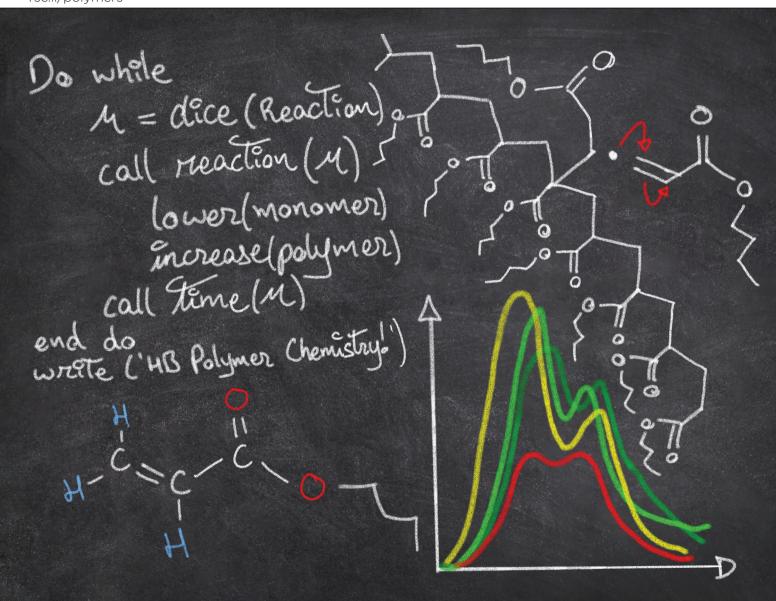
# Polymer Chemistry

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#### **PAPER**

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# Pulsed laser polymerization to retrieve kinetic parameters for a propagated mid-chain radical in poly(*n*-butyl acrylate) synthesis: a combined DFT and kinetic Monte Carlo study†

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Radical polymerization of n-butyl acrylate is characterized by backbiting of end-chain radicals (ECRs), with a propagation rate coefficient  $k_{p,e}$ , into mid-chain radicals (MCRs), with a propagation rate coefficient  $k_{\rm p.m.}$  In pulsed laser polymerization (PLP) kinetic studies, it is currently assumed that a MCR becomes a (fully developed) ECR after one propagation step. Here we demonstrate that a more gradual transition likely takes place, introducing a propagated mid-chain radical (PMR) with a propagation rate coefficient  $k_{p,P}$  or equivalently a transition propagation factor  $\gamma$  that at least theoretically can vary between 0 ( $k_{p,P}$  =  $k_{\rm p,m}$ ) and 1 ( $k_{\rm p,P}=k_{\rm p,e}$ ). Kinetic Monte Carlo (kMC) simulations under free radical polymerization (FRP) conditions hint at a  $\gamma$  not too close to 0 (e.g. not below 0.01), and Density functional theory (DFT) calculations at a  $\gamma$  not too close to 1 (e.g. not above 0.8). It is further shown that the ratio of the peak heights in a PLP – size exclusion chromatography (PLP-SEC) spectrum is sensitive to a variation in  $\gamma$ . This opens the door to the future experimental determination of  $k_{\rm p,p}$  considering different frequencies, provided that the initiator radical generation is well-described. At 325 K and using 500 Hz literature data, we currently put forward a γ of 0.1. In addition, the PMR backbiting potential is evaluated, introducing a backbiting scaling factor  $\delta$  with respect to the conventional ECR backbiting rate coefficient ( $k_{bb}$ ). It is showcased that this extra backbiting contributes to a better understanding of the migration mechanism and short branch formation in acrylate radical polymerization, although the experimental determination of  $\delta$  is less straightforward. Overall the current work highlights how acrylate-specific rate coefficients can be obtained in a roadmap format, considering higher and lower frequencies, and lower and higher temperatures.

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## Introduction

Free radical polymerization (FRP) is a widely used technique for the production of polyacrylics such as polyacrylates.<sup>1–5</sup> Such polymers are nowadays manufactured using a large variety of (co)monomers, both fuel- and biomass-based, making them very suitable for material optimization and property tuning.<sup>1,6–12</sup> However, for a given polyacrylate to suit a

certain application, a proper tuning of the molecular properties (*e.g.* molar mass distribution (MMD) or branching level) is desired. This is non-trivial as polyacrylate synthesis displays a complicated reaction scheme, dealing with multiple secondary reactions next to the conventional FRP reactions, *e.g.* initiation, (secondary) propagation, and termination. A detailed mechanistic understanding of acrylate polymerization is thus not straightforward and kinetic modeling is a desired pathway, provided that the (intrinsic) rate coefficients of all kinetically relevant reactions are carefully determined. <sup>13–17</sup>

A well-established technique for the determination of rate coefficients in radical polymerization is pulsed laser polymerization (PLP) in combination with size exclusion chromatography (SEC).<sup>18</sup> Aleksandrov *et al.*<sup>19</sup> originally studied kinetic and MMD variations in PLP. Later on Olaj *et al.*<sup>20</sup> extended the technique to obtain the propagation rate coefficient from the log-MMD. Additionally, the technique is recommended by the IUPAC Subcommittee on Modeling of Polymerization Kinetics and Processes.<sup>21-27</sup>

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Fig. 1 Top: End-chain radical (ECR) for acrylate radical polymerization (left); mid-chain radical (MCR) formed through backbiting over a six-membered transition state out of this ECR (right). Bottom: (left) Extra species explored in the present work, being a propagated mid-chain radical (PMR) as well (right) a new MCR after backbiting of this PMR.

PLP employes a laser beam to create pulse-wise initiator radicals, most commonly 2,2-dimethoxy-2-phenylacetophenone (DMPA) fragments, that initiate radical chain growth. <sup>28,29</sup> During the time between two laser pulses, which is called the dark time  $\Delta t$ , (macro)radicals grow and some of them terminate at the next pulse via the freshly generated initiator fragments in a kind of quenching manner. <sup>30</sup>

If only a (conventional) end-chain radical (ECR) is active as a macroradical in a PLP experiment, the chain length of specific dead polymer species  $(L_j)$  will therefore depend on the number of pulses (j),  $\Delta t$ , the initial monomer concentration  $([\mathbf{M}]_o)$ , and the ECR propagation rate coefficient  $k_{\mathrm{p,e}}$ :

$$L_j = k_{p,e}[\mathbf{M}]_0(j\Delta t). \tag{1}$$

Practically,  $L_1$  is the first inflection point (or peak maximum) of the SEC trace (j=1),  $^{31-35}$  and  $L_2$  provides a consistency check because it needs to be equal to twice  $L_1$ .  $^{21,36}$ 

In general, the subscript "app" should be used in eqn (1) to highlight that several macroradical types can exist, each with a distinct (intrinsic) propagation reactivity, together leading to an observed thus lumped/apparent propagation reactivity ( $k_{\rm p,app}$ ). For example, in high temperature acrylate radical polymerization  $k_{\rm p,app}$  does not equal  $k_{\rm p,e}$ . Mid-chain radicals (MCRs) are then also present, undergoing slower (tertiary) propagation (rate coefficient:  $k_{\rm p,m}$ ). Mechanistically, the formation of MCRs out of ECRs mainly proceeds through intramolecular chain transfer, *i.e.* backbiting. This reaction proceeds most easily via a six-membered transition state, leading to the creation of polymer chains with short side chain branches upon further (tertiary) propagation.  $^{37-40}$ 

