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# Above-room-temperature strain-stable half-metallic phase owing to a high thermoelectric response in $\text{CaCu}_3\text{Cr}_2\text{Re}_2\text{O}_{12}\uparrow$

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We present the electronic, magnetic, and thermoelectric properties of the  $\text{CaCu}_3\text{Cr}_2\text{Re}_2\text{O}_{12}$  quadruple double perovskite oxide (QDPO) using *ab initio* calculations. Strong antiferromagnetic interactions between  $\text{Cu}^{2+}\uparrow\text{Cr}^{3+}\uparrow\text{Re}^{5+}\downarrow$  result in a ferrimagnetic (FiM) ground state. A half-metallic (HM) state is evident with a finite energy gap ( $E_g$ ) of 1.62 eV in the spin-majority channel ( $N^\uparrow$ ), which is large enough to ensure a long mean free path for spin and prevent spin-flipping with a colossal spin-filtering ability. Due to a significant  $E_g$  in  $N^\uparrow$ , the system displays a high figure of merit (0.76) at 300 K. The calculated spin moments of  $+0.48/+2.55/-0.92 \mu_B$  and spin-magnetization densities on the Cu/Cr/Re further verify the FiM state. The magnetic phase transition yields a Curie temperature ( $T_C$ ) of 340 K, which is below the experimental value (360 K). Because thermal energy near  $T_C$  disrupts the magnetic ordering, magnetization is consequently reduced, which is also reflected in the susceptibility curve. Additionally, the FiM state of the structure was confirmed under modulated applied magnetic fields. Finally, the HM FiM state is also verified under a moderate biaxial ([110]) strain of  $\pm 5\%$ . Hence, this work provides deep insights into this QDPO, highlighting its stable HM FiM behavior, above-room-temperature  $T_C$  and high thermoelectric response, which promises potential applications in spintronics.

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## 1 Introduction

In the realm of magnetic materials fabricated at the ultra-small scale, special focus is placed on those composed of transition metals (TMs) such as Fe, Co, and Ni, along with their alloys.<sup>1</sup> One of the most promising types of magnetic materials is half-metallic (HM) compounds, such as ferromagnetic (FM) and ferrimagnetic (FiM) materials. These compounds exhibit metallic conductivity in one spin channel while behaving as semiconductors or insulators in the opposite spin channel.<sup>2</sup> This means that the electron carriers are entirely (100%) spin-polarized (SP) at the Fermi level ( $E_F$ ), producing HM magnetic motifs that are highly essential for spintronics applications, essentially enabling the manipulation and storage of information based on electron spins, such as in tunneling devices, spin transistors, and magnetic logic gates.<sup>3–9</sup> It has been observed that tunneling conduction in a spin-based trilayer essentially depends on the SP of the electrodes,<sup>10,11</sup> consequently resulting in a giant tunneling magnetoresistance (TMR), which can be utilized in high-density data storage and extremely efficient

magnetic sensors.<sup>12</sup> However, an enormous TMR ratio in trilayer devices is susceptible to temperature (temp.), and it sharply decreases with rising temp. due to a substantial reduction in SP magnitude near the magnetic transition temp. (MTT). Hence, materials that maintain maximum (100%) SP charge carriers at room temp. with an MTT > 300 K are highly beneficial for developing future high-temp. spintronic devices. The first predicted HM FM material was the NiMnSb half-Heusler alloy<sup>13</sup> followed by  $\text{CrO}_2$ <sup>14,15</sup> and  $\text{Fe}_3\text{O}_4$ <sup>16,17</sup>, which were also proposed as HM and investigated comprehensively. In this regard, perovskite oxides (POs) have become very important candidates, especially after the discovery of sizable magnetoresistance in  $\text{La}_{1-x}\text{Sr}_x\text{MnO}_3$ <sup>18</sup> and  $\text{Tl}_2\text{Mn}_2\text{O}_7$ <sup>19</sup>, further emphasizing the importance of HM structures. Similarly, double perovskite oxides (DPOs) with an ordered  $\text{A}_2\text{BB}'\text{O}_6$  form, where the B and B' ions are usually 3d and 4/5d TMs,<sup>20,21</sup> are highly beneficial for spintronic applications.<sup>22</sup> Excitingly, an HM FiM state is anticipated in the  $\text{Sr}_2\text{FeMoO}_6$  DPO, which has a metal-to-insulator transition (MIT) at 410 K and also demonstrates a large TMR ratio at room temperature. In this context, the  $\text{Fe}^{3+} 3d^5$  and  $\text{Mo}^{5+} 5d^1$  ions with  $S = \frac{5}{2}$  and  $\frac{1}{2}$  are coupled antiferromagnetically, resulting in a FiM spin-ordering (SO).<sup>3</sup> Similarly, an HM FiM behavior is observed in  $\text{Sr}_2\text{CrReO}_6$  owing to it having the highest Curie temp. ( $T_C$ ) of 635 K among the DPO family.<sup>23,24</sup> However, it is theoretically established that SP in HM DPOs such as  $\text{Sr}_2\text{FeMoO}_6$  substantially depends on temp. and cation disorder, as well as being proportional to the spin-

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magnetization of the cores.<sup>25</sup> In the past decade, numerous efforts have been dedicated to develop robust 2D FM/FiM materials with high  $T_C$ . One effective approach involves modulating the magnetism in existing 2D layered materials through post-treatment techniques, such as doping, ion or charge implantation,<sup>26,27</sup> strain engineering,<sup>28,29</sup> and defect engineering.<sup>30,31</sup> The research discovered that the stress-induced transformation of two-dimensional materials from an indirect to a direct energy gap ( $E_g$ ) significantly enhances photoluminescent (PL) efficiency, making them more suitable for optoelectronic devices.<sup>32–41</sup> Thus, novel nano-electronic and optoelectronic devices with stress-adjustable properties hold significant potential for spintronic applications. Moreover, to optimize material properties, the doping/ion implantation strategy has been explored, in which additional magnetic cations are introduced at the A-site in the DPO with a ratio of 1 to 3. This results in a new A- and B-site ordered quadruple DPO (QDPO) keeping an  $A'A_3B_2B'_2O_{12}$  form, which possesses a very high MTT and magnetization ( $M$ ). For instance, the antiferromagnetic (AFM) interaction between the magnetic cations induces a FiM state in the  $\text{CaCu}_3\text{Fe}_2\text{Re}_2\text{O}_{12}$  QDPO, which features a very high MIT of 560 K and 100% SP. In this state, the spin-majority and spin-minority channels ( $N^\uparrow$  and  $N^\downarrow$ ) exhibit nonconductive and conductive traits, respectively, along with a large total magnetic moment ( $m_t$ ) of  $8.7 \mu_B$ .<sup>42</sup> In this continuum, a newly ordered  $\text{NaCu}_3\text{Fe}_2\text{Os}_2\text{O}_{12}$  QDPO was synthesized, which exhibits an HM FiM nature with a wide energy gap ( $E_g$ ) in  $N^\uparrow$  and spin ordering of  $\text{Cu}^{2+}\uparrow\text{Fe}^{3+}\uparrow\text{Os}^{5.5+}\downarrow$ , showing a  $T_C$  above 380 K.<sup>43</sup> Combined experimental and theoretical studies demonstrate that the FiM  $\text{LaCu}_3^{2+}\text{Co}_2^{2+}\text{Re}_2^{5.5+}\text{O}_{12}$  QDPO is nearly 100% ordered with  $\text{Cu}^{2+}\uparrow\text{Fe}^{3+}\uparrow\text{Os}^{5.5+}\downarrow$  SO and a  $T_C$  of 150 K.<sup>44</sup> Wang *et al.* theoretically predicted a series of HM FiM  $\text{ACu}_3\text{Fe}_2\text{Re}_2\text{O}_{12}$  ( $A = \text{Ca}, \text{Sr}, \text{Ba}, \text{Pb}, \text{Sc}, \text{Y}, \text{La}$ ) QDPOs, where the AFM coupling between CuFe and Re is dominant.<sup>45</sup> It was established that compounds with  $A^{2+} = \text{Ca}/\text{Sr}/\text{Ba}/\text{Pb}$  and  $A^{3+} = \text{Sc}/\text{Y}/\text{La}$  ions exhibit  $T_C$  values greater than 405 K and 502 K, respectively. Similarly,  $\text{LaCu}_3\text{Fe}_2\text{Re}_2\text{O}_{12}$  is a HM material with a very large  $T_C$  of 710 K, where a strong AFM coupling of  $\text{Cu}^{2+}\uparrow\text{Fe}^{3+}\uparrow\text{Os}^{4.5+}\downarrow$  results in a FiM lowest energy state.<sup>46</sup> It was also observed that the saturated total  $m_t$  of  $7.0 \mu_B$  at 710 K increases to  $8.0 \mu_B$  at 2 K. Very recently, Zhang *et al.* experimentally verified the HM FiM nature in the  $\text{CaCu}_3\text{Cr}_2\text{Re}_2\text{O}_{12}$  (CCCRO) system, maintaining a spin ordering of  $\text{Cu}^{2+}\uparrow\text{Cr}^{3+}\uparrow\text{Re}^{5+}\downarrow$  above room temp. (360 K).<sup>47</sup> However, in this stable charge configuration, the calculated  $m_t$  of  $5.0 \mu_B$  is significantly greater than the experimentally measured value of  $1.6 \mu_B$  per f.u. Therefore, the intriguing features of this new class of materials, as outlined above, motivate us to explore the different characteristics of the recently synthesized CCCRO QDPO through density functional theory (DFT) calculations. These calculations demonstrate a FiM spin ordering, accompanied by a  $m_t$  of  $5.0 \mu_B$  per formula unit (f.u.), and a half-metallic nature, featuring a 1.62 eV gap in the  $N^\uparrow$  channel. This results in a high  $T_C$  of 340 K. The material shows metallic behavior in the  $N^\downarrow$  channel, with a p-type thermoelectric (TE) response. Moreover, the HM phase of the system remains stable

