

## RESEARCH ARTICLE

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## Deep-ultraviolet sulfamate halides with halogen-centered secondary building units for enhanced optical anisotropy†

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The insufficient birefringence of non- $\pi$ -conjugated optical materials presents a significant challenge for their deep-ultraviolet (DUV) applications. In this work, four DUV sulfamate halide co-crystals, AX(NH<sub>3</sub>SO<sub>3</sub>) (A = Rb, Cs; X = Cl, Br), were successfully synthesized through functional chromophore engineering. All four compounds exhibit promising DUV transparent windows, with RbCl(NH<sub>3</sub>SO<sub>3</sub>) and CsCl(NH<sub>3</sub>SO<sub>3</sub>) demonstrating short DUV cut-off edges below 185 nm. Remarkably, a significant improvement in birefringence, ranging from 0.069 to 0.075, was observed in all four crystals. These values represent the highest birefringence observed for non- $\pi$ -conjugated DUV optical materials and exhibit optical anisotropy comparable to that of DUV materials containing  $\pi$ -conjugated groups. Theoretical analysis using the real-space atom-cutting method reveals that the [XA<sub>m</sub>] (X = Cl, Br; A = Rb, Cs) secondary building units (SBUs) contribute significantly to the birefringence. The incorporation of halogen-centered chromophores provides a novel strategy for designing non- $\pi$ -conjugated DUV materials with enhanced birefringence and phase-matching capabilities.

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## Introduction

Deep-ultraviolet (DUV,  $\lambda \leq 200$  nm) optical crystals have been explored for decades, attributable to their birefringent and frequency-doubling capabilities, which arise from their unique anisotropic frameworks.<sup>1,2</sup> Since the emergence of  $\alpha$ -BaB<sub>2</sub>O<sub>4</sub> ( $\alpha$ -BBO) and KBe<sub>2</sub>BO<sub>3</sub>F<sub>2</sub> (KBBF) as excellent short-wavelength birefringent and nonlinear optical (NLO) materials,  $\pi$ -conjugated planar units have been considered ideal for providing optical anisotropy and enhancing birefringence.<sup>3–7</sup> In recent years, more materials featuring  $\pi$ -conjugated [CO<sub>3</sub>], [NO<sub>3</sub>], [H<sub>x</sub>C<sub>3</sub>N<sub>3</sub>O<sub>3</sub>] ( $x = 1–3$ ), and [C<sub>6</sub>N<sub>7</sub>O<sub>3</sub>] groups have been synthesized as short-wavelength optical materials, offering

suitable birefringence for beam splitting or phase matching (PM).<sup>8–12</sup> In contrast, although isotropic tetrahedral units such as [PO<sub>4</sub>], [BO<sub>4</sub>], and [SO<sub>4</sub>] typically exhibit large highest occupied molecular orbital and lowest unoccupied molecular orbital (HOMO–LUMO) gaps and wide transparent windows, the birefringence of non- $\pi$ -conjugated optical materials composed of alkali or alkaline earth metals is significantly reduced. This is due to the lack of anisotropy in both the cations and anions.<sup>13–16</sup>

Compared to conventional isotropic tetrahedra, their polar tetrahedral variants, such as [BO<sub>x</sub>F<sub>4–x</sub>] ( $x = 1–3$ ), [CH<sub>3</sub>BF<sub>3</sub>], [PO<sub>x</sub>F<sub>4–x</sub>] ( $x = 1–3$ ), [XSO<sub>3</sub>] (X = NH<sub>2</sub>, NH<sub>3</sub>, CH<sub>3</sub>, F), which arise from the breaking of  $T_d$  symmetry, not only exhibit large HOMO–LUMO gaps but also process higher polarizability anisotropy, hyperpolarizability and enhanced optical anisotropy.<sup>17–24</sup> By employing these polar tetrahedral units, researchers have discovered several materials exhibiting enhanced birefringence ( $0.05 \leq \Delta n \leq 0.06$ ), including NaNH<sub>4</sub>PO<sub>3</sub>F·H<sub>2</sub>O (0.053 @ 589.3 nm), Pc-Sr(NH<sub>2</sub>SO<sub>3</sub>)<sub>2</sub> (0.056 @ 589.3 nm), and Cs<sub>2</sub>Mg(NH<sub>2</sub>SO<sub>3</sub>)<sub>4</sub>·4H<sub>2</sub>O (0.054 @ 546.1 nm).<sup>23,25,26</sup> These materials show a significant improvement compared to benchmark non- $\pi$ -conjugated DUV materials with isotropic tetrahedra, such as KH<sub>2</sub>PO<sub>4</sub> (KDP, 0.04178 @ 546 nm) and BPO<sub>4</sub> (0.0056 @ 589 nm), offering better PM capacities.<sup>27,28</sup> In the sulfamate system, while the polar [NH<sub>x</sub>SO<sub>3</sub>] ( $x = 2, 3$ ) tetrahedra can significantly enhance the anisotropy of crystal frameworks compared to symmetric

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anionic groups, the birefringence of sulfamates remains relatively insufficient for optimal DUV PM condition ( $0.06 \leq \Delta n \leq 0.08$ ), limiting their practical applications.<sup>17,29</sup> To enhance the DUV optical performance of metal sulfamates, it is necessary to introduce additional chromophores that can improve birefringence while maintaining a suitable short-wavelength transparent window.