The existence of ECRs and MCRs (top of Fig. 1) in acrylate radical polymerization moves the SEC trace to the lower chain

length region, due to a lower  $k_{\rm p,m}$ ,  $^{40-47}$  which can be understood considering the bulkier and more carbon substituted nature of the MCR and the difference in stability between both radical types. In other words, whenever backbiting occurs and a MCR is formed, a decrease of  $k_{\rm p,app}$  takes place because a MCR propagates at a slower rate. The sufficiently high temperatures macromonomers are also formed, due to fragmentation ( $\beta$ -scission) of MCRs.  $^{48,49}$ 

Notably, the influence of certain secondary reactions such as backbiting can be minimized by adapting the PLP conditions. A low temperature and high laser pulse frequency enable for instance an accurate (isolated) determination of  $k_{\rm p,e}$ , as highlighted by Willemse and van Herk, <sup>50</sup> who studied the secondary propagation of methyl, ethyl, butyl, hexyl and benzyl acrylate at frequencies between 60 and 100 Hz and temperatures between –25 to 37 °C. Even higher frequencies, *i.e.* 500 Hz and 1 kHz, have been used for PLP of n-butyl acrylate by Barner-Kowollik  $et\ al.^{30}$  and Wenn and Junkers <sup>51</sup> respectively. Once  $k_{\rm p,e}$  is known, a stepwise modification of the (isothermal) PLP conditions can be done to determine other (secondary) rate coefficients ideally one by one, enabling to span a detailed reaction scheme. <sup>30,43,52,53</sup>

Recent work by Marien *et al.*<sup>54</sup> and Vir *et al.*<sup>18</sup> showed that the rate coefficients for backbiting, MCR propagation and  $\beta$ -scission can be determined through stepwise PLP combined with kinetic Monte Carlo (kMC) simulations once  $k_{\rm p,e}$  is known. The first step consists of varying frequencies in the low frequency region (*e.g.* 10 to 50 Hz) at low to intermediate temperature while also varying the solvent fraction, selecting as solvent the saturated analogue of the monomer. Under these conditions  $\beta$ -scission is negligible, so that an isolation of the backbiting rate coefficient ( $k_{\rm bb}$ ) and  $k_{\rm p,m}$  is possible. The second step follows the same procedure of varying frequencies and solvent fractions but deals with higher temperatures to

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determine the  $\beta$ -scission rate coefficient ( $k_{\beta}$ ), inputting pre-

viously determined  $k_{p,e}$ ,  $k_{bb}$  and  $k_{p,m}$  values.

for these PLP-EPR experiments. 57-68

Another experimental technique commonly used for the determination of rate coefficients in radical polymerization is the combination of PLP with Electron Paramagnetic Resonance (PLP-EPR). This technique involves measuring the intensity of an EPR signal as a function of time, and from this, deducing concentration as a function of time for the radical species giving rise to the measured signal, whether it be ECR or MCR, both of which may be monitored simultaneously. The EPR measurement is often combined with PLP

because it allows for control over the amount of radicals pro-

duced; specifically in certain cases authors used a single-pulse

Note that it is implicitly assumed in the current acrylate (PLP) modeling studies that a MCR becomes an ECR after one propagation step, although the computational chemistry work of Cuccato et al.<sup>69</sup> for instance indicated a possible difference in propagation reactivity of a single-unit short branched polymer. Such difference has been related to the bulkier nature of the involved radical, in the current work denoted as a propagated mid-chain radical (PMR; Fig. 1; bottom left), as compared to a well-developed ECR, i.e. one possessing a radical center that is several monomer units away from the original MCR backbone. Similarly, chain length dependencies have been reported for the activation of halogen-capped tertiary radical chains in atom transfer radical polymerization (ATRP) involving methacrylates, due to an entropic strain effect.<sup>70</sup> Also, for radical polymerizations with only ECRs, a different propagation rate coefficient for the first two to ten additions has been reported.<sup>71</sup>

In the present work, we enrich the PLP-SEC modeling analysis of acrylates by studying the kinetic and structural relevance of the transition from a MCR to a PMR, and this PMR to a (developed) ECR. We also perform density functional theory (DFT) simulations<sup>69,72–79</sup> complementary with the work of Cuccato *et al.*,<sup>69</sup> and we discuss PMR backbiting possibilities (new rate coefficient  $k_{\rm bb,P}$ ), producing different types of branches and contributing to radical migration (Fig. 1; bottom right).

Practically, we calculate the PMR propagation rate coefficient,  $k_{\rm p,P}$ , using a transition propagation factor  $\gamma$ , and we calculate  $k_{\rm bb,P}$  via a scaling factor  $\delta$ :

$$k_{p,p} = (k_{p,e} - k_{p,m})\gamma + k_{p,m}$$
 (2)

$$k_{\rm bb,P} = \delta k_{\rm bb} \tag{3}$$

Hence, for  $\gamma$  equal to 0,  $k_{\rm p,P}=k_{\rm p,m}$  results, for  $\gamma$  equal to 1  $k_{\rm p,P}=k_{\rm p,e}$  (the current assumption), and for  $\delta$  equal to 1  $k_{\rm bb,P}=k_{\rm bb}$ .

A mechanistic foundation is put forward hinting at  $\gamma$  and  $\delta$  values not being too close to 1, to then demonstrate that in future work  $\gamma$  could be experimentally determined by measuring peak height ratios in the PLP spectrum, taking into account a frequency variation and relying on a good determination of radical generation kinetic parameters (at lower temp-

eratures). Focusing at FRP conditions, we also highlight that  $\gamma$  is (likely) sufficiently higher than 0 (*e.g.*  $\gg$ 0.01), supporting current parameter tuning efforts from all IUPAC connected groups for  $k_{\rm p,m}$  and  $k_{\rm bb}$  ignoring the PMR species. Based on literature data at one frequency we assess  $\gamma$  as 0.1 at 325 K in the present work. For  $\delta$ , however, only a rough estimate is possible in future work considering PLP branching data.

Overall this work contributes to the identification of a better roadmap for the determination of the (intrinsic) reactivities of acrylate specific reaction steps, and the type of branched species present. We complement the current modeling studies by a refinement of the kinetic scheme in case more detailed branching descriptions are aimed at.

## **Methods**

#### Computational chemistry details

DFT calculations were performed using the Gaussian 16\_C.01 package. <sup>80</sup> The molecular model structures were optimized at the B3LYP/6-311+G(d,p) method and basis set. The thermal contributions were included using the harmonic oscillator approach at the same computational level. The structures used were confirmed to have zero imaginary frequencies for reactants and products, and one large imaginary frequency in the transition states. The prediction of the electronic energy was improved by using a single-point M06-2X/6-311+G(d,p) calculation employing the previously optimized geometries.

