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Origin of ^{13}C NMR chemical shifts elucidated based on molecular orbital theory: paramagnetic contributions from orbital-to-orbital transitions for the pre-α, α, β, α-X, β-X and *ipso*-X effects, along with effects from characteristic bonds and groups†

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^{13}C NMR chemical shifts (δ(C)) were analysed *via* MO theory, together with the origin, using σ^d(C), σ^p(C) and σ^t(C), where C^{4-} was selected as the standard for the analysis since σ^p(C: C^{4-}) = 0 ppm. An excellent relationship was observed between σ^d(C) and the charges on C for (C^{4+}, C^{2+}, C^0, C^{2-} and C^{4-}) and (C^{4-}, CH_2^{2-}, CH_3^- and CH_4). However, such a relationship was not observed for the carbon species other than those above. The occupied-to-unoccupied orbital ($\psi_i \rightarrow \psi_a$) transitions were mainly employed for the analysis. The origin was explained by the pre-α, α, β, α-X, β-X and *ipso*-X effects. The pre-α effect of an approximately 20 ppm downfield shift is theoretically predicted, and the observed α and β effects of approximately 10–15 ppm downfield shifts are well reproduced by the calculations, as are the variations in the α-X, β-X and *ipso*-X effects. Large downfield shifts caused by the formation of ethene ($\sim$120 ppm), ethyne ($\sim$60 ppm) and benzene ($\sim$126 ppm) from ethane and carbonyl ($\sim$146 ppm) and carboxyl ($\sim$110 ppm) groups from CH_3OH are also reproduced well by the calculations. The analysis and illustration of σ^p(C) through the $\psi_i \rightarrow \psi_a$ transitions enables us to visualize the effects and to understand the δ(C) values for the C atoms in the specific positions of the species. The occupied-to-occupied orbital ($\psi_i \rightarrow \psi_j$) transitions are also examined. The theoretical investigations reproduce the observed results of δ(C). The origin for δ(C) and the mechanism are visualized, which allows us to image the process in principle. The role of C in the specific position of a compound in question can be more easily understood, which will aid in the development of highly functional compounds based on NMR.

Introduction

NMR spectroscopy is one of the most important tools in current chemical and biological science research. ^{1}H and ^{13}C NMR spectra are commonly measured and analysed on a daily basis to determine the structures and/or follow up the reactions.[1–4] Lots of ^{1}H and ^{13}C NMR data have been reported thus far. The shift values spread over 20 and 300 ppm, respectively. NMR spectra, other than those above, are also measured on a daily basis.[5–8] The NMR chemical shifts of the atoms in the 3rd and higher periods, such as ^{31}P, ^{77}Se and ^{125}Te, are predominantly controlled by the paramagnetic terms, whereas those in the 1st period of ^{1}H are controlled by the diamagnetic terms. In the case of the atoms of the 2nd period, such as ^{15}N, ^{17}O and ^{19}F, the chemical shifts are controlled both by the two terms; therefore,

the mechanisms are more complex.[5–8] The relativistic effect cannot be avoided when considering those in the 5th and higher periods, whereas the effect can be treated as (much) smaller for the atoms in the 4th and lower periods.
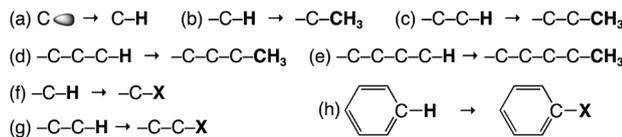
Our research interest lies in establishablishing the plain rules founded in theory for the origin and mechanism of the NMR chemical shifts of nuclei N [$\delta(N)$]. The mechanism of the origin will help experimental chemists understand the role of N at a specific position in the species over the empirical rules,[5,6] which are usually employed in assigning the spectra. The plain rules, which are established based on the theory, must be simple, easily imaged and easily understood for experimental scientists who are not specialists in this field. In our work, this purpose is given more importance than the usual NMR parameter calculations, which accurately predict the shift values of target compounds.

Scheme 1 illustrates the pre-α, α, β, γ and δ effects on δ(C), which are often employed to understand δ(C) uniformly. The typically encountered α, β and γ effects are 12–16 ppm (downfield shifts), 5–9 ppm (downfield shifts) and −2 ppm (upfield shifts), respectively, with the δ effect being negligibly small. The

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† Electronic supplementary information (ESI) available: Additional tables and the fully optimized structures given by Cartesian coordinates, together with total energies. See DOI: https://doi.org/10.1039/d4ra05980h

(a) C $\bullet$ → C–**H**　　(b) –C–**H** → –C–**CH₃**　　(c) –C–C–**H** → –C–C–**CH₃**

(d) –C–C–C–**H** → –C–C–C–**CH₃**　　(e) –C–C–C–C–**H** → –C–C–C–C–**CH₃**

(f) –C–**H** → –C–**X**

(g) –C–C–**H** → –C–C–**X**

(h) ⬡C–H → ⬡C–X

Scheme 1 The pre-α (a), α (b), β (c), γ (d), δ (e), α-X (f), β-X (g) and *ipso*-X (*i*-X) (h) effects, which are discussed in this paper.

"pre-α effect" has been proposed to establish plain rules and understand the mechanisms for δ(Se) in a unified form.[9] Scheme 1 contains the α-X, β-X and *ipso*-X (*i*-X) effects, where X stands for atoms or groups other than H and Me. The pre-α, α, and β effects are analysed based on the MO theory. The effects are calculated per unit group (per Me or H) and are discussed using the average values, if suitable. The effects of the characteristic bonds and groups are also examined.

The chemical shifts of the respective structures can be theoretically calculated with satisfactory accuracy. The total absolute magnetic shielding tensor (σ^t) is used for the analysis. As shown in eqn (1), σ^t is decomposed into the contributions from the diamagnetic shielding tensors (σ^d) and the paramagnetic shielding tensors (σ^p) under the DFT levels.[10–12] The magnetic shielding tensors consist of three components: σ^m_{xx}, σ^m_{yy} and σ^m_{zz}, (m = d, p and t). Eqn (2) shows the relationship. As shown in eqn (3), σ^d is simply expressed as the sum of the contributions over the occupied orbitals (ψ_i, so is ψ_j), where the contribution from each ψ_i to σ^d (σ^d_i) is proportional to the average inverse distance of electrons from the nuclei in ψ_i, $\langle r_i^{-1} \rangle$ (eqn (4)).[13] σ^p is evaluated by the coupled Hartree–Fock (CPHF) method. σ^p can be decomposed into contributions from the occupied orbitals or the orbital-to-orbital transitions,[14] under the DFT levels. σ^p is shown in eqn (5), although the contributions from the occupied-to-occupied orbital transitions are neglected.[9,13] The process to evaluate σ^p is highly complex; therefore, σ^p is discussed based on the approximate image derived from eqn (6),[14] where $(\varepsilon_a - \varepsilon_i)^{-1}$ is the reciprocal orbital energy gap, ψ_k is the k-th orbital function, and $\hat{L}_{z,N}$ is the orbital angular momentum around the resonance nucleus N, and r_N is the distance of electrons from N. The origin for δ(C) can be elucidated based on MO theory.

$$\sigma^t = \sigma^d + \sigma^p \tag{1}$$

$$\sigma^m = (\sigma^m_{xx} + \sigma^m_{yy} + \sigma^m_{zz})/3 \ (m = \text{d, p and t}) \tag{2}$$

$$\sigma^d = \Sigma_i^{occ} \sigma^d_i \tag{3}$$

$$\sigma^d_i = (\mu_o e^2/12\pi m_e)\langle r_i^{-1} \rangle \tag{4}$$

$$\sigma^p = \Sigma_i^{occ} \sigma^p_i = \Sigma_i^{occ} \times \Sigma_a^{unocc} \times \sigma^p_{i \to a} \tag{5}$$

$$\sigma^p_{zz} = -(\mu_o e^2/2m_e^2)\Sigma_i^{occ}\Sigma_a^{unocc}(\varepsilon_a - \varepsilon_i)^{-1}$$
$$\times \ \{\langle \psi_i|\hat{L}_z|\psi_a \rangle \langle \psi_a|\hat{L}_{z,N}r_N^{-3}|\psi_i \rangle$$
$$+ \ \langle \psi_i|\hat{L}_{z,N}r_N^{-3}|\psi_a \rangle \langle \psi_a|\hat{L}_z|\psi_i \rangle\} \tag{6}$$

The interpretation of NMR chemical shifts based on the empirical rules has traditionally been achieved by considering the distribution of electrons of molecules through the inductive and resonance effects, which has been developed in the theory of reactivity, such as the Hammett plots.[15] Indeed, this treatment has achieved a lot of success, but it does not eliminate the gap arising from the differences in the mechanisms controlling the energy and electromagnetic terms. The ^{1}H NMR chemical shifts could be essentially explained based on the inductive and resonance effects, if the magnetic anisotropic effect is suitably evaluated. However, the effect on the ^{13}C NMR chemical shifts would be complexly distributed in the σ^d and σ^p terms as shown by eqn (3)–(6). Therefore, the effects will not discuss in this paper.

Here, we report the analysis of ^{13}C NMR chemical shifts, based on the molecular orbital (MO) theory. It is intended to establish the plain rules founded in theory. The origin and mechanisms for δ(C) are discussed based on the MO theory for the effects shown in Scheme 1, together with the effects of ethene, ethyne, benzene and carbonyl and carboxyl groups. Similar investigations on δ(O), reported very recently,[16] with early investigations on δ(Se),[9] will aid in an easier understanding of δ(C).

Methodological details in the calculations

The calculations were optimized for various carbon species *via* the Gaussian 09 program package, including GaussView.[17] No specific conditions, such as the long-range interactions, were considered, unless otherwise noted. Optimizations were performed with opt = tight. The threshold (cutoff) values are 0.000015 au, 0.000010 au, 0.000060 au and 0.000040 au for the maximum force, the root mean square (RMS) force, the maximum displacement and the RMS displacement, respectively, where the predicted change in energy seems around 10^{-10} au. The structural optimizations were performed at the various DFT levels of B3LYP,[18–21] CAM-B3LYP,[22] PBE,[23] PBE0,[24] LC-ωPBE[25] and ωB97X-D[26] (L1) and MP2 (L2),[27–29] employing the 6–311++G(3df,3pd) (6D10F) basis set (BSS-A) (L/BSS-A where L = L1 + L2). HOMO and LUMO of the species, together with other MOs, were drawn using GaussView with an isovalue of 0.04 au. The gauge-independent atomic orbital (GIAO) method[30–34] was applied to calculate the absolute magnetic shielding tensors of C [σ^*(C: * = d, p and t)], employing the same method as that used in the optimizations (L$_a$/BSS-A//L$_a$/BSS-A, where L$_a$ stands for each level of L). The solvent effect was not considered in the discussion. The charge on C (Q(C)) was obtained *via* natural population analysis (NPA).[35] A utility program[36] was applied to evaluate the contributions from each ψ_i and/or $\psi_i \to \psi_a$ transition. The procedure is explained in the Appendix of the ESI.†

Results and discussion

Selection of standard and suitable level for the analysis of ^{13}C NMR chemical shifts based on σ^d(C), σ^p(C) and σ^t(C)

The σ^t(C) values of some carbon species (S) [σ^t(C: S)] were calculated with the GIAO method under B3LYP/BSS-A, for

Table 1 Absolute shielding tensors for $^{13}C*$ (* = 4+, 2+, 0, 2− and 4−) in the singlet state[a]

Nuclear	Configuration	σ^d_{B3LYP}(C: 1s)	σ^d_{B3LYP}(C: 2s)	σ^d_{B3LYP}(C: 2p)	σ^d_{B3LYP}(C)	σ^p_{B3LYP}(C)	σ^t_{B3LYP}(C)	σ^t_{MP2}(C)
C^{4+}	$(2s)^0(2p)^0$	201.71	0.00	0.00	201.71	0.00	201.71	201.77
C^{2+}	$(2s)^2(2p)^0$	200.65	37.58	0.00	238.23	0.00	238.23	238.09
C^0	$(2s)^2(2p)^2$	200.40	32.63	27.19 (×1)	260.22	3986.91	4247.13	2980.47
C^{2-}	$(2s)^2(2p)^4$	200.42	31.40	18.74 (×2)	269.23	4542.23	4811.46	3316.42
C^{4-}	$(2s)^2(2p)^6$	274.39	31.72	14.08 (×3)	274.39	0.00	274.39	276.12

[a] Calculated by applying the GIAO method under B3LYP/BSS-A and MP2/BSS-A.

instance, as were the σ^d(C: S) and σ^p(C: S) values. The σ^t(C) values were similarly calculated with MP2/MSS-A, where σ^d(C: S) and σ^p(C: S) are not obtained at the MP2 level. Table 1 lists the calculated σ^m(C: S) (m = d, p and/or t) values for S = C^{4+}, C^{2+}, C^0, C^{2-} and C^{4-}. The σ^t(C) values for C^{4+}, C^{2+} and C^{4-}, calculated with the two levels, were very close to each other. Among them, C^{4-} is taken as the standard for the analysis in this work. The reason is as follows: σ^p(C: C^{4-}) = 0.0 ppm, which is very favourable for our purpose, although σ^p(C: C^{2+}) and σ^p(C: C^{4+}) are also 0.0 ppm, as shown in Table 1. The electronic $^1S_0$ state of C^{4-} with eight valence electrons according to the octet rule and its spherical electron distribution are also favourable for this purpose.

It is necessary to determine the suitable level in this work, next. The σ^t(C: S) values were calculated for the 40 neutral carbon species (54 plots) at the DFT levels of B3LYP,[18–21] CAM-B3LYP,[22] PBE,[23] PBE0,[24] LC-ωPBE[25] and ωB97X-D[26] (L1) with BSS-A, together with σ^d(C: S) and σ^p(C: S). The MP2 level (L2) is also applied to obtain the σ^t(C: S) values. The basis set of def2TZVP[37,38] was also applied at the B3LYP level (B3LYP/def2TZVP). The results are collected in Tables S1–S7 and S9 of the ESI.†

The calculated σ^t(C: S) values are very close with each other. The $-\Delta\sigma^t$(C: S) values calculated at the L (= L1 + L2) levels are plotted versus the corresponding δ(C: S), respectively. The plot for S of the 40 neutral carbon species (54 plots) at B3LYP is drawn in Fig. S1 of the ESI.† The plot is analysed assuming the linear relationship ($y = ax + b$: R_c^2 (the square of the correlation coefficient)), where (a, b, R_c^2) = (1.05, 1.90, 0.998). (The plot is very similar to Fig. 3 for the neutral and charged 75 carbon species). Similar treatments were performed at L = L1 + L2. Table 2 collects the results. The correlations were very similar with each other. The R_c^2 values at the B3LYP, PBE and ωB97X-D levels (0.998) seem slightly better than others, therefore, the B3LYP level is selected for the calculations. The B3LYP level is most popularly accepted also by the experimental researchers, which is significant for our purposes.

