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Simulation of ultrafast transient absorption spectra of a perylene-based light harvesting antenna†

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Atomistic simulations of photo-induced responses in artificial light-harvesting molecular systems help to reveal the mechanisms of ultrafast intramolecular energy transfer between individual chromophores. These light-induced processes mimic the primary events occurring in natural photosynthesis. Modeling studies contribute to the design of more efficient molecular architectures enabling performance optimization for applications in light harvesting, energy conversion, and optoelectronics. Within this context, the direct comparison between simulated and experimental transient absorption pump–probe (TA-PP) spectra are especially valuable for validating theoretical approaches and deepening mechanistic understanding. Herein, we investigate the photoinduced dynamics of an antenna system composed of two naphthalene monoimides donor units covalently linked to a perylene derived acceptor. Following photoexcitation, the exciton rapidly self-traps on one of the donor units. Thereafter, efficient ultrafast energy transfer to the acceptor unit takes place *via* two possible pathways: either through transient exciton localization on the second donor unit or by direct transfer to the acceptor. The simulated TA-PP spectra clearly capture these distinct energy transfer pathways and enable a detailed comparison of their relative efficiencies. This highlights the system's potential for tunable exciton dynamics towards advancing light-harvesting and optoelectronic molecular materials.

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† Electronic supplementary information (ESI) available: Fig. S1 shows chemical structure of the dendrimer T1 indicating the x, y, and z directions of the body-fixed reference frame, spatial distributions of electronic transition densities and transition dipole moments (μ) for the five lowest energy electronic states; Fig. S2 presents distribution of the average fraction of the transition density matrix localized on the different chromophores; populations of electronic states at short times; Fig. S3 displays excited state natural orbitals; and Fig. S4 and S5 show the analysis of trajectories following the different energy transfer pathways; Fig. S6 displays SE contribution to the TA-PP signal at different times for the different energy relaxation pathways. Fig. S7 and S8 shows nonadiabatic coupling vectors associated to the different energy transfer between states, their projection onto D2A2 normal mode and normal modes with the highest contributions. See DOI: https://doi.org/10.1039/d5sc03157e

1 Introduction

Efficient artificial light-harvesting antenna systems are essential for solar energy conversion by enabling the capture of a significant portion of incident light.[1,2] Their design is often inspired by natural photosynthesis, where energy is absorbed, transferred to the reaction center, and used for charge separation in a highly efficient sequence.[3–6] These artificial systems are typically composed of carefully arranged chromophores with distinct chemical structures and complementary optical absorption profiles, allowing for optimal utilization of solar light spectrum.[7,8]

For robust performance, a light-harvesting antenna must not only efficiently capture energy, but also ensure smooth energy transfer among its chromophores, directing it toward the reactive site for downstream processes.[9,10] To achieve this, the electronic properties of the chromophores must be precisely matched, minimizing competing photoinduced processes that could reduce efficiency. By emulating nature's strategies, researchers aim to enhance energy collection and conversion for advanced solar-powered applications.[11]

The synthetic realization of new artificial multi-chromophoric antenna enables detailed investigations into the efficiency of processes affecting light-harvesting performance.[12–16] The rates of these excitation energy transfer

processes can vary widely, spanning a range from several nanoseconds to tens of femtoseconds. The presence of multiple energy transfer pathways with varying efficiencies, along with competing energy dissipation mechanisms, such as solvent relaxation, determines the overall performance of artificial light harvesters as potential components for solar cells.[6]

Over the past decade, atomistic on-the-fly non-adiabatic excited-state molecular dynamics has emerged as a robust method for exploring the photophysics of realistic molecular and material systems.[17–31] Photoinduced dynamics in multi-chromophore systems involve the interplay of multiple coupled excited states, undergoing nonadiabatic transitions and vibrational relaxation. These processes unfold through distinct energy transfer pathways with varying degrees of efficiency, leading to transient exciton re-localization among different chromophores as the system evolves through its excited-state landscape. Whitin this context, the NEXMD software package[31] has been developed for simulating large conjugated molecules featuring multiple coupled electronic excited states. This code has been previously employed to explore the relative efficiencies of energy transfer pathways in various light harvesting antenna systems.[32–37]

Transient-absorption pump–probe (TA-PP) spectroscopy allows for precise monitoring of ultrafast photoinduced non-adiabatic dynamics in complex molecular systems.[38–43] These experimental advancements can be effectively complemented by emerging modeling approaches that employ direct nonadiabatic molecular dynamics simulations.[44,45] One practical approach combines the classical approximation to the doorway-window (DW) representation introduced by Mukamel and coworkers,[46–48] with the on-the-fly trajectory-based simulations. This methodology has been successfully applied to the simulations of TA-PP signals of pyrazine,[44] phenylene ethynylene dendrimers building blocks,[49] azomethane,[50] a tetra-branched perylene-core dendrimer,[51] and extended to the simulation of electronic two dimensional spectroscopic signals.[52,53] The TA-PP signal is computed as the product of the doorway operator (evaluated at the initial time, $t = 0$) and the window operator (defined at the time delay t between the pump and probe pulses), averaged over an ensemble of quantum-classical nonadiabatic trajectories. These simulations are commonly performed using trajectory surface hopping (TSH) algorithms.[54,55]

In the present work, the photoinduced dynamics of a prototypical antenna system, composed of two naphthalene mono-imides donors linked to a perylene derived acceptor (D2A2), see Fig. 1(a) is explored using nonadiabatic molecular dynamics simulations.[31] Both dynamical observables and TA-PP signals are evaluated. D2A2 belongs to the family of perylene-3,4,9,10-tetracarboxylic acid (PTCA) derivatives, that have been utilized for the construction of artificial light-harvesting antennas owing their exceptional photo(chemical) stability, strong UV-Vis absorption, high electron affinities, and structural versatility that allows for precise molecular tuning.[5,16,56] Previous reports have shown that PTCA and naphthalene monoimide (NMI) derivatives act as an ideal chromophore pair owing to their complementary electronic properties and a combined spectral coverage up to 600 nm.[13,14,57] Light-harvesting antenna
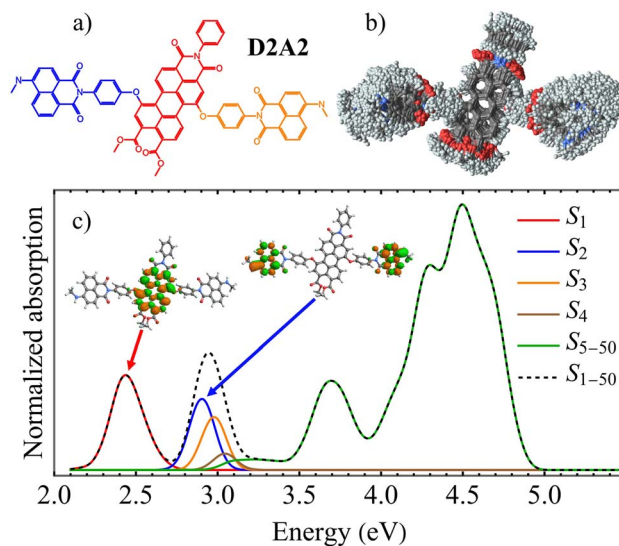

