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Interfacial chalcogen pair-mediated, biaxial strainand interlayer distance-tuneable type-2 band alignment in an SnSSe homogeneous bilayer: a density functional theory-based analysis†

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This study presents a comprehensive density functional theory-based investigation of the electronic properties of homogeneous bilayer Janus tin sulphide selenide (SnSSe) with different interfacial chalcogen pair configurations. This study focuses on interlayer band alignment, wherein the effects of interlayer distance modulation and applied biaxial strain are methodically studied. Next, the spatial distribution and lifetime of excitonic states are systematically analysed from the in-plane and inter-layer atomic orbital interactions, spatial separation of electron-hole wave functions, and spread of the conduction band in energy. Asymmetric interfacial chalcogen pairing exhibits a finite interlayer dipole moment and interlayer electric field. This reduces the energy bandgap and induces prominent type-2 band alignment between individual SnSSe layers, where band edge Bloch states are strongly localized in alternating layers. An increasing interlayer distance and applied biaxial tensile strain were found to retain the type-2 interlayer band alignment. In contrast, reducing the interlayer distance and biaxial compressive strain significantly altered interlayer atomic orbital interactions and annihilated the type-2 band alignment with a sharp reduction in the energy bandgap owing to the strong delocalization of band edge Bloch states. Thus, this study demonstrates the strain tuneable type-2 band alignment and interlayer excitonic properties of homogeneous bilayer SnSSe with broken interlayer mirror symmetry.

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1. Introduction

Recently, the successful realization of a large number of twodimensional (2D) materials with distinct and unique physicochemical properties has shown the potential to reshape the technological landscape, spanning conventional applications such as electronics, optoelectronics, sensing, photonics, and energy storage as well as emerging applications such as spintronics and valleytronics.^{1–5} Moreover, an ever-increasing research effort has been observed towards tuning the relevant properties of 2D materials using different material engineering strategies, leading to novel 2D material systems for specific applications. 6,7 In this context, breaking one or more under-

lying symmetries in 2D materials has shown remarkable promise for harvesting emergent electronic/optoelectronic/ magnetic/spintronic properties in such engineered 2D materials.^{7,8} Some of the most notable examples of such approaches include out-of-plane electric field and staggered substrate sub-lattice potential induced inversion symmetry breaking in bilayer graphene, interlayer twisting induced inversion symmetry breaking in bilayer transition metal di-chalcogenides (TMDs), magnetic field induced time reversal symmetry breaking in phosphorene, magnetic substrate induced time reversal symmetry breaking in TMDs, and carrier doping induced gauge symmetry breaking in TMDs. 7,9 In this effect, recently, the successful synthesis of 2D Janus metal dichalcogenides (JMDs), an artificial subclass of metal dichalcogenides (MDs), has paved the path for inherently breaking the out-ofplane (OOP) intra-layer mirror symmetry in monolayer MDs. 10,111 Unlike natural MDs, in JMDs, the metal is covalently bonded to two different chalcogen atoms, breaking mirror symmetry in the OOP direction around the metal atom centre. Furthermore, owing to the different electronegativities of chalcogen atoms, the asymmetric valence charge distributions in

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Paper Nanoscale

the top and bottom chalcogen layers result in a vertical intralayer electric field in JMDs.9 Specifically, the vertical intralayer electric field and natural OOP asymmetry in JMDs significantly influence their electronic/optoelectronic properties. The vertical intralayer electric field in JMDs reduces electron-hole wavefunction overlapping and increases Coulomb screening, leading to longer exciton lifetimes, wherein the natural OOP symmetry breaking in IMDs results in strong Rashba spinorbit coupling (SOC).7,9

MoSSe was the first JMD to be synthesized following the chemical vapor deposition (CVD) technique in 2017. 12,13 During MoSSe synthesis, either the top S-layer of the monolayer MoS₂ is first substituted with H, followed by selenization through vaporization of Se powders, 12 or sulfurization of the top Se-layer of the MoSe₂ monolayer.¹³ In this effect, an alternative room-temperature synthesis process for MoSSe and WSSe was demonstrated using a selective epitaxy atomic replacement process that efficiently removes and thereafter substitutes the top chalcogen layer. 14 Motivated by these advancements in group VIB, i.e. Molybdenum- and Tungsten-based IMD synthesis, several reports have attempted to synthesize other JMDs. Notably, among non-group VIB JMDs, tin (Sn)based JMDs have drawn significant research attention, wherein the successful synthesis of SnSSe has recently been reported using hot injection of Se precursor and S precursor the Sn precursor¹⁵ and plasma-driven solutions into selenization.16

However, research on Sn-based JMDs is still at an early stage, and a comprehensive theoretical understanding of the electronic and optoelectronic properties of these emerging artificial 2D materials is necessary for their effective integration into different devices. In this context, density functional theory (DFT)-based ab initio calculation has emerged as a highly efficient theoretical modelling technique for 2D material systems that can independently estimate the different properties of 2D materials and assess the efficacy of different material engineering strategies for tuning the relevant properties of specific 2D materials. This has led to DFT-based theoretical investigations of different Sn-based JMDs, including SnSSe, SnSeTe, and SnSTe. Recent DFT studies have demonstrated that SnSSe, SnSeTe, and SnSTe monolayers are thermally, dynamically, and mechanically stable. 17,18 Notably, SnSTe and SnSeTe monolayers exhibit metallic behaviour, whereas SnSSe monolayers exhibit indirect semiconducting characteristics. 18,19 This has drawn significant research interests in SnSSe, where the broken OOP mirror symmetry of SnSSe can be exploited for different electronic, optoelectronic, piezoelectric, thermoelectric, and sensing applications. 18,20-22 Specifically, recent DFT investigations have revealed that the electronic properties of monolayer SnSSe can be efficiently tuned by applying mechanical strain, 20,23 out-of-plane direction electric field,23 surface adatom adsorption,24 and vacancy

On the other hand, very recently, the homogeneous (consisting of the same JMD monolayers) and heterostructure (consisting of different JMD monolayers) bi-layer configuration of JMDs has drawn significant traction from researchers, as the interlayer stacking configuration is found to play a crucial role in determining the overall electronic/optoelectronic properties of bilayer JMDs. 26-30 To this effect, the homogeneous bilayers of JMDs offer additional design flexibility regarding their formation with respect to interfacial chalcogen pair specification in specific interlayer stacking configurations. The asymmetric interfacial chalcogen pair breaks the interlayer mirror symmetry around the interface, which can lead to emerging electronic and optoelectronic properties in such homogeneous bilavers. 27-29, 31-33 However, to date, only a few reports are available on the bilayer Janus SnSSe. 29,30,34,35 Typically, strong anharmonic phonon scattering,³⁴ non-zero dipole moments induced built-in electric fields, 30 interlayer stacking-dependent exciton binding energies,29 and interlayer twisting-dependent lattice thermal conductivity35 are theoretically demonstrated in bilayer SnSSe. However, to the best of the authors' knowledge, no reports have attempted to investigate the effects of mechanical strain on bilayer SnSSe, focusing on the effects of strainmediated modulation in interlayer atomic orbital interactions on the electronic properties of bilayer SnSSe. On the other hand, several theoretical and experimental studies have focused on interlayer excitons in vdW heterostructure TMD bilayers.36-39 Specifically, it has been observed that interlayer excitons are highly sensitive to interlayer interactions, and thereby can be efficiently tuned by applying strain or varying interlayer distance by either inserting an insulating layer (usually h-BN) or applying pressure. 36,38-40 In this context, the homogeneous bilayers of Janus TMDs exhibit both symmetric and asymmetric interfacial chalcogen pairings in their different interlayer stacking configurations. 29,33 The broken out-of-plane mirror symmetry along the interface of bilayer Janus TMDs offers a unique possibility of realizing type-2 band alignment and subsequent interlayer excitons under an asymmetric interfacial chalcogen pairing configuration.³³ However, to the best of the authors' knowledge, to date, no theoretical or experimental studies have exclusively analyzed the effects of strain and interlayer distance variation on the properties of interlayer excitons in homogeneous bilayers of Janus TMDs.

Based on this paradigm, in this study, the structural and electronic properties of homogeneous bilayer SnSSe in different interfacial chalcogen pair configurations are extensively studied, emphasizing interlayer charge transfer, dipole moment, electric field, and band alignment at different interfacial chalcogen pairings. Moreover, this study systematically investigates the electronic properties of bilayer SnSSe with asymmetric chalcogen pairing at various interlayer distances under biaxial strain. The key findings of this study are methodically analysed from atomic electronegativity-mediated localized charge distributions, inter-layer atomic orbital interactions, and band edge electronic state localization. In this context, the novelty of this study can be summarized as

1. In this study, for the first time, it was demonstrated that the interlayer band alignment, bandgap and excitonic properties can be efficiently tuned by varying the interlayer disNanoscale Paper

tance and applying biaxial mechanical strain in asymmetric interfacial chalcogen pairing in Janus TMD bilayers.

2. This study introduces a novel approach by systematically analyzing the electronic and excitonic property variations with interlayer distance and applying biaxial strain from the time-energy uncertainty relation near the band edges, spatial localization and overlap of electron and hole wave functions, and interlayer intrinsic electric field.

Finally, the specific contributions of this research in the context of existing theoretical research on other Janus TMD bilayers are summarized in Table 1.