Conformational and solvent effects on ^{13}C NMR chemical shifts

It is an important issue to examine the conformational effect on σ^t(C) in the calculations. The effect is examined exemplified by *n*-pentane. Five conformers of the different energies are optimized, which are called tt, tg, gt, gg_A and gg_B, together with the topological isomers of tg, where t and g stand for the trans and

Table 2 Correlations in the plots of calculated $-\Delta\sigma^t(^{13}C: S)$ versus observed $\delta(^{13}C: S)$ for the species.[a,b]

Entry	Level (L)	a	b	R_c^2	N
1	B3LYP	1.049	1.90	0.998	54
2	CAM-B3LYP	1.075	0.00	0.997	54
3	PBE	1.037	2.18	0.997	54
4	PBE0	1.056	0.31	0.997	54
5	LC-ωPBE	1.102	−1.55	0.998	54
6	ωB97X-D	1.058	0.46	0.998	54
7	MP2	1.017	1.89	0.995	54
8[c]	B3LYP	1.053	2.44	0.997	54
9[d]	B3LYP	1.036	1.37	0.997	54

[a] Calculated with the GIAO method under L/BSS-A. [b] Observed data are used for the corresponding species in the plot. [c] Under the solvent effect of CHCl₃. [d] Calculated with B3LYP/def2TZVP.

gauche conformations, respectively. Fig. 1 shows the structures of tt, tg, gt, gg_A and gg_B. The calculated $\sigma^t(C_i: i = 1–5)$ values are collected in Table S10 of the ESI,† together with the observed values. The energies of tg, gt, gg_A and gg_B from tt are also given in the Table, which are 3.7, 7.2, 6.8 and 14.3 kJ mol^{-1}, respectively. The $\sigma^t(C_i: i = 1–5)_{calcd}$ values are plotted versus the $\delta(C_i: i = 1–5)_{obsd}$ values for the five conformers. Fig. 2 shows the plots, which are also analysed assuming the linear relationship. Table 3 collects the (a, b, R_c^2) values, which are also given in Fig. 2.

As shown in Table 3, the correlation seems excellent for gt and gg_A, good for tt, and moderate for gg_B. The gt and/or gg_A conformers seem most suitable for the purpose, at first glance, however, they are less stable than tt by about 7 kJ mol^{-1}. Judging comprehensively, the tt conformer should also be recommended as the suitable one. The extended conformers would be recommended as the nice ones for the long-chained species in the calculations, since it is inferred that they would be less three-dimensionally crowded than other conformers. The selection of the extended conformers would not damage so much on our discussion, judging from the above discussion. However, other conformers must also be considered for the better discussion since other conformers contribute depending on their populations among the conformers.

The solvent effect of chloroform was also examined with the polarizable continuum model (PCM).[39] The calculated results are collected in Table S8 of the ESI† and the plot is contained in Fig. S8 of the ESI.† The correlation is shown in Table 2 (entry 8). The correlation seems very similar to (but very slightly poorer
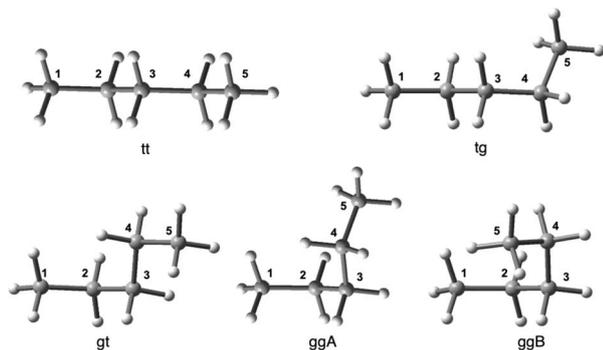
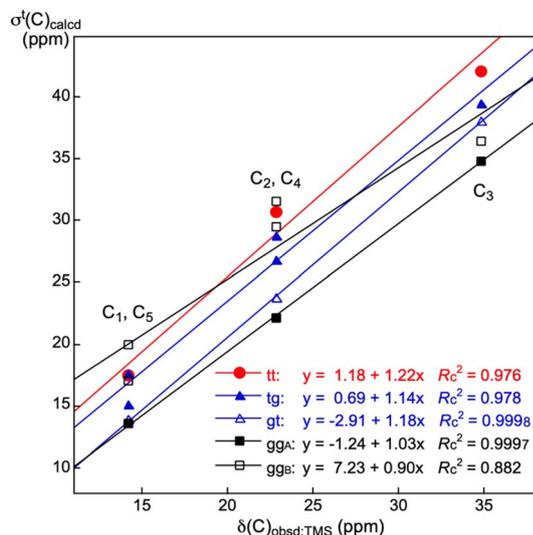Fig. 1   Optimized conformers for *n*-pentane with B3LYP/BSS-A.

Fig. 2   Plots of $-\Delta\sigma^{t}(C_i: i = 1-5)_{\text{calcd:TMS}}$ *versus* $\delta(C_i: i = 1-5)_{\text{obsd:TMS}}$ for five conformers in *n*-pentane.

Table 3   Correlations in the plots of $-\Delta\sigma^{t}(C)_{\text{calcd:TMS}}$ *versus* $\delta(C)_{\text{obsd}}$ for the optimized conformers of *n*-pentane.[a,b]

Entry	Conformer	a	b	R_c^2	N
1	tt	1.22	1.18	0.976	5
2	tg	1.14	0.69	0.978	5
3	gt	1.18	−2.91	0.9998	5
4	gg$_A$	1.03	−1.24	0.9997	5
5	gg$_B$	0.90	7.23	0.882	5

[a] Calculated with the GIAO method under B3LYP/BSS-A. [b] $-\Delta\sigma^{t}(C)_{\text{calcd:TMS}} = -[\sigma^{t}(C: \text{pentane})_{\text{calcd}} - [\sigma^{t}(C: \text{TMS})_{\text{calcd}}]$.

than) that without the solvent effect (entry 1). Therefore, the solvent effect is not considered in this work.

Calculated $\sigma^{t}(C)$ and observed $\delta(C)$ values

Table 4 lists the $\sigma^{m}(C: S)$, $\Delta\sigma^{m}(C: S)$ [$=\sigma^{m}(C: S) - \sigma^{m}(C: C^{4-})$: $\Delta\sigma^{p}(C)$ $(=\sigma^{p}(C))$ since $\sigma^{p}(C: C^{4-}) = 0$ ppm] and $\Delta\sigma^{m}(C: S)_e$ ($m = $ d, p and t) values, calculated with B3LYP/BSS-A for various carbon species of **1–56**, together with the $Q(C)$ values. The

$\Delta\sigma^{m}(C: S)_e$ values are explained later. The values are similar calculated for the carbon species of **S1–S20** and **S21–S70**. The calculated values are provided in Tables S11 and S12, respectively, of the ESI.†

The $\Delta\sigma^{m}(C: S)_e$ values are defined by $\Delta\sigma^{m}(C: S)_e = (1/n)$ $[\Delta\sigma^{m}(C: S) - \Delta\sigma^{m}(C: S_e)]$, for the pre-α, α, β, γ and δ effects, together with the α-X, β-X and *i*-X effects, where S_e are the starting species for the effects and n is the factor used to make $\Delta\sigma^{m}(C: S)_e$ per unit group. Scheme 2 explains the method used to calculate the effects, exemplified by the pre-α, α and β effects. The effects are calculated according to the definition. In the case of the β effect from $CH_3CH_2CH_3$ to $(CH_3)_2CHCH_2CH_3$, $(CH_3)_2CHCH_2CH_3$, $CH_3CH_2CH_3$ and 2 correspond to S, S_e and n, respectively. The difference in $\Delta\sigma^{t}(C: S)$ between $S_e = CH_3\text{-}CH_2CH_3$ ($\sigma^{t}(C) = 160$ ppm) and $S = (CH_3)_2CHCH_2CH_3$ (145 ppm) is −15 ppm, which corresponds to the 2β effect. The $\Delta\sigma^{t}(C: S)$ values are abbreviated as $\varDelta$ in Scheme 2. Therefore, the β effect in this process is evaluated as −8 ppm (=$\varDelta$/2), for example. The $\Delta\sigma^{d}(C: S)_e$ and $\Delta\sigma^{p}(C: S)_e$ values for the effect are calculated similarly. Scheme 3 summarizes the pre-α, α, β, γ and δ effects, together with the α-X, β-X and *i*-X effects and the effects of the characteristic bonds and groups. The $\Delta\sigma^{d}(C)_e$, $\Delta\sigma^{p}(C)_e$ and $\Delta\sigma^{t}(C)_e$ values are also shown in Scheme 3.

Fig. 3 shows the plots of $\delta(C: S)_{\text{obsd:TMS}}$ *versus* $-\Delta\sigma^{t}(C: S)_{\text{calcd:TMS}}$ for the various species of **1–56** shown in Table 4 and **S21–S70** in Table S12 of the ESI,† although the species are limited for those of the available $\delta(C: S)_{\text{obsd:TMS}}$ values. The $-\Delta\sigma^{t}(C: S)_{\text{calcd:TMS}}$ values are used in Fig. 3 for the convenience of the direct comparison between the observed and calculated values. The plot shows an excellent correlation ($y = -1.52 + 0.942x$: $R_c^2 = 0.998$), with some systematic deviations. The excellent correlation confirms the high reliability of the calculations. While the data for (CH_3F, CH_2F_2, CHF_3 and CF_4) are on the correlation line, those for (CH_3Cl, CH_2Cl_2, $CHCl_3$ and CCl_4) and (CH_3Br, CH_2Br_2, $CHBr_3$ and CBr_4) deviate systematically from the line.

While the data point for CH_3Cl is on the line, that from CH_3Br seems to deviate slightly downside from the correlation. Data for the chlorine and bromine species are analysed using the quadratic functions. The correlations are described by $y = -1.09 + 0.862x - 0.0014x^2$: $R_c^2 = 0.9999$ and $y = -1.59 + 0.712x - 0.0055x^2$: $R_c^2 = 0.990$, respectively. The relativistic effect must be responsible for the deviations, which will not be discussed here.[10,11,40–42]

Behaviour of $\sigma^{d}(C)$

Fig. 4 shows the plot of $\sigma^{d}(C)$ *versus* $Q(C)$ for (C^{4+}, C^{2+}, C^{0}, C^{2-} and C^{4-}). The correlation is excellent if analysed using the cubic function ($y = 0.1113x^3 - 1.352x^2 - 7.305x + 259.57$: $R_c^2 = 0.9998$). The behaviour of the $\sigma^{d}(C)$ values can essentially be understood by considering the two factors shown by eqn (3) and (4). If the number of occupied MOs (ψ_i) on C increases, the $\sigma^{d}(C)$ values increase, although the magnitude of each $\sigma_i^{d}(C)$ will decrease, especially for the outer ψ_i (as shown by $\sigma_{\text{B3LYP}}^{d}(C: AO)$). The average distance of the electrons from C(r_i) in question in ψ_i becomes longer because of the increase in the electron–electron

Table 4 The σ^m(C: S), $\Delta\sigma^m$(C: S) and $\Delta\sigma^m$(C: S)$_e$ (m = d, p and t) for various species of **1–56**, along with the pre-α, α, β, γ, δ, α-X, β-X and *ipso*-X (*i*-X) effects and the effects from the characteristic bonds and groups,[a,b] together with the Q(C) values