under biaxial strain, and the material exhibits promising TE and catalytic properties, making it a strong candidate for future device applications. Finally, this paper aims to develop a theory of the magnetization process for CCCRO QDPO-based ultra-thin spin valves, which have proven to be effective as high-temperature storage devices.

## 2 Computational details

To study the physical aspects of the considered material, DFT calculations were performed within the framework of the full-potential linearized augmented plane-wave (FP-LAPW) method as implemented in the WIEN2k code.<sup>48</sup> The generalized gradient approximation (GGA)<sup>49</sup> was used for the exchange–correlation function along with the Hubbard parameter ( $U$ ) of 4.0, 3.5, and 2.4 eV for the Cu 3d, Cr 3d, and Re 5d orbitals, respectively, to account for correlation effects.<sup>50</sup> Additionally, spin–orbit coupling (SOC) effects were included in the scalar relativistic form due to the presence of a heavy Re element. Inside the atomic sphere,  $l_{\text{max}} = 12$  was set as an upper limit, and the plane-wave cutoff was chosen as  $R_{\text{mt}} \times K_{\text{max}} = 7$  and  $G_{\text{max}} = 24$ . The  $K_{\text{max}}$  was chosen to ensure no charge leakage occurred and the total energy converged. A  $10 \times 10 \times 10$   $k$ -mesh was used, generating 76 points within the full Brillouin zone, sufficient for energy convergence. Moreover, the energy convergence as a function of the  $k$ -grid has been checked carefully, as shown in Fig. 1S of the ESI.† This clearly displays that the chosen  $k$ -point grid is large enough for the energy convergence. The atomic positions were fully relaxed until the atomic forces reached  $\sim 5$  mRy per a.u. Self-consistency was ensured by total energy ( $E_t$ ) and charge convergence criteria of  $10^{-5}$  Ry and  $10^{-4}$  C, respectively. Furthermore,  $T_C$  calculations were carried out using the Vampire code.<sup>51</sup> To perform the calculations, first, the experimental atomic sites are fully relaxed until the charge and forces converged to a minimum criterion mentioned above. After that, the Self-Consistent Field method is used to converge the  $E_t$  up to five decimal places, which is a very high metric to accurately described the electronic structure of the compound.

## 3 Results and discussion

The crystal diagrams of the A–B site ordered CCCRO QDPO are shown in Fig. 1, with different magnetic orderings (unconstrained system), exhibiting the space group  $Pn\bar{3}$  (No. 201).<sup>47</sup> The experimentally observed lattice constants of  $a = b = c = 7.4152 \text{ \AA}$ <sup>47</sup> were used for the present study and our DFT calculated value of  $7.4097 \text{ \AA}$  is in excellent agreement with the experiment. The Wyckoff positions for Ca, Cu, Cr, Re, and O ions are  $2a(0.25, 0.25, 0.25)$ ,  $6d(0.25, 0.75, 0.75)$ ,  $4b(0, 0, 0)$ ,  $4c(0.5, 0.5, 0.5)$ , and  $24h(0.5583, 0.7559, 0.0662)$ , respectively. First, we investigated the magnetically stable state of the system by considering four possible spin orderings (SOs): FM ( $\text{Cu}^{2+}\uparrow, \text{Cr}^{3+}\uparrow, \text{Re}^{5+}\uparrow$ ), FiM-1 ( $\text{Cu}^{2+}\uparrow, \text{Cr}^{3+}\uparrow, \text{Re}^{5+}\downarrow$ ), FiM-II ( $\text{Cu}^{2+}\downarrow, \text{Cr}^{3+}\uparrow, \text{Re}^{5+}\downarrow$ ), and FiM-III ( $\text{Cu}^{2+}\downarrow, \text{Cr}^{3+}\uparrow, \text{Re}^{5+}\uparrow$ ), as displayed in Fig. 1(a–d), respectively. In the case of the FM SO, the spins of all magnetic ions are aligned in the same direction (see Fig. 1(a)).



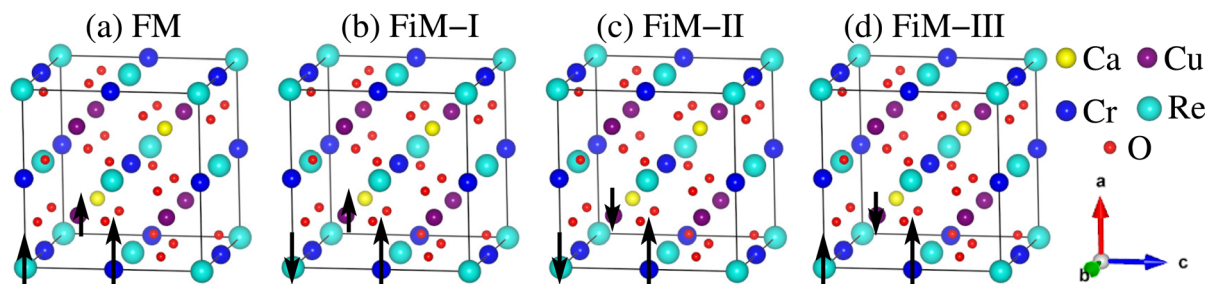


Fig. 1 Crystal structures of the  $\text{CaCu}_3\text{Cr}_2\text{Re}_2\text{O}_{12}$  quadruple structure in a (a) ferromagnetic (FM), (b) ferrimagnetic (FiM)-I, (c) FiM-II, and (d) FiM-III spin ordering.