Fig. 1 (a) Chemical structure of the light–harvesting antenna molecule D2A2 indicating individual chromophores: acceptor (red), and donors (blue and orange), (b) superposition of snapshots obtained from the ground state molecular dynamics simulations at room temperature indicating conformational flexibility of the molecule; (c) calculated linear absorption spectra (black dashed) from these snapshots with separate contributions (colors) from the different excited states. Insets show the spatial distribution of electronic transition densities of S_1 and S_2 states calculated at the optimized ground state geometry.

molecules consisting of NMI moieties attached to the 1- and 7-bay positions of PTCA derivatives exhibit a quantitative and ultrafast (~1 ps) electronic energy transfer.[13] The energy donors have been linked at the 1,7-bay-positions of the perylene derivatives, thus leaving the *peri* positions free for further functionalization and device construction. A highly stable and rigid structure, with no electronic communication between the donor and acceptor components, has been realized *via* an all-aromatic non-conjugated phenoxy spacer between the constituent chromophores. According to femtosecond TA-PP experiments performed by W. F. Jager and coworkers,[13] an ultrafast intramolecular energy transfer from donor naphthalene chromophores to the acceptor perylene is observed, without evidences of electron transfer. These observations of fast and efficient energy transfer alongside with broad visible-light absorption, made these antenna systems promising candidates for solar-to-electric and solar-to-fuel conversion technologies, where effective light harvesting and rapid exciton dynamics are critical for performance.

2 Results and discussion

The photoinduced dynamics of the D2A2 antenna has been studied at the atomistic level using nonadiabatic excited-state molecular dynamics simulations. D2A2 is a relatively floppy molecular system exhibiting free rotations at room temperature around the dihedral angles that connect its constituent chromophores. This conformational flexibility is evident from the superposition of D2A2 structures sampled during ground state

molecular dynamics simulations under ambient conditions, shown in Fig. 1(b) (see section Methods for details). The average values of dihedral angles connecting each donor and acceptor units are 55 ± 21° and 78 ± 42° for dihedral angles connecting the donor(blue) and donor (orange) with the acceptor (see Fig. 1(a)), revealing differences in the flexibility of both connections that were also observed during excited state simulations. We expect that the exciton localization and delocalization patterns during excited-state dynamics would be likely influenced by this conformational diversity. Fig. 1(c) shows the simulated absorption spectra based on the conformers in Fig. 1(b), with delineated contributions from various excited states. A good agreement with the experimental absorption spectra has been achieved,[13] showing a low energy band at approximately 2.4 eV (~520 nm) corresponding to the S_1 state, along with a more intense larger peak centered around 2.9 eV (~420 nm). The vertical excitation energies of the five lowest electronic states obtained at the ground state optimal geometry, are listed in Table 1, together with their respective transition dipole moments $\mu_{x,y,z,\text{tot}}$. These dipole components are defined with respect to a body-fixed reference frame, where the x and y axes lie in the plane of the pyrene moiety, as illustrated in ESI Fig. S1.†

The insets in Fig. 1(c) display the spatial distributions of electronic transition densities for the S_2 and S_1 states, computed in the ground-state optimal geometry. The corresponding orbital plots for the S_{3-5} states are provided in ESI Fig. S1.† S_1 is contained to the perylene acceptor. In contrast, while S_2 and S_3 states are localized in the naphthalene monoimide donors, S_4 and S_5 states are localized in the perylene-derived acceptor. In fact, the S_2 and S_3 states are nearly degenerate at the ground state optimal geometry, with their small energy splitting reflecting weak electronic coupling between the terminal naphthalene monoimides. However, this degeneracy is lifted by thermal fluctuations under ambient conditions (see Fig. 1(c)), leading to localization of the S_2 and S_3 wavefunctions on individual units. Not surprisingly, the D2A2 absorption spectra closely resemble the sum of the spectra of its constituent chromophores.[13] The high structural flexibility triggered by thermal fluctuations (Fig. 1(b)), combined with weak electronic coupling between the chromophores,

substantiates exciton localization on individual units. ESI Fig. S2† summarizes the fraction of transition density across the donor and acceptor units for the S_{1-5} electronic states, based on molecular geometries shown in Fig. 1(b). All excited states are localized on individual chromophore units. While S_1 is primarily localized on the acceptor, S_2 and S_3 are localized on a single donor unit. However, S_4 and S_5 exhibit fluctuating localization between the donor and acceptor, driven by thermal fluctuations that can alter their energy ordering. Photoexcitation to different excited states leads to exciton localization on one of the chromophore units. Since the initial experimental pump pulse mainly populates the S_2 and S_3 states, the primary pathway for exciton redistribution during internal conversion involves energy transfer from donor to acceptor units. Moreover, our analysis of the natural transition orbitals for various excited states, as shown in ESI Fig. S3,† confirms that all excited states of interest exhibit Frenkel-exciton character, with no indication of charge transfer processes. This observation is consistent with previous experimental results indicating that ultrafast energy transfer occurs from the donor excited state to the acceptor, while charge transfer processes remain minimal, even over longer time scales.[13,14]

Fig. 2 presents a concise overview of the photoexcited state population dynamics in D2A2, providing a mechanistic view on energy migration between different excited states. Panel (a) depicts the evolution of electronic state populations for low-lying excited S_1–S_5 states. We assume that the pump pulse, centered at $E_{\text{pu}} = 2.90$ eV, primarily excites the S_2 and S_3 states. As shown in Fig. 2(a), an ultrafast $S_3 \rightarrow S_2$ energy transfer takes place within the first ~100 fs, followed by a slower $S_2 \rightarrow S_1$ relaxation process. The population of S_1 state experiences an

Table 1 Vertical excitation energies (VEEs) and transition dipole moments (μ) of the five lowest energy electronic states obtained at the optimal ground state geometry. The primary spatial localization X of the initial transition density $\delta_X^\alpha(0)$ is also reported, indicating the region of the system where the electronic excitation is predominantly localized at time zero

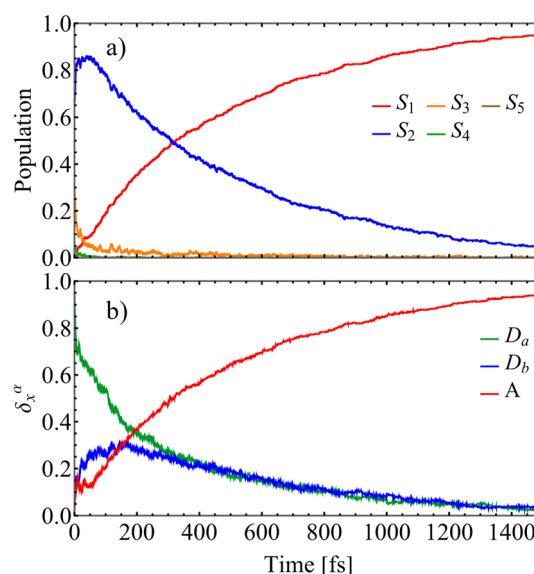| | | μ (a.u.) | | | | |
	VEE (eV)	x	y	z	tot	X
S_1	2.41	1.42	3.45	−0.23	3.74	A
S_2	2.93	3.02	1.26	−1.47	3.59	D_a
S_3	2.94	−0.33	−0.08	0.20	0.49	D_b
S_4	3.06	0.03	0.00	0.07	0.08	
S_5	3.09	−0.46	0.18	−0.04	0.50	