Species (nos: sym)	Q(C)	σ^d(C)	$\Delta\sigma^d$(C)	σ^p(C)[c]	σ^t(C)	$\Delta\sigma^t$(C)	$\Delta\sigma^d$(C)$_e$[d]	$\Delta\sigma^p$(C)$_e$[d]	$\Delta\sigma^t$(C)$_e$[d]	Effect
C^{4-} (**1**: O_h)	−4.000	274.39	0.00	0.00	274.39	0.00	0.00	0.00	0.00	—
HC^{3-} (**2**: $C_{\infty v}$)	−1.815	264.04	−10.35	1807.41	2071.45	1797.06	−10.35	1807.41	1797.06	Pre-α
H$_2$C^{2-} (**3**: C_{2v})	−2.156	261.96	−12.43	137.46	399.42	125.03	−6.22	68.73	62.51	Pre-α
H$_3$C$^-$ (**4**: C_{3v})	−1.400	249.53	−24.87	−2.26	247.26	−27.13	−8.29	−0.75	−9.04	Pre-α
CH$_4$ (**5**: T_d)	−0.805	238.98	−35.42	−49.66	189.32	−85.08	−8.85	−12.42	−21.27	Pre-α
CH$_3$H$_2$C$^-$ (**6**: C_s)	−1.000	250.87	−23.53	−98.55	152.32	−122.08	1.34	−96.29	−94.95	α
EtH$_2$C$^-$ (**7**: C_s)	−0.915	248.89	−25.51	−82.29	166.59	−107.80	−1.98	16.26	14.28	β
i-PrH$_2$C$^-$ (**8**: C_1)	−0.923	236.54	−37.85	−94.11	142.43	−131.96	−7.16	2.22	−4.94	β
t-BuH$_2$C$^-$ (**9**: C_s)	−0.985	236.18	−38.22	−62.01	174.16	−100.23	−4.90	12.18	7.28	β
n-PrH$_2$C$^-$ (**10**: C_s)	−0.990	260.85	−13.54	−87.90	172.96	−101.44	11.97	−5.61	−5.61	γ
n-BuH$_2$C$^-$ (**11**: C_s)	−0.938	262.85	−11.55	−88.82	174.03	−100.37	1.99	−0.92	1.07	ε
CH$_3$CH$_3$ (**12**: D_{3d})	−0.571	238.60	−35.80	−65.21	173.39	−101.00	−0.38	−15.55	−15.92	α
CH$_3$CH$_2$CH$_3$ (**13a**: C_{2v})	−0.568	232.81	−41.58	−68.71	164.10	−110.30	−5.79	−3.51	−9.29	β
CH$_3$CH$_2$CH$_3$ (**13b**: C_{2v})	−0.382	251.23	−23.17	−91.12	160.10	−114.29	6.12	−20.73	−14.61	α
Me$_2$CHCH$_3$ (**14a**: C_{3v})	−0.565	230.20	−44.20	−73.87	156.33	−118.06	−4.20	−4.33	−8.53	β
Me$_3$CH (**14b**: C_{3v})	−0.232	267.54	−6.85	−114.35	153.19	−121.21	9.52	−21.56	−12.04	α
t-BuCH$_3$ (**15**: T_d)	−0.563	229.82	−44.58	−78.63	151.19	−123.20	−2.93	−4.47	−7.40	β
CH$_3$CH$_2$CH$_2$CH$_3$ (**16a**: C_{2h})	−0.565	236.01	−38.38	−70.67	165.34	−109.05	3.20	−1.96	1.24	γ
CH$_3$CH$_2$CH$_2$CH$_3$ (**16b**: C_{2h})	−0.377	244.34	−30.06	−93.60	150.74	−123.66	−6.89	−2.48	−9.37	β
n-BuCH$_3$ (**17a**: C_{2v})	−0.375	233.25	−41.15	−67.69	165.55	−108.84	−2.77	2.98	0.21	δ
n-PrMeCH$_2$ (**17b**: C_{2v})	−0.564	252.13	−22.27	−99.81	152.32	−122.08	7.79	−6.21	−6.21	γ
i-PrMeCH$_2$ (**18a**: C_1)	−0.372	247.55	−26.84	−102.18	145.37	−129.02	−1.84	−5.53	−7.37	β
EtMe$_2$CH (**18b**: C_1)	−0.225	265.39	−9.01	−118.76	146.63	−127.77	−2.15	−4.41	−6.56	β
t-BuMeCH$_2$ (**19**: C_s)	−0.371	251.79	−22.60	−112.21	139.58	−134.81	0.19	−7.03	−6.84	β
n-BuMeCH$_2$ (**20**: C_{2h})	−0.374	243.63	−30.77	−101.29	142.33	−132.06	−8.50	−1.48	−9.98	δ
i-PrMe$_2$CH (**21**: C_{2h})	−0.219	259.35	−15.04	−118.14	141.21	−133.18	−4.10	−1.89	−5.99	β
t-BuMe$_2$CH (**22**: C_s)	−0.215	265.19	−9.20	−127.39	137.80	−136.60	−0.78	−4.35	−5.13	β
n-PrMe$_2$CH (**23**: C_1)	−0.224	274.83	0.43	−128.33	146.50	−127.90	9.44	−9.57	−9.57	γ
n-BuMe$_2$CH (**24**: C_1)	−0.223	276.20	1.80	−128.65	147.55	−126.84	1.37	−0.31	1.06	ε
H$_3$C$^+$ (**25**: C_{3v})	0.362	240.45	−33.94	−467.68	−227.23	−501.62	[e]e	[e]e	[e]e	[e]e
MeH$_2$C$^+$ (**26**: C_s)	−0.215	242.18	−32.21	−219.86	22.32	−252.08	1.73	247.82	249.55	α
EtH$_2$C$^+$ (**27**: C_s)	−0.256	242.53	−31.87	−140.46	102.07	−172.33	0.35	79.40	79.75	β
i-PrH$_2$C$^+$ (**28**: C_1)	−0.472	256.69	−17.70	−139.73	116.96	−157.44	7.26	40.07	47.32	β
t-BuH$_2$C$^+$ (**29**: C_1)	−0.489	270.61	−3.79	−149.75	120.85	−153.54	9.48	23.37	32.84	β
Me$_2$HC$^+$ (**30**: C_2)	0.396	247.98	−26.42	−400.37	−152.39	−426.79	3.76	33.66	37.42	α
EtMeHC$^+$ (**31**: C_1)	0.366	256.56	−17.84	−396.76	−140.20	−414.59	256.56	−396.76	−140.20	β
i-PrMeHC$^+$ (**32**: C_1)	0.174	268.19	−6.21	−284.57	−16.39	−290.78	134.09	−142.29	−8.19	β
t-BuMeHC$^+$ (**33**: C_1)	−0.327	293.49	19.10	−182.60	110.89	−163.50	97.83	−60.87	36.96	β
Me$_3$C$^+$ (**34**: C_1)	0.536	242.28	−32.12	−411.12	−168.84	−443.23	0.61	18.86	19.46	α
EtMe$_2$C$^+$ (**35**: C_1)	0.540	242.21	−32.19	−414.36	−172.15	−446.55	−0.07	−3.24	−3.31	β
i-PrMe$_2$C$^+$ (**36**: C_1)	0.544	242.44	−31.95	−404.51	−162.07	−436.46	0.08	3.30	3.39	β
t-BuMe$_2$C$^+$ (**37**: C_1)	0.537	242.76	−31.63	−402.64	−159.88	−434.27	0.16	2.83	2.99	β
CH$_3$OH (**38**: C_s)	−0.191	232.16	−42.24	−104.67	127.49	−146.90	−6.82	−55.01	−61.82	α-X
CH$_3$SH (**39**: C_s)	−0.692	243.86	−30.54	−73.63	170.23	−104.16	4.88	−23.97	−19.09	α-X
CH$_3$SeH (**40**: C_s)	−0.737	240.42	−33.97	−66.34	174.08	−100.31	1.45	−16.68	−15.23	α-X
CH$_3$SSMe (**41**: C_2)	−0.709	241.38	−33.02	−85.75	155.63	−118.77	2.40	−36.09	−33.69	α-X
CH$_3$F (**42**: C_{3v})	−0.066	232.99	−41.40	−126.01	106.99	−167.41	−5.98	−76.35	−82.33	α-X
CH$_3$Cl (**43**: C_{3v})	−0.529	243.61	−30.79	−93.19	150.42	−123.98	4.63	−43.53	−38.90	α-X
CH$_3$Br (**44**: C_{3v})	−0.601	241.70	−32.69	−83.06	158.65	−115.75	2.73	−33.40	−30.67	α-X
CH$_3$I (**45**: C_{3v})	−0.719	236.32	−38.08	−56.17	180.15	−94.24	−2.66	−6.51	−9.17	α-X
CH$_3$CO$_2$Me (**46**: C_s)	−0.666	248.04	−26.36	−87.22	160.82	−113.58	9.06	−37.56	−28.50	α-X
CH$_3$CN (**47**: C_{3v})	−0.677	220.25	−54.14	−38.56	181.70	−92.70	−18.72	11.10	−7.62	α-X
CH$_3$NH$_2$ (**48**: C_S)	−0.360	229.80	−44.60	−79.79	150.01	−124.39	−9.18	−30.13	−39.31	α-X
CH$_3$NO$_2$ (**49**: C_s)	−0.410	231.58	−42.82	−114.08	117.50	−156.90	−7.40	−64.42	−71.82	α-X
CH$_3$CH$_2$OH (**50a**: C_s)	−0.016	225.96	−48.44	−108.36	117.60	−156.80	−12.64	−43.15	−55.79	α-X
CH$_3$CH$_2$OH (**50b**: C_s)	−0.587	245.33	−29.07	−81.19	164.14	−110.26	6.73	−15.98	−9.25	β-X
H$_2$C=CH$_2$ (**51**: D_{2h})	−0.365	246.91	−27.49	−194.83	52.08	−222.31	8.31	−129.62	−121.31	C$_2$H$_4$[f]
HC≡CH (**52**: $D_{\infty h}$)	−0.225	255.62	−18.77	−145.56	110.06	−164.34	17.03	−80.35	−63.33	C$_2$H$_2$[f]
C$_6$H$_6$ (**53**: D_{6h})	−0.106	239.66	−34.73	−192.70	46.96	−227.43	1.07	−127.49	−126.43	C$_6$H$_6$[f]

Table 4 (*Contd.*)

Species (nos: sym)	$Q(C)$	$\sigma^d(C)$	$\Delta\sigma^d(C)$	$\sigma^p(C)^c$	$\sigma^t(C)$	$\Delta\sigma^t(C)$	$\Delta\sigma^d(C)_e{}^d$	$\Delta\sigma^p(C)_e{}^d$	$\Delta\sigma^t(C)_e{}^d$	Effect
C_6H_5OH (**54**: C_s)	0.449	258.53	−15.87	−243.01	15.52	−258.88	18.86	−50.31	−31.45	*i*-X
$H_2C{=}O$ (**55**: C_{2v})	0.307	245.20	−29.19	−263.64	−18.44	−292.83	13.05	−158.97	−145.93	**C=O**
$H(HO)C{=}O$ (**56**: C_s)	0.675	245.49	−28.90	−228.53	16.97	−257.43	13.34	−123.86	−110.53	O**C=O**

[a] Calculated with the GIAO-DFT method under B3LYP/BSS-A. [b] $\Delta\sigma^m(C: S) = \sigma^m(C: S) − \sigma^m(C: C^{4−})$ (m = d, p and t). [c] $\Delta\sigma^p(C) = \sigma^p(C)$, since $\sigma^p(C: C^{4−})$ = 0 ppm. [d] $\Delta\sigma^m(C: S)_e = (1/n)(\Delta\sigma^m(C: S) − \Delta\sigma^m(C: S_e))$; see the text for n, S and S_e. [e] The effect not being defined. [f] From C_2H_6.
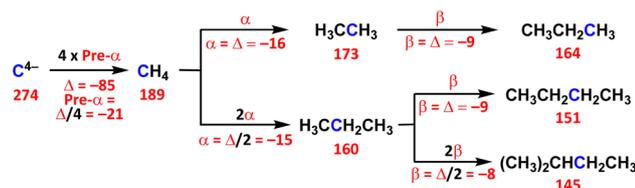
Scheme 2 Evaluation of the pre-α, α and β effects. The σ^t(C: S) values in ppm are given in red bold, and the differences between the two values are Δ.

repulsion if the number of occupied MOs increases. In this case, each $\langle r_i^{-1}\rangle$ and σ_i^d in eqn (4) decreases. The σ_i^d values collected in Table 4 are well understood as the total effect of the two. Fig. 2 also shows the plot of σ^d(C) *versus* Q(C) for ($C^{4−}$, $CH_2^{2−}$, $CH_3^−$, and CH_4). The correlation is also excellent if analysed using the quadratic function ($y = −3.112x^2 − 26.145x + 219.66$: $R_c^2 = 0.9998$).

Fig. 4 contains similar plots for (O^{6+}, O^{4+}, O^{2+}, O^0 and $O^{2−}$)[16] and (Se^{6+}, Se^{4+}, Se^{2+}, Se^0 and $Se^{2−}$),[9] whose correlations are excellent ($y = −0.006x^3 − 1.639x^2 − 10.218x + 394.40$: $R_c^2 = 1.0000$ for O and $y = 0.003x^3 − 0.678x^2 − 5.914x + 2996.70$: $R_c^2 = 0.9999$ for Se). The correlations become less sharp in the order of N = O > C > Se. The $\Delta\sigma^d(N^{2−:2+})$ ($=(\sigma^d(N^{2−}) − \sigma^d(N^{2+}))$) value was divided by the overall chemical shift width for each N. The values were compared with each other to estimate roughly the contributions of $\sigma^d(N)$ to $\sigma^t(N)$. The ratio is 0.103 (=31.0/300) for C, 0.016 (=41.1/2500) for O and 0.003 (=23.9/8000) for Se. The results show that the contributions of $\sigma^d(N)$ to the overall chemical shifts decreased in the order of N = C >> O >> Se. As a result, the $\sigma^d(C)$ term should be considered carefully for N = C relative to the cases of O and Se.

Fig. 5 shows the plot of σ^d(C: S) *versus* Q(C) for **1–56** in Table 4, except for those plotted in Fig. 4 (**1–5**). The σ^d(C: S) values are analysed separately by the types of S: $RH_2C^−$ (**6–11**), RCH_3 (**12–16**), $RMeCH_2$ (**17–20**), RMe_2CH (**21–25**), RH_2C^+ (**26–30**), $RMeHC^+$ (**31–34**), RMe_2C^+ (**35** and **36**) and CH_3X (**37–50**), together with C_2H_4 (**51**), C_2H_2 (**52**), C_6H_6 (**53**), $H_2C{=}O$ (**54**) and $H(HO)C{=}O$ (**55**). The range of σ^d(C) in each plot is less than approximately 15 ppm, except for that of $RMeCH_2$ (**17–20**), which ranges from 30 ppm. The σ^d(C: S) values increase in the order of R = Me < Et < *i*-Pr < *t*-Bu for $RH_2C^−$ and RCH_3. However, the behaviour seems complex for others.

The origin and mechanisms of the effects are discussed next, using an approximated image derived from eqn (6).

Origin of the pre-α effect

The analysis of the ^{13}C NMR chemical shifts starts from the pre-α effect,[9] this is the important starting point of our NMR analysis. The pre-α effect is evaluated by the ($\Delta\sigma^d(C)_e$, $\Delta\sigma^p(C)_e$, $\Delta\sigma^t(C)_e$) values. The average values from $C^{4−}$ to H_4C are (−8.9, −12.4, −21.3 ppm) (see Table 4), which are calculated per unit group (per H in this case). The pre-α effect is theoretically predicted to be a downfield shift of 21 ppm based on the average value of $\Delta\sigma^t(C)_e$ from $C^{4−}$ to H_4C. The solvent effect is not considered for the pre-α effect on each process from $C^{4−}$ to CH_4, although the negative charge would also be of importance (see Scheme 3).

Table 5 lists the $\sigma^d(C)$, $\sigma^p(C)$ and $\sigma^t(C)$ values of $C^{4−}$, $H_2C^{2−}$, $H_3C^−$ and H_4C, separately by each MO. The inner MO of ψ_1 is formed by the 1s(C) AO; therefore, it greatly contributes to $\sigma^d(C)$ but not $\sigma^p(C)$. The second inner ψ_2 is constructed mainly by the 2s(C) AO; therefore, it contributes substantially to $\sigma^d(C)$ but slightly to $\sigma^p(C)$. The outer MOs of ψ_3, ψ_4 and ψ_5 are constructed mainly by the 2p$_x$(C), 2p$_y$(C) and 2p$_z$(C) AOs with 1s(H) AO(s), if any. Therefore, they contribute greatly to $\sigma^p(C)$ but slightly to $\sigma^d(C)$, although $\sigma^p(C)$ = 0 ppm for all the MOs in $C^{4−}$. The MOs of ψ_3, ψ_4 and ψ_5 in $C^{4−}$ are equivalent; therefore, the total values of the three are given in the Table, as are ψ_3 and ψ_4 in $H_3C^−$.