Among all functional units, those with strong electro-negativity, such as halogens, have been shown to coordinate with metals to form flexible  $[XA_m]$  (X = halogens, A = metals) secondary building units (SBUs), effectively enhancing optical anisotropy. This has been demonstrated by examples such as  $[B_6O_{10}]XA_3$  (X = Cl, Br, A = alkali metals),  $Ba_3P_3O_{10}X$  (X = Cl, Br),  $ABi_2(IO_3)_2F_5$  (A = K, Rb, Cs), and  $CsZn_2BO_3X_2$  ( $X_2 = F_2, Cl_2, FCl$ ).<sup>30–33</sup> Inspired by these findings, it is evident that combining halogen-centered SBUs with polar tetrahedral units can effectively improve the birefringent capabilities of non- $\pi$ -conjugated materials. Based on the sulfamate system, which has yielded several materials with excellent DUV properties, we successfully combined  $[XA_m]$  (X = Cl, Br; A = Rb, Cs) SBUs with  $[NH_3SO_3]$  polar tetrahedra to synthesize a series of co-crystals comprising metal halides and sulfamic acid, denoted as AX ( $NH_3SO_3$ ) (A = Rb, Cs; X = Cl, Br). All four compounds exhibit notably enhanced birefringence, ranging from 0.069 to 0.075, compared to known non- $\pi$ -conjugated DUV optical materials ( $\Delta n \leq 0.056$ ). Meanwhile, the chloride co-crystals, RbCl ( $NH_3SO_3$ ) and CsCl( $NH_3SO_3$ ), retain excellent DUV cut-off edges below 185 nm.

## Experimental section

### Reagent and crystal growth

RbCl (Adamas, 99.9%), CsCl (Adamas, 99.9%), RbBr (Adamas, 99.9%), CsBr (Adamas, 99.9%), and sulfamic acid (Fisher chemical,  $\geq 99\%$ ) were used as received without further purification. All four crystals, AX( $NH_3SO_3$ ) (A = Rb, Cs; X = Cl, Br), were synthesized *via* a room-temperature aqua-solution method using a stoichiometric ratio of 1:1 of the corresponding metal halides and sulfamic acid. For example, RbCl ( $NH_3SO_3$ ) was synthesized by placing RbCl (1 mmol, 0.121 g) and  $HSO_3NH_2$  (1 mmol, 0.097 g) in 10 mL of distilled water in a 20 mL beaker. The mixture was stirred thoroughly to ensure complete reaction. The resulting clear solution was placed in a 30 °C oven for slow evaporation, yielding transparent RbCl ( $NH_3SO_3$ ) crystals. The other three compounds were synthesized following similar procedures. The yields of the four compounds were calculated based on their respective metals, yielding values of 92.3%, 89.8%, 91.4%, and 94.2% for RbCl ( $NH_3SO_3$ ), CsCl( $NH_3SO_3$ ), RbBr( $NH_3SO_3$ ), and CsBr( $NH_3SO_3$ ), respectively.

### X-ray diffraction analysis

The crystal structures of AX( $NH_3SO_3$ ) (A = Rb, Cs; X = Cl, Br) were determined by single crystal X-ray diffraction (SC-XRD) using a BRUKER D8 QUEST diffractometer equipped with

monochromatic Mo K $\alpha$  radiation ( $\lambda = 0.71073 \text{ \AA}$ ) at the Advanced Bio-Interface Core Research Facility at Sogang University. Data integration and absorption correction were performed using the SAINT and SCALE programs, respectively.<sup>34</sup> The structural refinement was conducted using the OLEX2 crystallographic software suite.<sup>35</sup> All non-hydrogen atoms were refined *via* full-matrix least-squares techniques. Final least-squares refinement was performed on  $F_o^2$ , using data satisfying  $F_o^2 \geq 2\sigma(F_o^2)$ . Hydrogen atom positions were initially estimated from difference Fourier maps and further optimized through first-principles calculations. Symmetry checks were performed using the PLATON program.<sup>36</sup> Refined crystallographic data are summarized in Table S1.† Bond valence sums (BVS) of all non-H atoms were calculated using the bond valence model developed by Brown.<sup>37</sup> Detailed information, including atomic coordinates, equivalent isotropic displacement parameters, BVS, selected bond lengths and angles, and hydrogen bond distances, is provided in Tables S2–S10 in the ESI.†

Powder X-ray diffraction (PXRD) patterns were collected using a Rigaku MiniFlex 600 diffractometer with Cu K $\alpha$  radiation ( $\lambda = 1.5418 \text{ \AA}$ ). The patterns were recorded over a 5–60° 2 $\theta$  range with a step size of 0.02° and a scan speed of 7° min<sup>−1</sup>. Experimental PXRD patterns for AX( $NH_3SO_3$ ) (A = Rb, Cs; X = Cl, Br) closely matched their theoretical patterns simulated from SC-XRD data (Fig. S1†).

### Spectroscopy

Infrared (IR) spectra were recorded on a Bruker TENSOR 27 ATR-FT-IR spectrometer in the range of 525–4000 cm<sup>−1</sup>. Ground samples were placed in direct contact with the diamond attenuated total reflectance crystal. The UV-vis diffuse reflectance spectrum was measured at 25 °C using a Lambda 1050 scan UV-vis spectrophotometer, covering the wavelength range of 185–900 nm.

### Scanning electron microscopy-energy dispersive analysis by X-ray (SEM-EDX)

SEM-EDX measurements were performed using a JSM-7100F thermal field emission scanning electron microscope equipped with a lens-type ZrO/W Schottky field emission gun. Polycrystalline samples were mounted on carbon tape and coated with platinum prior to analysis. The SEM-EDX results confirmed the presence of Cs, Rb, S, O, N, Cl, and Br in the corresponding compounds, with no other elements detected (Table S11†). These results support the correctness of the structural solutions (Fig. S2†).

### Thermogravimetric (TG) analysis

TG analysis was carried out using a SCINCO TGA-N 1000 thermal analyzer. For each measurement, 5–10 mg of ground polycrystalline sample was placed in an alumina crucible and heated under a flow of argon gas from room temperature to 900 °C at a rate of 5 °C min<sup>−1</sup>.