Next, the organization of the subsequent sections of this paper is summarized. Section 2 provides a comprehensive overview of the computational methodology, highlighting the simulation methods and parameters used in the DFT simulations and the parameter definitions used to quantify the relevant material properties. The reliability of the simulation framework was verified by calibrating the calculated structural and electronic properties in accordance with previous literature. Section 3 incorporates a comprehensive stability analysis of the individual bilayers, followed by a detailed account of their structural and electronic properties. Furthermore, in this section, the impact of externally applied biaxial strain and

interlayer distance variations on electronic properties is explored in detail, providing a systematic analysis of the key findings in relation to fundamental atomistic characteristics. Finally, section 4 summarizes the primary outcomes of this study, discusses their significance for potential technological applications, and suggests avenues for future explorations.

Computational methodology

This section presents the computational methodology of this study, in which the material specifications, simulation framework, and analytical parameter definition are discussed in three sub-sections.

2.1. Material specifications

This study focused on the bilayer of Janus tin sulphide selenide (2L-SnSSe). The monolayer tin di-sulphide (SnS₂) and tin di-selenide (SnSe₂) belong to $P\bar{3}m1$ space group with a hexagonal lattice structure, exhibiting mirror symmetry around the central Sn atom, ²⁹ as shown in Fig. 1a and b. However, due to the asymmetrical chalcogen composition of their Janus counterpart, *i.e.* SnSSe lacks mirror symmetry and belongs to a

Table 1 Comparison of the existing literature on the Janus TMD bilayer and this study

Material specification	Ab initio DFT methods	Key findings	Ref.
2L-MoSSe	GGA-PBE	Strain engineering enhances Li diffusion in bilayer	41
2L-MoSSe	GGA-PBE	Interlayer stacking engineering can tune the interlayer dipole moments and carrier mobilities	42
2L-MoSeTe and 2L-WSeTe	GGA-PBE	Rashba spin splitting at the band edges can be tuned using strain engineering	43
2L-WSSe	GGA-PBE	Bandgap and optical anisotropy control using strain engineering	44
2L-SnSSe	GW	Interlayer stacking engineering can tune the energy bandgap and excitonic binding energies	29
2L-SnSSe	GGA-PBE	Interlayer stacking engineering can tune the interlayer dipole moment/electric field and carrier mobility	30
2L-SnSSe [this work]	HSE-06	Strain and interlayer distance engineering to tune interlayer band alignment, bandgap and excitonic lifetime by changing in-plane and out-of-plane orbital hybridization, and electron-hole wave function overlap	_

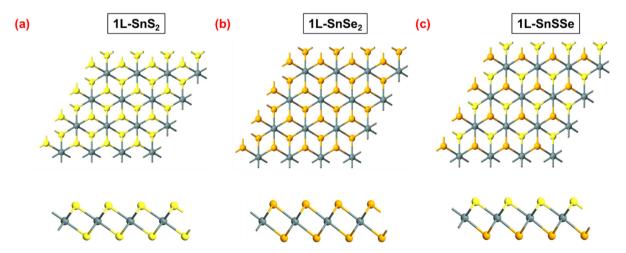


Fig. 1 Schematic representation of the top and side views of a 4 × 4 × 1 super-cell of (a) 1L-SnSe₂, (b) 1L-SnSe₂, and (c) 1L-SnSSe.

Paper Nanoscale

symmetry-reduced *P3m1* space group with a hexagonal lattice structure,²⁹ as shown in Fig. 1c. For the formation of bilayer SnSse, the natural stacking order of bilayer SnS₂ and SnSe₂ is considered in this study, where the Sn atom of the top layer is perfectly aligned with the Sn of the bottom monolayer. This suggests that during bilayer SnSSe formation, three distinct interlayer stacking configurations can be considered based on the interlayer chalcogen pairing layers (*i.e.* S–S, S–Se, and Se–Se) between two monolayers of SnSSe. In their earlier study, the authors reported that interlayer chalcogen pairing plays a vital role in determining the overall electronic properties of any bilayer on Janus TMDs.²⁶

The presence of two different chalcogen atoms in SnSSe indicates that three distinct interface chalcogen pair configurations are possible during bilayer formation.²⁹ Subsequently, in this study, the bilayers of SnSSe are considered in the natural interlayer stacking order (AA) of bilayer SnS2 and SnSe₂, with S-S, S-Se, and Se-Se interlayer chalcogen pairings, in their unit cell $(1 \times 1 \times 1)$ configurations. A previous theoretical study on different artificial and natural SnSSe bilayer stacking orders demonstrated that the natural stacking order is the most stable (with the lowest formation energy) stacking order of bilayer SnSSe.²⁹ Hence, only the natural AA stacking order was considered in this study. In addition, unlike van der Waals (vdW) hetero-bilayers, the three distinct bilayers of SnSSe considered in this study form homogeneous bilayers, where no lattice mismatch strain can be observed, and the unit-cell configuration should suffice for the theoretical analysis. Furthermore, a vacuum of 40 Å is considered in the outof-plane direction of the unit cells of SnS₂, SnSe₂, and SnSSe monolayers and bilayers to ensure no artificial interaction from the periodic images in these directions.^{29,35} Similar to monolayers of SnSSe, natural bilayers of SnSSe also exhibit a hexagonal lattice structure, preserving the hexagonal symmetry of their Brillouin zone. Consequently, the Brillouin zone of all the monolayers and bilayers under investigation in this study was sampled across the characteristic G-M-K-G high symmetry path for energy band structure calculations.

2.2. Simulation framework

This study investigates the structural and electronic properties of materials using first-principles calculations implemented through the Atomistix Tool Kit (ATK) and Virtual Nano Lab (VNL) simulation packages, available from Synopsys Quantum Wise. The first-principal calculations employ a linear combination of atomic orbitals (LCAO) with a PseudoDojo basis set, utilizing a density mesh cut-off energy of 125 Hartree and a 12

× 12 × 1 Monkhorst–Pack grid for sampling the Brillouin zone. Initially, the individual unit cells of monolayers and bilayers of SnSSe are structurally relaxed to minimize the total energy and the forces acting on individual atoms using geometry optimization. This optimization was performed using the limited-memory Broyden–Fletcher–Goldfarb–Shanno (LBFGS) algorithm, with pressure and force tolerances set at 0.0001 eV Å⁻³ and 0.01 eV Å⁻¹, respectively. Furthermore, during geometry optimization, the Generalized Gradient Approximation (GGA) method with the Perdew–Burke–Ernzerhof (PBE) exchange–correlation functional is considered. The structural parameters of the optimized monolayers for SnS₂, SnSe₂, and SnSSe are illustrated in Fig. S1.†

The energetics of individual monolayer materials were also calculated using the GGA method with the PBE exchange-correlation functional.45 For the energy calculations of bilayers, the Grimme DFT-D3 method is employed to accurately account for the vdW interactions between the monolayers, while the counterpoise (CP) correction is applied to mitigate the basis set superposition error (BSSE) inherent in the LCAO basis. 45 Standard DFT methods, such as LDA-PZ and GGA-PBE, tend to underestimate the energy bandgaps of layered materials due to self-interaction errors. 45 Consequently, to attain a more precise assessment of the energy band structures for the geometryoptimized monolayers and homogeneous bilayers, electronic properties were computed using the advanced Heyd-Scuseria-Ernzerhof-06 (HSE-06) method following geometry optimization. Next, the HSE-06 calculated energy bandgaps were compared against existing literature, as summarized in Table 2, which shows reasonable agreement with previously reported HSE calculated bandgap values. 25,46-49 The standard DFT functional, such as GGA, tends to underestimate the bandgaps of 2D semiconductors like SnSSe. However, the advanced HSE-06 functional offers a more accurate assessment of the energy bandgap of 2D semiconductors. 50 Moreover, the HSE-06 functional is widely considered in the theoretical literature for estimating the energy band structures of monolayer and few-layer SnS₂, SnSe₂, ⁴⁷ SnSSe^{20,29,34,51} and some other Janus TMDs. 52-55 Consequently, in this study, the energy band structures are simulated using HSE-06 (with SOC). Finally, in this study, the dynamic stability of bilayers with these chalcogen pairings was investigated using phonon spectrum calculations performed on a 4 × 4 × 1 supercell of bilayers, 29 with a maximum displacement set at 0.01 Å, using the phonopy code.⁵⁶ To estimate the thermal stability of the bilayers of these chalcogen pairings, the Nose-Hoover thermostat-based Ab initio molecular dynamic (AIMD) simulations were per-

Table 2 Structural and electronic properties of relaxed 1L-SnS₂, 1L-SnSe₂ and 1L-SnSSe

Material	Calculated (reported) bond length of $M-X$ (Å)	Calculated (reported) bond angle X–M–X (°)	Calculated (reported) lattice constant (Å)	Calculated (reported) bandgap (eV)
1L-SnS ₂	2.61 (2.59) ⁴⁶	89.51 (90.81) ⁴⁶	$3.71 (3.70)^{46}$	$2.20 (2.40)^{47} 1.35 (1.41)^{47} 1.44 (1.46)^{25}$
1L-SnSe ₂	2.78 (2.73) ⁴⁶	90.98 (90) ⁴⁸	$3.83 (3.86)^{49}$	
1L-SnSSe	Sn-S: 2.65 (2.63), Sn-Se: 2.75 (2.72) ²⁵	89.82 (89.90°) ²⁵	$3.82 (3.78)^{25}$	