To calculate enthalpies, entropies and free Gibbs energies in the gas phase, standard thermodynamic equations were used. Solvation effects were included using COSMO-RS theory 2-84 to calculate the free Gibbs energy of solvation  $\Delta G_{\rm solv}$ , as implemented in the COSMOtherm software package. The COSMO-RS calculation uses the electronic energy calculated by BP86/TZVP single point calculations performed on the previously B3LYP/6-311+G(d,p) optimized geometry, using the density of nBua at 298 K of 894 g L<sup>-1</sup>.

The transition state theory (TST) was used to calculated the rate coefficients, using the free Gibbs reaction barrier including solvation effects:<sup>86,87</sup>

$$k(T) = \kappa(T) \frac{k_{\rm B} T}{h} (C^0)^{-\Delta^{\frac{1}{4}} n} \exp\left(-\frac{\Delta^{\frac{1}{4}} G_{\rm cond}^{\circ}}{RT}\right) \tag{4}$$

in which  $\kappa$  is the quantum tunneling correction factor calculated via the Eckart method,  $^{88}$   $k_{\rm B}$  is the Boltzmann constant, h the Planck constant,  $C^0$  the standard concentration,  $\Delta n$  the difference in moles between reactant and transition state,  $\Delta^{\frac{1}{\tau}}G_{\rm cond}^{\circ}$  the temperature-dependent free Gibbs energy barrier, and R the universal gas constant.

We calculated the propagation rate coefficient for PMR,  $k_{\rm p,p}$ , using the molecular model depicted in Fig. 2 (top). This model consists of a tetramer radical, which represents the intermediate between a MCR and ECR, propagating toward a monomer unit and forming the pentamer branched structure shown in Fig. 2 (top right). The use of multiple diastereomers, as incor-

Fig. 2 Top: Molecular model used to predict the propagation rate coefficient of the propagated mid-chain radical (PMR). It consists of a tetramer radical, propagating towards a monomer. Bottom: Molecular model used to predict the propagation rate coefficient of the mid-chain radical (MCR). It consists of a trimer radical, propagating towards a monomer.

porated in previous work, was unnecessary for this model, because the influence of the stereochemistry of adjacent units on the rate coefficient in propagation reactions is minimal.<sup>74</sup> Furthermore, the computational effort, required to calculate the large structures of the model, can be significantly reduced by using a single diastereomer, making the calculations more feasible.

Similarly, the MCR propagation rate coefficient,  $k_{\rm p,m}$ , was calculated using the molecular model shown in Fig. 2 (bottom), which consist of a symmetric trimer  $n{\rm BuA}$  structure with a radical in the middle unit, propagating towards a  $n{\rm BuA}$  monomer. We employed a single diastereomer for this calculation, as the reaction represents an equivalent propagation process with no significant influence from the stereochemistry of adjacent units.

The rate coefficient for the ECR propagation,  $k_{\rm p,e}$ , was calculated using a model consisting of a unimer radical propagating towards a monomer  $n{\rm BuA}$  unit.

Besides DFT analysis, it can be interesting to look at spectroscopic experimental techniques that can prove or measure details about the PMR radical. One technique could be EPR, which can detect different radicals within a system. However, the subtle structural difference between an ECR and a PMR might not be distinguishable by this technique, because in essence, both of these radicals are secondary radicals and the difference arises from the different nearby substituents. One can only hypothesize about which effect is greater than the other. In Kajiwara's work, <sup>89–91</sup> the noisy spectrum at lower temperatures might be a result of the subtle differences between ECR and PMR, but nobody has looked for these species before because the PMR has not been discussed previously. Another technique might be detection by nuclear mag-

netic resonance (NMR). However, the applicability of this technique comes likely with various challenges because polymer samples produce a high signal-to-noise ratio, due to the existence of the large –CH<sub>2</sub>– signal. Hence, overall DFT is expected to be the easiest way to study the qualitative differences between ECR and PMR.

## **Kinetic Monte Carlo model details**

For the prediction of the complete PLP-SEC trace and inflection point data, the previously developed kinetic Monte Carlo (kMC) model of our group was utilized as a starting point  $^{18,28,34,54}$  but including the two extra reactions with PMR via the already introduced formulas for  $\gamma$  and  $\delta$  in the introduction (eqn (2) and (3)). It is important to mention that adding two extra parameters to a modelling system provides extra flexibility regarding the description of experimental data. However, both these parameters,  $\gamma$  and  $\delta$ , are introduced to physically account for rate coefficients of species that likely have different reactivities because their chemical structures are different.

The kMC model considers a detailed reaction scheme, accounting for chain length (and monomer conversion) dependent apparent termination reactivities with all kinetic parameters taken from the literature (with  $\gamma=1$ ). Under the conditions studied, namely a low temperature, a low monomer conversion and a high pulse rate,  $\beta$ -scission, macromonomer propagation and thermal self-initiation can be ignored. <sup>18</sup>

The Arrhenius parameters for termination (and chain transfer to monomer) with PMR are approximated as if the radical was an ECR. Fig. S1 of the ESI† shows that the impact of PMR-based radical termination over the polymer properties is limited within the expected theoretical limits, being defined by mutual ECR termination and mutual MCR termination,

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supporting this approximation. Additionally, any previous determination of termination reactivities might have clumped the effect of the PMR in the reported values, making the approximation of PMR reactivity as an ECR quite suitable. If the PMR termination kinetics would be of more relevance, the introduction of another type of radical would complicate further the determination of termination rate coefficients. However, this radical will not dominate the amount of radicals within the PLP so it is not kinetically relevant in the context of the present work.

Taking into account the decrease in light intensity along the optical path, <sup>92</sup> the amount of radicals produced by photodissociation ( $\Delta R_0$ ) is explicitly calculated: <sup>28,34,93,94</sup>

$$\Delta[\mathbf{R}_0] = 2\varPhi \frac{E_{\mathrm{pulse}}\lambda}{hcN_{\mathrm{A}}V}[1 - \exp(-2.303\varepsilon[\mathbf{I}_2]L)] \tag{5}$$

in which  $\Phi$  is the quantum yield for photodissociation as ideally determined at low temperature with no kinetic relevance of PMR (and MCR) species,  $\lambda$  the wavelength of the laser,  $E_{\rm pulse}$  the energy of a laser pulse, h the Planck constant, c the speed of light,  $N_{\rm A}$  the Avogadro constant, V the volume of the sample,  $[I_2]$  the photoinitiator concentration,  $\varepsilon$  the molar absorptivity, and L the optical path length.

The kMC model simulates the PLP experiment, including a total number of 100 pulses and an additional consideration of 10 seconds of reaction until the quenching agent is introduced in line with Marien  $et~al.^{34}$  The log-MMDs are corrected for SEC broadening, in agreement with work by Buback  $et~al.^{103}$  (SEC broadening  $\sigma_{\rm v}b=0.042$ ). Also here it is recommended to have this SEC broadening determined at lower temperatures where the effects of the PMR and MCR are irrelevant.

A Monte Carlo control volume of  $10^{-14}$  L is considered to ensure convergence, considering previous work, optimizing the required simulation conditions to achieve the desired convergence in PLP simulations with many peaks and radical species.  $^{104,105}$ 

## Results and discussion

In what follows, we first highlight that  $\gamma$  is likely not too close to 0 (e.g. not 0.01), by considering FRP simulations  $\nu s$ . typical experimental trends to then finetune that  $\gamma$  is likely also not too close to 1 (e.g. not 0.8), based on DFT calculations. We then propose a PLP-based method to determine  $\gamma$  with a first assessment of its value being 0.1 (325 K) based on literature data, to also formulate guidelines on the determination of acrylate specific rate coefficients in a roadmap format, including a focus on  $\delta$ .