## Birefringence measurement

Birefringence was determined using a ZEISS Axiolab 5 polarized microscope equipped with a 546.1 nm monochromator and a Berek compensator. Retardation ( $R$ ) was measured for transparent plate-like crystals, with their thickness ( $d$ ) determined using a BRUKER D8 QUEST diffractometer. The birefringence ( $\Delta n$ ) of the selected crystals was calculated using the formula:  $R = \Delta n \times d$ .

## First principles calculations

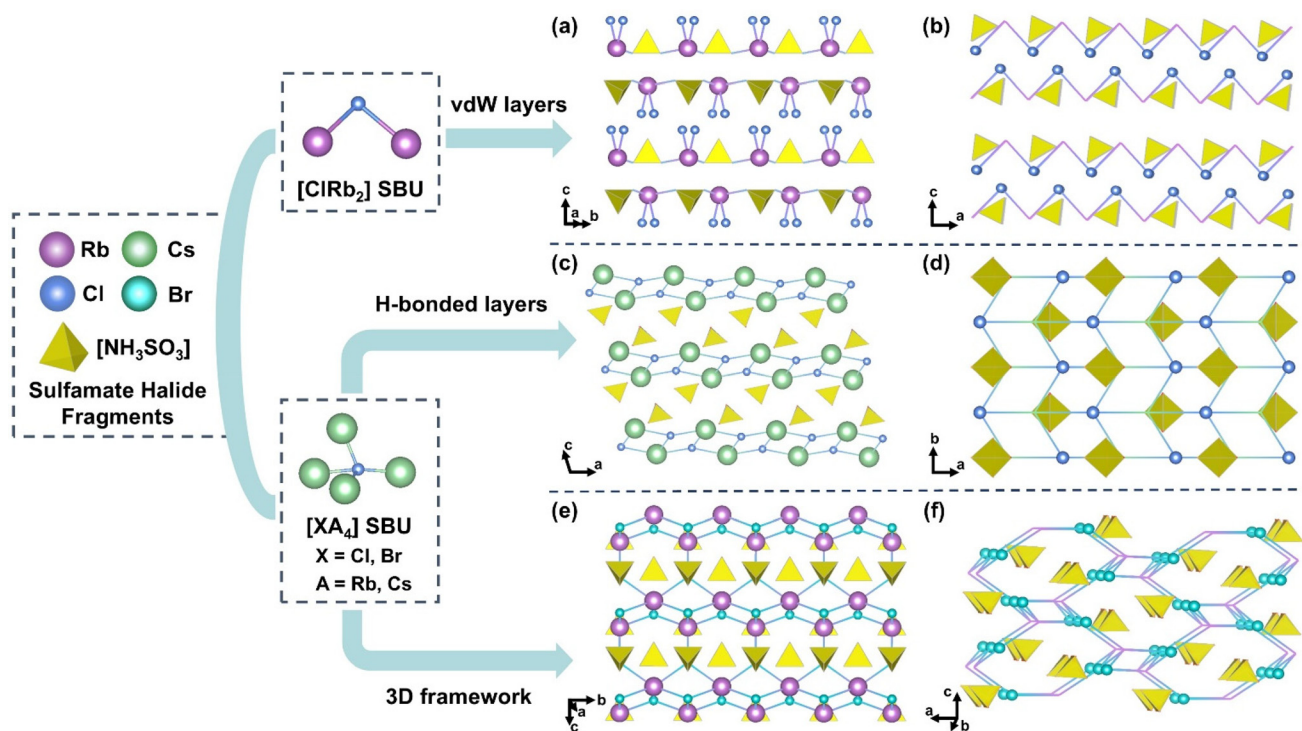
The electronic structure and linear optical properties were analyzed using the CASTEP package, which adopt a plane-wave pseudopotential method based on density functional theory.<sup>38</sup> The Perdew–Burke–Ernzerhof functional within the generalized gradient approximation framework was employed. The plane wave energy cut-off was set to 830 eV with norm-conserving pseudopotentials to ensure convergence.<sup>39</sup> The valence electronic configurations were specified as follows: Rb:  $4s^2 4p^6 5s^1$ , Cs:  $5s^2 5p^6 6s^1$ , S:  $3s^2 3p^4$ , O:  $2s^2 2p^4$ , N:  $2s^2 2p^3$ , Cl:  $3s^2 3p^5$ , Br:  $4s^2 4p^5$ , H:  $1s^1$ . A Monkhorst–Pack grid with  $k$ -points in the Brillouin zone was set to  $3 \times 2 \times 3$ .<sup>40</sup> Other calculation parameters and convergence criteria adhered to the default settings in the CASTEP code. To elucidate the birefringence contributions of each functional unit, the real-space atom-cutting method was employed.<sup>41</sup>

## Results and discussion

### Crystal structure of $\text{RbCl}(\text{NH}_3\text{SO}_3)$

$\text{RbCl}(\text{NH}_3\text{SO}_3)$  crystallizes in the monoclinic centrosymmetric space group,  $P2_1/m$ . The asymmetric unit contains one crystallographically independent Rb atom, one Cl atom, one S atom, one N atom, and two O atoms. The Rb1 atoms are coordinated with eight O atoms and two Cl atoms, forming  $[\text{RbO}_8\text{Cl}_2]$  polyhedra (Fig. S3a†). The Rb–O bond lengths range from 2.9556 (13) to 3.1891 (14) Å, while the Rb–Cl bond length is 3.4336 (7) Å. The S atoms are coordinated with three O atoms and one N atom, forming  $[\text{NSO}_3]$  tetrahedra. The S–O bond lengths vary from 1.4345 (13) to 1.4383 (19) Å, and the S–N bond length is 1.759 (2) Å. Due to the distinct electronic environments of amine and ammonia groups, the S–N bond lengths in  $[\text{NSO}_3]$  tetrahedra differ significantly between  $[\text{NH}_2\text{SO}_3]$  and  $[\text{NH}_3\text{SO}_3]$  configurations. Based on previously reported sulfamates and sulfamic acid co-crystals, the S–N bond lengths range from 1.62 Å to 1.64 Å for  $[\text{NH}_2\text{SO}_3]$  units and from 1.74 Å to 1.76 Å for  $[\text{NH}_3\text{SO}_3]$  units. Therefore, the compound is identified as a co-crystal comprising RbCl and sulfamic acid. Similarly,  $\text{CsCl}(\text{NH}_3\text{SO}_3)$ ,  $\text{RbBr}(\text{NH}_3\text{SO}_3)$ , and  $\text{CsBr}(\text{NH}_3\text{SO}_3)$  were determined to be co-crystals of sulfamic acid and their respective metal halides, following the same bond-length principles for S–N bonds.