The protonation of $C^{4−}$ introduces $\sigma(C–H)$ and $\sigma^*(C–H)$ orbitals in the resulting species, resulting in the asymmetrical distribution of electrons. The symmetrical and unsymmetrical components of the electron distribution produce $\sigma^d(C)$ and $\sigma^p(C)$, respectively, as mentioned above. The $\sigma^p(C)$ terms are caused through orbital-to-orbital transitions, such as the $\psi_i\rightarrow\psi_a$ transition, where $\sigma(C–H)$ and $\sigma^*(C–H)$ are expected to operate as the typical ψ_i and ψ_a, respectively, in the transitions. Table 6 lists the $\psi_i\rightarrow\psi_a$ transitions that contributed mainly to $\sigma_{i\rightarrow a:kk}^p$(C: $k = x$, y and/or z) for $H_2C^{2−}$ and H_4C. The magnitudes of $\sigma_{i\rightarrow a}^p$(C), which are greater than 10 ppm in magnitude, are provided in Table 6. In the case of $H_2C^{2−}$, the $\psi_3\rightarrow\psi_9$ ($\sigma_{3\rightarrow9:zz}^p$(C) = −113.8 ppm) and $\psi_4\rightarrow\psi_9$ ($\sigma_{4\rightarrow9:yy}^p$(C) = −87.6 ppm) transitions largely contribute to $\sigma_{i\rightarrow a}^p$(C), with large positive contributions from the $\psi_4\rightarrow\psi_7$, $\psi_5\rightarrow\psi_6$, $\psi_5\rightarrow\psi_7$ and $\psi_5\rightarrow\psi_8$ transitions. The $\psi_3\rightarrow\psi_{15}$, $\psi_3\rightarrow\psi_{16}$, $\psi_4\rightarrow\psi_{14}$, $\psi_4\rightarrow\psi_{16}$, $\psi_5\rightarrow\psi_{14}$ and $\psi_5\rightarrow\psi_{15}$ transitions contribute greatly to $\sigma^p(C)$ ($\sigma_{i\rightarrow a:kk}^p$(C) = −33.3 ppm) in H_4C.

Fig. 6a and b illustrate the selected $\psi_i\rightarrow\psi_a$ transitions for $H_2C^{2−}$ and H_4C, respectively, along with the characteristics of ψ_i and ψ_a and the orbital energies. Fig. 6a shows the $\psi_3\rightarrow\psi_9$, $\psi_4\rightarrow\psi_7$, $\psi_4\rightarrow\psi_9$, $\psi_5\rightarrow\psi_6$, $\psi_5\rightarrow\psi_7$ and $\psi_5\rightarrow\psi_8$ transitions in $H_2C^{2−}$, whereas the $\psi_3\rightarrow\psi_{15}$, $\psi_3\rightarrow\psi_{16}$, $\psi_4\rightarrow\psi_{14}$, $\psi_4\rightarrow\psi_{16}$, $\psi_5\rightarrow\psi_{14}$ and $\psi_5\rightarrow\psi_{15}$ transitions in H_4C are shown in Fig. 6b.
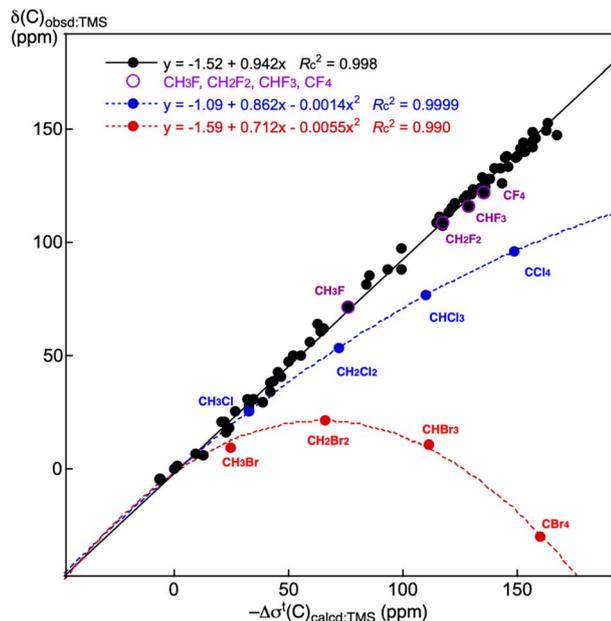
(a) ^{13}C NMR Chemical Shifts: The Pre-α, α, β, γ and δ Effects   Effect:[a]

Pre-α:
C^{4-} →(**1797** (−10.4; 1807)) HC^{3-} →(**−1672** (−2.1; −1670)) H_2C^{2-} →(**−152.2** (−12.4; −139.7)) H_3C^-

H_3C^{-a} →(**−58.0** (−10.6; −47.4)) H_4C --------------→ H_3C^+ Pre-α

α:
MeH$_2$C$^-$: **−95.0** (1.3; −96.3)
MeCH$_3$: **−15.9** (−0.4; −15.6)
Me$_2$CH$_2$: **−13.3** (12.6; −25.9) ; **−6.9** (16.3; −23.2)
Me$_3$CH
MeC$^+$H$_2$: **249.6** (1.7; 247.8) ; **−174.7** (5.8; −180.5)
Me$_2$C$^+$H : **−16.5** (−5.7; −10.8)
Me$_3$C$^+$

β:
EtH$_2$C$^-$: **14.3** (−2.0; 16.3)
EtCH$_3$: **−9.3** (−5.8; −3.5)
EtMeCH$_2$: **−9.4** (−6.9; −2.5)
EtMe$_2$CH : **−6.6** (−2.2; −4.4)
EtC$^+$H$_2$: **79.8** (0.4; 79.4)
EtMeC$^+$H : **−12.2** (8.6; 3.6)
EtMe$_2$C$^+$: **−3.3** (−0.1; −3.2)

β:
i-PrH$_2$C$^-$: **−24.2** (−12.4; −11.8)
i-PrCH$_3$: **−7.8** (−2.6; −5.2)
i-PrMeCH$_2$: **−5.4** (3.2; −8.6)
i-PrMe$_2$CH : **−5.4** (−6.0; −0.6)
i-PrC$^+$H$_2$: **14.9** (14.2; −0.7)
i-PrMeC$^+$H : **123.8** (11.6; 112.2)
i-PrMe$_2$C$^+$: **10.1** (0.2; 9.9)

β:
t-BuH$_2$C$^-$: **31.7** (−0.4; 32.1)
t-BuCH$_3$: **−5.1** (−0.4; −4.8)
t-BuMeCH$_2$: **−5.8** (4.2; −10.0)
t-BuMe$_2$CH : **−3.4** (5.8; −9.3)
t-BuC$^+$H$_2$: **3.9** (13.9; −10.0)
t-BuMeC$^+$H : **127.3** (25.3; 102.0)
t-BuMe$_2$C$^+$: **2.2** (0.3; 1.9)

γ:
n-PrCH$_3$: **1.2** (3.2; −2.0)
n-PrMeCH$_2$: **1.6** (7.8; −6.2)
n-PrMe$_2$CH : **−0.1** (9.4; −9.6)

$\Delta\sigma^t(C)$
$(\Delta\sigma^d(C); \Delta\sigma^p(C))$

δ:
n-BuCH$_3$: **0.2** (−2.8; 3.0)
n-BuMeCH$_2$: **−10.0** (−8.5; −1.5)
n-BuMe$_2$CH : **1.0** (1.4; −0.3)

[a] Averaged values of $(\Delta\sigma^t(C); \Delta\sigma^d(C); \Delta\sigma^p(C))$ = (**−9.0**; −8.3; −0.8) in ppm for H$_3$C$^-$ from C^{4-}.

(b) ^{13}C NMR Chemical Shifts: The α-X, β-X, and i-X Effects and the Effects from the Characteristic Bonds and Groups   Effect:[a]

CH$_4$ ────────→ H$_3$CX

X =	OH	F	Cl	Br	NH$_2$	NO$_2$	SH	SeH	CO$_2$Me	
	−61.8 (−6.8; −55.0)	**−82.3** (−6.0; −76.4)	**−38.9** (4.6; −43.5)	**−30.7** (2.7; −33.4)	**−39.3** (−9.2; −30.1)	**−71.8** (−7.4; −64.4)	**−19.1** (4.9; −24.0)	**−15.2** (1.5; −16.7)	**−28.5** (9.1; −37.6)	α-X

CH$_3$CH$_3$ ────────→ ^{β}CH$_3$^{α}CH$_2$X

X =	OH	F	Cl	Br	NH$_2$	NO$_2$	SH	SeH	CO$_2$Me	
	−55.8 (−12.6; −43.2)	**−8.9** (3.7; −12.6)	**−40.8** (15.4; −56.2)	**−35.9** (9.4; −45.2)	**−35.3** (−1.2; −34.1)	**−65.2** (0.7; −65.9)	**−18.0** (11.8; −29.8)	**−16.4** (5.0; −21.4)	**−21.7** (40.3; −61.9)	α-X
	−9.3 (6.7; −16.0)	**−77.2** (−10.3; −66.9)	**−12.2** (−6.9; −5.3)	**−12.7** (−3.1; −9.6)	**−16.2** (−1.9; −14.3)	**−3.2** (0.1; −3.3)	**−6.9** (−2.5; −4.3)	**−6.6** (0.9; −7.6)	**−1.3** (−15.4; 14.1)	β-X

C$_6$H$_6$ ────────→ C$_6$H$_5$X

X =	OH	F	Cl	Br	NH$_2$	NO$_2$	SH	SeH	CO$_2$Me	
	−31.5 (−18.9; −50.3)	**−39.7** (35.2; −74.9)	**−15.2** (−26.3; 11.1)	**−14.7** (−0.5; −14.2)	**−21.2** (17.6; −38.7)	**−22.4** (31.3; −53.7)	**−12.0** (−82.5; 70.5)	**−15.6** (11.4; −27.0)	**−2.8** (−38.8; 36.1)	i-X

Effect:[a]

CH≡CH C$_2$H$_2$: **−63.3** (17.0; −80.3)

H$_2$C=CH$_2$ C$_2$H$_4$: **−121.3** (8.3; −129.6) ; **58.0** (8.7; 49.3)

H$_3$CCH$_3$ → C$_6$H$_6$: **−126.4** (1.1; −127.5) ; **−5.1** (−7.2; 2.1)

Effect:[a]

H$_2$C=O C=O : **−145.9** (13.1; −159.0)

H$_3$COH → H(HO)C=O CO$_2$: **−110.5** (13.3; −123.9) ; **35.4** (0.2; 35.1)

Scheme 3 Pre-α, α, β, γ and δ effects calculated in alkanes and the related species (a) and the α-X, β-X and i-X effects and the effects from the characteristic bonds and groups (b) calculated with the GIAO method under B3LYP/BSS-A.

Origin of the α effect

A downfield shift of approximately 10–15 ppm is usually observed for the α effect, which is well supported by the calculated $(\Delta\sigma^d(C)_e, \Delta\sigma^p(C)_e, \Delta\sigma^t(C)_e)$ values of $(−0.4, −15.6, −15.9$ ppm) for CH$_3$CH$_3$ from CH$_4$ (see Table 4 and Scheme 3).

Table 7 lists the $\sigma^d(C)$, $\sigma^p(C)$ and $\sigma^t(C)$ values of C$_2$H$_6$, separately for each MO. Similar to the case of H$_4$C, the first and

Fig. 3 Plots of $\delta(\text{C: S})_{\text{obsd:TMS}}$ versus $-\Delta\sigma^t(\text{C: S})_{\text{calcd:TMS}}$ for **1–56** and S21–S70, CH_3X, CH_2X_2, CHX_3 and CX_4 (X = F, Cl and Br).

Fig. 5 Plots of $\sigma^d(C)$ versus $Q(C)$ for various species, **1–56**, except for $H_kC^{(4-k)-}$ (**1–4**), collected in Table 4.

Fig. 4 Plots of $\sigma^d(N: N = C, O$ and Se) versus $Q(N)$ for N^{6+}, N^{4+}, N^{2+}, N^0, N^{2-} and/or N^{4-}, drawn from the red (C), blue (O) and black (Se) curves. The plot of $\sigma^d(C)$ versus $Q(C)$ for C^{4-}, CH_2^{2-}, CH_3^- and CH_4 is also shown by the red hollow circles.

Table 5 The $\sigma^d(C)$, $\sigma^P(C)$ and $\sigma^t(C)$ values for C^{4-}, H_2C^{2-}, H_3C^- and H_4C, given separately by each MO[a]

MO (i in ψ_i)	$\sigma_i^d(C)$	$\sigma_i^P(C)$	$\sigma_i^t(C)$
$\mathbf{C^{4-}}$ $(\boldsymbol{O_h})$[b]			
1 (A1g)	200.45	0.00	200.45
2 (A1g)	31.72	0.00	31.72
3 (T1u)–5 (T1u)	42.04	0.00	42.04
Total	274.39	0.00	274.39
$\mathbf{H_2C^{2-}}$ $(\boldsymbol{C_{2v}})$			
1 (A1)	200.37	0.00	200.37
2 (A1)	23.73	−8.06	15.68
3 (B2)	1.27	−93.29	−92.02
4 (A1)	20.18	−16.17	4.01
5 (B1)	16.41	197.59	214.00
ψ_{occ} to ψ_{occ}		57.39	
Total	261.96	137.46	399.42
$\mathbf{H_3C^-}$ $(\boldsymbol{C_{3v}})$			
1 (A1)	200.32	0.00	200.32
2 (A1)	24.93	−3.19	21.74
3 (E)–4 (E)	3.28	−148.47	−145.19
5 (A1)	21.00	24.22	45.22
ψ_{occ} to ψ_{occ}		125.17	
Total	249.52	−2.26	247.26
$\mathbf{H_4C}$ $(\boldsymbol{T_d})$			
1 (A1)	200.28	0.00	200.28
2 (A1)	26.97	0.33	27.30
3 (T2)–5 (T2)	11.73	−175.52	−163.83
ψ_{occ} to ψ_{occ}		125.55	
Total	238.98	−49.66	189.32

[a] Calculated with the GIAO-DFT method under B3LYP/BSS-A. [b] MOs of ψ_1, ψ_2, ψ_3, ψ_4 and ψ_5 of C^{4-} are constructed mainly by 1s(C), 2s(C), $2p_x$(C), $2p_y$(C) and $2p_z$(C) AOs, respectively.

second inner MOs of ψ_1 and ψ_2 are constructed by the 1s(C) AOs; therefore, they greatly contribute to $\sigma^d(C)$ but not $\sigma^P(C)$. The third and fourth inner MOs of ψ_3 and ψ_4 are formed mainly by the 2s(C) AOs; therefore, they contribute to $\sigma^d(C)$ and $\sigma^P(C)$, more or less. The outer MOs of ψ_5–ψ_9 are constructed mainly by the 2p(C) AOs with the 1s (H) AOs; therefore, they contribute largely to $\sigma_i^P(C)$ (−36.6 to −42.3 ppm), with very small contributions to $\sigma^d(C)$ (−4.1 to 8.0 ppm). Table 8 lists the $\psi_i \rightarrow \psi_a$ transitions contributing to $\sigma_{i \rightarrow a:kk}^P(C: k = x, y$ and/or $z)$, where

Table 6 Main contributions from the occupied-to-unoccupied orbital transitions on $\sigma^p(C)$, exemplified by H_2C^{2-} and H_4C.[a]

$i \to a$[b]	$\sigma^p_{i\to a:xx}(C)$	$\sigma^p_{i\to a:yy}(C)$	$\sigma^p_{i\to a:zz}(C)$	$\sigma^p_{i\to a}(C)$
H_2C^{2-} (C_{2v})				
$3 \to 9$	0.00	0.00	−113.76	−37.92
$4 \to 7$	72.46	0.00	0.00	24.15
$4 \to 9$	0.00	−87.63	0.00	−29.21
$5 \to 6$	0.00	216.63	0.00	72.21
$5 \to 7$	0.00	0.00	225.75	75.25
$5 \to 8$	0.00	143.42	0.00	47.81
CH_4 (T_d)				
$3 \to 15$	−33.27	0.00	0.00	−11.09
$3 \to 16$	0.00	−33.27	0.00	−11.09
$4 \to 14$	−33.27	0.00	0.00	−11.09
$4 \to 16$	0.00	0.00	−33.27	−11.09
$5 \to 14$	0.00	−33.27	0.00	−11.09
$5 \to 15$	0.00	0.00	−33.27	−11.09

[a] Calculated with the GIAO method under B3LYP/BSS-A. [b] The magnitudes of $\sigma^p_{i\to a}(C)$ larger than 10 ppm are shown. In $\psi_i \to \psi_a$.

