressure and substrate rheology is a less important feature, since osmotic fluxes between biofilm and the surrounding medium will dominate over the solvent exchange between biofilm and substrate. Furthermore, more complex situations may be investigated in parallel with experiments, *e.g.* biofilm spreading on soft substrates with spatially varying stiffness or the coupling between matrix/surfactant production and softness.

While our model cannot capture important (species-dependent) biological factors of biofilm initiation and development (*e.g.* quorum sensing), it constitutes nevertheless a useful tool to understand how the physico-chemical and mechanical environmental parameters impact the dynamics of the advancing biofilm edge and may help *e.g.* to develop alternative therapeutic strategies in a targeted manner that do not rely on antibiotic drugs.

Author contributions

AP, KJ, and UT designed research. AP performed all numerical calculations. AP, KJ, and UT wrote the manuscript.

Data availability

All data necessary to plot Fig. 2–6 and the Fig. S1–S3 (ESI[†]) are available in the zenodo repository under the URL https://zenodo.org/records/14235001.

Conflicts of interest

There are no conflicts to declare.

Acknowledgements

We acknowledge support by the Studienstiftung des Deutschen Volkes (AP), the doctoral school "Active living fluids" funded by the German French University (Grant No. CDFA-01-14); the Deutsche Forschungsgemeinschaft (DFG, Grant No. TH781/ 12-2 within SPP 2171). The authors thank Sigolène Lecuyer, Delphine Débarre and Lionel Bureau for fruitful discussions.

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