$\text{RbCl}(\text{NH}_3\text{SO}_3)$  exhibits a characteristic two-dimensional (2D) layered structure, with the layers stacking along the  $c$ -axis (Fig. 1a). The  $[\text{NH}_3\text{SO}_3]$  molecules adopt an anti-parallel



**Fig. 1** (a) The 2D vdW layers of  $\text{RbCl}(\text{NH}_3\text{SO}_3)$  viewed perpendicular to the  $c$ -axis. (b) The infinite  $[\text{ClRb}]_\infty$  1D chains in  $\text{RbCl}(\text{NH}_3\text{SO}_3)$  viewed along the  $b$ -axis. (c) The layered structure of  $\text{CsCl}(\text{NH}_3\text{SO}_3)$  viewed along the  $a$ -axis. (d) The 2D  $[\text{ClRb}]_\infty$  layers in  $\text{CsCl}(\text{NH}_3\text{SO}_3)$  viewed along the  $c$ -axis. (e) The 3D halogen-metal framework of  $\text{RbBr}(\text{NH}_3\text{SO}_3)$  viewed along the pseudo-layered direction. (f) The 3D halogen-metal framework of  $\text{RbBr}(\text{NH}_3\text{SO}_3)$  viewed perpendicular to the pseudo-layered direction.

arrangement due to the symmetric operation of the  $2/m$  point group. Adjacent Rb1 atoms coordinate with the oxygen atoms of the  $[\text{NH}_3\text{SO}_3]$  molecules through corner- and edge-sharing, forming a pseudo-double layer along the  $ab$  planes (Fig. S3b†). Due to the strong electronegativity of Cl atoms, the Cl1 atoms are displaced from the pseudo-layers and bridge two Rb atoms, forming  $[\text{ClRb}_2]$  SBUs. These SBUs further create infinite  $[\text{ClRb}]_\infty$  1D chains along the  $a$ -axis, which are alternately arranged with  $[\text{NH}_3\text{SO}_3]$  molecules in the  $ab$  plane (Fig. 1b). The BVS calculations and the donor-acceptor distance between Cl1 and N1 atoms suggest that Cl1 acts as a hydrogen bond acceptor from the  $[\text{NH}_3\text{SO}_3]$  molecules. The donor-acceptor distances range from 3.2049(7) to 3.214(2) Å. As no typical chemical bonds exist between adjacent layers,  $\text{RbCl}(\text{NH}_3\text{SO}_3)$  is classified as a layered molecular crystal, held together by van der Waals (vdW) forces.

### Crystal structure of $\text{CsCl}(\text{NH}_3\text{SO}_3)$

$\text{CsCl}(\text{NH}_3\text{SO}_3)$  crystallizes in the  $P2_1/m$  space group. However, the material exhibits a structure distinct from  $\text{RbCl}(\text{NH}_3\text{SO}_3)$  attributed to the larger ionic radius of  $\text{Cs}^+$ . The asymmetric unit consists of one Cs atom, one Cl atom, one S atom, one N atom, and two O atoms. The Cs1 atom is coordinated with seven O atoms and four Cl atoms, forming  $[\text{CsO}_7\text{Cl}_4]$  polyhedra (Fig. S4a†). The Cs–O bond lengths range from 3.1135(17) to 3.534(3) Å, while the Cs–Cl bond lengths vary from 3.5808(17) to 3.6759(11) Å. The  $[\text{NH}_3\text{SO}_3]$  molecules adopt an anti-parallel arrangement and coordinate with the Cs1 atoms through corner- and edge-sharing, creating a 2D pseudo-layer along the  $ab$  plane (Fig. 1c). Due to the difference in ionic radii between  $\text{Cs}^+$  and  $\text{Rb}^+$ , the coordination environment of the Cl1 atom in  $\text{CsCl}(\text{NH}_3\text{SO}_3)$  differs significantly from the 2-coordinated Cl atoms in  $\text{RbCl}(\text{NH}_3\text{SO}_3)$ . In  $\text{CsCl}(\text{NH}_3\text{SO}_3)$ , the Cl1 atom coordinates with four Cs atoms, forming  $[\text{ClCs}_4]$  SBUs. These SBUs assemble into infinite 2D  $[\text{ClCs}]_\infty$  layers extending within the  $ab$  plane, oriented perpendicular to the pseudo-layer formed by the sulfamic acid molecules (Fig. 1d). Consequently, adjacent layers are linked by weak Cs–Cl and Cs–O ionic interactions, in contrast to the vdW forces observed in  $\text{RbCl}(\text{NH}_3\text{SO}_3)$ .