# Sensitivity analysis under FRP conditions: likely a $\gamma$ value not too close to 0

For  $\gamma = 1$ , a PMR becomes an ECR and, hence, the original kMC model from our previous work results. <sup>18,28,34,54</sup> For (solution) FRP conditions (333 K; AIBN as conventional initiator), this means variations for the monomer conversion, log-MMD,

and MMD branching density at a monomer conversion of 0.9, as shown by the dark green lines/points in Fig. 3.

Specifically, the monomer conversion profile time range (hour scale) and the branching density (1–3%) are in line with typical experimental variations. <sup>106,107</sup> Note that Zhang *et al.* <sup>108</sup> *e.g.* shows that a methyl acrylate (MA) conversion of 40% results in roughly half an hour. As *n*BuA propagates faster than MA, the dark green line in Fig. 3a can be seen as at least qualitatively representative.

Moreover, Fig. 3 presents the updates for the conversion profile, log-MMD and branching density in case  $\gamma$  values highly different from 1 are considered (not green but red lines). It follows that for the lowest  $\gamma$  value of zero, a completely different FRP is simulated. If  $\gamma$  is (very) low, implying an MCR-like propagation behavior for PMR, we obtain a very strong retardation, a very pronounced lowering of the chain length (although the branching density remains the same). These shifts are very unlikely seeing that common experimental FRP ranges<sup>106,107</sup> are closer to the green lines/points ( $\gamma$  values larger than 0.01).

Furthermore, as illustrated in Fig. S3 of the ESI,† PMR backbiting has no impact on the key FRP properties, even if a very unrealistic high rate coefficient would be employed, implying a very high backbiting scaling factor  $\delta$  (eqn (3)).

## DFT mechanistic insights: a $\gamma$ value likely not too close to 1

The DFT predicted rate coefficients are shown in Table 2 along with a previously published result *via* computational chemistry. Our calculations reveal a higher activation energy and a lower pre-exponential parameter for PMR propagation, which could be related to the use of difference combination of basis set and model for the energetic correction. The difference between the literature published rate coefficient and our DFT calculation must be seen as qualitatively close. A comparison of exact numbers must be made with care because the energy correction method and the basis sets used are different, which can cause even orders of magnitude of difference. Moreover, the DFT predictions for ECR and MCR propagation are a good match with experimental values found out in literature. <sup>25,72</sup>

According to the computational chemistry results, the calculated PMR propagation rate coefficient is lower than the ECR propagation rate coefficient and more similar to the rate coefficient of the MCR propagation, hence,  $\gamma$  is likely not too close to 1. The FRP results of Fig. 3 hinted at the opposite result so that overall intermediate  $\gamma$  values are too be expected. In any case, one should be careful by simply plugging in values from computational chemistry in kinetic modeling studies. However, the current DFT study gives credibility to the existence of a PMR with different reactivity than an MCR and ECR.

## Further mechanistic insights: introducing a non-zero $\delta$

The PMR species is likely capable of undergoing backbiting, similar to an ECR, although with some mechanistic differences. The ECR readily undergoes backbiting, due to the availability of a hydrogen atom for abstraction at a position that

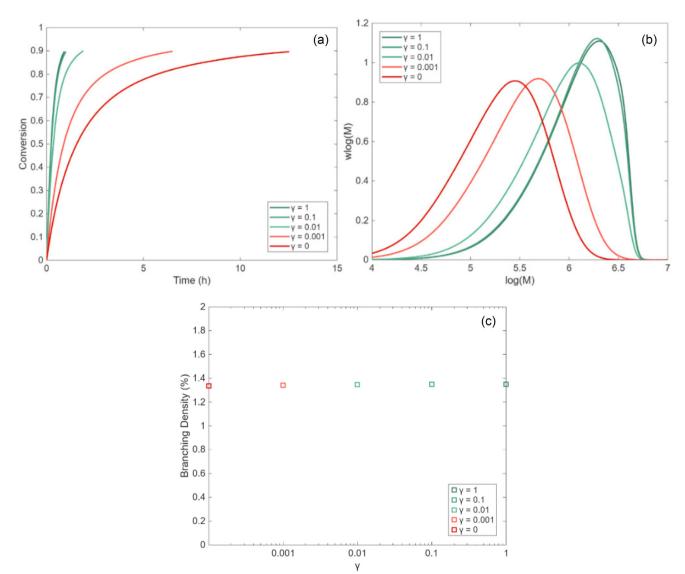


Fig. 3 kMC simulation of FRP of *n*BuA initiated by AIBN, considering the parameters in Table 1 for different values of  $\gamma$  ( $\delta$  fixed at 1). (a) Monomer conversion vs time (h). (b) Log-MMD at a monomer conversion of 0.9. (c) Branching density at a monomer conversion of 0.9, defined as number of branches per monomer unit; 333 K and solvent fraction of 0.55; [AIBN]<sub>0</sub> =  $3 \times 10^{-3}$  mol L<sup>-1</sup>. Green lines are realistic simulations so not too low  $\gamma$  values are expected (the currently accepted model is with  $\gamma$  = 1 and gives specifically the expected experimental variation in polymerization rate). In the current work we assess  $\gamma$  as 0.1 at 325 K, consistent with the statement of not too low  $\gamma$  values.

facilitates the formation of a stable 6-membered ring transition state. In contrast, the PMR has a more restricted polymer backbone, implying at first sight a  $\delta$  lower than 1. However, as shown at the top of Fig. 4, a PMR has available hydrogens atoms on both sides ("left" and "right") so that ignoring the previous effect a  $\delta$  of 2 could be used.

The most likely reaction at low temperature conditions for the formed MCRs is further propagation with monomer, leading to the structures depicted in Fig. 4 (bottom). The obtained products represent extra PMRs in terms of the radical placement in relation to the polymer backbone. However, now the structures have only one hydrogen atom available for an extra abstraction, as opposed to the two hydrogen atoms present in the initially formed PMR. This structural difference creates an issue with the previously introduced factor 2 used to account for the two backbiting possibilities (assuming a "lumped" PMR species). One can thus expect more a factor between 1 and 2 (still assuming similar mobilities between "left" and "right").