However, in FiM-1 SO, the Cu and Cr spins are parallel to each other, but anti-parallel to that of Re (see Fig. 1(b)). For FiM-II SO, the Cu and Re spins are aligned with each other but anti-aligned to that of Cr (see Fig. 1(c)). Finally, in FiM-III SO, the spins of Cr and Re are aligned in the same direction as each other, whereas they are anti-aligned with the Cu spin (see Fig. 1(d)). Henceforth, the  $\text{Cu}^{2+}\uparrow\text{Cr}^{3+}\uparrow\text{Re}^{5+}\downarrow$  (FiM-1) configuration is the lowest energy state with energy differences of  $-105/-78/-55$  meV to the FM/FiM-II/FiM-III SO. This state has a  $m_t$  of  $5.0 \mu_B$  per f.u., which is in excellent agreement with recent experimental observations.<sup>47</sup> Notably, the lengths of the arrows in the figures represent the magnitude of each atom's spin magnetic moment ( $m_s$ ). Next, we studied the structural stability of the CCCRO material in its stable FiM-I phase by calculating the formation and cohesive energies ( $E_{\text{for.}}$  and  $E_{\text{coh.}}$ ) as:

$$E_{\text{for.}} = E_t^{\text{CaCu}_3\text{Cr}_2\text{Re}_2\text{O}_{12}} - E_{\text{Ca}}^{\text{bulk}} - 3E_{\text{Cu}}^{\text{bulk}} - 2E_{\text{Cr}}^{\text{bulk}} - 2E_{\text{Re}}^{\text{bulk}} - \frac{12}{2}E_{\text{O}_2}^{\text{bulk}}, \quad (1)$$

$$E_{\text{coh.}} = E_t^{\text{CaCu}_3\text{Cr}_2\text{Re}_2\text{O}_{12}} - E_{\text{Ca}}^{\text{iso.}} - 3E_{\text{Cu}}^{\text{iso.}} - 2E_{\text{Cr}}^{\text{iso.}} - 2E_{\text{Re}}^{\text{iso.}} - \frac{12}{2}E_{\text{O}_2}^{\text{iso.}}, \quad (2)$$

where  $E_t^{\text{CaCu}_3\text{Cr}_2\text{Re}_2\text{O}_{12}}$  is the DFT-computed  $E_t$  of the CCCRO structure, while  $E_{\text{Ca}}^{\text{bulk}}$ ,  $E_{\text{Cu}}^{\text{bulk}}$ ,  $E_{\text{Cr}}^{\text{bulk}}$ ,  $E_{\text{Re}}^{\text{bulk}}$ , and  $E_{\text{O}_2}^{\text{bulk}}$  are the DFT-determined  $E_t$  for the Ca, Cu, Cr and Re ions and O molecules in their bulk stable phases, respectively. Similarly,  $E_{\text{Ca}}^{\text{iso.}}$ ,  $E_{\text{Cu}}^{\text{iso.}}$ ,  $E_{\text{Cr}}^{\text{iso.}}$ ,  $E_{\text{Re}}^{\text{iso.}}$ , and  $E_{\text{O}_2}^{\text{iso.}}$  are the DFT-measured  $E_t$  for the isolated Ca, Cu, Cr and Re ions, and oxygen molecule, accordingly. The calculated  $E_{\text{for.}}/E_{\text{coh.}}$  per atom is  $-2.31$  eV/ $-4.89$  eV. The negative signs for both energies confirm that the structure is thermodynamically stable and supports an exothermic reaction. Moreover, the mechanical stability of the structure is utilized by calculating the elastic tensors ( $C_{ij}$ ). The computed three independent elastic parameters, namely  $C_{11}$ ,  $C_{12}$ , and  $C_{44}$ , satisfied the basic demands and Born criteria as  $(C_{11} - C_{12}) > 0$ ,  $(C_{11} + 2C_{12}) > 0$ ,  $C_{11} > 0$ ,  $C_{44} > 0$ , and  $C_{12} < B < C_{11}$  (ref. 52) for the mechanical stability. Hence, the determined  $C_{11}$ , and  $C_{12}$ , and  $C_{44}$  are 289, 211, and 140, correspondingly, which satisfies the above-mentioned mechanical stability standard.

To describe the electronic structure of the CCCRO, we calculated and presented the SP total/partial density of states (TDOS/PDOS) within the GGA+ $U$  and TDOS for GGA+ $U$ +SOC methods in Fig. 2(a, a' and b), respectively. Fig. 2(a) suggests

that the system is HM within the GGA+ $U$  method with fully SP conduction electrons, which is consistent with the experimental findings.<sup>47</sup> A large  $E_g$  of 1.62 eV remains in the  $N^\uparrow$  channel, and a few TDOS states appear at the Fermi level ( $E_F$ ) in  $N^\downarrow$ , leading to a metallic behavior of  $N^\downarrow$ . Consequently, the entire system illustrates an HM phase. The broad  $E_g$  in  $N^\uparrow$  is sufficiently large to prevent spin-flipping, which helps to avoid thermal excitation of the electrons and ensures that the HM nature of the system is stable at or above room temp. to some extent. From Fig. 2(a'), we observe that only Re 5d and O 2p states (where hybridization occurs between Re 5d and O 2p states near the  $E_F$ ) cross the  $E_F$  in  $N^\downarrow$ , transitioning from the valence band (VB) to the conduction band (CB), which is responsible for the metallicity. In contrast, no ion states cross or lie at the  $E_F$  in the  $N^\uparrow$ , confirming the 100% SP at the  $E_F$ . Additionally, the GGA+ $U$ +SOC calculated TDOS (see Fig. 2(b)) exhibits the metallic behavior of the system. Furthermore, the calculated SP band structures within the GGA+ $U$  and GGA+ $U$ +SOC methods (shown in Fig. 3(a/a' and b), respectively), validate the HM and metallic nature of the structure as demonstrated by the TDOS in Fig. 2(a and b). To further confirm the HM state of the structure, we calculated the spin-

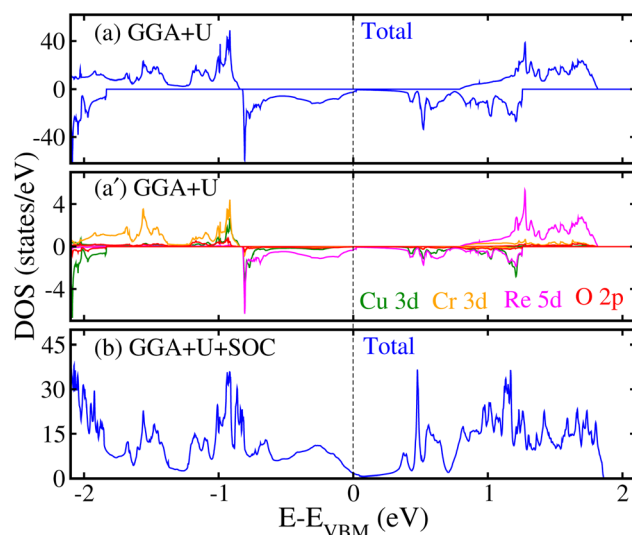


Fig. 2 Calculated spin-polarized density of states (DOS) in the  $\text{CaCu}_3\text{Cr}_2\text{Re}_2\text{O}_{12}$  quadruple structure: (a/a') total/partial DOS for the GGA+ $U$  and (b) total DOS for the GGA+ $U$ +SOC method.



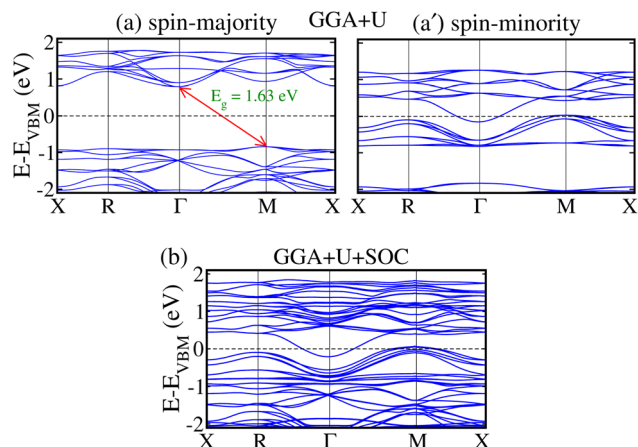


Fig. 3 Calculated spin-polarized band structures in the  $\text{CaCu}_3\text{Cr}_2\text{Re}_2\text{O}_{12}$  quadruple structure, for the (a/a') spin-majority/spin-minority channel within the GGA+ $U$  (1st-row) and (b) GGA+ $U$ +SOC (2nd-row) methods.

polarized TDOS of the system using the hybrid functional PBE0, as shown in Fig. 2S of the ESI† which is implemented in Wien2K and gives almost the same high accuracy in results as found in the case of HSE06, which is implemented in the VASP code. One can see that the calculated TDOS exhibits a HM state where  $N^\uparrow$  contains a large  $E_g$ , while  $N^\downarrow$  is showing a metallic behavior within PBE0 (see Fig. 2S of the ESI†), as predicted in the case of the GGA+ $U$  method (see Fig. 2(b)).