### Crystal structures of $\text{RbBr}(\text{NH}_3\text{SO}_3)$ and $\text{CsBr}(\text{NH}_3\text{SO}_3)$

Both  $\text{RbBr}(\text{NH}_3\text{SO}_3)$  and  $\text{CsBr}(\text{NH}_3\text{SO}_3)$  crystallize in the orthorhombic  $Pnma$  space group, sharing an isostructural framework and similar cationic coordination environments. The slight differences in unit cell parameters along the  $a$ - and  $c$ -axes arise from the variation in ionic radii between  $\text{Rb}^+$  and  $\text{Cs}^+$ . The asymmetric unit of  $\text{RbBr}(\text{NH}_3\text{SO}_3)$  comprises one Rb atom, one Br atom, one S atom, one N atom, and two O atoms, while in  $\text{CsBr}(\text{NH}_3\text{SO}_3)$ , the Rb atom is replaced by a Cs atom (Fig. S4b†). The  $[\text{RbO}_7\text{Br}_4]$  ( $[\text{CsO}_7\text{Br}_4]$ ) polyhedra are formed by the coordination of the Rb1 (Cs1) atom with seven O atoms and four Br atoms. The bond distances for Rb–O and Cs–O are 3.025(2)–3.2141(13) Å and 3.224(4)–3.315(4) Å, respectively, while the Rb–Br and Cs–Br bond distances are 3.6459(10)–3.7213(9) Å and 3.7390(7)–3.9088(11) Å, respectively. The Br

atoms in  $\text{RbBr}(\text{NH}_3\text{SO}_3)$  and  $\text{CsBr}(\text{NH}_3\text{SO}_3)$  coordinate with four Rb (or Cs) atoms, forming the  $[\text{BrRb}_4]$  ( $[\text{BrCs}_4]$ ) SBUs (Fig. 1e). Unlike  $\text{CsCl}(\text{NH}_3\text{SO}_3)$ , the incorporation of larger  $\text{Br}^-$  ions leads to SBUs with higher connectivity, resulting in 3D  $[\text{BrRb}]_\infty$  ( $[\text{BrCs}]_\infty$ ) halogen-metal frameworks (Fig. 1f). The longer Rb–Br and Cs–Br bond distances and the looser framework structures cause the  $[\text{NH}_3\text{SO}_3]$  molecules to intersect at angles of  $115.7(1)^\circ$  and  $120.5(4)^\circ$ , rather than adopting the antiparallel arrangement seen in  $\text{CsCl}(\text{NH}_3\text{SO}_3)$  (Fig. S5†). These differences in molecular arrangements highlight the flexibility of halogen-metal frameworks and suggest a promising approach for regulating the arrangement of neutral or anionic groups to achieve desirable properties.

### Thermal analysis

TG analysis was conducted to assess the thermal stability of the four compounds (Fig. S6†). All four compounds exhibit similar thermal stability up to approximately 142 °C. Beyond this temperature, gradual weight losses were observed between 142 and 800 °C, attributed to the decomposition of sulfamic acid and halogens. At 800 °C, the observed residual weights for  $\text{CsCl}(\text{NH}_3\text{SO}_3)$  and  $\text{CsBr}(\text{NH}_3\text{SO}_3)$  are 73.01% and 61.97%, respectively, which closely align with the calculated values of 68.30% and 58.41% based on the decomposition products of  $\text{Cs}_2\text{SO}_4$ . Similarly,  $\text{RbCl}(\text{NH}_3\text{SO}_3)$  and  $\text{RbBr}(\text{NH}_3\text{SO}_3)$  exhibit residual weights of 68.41% and 58.12%, respectively, which are slightly higher than the calculated values of 61.51% and 50.86% based on the decomposition products of  $\text{Rb}_2\text{SO}_4$ . These discrepancies may be attributed to incomplete decomposition of the compounds. Theoretical and experimental weight loss data are provided in the ESI (Table S12†).

### IR and UV-vis spectroscopic analysis

IR spectra of the four compounds, recorded in the range of 4000–400  $\text{cm}^{-1}$ , were analyzed to identify their functional groups (Fig. S7†). The characteristic peaks of  $\text{RbCl}(\text{NH}_3\text{SO}_3)$  are described as representative due to the similarity in vibrational features across all four compounds. Peaks at 1265, 1060, 978, and 691  $\text{cm}^{-1}$  are attributed to the anti-symmetric and symmetric stretching vibrations of the S–O interactions in the  $[\text{NH}_3\text{SO}_3]$  groups. Absorption peaks in the ranges of 1410–1425  $\text{cm}^{-1}$ , 2430–2440  $\text{cm}^{-1}$ , and 3160–3210  $\text{cm}^{-1}$  correspond to the bending, wagging, and stretching vibrations of the  $[\text{NH}_3]$  units, respectively. The assigned peaks for all four compounds are consistent with previously reported experimental and theoretical IR data for sulfamates (Table S13†).<sup>23</sup>

The UV-vis diffuse reflectance spectra were measured to determine the UV transparent windows of the four compounds. As shown in Fig. 2a and b,  $\text{RbCl}(\text{NH}_3\text{SO}_3)$  and  $\text{CsCl}(\text{NH}_3\text{SO}_3)$  exhibit high reflectance from the visible light region to the DUV range, with reflectance values of 85.26% and 46.40% at 185 nm, respectively. These results indicate wide DUV transparent windows. In contrast, the presence of  $\text{Br}^-$  anions cause a red-shift in the cut-off edges of  $\text{RbBr}(\text{NH}_3\text{SO}_3)$  and  $\text{CsBr}(\text{NH}_3\text{SO}_3)$  to 193 nm and 195 nm, respectively (Fig. 2c and d). The optical band gaps of the compounds were esti-