Furthermore, the consideration of PMR backbiting (and further reactions) can result in a series of short branches next to each other. Such PMR-based mechanism increases the number of branches and additionally serves as a new mechanism for radical migration, similar to the consecutive six-ring hydrogen abstraction mechanism proposed by Kajiwara. <sup>89–91</sup> This author stated that an actual mechanism is still ambiguous but there should be some stabilized mechanism to form helical structures of the model propagating radicals that have

Table 1 Reactions and respective Arrhenius parameters applied in the kMC model for PLP and FRP; note that for  $\gamma = 1$  a PMR becomes an ECR, hence, the original model is obtained 18,28,34,54

| Nr | Reaction                          | Equation  | A, L mol <sup>-1</sup> s <sup>-1</sup> or s <sup>-1</sup> | $E_{ m a}$ , kJ ${ m mol}^{-1}$ | $k \equiv 306 \text{ K},$<br>L mol <sup>-1</sup> s <sup>-1</sup> or s <sup>-1</sup> | Ref.          |
|----|-----------------------------------|---|---|---------------------------------|---|---------------|
| 1  | Photo-dissociation <sup>a,b</sup> | $I_2 \xrightarrow{h\nu} R_{0,e}^{\mathrm{I}} + R_{0,e}^{\mathrm{II}}$   |   |                                 |   | 18 and 28     |
| 2  | Chain initiation <sup>c</sup>     | $R_0^{\mathrm{I/III}} + \mathbf{M} \stackrel{k_{\mathrm{p.I/III}}}{\longrightarrow} R_{1,\mathrm{e}}$   | $2.4\times10^8$   | 17.9                            | $2.1\times10^5$   | 25, 34 and 95 |
| 3  | $Propagation^d$                   | $R_{i,\mathrm{e}} + \mathbf{M} \xrightarrow{k_{\mathrm{p.e}}} R_{i+1,\mathrm{e}}$   | $2.2\times10^7$   | 17.9                            | $1.9\times10^4$   | 25            |
| 4  |                                   | $R_{i,\mathrm{m}} + \mathbf{M} \xrightarrow{k_{\mathrm{p,m}}} R_{i+1,\mathrm{P}}$   | $1.94\times10^6$  | 28.3                            | $1.4\times10^{1}$   | 18            |
| 5  |                                   | $R_{i,\mathrm{P}} + \mathbf{M} \xrightarrow{k_{\mathrm{p},\mathrm{P}}} R_{i+1,\mathrm{e}}$  | $k_{\rm p,P} = \gamma (k_{\rm p,e} - k_{\rm p,r})$        | $_{\rm m}) + k_{ m p,m}$        |   | This work     |
| ō  | Backbiting                        | $R_{i,\mathrm{e}} \xrightarrow{k_\mathrm{bb}} R_{i,\mathrm{m}},  i \geq 3$  | $1.6\times10^8$   | 34.7                            | $1.9\times10^2$   | 18            |
| 7  |                                   | $R_{i,\mathrm{P}} \stackrel{k_{\mathrm{bb},\mathrm{P}}}{\longrightarrow} R_{i,\mathrm{m}},  i \geq 3$   | $k_{ m bb,P} = \delta k_{ m bb}$                          |                                 |   | This work     |
| 3  | Chain transfer to monomer         | $R_{i,e} + \mathbf{M} \xrightarrow{k_{\mathrm{tr}_{\mathbf{M}},e}} P_i + R_{0,e}^{\mathrm{III}}$  | $2.9\times10^5$   | 32.6                            | $7.8 \times 10^{-1}$  | 96            |
| )  |                                   | $R_{i,\mathrm{m}} + \mathbf{M} \stackrel{k_{\mathrm{tr_{\mathbf{M}},m}}}{\longrightarrow} P_i + R_{0,\mathrm{e}}^{\mathrm{III}}$                    | $2.0\times10^5$   | 46.1                            | $2.7 \times 10^{-3}$  | 96            |
| 10 |                                   | $R_{i,\mathrm{P}} + \mathbf{M} \overset{k_{\mathrm{tr}_{\mathbf{M}},\mathrm{P}}}{\longrightarrow} P_i + R_{0,\mathrm{e}}^{\mathrm{III}}$            | $2.9\times10^5$   | 32.6                            | $7.8 \times 10^{-1}$  | This work     |
| 11 | Termination <sup>e</sup>          | $R_{i,\mathrm{e}} + R_{j,\mathrm{e}} \stackrel{k_{\mathrm{t,app},i,j}^{\mathrm{e-e}}}{\longrightarrow} P_{i+j}$                                     | $1.3\times10^{10}$  | 8.4                             | $9.6\times10^8$   | 97            |
|    |                                   | $R_{i,\mathrm{e}} + R_{j,\mathrm{e}} \stackrel{k_{\mathrm{t,app},i,j}^{\mathrm{e}-\mathrm{e}}}{\longrightarrow} P_i + P_j$                          |   |                                 |   |               |
| 12 |                                   | $R_{i,\mathrm{e}} + R_{j,\mathrm{m}} \stackrel{k_{\mathrm{t,app},i,j}^{\mathrm{e-m}}}{\longrightarrow} P_{i+j}$                                     | $4.2\times10^{9}$   | 6.6                             | $2.1 \times 10^8$   | 97            |
|    |                                   | $R_{i,\mathrm{e}} + R_{j,\mathrm{m}} \stackrel{k_{\mathrm{t,app},i,j}^{\mathrm{e-m}}}{\longrightarrow} P_i + P_j$                                   |   |                                 |   |               |
| 13 |                                   | $R_{i,\mathrm{m}} + R_{j,\mathrm{m}} \stackrel{k_{\mathrm{t,app},i,j}^{\mathrm{m-m}}}{\longrightarrow} P_{i+j}$                                     | $9.0 \times 10^6$   | 5.6                             | $2.0\times10^6$   | 97            |
|    |                                   | $R_{i,\mathrm{m}} + R_{j,\mathrm{m}} \stackrel{k_{\mathrm{t,app},i,j}^{\mathrm{m-m}}}{\longrightarrow} P_i + P_j$                                   |   |                                 |   |               |
| 14 |                                   | $R_{i,\mathrm{P}} + R_{j,\mathrm{P}} \stackrel{k_{\mathrm{t,app},ij}^{\mathrm{P-P}}}{\longrightarrow} P_{i+j}$                                      | $1.3\times10^{10}$  | 8.4                             | $9.6 \times 10^8$   | This work     |
|    |                                   | $R_{i,\mathrm{P}} + R_{j,\mathrm{P}} \stackrel{k_{\mathrm{t,app},ij}^{\mathrm{P-P}}}{\longrightarrow} P_i + P_j$                                    |   |                                 |   |               |
| 15 |                                   | $R_{i,\mathrm{P}} + R_{j,\mathrm{e}} \stackrel{k_{\mathrm{t,app},i,j}^{\mathrm{P-c}}}{\longrightarrow} P_{i+j}$                                     | $1.3\times10^{10}$  | 8.4                             | $9.6 \times 10^{8}$   | This work     |
|    |                                   | $R_{	ext{i},	ext{P}} + R_{j,	ext{e}} \stackrel{k_{	ext{t},	ext{app},ij}^{	ext{P}-	ext{e}}}{\longrightarrow} P_i + P_j$                              |   |                                 |   |               |
| 16 |                                   | $R_{i,\mathrm{P}} + R_{j,\mathrm{m}} \stackrel{k_{\mathrm{t,app},ij}^{\mathrm{P-m}}}{\longrightarrow} P_{i+j}$                                      | $4.2 \times 10^{9}$                                       | 6.6                             | $2.1 \times 10^8$   | This work     |
|    |                                   | $R_{i,\mathrm{P}} + R_{j,\mathrm{m}} \stackrel{k_{\mathrm{t,app},i,j}^{\mathrm{P-m}}}{\overset{k_{\mathrm{t,app},i,j}}{\longrightarrow}} P_i + P_j$ |   |                                 |   |               |
| 17 |                                   | $R_{0,\mathrm{e}}^{\mathrm{I/II/III}} + R_{0,\mathrm{e}}^{\mathrm{I/II/III}} \overset{k_{\mathrm{t.app},i,j}^{0-0}}{\longrightarrow} P_0$           | $1.3\times10^{10}$  | 8.4                             | $9.6 \times 10^8$   | f             |
| 18 |                                   | $R_{0,\mathrm{e}}^{\mathrm{I/II/III}} + R_{i,\mathrm{e}} \stackrel{k_{\mathrm{t,app},i,j}^{0-\mathrm{e}}}{\longrightarrow} P_i + (P_0)$             | $1.3\times10^{10}$  | 8.4                             | $9.6 \times 10^{8}$   | g             |
| .9 |                                   | $R_{0,\mathrm{e}}^{\mathrm{I/II/III}} + R_{i,\mathrm{m}} \stackrel{k_{\mathrm{t,app},ij}^{0-\mathrm{m}}}{\longrightarrow} P_i + (P_0)$              | $4.2 \times 10^9$   | 6.6                             | $2.1 	imes 10^8$  | h             |
| 20 |                                   | $R_{0,\mathrm{e}}^{\mathrm{I/II/III}} + R_{i,\mathrm{P}} \stackrel{k_{\mathrm{t.app},ij}^{0-\mathrm{e}}}{\longrightarrow} P_i + (P_0)$              | $1.3\times10^{10}$  | 8.4                             | $9.6 \times 10^8$   | i             |