Fig. 2 (a) Evolution of average populations of electronic states calculated from the fraction of trajectories in a particular state at a given time after the initial photoexcitation; (b) evolution of the average fraction of the transition density $\delta_X^\alpha(t)$ on the donors, $D_{a/b}$, (with the highest/lowest initial value of $\delta_X^\alpha(0)$, respectively), and the acceptor (A).

ultrafast rise that follows a single exponential rise profile $1 - \exp(t/\tau)$, with a time constant $\tau = 0.5$ ps. This is somewhat faster than the experimentally reported value of 1.16 ps.[13] A deeper insight into the internal conversion process can be obtained by monitoring changes in the spatial localization of the transition density across the different chromophore units. This is illustrated in Fig. 2(b), which depicts the time evolution of the average fraction of the transition density, $\delta_X^\alpha(t)$, across different chromophores. To perform this analysis, donor units were identified based on their initial excitation levels following photoexcitation. Specifically, the monomer exhibiting the higher transition density was labeled as D_a, while the one with the lower transition density was designated as D_b. This distinction reflects the fact that, at the moment of excitation, D_a absorbs a larger fraction of the excitation energy and is thus more strongly photoexcited than D_b. An ultrafast exchange between donors leads to a subsequent donor-to-acceptor, $(D_{a/b}) \to (A)$, population transfer. Importantly, Fig. 2(b) reveals the existence of two distinct energy transfer pathways: a direct pathway from $D_a \to A$, and an indirect pathway involving $D_a \to D_b \to A$ steps. These alternative energy migration routes between chromophore units can be further characterized and distinguished using the transition density flux analysis[58,59] (see ESI† Transition density flux analysis section). This method directly tracks the distinct pathways of energy redistribution among chromophore units following initial photoexcitation. During nonadiabatic simulations, the effective change in transition density, $\delta_X^\alpha(t)$ (see eqn (1)), is monitored by the flow matrix $f(t)$. This matrix has zero-valued diagonal elements, while the off-diagonal elements, $f_{XY}(t)$, represent the amount of $\delta_X^\alpha(t)$ transferred between units X and Y.[59] Fig. 3 shows the time evolution of the transition density accumulated fluxes $f_{XY}(t)$. We observe that the direct $D_a \to A$ pathway, described by $f_{D_aA}(t)$, accounts for approximately 60% of the intramolecular energy transfer, while the indirect $D_a \to D_b \to A$ pathway, described by the combined fluxes $f_{D_aD_b}(t)$ and $f_{D_bA}(t)$, contributes to the remaining ~40%. This quantitative breakdown reflects the presence of competing energy transfer routes and the relative importance of sequential exciton migration in the overall photoinduced dynamics. The exciton exchange between donors (i.e. $f_{D_aD_b}(t)$) takes place at the early times after photoexcitation, i.e., within the first ~100 fs, that corresponds to the ultrafast

$S_3 \to S_2$ energy transfer. Furthermore, nonadiabatic excited-state trajectories can be classified based on the specific energy transfer pathways they follow during our simulations. To accomplish this, trajectories in which the exciton becomes transiently localized on the D_b unit at any point during the excited-state dynamics—specifically, those where $\delta_{D_b}^\alpha(t) > 0.5$ at any moment—are associated with the indirect $D_a \to D_b \to A$ pathway. In contrast, trajectories where $\delta_{D_b}^\alpha(t)$ remains below 0.5 throughout the entire simulation time, indicating that only one donor (D_a) participates in the transfer process, are associated with the direct $D_a \to A$ pathway. The corresponding evolution of the average populations of electronic states and fraction of the transition density $\delta_X^\alpha(t)$ are displayed in ESI Fig. S4 and S5.† The two pathways exhibit two different time scales of donor → acceptor energy migration. The direct $D_a \to A$ energy transfer pathway leads to an ultrafast population of the S_1 state, characterized by a rapid rise following the function $A - B\exp(t/\tau)$ with a time-constant $\tau = 0.2$ ps. In contrast, the indirect $D_a \to D_b \to A$ pathway involves a slower step-wise transfer with a characteristic rise time of approximately $\tau = 0.8$ ps, reflecting the additional intermediate exciton relocalization step prior to reaching the acceptor.

Further analyses of the ultrafast photoinduced non-adiabatic dynamics after photoexcitation of the D2A2 antenna are directly related to time-resolved spectroscopic measurements. Fig. 4 and 5 showcase the net TA-PP signals simulated using the on-the-fly DW approach (see Methods). The results are shown for both parallel ($s_{pu} = s_{pr}$) and perpendicular ($s_{pu} \perp s_{pr}$) linear polarizations of the pump and probe pulses, respectively.

Fig. 4 and 5 summarize the individual contributions of the ground-state bleaching (GSB), stimulated emission (SE), excited-state absorption (ESA), as well as the total TA-PP signal.
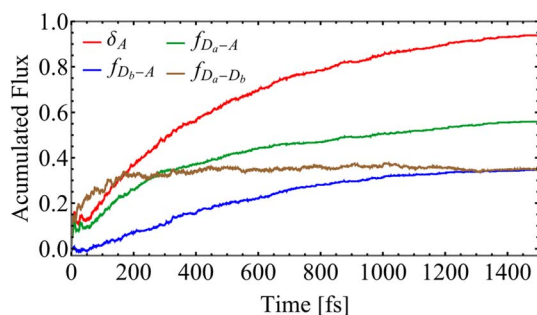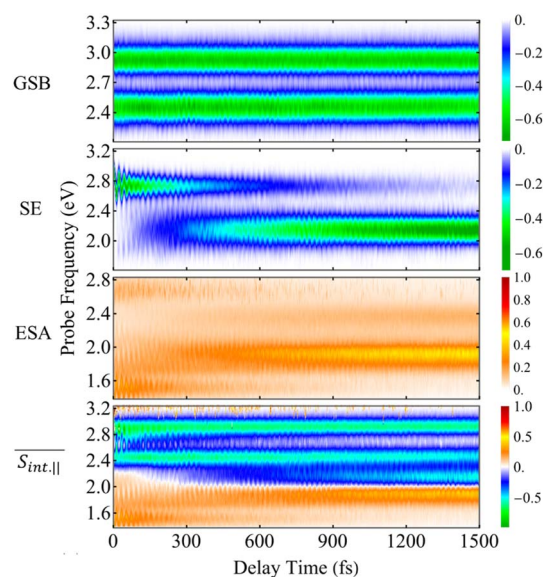