Nanoscale Paper

formed at room temperature (300 K) in a $4 \times 4 \times 1$ supercell for 1000 time steps with a total time evaluation of 10 Pico-sec.⁵⁷

In this study, following the theoretical literature, a standard strain range of -5% to +5% is considered. Specifically, theoretically ±10% biaxial strain in monolayer SnSSe, 23 ±10% biaxial strain in monolayer SnS₂, 58 and +5% biaxial strain in monolayer MoSSe⁵⁹ have been reported in the literature. Moreover, experimentally, monolayer MoS₂ is subjected to 3% biaxial strain,60 5.6% biaxial strain,61 bilayer MoS2 is subjected to 2.2% uniaxial strain, 62 3% uniaxial strain, 63 and bilayer WSe₂ is subjected to 5% uniaxial strain.⁶⁴ These theoretical and experimental reports suggest that the ±5% biaxial strain can be considered a standard range of strain for bilayer SnSSe. Next, in the theoretical literature, -0.3 Å to +0.4 Å ILD variation has been reported for bilayer MoSSe, 31 wherein experimental observations indicate interlayer separations reaching up to ~0.68 nm (6.8 Å) in MoTe₂.65 However, in few-layered 2D materials, experimentally, the interlayer distances can be effectively tuned to a larger extent by either inserting an insulating layer (usually h-BN) or applying pressure. 36,38-40 Consequently, in this study, the ILD variation is considered within a reasonable range between -1.5 Å to +1.5 Å for SnSSe bilayers.

2.3. Theoretical model validation

To ensure the consistency and accuracy of the computational framework, a comprehensive validation procedure was implemented through systematic comparison with previous computational reports. This validation process focused on the structural, electrostatic, and electronic properties to verify the reliability of the theoretical calculation framework of this study. The optimized structural parameters (in-plane lattice vector, Sn–S/Sn–Se bond length, and S–Sn–Se bond angle) were compared with existing literature values, as summarized in Table 2. Notably, the calculated structural parameters showed good agreement with previously reported structural properties, 25,46–49 confirming the reliability of the geometry optimization framework used in this study.

Next, for SnSSe bilayers, the calculated lattice vectors of 3.86 Å, Sn-S bond lengths of 2.66 Å, and Sn-Se bond lengths of 2.76 Å are also in reasonable agreement with the reported lattice vectors of 3.77 Å, Sn-S bond lengths of 2.62 Å, and Sn-Se bond lengths of 2.71 Å.³⁴ Furthermore, the calculated inter-layer distances of 2.70 Å (S-S), 2.81 Å (S-Se), 2.97 Å (Se-Se) are also in good agreement with previously reported inter-layer distances of 2.83 Å (S-S), 2.92 Å (S-Se), 2.99 Å (Se-Se).29 For SnSSe bilayers, the HSE calculated bandgap values of 1.49 eV (S-S), 1.47 eV (Se-Se), and 1.27 eV (S-Se) are consistent with previously reported HSE-06-SOC simulated bandgap values of 1.37 eV (S-S), 1.40 eV (Se-Se), and 1.26 eV (S-Se).34 Furthermore, similar to previous theoretical reports, each SnSSe bilayer exhibits an indirect bandgap, with the CBM located at the 'M' point and the 'VBM' at the 'G' point. 29,34 Finally, for the S-Se configuration of the SnSSe bilayer, the calculated interlayer electric field of 0.14 V Å⁻¹ and interlayer dipole moment of 0.27 D

are also comparable to the previously reported electric field of 0.18 V Å^{-1} (ref. 29) and interlayer dipole moment of 0.27 D.³⁰ Thus, the close agreement of the calculated structural, electrostatic, and electronic parameters with those of previous reports confirms the reliability of the computational framework of this study.

2.4. Parameter definitions

In this study, the structural stability of natural SnSSe bilayers was quantified using two key metrics: the cohesive energy per unit atom (E_{coh}) and the interlayer interaction energy per unit in-plane area ($E_{\text{interlayer interaction}}$), which are defined as.²⁶

$$E_{\rm coh} = \frac{E_{\rm bilayer} - (2E_{\rm Sn} + E_{\rm ch1} + E_{\rm ch2} + E_{\rm ch3} + E_{\rm ch4})}{6}$$
 (1)

$$E_{\text{Interlayer_interaction}} = \frac{E_{\text{bilayer}} - (E_{\text{monolayer1}} + E_{\text{monolayer2}})}{(\text{area})}$$
(2)

In eqn (1), $E_{\rm bilayer}$ and $E_{\rm Sn}$ denote the ground-state energies of the vdW bilayer and an isolated Sn atom, respectively. Similarly, $E_{\rm chi,i=1-4}$ represents the ground-state energies of individual chalcogen atoms (i=1-4) within the bilayer. In eqn (2), $E_{\rm monolayer,j=1,2}$ represents the ground-state energies of the individual monolayers (j=1-4), and Area is the in-plane unit cell area of the bilayer. For a structurally stable 2D crystal, the cohesive energy ($E_{\rm coh}$) must be negative, i.e. $E_{\rm coh} < 0$. Similarly, stable bilayer formation requires a negative interlayer interaction energy ($E_{\rm interlayer_interaction}$), i.e. $E_{\rm interlayer_interaction} < 0$. Moreover, larger magnitudes of $E_{\rm coh}$ and $E_{\rm interlayer_interaction}$ indicate superior structural stability and interlayer binding strength of the bilayers, respectively.

The formation of heterostructure bilayers usually involves charge transfer between the constituent monolayers. Similarly, in this study, interlayer charge transfer ($Q_{transfer_layer}$) between individual SnSSe monolayers was considered for individual bilayer SnSSe configurations. The charge transfer is quantified through Mulliken charge analysis, which assigns partial charges to individual atoms in any material system. The $Q_{transfer_layer}$ is represented by:

$$Q_{\text{Transfer_layer}} = Q_{\text{monolayer_in_bilayer}} - Q_{\text{monolayer}}$$
 (3)

In eqn (3), $Q_{\text{monolayer_in_bilayer}}$ and $Q_{\text{monolayer}}$ represent the total Mulliken charges in the monolayer SnSSe within the bilayer and in the isolated monolayers, respectively. In this context, $Q_{\text{transfer_layer}} > 0$ indicates that one monolayer is accepting electrons from another, whereas the other monolayer donates electrons corresponding to $Q_{\text{transfer_layer}} < 0$.

Similarly, the local charge redistributions during lattice formation can be accessed from the Mulliken charge transfer with respect to each atom ($Q_{transfer_atom}$) in Janus monolayers and bilayers, which is expressed as:

$$Q_{\text{transfer_atom}} = Q_{\text{lattice}} - Q_{\text{isolated}} \tag{4}$$

In eqn (4), $Q_{\rm lattice}$ denotes the Mulliken charge of the atom within the lattice, and $Q_{\rm isolated}$ represents the Mulliken charge of the isolated atom.

Paper Nanoscale

Finally, in this study, a biaxial strain is applied to homogeneous bilayers of SnSSe, where the strain (S) is calculated as follows^{66,67}

$$S = \frac{a_{\text{strained}} - a_{\text{relaxed}}}{a_{\text{relaxed}}} \tag{5}$$

In eqn (5), a_{strained} and a_{relaxed} represent the in-plane lattice vectors of the strained and relaxed SnSSe bilayers, respectively. S > 0 indicates the application of biaxial tensile stress, which results in biaxial compressive (BC) strain in the lattice. Conversely, S < 0 corresponds to the presence of biaxial tensile (BT) strain. This study investigates bilayers in a strain range of 5% BT (-5%) to 5% BC (+5%), within which qualitative trends in the modulation of electronic properties due to strain can be reliably analyzed. The range of biaxial strain was consistent with that of previous theoretical reports on strained SnS₂, SnSe₂ and SnSSe.^{23,68-70}

For analysing the electrostatics of SnSSe bilayers, in this study, the electron difference density $(\delta n(r))$ and electrostatic difference potential $(V_{\rm E}(r))$ are considered, which are related to each other by Poisson's equation, as follows:⁴⁵

$$\nabla^2 V_{\rm E}(r) = e \frac{\delta n(r)}{\varepsilon} \tag{6}$$

In eqn (6), e and ε are the charge (magnitude) of an electron and the permittivity of the material system, respectively. The electron difference density represents the difference between the self-consistent valence charge density of the material systems and the superposition of the valence densities of constituting atoms.45

2.5. Glossary of computational terminologies

In this section, brief descriptions of specific computational methods are incorporated for the general readers.