<sup>&</sup>lt;sup>a</sup> Initiator radicals (I and II) are different radicals created by the photodissociation of DMPA. <sup>34</sup> <sup>b</sup> For the FRP case, we use instead an initiator dissociation with the following kinetic parameters:  $A = 3.1 \times 10^{15}$  s<sup>-1</sup> and  $E_a = 131$  kJ mol<sup>-1</sup>. <sup>98,99</sup> For the PLP case the amount of initiator radicals produced by photodissociation in each laser pulse is calculated by eqn (5). Using  $\lambda = 351 \times 10^{-9}$  m,  $E_{\text{pulse}} = 2.5 \times 10^{-3}$  J,  $V = 2 \times 10^{-7}$  m³ and  $L = 5.2 \times 10^{-3}$ , <sup>34</sup>  $\Delta[R_0]$  equals  $4.8 \times 10^{-5}$  mol L<sup>-1</sup> at the first laser pulse. <sup>c</sup> The second radical of the initiator  $R_{0,\text{II}}$  is considered to not chain initiate. <sup>d</sup> Only the plateau value is shown for ECR propagation reactivity, chain length dependency is considered based on the work of Heuts and Russell, <sup>71</sup> see ESI S2.† <sup>e</sup> Chain length dependent apparent termination rates are considered (see ESI S2†); <sup>97</sup> only the apparent unimer rate coefficient is shown, taking into account a correction factor 2; <sup>100</sup> the fraction of termination done by recombination is assumed 0.9 for entries 11, 17 and 18, 0.3 for entries 12 and 19, and 0.1 for entry 13, in agreement with literature data; <sup>101,102</sup> one of the disproportionation products is a macromonomer (not assumed reactive). <sup>f</sup> Assumed equal to  $k_{(t,e-e)}^{app}$  (1,1);  $k_{(t,e-e)}^{app}$  (1,1) is reported here. <sup>h</sup> Assumed equal to  $k_{(t,e-e)}^{app}$  (1,1);  $k_{(t,e-e)}^{app}$  (1,1);  $k_{(t,e-e)}^{app}$  (1,1) is reported here. <sup>h</sup> Assumed equal to here.

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**Table 2** Arrhenius parameters determined *via* DFT calculations for the different propagations involved in *n*BuA polymerization: ECR propagation, MCR propagation and PMR propagation. Literature values are also included for the latter

| Reaction  | Model/basis set                                     | A, L mol <sup>-1</sup> s <sup>-1</sup>  | $E_{\rm a}$ , kJ ${ m mol}^{-1}$ | k (306 K), L mol <sup>-1</sup> s <sup>-1</sup>                                  | Ref.                                      |
|---|---|---|----------------------------------|---|---|
| ECR propagation<br>MCR propagation<br>PMR propagation | B3LYP/M06-2X//6-311+G(d,p) B3LYP/MPWB1K//6-31G(d,p) | $7.21 \times 10^{6}$ $8.93 \times 10^{5}$ $1.33 \times 10^{6}$ $1.17 \times 10^{5}$ | 21.3<br>25.0<br>27.5<br>20.2     | $1.7 \times 10^{3}$ $4.9 \times 10^{1}$ $2.7 \times 10^{1}$ $4.2 \times 10^{1}$ | This work<br>This work<br>This work<br>69 |

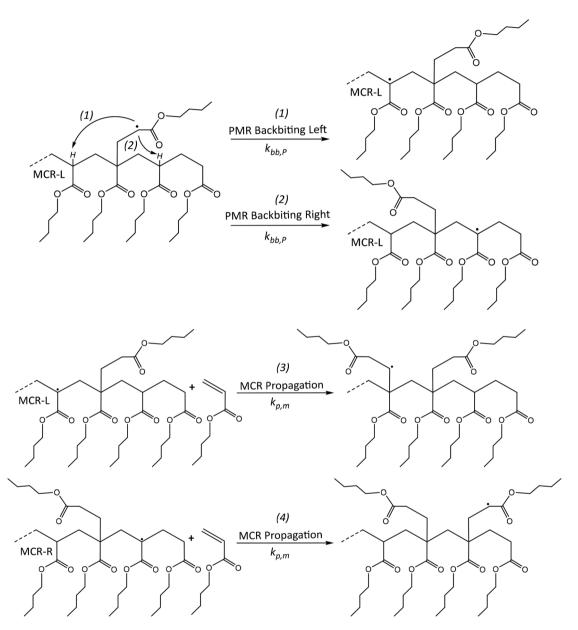


Fig. 4 Top: Two backbiting reactions for PMR, for simplicity L(eft) and R(ight); Bottom: follow-up propagations.

longer alkyl side groups. In this context, we hypothesize that the PMR will be part of the cause of said phenomena.

Note that short chain branching is a well-known structural property of vinyl polymers such as low density polyethylene.  $^{93}$ 

However, the consideration of PMR backbiting in acrylate polymerization kinetics (and further reactions) can result in two types of different branches: the first, a series of sequential short branches next to each other separated only by one monomeric **Paper** 

unit, the second, a branch with 3 or more units with little 1 unit protrusions. The first is a product of the PMR backbiting towards the "right" (see Fig. 4) and then further propagation of the MCR/ PMR. The second is a product of the PMR backbiting towards the "left" (see also Fig. 4), resulting in a 3 unit branch with a small 1 unit protrusion. This last type of branch can be further extended with further PMR backbiting/MCR propagation sequences, extending the short branch by one unit and adding one small protrusion each time the cycle is repeated.