Table 7 The $\sigma^d(C)$, $\sigma^p(C)$ and $\sigma^t(C)$ values contributed from each MO of CH_3CH_3 (D_{3d})[a]

MO (i in ψ_i)	$\sigma^d_i(C)$	$\sigma^p_i(C)$	$\sigma^t_i(C)$
1 (A1g); 2 (A2u)	200.29	0.00	200.29
3 (A1g)	15.73	−3.49	12.24
4 (A2u)	17.28	5.92	23.20
5 (Eu)	2.78	−36.60	−33.81
6 (Eu)	2.78	−36.74	−33.95
7 (A1g)	7.97	−42.31	−34.34
8 (Eg)	−4.12	−36.94	−41.06
9 (Eg)	−4.12	−36.94	−41.06
ψ_{occ} to ψ_{occ}		121.88	
Total	238.60	−65.21	173.39

[a] Calculated with the GIAO-DFT method under B3LYP/BSS-A.

Table 8 Main contributions from the $\psi_i \to \psi_a$ transitions on $\sigma^p_{i\to a:kk}$(C: $k = x$, y and/or z) of CH_3CH_3 (D_{3d})[a,b]

$i \to a$[b]	$\sigma^p_{i\to a:xx}(C)$	$\sigma^p_{i\to a:yy}(C)$	$\sigma^p_{i\to a:zz}(C)$	$\sigma^p_{i\to a}(C)$
$5 \to 29$	0.00	−20.97	0.00	−6.99
$6 \to 29$	−20.53	0.00	0.00	−6.84
$7 \to 26$	−25.48	0.00	0.00	−8.49
$7 \to 27$	0.00	−25.47	0.00	−8.49
$8 \to 27$	0.00	−0.54	−21.14	−7.23
$9 \to 26$	0.00	−0.54	−21.16	−7.23

[a] Calculated with the GIAO method under B3LYP/BSS-A. Magnitudes of $\sigma^p_{i\to a}(C)$ larger than 6 ppm are shown. [b] In $\psi_i \to \psi_a$.

Fig. 6 Contributions from each $\psi_i \to \psi_a$ transition to the components of $\sigma^p(C)$ in H_2C^{2-} (a) and H_4C (b) with an isovalue of 0.04 au.

ppm), $\psi_7 \to \psi_{27}$ $\sigma^p_{7\to 27:yy}(C) = -25.5$ ppm), $\psi_8 \to \psi_{27}$ ($\sigma^p_{8\to 27:zz}(C) = -21.1$ ppm) and $\psi_9 \to \psi_{26}$ ($\sigma^p_{9\to 26:zz}(C) = -21.2$ ppm) contribute a lot to $\sigma^p_{i\to a:kk}$(C: $k = x$, y and/or z).

Fig. 7 shows the selected transitions of CH_3CH_3 (D_{3d}), as shown in Table 8. The occupied-to-unoccupied MO transitions play an important role in the α effect in CH_3CH_3. While the HOMO of ψ_9 acts as a good donor, the LUMOs of ψ_{10} and ψ_{11}–ψ_{25} do not seem to contribute substantially to the transitions.
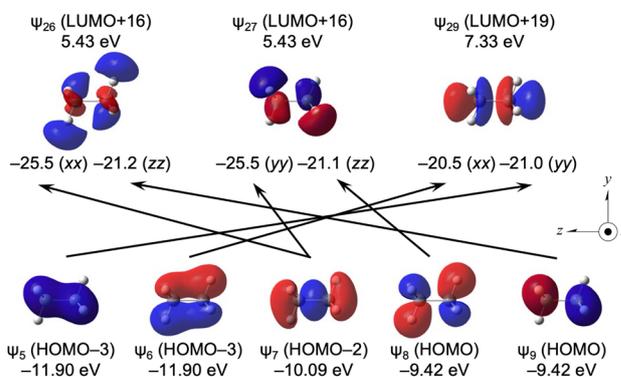
Fig. 7 Contributions from each $\psi_i \to \psi_a$ transition to the $\sigma^p_{i\to a:kk}$(C: $k = x$, y and/or z) in CH_3CH_3 with an isovalue of 0.04 au.

a larger than *ca.* 20 ppm in magnitude. The $\psi_i \to \psi_a$ transitions of $\psi_5 \to \psi_{29}$ ($\sigma^p_{5\to 29:yy}(C) = -21.0$ ppm), $\psi_6 \to \psi_{29}$ ($\sigma^p_{6\to 29:xx}(C) = -20.5$ ppm), $\psi_7 \to \psi_{26}$ ($\sigma^p_{7\to 26:xx}(C) = -25.5$

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Table 9 The $\sigma^d(C)$, $\sigma^P(C)$ and $\sigma^t(C)$ values contributed from each MO of $CH_3CH_2CH_3$ $(C_{2v})^a$

MO (i in ψ_i)	$\sigma^d(C)$	$\sigma^P(C)$	$\sigma^t(C)$
1 (A1)–3 (A1)	200.29	0.00	200.29
4 (A1)	16.20	−2.72	13.48
5 (B2)	6.36	−1.23	5.13
6 (A1)	16.89	4.51	21.39
7 (B1)	4.00	−33.20	−29.20
8 (A1)	7.27	−21.55	−14.28
9 (B2)	11.57	2.10	13.68
10 (A2)	−0.60	−2.62	−3.22
11 (B2)	0.28	−29.63	−29.35
12 (A1)	−5.18	−48.71	−53.89
13 (B1)	−5.87	−41.71	−47.58
ψ_{occ} to ψ_{occ}		83.64	
Total	251.23	−91.12	160.10

^{a} Calculated with the GIAO-DFT method under B3LYP/BSS-A.

Table 10 Main contributions from the $\psi_i \rightarrow \psi_a$ transitions on $\sigma^P_{i \rightarrow a:kk}$(C: $k = x$, y and/or z) in $CH_3CH_2CH_3$ $(C_{2v})^{a,b}$

| $i \rightarrow a^c$	$\sigma^P_{i \rightarrow a:xx}(C)$	$\sigma^P_{i \rightarrow a:yy}(C)$	$\sigma^P_{i \rightarrow a:zz}(C)$	$\sigma^P_{i \rightarrow a}(C)$
8→41	−15.15	0.00	0.00	−5.05
11→36	0.00	0.00	−20.07	−6.69

^{a} Calculated with the GIAO method under B3LYP/BSS-A. ^{b} The magnitudes of $\sigma^P_{i \rightarrow a}(C)$ larger than 5 ppm are shown. ^{c} In $\psi_i \rightarrow \psi_a$.

Origin of the β effect

A downfield shift of approximately 10 ppm is often observed for the β effect. The β effect is evaluated for $CH_3CH_2CH_3$ (C_{2v}), $(CH_3)_2CHCH_3$ (C_{3v}) and $(CH_3)_3CCH_3$ from the corresponding species. The calculated $(\Delta\sigma^d(C)_e, \Delta\sigma^P(C)_e, \Delta\sigma^t(C)_e)$ values for the species are $(−5.8, −3.5, −9.3$ ppm), $(−4.2, −4.3, −8.5$ ppm) and $(−2.9, −4.5, −7.4$ ppm), respectively, which reproduce the observed β effect well (see Table 4 and Scheme 3).

Table 9 lists the $\sigma^d(C)$, $\sigma^P(C)$ and $\sigma^t(C)$ values for $CH_3CH_2CH_3$ (C_{2v}) separately by ψ_i. The contributions from ψ_7, ψ_8, ψ_{11}, ψ_{12} and ψ_{13} to $\sigma^P_i(C)$ are large ($−21.6$ to $−48.7$ ppm), although the contributions seem to be widely distributed to ψ_i. Table 10 shows the main $\psi_i \rightarrow \psi_a$ transitions contributing to $\sigma^P_{i \rightarrow a:kk}$(C: $k = x$, y and/or z). The contributions are relatively large for $\psi_8 \rightarrow$
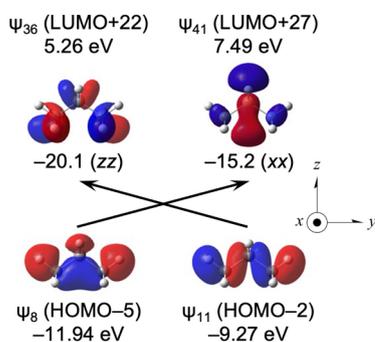
Fig. 8 Contributions from each $\psi_i \rightarrow \psi_a$ transition to the $\sigma^P_{i \rightarrow a:kk}$(C: $k = x$, y and/or z) of $CH_3CH_2CH_3$ with an isovalue of 0.04 au.

ψ_{41} $(\sigma^P_{8 \rightarrow 41:xx}(C) = −15.2$ ppm) and $\psi_{11} \rightarrow \psi_{36}$ $(\sigma^P_{11 \rightarrow 36:zz}(C) = −20.1$ ppm).

Fig. 8 shows the $\psi_8 \rightarrow \psi_{41}$ and $\psi_{11} \rightarrow \psi_{36}$ transitions, together with the orbital energies and the axes of $CH_3CH_2CH_3$. The transitions are well visualized. However, it is curious that ψ_{14} (LUMO) and those near it seem not to operate effectively as acceptors in the transitions. Similar results are obtained for $EtMeCH_2$, i-$PrMeCH_2$ and t-$BuMeCH_2$ from the corresponding species. The calculated $(\Delta\sigma^d(C)_e, \Delta\sigma^P(C)_e, \Delta\sigma^t(C)_e)$ values are $(−6.9, −2.5, −9.4$ ppm), $(−1.8, −5.5, −7.4$ ppm) and $(0.2, −7.0, −6.8$ ppm), respectively, for the species. For ionic $EtH_2C^−$, t-$BuH_2C^−$ and EtH_2C^+, the calculated $(\Delta\sigma^d(C)_e, \Delta\sigma^P(C)_e, \Delta\sigma^t(C)_e)$ values are predicted to be $(−2.0, 16.3, 14.3$ ppm), $(−4.9, 12.2, 7.3$ ppm) and $(0.4, 79.4, 79.8$ ppm) respectively, from the corresponding species. The (large) upfield shifts are again predicted for the β effect for the ionic species. A large positive $\Delta\sigma^t(C)_e$ value of 79.8 ppm is predicted for EtH_2C^+ from the corresponding species. The vacant 2p(C) orbital in EtH_2C^+ is responsible for these results.

Origin of the γ and δ effects

An upfield shift of $\sim$2 ppm is often encountered for the γ effect. The conformational effect cannot be avoided in the γ and δ effects,[9] contrary to the α and β effects in the cases of CH_4, CH_3CH_3 and $CH_3CH_2CH_3$, as discussed above. The γ and δ effects are not discussed further here since they are negligibly small.

Origin of the α-X and β-X effects

The α-X effect is examined for $CH_3–X$ from CH_4 and $CH_3CH_2–X$ from CH_3CH_3 (X = OH, SH, SeH, SSCH_3, F, Cl, Br, I, CO_2Me, CN, NH_2 and/or NO_2) (see Scheme 3, Table 4 and Table S11 of the ESI†). The $(\Delta\sigma^d(C)_e, \Delta\sigma^P(C)_e, \Delta\sigma^t(C)_e)$ values of $(−18.7$–$40.3, −76.4$–$−11.1, −82.3$–$−4.4$ ppm) are predicted for the species. The β-X effect is similarly examined for $CH_3CH_2–X$ from CH_3CH_3 (X = OH, SH, SeH, SSCH_3, F, Cl, Br, I, CO_2Me, CN, NH_2 and NO_2) (see Scheme 3, Table 4 and Table S11 of the ESI†). The $(\Delta\sigma^d(C)_e, \Delta\sigma^P(C)_e, \Delta\sigma^t(C)_e)$ values of $(−16.8$–$0.9, −66.9$–$14.1, −77.2$–$−1.3$ ppm) are calculated for the species. It seems difficult to find a good relation between the α-X and β-X effects in the same species, as a whole. However, such relation could be found is the species are divided to some groups, as shown in Fig. S10 of the ESI.† The β-X effect of $−77.2$ ppm for X = F is notable.

Table 11 lists the $\sigma^d(C)$, $\sigma^P(C)$ and $\sigma^t(C)$ values for CH_3CH_2OH and CH_3CH_2OH, separately for each MO. The outer MOs of HOMO (ψ_{13}), HOMO–1 (ψ_{12}), HOMO-4 (ψ_9) and HOMO–5 (ψ_8) contribute greatly to $\sigma^P(C)$ in CH_3CH_2OH. On the other hand, the outer MOs of HOMO-2 (ψ_{11}) and HOMO–3 (ψ_{10}) contribute greatly to $\sigma^P(C)$ in CH_3CH_2OH. Table 12 lists the $\psi_i \rightarrow \psi_a$ transitions contributing to $\sigma^P_{i \rightarrow a:kk}$(C: $k = x$, y and/or z), which are greater than 5 ppm in magnitude. The contributions from the $\psi_i \rightarrow \psi_a$ transitions seem greater for $\psi_8 \rightarrow \psi_{38}$ $(\sigma^P_{8 \rightarrow 33:xx}(C) = −13.1$ ppm and $\sigma^P_{8 \rightarrow 33:yy}(C) = −3.2$ ppm) in CH_3CH_2OH. The contributions are greater for $\psi_{10} \rightarrow \psi_{31}$ $(\sigma^P_{10 \rightarrow 31:yy}(C) =$

Table 11 The $\sigma^d(C)$, $\sigma^P(C)$ and $\sigma^t(C)$ values of CH_3CH_2OH, given separately by each ψ_i[a]

| MO (i in ψ_i)	$\sigma_i^d(C)$	$\sigma_i^P(C)$	$\sigma_i^t(C)$
CH_3CH_2OH (C_s)			
1 (A′)–3 (A′)	200.33	0.00	200.32
4 (A′)–6 (A′)	30.44	−6.12	24.33
7 (A′)	4.08	−28.13	−24.05
8 (A″)	4.62	−50.64	−46.02
9 (A′)	−4.90	−48.07	−52.97
10 (A′)	−2.22	−9.91	−12.13
11 (A″)	−1.61	−16.19	−17.80
12 (A′)	1.21	−47.21	−46.00
13 (A″)	−6.00	−27.71	−33.70
ψ_{occ} to ψ_{occ}		125.61	
Total	225.95	−108.36	117.60
CH_3CH_2OH (C_s)			
1 (A′)–3 (A′)	200.27	−0.03	200.24
4 (A′)–6 (A′)	30.09	0.84	31.14
7 (A′)	2.12	−5.52	−3.41
8 (A″)	3.12	−18.92	−15.80
9 (A′)	15.42	−6.30	9.12
10 (A′)	−3.19	−72.62	−75.82
11 (A″)	−2.25	−50.07	−52.31
12 (A′)	0.94	−20.25	−19.32
13 (A″)	−1.18	−2.31	−3.50
ψ_{occ} to ψ_{occ}		93.77	
Total	245.33	−81.19	164.14

[a] Calculated with the GIAO method under B3LYP/BSS-A.