1. Local Density Approximation (LDA)

Local Density Approximation (LDA) is one of the earliest and simplest approximations used in DFT. The exchange-correlation energy at any given point in space is assumed to depend only on the local electron density at that point. LDA provides good results for systems with relatively uniform electron density, such as metals. However, LDA often fails to accurately describe systems where the electron density varies significantly, such as in molecules or semiconductors, and tends to underestimate the band gaps of semiconductor/insulator materials.71,72

2. Generalized Gradient Approximation (GGA)

GGA improved upon LDA by incorporating the electron density gradient in addition to the local density. This allows GGA to account for the spatial variations in electron density, leading to more accurate results. One of the most widely used GGA functionals is the Perdew-Burke-Ernzerhof (PBE) functional. GGA-PBE is usually preferred for geometry optimization and total energy calculations of crystalline materials compared to LDA. However, the GGA-PBE still tends to underestimate the energy band gaps of semiconductors and insulators.⁷²

3. Hybrid functionals - HSE-06

Both LDA and GGA fail to accurately calculate the bandgap semiconductors/insulators with strong correlation. 71,72 To address this limitation, advanced hybrid functionals combine part of the exact exchange from Hartree-Fock (HF) theory with a PBE functional. One of such widely used hybrid functionals is HSE-06 (Heyd-Scuseria-Ernzerhof), which improves upon GGA by incorporating a screened Coulomb interaction in the exchange term. 73,74 HSE-06 is particularly effective for reliably calculating the energy band gaps for a wide range of semiconductors and insulators, including 2D materials.⁷²

4. Mulliken charge analysis

Mulliken charge analysis is a method for partitioning the total electron density into individual atomic contributions by calculating the electron density associated with each atomic orbital.⁷⁵ Mulliken population analysis provides a quantitative measure of charge distributions in individual atoms, resulting in a reliable assessment of charge transfer, electron density redistribution, and bonding characteristics in crystalline materials, including 2D materials.75

3. Results and discussion

Stability analysis of bilayers

The stability of homogeneous bilayer SnSSe is crucial for the accurate estimation of the structural and electronic properties at their equilibrium configuration, as well as for accessing the potential of their experimental realization. Subsequently, in this section, the structural, dynamic and thermal stabilities of SnSSe bilayers with different chalcogen pairings are systematically analysed.

3.1.1 Structural stability and dynamic stability analysis. The homogeneous bilayers of SnSSe with three distinct chalcogen pairings i.e., S-S, S-Se, and Se-Se configurations, are stacked in their natural interlayer stacking (AA) configuration. The structural stabilities of these bilayers were evaluated based on the cohesive energy per atom (E_{coh}) and the interlayer interaction energy per unit in-plane area ($E_{\text{interlayer interaction}}$), as defined in eqn (1) and (2). Fig. 2a shows the cohesive energies of the SnSSe bilayers, indicating that all homogeneous bilayers were structurally stable, as supported by their negative cohesive energies. Fig. 2b presents the interlayer interaction energies for the different bilayers, where the negative interaction energies confirm the stability of the bilayer structures.

Interestingly, Fig. 2a and b illustrate that E_{coh} and Einterlayer interaction remain comparable under different interlayer chalcogen configurations in the SnSSe bilayer. Specifically, marginal variations of ~0.0004 eV per atom in $E_{\rm coh}$ and ~0.001 eV Å⁻² in $E_{\rm interlayer_interaction}$ were observed between different bilayer configurations. This indicates that each interlayer chalcogen configuration is equally likely to form; therefore, these configurations were extensively analysed in this study.

The dynamic stability of individual homogeneous bilayers was determined from the phonon spectrum analysis, as illus-

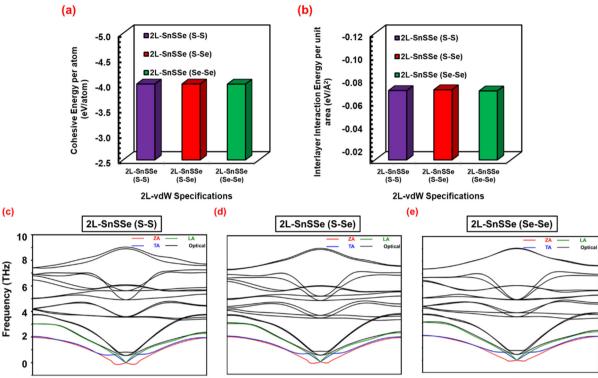


Fig. 2 (a) Cohesive energy, (b) interlayer interaction energy, and (c-e) phonon dispersion curves of 2L-SnSSe for S-S, S-Se, and Se-Se chalcogen pairings.

trated in Fig. 2c-e. In general, each SnSSe bilayer exhibits negligible negative frequencies at the zone center ('G' point), suggesting that the bilayers are dynamically stable, regardless of their interlayer chalcogen pair specifications. The phonon spectrum analysis in this study is consistent with previous reports on SnSSe bilayers, in which all interlayer chalcogen pair configurations were found to be dynamically stable.²⁹ The bilayer SnSSe unit cell contains six atoms, giving rise to 18 phonon branches comprising three acoustic and 15 optical modes. In the acoustic branches, red represents the out-ofplane acoustic mode (ZA), blue indicates the in-plane transverse acoustic mode (TA), and green denotes the in-plane longitudinal acoustic mode (LA). The optical branches are represented in black. The analysis performed along the K-Γ-M high-symmetry path reveals that the maximum vibration frequencies for the LA mode are approximately 3.06 THz (102.07 cm⁻¹), 3.04 THz (101.40 cm⁻¹), and 3.07 THz (102.40 cm⁻¹) for the S-S, S-Se, and Se-Se configurations, respectively, which closely match previously reported phonon frequencies of 103.08 cm⁻¹ in S-S, ~101.39 cm⁻¹ in S-Se and ~105.68 cm⁻¹ in Se-Se.³⁴

3.1.2. Thermal stability. The thermal stability of different chalcogen configurations in SnSSe bilayers is assessed using Nose-Hoover thermostat-based *ab initio* molecular dynamics (AIMD) simulations at room temperature (300 K), as shown in Fig. 3. The results indicate that the potential energy does not

change significantly over time for all configurations. Moreover, after 10 ps AIMD simulations, no structural degradation, bond breaking, or significant geometric distortion were observed. Consequently, all three interfacial chalcogen pair configurations were thermally stable.

The stability analysis confirmed that all bilayers, irrespective of interlayer chalcogen pairing, were structurally, dynamically and thermally stable in their relaxed configurations. Consequently, the structural properties of these bilayers at equilibrium are analysed in the subsequent section.

3.2. Structural properties

In this section, the relevant structural properties such as bond length, bond angle, interlayer distance (ILD), and lattice vectors of the optimized SnSSe bilayers are considered in different interlayer chalcogen pairing configurations, as illustrated in Fig. 4a–c. Next, these properties are compared with those of the monolayers of SnSSe, SnS₂ and SnSe₂ as indicated in the ESI (Fig. S1†) to assess the influence of the interlayer chalcogen pair environment on the overall structural characteristics.

The lattice constant of the SnSSe monolayer is 3.82 Å, which lies between the lattice constants of SnS_2 (3.71 Å) and $SnSe_2$ (3.91 Å) monolayers (Fig. S1†), and is consistent with previous theoretical reports.^{23,29} Similarly, in the SnSSe monolayer, the $\angle S$ -Sn-Se bond angles assume an intermediate value

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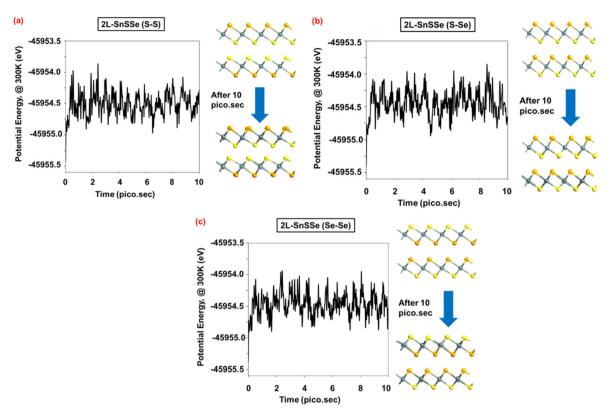


Fig. 3 Structural evolution of a 4 × 4 × 1 supercell of 2L-SnSSe for (a) S-S, (b) S-Se, and (c) Se-Se configurations.

(89.82°) compared to \angle S-Sn-S bond angle (89.51°) and \angle Se-Sn-Se bond angle (90.98°) in SnS₂ and SnSe₂ monolayers, respectively (Fig. S1†). Interestingly, in the SnSSe environment, the Sn-S (Sn-Se) bond length increases (decreases) from 2.61 Å to 2.65 Å (2.78 Å to 2.75 Å) compared to monolayer SnS₂ (SnSe₂) (Fig. S1†). This suggests that the Janus (SnSSe) environment notably influences the in-plane tin (Sn)-chalcogen (S/Se) atomic orbital interactions compared to natural (SnS₂ and SnSe₂) environments.

As indicated in Fig. 4a-c, the presence of monolayer SnSSe in a bilayer configuration introduces three distinct chalcogen pairings i.e., S-S, S-Se, and Se-Se. In the SnSSe bilayer, irrespective of chalcogen pairing, the Sn-S and Sn-Se bond lengths slightly increased from 2.65 Å to 2.66 Å and 2.75 Å to 2.76 Å, respectively, as compared to the SnSSe monolayer (Fig. S1c \dagger). Moreover, the \angle S-Sn-Se bond angles of SnSSe decrease from 89.82° to 88.80° in S-S, 89.82° to 89.17° in Se-Se, and 89.82° to 89.18° (top monolayer), 89.82° to 89.03° (bottom monolayer) in S-Se chalcogen pairings of the bilayer SnSSe compared to the SnSSe monolayer (Fig. S1c†). This indicates that bilayer formation leads to simultaneous expansion in the in-plane direction and compression in the vertical direction in individual monolayers of SnSSe. Consequently, in each bilayer configuration, the tin (Sn)-chalcogen (S/Se) atomic orbital interactions are relatively weakened, which is expected to influence the energy band (E-k) structure of the bilayers.