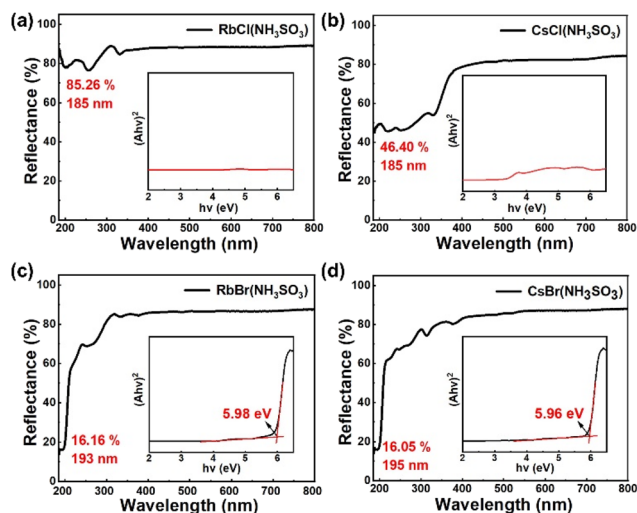


Fig. 2 UV-vis diffuse reflectance spectra of (a)  $\text{RbCl}(\text{NH}_3\text{SO}_3)$ , (b)  $\text{CsCl}(\text{NH}_3\text{SO}_3)$ , (c)  $\text{RbBr}(\text{NH}_3\text{SO}_3)$ , and (d)  $\text{CsBr}(\text{NH}_3\text{SO}_3)$ .

mated using the Kubelka–Munk function. The calculated band gaps are  $>6.70$  eV for  $\text{RbCl}(\text{NH}_3\text{SO}_3)$  and  $\text{CsCl}(\text{NH}_3\text{SO}_3)$ , 5.98 eV for  $\text{RbBr}(\text{NH}_3\text{SO}_3)$ , and 5.96 eV for  $\text{CsBr}(\text{NH}_3\text{SO}_3)$ . These results demonstrate that the introduction of halides maintains wide UV and DUV transparent windows while only slightly reducing the bandgaps compared to metal sulfamates.

### Electronic structures

First-principles calculations were performed to analyze the electronic band structures and the total and partial density of states (DOS) of the four compounds. The results reveal that the valence band maximum and conduction band minimum for all four compounds are located at the  $\Gamma$  point, indicating direct band gaps of 4.584, 4.607, 4.217, and 4.233 eV for  $\text{RbCl}(\text{NH}_3\text{SO}_3)$ ,  $\text{CsCl}(\text{NH}_3\text{SO}_3)$ ,  $\text{RbBr}(\text{NH}_3\text{SO}_3)$ , and  $\text{CsBr}(\text{NH}_3\text{SO}_3)$ , respectively (Fig. S8†). An analysis of the total and partial DOS shows that the tops of the valence bands are primarily dominated by Cl-3p and Br-4p orbitals. In contrast, the bottoms of the conduction bands consist of hybridized s and p orbitals

from Rb, Cs, S, O, and N atoms, depending on the specific compound. These results suggest that the band gaps of these compounds are predominantly influenced by A–X (A = Rb, Cs; X = Cl, Br) interactions (Fig. 3).

### Birefringence and contributions of halogen-centered SBUs

The birefringence of the four compounds was quantitatively determined by measuring the wavelength retardation of the crystals using a Berek compensator. Plate-like crystals with thicknesses of 12.079  $\mu\text{m}$  for  $\text{RbCl}(\text{NH}_3\text{SO}_3)$ , 17.443  $\mu\text{m}$  for  $\text{CsCl}(\text{NH}_3\text{SO}_3)$ , 9.977  $\mu\text{m}$  for  $\text{RbBr}(\text{NH}_3\text{SO}_3)$ , and 6.662  $\mu\text{m}$  for  $\text{CsBr}(\text{NH}_3\text{SO}_3)$  were used in the measurements. The recorded retardations were 843.9, 1277.3, 719.28, and 449.72 nm, corresponding to birefringence values of 0.069, 0.073, 0.072, and 0.075 at 546.1 nm, respectively (Fig. 4a–d).

The frequency-dependent birefringence of the four compounds was estimated using first principles calculations (Fig. 4e–h). Due to the typical underestimation of band gaps by the generalized gradient approximation used in the exchange–correlation energy functional, scissor operators of 1.763 eV and 1.727 eV were applied to correct the refractive index calculations for  $\text{RbBr}(\text{NH}_3\text{SO}_3)$  and  $\text{CsBr}(\text{NH}_3\text{SO}_3)$ , based on their experimental band gaps. For  $\text{RbCl}(\text{NH}_3\text{SO}_3)$  and  $\text{CsCl}(\text{NH}_3\text{SO}_3)$ , the band gaps were calculated using the HSE06 hybrid functional, yielding values of 6.942 eV and 6.923 eV, respectively. Corresponding scissor operators of 2.358 eV and 2.316 eV were applied for corrections. The estimated birefringence values at 532 nm were 0.065, 0.066, 0.071, and 0.064 for  $\text{RbCl}(\text{NH}_3\text{SO}_3)$ ,  $\text{CsCl}(\text{NH}_3\text{SO}_3)$ ,  $\text{RbBr}(\text{NH}_3\text{SO}_3)$ , and  $\text{CsBr}(\text{NH}_3\text{SO}_3)$ , respectively. These values are consistent with the experimental results at 546.1 nm, confirming the birefringence enhancement in non- $\pi$ -conjugated system.