Table 12 Main contributions from the $\psi_i \rightarrow \psi_a$ transitions on $\sigma_{i\rightarrow a:kk}^P(C: k = x, y \text{ and/or } z)$ in CH_3CH_2OH[a,b]

$i \rightarrow a$[c]	$\sigma_{i\rightarrow a:xx}^P(C)$	$\sigma_{i\rightarrow a:yy}^P(C)$	$\sigma_{i\rightarrow a:zz}^P(C)$	$\sigma_{i\rightarrow a}^P(C)$
CH_3CH_2OH (C_s)				
8→33	−13.09	−3.24	0.00	−5.44
CH_3CH_2OH (C_s)				
10→31	−3.47	−28.67	0.00	−10.71
10→35	0.00	0.00	−17.07	−5.69
10→59	0.00	0.00	−15.29	−5.10

[a] Calculated with the GIAO method under B3LYP/BSS-A. [b] The magnitudes of $\sigma_{i\rightarrow a}^P(C)$ larger than 5 ppm are shown. [c] In $\psi_i \rightarrow \psi_a$.

−28.7 ppm), $\psi_{10} \rightarrow \psi_{35}$ ($\sigma_{10\rightarrow35:zz}^P(C) = -17.1$ ppm) and $\psi_{10} \rightarrow \psi_{59}$ ($\sigma_{10\rightarrow59:zz}^P(C) = -15.36$ ppm) in CH_3CH_2OH.

Fig. 9a shows the $\psi_8 \rightarrow \psi_{33}$ transition in CH_3CH_2OH and the $\psi_{10} \rightarrow \psi_{31}$, $\psi_{10} \rightarrow \psi_{35}$ and $\psi_{10} \rightarrow \psi_{59}$ transitions in CH_3CH_2OH are illustrated in Fig. 9b. The α-X and β-X effects are well visualized, employing the $\psi_i \rightarrow \psi_a$ transitions.

The α-X effect is also typical detected in CH_3NH_2 and CH_3NO_2. The $\sigma^d(C)$, $\sigma^P(C)$ and $\sigma^t(C)$ values for CH_3NH_2 and CH_3NO_2 are listed in Table S13 of the ESI,† separately for each MO. In the case of CH_3NH_2, which has a very strong electron donating X of NH_2, the outer MOs of the HOMO−1 (ψ_8) ∼ HOMO−3 (ψ_6) contribute greatly to $\sigma^P(C)$. In the case of CH_3NO_2, with the very strong electron accepting group X of NO_2, the somewhat more inner HOMO−3 (ψ_{13}) and HOMO−4 (ψ_{12}) also
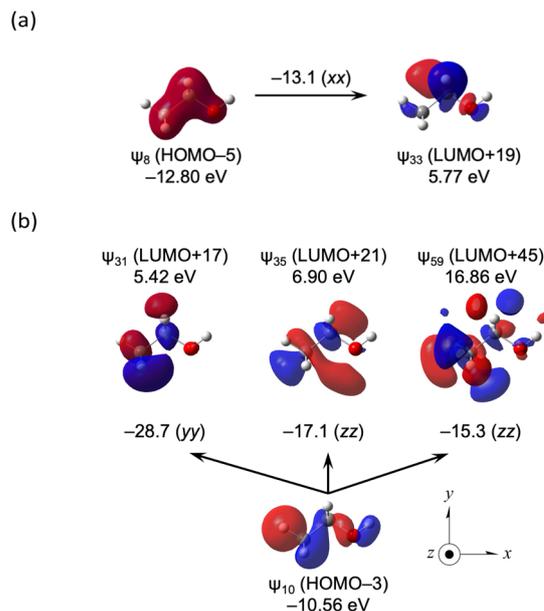
Fig. 9 Contributions from each $\psi_i \rightarrow \psi_a$ transition to the components of $\sigma^P(C)$ for CH_3CH_2OH (a) and CH_3CH_2OH (b), together with the axes with an isovalue of 0.04 au.

strongly affect $\sigma^P(C)$. The $\psi_i \rightarrow \psi_a$ transitions contributing to $\sigma_{i\rightarrow a:kk}^P(C: k = x, y \text{ and/or } z)$ from the species are collected in Table S14 of the ESI.† The contributions to CH_3NH_2 are large for the $\psi_i \rightarrow \psi_a$ transitions of $\psi_7 \rightarrow \psi_{26}$ ($\sigma_{7\rightarrow26:zz}^P(C) = -19.9$ ppm), $\psi_7 \rightarrow \psi_{41}$ ($\sigma_{7\rightarrow41:zz}^P(C) = -18.8$ ppm), $\psi_8 \rightarrow \psi_{23}$ ($\sigma_{8\rightarrow23:yy}^P(C) = -31.4$ ppm) and $\psi_8 \rightarrow \psi_{26}$ ($\sigma_{8\rightarrow26:xx}^P(C) = -22.9$ ppm). Those in CH_3NO_2 are large for $\psi_{12} \rightarrow \psi_{28}$ ($\sigma_{12\rightarrow28:xx}^P(C) = -28.7$ ppm) and $\psi_{12} \rightarrow \psi_{29}$ ($\sigma_{12\rightarrow29:yy}^P(C) = -29.2$ ppm) and $\psi_{13} \rightarrow \psi_{28}$ ($\sigma_{13\rightarrow28:zz}^P(C) = -31.6$ ppm). The $\psi_i \rightarrow \psi_a$ transitions of $\psi_7 \rightarrow \psi_{26}$, $\psi_7 \rightarrow \psi_{41}$, $\psi_8 \rightarrow \psi_{23}$ and $\psi_8 \rightarrow \psi_{26}$ for CH_3NH_2 and those of $\psi_{12} \rightarrow \psi_{28}$, $\psi_{12} \rightarrow \psi_{29}$, $\psi_{13} \rightarrow \psi_{28}$ and $\psi_{13} \rightarrow \psi_{30}$ for CH_3NO_2 are shown in Fig. S11a and b of ESI,† respectively. The α-X effect is well visualized both for X of a very good donor and a very good acceptor, employing $\psi_i \rightarrow \psi_a$ transitions.

Effect from ethene and ethyne and the origin

Large downfield shifts in $\delta(C)$ are reported for ethene (∼120 ppm) and ethyne (∼60 ppm) from ethane.[1–4] The calculated ($\Delta\sigma^d(C)_e$, $\Delta\sigma^P(C)_e$ and $\Delta\sigma^t(C)_e$) values for $H_2C=CH_2$ and $HC\equiv CH$ from CH_3CH_3 are (8.3, −129.6, −121.3 ppm) and (17.0, −80.4, −63.3 ppm), respectively, which reproduce the observed results well.

Table 13 lists the $\sigma^d(C)$, $\sigma^P(C)$ and $\sigma^t(C)$ values of $H_2C=CH_2$ (D_{2h}) and $HC\equiv CH$ ($D_{\infty h}$), separately for each MO, whereas HOMO−1 (ψ_7) ∼ HOMO−3 (ψ_5) contribute a lot to $\sigma^P(C)$ in $H_2C=CH_2$ (D_{2h}), HOMO−2 (ψ_5) and HOMO−3 (ψ_4) strongly affect $HC\equiv CH$ ($D_{\infty h}$). Table 14 shows that the $\psi_i \rightarrow \psi_a$ transitions largely contribute to $\sigma^P(C)$ in $H_2C=CH_2$ (D_{2h}) and $HC\equiv CH$ ($D_{\infty h}$). The $\psi_i \rightarrow \psi_a$ transitions of $\psi_6 \rightarrow \psi_9$ ($\sigma_{6\rightarrow9:yy}^P(C) = -175.0$ ppm), $\psi_6 \rightarrow \psi_{17}$ ($\sigma_{6\rightarrow17:yy}^P(C) = -47.7$ ppm), $\psi_6 \rightarrow \psi_{37}$ ($\sigma_{6\rightarrow37:yy}^P(C) = -31.9$ ppm), $\psi_7 \rightarrow \psi_9$ ($\sigma_{7\rightarrow9:zz}^P(C) = -126.0$ ppm) and $\psi_7 \rightarrow \psi_{17}$

Table 13 The $\sigma^d(C)$, $\sigma^p(C)$ and $\sigma^t(C)$ values of $H_2C=CH_2$ (D_{2h}) and $HC\equiv CH$ ($D_{\infty h}$), given separately by each ψ_i[a]

MO (i in ψ_i)	$\sigma_i^d(C)$	$\sigma_i^p(C)$	$\sigma_i^t(C)$
$H_2C=CH_2$ (D_{2h})			
1 (Ag); 2 (B1u)	200.30	0.02	200.32
3 (Ag)	16.54	−10.56	5.98
4 (B1u)	13.95	−0.39	13.56
5 (B2u)	1.14	−33.89	−32.75
6 (Ag)	5.18	−112.14	−106.96
7 (B3g)	−7.49	−87.51	−94.99
8 (B3u)	17.28	−19.65	−2.37
ψ_{occ} to ψ_{occ}		69.30	
Total	246.91	−194.83	52.08
$HC\equiv CH$ ($D_{\infty h}$)			
1 (Σg); 2 (Σu)	200.21	−0.46	199.74
3 (Σg)	17.82	−22.76	−4.95
4 (Σu)	2.99	−34.63	−31.64
5 (Σg)	−2.03	−131.94	−133.97
6 (Πu)	18.32	−10.20	8.12
7 (Πu)	18.32	0.04	18.36
ψ_{occ} to ψ_{occ}		54.39	
Total	255.62	−145.56	110.06

[a] Calculated with the GIAO method under B3LYP/BSS-A.

Table 14 Main contributions from the $\psi_i \rightarrow \psi_a$ transitions in the $\sigma^p(C)$ of $H_2C=CH_2$ (D_{2h}) and $HC\equiv CH$ ($D_{\infty h}$)[a,b]

$i \rightarrow a$[c]	$\sigma_{i\rightarrow a:xx}^p(C)$	$\sigma_{i\rightarrow a:yy}^p(C)$	$\sigma_{i\rightarrow a:zz}^p(C)$	$\sigma_{i\rightarrow a}^p(C)$
$H_2C=CH_2$ (D_{2h})				
6→9	0.00	−174.98	0.00	−58.33
6→17	0.00	−47.66	0.00	−15.89
6→37	0.00	−31.93	0.00	−10.64
7→9	0.00	0.00	−126.04	−42.01
7→17	0.00	0.00	−32.05	−10.68
7→19	−21.82	0.00	0.00	−7.27
7→37	0.00	0.00	−16.43	−5.48
$HC\equiv CH$ ($D_{\infty h}$)				
5→10	0.00	−84.16	0.00	−28.05
5→11	−84.16	0.00	0.00	−28.05
5→17	−48.66	0.00	0.00	−16.22
5→18	0.00	−48.66	0.00	−16.22
5→30	−22.78	0.00	0.00	−7.59
5→31	0.00	−22.78	0.00	−7.59
5→37	−23.40	0.00	0.00	−7.80
5→38	0.00	−23.40	0.00	−7.80

[a] Calculated with the GIAO method under B3LYP/BSS-A. [b] The magnitudes of $\sigma_{i\rightarrow a}^p(C)$ larger than 5 ppm are shown. [c] In $\psi_i \rightarrow \psi_a$.

($\sigma_{7\rightarrow 17:zz}^p(C) = −32.1$ ppm) provide great contributions to $H_2C=CH_2$ (D_{2h}). Similarly, the transitions of $\psi_5 \rightarrow \psi_{10}$ ($\sigma_{5\rightarrow 10:yy}^p(C) = −84.2$ ppm), $\psi_5 \rightarrow \psi_{11}$ ($\sigma_{5\rightarrow 11:xx}^p(C) = −84.2$ ppm), $\psi_5 \rightarrow \psi_{17}$ ($\sigma_{5\rightarrow 17:xx}^p(C) = −48.7$ ppm) and $\psi_5 \rightarrow \psi_{18}$ ($\sigma_{5\rightarrow 18:yy}^p(C) = −48.7$ ppm) greatly contribute to $HC\equiv CH$ ($D_{\infty h}$).

Fig. 10a shows the $\psi_6 \rightarrow \psi_9$, $\psi_6 \rightarrow \psi_{17}$, $\psi_6 \rightarrow \psi_{37}$, $\psi_7 \rightarrow \psi_9$ and $\psi_7 \rightarrow \psi_{37}$ transitions in $H_2C=CH_2$ (D_{2h}), and Fig. 10b shows the $\psi_5 \rightarrow \psi_{10}$, $\psi_5 \rightarrow \psi_{11}$, $\psi_5 \rightarrow \psi_{17}$ and $\psi_5 \rightarrow \psi_{18}$ transitions in $HC\equiv CH$ ($D_{\infty h}$). The MO energies and axes are also shown in the figure.
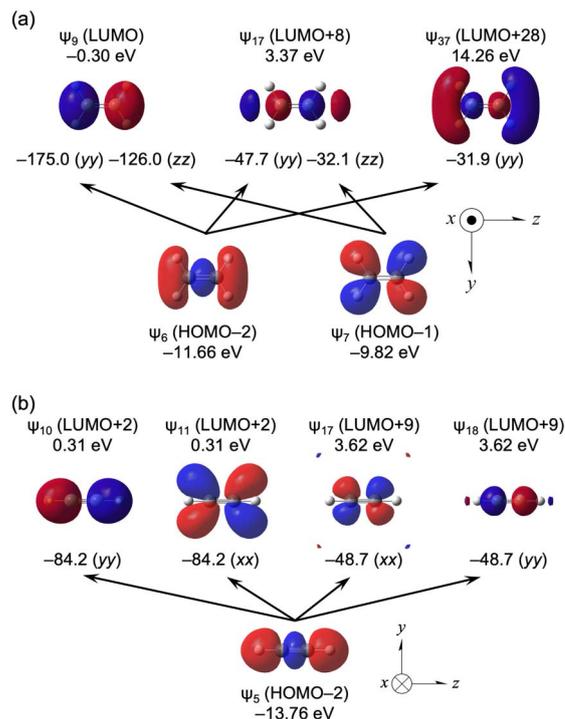
Fig. 10 Contributions from each $\psi_i \rightarrow \psi_a$ transition to the components of $\sigma^p(C)$ in $H_2C=CH_2$ (D_{2h}) (a) and $HC\equiv CH$ ($D_{\infty h}$) (b), together with the axes with an isovalue of 0.04 au.