Apart from the modulation of in-plane atomic orbital interactions, out-of-plane atomic orbital interactions between monolayers are another crucial factor in the bilayer environment. This can be observed from the fact that in each configuration, the interfacial chalcogen atoms exhibit a notably larger valence charge redistribution, *i.e.* $Q_{\text{transfer_atom}}$ compared to the surface chalcogen atoms. Therefore, the atomic orbital interactions between the interlayer chalcogen atoms are expected to have a significant influence on the energy band (E-k) structure of the bilayers. In this effect, the average electron density projections in the out-of-plane direction of bilayer SnSSe at different interlayer chalcogen pair configurations are compared with isolated monolayer SnSSe, as illustrated in Fig. 4d–g.

The average electron density projections of monolayer SnSSe exhibit two peaks, where the larger and smaller peaks are consistent with the presence of Se (4s² 4p⁴) and S (3s² 3p⁴) atoms, respectively. In bilayer SnSSe, irrespective of interlayer chalcogen pair configurations, a finite average electron density is observed at the interface of the top and bottom layers, suggesting a significant atomic orbital interaction between the interlayer chalcogen atoms. However, the difference in interlayer atomic orbital interaction in different bilayers can be appreciated from the fact that ILD significantly varies from one chalcogen pair configuration to another. The trend observed in the ILD is consistent with previous reports, wherein the largest and smallest ILDs are observed in the Se-

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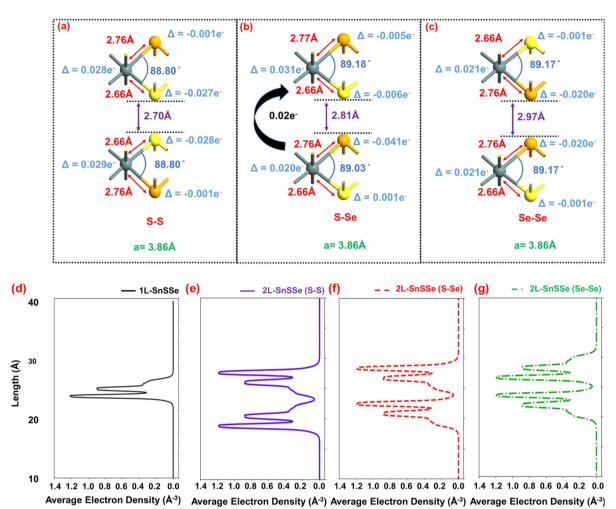


Fig. 4 Schematic representation of the unit-cell of 2L-SnSSe for (a) S-S, (b) S-Se and (c) Se-Se configurations and their average electron densities of (d) 1L-SnSSe, (e) 2L-SnSSe, (S-S) (f) 2L-SnSSe (S-Se), and (g) 2L-SnSSe (Se-Se) configurations.

Se and S-S configurations, respectively.²⁹ Specifically, the effective out-of-plane van der Waals (vdW) radius overlapping in S-S, S-Se, and Se-Se configurations are 1.08 Å (S vdW radius 1.89 Å), 0.90 Å (S vdW radius 1.89 Å, Se vdW radius 1.82 Å), 0.67 Å (Se vdW radius 1.82 Å), suggesting the interlayer atomic orbital interactions are distinctly different in each of the bilayers. On the other hand, in the case of S-S and Se-Se interlayer chalcogen pair configurations, a symmetric out-of-plane S-S and Se-Se p-orbital hybridization is expected, wherein S-Se interlayer chalcogen pairing should result in asymmetric out-of-plane S (3s² 3p⁴) and Se (4s² 4p⁴) p-orbital hybridizations. Such asymmetric out-of-plane atomic orbital hybridization is expected to have distinct influences on the electronic (Bloch states) states of the S-Se configuration, compared to S-S and Se-Se configurations.

Next, the S-S pairing of bilayer SnSSe, compared to the monolayer, presents a symmetric electron density distribution around a horizontal axis between the layers, with the electron

density distribution of the second layer mirroring the first. Similarly, the Se-Se bilayer exhibits a symmetric distribution. In contrast, the S-Se pairing breaks the interlayer mirror symmetry in the average electron density distribution due to dissimilar chalcogen pairing. The asymmetric electronic distribution in S-Se interlayer chalcogen pair configuration suggests distinctly different out-of-plane atomic orbital interactions compared to S-S and Se-Se configurations. The asymmetric electronic distribution at the interlayer interface in the S-Se configuration results in a finite interlayer charge transfer, which is quantified from the Mulliken charge analysis. Consequently, unlike S-S and Se-Se configurations, for the S-Se configuration, a bottom-to-top layer charge transfer $(Q_{\text{transfer layer}} = 0.02 \text{ e}^{-} \text{ per unit-cell}, i.e. 2.2 \mu \text{C cm}^{-2}) \text{ is}$ observed, which results in an intrinsic interlayer dipole moment (considering ILD = 2.81 Å) of \sim 0.27 D unit-cell, i.e. $1.81 \times 10^{14} \text{ D cm}^{-2}$. The presence of such interlayer dipole moments in the S-Se configuration of bilayer SnSSe is consistent with previous theoretical reports. 29,30

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Thus, the factors discussed above are expected to characteristically influence the energy band (E-k) structure of S-Se bilayers compared to their S-S and Se-Se bilayer counterparts.

3.3. Electrostatic and electronic properties

The average electron density projection analysis presented in the previous section suggests the possibility of chalcogen pair configuration-dependent interlayer charge transfer in bilayer SnSSe. Consequently, in this section, the electrostatics of the bilayers are considered in terms of the average electrostatic difference potential and electron difference densities, as illustrated in Fig. 5. Next, to assess the influence of the aforementioned factors on the electronic properties of SnSSe bilayers, in this section, the energy band structures, total density of states (TDOS) profiles, individual monolayer projected density of states (PDOS), and spatial distributions of electronic states (Bloch states) at the conduction and valence band edges are analysed, and the results are shown in Fig. 6 and 7.

3.3.1 Electrostatics analysis of SnSSe bilayers. Fig. 5 presents the out-of-plane direction projections of the average electrostatic difference potential with subsequent spatial electron difference density profiles for different chalcogen pair configurations of SnSSe bilayers. Fig. 5 indicates that the electron difference density distribution is more concentrated on the Sn-S bond and relatively less concentrated on Sn-Se in each monolayer in the bilayer environment. This can be attributed to the relatively higher electronegativity of S (2.58 in Pauling scale) compared to Se (2.55 in Pauling scale), leading to a larger valence charge re-distribution in the Sn-S bond compared to the Sn-Se bond. A closer observation reveals that the larger electron difference density across the

Sn-S bond results in higher electrostatic difference potential in the interlayer interface of the S-S chalcogen pair configuration compared to that of the Se-Se chalcogen pair configuration, as shown in Fig. 5a and c. Interestingly, the symmetric electron difference density distributions at the interlayer interface for both S-S and Se-Se configurations ensure a mirror symmetry around the interface axis in the electrostatic difference potential profile. In contrast, the clear asymmetry in the electron difference density distribution around the interlayer interface in S-Se chalcogen pair configuration breaks the mirror symmetry around the interface axis in the electrostatic difference potential profile, as illustrated in Fig. 5c.

Moreover, the average electrostatic difference potential peaks around the Sn atoms of each monolayer remain comparable in magnitude for S-S and Se-Se configurations. However, these electrostatic difference potential peaks have notably different magnitudes ($\Delta \varphi = 0.14 \text{ V}$) in both monolayers of the S-Se configuration. In this context, an effective interlayer electric field (E_{eff}) is defined in this study as follows:

$$|E_{\rm eff}| = \frac{\Delta \varphi}{d} \tag{7}$$

In eqn (7), d is the ILD between the two SnSSe layers. Therefore, it can be inferred that the interlayer charge transfer induces an electrostatic potential difference $(\Delta \varphi)$ between the SnSSe layers, and consequently, a finite E_{eff} is expected in the S-Se configuration. Therefore, an $E_{\rm eff}$ of ~ 0.5 V nm⁻¹ was calculated for the S-Se configuration of bilayer SnSSe. The presence of such an interlayer electric field in the S-Se configuration of bilayer SnSSe is consistent with previous theoretical reports.30

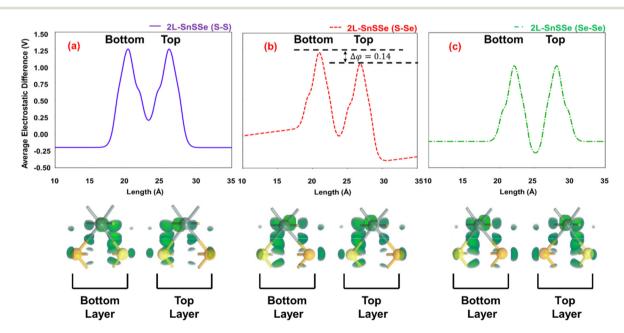
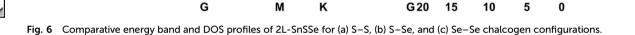


Fig. 5 Representation of average electrostatic difference potential and electron difference density of 2L-SnSSe for (a) S-S, (b) S-Se, and (c) Se-Se configurations.