Fig. 4 The GSB, SE, and ESA contributions and the total $\overline{S_{\text{int},\parallel}}(t, E_{pr})$ TA-PP signal for the pump and probe pulses with parallel polarizations, $s_{pu} = s_{pr}$. The calculated signals are plotted as a function of the time delay between the pump and probe pulses, and the probe pulse frequency.
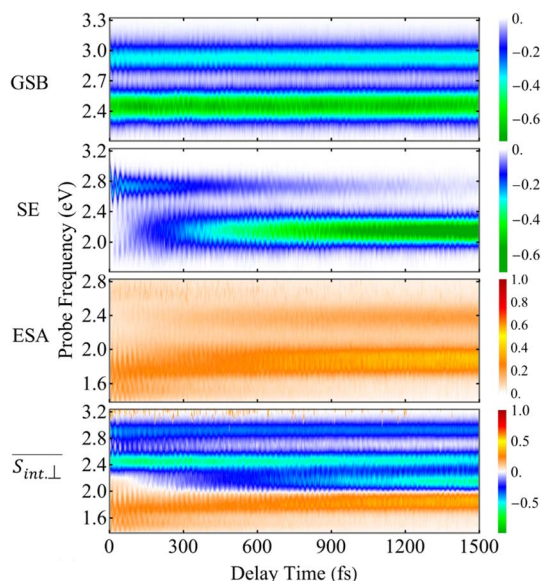

Fig. 3 Accumulated transition density fluxes for the donors ($D_{a/b}$) and the acceptor (A).

Fig. 5 Same as Fig. 4 but for the $\overline{S_{\text{int},\perp}}(t, E_{\text{pr}})$ TA–PP signal obtained for the pump and probe pulses with orthogonal polarizations, $s_{\text{pu}} \perp s_{\text{pr}}$.

To analyze these spectra, we delineate relevant electronic states into 3 distinct manifolds: manifold {0} includes ground state only (S_0), manifold {I} comprises low-lying S_1–S_5 excited states interrogated by the optical pump, and finally manifold {II} encompasses higher-lying S_6–S_{200} excited states, which are involved in the optical probe excitations. In the frequency domain, the signals extend across a broad energy range, reflecting multiple electronic transitions. These include transitions between the ground state and the low-lying excited state of manifold {I}, as well as transition between the states within manifold {I} and higher-lying excited states of manifold {II}. In the time domain, GSB exhibits underdamped oscillations, while SE and ESA signals display slightly damped oscillations, reflecting the wavepacket motion within manifolds {0} and {I}, respectively. Due to the large number of nuclear degrees of freedom involved—most of which are anharmonic—the oscillations observed in the signal lack a clearly defined period. Nevertheless, the separation between the first two SE maxima is around 20 fs. These oscillations are most likely associated with double bond stretching vibrations. According to the distribution of the average fraction of the transition density matrix ($\delta_{\text{X}}^{\alpha}(t)$) displayed in Fig. 2, excited states S_2 and S_3 are mainly localized in the naphthalene monoimides donor units. Therefore, oscillations initially present in the SE and ESA signals can be associated with the double CC bonds in the naphthalene monoimides donor units. ESI Fig. S7(a)† shows the nonadiabatic coupling vector (NACR$_{32}$) associated to $S_3 \rightarrow S_2$ energy transfer. NACR$_{32}$ represents the direction of the force acting on the nuclei during the $S_3 \rightarrow S_2$ transition. We can observe its delocalization between both naphthalene monoimides donor units. The projection of NACR$_{32}$ on the D2A2 normal modes (ESI Fig. S7(b)†) reveals main overlaps with normal modes with periods around 20 fs, in agreement with oscillations initially observed in the SE and ESA signals. Normal modes with the

highest overlap are also shown. The analysis of the nonadiabatic coupling vector (NACR$_{21}$) associated to $S_2 \rightarrow S_1$ energy transfer is shown in ESI Fig. S8(a).† NACR$_{21}$ is delocalized between one of the naphthalene monoimides donor units and the acceptor, as it is expected by the distribution of the average fraction of the transition density matrix ($\delta_{\text{X}}^{\alpha}(t)$) displayed in Fig. 2, where S_2 is mainly localized in one of the naphthalene monoimides donor unit while S_1 is localized in the acceptor. As in the case of NACR$_{32}$, the projection of NACR$_{21}$ on the D2A2 normal modes (ESI Fig. S8(b)†) reveals main overlaps with normal modes with periods around 20 fs. Nevertheless, the main normal modes involved in these transitions present different spatial localization, being mostly localized in the acceptor. Similar spectral features have been previously reported in a light harvesting dendrimer analyzed using broadband, high-resolution TA-PP spectroscopy.[49,51,60]

The GSB signal describes the motion of the "hole" punched by the pump pulse in the electronic ground state. This hole in the nuclear phase space is described by the doorway function D_in of eqn (2). It creates non-stationary nuclear distribution in the electronic ground state. This nonstationary distribution, in turn, produces moving vibrational wavepackets in the electronic ground state which are monitored by the GSB signal. The GSB signal probes transitions from manifold {0} (S_0) to manifold {I} states. In the case of the averaged parallel polarization signal, $\overline{S_{\text{int},\parallel}}$ (Fig. 4), the spectrum exhibits two contributions of comparable intensity centered around $E_{\text{pr}} \approx 2.9$ eV, and ≈ 2.4 eV. These features correspond to electronic transitions from S_0 to S_1 and $S_{2/3}$, respectively. In contrast, for the averaged parallel polarization signal, $\overline{S_{\text{int},\perp}}$, the GSB signal at ≈ 2.4 eV is stronger than the one at ≈ 2.9 eV (Fig. 5). This difference arises from the distinct orientations of the transition dipole moments, μ_{01} vs. $\mu_{02/3}$ (see Table 1 and ESI Fig. S1†), demonstrating that polarization schemes in the detection of TA-PP spectra of dendrimers can be tuned to be sensitive to specific transitions. On the other hand, the underdamped oscillations observed the GSB signals expose the wavepacket motion within the electronic ground state. As noted in previous studies,[49,51] these oscillations are a hallmark of significant non-Condon effects, which result from the strong dependence of transition dipole moments between manifolds {0} and {I} on the nuclear configurations.

The SE signal captures the projection of the nuclear wavepacket motion in manifold {I} onto the ground state, offering deeper insight into nonadiabatic transitions beyond the population dynamics depicted in Fig. 2(a). The ultrafast $S_3 \rightarrow S_2$ internal conversion is evident as a redshift in the SE signal in the frequency domain. Initially centered around $E_{\text{pr}} \approx 2.9$ eV, the SE spectrum shifts toward lower energies within 50 fs of photoexcitation. Subsequently, the $S_2 \rightarrow S_1$ transition depletes the population of the S_2 state, which is centered at $E_{\text{pr}} \approx 2.8$ eV, further shifting the signal to $E_{\text{pr}} \approx 2.2$ eV, thereby revealing the emergence of the S_1 state. After approximately 400 fs, half of the excited state population has transferred to the S_1 state, as indicated by the crossing of the intensities of the SE signal for $E_{\text{pr}} \approx 2.8$ eV and 2.2 eV.