## Kinetic Monte Carlo PLP simulations to determine $\gamma$ and $\delta$

As highlighted in eqn (2),  $\gamma$  is a factor that adjusts the value of  $k_{p,P}$  linearly between its extreme theoretical values of either MCR or ECR propagation behavior ( $\gamma = 0$  and 1). In this subsection, we exploit PLP conditions to identify in the SEC trace sensitivities towards this  $\gamma$  factor. In a first phase, we deal with a frequency of 500 Hz, 100 laser pulses, a temperature of 306 K, and bulk conditions ( $\delta$  fixed to 1).

The results of the sensitivity analysis are shown in Fig. 5 (left) and indicate sensitivity of the PLP-SEC peak heights with respect to a  $\gamma$  variation. With  $\gamma$  becoming smaller, the average length of the polymer chains is reduced, because the PMR propagation resembles more the slower MCR propagation. This is consistent with the height of the first peak increasing (more shorter chains) and a reducing of the height of the second peak (less longer chains). The same trend is followed by the left and right tail of the MMD. The front (left tail), dealing with shorter chains, is more evident in case  $\gamma$  is lower, and the (right) tail, dealing with longer chains becomes less stretched in case  $\gamma$  is lower.

It should be reminded that in Fig. 5 (left) the  $\gamma$  values between 1 and 0.01 are the more realistic ones. As shown in Fig. S4 of the ESI,† still at 500 Hz but taking a temperature of 325 K, a reasonable experimental description of the PLP log-MMD is indeed obtained for a  $\gamma$  of 0.1. It should although be reminded that no other parameters have been tuned and here only one literature frequency is considered.

Notably, as shown by the triangles in Fig. 5 (left), the  $\gamma$  variation at this studied high frequency of 500 Hz does not move the first inflection point of the MMD, which is used to determine  $k_{p,app}$  via eqn (1). This implies the overall consistency of the PLP-SEC method previously applied to determine  $k_{p,app}$  for acrylates.21-27 The introduction of PMR as a different species does thus not invalidate previous research using a "simplified" model under the conditions of high frequency and low temperature. Complementary, the PMR as a new species can help to describe other features of the log-MMD and branching levels that were previously inaccessible.

The extra PMR species changes the quasi-steady state based expression of the average propagation rate coefficient  $k_{\text{p.av}}$ , as highlighted in section S5 of the ESI.† Such average  $k_{p,av}$  is more representative for lower PLP frequencies, hence, one can expect that at such frequencies the consistency of the inflection points no longer holds. Indeed, as shown in Fig. 5 (right) at a lower frequency of 50 Hz, the inflection point of the MMD becomes sensitive to the value of  $\gamma$ . Lower values of  $\gamma$  shift the inflection point, due to the slower propagation with PMR, reducing  $k_{\text{p,app}}$  even by half if  $\gamma$  is very low. However, the likelihood of such a low value of  $\gamma$  is very low, reminding the results in Fig. 3 for the FRP case.

The clear sensitivity of the peak heights at different frequencies in Fig. 6 (left) is the basis to experimentally determine  $k_{p,P}$  in future work, at least if the frequencies are not too low (reminding Fig. 5; right). Fig. 6 (left) shows how the ratio of these peak heights (first vs. second:  $h_1/h_2$ ) changes dependent on the pulse laser frequency as a function of  $\gamma$ . For a

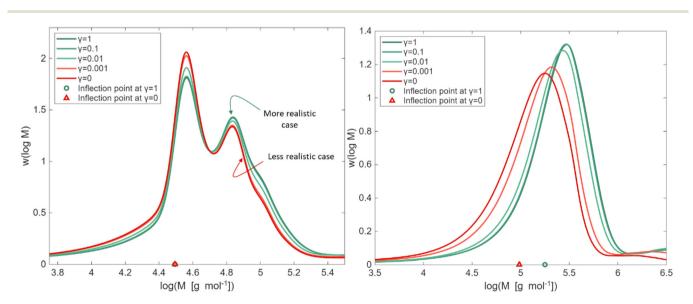


Fig. 5 Left: kMC simulation of bulk PLP of nBuA at a laser pulse frequency of 500 Hz and 306 K, with a variation of  $\gamma$  (eqn (2);  $\gamma = 1$  implying  $k_{\rm p,P} = 1$  $k_{\rm p,e}$  and  $\gamma=0$  implying  $k_{\rm p,P}=k_{\rm p,m}$ ). Right similar plot but at a lower laser pulse frequency of 50 Hz; on the x-axis the identification of the first inflection points (left coinciding; right shift). Same coloring as in Fig. 3, regarding expected behavior.

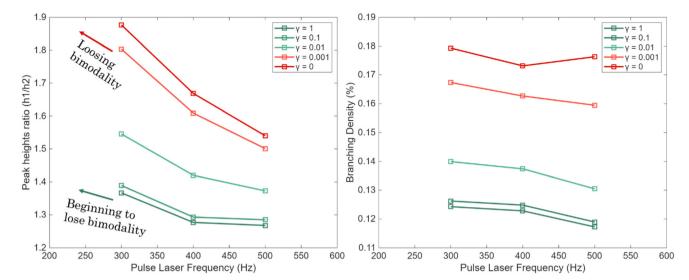


Fig. 6 Left peak heights ratio at different values of  $\gamma$  (egn (2)) for PLP of nBuA at a laser pulse frequency of 500 Hz, at 306 K, and in bulk. The green lines represent the more likely values of  $\gamma$  within the 1–0.01 range (see Fig. 1), and the red lines represent the more unlikely values of  $\gamma$  between 0.001-0. Right Corresponding branching densities.

lower  $\gamma$ , the peak ratio increases and for a given  $\gamma$  a lower frequency has the same effect. For a lower  $\gamma$  (close to 0), a quasilinear behavior is obtained with a lower frequency, and for a higher  $\gamma$  (close to 1) a clearer change in slope is obtained, with more steepness for a lower frequency. Extra sensitivity is thus identified, as slope dependency would be seen or not, likely the former seeing the discussion of the FRP data in Fig. 3.

As shown in section S6 of the ESI,† at lower frequencies, the bimodality of the SEC trace starts to disappear, consistent with Nikitin's work on backbiting.43 The behavior of the double peaks is maintained roughly until a frequency of 300 Hz, with further lowering resulting in the loss of the bimodality behavior for  $\gamma$  values closer to 0.

It should also be admitted that the experimental determination of  $k_{p,P}$  by using the peak heights comes with several challenges, because these heights are also dependent on the termination kinetics, the pulse radical production and SEC broadening. Regarding termination kinetics, section S1 of the ESI† shows the negligible relevance of PMR termination towards the overall system. The pulse radical production in turn can cause differences in the peak heights as the amount of radicals produced change the rates of termination, causing macromolecules to move from one peak to the other. However, the amount of initiator radicals produced per pulse can be calculated using the Beer-Lambert law: 92 eqn (5). This equation allows to calculate the amount of radicals produced per pulse, and it is dependent on the properties of the laser and volume of the sample, which are not affected by the PMR kinetics. Additionally, the amount of radicals produced is affected by the quantum yield, which can also be related to the peak heights, <sup>28</sup> although this parameter can be determined at a low temperature at which PMR/MCR are irrelevant. Hence, effectively decoupling the pulse radical production from the PMR kinetics is possible. Similarly, the band broadening function

can be determined through independent experiments, especially for the acrylics esters whose propagation rates are high. 109 These independent calibration experiments use narrow standard polymers, integrity plots, or band broadening function deconvolution with known distributions. 110,111

Fig. S7 of the ESI† shows the fractions of ECR, MCR and PMR as a function of temperature for different  $\gamma$  values at a frequency of 20 Hz, supported by EPR experimental data from Willemse et al.56 considering only ECR and MCR fractions. In any case, the MCR radicals are dominant and PMR radicals are the least present in such a way that the trend from Willemse et al. 56 remains. Again the current work is thus in line with previously established trends.