The main characteristics of ψ_6, ψ_7, ψ_9, ψ_{17} and ψ_{37} with $H_2C=CH_2$ are occupied $\sigma(C=C)$, $\sigma(C-H)$, vacant $\pi^*(C=C)$, $\sigma^*(C-C)$ and $\sigma^*(C-H)$, respectively. The LUMO of ψ_9 acts as a great acceptor in the transition, whereas the HOMO of ψ_8 does not seem to do so. The main characteristic of ψ_5 in $HC\equiv CH$ is the occupied $\sigma(C-C)$, whereas those of ψ_{10} and ψ_{11} are the vacant $\pi^*(C=C)$, and those of ψ_{17} and ψ_{18} seem to be higher vacant $\pi^*(C=C)$. The HOMO and LUMO in $HC\equiv CH$ seem not to act as good donors and acceptors, respectively.

Effect of benzene and its origin

Large downfield shifts in $\delta(C)$ (~127 ppm) are reported for benzene.[1–4] The calculated $(\Delta\sigma^d(C)_e, \Delta\sigma^p(C)_e, \Delta\sigma^t(C)_e)$ values from CH_3CH_3 are (1.1, −127.5, −126.4 ppm). The calculations reproduced the observed results well.

Table 15 lists the $\sigma^d(C)$, $\sigma^p(C)$ and $\sigma^t(C)$ values of C_6H_6, separately, by ψ_i. The contributions from HOMO−2 (ψ_{19}), HOMO−5 (ψ_{16}) and HOMO−7 (ψ_{14}) are very large, together with HOMO−3 (ψ_{18}). Table 16 lists the $\psi_i \rightarrow \psi_a$ transitions that greatly contribute to $\sigma^p(C)$. The transitions of $\psi_{14} \rightarrow \psi_{22}$ ($\sigma_{14\rightarrow 22:yy}^p(C) = −95.9$ ppm), $\psi_{16} \rightarrow \psi_{22}$ ($\sigma_{16\rightarrow 22:xx}^p(C) = −95.3$ ppm), $\psi_{16} \rightarrow \psi_{78}$ ($\sigma_{16\rightarrow 78:xx}^p(C) = −40.1$ ppm) and $\psi_{19} \rightarrow \psi_{40}$ ($\sigma_{19\rightarrow 40:xx}^p(C) = −38.3$ ppm) contribute greatly, together with $\psi_{18} \rightarrow \psi_{40}$ ($\sigma_{18\rightarrow 40:yy}^p(C) = −43.9$ ppm) and $\psi_{18} \rightarrow \psi_{50}$ ($\sigma_{18\rightarrow 50:yy}^p(C) = −31.2$ ppm).

Fig. 11 shows the $\psi_i \rightarrow \psi_a$ transitions in C_6H_6, shown in Table 16, although they are limited to those discussed above, together with the MO energies and axes. The main characteristics of ψ_{14},

Table 15 The σ^d(C), σ^P(C) and σ^t(C) values of C_6H_6 (D_{6h}), given separately by each $\psi_i{}^a$

MO (i in ψ_i)	σ_i^d(C)	σ_i^P(C)	σ_i^t(C)
1 (A1g)	33.37	−0.01	33.37
2 (E1u)–6 (B1u)	167.08	0.17	167.23
7 (A1g)	5.82	−5.41	0.42
8 (E1u)	2.95	−4.84	−1.89
9 (E1u)	11.07	−3.02	8.05
10 (E2g)	0.88	−15.67	−14.78
11 (E2g)	7.07	2.34	9.41
12 (A1g)	1.95	−11.67	−9.72
13 (B2u)	3.33	−10.46	−7.13
14 (B1u)	2.84	−48.38	−45.54
15 (E1u)	6.87	−0.43	6.44
16 (E1u)	−19.97	−107.31	−127.28
17 (A2u)	8.37	−9.28	−0.91
18 (E2g)	1.65	−30.56	−28.91
19 (E2g)	−5.76	−48.14	−53.90
20 (E1g)	11.06	−11.58	−0.51
21 (E1g)	2.08	−1.36	0.72
ψ_{occ} to ψ_{occ}		111.93	
Total	240.68	−193.67	47.00

^{a} Calculated with the GIAO method under B3LYP/BSS-A.

Table 16 Main contributions from the $\psi_i \rightarrow \psi_a$ transitions in the σ^P(C) of C_6H_6 (D_{6h})^{a,b}

| $i \rightarrow a{}^c$	$\sigma_{i \rightarrow a:xx}^P$(C)	$\sigma_{i \rightarrow a:yy}^P$(C)	$\sigma_{i \rightarrow a:zz}^P$(C)	$\sigma_{i \rightarrow a}^P$(C)
3 → 22	−36.14	0.00	0.00	−12.05
14 → 22	0.00	−95.93	0.00	−31.98
15 → 22	0.00	−27.30	0.00	−9.10
16 → 22	−95.30	0.00	0.00	−31.77
16 → 68	0.00	0.00	−26.05	−8.68
16 → 78	−40.08	0.00	0.00	−13.36
16 → 93	0.00	0.00	−25.58	−8.53
16 → 117	0.00	0.00	−28.12	−9.37
18 → 40	0.00	−43.94	0.00	−14.65
18 → 50	0.00	−31.15	0.00	−10.38
19 → 40	−38.27	0.00	0.00	−12.76
19 → 50	−26.96	0.00	0.00	−8.99
19 → 59	0.00	0.00	−26.04	−8.68

^{a} Calculated with the GIAO method under B3LYP/BSS-A. ^{b} The magnitudes of $\sigma_{i \rightarrow a}^P$(C) larger than 8 ppm are shown. ^{c} In $\psi_i \rightarrow \psi_a$.

ψ_{16} and ψ_{19} are the occupied σ(C–C), σ(C–C) with σ(C–H) and σ(C–C) with σ(C–H), respectively, whereas those of ψ_{22}, ψ_{40} and ψ_{78} are vacant π*(C=C), π*(C_6H_6), and much higher π*(C_6H_6), respectively. The LUMO of ψ_{22} acts as a great acceptor in the transition, whereas the HOMO does not seem to do so.

Origin of the i-X effect

The i-X effect is examined for C_6H_5–X from C_6H_6 (X = OH, SH, SeH, F, Cl, Br, I, NH_2, CO_2Me, CN and NO_2) (see Scheme 3, Table 4 and Table S11 of the ESI†). The calculated ($\Delta\sigma^d$(C)$_e$, $\Delta\sigma^P$(C)$_e$, $\Delta\sigma^t$(C)$_e$) values are (−82.5–35.2, −74.9–70.5, −39.7–14.0 ppm) for the species.

The σ^d(C), σ^P(C) and σ^t(C) values of C_6H_5OH, are listed in Table S15 of the ESI,† separately for each MO. The outer MOs of
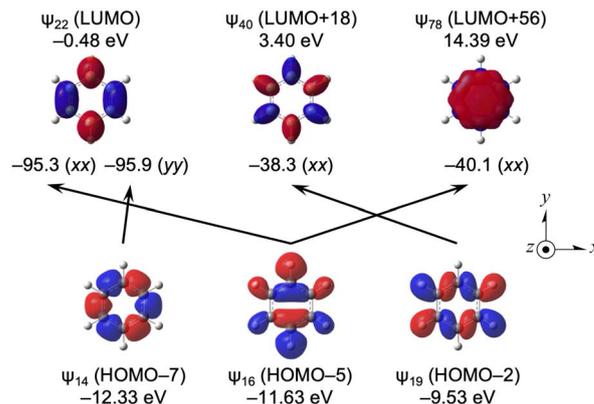
Fig. 11 Contributions from each $\psi_i \rightarrow \psi_a$ transition to the components of σ^P(C) in C_6H_6 (D_{6h}), together with their axes by the isovalue of 0.04 au.

HOMO−3 (ψ_{22}), HOMO−8 (ψ_{17}) and HOMO−9 (ψ_{16}) contribute greatly to σ^P(C). The $\psi_i \rightarrow \psi_a$ transitions contributing to $\sigma_{i \rightarrow a:kk}^P$(C: $k = x$, y and/or z), greater than 18 ppm, are listed in Table S16 of the ESI.† The $\psi_i \rightarrow \psi_a$ transitions of $\psi_{16} \rightarrow \psi_{28}$ ($\sigma_{16 \rightarrow 28:yy}^P$(C) = −53.5 ppm), $\psi_{17} \rightarrow \psi_{28}$ ($\sigma_{17 \rightarrow 28:xx}^P$(C) = −25.5 ppm), $\psi_{17} \rightarrow \psi_{87}$ ($\sigma_{17 \rightarrow 87:xx}^P$(C) = −24.9 ppm) and $\psi_{22} \rightarrow \psi_{44}$ ($\sigma_{22 \rightarrow 44:yy}^P$(C) = −28.1 ppm) contribute a lot to $\sigma_{i \rightarrow a:kk}^P$(C: $k = x$, y and/or z). The $\psi_i \rightarrow \psi_a$ transitions of $\psi_{16} \rightarrow \psi_{28}$, $\psi_{17} \rightarrow \psi_{28}$, $\psi_{17} \rightarrow \psi_{87}$ and $\psi_{22} \rightarrow \psi_{44}$ are drawn in Fig. S15 of the ESI,† where the transitions of large contributions are omitted if the contributions from ψ_i are small in C_6H_5OH. The i-X effect is well visualized through the occupied-to-unoccupied orbital transitions.

Effect of the carbonyl group and its origin

Very large downfield shifts of $\delta(^{13}C)$ (∼200 ppm) are usually observed for the carbonyl group.[1–4] The calculated ($\Delta\sigma^d$(C)$_e$, $\Delta\sigma^P$(C)$_e$, $\Delta\sigma^t$(C)$_e$) values for $H_2C=O$ from MeOH are (13.1, −159.0, −145.9 ppm), which explains the observed results well.

Table 17 lists the σ^d(C), σ^P(C) and σ^t(C) values of $H_2C=O$, separately, by ψ_i. The outer MOs of HOMO (ψ_8), HOMO−2 (ψ_6) and HOMO−3 (ψ_5) contribute a lot to σ^P(C), whose values amount to −95.7, −118.8 and −64.5 ppm, respectively. The $\psi_i \rightarrow \psi_a$ transitions of $\psi_5 \rightarrow \psi_9$ ($\sigma_{5 \rightarrow 9:zz}^P$(C) = −62.6 ppm), $\psi_6 \rightarrow \psi_9$

Table 17 The σ^d(C), σ^P(C) and σ^t(C) values of $H_2C=O$ (C_{2v}), given separately by each $\psi_i{}^a$

| MO (i in ψ_i)	σ^d(C)	σ^P(C)	σ^t(C)
1 (A1); 2 (A1)	200.29	−0.02	200.27
3 (A1)	7.42	−21.88	−14.46
4 (A1)	22.01	−2.20	19.82
5 (B2)	6.81	−64.47	−57.66
6 (A1)	1.98	−118.84	−116.86
7 (B1)	14.00	−13.21	0.79
8 (B2)	−7.32	−95.73	−103.05
ψ_{occ} to ψ_{occ}		52.70	
Total	245.20	−263.64	−18.44

^{a} Calculated with the GIAO method under B3LYP/BSS-A.

Table 18 Main contributions from the $\psi_i \to \psi_a$ transitions on the $\sigma^P(C)$ of $H_2C{=}O$ (C_{2v})^{a,b}

$i \to a^c$	$\sigma^P_{i \to a:xx}(C)$	$\sigma^P_{i \to a:yy}(C)$	$\sigma^P_{i \to a:zz}(C)$	$\sigma^P_{i \to a}(C)$
$5 \to 9$	0.00	0.00	−62.57	−20.86
$6 \to 9$	0.00	−195.32	0.00	−65.11
$6 \to 13$	0.00	−30.34	0.00	−10.11
$8 \to 9$	0.00	0.00	−185.66	−61.89

^{a} Calculated with the GIAO method under B3LYP/BSS-A. ^{b} The magnitudes of $\sigma^P_{i \to a}(C)$ larger than 10 ppm are shown. ^{c} In $\psi_i \to \psi_a$.
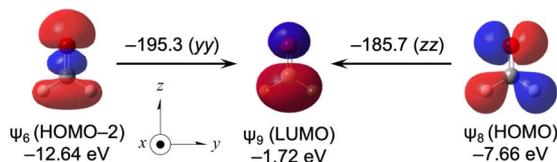
Fig. 12 Contributions from each $\psi_i \to \psi_a$ transition to the components of $\sigma^P(C)$ in $H_2C{=}O$ (C_{2v}), together with the axes with an isovalue of 0.04 au.

($\sigma^P_{6 \to 9:yy}(C) = -195.3$ ppm), $\psi_6 \to \psi_{13}$ ($\sigma^P_{6 \to 13:yy}(C) = -30,3$ ppm) and $\psi_8 \to \psi_9$ ($\sigma^P_{8 \to 9:zz}(C) = -185.7$ ppm) contribute predominantly to $\sigma_{i \to a}^P$, as shown in Table 18.

Fig. 12 shows the $\psi_6 \to \psi_9$ and $\psi_8 \to \psi_9$ transitions of $H_2C{=}O$, along with the MO energies and the molecular axes. The main characteristics of ψ_6, ψ_8 and ψ_9 are the occupied $\sigma(C{=}O)$, $n_p(C)$ and vacant $\pi^*(C{=}O)$, respectively. HOMO (ψ_8) and LUMO (ψ_9) act as excellent donors and acceptors, respectively, to produce very large $\sigma^P(C)$ values in $H_2C{=}O$. HOMO−1 (ψ_7) ($\pi(C{=}O)$) in $H_2C{=}O$ does not seem to act as a good donor, contrary to the excellent donors of HOMO (ψ_8) ($n_p(C)$) and HOMO−2 (ψ_6) ($\sigma(C{=}O)$).