As previously noted, intramolecular donors-to-acceptor energy transfer occurs during the photoinduced dynamics

within manifold {I} (see Fig. 3). This process is also reflected in the SE signal, which clearly captures the inter-state population-transfer timescales. Interestingly, the initial SE intensity at $E_{pr} \approx 2.8$ eV of the $\overline{S_{int,\parallel}}$ signal (Fig. 4) is higher than that of the $\overline{S_{int,\perp}}$ signal (Fig. 5). However, this trend reverses for $E_{pr} \approx 2.2$ eV at longer times. Despite this, the SE contribution at $E_{pr} \approx 2.8$ eV persists somewhat longer in the $\overline{S_{int,\parallel}}$ signal compared to the $\overline{S_{int,\perp}}$ signal. This behavior arises from the orthogonal orientations of μ_{02} and μ_{03} relative to μ_{01}, and can be used for enhancing or suppressing specific contributions to the TA-PP signal.

The manifold {II} comprises 195 high-lying excited states that frequently intersect during dynamical simulations, making it challenging to track specific dominant states. However, we can estimate and analyze key transition energies, as the ESA maxima in the energy domain correspond to the energy gaps between states in manifolds {II} and {I}. For instance, the ESA contribution at $E_{pr} \approx 1.8$ eV primarily originates from the S_1 state, and its intensity increases as the S_1 population grows. As expected, this effect is more pronounced in $\overline{S_{int,\perp}}$ than in $\overline{S_{int,\parallel}}$. Importantly, the simulated signals align well with the experimentally observed broad ESA band spanning 620–900 nm,[13] further reinforcing the accuracy of our theoretical predictions. In principle, both the SE and ESA signals contain information about the photoinduced nuclear wavepacket dynamics in manifold {I}, but they do so through different "spectacle" states onto which this wavepacket motion is promoted: SE projects the wavepacket motion onto the electronic ground state, whereas ESA projects it onto the high-lying states of manifold {II}. Hence, the ESA signal at $E_{pr} \approx 2.4$ eV and the SE signal at $E_{pr} \approx 2.2$ eV appear qualitatively similar, as both are shaped by the same wavepacket dynamics. On the other hand, the ESA signal at $E_{pr} \approx 1.8$ eV and the SE signal at $E_{pr} \approx 2.8$ eV show qualitatively different behavior, due to the fact that manifold {II} contains many states which are optically allowed from manifold {I}. Fortunately, the rise of intensity of the $E_{pr} \approx 1.8$ eV ESA signal and the loss of intensity of the $E_{pr} \approx 2.8$ eV SE signal, are both driven by the same underlying process: the internal conversion from S_2 to S_1. These observations illustrate how different spectroscopic features can be interconnected and used to infer the same underlying excited-state dynamics through complementary perspectives.

In the frequency domain, the total signals are dominated by ESA at lower E_{pr} and by the GSB + SE at higher E_{pr}. At short times (<300 fs), the S_2 contribution is more intense in $\overline{S_{int,\parallel}}$ (Fig. 4) compared to that in $\overline{S_{int,\perp}}$ (Fig. 5). At longer times, the S_1 state signatures become more pronounced in $\overline{S_{int,\perp}}$. As explained above, this effect is attributed to the transition dipole moment reorientations in the S_1 state. Importantly, while the $S_3 \rightarrow S_2$ and $S_2 \rightarrow S_1$ transitions are clearly visible in the SE signal, they become obscured in the total TA-PP signal due to the dominant GSB contribution masking the weaker SE features. However, as discussed above, information about the $S_2 \rightarrow S_1$ internal conversion can be readily extracted from the ESA signal centered around $E_{pr} \approx 1.8$ eV, which is well separated spectrally in the total TA-PP spectrum. This spectral separation allows for selective monitoring of excited-state population dynamics,

indicating the value of ESA as a sensitive probe of nonadiabatic transitions when GSB and SE signals overlap spectrally.

To compare our simulations with the experimental TA-PP spectra reported in ref. 13 and Fig. 6(a) shows the total TA-PP spectrum, $\overline{S_{int,M}}(t, E_{pr})$, evaluated at the magic angle between pump- and probe-pulse polarizations. This orientation averages out anisotropic contributions and provides a spectrum that is qualitatively similar to both $\overline{S_{int,\parallel}}(t, E_{pr})$ and $\overline{S_{int,\perp}}(t, E_{pr})$. For deeper analysis, we focus on spectral cuts presented in Fig. 6(b). The experimental TA-PP spectra from ref. 13 exhibit negative bands in the range of approximately 460–620 nm ($\sim$2.0–2.7 eV). ESI Fig. S5† displays individual contributions from GSB, SE, and ESA. The band around 510 nm is attributed to GSB, while the one around 580 nm corresponds to SE. Wavelengths longer than 620 nm are predominantly assigned to ESA signals. Our simulations (Fig. 6(b)) successfully reproduce the overall shape and key features of the experimental spectra (Fig. 6(c)). However, some differences are apparent, with the most significant discrepancy being the signal intensity at wavelengths longer than 700 nm, where the simulated ESA signal deviates more substantially from the experiment. This indicates that while the simulated GSB and SE components show strong agreement with experiment, the ESA signals show stronger deviations being more sensitive to the lower accuracy of calculated higher-lying excited states, besides the missing of double excitations in the current method. This direct comparison with experiments, shown in Fig. 6(b and c), evidence the faster relaxation observed in our simulations ($\sim$0.5 ps) with respect to
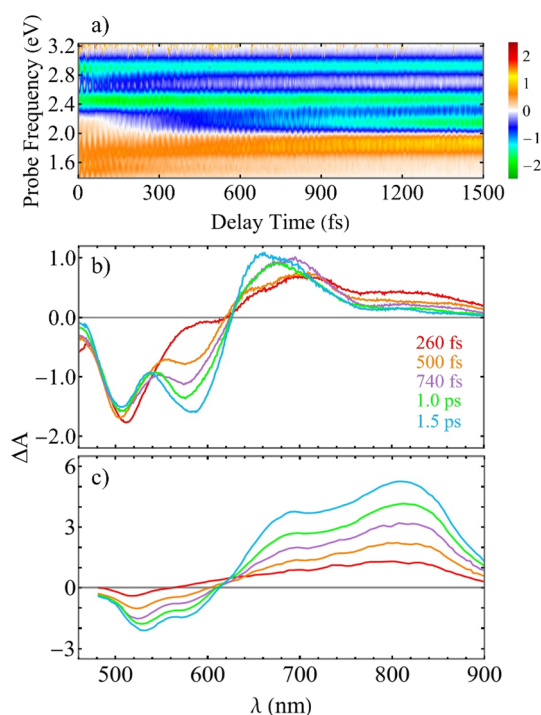