Next, we discuss the system's magnetism, where the energetically stable FiM-I configuration  $\text{Cu}^{2+}\uparrow\text{Cr}^{3+}\uparrow\text{Re}^{5+}\downarrow$  produces an  $m_t$  of  $5.0 \mu_B$  per f.u., which is higher than that of other spin configurations. This value is reasonable, as also mentioned in ref. 47. However, it remains considerably higher than the experimentally measured value of  $1.6 \mu_B$  per f.u.<sup>47</sup> The calculated  $m_s$  for the Cu, Cr, and Re ions within the muffin-tin sphere are  $0.48/2.54/-0.92 \mu_B$  using the GGA+ $U$  method, which changes slightly to  $0.47/2.53/-0.89 \mu_B$  upon including spin-orbit coupling (SOC). The “-” sign in the Re  $m_s$  indicates that its spin is oppositely aligned with the Cu and Cr spins, confirming the FiM state. The Cu, Cr, and Re ions are in the +2 ( $3d^9$ ), +3 ( $3d^3$ ), and +5 ( $5d^2$ ) states, respectively, holding electronic configurations of  $t_{2g}^3\uparrow t_{2g}^3\downarrow e_g^2\uparrow e_g^1\downarrow$ ,  $t_{2g}^3\uparrow t_{2g}^0\downarrow e_g^0\uparrow e_g^0\downarrow$ , and  $t_{2g}^2\uparrow t_{2g}^0\downarrow e_g^0\uparrow e_g^0\downarrow$  with spin quantum numbers  $S = \frac{1}{2}$ ,  $\frac{3}{2}$  and 1, respectively. Hence, the computed  $m_s$  on each ion also verifies their respective valence states. The induced orbital magnetic moment ( $m_{\text{orb}}$ ) on the Cu/Cr/Re ion is  $0.06/-0.05/0.23 \mu_B$ . Compared to that on the Cu and Cr, the sizable magnitude of  $m_{\text{orb}}$  on the Re ion highlights the strong SOC influence. Furthermore, as Cu lies in a more than half-occupied d state, its  $m_s$  and  $m_{\text{orb}}$  are aligned with each other (*i.e.*, both have a “+” sign), as discussed in ref. 53. Conversely, Cr and Re ions lie in less than half-filled d states, so their  $m_s$  and  $m_{\text{orb}}$  are anti-aligned. For Cr, the signs are “+/-” for  $m_s/m_{\text{orb}}$ , while for Re, they are “-/+”, as described in ref. 54. Thus, the above discussions support the AFM interactions between the Cu/Cr and Re ions.

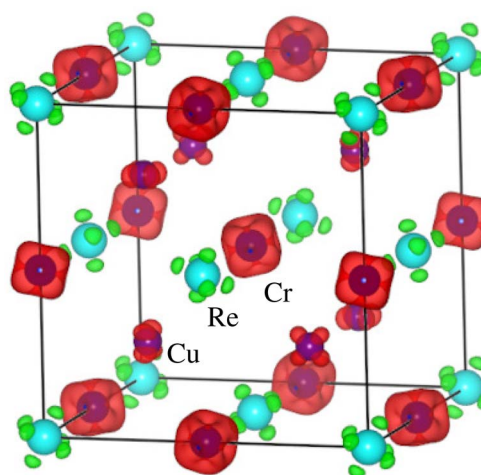


Fig. 4 Calculated three-dimensional spin-magnetization density iso-surfaces with an iso-value of  $\pm 0.005 e \text{ \AA}^{-3}$  in the  $\text{CaCu}_3\text{Cr}_2\text{Re}_2\text{O}_{12}$  quadruple structure. For simplicity, Ca and oxygen ions are omitted.

To further directly confirm the  $m_s$  magnitude on the magnetic ions and the FiM SO in the system, we visualized the three-dimensional spin-magnetization density iso-surfaces with an iso-value of  $\pm 0.005 e \text{ \AA}^{-3}$  in Fig. 4. Firstly, the high densities around the Cr ion, compared to those around the Cu and Re ones, establish that Cr is the primary contributor to the system magnetism and confirm the calculated  $m_s$  values on each ion. Secondly, the Cu and Cr density colors are the same (red), in contrast to that of Re (light green). This indicates that the Cu and Cr spins are aligned in the same direction (parallel to each other), but they are anti-aligned to the Re-spin, which further supports the FiM-I ( $\text{Cu}^{2+}\uparrow\text{Cr}^{3+}\uparrow\text{Re}^{5+}\downarrow$ ) SO. Additionally, the combined  $e_g$  and  $t_{2g}$  orbital features are evident in the Cu and Cr/Re ion densities as they occupy +2 ( $e_g^2\uparrow e_g^1\downarrow$ ) and +3 ( $t_{2g}^3\uparrow$ )/+5 ( $t_{2g}^2\uparrow$ ) states, respectively. Therefore, the AFM coupling between Cu/Cr and Re ions can be understood using the superexchange interaction concept, where the possible electron transfer between them is illustrated in Fig. 5. Since Cr and Re maintain +3 and +5 valence states, as  $t_{2g}$  states are less than half-filled in both cases (see Fig. 5), virtual hopping between these  $t_{2g}$  orbitals leads to AFM coupling, resulting in a FiM state.

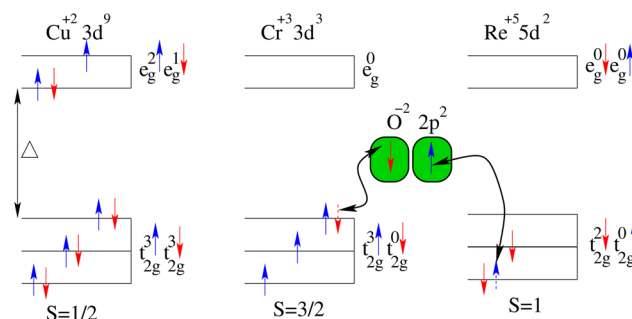


Fig. 5 Schematic representation of the antiferromagnetic superexchange coupling between  $\text{Cu}^{2+}$  ( $3d^9$ )/ $\text{Cr}^{3+}$  ( $3d^3$ ) and  $\text{Re}^{5+}$  ( $5d^2$ ) orbitals via  $\text{O}^{2-}$  ( $2p^2$ ) in the  $\text{CaCu}_3\text{Cr}_2\text{Re}_2\text{O}_{12}$  quadruple structure.



The total  $m_s$  of an atom is the result of the combined contributions from the  $m_s$  values of its electrons, including the  $m_{\text{orb}}$  component. In FiM materials, the magnetism primarily originates from the  $m_s$  of the unpaired metal ions within the crystalline lattice. Consequently, these materials display magnetic moments with spontaneous long-range ordering, driven by a quantum mechanical phenomenon called the exchange or interchange interaction. The exchange interaction, which governs SO, can be categorized into short-range (direct), long-range, or indirect exchange interactions. This interaction is characterized by the presence of two distinct sublattices, A and B, and at least three different exchange interactions:  $J_{AA}$ ,  $J_{AB}$ , and  $J_{BB}$ .<sup>55</sup> The ions in sublattice A are oriented in one direction, whereas those in sublattice B are oriented in the opposite direction. For example, the exchange interaction results from the parallel alignment of atomic  $m_s$  in FiM materials. Hence, to figure out the origin of the high  $T_C$  in the CCCRO system, the magnetic exchange couplings were computed using the Heisenberg spin method:<sup>56,57</sup>