Effect of the carboxyl group and its origin

The carboxyl effect is closely related to the carbonyl effect. Very large downfield shifts of $\delta(^{13}C)$ (∼180 ppm) are usually recorded for the carboxyl group.[1–4] The calculated ($\Delta\sigma^d(C)_e$, $\Delta\sigma^P(C)_e$,

Table 19 The $\sigma^d(C)$, $\sigma^P(C)$ and $\sigma^t(C)$ values of $H(HO)C{=}O$ (C_s), given separately by each $\psi_i{}^a$

MO (i in ψ_i)	$\sigma^d(C)$	$\sigma^P(C)$	$\sigma^t(C)$
1 (A′)–3 (A′)	200.31	−0.03	200.28
4 (A′)	8.56	−8.27	0.29
5 (A′)	3.00	−23.65	−20.65
6 (A′)	13.84	−11.59	2.25
7 (A′)	6.02	−68.76	−62.74
8 (A′)	5.29	−30.62	−25.34
9 (A″)	14.46	−20.58	−6.13
10 (A′)	−4.35	−86.16	−90.51
11 (A″)	1.96	−0.95	1.01
12 (A′)	−3.59	−24.60	−28.19
ψ_{occ} to ψ_{occ}		46.69	
Total	245.49	−228.53	16.97

^{a} Calculated with the GIAO method under B3LYP/BSS-A.

Table 20 Main contributions from the $\psi_i \to \psi_a$ transitions on $\sigma^P(C)$ of $H(HO)C{=}O$ (C_s)^{a,b}

$i \to a^c$	$\sigma^P_{i \to a:xx}(C)$	$\sigma^P_{i \to a:yy}(C)$	$\sigma^P_{i \to a:zz}(C)$	$\sigma^P_{i \to a}(C)$
$5 \to 13$	−0.10	−30.55	0.00	−10.22
$7 \to 13$	−83.72	−12.66	0.00	−32.13
$8 \to 13$	−0.90	−38.10	0.00	−13.00
$10 \to 13$	−29.23	−108.63	0.00	−45.95
$12 \to 13$	−45.55	2.78	0.00	−14.25

^{a} Calculated with the GIAO method under B3LYP/BSS-A. ^{b} The magnitudes of $\sigma^P_{i \to a}(C)$ larger than 10 ppm are shown. ^{c} In $\psi_i \to \psi_a$.
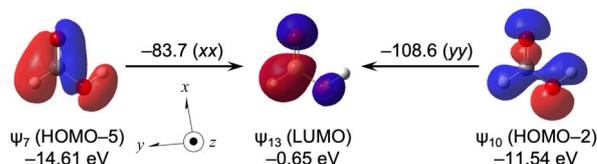
Fig. 13 Contributions from each $\psi_i \to \psi_a$ transition to the components of $\sigma^P(C)$ in $H(HO)C{=}O$ (C_s), together with the axes with an isovalue of 0.04 au.

$\Delta\sigma^t(C)_e$) values are (13.3, −123.9, −111.5 ppm) for $H(OH)C{=}O$ from MeOH, which explains the observed results well.

Table 19 lists the $\sigma^d(C)$, $\sigma^P(C)$ and $\sigma^t(C)$ values of $H(HO)C{=}O$, separately, by ψ_i. The contributions from HOMO−2 (ψ_{10}) and HOMO−5 (ψ_7) to $\sigma_i^P(C)$ are very large, with values of −86.2 and −68.8 ppm, respectively. Table 20 lists the $\psi_i \to \psi_a$ transition in $H(HO)C{=}O$, which mainly contributes to $\sigma^P_{i \to a:kk}$(C: $k = x$, y and/or z), larger than approximately 10 ppm. The $\psi_i \to \psi_a$ transitions of $\psi_7 \to \psi_{13}$ ($\sigma^P_{7 \to 13:xx}(C) = -83.7$ ppm with $\sigma^P_{7 \to 13:yy}(C) = -12.7$ ppm), $\psi_8 \to \psi_{13}$ ($\sigma^P_{8 \to 13:yy}(C) = -38.1$ ppm) and $\psi_{10} \to \psi_{13}$ ($\sigma^P_{10 \to 13:yy}(C) = -108.6$ ppm with $\sigma^P_{10 \to 13:xx}(C) = -29.2$ ppm) contribute predominantly to $\sigma^P_{i \to a}(C)$, together with $\psi_5 \to \psi_{13}$ ($\sigma^P_{5 \to 13:yy}(C) = -30.6$ ppm) and $\psi_{12} \to \psi_{13}$ ($\sigma^P_{12 \to 13:xx}(C) = -45.6$ ppm).

Fig. 13 shows the $\psi_7 \to \psi_{13}$ and $\psi_{10} \to \psi_{13}$ transitions in $H(HO)C{=}O$, along with the MO energies and the molecular axes. The characters of ψ_7 and ψ_{10} are the occupied $\sigma(O{-}C{=}O)$ of A′ spread over the whole molecule, whereas that of ψ_{13} is the vacant $\pi^*(O{-}C{=}O)$. While ψ_7 and ψ_{10} operate as excellent donors, ψ_{13} (LUMO) is an excellent acceptor in $H(HO)C{=}O$.

The ($\Delta\sigma^d(C)_e$, $\Delta\sigma^P(C)_e$, $\Delta\sigma^t(C)_e$) values are (13.3, −123.9, −111.5 ppm) for $H(HO)C{=}O$ from CH_3OH, as mentioned above. However, the values for the conversion of $H(HO)C{=}O$ from $H_2C{=}O$ are also of interest. The values are (0.3, 35.1, 35.4 ppm). Specifically, the NMR signal of $H(HO)C{=}O$ is predicted to appear at a higher field of approximately 35 ppm than that of $H_2C{=}O$. The specific π-allyl type $O{-}C{=}O$ interaction is responsible for these results. The charge on C of $H(HO)C{=}O$ is less positive than that of $H_2C{=}O$ because of the donation from HO to $C{=}O$ in $H(HO)C{=}O$, which should lead to an upfield shift.

It is necessary to consider the effect of the wider extension of the MOs over the entire molecule in $H(HO)C{=}O$. One explanation is as follows: It does not directly increase the $\sigma^P(C)$ value

when the occupancy of electrons becomes higher at the carbon atom in question in an important orbital of $H(HO)C=O$ relative to the case of $H_2C=O$. The energy differences between the two orbitals that make up the transitions also affect $\sigma^p(C)$. Nevertheless, a more upfield shift in $\sigma^p(C)$ is expected to be predicted when the charge on C becomes less positive. However, more complex mechanisms control the real shift values.

The analysis of $H_2C=O$ and $H(HO)C=O$ will help to understand the $\delta(C)$ values of similar structures. The upfield shifts in $RC(=O)NHR'$ and $ROC(=O)OR'$ relative to $R_2C=O$ can also be understood based on the structural similarities to $R(R'O)C=O$. However, further investigations are necessary to understand the much greater downfield shifts of the species containing low-lying vacant orbitals, such as some cationic species, carbenes and radicals.

Illustration of the terms used to control $\Delta\sigma^t(C)$

The $\Delta\sigma^d(C)$, $\Delta\sigma^p(C)$, $\Delta\sigma^t(C)$ ($=\Delta\sigma^d(C) + \Delta\sigma^p(C)$) values and the components are plotted for CH_3CH_3, $CH_2=CH_2$, $CH\equiv CH$, C_6H_6 and $H_2C=O$. Fig. 14 shows the plot. The $\Delta\sigma^d(C)$ and $\Delta\sigma^p(C)$ values are all negative for the species, where C^{4-} is taken as the standard. However, the contributions from the occupied-to-occupied (occ-to-occ) orbital ($\psi_i \rightarrow \psi_j$) transitions are all positive for the species shown in Fig. 14. The magnitudes of $\Delta\sigma^d(C)$ seem almost constant for the species, whereas those of $\Delta\sigma^p(C)$ change widely depending on the structure of the species, which increases the variety of the $\Delta\sigma^t(C)$ values. The magnitudes of $\Delta\sigma^t(C)$ ($=\Delta\sigma^d(C) + \Delta\sigma^p(C)$) increase in the order of $S=CH_3CH_3 < CH\equiv CH < CH_2=CH_2 < C_6H_6 < H_2C=O$, as expected. The $\sigma^p(C)$ values originate from the unsymmetric component of the electron distribution derived from the unsymmetric MOs on the unsymmetric structure of the species.

The unsymmetric MOs are constructed mainly by the $2p_x(C)$, $2p_y(C)$ and $2p_z(C)$ AOs. These MOs are expected to exist near the

HOMO; however, they sometimes reside in (much) deeper areas. The magnitudes of the terms, such as $\Delta\sigma^d(C)$, $\Delta\sigma^p(C)$, $\Delta\sigma^t(C)$ and the components, are well visualized in Fig. 14, which helps us to understand the plain rules founded in theory, supported by the origin and mechanism, for ^{13}C NMR chemical shifts.

The occupied-to-occupied orbital ($\psi_i \rightarrow \psi_j$) transitions arise through the redistribution of electrons in a species under an applied magnetic field. They are usually not considered to be important; therefore, they are often neglected in analyses and discussions. However, they contribute to $\sigma^p(C)$ more than those expected in some cases, as shown in Fig. 14. Specifically, the occupied-to-occupied orbital transitions may play an important role in the (observed) ^{13}C NMR chemical shifts, which are hidden in the unconscious realm of the measurers.

Conclusions

The plain rules associated with the origin and mechanism for $\delta(C)$ are intended to be established, without compromising theoretical requirements, in this work. The rules should be simple, easily imaged and easily understood for experimental scientists, who are not specialists. The rules should help experimental scientists image the role of C at a specific position in a species over the empirical rules usually employed in assigning the spectra. The $\delta(C)$ values are analysed by employing the calculated σ^d, σ^p and σ^t terms. The contributions from $\sigma^d(C)$ to $\sigma^t(C)$ are approximately one tenth of those from $\sigma^p(C)$, although the ratio changes depending on the species. The plot of $\sigma^d(C)$ versus $Q(C)$ for C^{4+}, C^{2+}, C^0, C^{2-} and C^{4-} gave excellent correlations if analysed via a cubic regression curve, as did the plots for C^{4-}, CH_2^{2-}, CH_3^- and CH_4 with a quadratic curve. The $\sigma^d(C)$ values can be understood based on $Q(C)$ for the species; however, $\sigma^d(C)$ of those other than those above do not correlate with $Q(C)$. The relationship between $\sigma^p(C)$ and $Q(C)$ was not examined further, which would be hidden in the complex combinations of the $\psi_i \rightarrow \psi_a$ transitions, as shown in eqn (6).

The pre-α effect of an approximately 20 ppm downfield shift is theoretically predicted based on the average value of $\Delta\sigma^t(C)_e$ from C^{4-} to H_4C. The α and β effects of approximately 10 ppm downfield shifts are reproduced well by the calculated $\Delta\sigma^t(C)_e$ values. The variety of the α-X, β-X and i-X effects are clarified by the calculations. Large downfield shifts by ethene ($\sim$120 ppm), benzene ($\sim$127 ppm) and ethyne ($\sim$60 ppm) and very large downfield shifts by the carbonyl group ($\sim$200 ppm) and carboxyl group ($\sim$180 ppm) are also well reproduced by the calculations.

The orbital-to-orbital transitions in $\sigma^p(C)$ are widely employed to clarify the origin and the mechanism for $\delta(C)$ in this work. The occupied-to-unoccupied orbital ($\psi_i \rightarrow \psi_a$) transitions in $\sigma^p(C)$ enable us to visualize the origin and the mechanism. The occupied-to-occupied orbital ($\psi_i \rightarrow \psi_j$) transitions, which are usually neglected, are also examined: The contributions from the $\psi_i \rightarrow \psi_j$ transitions are greater than those expected in some cases. The examination provided useful information for $\sigma^p(C)$. As a result, the plain rules with the origin and the mechanism are formulated for $\delta(C)$. The origin and the mechanism for $\delta(C)$ can be imaged and understood more easily
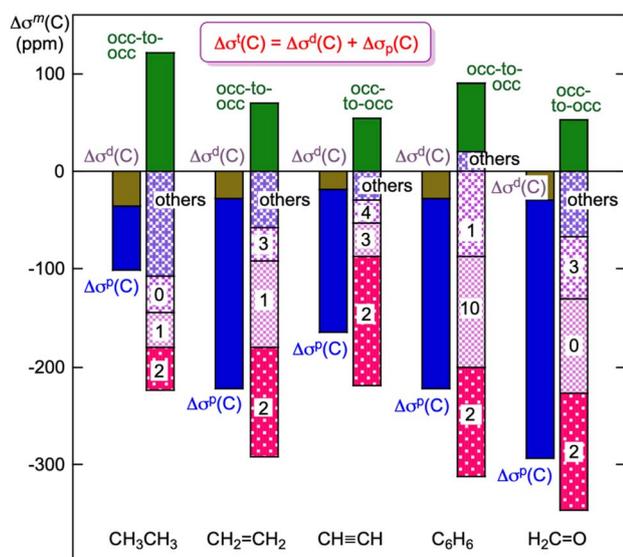

Fig. 14 Plots of $\Delta\sigma^d(C)$, $\Delta\sigma^p(C)$, $\Delta\sigma^t(C)$ and the components for CH_3CH_3, $CH_2=CH_2$, $CH\equiv CH$, C_6H_6 and $H_2C=O$. Each MO contributing to $\sigma^p(C)$ is shown by n in HOMO$-n$.

based on the treatments also by experimental scientists. The results will help in understanding the role of C in question in the specific position of a compound. By expanding the image of the orbital-to-orbital transitions, it would be possible to envision the molecular orbitals around the carbon in question in the compound and their interactions. The expansion will hopefully lead to the development of the highly functionality based on the inherent properties of the compound. Namely, this work also has the potential to provide an understanding $\delta(C)$ of unknown species and facilitate new concepts for strategies to create highly functional materials on the basis of the $\delta(C)$ values.

Data availability

The data supporting this article have been included as part of the ESI.†

Author contributions

W. N. and S. H. formulated the project and organized the data; contributed to supervision, data curation and resources; and wrote, reviewed and edited the paper. K. M. contributed to the investigation. All of the authors have read and agreed to the published version of the manuscript.

Conflicts of interest

The authors declare that they have no conflicts of interest.

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13 The occupied-to-unoccupied orbital $(\psi_i \rightarrow \psi_a)$ transitions mainly contribute to σ^p, whereas the occupied-to-occupied orbital $(\psi_i \rightarrow \psi_j)$ transitions sometimes play an important role in σ^p.

14 Based on the second-order perturbation theory at the level of the HF and single-excitation CI approximation, $\sigma^p_{i \rightarrow a}$ on a resonance nucleus N is shown to be proportional to reciprocal orbital energy gap $(\varepsilon_a - \varepsilon_i)^{-1}$ as expressed in eqn (5), where ψ_k is the k-th orbital function, $\hat{L}_{z,N}$ is orbital angular momentum around the resonance nucleus, and r_N is the distance from the nucleus N.

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