(a) 2L-SnSSe (S-S) Total Density of States(eV-1) 3 Energy, E- E_F (eV) 1.49 eV -3 G М Κ 15 (b) 2L-SnSSe (S-Se) Total Density of States(eV-1) 3 Energy, E- E_F (eV) 1.27 eV 10 G М G20 15 (c)

1.47 eV

2L-SnSSe (Se-Se) Total Density of States(eV-1)



3.3.2 Band structure and density of states analysis. Next, in Fig. 6, the energy band structures of different SnSSe bilayer configurations show an indirect bandgap in each case, where the conduction band minima (CBM) and valence band maxima (VBM) appear at the 'M' and 'G' high symmetry points of the BZ, respectively. However, a significantly reduced energy bandgap (E_g) can be observed in the S–Se configuration (E_g = 1.27 eV) compared with the S–S (E_g = 1.49 eV) and Se–Se (E_g = 1.47 eV) configurations. Specifically, in the S–Se configuration, the VBM (CBM) is at -0.64 eV (0.63 eV) compared to the VBM position at -0.77 eV (0.72 eV) and -0.71 eV (0.71 eV) in S–S and Se–Se configurations, respectively. Therefore, the simultaneous shift in the CBM and VBM towards the Fermi level (E_F) in the S–Se configuration leads to a reduction in the bandgap. This reduction in bandgap can be attributed to the

Energy, E- E_F (eV)

built-in interlayer electric field ($E_{\rm eff}$) directed from the bottom to the top SnSSe monolayer, which raises the electrostatic potential of the bottom layer with respect to the top layer. Consequently, the band structure of the top layer will move upward (in electronic energy scale as electrostatic potential decreases), whereas the band structure of the bottom layer will move downward (in electronic energy scale as electrostatic potential increases). This shifts the VBM of the top layer and the CBM of the bottom layer towards $E_{\rm F}$ and effectively reduces the bandgap.

Consequently, in this study, the energy band structures were simulated using HSE-06 (with SOC), where the calculated bandgap values of 1.49 eV (S–S), 1.47 eV (Se–Se), and 1.27 (S–Se) are consistent with previously reported HSE-06-SOC simulated bandgap values of 1.37 eV (S–S), 1.40 eV (Se–Se),

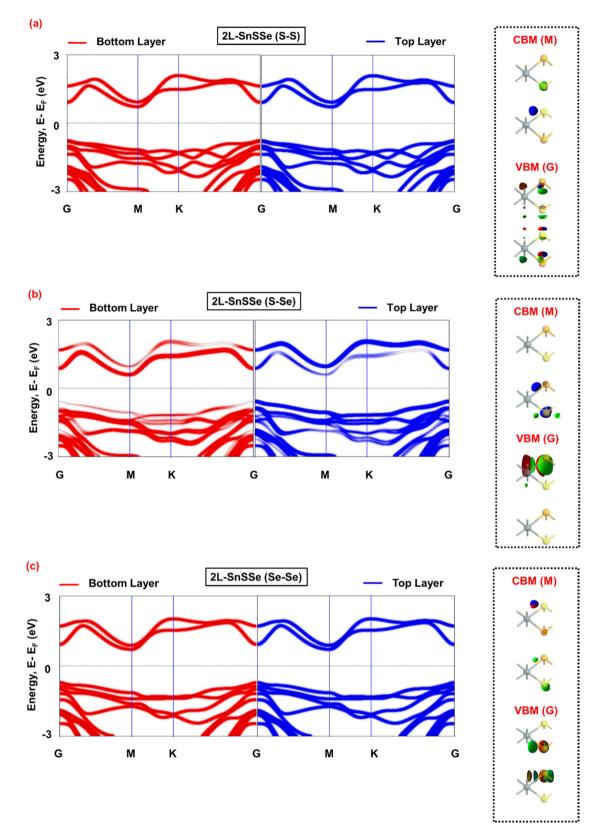


Fig. 7 Comparative band structure projections and Bloch states of 2L-SnSSe for (a) S-S, (b) S-Se, (c) Se-Se chalcogen configurations.

framework proposed in this study.

and 1.26 (S–Se).³⁴ Furthermore, similar to previous theoretical reports, each SnSSe bilayer exhibits an indirect bandgap, with the CBM located at the 'M' point and the 'VBM' at the 'G' point.^{29,34} Thus, the close agreement between the energy band structure and the bandgap values previously reported in previous studies confirms the reliability of the computational

In general, the bands below the VBM of each bilayer show a relatively less dispersive nature, leading to larger DOS at the VBM as well as localized DOS peaks below the VBM, as shown in the TDOS profiles in Fig. 6. In contrast, a delocalized and relatively smaller DOS profile was observed above the CBM in each bilayer. Interestingly, in the S-Se configuration, the bands below the VBM showed better dispersion, resulting in reduced localized peaks in the DOS below the VBM in this case. For a more detailed analysis of the electronic properties of different bilayers, the atomic orbital projected DOS profiles were considered and are presented as ESI (Fig. S2†). PDOS analysis demonstrates that in each bilayer, the conduction band (CB) is populated by the s-orbital of the Sn atom and predominantly the in-plane p_r - and p_v -orbitals of both S and Se atoms. In contrast, the valence band (VB) of these bilayers is predominantly populated by the out-of-plane pz-orbitals of both S and Se atoms. Moreover, an effectively uniform Sn s-orbital and S and Se p_x/p_y -orbitals hybridization is observed in the CB of each bilayer. This suggests that the in-plane tin-chalcogen orbital interaction is expected to exert significant influence on the CB, whereas the out-of-plane orbital interactions of interlayer chalcogen atoms are expected to notably influence the VB of these bilayers.

3.3.3 Band alignment and bloch state analysis. On the other hand, the built-in $E_{\rm eff}$ induced relative movements in the band structures of the top and bottom layers are also expected to introduce a type-2 band alignment in the S–Se chalcogen pair configuration of the homogeneous bilayer of SnSSe. To analyse this aspect, the individual monolayer projected band structures and the spatial distributions of the CBM and VBM Bloch states are considered in Fig. 7.

A systematic inspection of Fig. 7 establishes that for S-S and Se-Se configurations, the CBM (at 'M' point) and the VBM (at 'G' point) are equally populated by the top and bottom layers. In this effect, the CBM and VBM Bloch states are spatially distributed in both SnSSe layers, consistent with the band structure analysis. Typically, in the S-S configuration, the VBM Bloch state is delocalized across the entire lattice, which is consistent with the strongest vdW radius overlapping (1.08 Å) of the interlayer S atoms. Whereas, in Se-Se configuration, the VBM Bloch states are more localized around the interfacial chalcogen atoms, which can be correlated with the weakest vdW radius overlapping (0.67 Å) in this case. Interestingly, the CBM Bloch state is localized around the interface chalcogen atoms in S-S configurations, and delocalized across the entire lattice in Se-Se configurations.

The individual monolayer projected band structure of S-Se configuration shows a stark contrast compared to that of S-S and Se-Se configurations, where a clear type-2 band alignment

is observed. A similar type-2 band alignment with an intrinsic electric field was previously reported in bilayer MoSSe. 33 In the S-Se configuration of a bilayer, the CBM is occupied by the bottom SnSSe layer, and the VBM is occupied by the top SnSSe layer. In agreement with the projected band structure, in the S-Se configuration, the CBM and VBM Bloch state distributions are confined in the bottom and top layers, respectively. This scenario is perfectly consistent with the interlayer charge transfer and subsequent $E_{\rm eff}$ analysis. The VBM Bloch state confinement at the top SnSSe layer and the CBM Bloch state confinement at the bottom SnSSe layer suggest that in their ground-state configurations, electrons and holes are spatially separated in different monolayers of bilayer SnSSe. Moreover, the projected band structure indicates that at CB (VB), the contribution bottom (top) SnSSe layer appears at a notably higher \sim 0.36 eV (lower \sim 0.29 eV) energy (offset) than the bottom (top) SnSSe layer. This suggests the stability of interlayer separated electrons and holes even at room temperature (offsets $\gg KT \sim$ 0.026 eV at T = 300 K) in their respective monolayers.

The bilayer SnSSe exhibits an indirect band gap in each stacking configuration, indicating a relatively larger radiative excitonic lifetime. 36,39 On the other hand, compared to S-S and Se-Se stacking configurations, the S-Se configuration shows a clear type-2 band alignment with a relatively larger band offset, suggesting thermally stable interlayer excitons. It is well established that the overlap between electron and hole wavefunctions significantly influences the oscillation strength, which is inversely proportional to the radiative excitonic lifetime. 76,77 Therefore, in S-Se configuration, the localization of the CBM (electron) and VBM (hole) Bloch states (electronic wavefunction) in the alternative SnSSe monolayer reduced the electron and hole wave function overlap and should lead to a larger radiative excitonic lifetime due to the decreased oscillation strength owing to the reduced wave function overlap between spatially separated electrons and holes. A similar trend was previously observed in vdW TMD bilayers with type-2 band alignment. 36,39,78

Next, in this study, the effects of biaxial strain and interlayer distance variation are systematically studied on the electronic and excitonic properties of a homogeneous bilayer of SnSSe in the S-Se stacking configuration. The biaxial strain influences both in-plane and interlayer atomic orbital interactions, wherein interlayer distance variation primarily influences the interlayer atomic orbital interactions. 38,39,79 These modulations in the in-plane and interlayer atomic orbital interactions are manifested in the spread of the conduction band in energy, which can, in turn, be qualitatively correlated with the excitonic radiative lifetime following a time-energy uncertainty argument. The excitonic lifetime depends on multiple factors, and a detailed analysis of the lifetime requires extensive analytical modelling, preferably supported by experimental optical characterizations. However, these aspects are out of the scope of this study, where a simplified qualitative analysis based on the time-energy uncertainty relation and spatial separation of electron and hole wave functions can offer a reasonable assessment of excitonic radiative lifetime variations with biaxial strain and interlayer distance variation.