To elucidate the origin of enhanced birefringence in sulfamate halide co-crystals, the real-space atom-cutting method, based on theoretically calculated refractive indices, was employed to analyze the birefringence contributions of each functional unit. Since the structures of the four compounds comprise isolated covalent molecules and metal–halide ionic frameworks, they were divided into sulfamic acid molecules

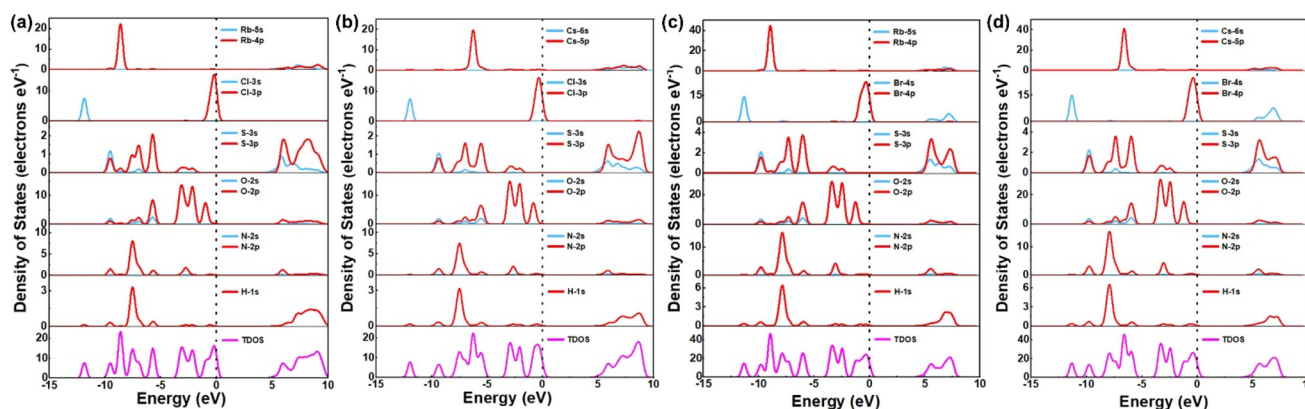
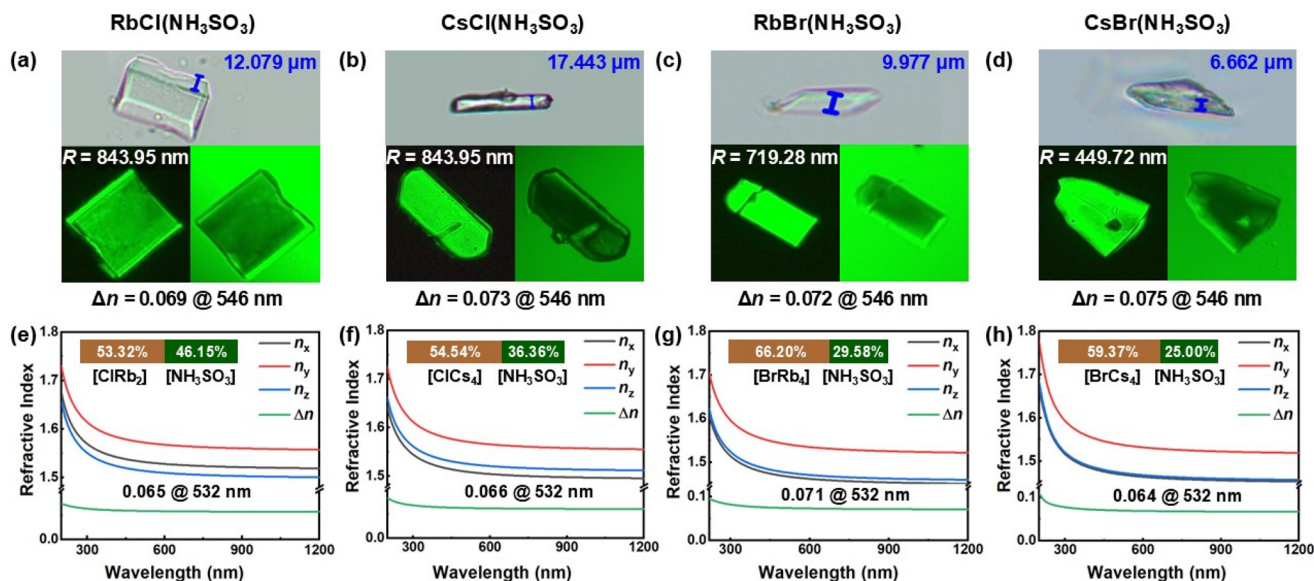


Fig. 3 Total and partial DOS of (a)  $\text{RbCl}(\text{NH}_3\text{SO}_3)$ , (b)  $\text{CsCl}(\text{NH}_3\text{SO}_3)$ , (c)  $\text{RbBr}(\text{NH}_3\text{SO}_3)$ , and (d)  $\text{CsBr}(\text{NH}_3\text{SO}_3)$ .

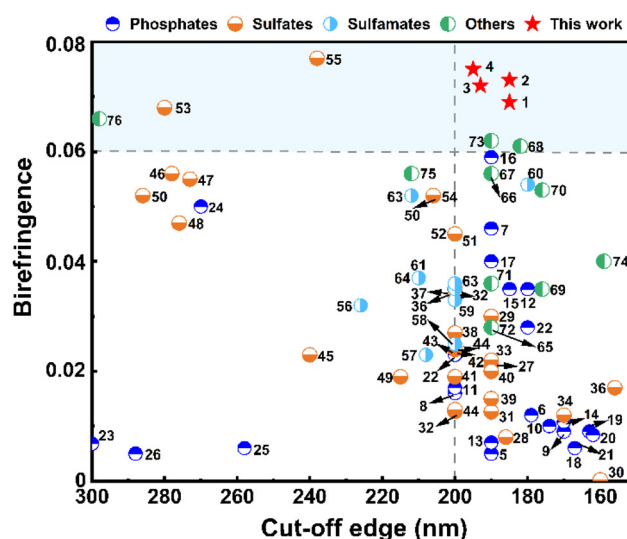


**Fig. 4** Measured birefringence at 546.1 nm of (a)  $\text{RbCl}(\text{NH}_3\text{SO}_3)$ , (b)  $\text{CsCl}(\text{NH}_3\text{SO}_3)$ , (c)  $\text{RbBr}(\text{NH}_3\text{SO}_3)$ , and (d)  $\text{CsBr}(\text{NH}_3\text{SO}_3)$ . Calculated frequency-dependent refractive indices and birefringence of (e)  $\text{RbCl}(\text{NH}_3\text{SO}_3)$ , (f)  $\text{CsCl}(\text{NH}_3\text{SO}_3)$ , (g)  $\text{RbBr}(\text{NH}_3\text{SO}_3)$ , and (h)  $\text{CsBr}(\text{NH}_3\text{SO}_3)$ . Insets of (e)–(h) show the birefringence contributions of halogen-centered SBUs and sulfamic acid polar tetrahedral groups, as calculated using the real-space atom-cutting method.