$$H = -\sum_{\langle i,j \rangle} J_{ij} S_i S_j \quad (3)$$

Here,  $J_{ij}$  represents the interaction between the magnetic ions  $i$  and  $j$  due to exchange forces. If  $J_{ij}$  is positive ( $J_{ij} > 0$ ), an FM interaction occurs, allowing the spins to align in a parallel configuration ( $\uparrow\uparrow$ ). In contrast, if  $J_{ij}$  is negative ( $J_{ij} < 0$ ), an AFM interaction arises, resulting in an antiparallel spin alignment ( $\uparrow\downarrow$ ). FM materials exhibit the former behavior, while AFM and FiM are associated with the latter.  $S_i/S_j$  is the spin vector of the Cu/Cr/Re ion at the  $i/j$  site and represents the spin variables. For simplicity, only the three nearest neighbors  $J_{ij}$ , namely  $J_{\text{Cu-Cr}}$ ,  $J_{\text{Cu-Re}}$ , and  $J_{\text{Cr-Re}}$ , are taken into account. To do this,  $J_{ij}$  in four varying SOs, namely FM ( $\text{Cu}^{2+}\uparrow\text{Cr}^{3+}\uparrow\text{Re}^{5+}\uparrow$ ), FiM-I ( $\text{Cu}^{2+}\uparrow\text{Cr}^{3+}\uparrow\text{Re}^{5+}\downarrow$ ), FiM-II ( $\text{Cu}^{2+}\downarrow\text{Cr}^{3+}\uparrow\text{Re}^{5+}\downarrow$ ), and FiM-III ( $\text{Cu}^{2+}\downarrow\text{Cr}^{3+}\uparrow\text{Re}^{5+}\uparrow$ ), as shown in Fig. 1, is calculated as:<sup>46</sup>

$$E_t(\text{FM}) = E_0 + 12J_{\text{Cu-Cr}}S_{\text{Cu}}S_{\text{Cr}} + 12J_{\text{Cu-Re}}S_{\text{Cu}}S_{\text{Re}} + 12J_{\text{Cr-Re}}S_{\text{Cr}}S_{\text{Re}} \quad (4)$$

$$E_t(\text{FiM-I}) = E_0 + 12J_{\text{Cu-Cr}}S_{\text{Cu}}S_{\text{Cr}} - 12J_{\text{Cu-Re}}S_{\text{Cu}}S_{\text{Re}} - 12J_{\text{Cr-Re}}S_{\text{Cr}}S_{\text{Re}} \quad (5)$$

$$E_t(\text{FiM-II}) = E_0 - 12J_{\text{Cu-Cr}}S_{\text{Cu}}S_{\text{Cr}} + 12J_{\text{Cu-Re}}S_{\text{Cu}}S_{\text{Re}} - 12J_{\text{Cr-Re}}S_{\text{Cr}}S_{\text{Re}} \quad (6)$$

$$E_t(\text{FiM-III}) = E_0 - 12J_{\text{Cu-Cr}}S_{\text{Cu}}S_{\text{Cr}} - 12J_{\text{Cu-Re}}S_{\text{Cu}}S_{\text{Re}} + 12J_{\text{Cr-Re}}S_{\text{Cr}}S_{\text{Re}} \quad (7)$$

Our results show that the three considered couplings are AFM. In the case of  $\text{Cu}^{2+}\uparrow\text{Cr}^{3+}\uparrow$ ,  $J_{ij} = 0.957$  meV for the atom interactions closest to Cu-Cr and becomes  $-0.374$  meV for the second-to-nearest ones, hinting at the AFM coupling between  $\text{Cu}^{2+}\uparrow$  and  $\text{Cr}^{3+}\uparrow$ . However, the AFM  $\text{Cu}^{2+}\uparrow\text{Re}^{5+}\downarrow$  and  $\text{Cr}^{3+}\uparrow\text{Re}^{5+}\downarrow$  interactions are much stronger than those of  $\text{Cu}^{2+}\uparrow\text{Cr}^{3+}\downarrow$ , resulting in a long-ranged  $\text{Cu}^{2+}\uparrow\text{Cr}^{3+}\uparrow\text{Re}^{5+}\downarrow$  SO (FiM-I) as the lowest energy state of CCCRO. The calculated values of the AFM exchange coupling constants  $J_{\text{Cr-Re}} = -30.21$  meV and

$J_{\text{Cu-Re}} = -28.57$  meV for the interactions  $S_{\text{Cr}}\uparrow\text{Re}^{5+}\downarrow$  and  $S_{\text{Cu}}\uparrow\text{Re}^{5+}\downarrow$  are substantially higher than the 5.85 meV for  $J_{\text{Cu-Cr}}S_{\text{Cu}}\uparrow\text{Cr}^{3+}\uparrow$ . Therefore, the much stronger AFM interactions between the Cu/Cr and Re ions result in a high  $T_C = 340$  K for the system.

Magnetic materials typically form magnetic domains, regions where the magnetic moments are highly aligned, and the boundaries between the magnetic domains (domain walls) shift in the presence of an external magnetic field ( $H$ ), leading to changes in the material's  $M$ . The domain structure organizes itself to minimize the overall magnetostatic energy of the material. The domains' size, shape, and orientation are determined by the interactions between the exchange, magnetostatic, and anisotropic energies of the system. Consequently, exposure of a material to an external  $H$  induces an  $M$  within the material. The magnitude of the  $M$  is directly proportional to the applied  $H$ , as given by the relation:

$$M = \chi H$$

In this equation,  $\chi$  represents the material's magnetic susceptibility, a dimensionless quantity in SI units. The behavior of solid materials under an external  $H$  is affected by factors including their atomic structure, electromagnetic excitation, pressure, and temperature. Hence, to visualize the magnetic phase transition at  $T_C$  in the CCCRO QDPO,  $M$  versus  $T_C$  calculations have been performed (presented in Fig. 6) using the Vampire code.<sup>51,58</sup> The computed  $T_C$  is 340 K,  $\sim 7\%$  lower than the experimentally observed value of 360 K.<sup>47</sup> This discrepancy can primarily be attributed to inherent differences in computational modeling and experimental conditions. As the temp. approaches  $T_C$ , thermal energy disrupts the ordered alignment of  $m_s$ , corresponding to a sharp decrease in  $M$ . This results in a corresponding decrease in the  $m_s$  of the constituent ions due to the reduced number of unpaired d-electrons. This phase transition is critical as it signifies the loss of spontaneous  $M$  and the onset of enhanced thermal fluctuations, which can be seen in the  $\chi$  curve shape as depicted in Fig. 6. This implies some level of anisotropy within the material and the influence of opposing magnetic interactions.<sup>59</sup> Importantly, the sharp peak in  $\chi$  observed at  $T_C$  indicates the material's heightened sensitivity to  $H$  due to increased SO.

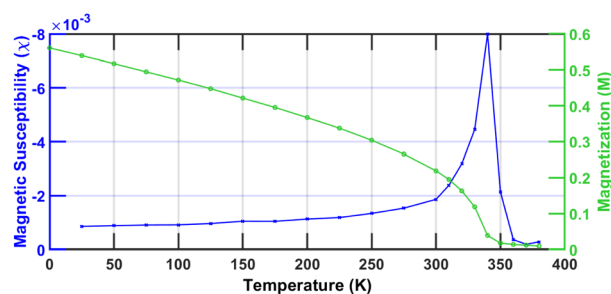


Fig. 6 Calculated susceptibility and magnetization curves versus Curie temperature of the  $\text{CaCu}_3\text{Cr}_2\text{Re}_2\text{O}_{12}$  quadruple structure.



Recently, a material which is applicable for spintronics application, contain the  $M$  process of the spin valve of HM ferrites, has been attracting deep attention.  $M$  as a function of the applied  $H$  is represented by the  $M$ - $H$  curve, which reveals the saturation  $M$  that is reached beyond a certain threshold of  $H$ . As  $H$  decreases to zero after saturation,  $M$  does not revert to zero, a behavior referred to as hysteresis. This property is critical for various applications, such as magnetic sensing devices. Therefore, the magnetic properties of CCCRO are evaluated by measuring  $M$  in terms of the applied  $H$  and temp. of 2 T/5 T and 2/100/200/300 K, respectively, as shown in Fig. 7(a) and (b). At low temp. (2 K), as shown in Fig. 7(a), the material exhibits strong SO and quickly drives the system to saturation, displaying sharp transitions in the hysteresis loop. As the temp. increases to 100 K, thermal fluctuations begin to reduce the  $M$ , however, the material still reaches a saturation, as found under 2 T (see Fig. 7(a)), though more gradually. At 5 T (see Fig. 7(b)), the material achieves saturation more effectively, but the saturated  $M$  is lower at 2 K. At higher temp. (200 K and 300 K), the material's  $M$  continues to decrease due to an increase in thermal agitation, and the transition to saturation becomes more gradual. However, the high field (5 T) still drives the material towards saturation, but the overall  $M$  is lower.