Fig. 6 (a) The total TA-PP spectrum $\overline{S_{int,M}}(t, E_{pr})$ evaluated at the magic angle (54.7°) between polarizations of the pump and probe pulses ($s_{pu}s_{pr} = 1/\sqrt{3}$), (b) simulated and (c) experimental[13] spectral cuts at selected delay times t indicated in panel (b).

experiments (1.16 ps), previously discussed in the fitting of the population rise of S_1 state to a single exponential shown in Fig. 2. This indicates that while the simulated GSB and SE components show strong agreement with experiment, the ESA signals show stronger deviations being more sensitive to the lower accuracy of calculated higher-lying excited states. Additionally, the present methodology does not address electronic excitations that have correlated nature such as double excitations. This direct comparison with experiments, shown in Fig. 6(b and c), evidence the faster relaxation observed in our simulations ($\sim$0.5 ps) with respect to experiments (1.16 ps), previously discussed in the fitting of the population rise of S_1 state to a single exponential shown in Fig. 2. We note that calculated non-radiative decay rate is extremely sensitive to the values of gaps between states[61] so that this disagreement is expected.

At this point it is interesting to mention that our non-adiabatic molecular dynamics simulations address non-radiative decay between S_3/S_2 and S_1 excited states. These states are separated by about 0.5 eV gap in the ground state conformations (see absorption spectrum in Fig. 1(c)). As a result, we do not see frequent direct crossing between PES between these states. Subsequently, the calculated no-radiative decay rate is still ultrafast, about 0.5 ps (Fig. 2), as reflected in TA-PP spectra (Fig. 4 and 5) in agreement with experiment (Fig. 6(c)) and in line with typical internal conversion rates in molecules.

A deeper understanding of the microscopic origin of the TA-PP signal can be gained by analyzing the individual contributions from the direct $D_a \rightarrow A$ and indirect $D_a \rightarrow D_b \rightarrow A$ energy transfer pathways. Fig. 7 and ESI S6† show the SE spectra evaluated using trajectories corresponding to each of these distinct pathways. The direct $D_a \rightarrow A$ pathway leads to a considerably faster decrease of the SE signal at $E_{pr} \approx 2.8$ eV

during the first $\sim$100 fs, followed by an increase of the signal at $E_{pr} \approx 2.2$ eV (Fig. 6(a)). In contrast, the SE signal produced by the trajectories following the indirect $D_a \rightarrow D_b \rightarrow A$ pathway experience this spectral shift at longer times, beyond 300 fs (Fig. 6(b)). This delay manifests the additional step of exciton relocalization on the second donor unit before reaching the acceptor. The total SE signal (Fig. 6(c)) is a superposition of these two distinct relaxation mechanisms. Furthermore, ESI Fig. S6† shows that the SE signals produced by the two pathways have markedly different spectral shapes at various delay times. These differences reflect the moving nonadiabatic nuclear wavepacket within manifold {I} across different potential energy surfaces associated with excited states. This analysis illustrates the pathway-dependent nature of the excited-state dynamics and emphasizes the importance of nonadiabatic nuclear wave-packet motion in shaping the time-resolved spectroscopic response.

3 Conclusions

This study presents a computational investigation of photoinduced donor-to-acceptor energy transfer in the D2A2 antenna system, which is composed of two naphthalene monoimide donors linked to a perylene-derived acceptor, using atomistic nonadiabatic excited-state molecular dynamics simulations. The system's high structural flexibility, driven by thermal fluctuations, combined with the weak electronic coupling between chromophores, results in transient exciton localization on individual chromophore units. Consequently, photoexcitation to different excited states leads to exciton confinement on a specific chromophore, establishing localized initial conditions for subsequent energy transfer dynamics.

Our analysis identifies two distinct energy transfer pathways that define internal conversion in the D2A2 system. The first is a faster and more efficient direct $D_a \rightarrow A$ pathway, where the exciton initially localizes on donor D_a and subsequently transfers directly to the acceptor. The second is a slower indirect $D_a \rightarrow D_b \rightarrow A$ pathway, which involves transient exciton localization on the secondary donor unit D_b before ultimately reaching the acceptor. These pathways operate at different relaxation rates, and their relative contributions significantly affect the shape and evolution of the simulated TA-PP spectra. Information about the dynamics and efficiencies of each pathway can be extracted from the spectral features, offering powerful means to decode exciton migration mechanisms from time-resolved spectroscopic measurements.

Overall, our simulations demonstrate a fast and efficient donor-to-acceptor energy transfer in the D2A2 antenna, under-scoring its potential for emerging solar energy conversion technologies. The ability of these systems to rapidly and effectively funnel excitation energy toward the acceptor site minimizes energy losses and maximizes light-harvesting efficiency, showing promises for solar-to-electric and solar-to-fuel applications. The presence of well-defined energy transfer pathways and ultrafast internal conversion dynamics suggests that such architectures could be integrated into artificial photosynthetic systems or photovoltaic devices, enhancing light absorption,
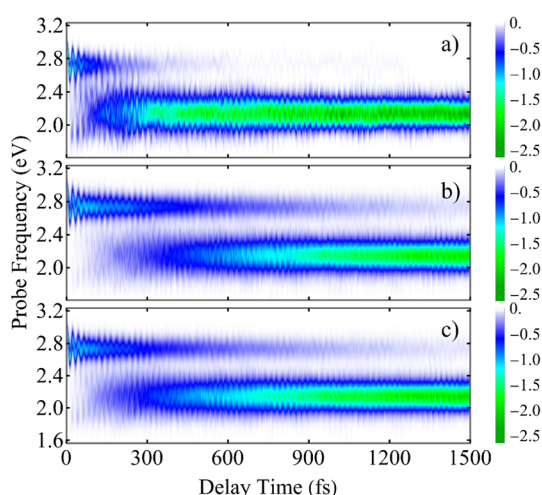

Fig. 7 The SE contribution to the TA-PP signal $\overline{S_{int,M}}(t, E_{pr})$ plotted as a function of the delay time t between the pump and probe pulses and the probe pulse frequency E_{pr}. The data is averaged over different sets of trajectories corresponding to (a) the direct $D_a \rightarrow A$ energy transfer pathway, (b) the indirect $D_a \rightarrow D_b \rightarrow A$ energy transfer pathway, and (c) the entire ensemble of trajectories.

charge separation, and energy conversion. Furthermore, the tunability of their structural and electronic properties opens avenues for optimizing their performance under different environmental conditions.