and halogen-centered SBUs, specifically  $[\text{ClRb}_2]$ ,  $[\text{ClCs}_4]$ ,  $[\text{BrRb}_4]$ , and  $[\text{BrCs}_4]$  in the respective compounds. Due to approximations made near the edges of electron clouds when estimating the spatial contributions of atomic or ionic groups, the sum of birefringence contributions from each unit may not strictly equal 100%. However, this discrepancy does not affect the scientific conclusions. The  $[\text{XA}_m]$  ( $\text{X} = \text{Cl}, \text{Br}; \text{A} = \text{Rb}, \text{Cs}$ ) SBUs make substantial contributions to birefringence, specifically 52.31% and 54.54% for  $\text{RbCl}(\text{NH}_3\text{SO}_3)$  and  $\text{CsCl}(\text{NH}_3\text{SO}_3)$ , and dominantly 66.20% and 59.37% for  $\text{RbBr}(\text{NH}_3\text{SO}_3)$  and  $\text{CsBr}(\text{NH}_3\text{SO}_3)$ , respectively. These results indicate that introducing halogens enhances optical anisotropy while providing an effective strategy to improve DUV phase-matching capabilities in potential noncentrosymmetric metal sulfamate halides.

To validate this improvement, a statistical analysis of cut-off edges and birefringence values for UV and DUV optical materials composed exclusively of non- $\pi$ -conjugated functional units – including phosphates, sulfates, sulfamates, and other tetrahedral structures was performed (Fig. 5 and Table S14†). Non- $\pi$ -conjugated functional units typically exhibit limited microscopic optical anisotropy. Consequently, most DUV phosphates and sulfates containing alkali or alkaline earth metals have relatively low birefringence, typically ranging from 0 to 0.05. Materials featuring stereochemically active metals, such as  $\text{Bi}^{3+}$  and  $\text{Sb}^{3+}$ , or S–S tetrahedral overlap achieve higher birefringence but suffer from noticeable red-shift in their cut-off edges, often exceeding 230 nm. While sulfamates and other polar non- $\pi$ -conjugated tetrahedra show improved birefringence compared to phosphates and sulfates, achieving optimal phase-matching birefringence in the range of 0.06–0.08 with

suitable DUV cut-off edges remains a challenge. The four sulfamate halide co-crystals stand out by combining large birefringence with wide DUV-transparent windows, underscoring the effectiveness of integrating halogen-centered SBUs with polar tetrahedra. Notably, the birefringence values of  $\text{RbCl}(\text{NH}_3\text{SO}_3)$  and  $\text{CsCl}(\text{NH}_3\text{SO}_3)$  exceed the previously established ceiling for DUV non- $\pi$ -conjugated optical materials (0.056 @ 589.3 nm for  $\text{Pc-Sr}(\text{NH}_2\text{SO}_3)_2$ ) while avoiding red-shifts in their cut-off edges.<sup>17</sup> Moreover, the birefringence values are comparable to



**Fig. 5** Comparison of non- $\pi$ -conjugated optical materials derivatives in the UV and DUV regions.

those of optical materials with  $\pi$ -conjugated functional groups, such as KBBF (0.077 @ 1064 nm), BaB<sub>4</sub>O<sub>6</sub>F<sub>2</sub> (0.065 @ 400 nm), Sr<sub>2</sub>NO<sub>3</sub>(OH)<sub>3</sub> (0.076 @ 532 nm), Na<sub>2</sub>Ca<sub>2</sub>(CO<sub>3</sub>)<sub>3</sub> (0.061 @ 1064 nm), Y<sub>8</sub>O(OH)<sub>15</sub>(CO<sub>3</sub>)<sub>3</sub>Cl (0.045 @ 1064 nm).<sup>42–46</sup>

## Conclusions

In summary, the first four DUV sulfamate halide co-crystals, AX(NH<sub>3</sub>SO<sub>3</sub>) (A = Rb, Cs; X = Cl, Br), were successfully synthesized using a room-temperature aqua-solution method. The introduction of Cl<sup>−</sup> and Br<sup>−</sup> anions has a minimal impact on the short-wavelength transparent window. Specifically, the chloride co-crystals, RbCl(NH<sub>3</sub>SO<sub>3</sub>) and CsCl(NH<sub>3</sub>SO<sub>3</sub>), exhibit short DUV cut-off edges below 185 nm. Remarkably, the four crystals display improved birefringence values in the range of 0.069–0.075, as determined using a polarized microscope. These values are comparable to those of DUV materials featuring  $\pi$ -conjugated groups. Theoretical analysis employing the real-space atom-cutting method reveals that the [X<sub>A<sub>m</sub></sub>] (X = Cl, Br, A = Rb, Cs) SBUs contribute significantly to the optical anisotropy and birefringence. These findings not only demonstrate that sulfamate halides are a promising system for developing DUV optical materials but also provide a novel approach for designing non- $\pi$ -conjugated DUV materials with enhanced birefringence and phase-matching capabilities.

## Data availability

Data available on request from the authors.

The data that support the findings of this study are available from the corresponding authors, KMO, QJ, or QW upon reasonable request.

## Conflicts of interest

There are no conflicts to declare.

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