By analyzing the band structure, the material's metallic, semiconducting, or insulating nature can be inferred from its transport properties. A decrease in the Hall coefficient ( $R_H$ ) with increasing temp. suggests metallic behavior, while a Seebeck coefficient ( $S$ ) greater than zero signifies p-type semiconducting characteristics. Thus, the transport properties of the CCCRO QDPO were computed using the BoltzTraP2 software<sup>60</sup> under the constant relaxation time approximation ( $\tau = 1 \times 10^{-19}$  s). The electrical conductivity per unit relaxation time ( $\frac{\sigma}{\tau}$ ) exhibits a distinct temp. dependence due to the SP electronic structure. There is a significant increase in  $\sigma$  for non-metallic  $N^\uparrow$ , from  $3.18 \times 10^{19}$  S m<sup>-1</sup> at 300 K to  $4.0 \times 10^{19}$  S m<sup>-1</sup> at 800 K, as thermal excitation promotes electrons across the gap. In contrast,  $N^\downarrow$  shows a weaker temp. dependence, from  $2.58 \times 10^{19}$  S m<sup>-1</sup> at 300 K to  $2.80 \times 10^{19}$  S m<sup>-1</sup> at 800 K, as conductivity is primarily limited by electron-phonon scattering (see Fig. 8(a)). Initially,  $N^\uparrow$  has a higher  $S$  ( $1.92 \times 10^{-5}$  V K<sup>-1</sup>) at 300 K due to limited thermally excited carriers, while  $N^\downarrow$  exhibits a lower  $S$  ( $-2.94 \times 10^{-6}$  V K<sup>-1</sup>) at 300 K. As temp. increases (up to 800 K), the  $S$  for  $N^\uparrow$  decreases ( $-3.73 \times 10^{-6}$  V K<sup>-1</sup>) as thermal excitation saturates available states, while the  $S$  for  $N^\downarrow$

increases ( $8.66 \times 10^{-6}$  V K<sup>-1</sup>) due to enhanced carrier diffusion (Fig. 8(b)). After a certain temp.,  $S$  stabilizes for both channels, indicating saturation in the TE potential.

The thermal conductivity per unit relaxation time ( $\frac{\kappa_e}{\tau}$ ) increases linearly with temp. primarily due to phonon-electron scattering, peaking around 800 K for both channels. For  $N^\uparrow$ , the conductivity is slightly higher, with the value increasing from  $2.88 \times 10^{14}$  W m<sup>-1</sup> K at 300 K to  $1.02 \times 10^{15}$  W m<sup>-1</sup> K at 800 K (Fig. 8(c)). This difference arises from the increased availability of high-energy states in  $N^\uparrow$  due to thermal excitation across the  $E_g$ .  $N^\downarrow$ , being metallic, shows a less pronounced increase, from  $2.01 \times 10^{14}$  W m<sup>-1</sup> K at 300 K to  $6.27 \times 10^{14}$  W m<sup>-1</sup> K at 800 K, due to the relatively constant DOS at the  $E_F$ .  $\chi$  is higher for  $N^\downarrow$  than  $N^\uparrow$  at lower temp. as  $N^\downarrow$  is metallic and has a higher DOS at the  $E_F$ . At 300 K,  $\chi$  for  $N^\downarrow$  is  $1.59 \times 10^{-11}$  and decreases to  $1.57 \times 10^{-11}$  at 800 K due to thermal excitation disrupting spin alignment. For  $N^\uparrow$ ,  $\chi$  increases from  $1.35 \times 10^{-11}$  at 300 K to  $1.47 \times 10^{-11}$  at 800 K as thermal excitation promotes electrons across the  $E_g$ , allowing for stronger spin alignment. However,  $\chi$  for  $N^\uparrow$  saturates around the  $T_C$  due to phase transition effects (Fig. 8(d)). The Hall coefficient ( $R_H$ ) for  $N^\uparrow$  remains positive across this temp. range, indicating hole conduction, while for  $N^\downarrow$ , it decreases with increasing temp., signifying metallic behavior (shown in Fig. 8(e)). In  $N^\downarrow$ ,  $R_H$  decreases with temp. as thermally activated carriers dominate, signaling the metallic behavior. For  $N^\uparrow$ ,  $R_H$  increases as thermal excitation generates additional carriers, enhancing the  $R_H$ . Further, the molar specific heat capacity ( $C_V$ ) increases with temp. following the Debye Law, reflecting stronger atomic binding and activation of additional vibrational modes. Despite differing electronic properties,  $C_V$  remains nearly identical for both spin channels because it is governed primarily by phonon vibrations in the lattice, which are independent of the SP electronic structure. Finally, the thermal performance of the systems as quantified by the figure of merit,

$$(ZT) = \frac{S^2 \sigma T}{\kappa_e}$$

, is significantly higher for the  $N^\uparrow$  channel at room temp. This is due to its enhanced  $S$  and lower  $\kappa_e$ , which collectively results in improved TE performance. At ambient temp., the  $ZT$  values for  $N^\uparrow$  and  $N^\downarrow$  are 0.76 and 0.001, respectively, highlighting the superior TE efficiency of the  $N^\uparrow$  channel. This behavior is depicted in Fig. 8(f), which illustrates the temp. dependence and contrast in  $ZT$  values for the two spin channels.

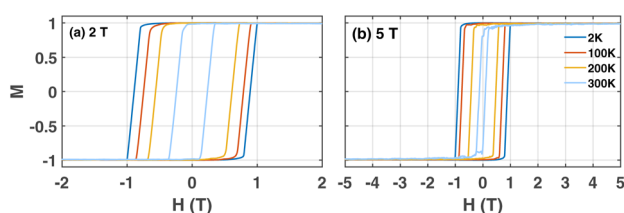


Fig. 7 Variation of the saturated magnetization ( $M$ ) with applied magnetic field ( $H$ ) for (a) 2 T and (b) 5 T at a fixed temperature of 2/100/200/300 K in the  $\text{CaCu}_3\text{Cr}_2\text{Re}_2\text{O}_{12}$  quadruple structure.

## 4 Strained system

DOS and  $E_g$  are crucial descriptors of the electronic properties of materials. The DOS represents the number of electronic states at each energy level, while the  $E_g$  refers to the energy difference between the CB and VB. Thus, the orbital hybridization between the O 2p orbitals and the Cr 3d and Cu 3d orbitals plays a central role in determining these properties. Changes in atomic distance, induced by strain, affect the overlap between these orbitals, thereby influencing the  $E_g$  and DOS