3.4 Influence of interlayer distance on the electronic properties of bilayer SnSSe in S-Se interlayer chalcogen pair configuration

The electronic property analysis indicates that the interlayer atomic orbital interactions of chalcogen atoms have a crucial influence on the band edge electronic states and thereby on the overall electronic properties of bilayers, which is most significant in S-Se interlayer chalcogen pair configuration owing to the type-2 band alignment in this homogeneous bilayer. However, the strength of such interlayer atomic orbital interactions can be efficiently tuned by varying the ILD between the SnSSe monolayers. Thus, in this section, the influence of ILD variations on the overall electronic properties of S-Se interlayer chalcogen pair configurations is studied, where the ILD compression and expansion are restricted up to 1.5 with respect to the equilibrium ILD of the S-Se configuration. The effects of ILD variation on the CBM energy, VBM energy, energy bandgap, energy band structure, and individual monolayer projected energy band structure are presented in plots in Fig. 8. To further analyse these aspects, the spatial distribution of band edge Bloch states and atomic orbital projected density

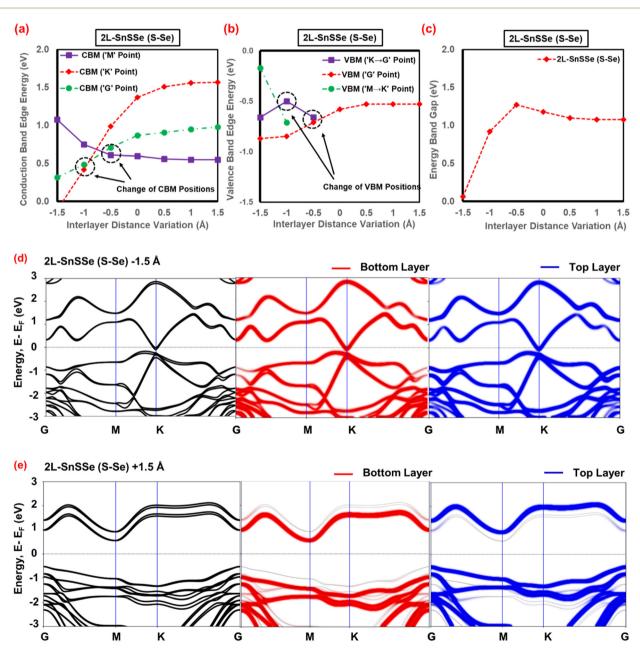


Fig. 8 Comparative analysis of interlayer distance variation for (a) conduction band edge energies for S-Se, (b) valence band edge energies for S-Se, (c) electronic bandgap of bilayer SnSSe, (d) band structure and monolayer projections for 1.5 Å interlayer distance reduction, and (e) band structure ture and monolayer projections for +1.5 Å interlayer distance expansion.

of states were considered for increased and reduced interlayer

separations in the ESI (Fig. S3†).

3.4.1 Effect of interlayer distance on band edge energies and bandgaps. Fig. 8a and b indicate that increasing ILD initially slightly reduces (increases) the energy of the CBM (VBM) at 'M' ('G') high symmetry point, which thereafter saturates with increasing ILD. This leads to a small energy bandgap reduction in the S-Se interlayer chalcogen pair configuration at a higher interlayer separation, as shown in Fig. 8c. Interestingly, at a higher interlayer separation, the S-Se demonstrates more prominent type-2 band alignment compared to equilibrium interlayer separation, with a CB (VB) edge separation of ~ 0.37 eV (~ 0.43 eV) between the top and bottom (bottom and top) SnSSe layer, as shown in Fig. 8e and 7b. The Bloch state distribution at a higher ILD exhibits that similar to the equilibrium ILD, the CBM (VBM) Bloch state at 'M' ('G') point are restricted in the bottom (top) SnSSe layer (Fig. S3b†), which is consistent with the observed type-2 band alignment. In contrast, the reducing ILD significantly affects the overall energy band structure of S-Se configuration by changing the CBM (VBM) from 'M' ('G') 'G' (between 'K' to 'G') point and thereafter 'K' (between 'M' to 'K') point, as shown in Fig. 8a and b. The reduction of ILD also sharply reduces (increases) the energy of CBM (VBM), leading to a semi-metallic energy band structure with zero bandgap, as illustrated in Fig. 8c and d. Furthermore, Fig. 8d suggests that at a smaller interlayer separation, the type-2 band alignment is annihilated in the S-Se configuration of the SnSSe bilayer. In agreement with this observation, at a lower ILD, both the CBM and VBM Bloch states were delocalized across the SnSSe bilayer (Fig. S3a†).

3.4.2 Effect of interlayer distance on orbital hybridization. Interestingly, the PDOS analysis revealed that the p_z-orbital contribution of S and Se (s-orbital contribution of Sn) at the VB considerably diminished (slightly increases) at smaller ILDs compared to larger ILDs (Fig. S3c and S3d†). On the other hand, the s-orbital contribution of Sn at the CB reduces and becomes delocalized at smaller ILDs compared to larger ILDs (Fig. S3c and S3d†). Therefore, the PDOS analysis suggests that the increasing ILD effectively retains the qualitative trend of atomic orbital hybridization in the CB and VB with respect to equilibrium interlayer separation, which may be the key factor for preserving the type-2 band alignment at higher ILD. In contrast, reducing ILD significantly alters the atomic orbital hybridization trend observed at equilibrium interlayer separation. Specifically, the s-orbital of Sn tends to interact with p-orbitals of S and Se from the same and different SnSSe layers owing to the proximity of both layers, which may lead to the annihilation of the type-2 band alignment and delocalization of the CBM and VBM Bloch states (Fig. S3a and S3b†). The strong delocalization of both band-edge Bloch states can reduce the CBM and VBM energies and impart a semi-metallic nature at a significantly smaller ILD. At the same time, from the PDOS and conduction band spread analysis (Fig. S3c, S3d and S7a†), it can be observed that the reducing ILD delocalizes the CB in energy owing to the stronger interlayer atomic orbital interactions, which leads to an increase in energy

uncertainty in both the CB. Thus, from the energy-time uncertainty relationship, it can be inferred that reducing the ILD decreases the average lifetime of electrons in the CB. This suggests that reducing ILD notably degrades the exciton radiative lifetime in the S-Se configuration of the SnSSe bilayer. In contrast, the increasing ILD marginally influences the localization of CB in energy, thereby affecting their energy-time uncertainty. On the other hand, the reducing (increasing) ILD reduces (increases) the spatial separation between the electron and hole wavefunctions (Fig. S3c and S3d†), which increases (reduces) the oscillation strength and thereby decreases (increases) the radiative lifetime of excitons. Thus, from both the energy-time uncertainty argument and electron-hole wave function overlap analysis, it can be predicted that reducing the ILD will decrease the exciton radiative lifetime, which is also consistent with the annihilation of type-2 band alignment at smaller ILDs. At the same time, the increasing ILD will decrease electron-hole wavefunction overlap, which should improve the exciton radiative lifetime. Interestingly, a similar trend has been experimentally observed in different vdW TMDs, where the radiative lifetime of interlayer excitons is reduced by applying pressure (reduction of ILD) in WS₂/MoSe₂ heterostructure, 39 MoS₂/WSe₂ heterostructure, 38 and increased by inserting hexagonal Boron Nitride (h-BN) layers (increase of ILD) within WS₂/WSe₂ heterostructure.⁸⁰

3.4.3 Effect of interlayer distance on band edge offsets and exciton stability. Next, for the type-2 band alignment, the CB and VB edge separation (offset) between the top and bottom SnSSe layers was considered as a function of ILD, and is illustrated in Fig. 9. The type-2 band alignment is annihilated with even a smaller reduction in ILD; therefore, the band edge offset is not considered for reducing ILD. The results indicate that the CB offset is effectively comparable, whereas the VB offset slightly decreases with increasing ILD. This suggests that along with the increasing prominence of type-2 band alignment and improving the interlayer exciton lifetime with increasing ILD, stable interlayer exciton can be realized at room temperature (offsets $\gg KT \sim 0.026$ eV at T = 300 K) at higher ILD through suitable optical excitation in the S-Se configuration of the SnSSe bilayer.

This analysis revealed that ILD significantly modulates the electronic and excitonic properties of the S-Se configuration of the SnSSe homogeneous bilayer, suggesting further design flexibility in terms of band alignment tailoring by tuning the ILD.