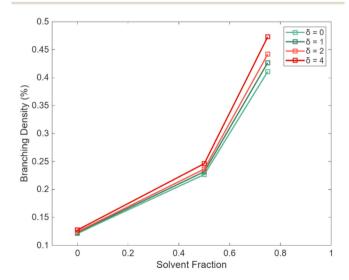


Fig. 7 Branching density as a function of the solvent fraction for different  $\delta$  (eqn (3)) values; PLP conditions: 500 Hz, at 306 K, fixing the value of  $\gamma$  to 1. In practice, one likely will end up setting  $\delta$  equal to 1.

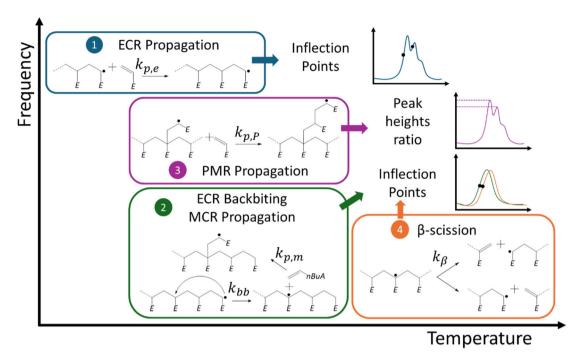


Fig. 8 Roadmap to determine acrylate specific intrinsic rate coefficients, using PLP technique in combination with kMC simulations; not shown is the determination of  $k_{bb,P}$  for which branching densities can be used in Step 3, although likely  $k_{bb,P}$  is seen as  $k_{bb}$ .

Additional to the peak heights ratios, the branching density, which is accessible by NMR, shows sensitivity to the value of  $\gamma$ , as shown in Fig. 6 (right). In case PMR propagation becomes slower (smaller  $\gamma$ ), the backbiting with PMR is more prominent, generating more one-unit branches besides each other in the polymer backbone, therefore, increasing the amount of branches as the value of  $\gamma$  decreases. Reminding the FRP results, a too low  $\gamma$  is although not expected, as otherwise the simulated values for the branching density are too high compared to typical measured branching densities of PLP-made acrylate polymers. Hence, the results in Fig. 6 (right) highlight that the branching density could serve as a property to determine the value of  $\gamma$  together with the peak heights ratio, although NMR analysis is more tedious. In any case,  $\gamma$  values between 0.1 and 1 seem to be undistinguishable.

For the  $\delta$  factor (eqn (3)), the sensitivity toward PLP parameters is much less. For example, as shown in Section S8 of the ESI† there is no sensitivity towards branching density, the inflection point nor the peak height, even at unlikely high  $\delta$  values ( $\gamma$  fixed at 1). However, by increasing the PLP solvent fraction, we can exploit the relation between the monomolecular backbiting reaction and the bimolecular propagation reaction. Fig. 7 shows the effect of varying the solvent fraction for the branching density at different values of  $\delta$ . It follows that for a sufficiently diluted system a certain sensitivity is obtained, at least in case  $\delta$  would be above 1, which is unfortunately in the more unrealistic zone of expected parameters. Hence, we expect that in many experimental cases we would end up with a  $\delta$  set to 1.

Roadmap to determine  $k_{\rm p,e}$ ,  $k_{\rm p,m}$ ,  $k_{\rm p,P}$ ,  $k_{\rm bb}$ ,  $k_{\rm bb,P}$ , and  $k_{\rm \beta}$ . Supported by previous work on  $k_{\rm p,e}$  and  $k_{\rm \beta}$  determination 18,25 and the insights in the present work, we

can formulate a step-wise PLP roadmap to come to reliable  $k_{p,e}$ ,  $k_{p,m}$ ,  $k_{p,p}$ ,  $k_{bb}$ ,  $k_{bb,p}$ , and  $k_{\beta}$  data, as illustrated in Fig. 8.

For the PLP experiments, a distinction is made between frequency and temperature as well as four steps, in each step *e.g.* accounting for 3 temperatures to enable for the determination of Arrhenius parameters.

The first step deals with high frequencies and a low temperature to only allow for sensitivity toward the kinetic parameter with the highest rate coefficient and link to the primary ECR. Hence, Step 1 is devoted to the determination of  $k_{\rm p,e}$ . In Step 2, the temperature is increased and the frequency lowered so that backbiting and tertiary propagation become kinetically relevant. Their joint estimation can be done to then check whether  $k_{\rm p,P}$  (or better said  $\gamma$ ; eqn (2)) is interfering or not. Likely this is not the case (so more  $\gamma$  away from 0) as verifiable by looking at the peak height ratios for different frequencies in Step 3. In parallel,  $k_{\rm bb,P}$  (or  $\delta$ ; eqn (3)) can be assessed but it can be expected that this parameter needs to be approximated by  $k_{\rm bb}$  ( $\delta$  = 1). In Step 4, the temperature can be increased to allow for  $\beta$ -scission and, hence, the determination of  $k_{\rm B}$  is within reach.

# Conclusions

By combining DFT and kMC simulations it is demonstrated that a MCR in *n*BuA radical polymerization is not directly transformed in a fully developed ECR. From a fundamental point of view, a propagated MCR (PMR) is better introduced to describe the kinetics in a more fundamental manner.

This PMR is kinetically defined by a transition propagation factor  $\gamma$  somewhat between 0 and 1, these borders implying MCR

and ECR propagation behavior, respectively. kMC simulations under FRP conditions reveal that  $\gamma$  is likely not close to 0, and DFT calculations that  $\gamma$  is likely not close to 1. More importantly, the ratio of the peak heights under PLP conditions (at sufficiently high frequencies) is sensitive to  $\gamma$ , so that this experimentally accessible parameter can become relevant for  $\gamma$  determination in case the interfering model parameters, *e.g.* quantum yield, have been determined at low temperatures. Current literature PLP data at 500 Hz suggest a  $\gamma$  value of 0.1 at 325 K.

Furthermore, it is shown that PMR species can backbite, leading to a new migration mechanism as well as the formation of consecutive branches. Practically, the associated backbiting scaling factor  $\delta$  can be taken equal to 1, although it can be worthwhile to consider a variation of the solvent volume fraction in the PLP region.

The current work puts forward an updated roadmap for the determination of acrylate specific rate coefficients, differentiating between the determination of  $k_{\rm p,e}$ ,  $k_{\rm p,m}$ ,  $k_{\rm p,p}$ ,  $k_{\rm bb}$ ,  $k_{\rm bb,p}$ , and  $k_{\rm b}$ .

## Conflicts of interest

There are no conflicts to declare.

# Data availability

All key data is reported in the manuscript and the ESI.†

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