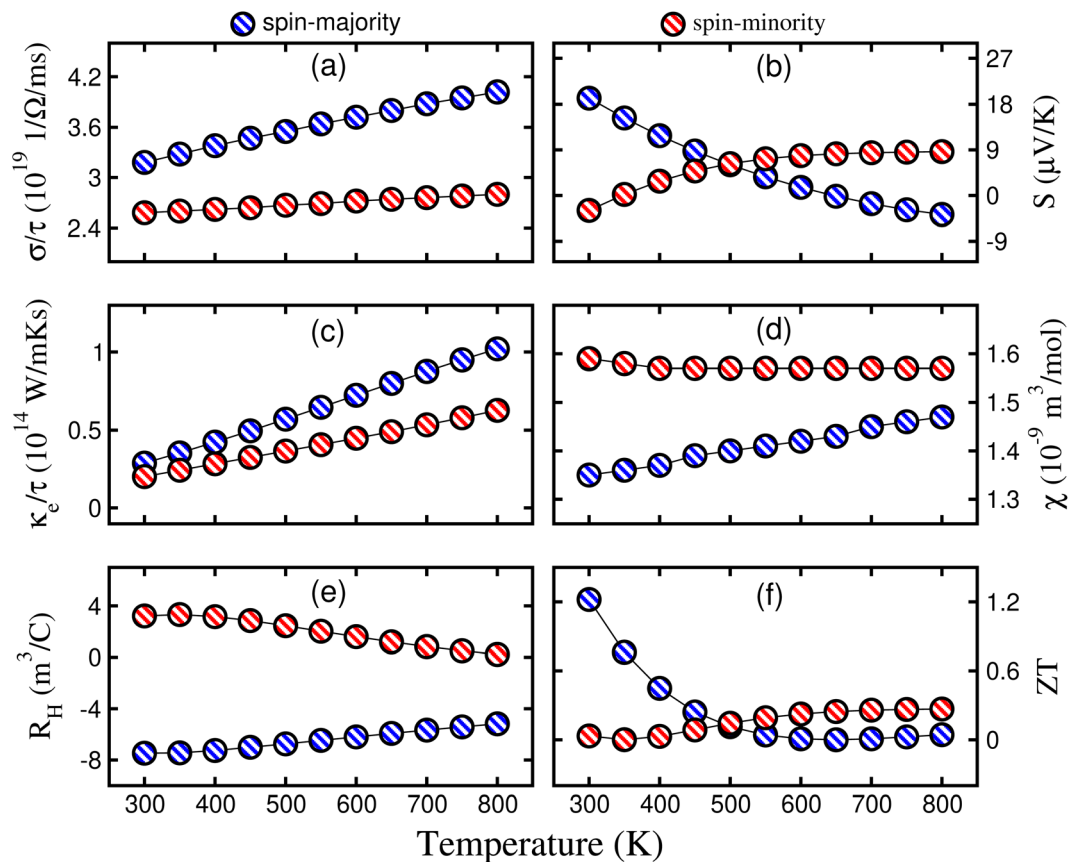


Fig. 8 Calculated (a) electrical conductivity per unit relaxation time ( $\frac{\sigma}{\tau}$ ), (b) Seebeck coefficient ( $S$ ), (c) thermal conductivity per unit relaxation time ( $\frac{\kappa_e}{\tau}$ ), (d) molar magnetic susceptibility ( $\chi$ ), (e) Hall-coefficient ( $R_H$ ), and (f) figure of merit ( $ZT$ ) of the  $\text{CaCu}_3\text{Cr}_2\text{Re}_2\text{O}_{12}$  quadruple structure.

peak height. Interatomic distances are reduced in materials under compressive (comp.) strain, leading to more substantial orbital overlap and hybridization. This typically results in a narrowing of the  $E_g$  and a reduction in the sharpness of the DOS peak. Conversely, under tensile (tens.) strain, interatomic distances are increased, which weakens orbital overlap and can lead to a widening of the  $E_g$  and a sharper DOS peak. Therefore, we perform DFT calculations to simulate the effects of comp. and tens. strain on the CCCRO QDPO. A comp. strain is applied by reducing the lattice constant, bringing the atoms closer together, and tens. strain is applied by increasing the lattice constant, causing the atoms to move farther apart. To assess the stability of the HM phase in the CCCRO QDPO, we examine the effects of biaxial ([110]) strain on the electronic and magnetic properties within a reasonable range of  $\pm 5\%$ . First, the structural robustness of the aforementioned systems is evaluated by plotting the  $E_{\text{for.}}/E_{\text{coh.}}$  in blue/red with respect to the strain, as shown in Fig. 9(a). Both quantities remain negative throughout the entire applied strain range. However, structures under comp. strain exhibit lower stability compared to those under tensile strain, as the values of  $E_{\text{for.}}/E_{\text{coh.}}$  shift toward higher (more positive) energies with increasing strain from 0% to  $-5\%$ . Next, to quantitatively analyze the variations in the electronic structure of the system resulting from strain, we display only the calculated  $E_g$  of  $N^\uparrow$  in Fig. 9(b), since  $N^\downarrow$  remains metallic across

the entire strain range considered. It is observed that  $E_g$  decreases solely from 1.62 to 1.24 eV with the varying compressive strain from 0% to  $-5\%$ . The change in  $E_g$  is mainly due to the charge re-distribution (Cu 3d, Cr 3d and O 2p) state hybridization. It is observed that the Re–Cr bond lengths are least affected for the entire strain ranges, but the Cr–Cu bond

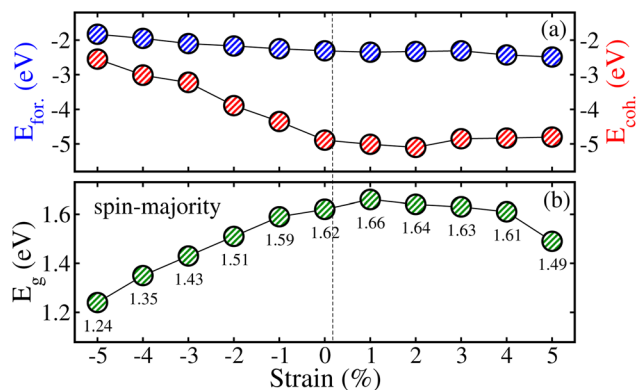


Fig. 9 Calculated (a) formation/cohesive energy ( $E_{\text{for.}}/E_{\text{coh.}}$ ) in blue/red color and (b) energy gap ( $E_g$ ) in the spin-majority channel with respect to  $\pm 5\%$  biaxial ([110]) strain in the  $\text{CaCu}_3\text{Cr}_2\text{Re}_2\text{O}_{12}$  quadruple structure.



lengths increase significantly (from 3.21 Å to 3.70 Å). This also changes the interaction forces among the ions linked with the stretched bond lengths. As a result, the energies around the  $E_F$  change (the ground state energies of the CB/VB show a decreasing/increasing trend, respectively). This causes the decrease in  $E_g$ . However, small changes were found for the cases of tensile strain compared to the ones without stress (0%).

Under comp. strain, the interatomic distances between O, Cr, and Cu atoms decrease, bringing their atomic orbitals into closer proximity. This leads to stronger orbital hybridization between the O 2p and the Cr 3d and Cu 3d orbitals. The closer proximity of the orbitals causes the electronic states to become more delocalized, reducing the band gap  $E_g$  as the conduction and valence bands move closer together. This narrowing of the  $E_g$  indicates a transition toward a more metallic or semi-conducting state. Also, the DOS peak height decreases because the increased overlap between the atomic orbitals leads to a broader distribution of electronic states near the  $E_F$ . As a result, the DOS peak becomes less sharp due to the more delocalized electronic states. As shown in Fig. 3S of the ESI,<sup>†</sup> this effect is observed for the Cr and Cu 3d states. Fig. 4S of the ESI<sup>†</sup> shows similar behavior for the O 2p states under comp. strain. In contrast, under tens. strain, the interatomic distances between the atoms increase, which causes the O 2p orbitals and Cr/Cu 3d orbitals to become more localized. This increases the distance of the O 2p orbitals from the Fermi level  $E_F$ , while the Cr and Cu 3d orbitals are pushed even further away due to decreased orbital overlap. The reason for this decrease is the increasing localization of these orbitals, which leads to a reduction in the number of available electronic states near the  $E_F$ , thus decreasing the DOS peak height. For the O 2p orbitals,

the peak height increases under tens. strain. This is because as the strain increases, the O 2p orbitals become more localized near the  $E_F$ , which increases the DOS in this region. Despite the increase in peak height for the O 2p orbitals, the total DOS does not show a significant increase under tens. strain. This is because, although the O 2p orbitals become more localized and their peak height increases, the overall distribution of electronic states remains narrow, and the states of the Cr and Cu 3d orbitals are less delocalized. Therefore, the overall DOS profile does not exhibit a significant broadening, and the peak height for the TDOS remains nearly unchanged.