We would like to conclude with a remark on the accuracy and reliability of the on-the-fly simulation methodologies. Nowadays, there is a surging interest in benchmarking trajectory-based nonadiabatic molecular dynamics simulation protocols against their fully quantum-mechanical analogs using carefully selected model systems.[62] In this broader context, the comparison between experimental and simulated spectroscopic signals offers an additional, highly valuable opportunity for validation of theoretical approaches. In the present work, our simulation methodology has shown good agreement with experimental observations, particularly in reproducing key features of the TA-PP spectra. This outcome suggests the robustness and predictive power of our NEXMD techniques and supports the application of this code to realistic, complex photoactive systems. We show that atomistic on-the-fly non-adiabatic excited-state molecular dynamics provides a powerful and complementary to experiment approach for investigating multichromophoric and even supramolecular conjugated systems and polymers of relatively large size. This method enables a deeper understanding of excited-state behavior and can effectively disentangle distinct energy transfer pathways, such as long-range *versus* short-range transfer, thus providing valuable insights into the fundamental mechanisms governing these complex systems.

4 Methods

The photoinduced excited-state molecular dynamics in the D2A2 antenna system, depicted in Fig. 1(a), has been simulated using Non-adiabatic EXcited state Molecular Dynamics (NEXMD) software.[29,31] This code is designed for on-the-fly simulations of non-adiabatic photoexcited dynamics in multichromophoric molecular systems, enabling the treatment of multiple coupled electronic states *via* a range of hybrid quantum-classical approaches. In this study, we employ Tully's Fewest Switches Surface Hopping (FSSH) algorithm.[63] As implemented in NEXMD, the excited-state energies, energy gradients and non-adiabatic coupling terms are computed using configuration interaction singles (CIS) approach and the semiempirical Austin Model 1 (AM1) Hamiltonian model.[64] NEXMD has been successfully applied in previous studies to simulate light-induced dynamics in various light-harvesting antenna systems, proving its utility in modeling photoexcited energy relaxation, exciton dynamics, and energy transfer mechanisms in complex molecules.[34,36,51,65–68]

Within the NEXMD framework, spatial exciton localization is evaluated using the fraction of the transition density $\rho^{0\alpha}$, which represents the contribution of the ground-to-excited state α transition density that is localized on each chromophore. It is formally expressed as:

$$\delta_{\mathrm{X}}^{\alpha}(t) = \left(\rho^{0\alpha}(t)\right)_{\mathrm{X}}^{2} = \sum_{n_{\mathrm{A}}} \left(\rho^{0\alpha}(t)\right)_{n_{\mathrm{A}}n_{\mathrm{A}}}^{2}, \quad (1)$$

where the index n_{A} runs over all the atomic orbitals of atoms belonging to the chromophore X.

Our excited-state simulations are performed using initial conditions sampled from a 1 ns equilibrated ground-state molecular dynamics simulation of the dendrimer at room temperature ($T = 300$ K), using a Langevin thermostat with a friction coefficient of $\gamma = 20.0$ ps^{-1}. The subsequent nonadiabatic excited-state dynamical simulations are carried out under constant energy (microcanonical) conditions, during which 500 individual excited-state trajectories are propagated. For each trajectory, the initially (subscript "in") populated excited state α is selected based on a positively defined doorway function,[45]

$$\mathcal{D}_{\mathrm{in}}\left(\boldsymbol{R}_0, \ \boldsymbol{P}_0, E_{\mathrm{pu}}\right) = \mathcal{E}_{\mathrm{pu}}^{2}\left(E_{\mathrm{pu}} - E_{0\alpha}(R_0)\right)\left|\boldsymbol{\mu}_{0\alpha}(\boldsymbol{R}_0)\right|^{2} \quad (2)$$

which is proportional to the probability of excitation of the molecular system with the pump pulse. Here

$$\mathcal{E}_{\mathrm{pu}}\left(E_{\mathrm{pu}} - E_{0\alpha}(\boldsymbol{R}_0)\right) = \exp\left[-2\pi^2\sigma^2\left(E_{\mathrm{pu}} - E_{0\alpha}(\boldsymbol{R}_0)\right)^2\right] \quad (3)$$

where $\mathcal{E}_{\mathrm{pu}}(\omega)$ and E_{pu} represent the spectral profile and the carrier frequency of the pump pulse, respectively, and $E_{0\alpha}$ is the energy of the αth state with respect to the ground state. A total of 200 excited states are included to simulate TA-PP signals, capturing a broad range of electronic transitions. The pump pulse is centered at the absorption spectrum maximum, $E_{\mathrm{pu}} = 427$ nm (2.9 eV), see Fig. 1(c). In the time domain, its time profile follows a Gaussian envelope, $\mathcal{E}_{\mathrm{pu}}(t) = \exp(-t^2/2\sigma^2)$, where $\sigma = 42.5$ fs corresponds to a Full Width at Half Maximum (FWHM) of 100 fs. For classical nuclear trajectory propagation, time steps of 0.5 and 0.1 fs are used in the ground state and excited state simulations, respectively. A quantum time step of 0.025 fs is selected to propagate the electronic coefficients in the time-dependent Schrodinger equation. Further technical details on the treatments of decoherence and handling trivial unavoided crossings, as well as the overall theoretical framework, implementation, and testing parameters of the NEXMD package can be found elsewhere.[29,31]

The details of the TA-PP simulation have been previously described in ref. 51. Here, we provide a brief summary of this approach. Our simulations follow the DW simulation protocol,[44,45] which assumes that the integral TA-PP can be evaluated using (semi)classical trajectories. This methodology also incorporates orientational averaging and polarization-sensitive detection of TA-PP signals.[49,51] Thus, we evaluate the partial TA-PP signals $S_{\mathrm{int}}^{(abcd)}(t,E_{\mathrm{pr}})$, where $a, b, c, d = x, y, z$ specify the corresponding components of the transition dipole moments interacting with the pump (a, b) and probe (c, d) pulses in an arbitrary reference frame. E_{pr} denotes the probe pulse carrier frequency.

According to the DW simulation protocol, the partial TA-PP signals are computed as

$$
\begin{aligned}
S_{\mathrm{int}}^{(abcd)}\left(t, E_{\mathrm{pr}}\right) \sim \Big\langle & \mathcal{D}^{(ab)}(\boldsymbol{R}_0)\Big(W_0^{\mathrm{int}(cd)}\left(\boldsymbol{R}_0(t), \boldsymbol{P}_0(t), E_{\mathrm{pr}}\right) \\
& + W_{\mathrm{I}}^{\mathrm{int}(cd)}\left(\boldsymbol{R}_\alpha(t), \boldsymbol{P}_\alpha(t), E_{\mathrm{pr}}\right) \\
& - W_{\mathrm{II}}^{\mathrm{int}(cd)}\left(\boldsymbol{R}_\alpha(t), \boldsymbol{P}_\alpha(t), E_{\mathrm{pr}}\right)\Big)\Big\rangle
\end{aligned}
\quad (4)
$$