For qualitative evaluation, we plotted the TDOS for various comp. and tens. strains of the motif, as shown in Fig. 10. This established the fact that  $N^\uparrow$  maintained a definite  $E_g$  value, while in  $N^\downarrow$ , states lie at the  $E_F$  for  $-1/-3/-5%$  (comp.) and  $+1/+3/+5%$  (tens.) strained systems, as shown in (Fig. 10(a-c) and 10(a')-(c')), respectively. Hence, this ensures the robustness of the HM nature of the system under the considered  $\pm 5%$  biaxial strain and maybe above it. Finally, we plotted the calculated  $m_s$  values on the Cu/Cr/Re ion as a function of strain in Fig. 11. In the case of the Cr/Re ion, a small reduction/increment in  $m_s$  magnitude is observed when comp./tens. strain is adjusted from  $-1%$  to  $-5%/+1%$  to  $+5%$ . However, it almost remains the same for the whole strain range on the Cu ion. So, an increase/decrease in  $m_s$  value for the comp./tens. strain can be readily explained by taking the hybridization factor into account. As the comp. strain amplitude increases, the ions move closer together, resulting in stronger hybridization. This leads to greater charge transfer among the ions, reducing the  $m_s$  magnitude of the individual magnetic ions. In contrast, the ions move further apart for tensile strained systems, which weakens

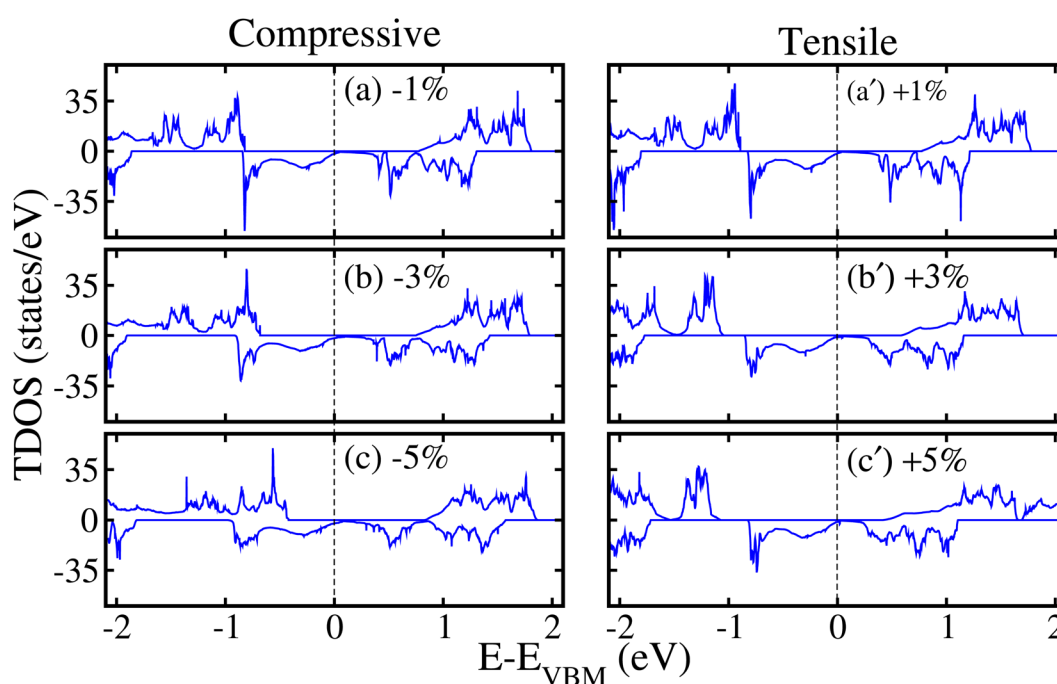


Fig. 10 GGA+ $U$  calculated total density of states (TDOS) for (a/a')  $-1/+1%$ , (b/b')  $-3/+3%$ , and (c/c')  $-5/+5%$  compressive/tensile biaxial ([110]) strains in the stable ferrimagnetic-I spin ordering of the  $\text{CaCu}_3\text{Cr}_2\text{Re}_2\text{O}_{12}$  quadruple structure.



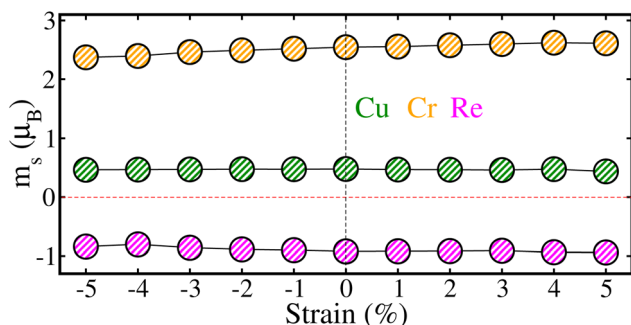


Fig. 11 Calculated partial spin magnetic moments ( $m_s$ ) on the Cu, Cr, and Re ions for  $\pm 5\%$  biaxial  $([110])$  strain in the stable ferrimagnetic- $\downarrow$  ordering of the  $\text{CaCu}_3\text{Cr}_2\text{Re}_2\text{O}_{12}$  quadruple structure.

the hybridization between them. This causes less charge transfer among ions and enhances the  $m_s$  value, as illustrated in this article.<sup>61</sup> Additionally, both Cu and Cr ions have “+” signs on their  $m_s$ , whereas it’s a “−” for that of the Re ion over the whole strain range. This further endorses the AFM coupling between Cu/Cr and Re, which turns out to have a FiM SO.

## 5 Conclusion

These *ab initio* calculations lay a foundational understanding for developing a quadruple-double perovskite oxide,  $\text{CaCu}_3\text{-Cr}_2\text{Re}_2\text{O}_{12}$ , with potential applications in spintronics. We demonstrated that magnetic properties can be engineered through doping (charge/ion implantation) to create ferromagnetic (FM) and various ferrimagnetic (FiM) spin orderings (SOs) to figure out the magnetic ground state of the system, which is  $\text{Cu}^{2+}\uparrow\text{Cr}^{3+}\uparrow\text{Re}^{5+}\downarrow$ , while keeping a reasonable total magnetic moment of  $5.0 \mu_B$  per f.u. along with partial spin moments of  $0.48/2.54/-0.92 \mu_B$  on the Cu/Cr/Re ions. This leads the system into a FiM phase, which is further confirmed by plotting the three-dimensional spin-magnetization density isosurfaces. Interestingly, the system exhibits a half-metallic (HM) nature with a sufficiently large energy gap ( $E_g$ ) of 1.62 eV in the spin majority channel ( $N^\uparrow$ ), which is an essential parameter to avoid spin-flipping above room temperature (temp.), with a Curie temperature ( $T_C$ ) of 340 K. Moreover, the transport properties of the system reveal its metallic nature in the spin minority channel ( $N^\downarrow$ ) and an insulating trait in the spin majority channel ( $N^\uparrow$ ), as evidenced by the increasing/decreasing Hall coefficient ( $R_H$ ) for  $N^\uparrow/N^\downarrow$  and increasing electrical conductivity with temperature. The positive Seebeck coefficient confirms p-type behavior, while thermal conductivity trends reflect the influence of phonon–electron interactions. These findings underscore the material’s potential for thermoelectric (TE) applications, driven by its favorable charge carrier dynamics and heat transport traits. Moreover, the computed  $T_C$  is further explained regarding magnetization ( $M$ ) and magnetic susceptibility parameters. We have explicitly discussed the behavior of the spin-polarized (SP) electron population within the material by applying an external magnetic field ( $H$ ) of varying strength (2 T and 5 T), enabling the tuning of magnetic properties. Further,

it is predicted that the system demonstrates a robustness of its HM state against a reasonable range of  $\pm 5\%$  biaxial  $([110])$  strains. Hence, the combination of a robust HM FiM state, large  $E_g$  in  $N^\uparrow$ , high  $T_C$  (above room temp.), and reasonable TE response of the  $\text{CaCu}_3\text{Cr}_2\text{Re}_2\text{O}_{12}$  structure opens pathways for further research in spintronics, offering insight into how materials can be tailored for applications such as memory devices, quantum computing, and spin-based transistors at high temperature.

## Data availability

The datasets used and/or analyzed during the current study are available from the corresponding author on reasonable request.

## Author contributions

Shehla Yasmeen: writing – original draft, investigations, formal analysis, data curation. S. Nazir: writing – review and editing, validation, supervision, project administration, conceptualization.

## Conflicts of interest

The authors declare no competing interests.

## Acknowledgements

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