In eqn (4), the three contributing terms correspond to ground state bleach (GSB), stimulated emission (SE), and excited-state absorption (ESA). The angular brackets denote averaging over quasi-classical trajectories sampled from the doorway function in eqn (2). The tensor DW functions are defined as follows:

$$\mathcal{D}^{(ab)}(\boldsymbol{R}_0) = \frac{\boldsymbol{\mu}_{0\alpha}^{(a)}(\boldsymbol{R}_0)\boldsymbol{\mu}_{0\alpha}^{(b)}(\boldsymbol{R}_0)}{|\boldsymbol{\mu}_{0\alpha}(\boldsymbol{R}_0)|^2} \tag{5}$$

$$W_0^{\text{int}(cd)}(\boldsymbol{R}_0(t),\boldsymbol{P}_0(t),E_{\text{pr}}) = \\ \mathcal{E}_{\text{pr}}^2(E_{\text{pr}} - E_{0\alpha}(\boldsymbol{R}_0(t)))\mu_{0\alpha}^{(c)}(\boldsymbol{R}_0(t))\mu_{0\alpha}^{(d)}(\boldsymbol{R}_0(t)) \tag{6}$$

$$W_{\text{I}}^{\text{int}(cd)}(\boldsymbol{R}_\alpha(t),\boldsymbol{P}_\alpha(t),E_{\text{pr}}) = \\ \mathcal{E}_{\text{pr}}^2(E_{\text{pr}} - E_{0\alpha}(\boldsymbol{R}_\alpha(t)))\mu_{0\alpha}^{(c)}(\boldsymbol{R}_\alpha(t))\mu_{0\alpha}^{(d)}(\boldsymbol{R}_\alpha(t)) \tag{7}$$

$$W_{\text{II}}^{\text{int}(cd)}(\boldsymbol{R}_\alpha(t),\boldsymbol{P}_\alpha(t),E_{\text{pr}}) = \\ \mathcal{E}_{\text{pr}}^2(E_{\text{pr}} - E_{\alpha\beta}(\boldsymbol{R}_\alpha(t)))\mu_{\alpha\beta}^{(c)}(\boldsymbol{R}_\alpha(t))\mu_{\alpha\beta}^{(d)}(\boldsymbol{R}_\alpha(t)) \tag{8}$$

Here the subscripts 0 and α, β denote, respectively, the ground and excited electronic states, $\boldsymbol{R}_0, \boldsymbol{P}_0$, and $\boldsymbol{R}_\alpha(t), \boldsymbol{P}_\alpha(t)$ are nuclear positions and momenta in these states, $E_{0\alpha}(\boldsymbol{R}_0(t))$ and $E_{\alpha\beta}(\boldsymbol{R}_\alpha(t))$ are the differences between the electronic energies along trajectories. The superscripts $(a, b, c, d = x, y, z)$ denote projections of the transition dipole moments $\boldsymbol{\mu}_{0\alpha}(\boldsymbol{R}_\alpha(t))$ and $\boldsymbol{\mu}_{\alpha\beta}(\boldsymbol{R}_\alpha(t))$ on the axes of the reference frame, and $\mathcal{E}_{\text{pr}}(\omega) = \mathcal{E}_{\text{pu}}(\omega)$ is the spectrum of the probe pulse.

To maintain consistency with the initial $0 \rightarrow \alpha$ excitations (eqn (2)), $\alpha \rightarrow \beta$ excitations for the ESA contribution are selected similarly. At each time step, a β state is chosen with a weight proportional to $\mathcal{E}_{\text{pr}}^2(E_{\text{pr}} - E_{\alpha\beta}(\boldsymbol{R}_\alpha))|\boldsymbol{\mu}_{\alpha\beta}(\boldsymbol{R}_0)|^2$.

After computing the partial $S_{\text{int}}^{(abcd)}(t,E_{\text{pr}})$ components, the orientationally-averaged TA-PP signal can be evaluated as

$$\overline{S_{\text{int}}(t, E_{\text{pr}})} = \frac{1}{15}\left(1 + 2(\boldsymbol{s}_{\text{pu}}\boldsymbol{s}_{\text{pr}})^2\right)\left(S_{\text{int}}^{(xxxx)} + S_{\text{int}}^{(yyyy)} + S_{\text{int}}^{(zzzz)}\right) + \frac{1}{15}\left(2 - (\boldsymbol{s}_{\text{pu}}\boldsymbol{s}_{\text{pr}})^2\right)\left(S_{\text{int}}^{(yyxx)} + S_{\text{int}}^{(zzxx)} + S_{\text{int}}^{(xxyy)} + S_{\text{int}}^{(zzyy)} + S_{\text{int}}^{(xxzz)} + S_{\text{int}}^{(yyzz)}\right) \\ + \frac{2}{15}\left(3(\boldsymbol{s}_{\text{pu}}\boldsymbol{s}_{\text{pr}})^2 - 1\right)\left(S_{\text{int}}^{(yxyx)} + S_{\text{int}}^{(zxzx)} + S_{\text{int}}^{(zyzy)}\right) \tag{9}$$

where $\boldsymbol{s}_{\text{pu}}$ and $\boldsymbol{s}_{\text{pr}}$ are the unit vectors along linear polarizations of the pump and probe pulses, respectively. For brevity, the explicit dependence of $S_{\text{int}}^{(abcd)}$ on t and E_{pr} is omitted. In this way, we examine three specific polarization configurations: $\boldsymbol{s}_{\text{pu}}\|\boldsymbol{s}_{\text{pr}}$ with $\boldsymbol{s}_{\text{pu}}\boldsymbol{s}_{\text{pr}} = 1$, $\boldsymbol{s}_{\text{pu}}\perp\boldsymbol{s}_{\text{pr}}$ with $\boldsymbol{s}_{\text{pu}}\boldsymbol{s}_{\text{pr}} = 0$, and the magic angle condition where $\boldsymbol{s}_{\text{pu}}\boldsymbol{s}_{\text{pr}} = 1/\sqrt{3}$. The corresponding signals are denoted as $\overline{S_{\text{int},\|}(t, E_{\text{pr}})}$, $\overline{S_{\text{int},\perp}(t, E_{\text{pr}})}$, and $\overline{S_{\text{int},M}(t, E_{\text{pr}})}$, where the subscript M represent the magic angle. These signals satisfy the relation $\overline{S_{\text{int},\|}(t, E_{\text{pr}})} + 2\overline{S_{\text{int},\perp}(t, E_{\text{pr}})} = 3\overline{S_{\text{int},M}(t, E_{\text{pr}})}$.

Data availability

All study data are included in the article and/or ESI.†

Author contributions

R. P.-C. performed the non-adiabatic simulations and calculated and analyzed the TA-PP signals. V. M. F. helped in derived, computing and analyzing the TA-PP signals and supervised the project. A. M.-M., and L. U.-P. contributed to write the manuscript. S. T. contributed wrote the manuscript and supervised the project. M. F. G. derived, supervised the calculation and analysis of the TA-PP signals and contributed to write the manuscript. S. F.-A. designed and supervised the project and wrote the manuscript.

Conflicts of interest

There are no conflicts to declare.

Acknowledgements

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