3.5 Influence of biaxial strain on the electronic properties of bilayer SnSSe in S-Se interlayer chalcogen pair configuration

This section investigates the influence of biaxial tensile (BT) and biaxial compressive (BC) strains on the electronic properties of the S-Se configuration of bilayer SnSSe. Specifically, the energy band structures, spatial distribution of band edge Bloch states, individual monolayer projection on the energy band structure, and total density of states were considered at 5% BC and BT strain, and are illustrated in Fig. 10. In this context, the E_{eff} , energy bandgap, primary and secondary band

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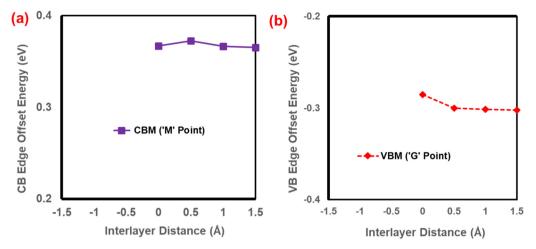


Fig. 9 Plot of (a) CB edge offset energy and (b) VB edge offset energy variations with interlayer distance variation for S-Se configuration of the SnSSe bilayer.

edge energies are considered as functions of biaxial strain variation, as illustrated in Fig. 11.

Biaxial compressive strain suggests that a material is subjected to tensile (outward) stress along two in-plane lattice vector directions, which strains the material, and the direction of strain is opposite to the stress. Consequently, the biaxial tensile stress will lead to biaxial compressive strain, and following a similar argument, biaxial compressive stress will lead to biaxial tensile strain. Sepecifically, under such compressive strain, the material undergoes elongation in the in-plane lattice directions that increases the bond lengths, as shown in Fig. S4.† Conversely, biaxial tensile strain contracts the material in the in-plane lattice directions, causing bond length reduction, as shown in Fig. S4.† Following this notion in this paper, the induced strain and applied stress are simultaneously mentioned in the "strain-type (corresponding stress type)" format.

3.5.1 Effect of biaxial strain on orbital hybridization. First, to understand the effects of BC and BT strain on the electronic properties of the S-Se configuration, the in-plane and out-ofplane structural properties, such as bond lengths, bond angles, and interlayer distances, were investigated as a function of biaxial strain. These results are presented in the ESI (Fig. S4†). Moreover, to further complement this analysis, the energy band structures and atomic orbital projected DOS at different biaxial strains are also considered in the ESI (Fig. S5 and S6†). The application of compressive (tensile) stress i.e. BT (BC) strain, simultaneously compresses (expands) the individual SnSSe layers in the in-plane direction and expands (compresses) them in the out-of-plane direction (Fig. S4†). Consequently, the BT (BC) strain reduces (increases) the Sn-S/ Sn–Se bond lengths, increases (reduces) the ∠S–Sn–Se bond angles, and increases (reduces) the ILD. This suggests that the BT (BC) strain strengthens (weakens) the in-plane Sn s-orbital and S and Se p_x/p_y -orbitals hybridization, which can be appreciated from the increasing (decreasing) delocalization

over energy of these orbitals in CB (Fig. S5 and S6†). At the same time, the BT (BC) strain weakens (strengthens) the out-of-plane p_z -orbital hybridization of S and Se atoms at the interface, which can be verified from the decreasing (increasing) delocalization over the energy of these orbitals in VB. At the same time, the BC strain marginally increases the Sn s-orbital contribution in the VB, suggesting s-orbital of Sn interaction with p-orbitals of S and Se from the same and different SnSSe layers. Therefore, BC and BT strains induce distinct influences on the in-plane and out-of-plane atomic orbital interactions, which are expected to exert a notable influence on the electronic states in the CB and VB in the S–Se configuration of the SnSSe bilayer.

3.5.2 Effects of biaxial strains on band structure and band alignment. Fig. 10a indicates that the application of 5% BC and BT strain reduced the bandgap in the S-Se configuration of the SnSSe bilayer. For a 5% BT strain, compared with the relaxed configuration, the CBM and VBM remain at the 'M' and 'G' points, respectively. In contrast, compared with the relaxed configuration, the CBM shifts from the 'M' to the 'G' point, and the VBM shifts from the 'G' to the 'K-G' point under 5% BC strain. Consequently, for a 5% BT (BC) strain, compared with the relaxed configurations, an overall bandgap reduction of ~42% (~34%) was observed. The spatial distribution of the band edge Bloch state in Fig. 10b reveals that for 5% BT strain, the CBM (VBM) Bloch state remains confined at the bottom (top) in the SnSSe bilayer, which is consistent with the type-2 band alignment observed from monolayer projected band structures in Fig. 10c. In contrast, at 5% BC strain, the type-2 band alignment is annihilated, and both the CBM and VBM Bloch states become delocalized across the top and bottom SnSSe layers, as shown in Fig. 10b and c. Such annihilation of the type-2 band alignment at a larger BC strain can be correlated with the notable reduction in ILD and subsequent Sn s-orbital interactions with the p-orbitals of S and Se from the same and different SnSSe layers. Fig. 10d demonstrates

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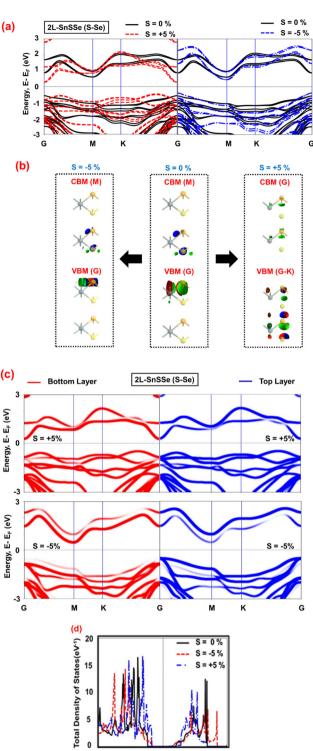


Fig. 10 Plots of (a) energy band structure, (b) Bloch states, (c) monolayer projected band structure, and (d) TDOS of bilayer SnSSe in S-Se configuration for 5% BC and 5% BT strains.

Energy, E- E_F (eV)

that biaxial strain significantly influences the TDOS in the S-Se configuration of the SnSSe bilayer. Specifically, the CBM and VBM shifted towards $E_{\rm F}$ under 5% BC and 5% BT strain.

Moreover, the 5% BT (BC) strain reduces (increases) the magnitude of DOS at VBM. In contrast, at the CB edge, the DOS remained small and comparable to that of the relaxed configuration for the 5% BC and 5% BT strains.

At the same time, from the PDOS and conduction band spread analysis (Fig. S5, S6 and S7b†), it can be observed that the 5% BT strain delocalizes the CB electronic states in energy owing to the stronger in-plane atomic orbital interactions, which leads to an increase in energy uncertainty in CB. However, the type-2 band alignment was preserved under a 5% BT strain. The application of strain simultaneously modifies both in-plane and interlayer atomic orbital interactions, where increasing BT (BC) strain reduces (enhances) interlayer atomic orbital interaction and increases (decreases) in-plane atomic orbital interaction. Consequently, increasing interlayer atomic orbital interaction with BC strain annihilates the type-2 band alignment. Moreover, increasing BC strain marginally influences the localization of CB in energy, thereby affecting their energy-time uncertainty. Interestingly, the increasing BT (BC) strain increases (decreases) the ILD and thereby the separation of electron and hole wave functions, which is expected to reduce (enhance) the oscillation strength and thereby improve (degrade) the excitation radiative lifetime. Therefore, combining both spatial separation electron-hole wave function and energy-time uncertainty argument, it can be surmised that the increase in BC and BT strain involves competing influences on the radiative lifetime of excitons and is expected to degrade the overall radiative lifetime of excitons compared to the relaxed configuration. However, owing to the annihilation of type-2 band alignment, this effect is expected to be more prominent in larger BC strains. A similar trend has been experimentally observed in a MoS₂/WSe₂ heterostructure,³⁸ where the radiative lifetime of interlayer excitons is reduced after applying both uniaxial tensile and compressive strain.

3.5.3 Effects of biaxial strains on band edge offsets. Next, the effective interlayer electric field profile (as defined in eqn (7)) in Fig. 11a indicates that increasing BC strain monotonically reduces E_{eff} , whereas E_{eff} increases with increasing BT strain. Consequently, as shown in Fig. 11b, with increasing BT strain, the E_g starts to decrease, suggesting that E_{eff} dominates the $E_{\rm g}$ variation with BT strain, which is also consistent with the observed type-2 band alignment at 5% BT strain (Fig. 10c). In addition to increasing the interlayer electric field, the modulations in orbital interactions also play a notable role in the shift of the CBM and VBM towards the Fermi level and subsequent bandgap reduction with the BT strain. Specifically, the applied BT strain leads to contraction (elongation) of the lattice in the in-plane (out-of-plane) direction, which simultaneously reduces Sn-S/Sn-Se bond lengths and increases the S-Sn-Se bond angles in each monolayer (Fig. S4†). Consequently, under the applied BT strain, reducing the interaction between the s-orbital of the Sn atom with in-plane p_x/p_y orbitals of the S and Se atoms (Fig. S6†) may also contribute to the shift of the CBM towards the Fermi level. On the other hand, the increasing S-Sn-Se bond angles reduce the intralayer interaction between the p_z/p_v orbitals of the S atom and

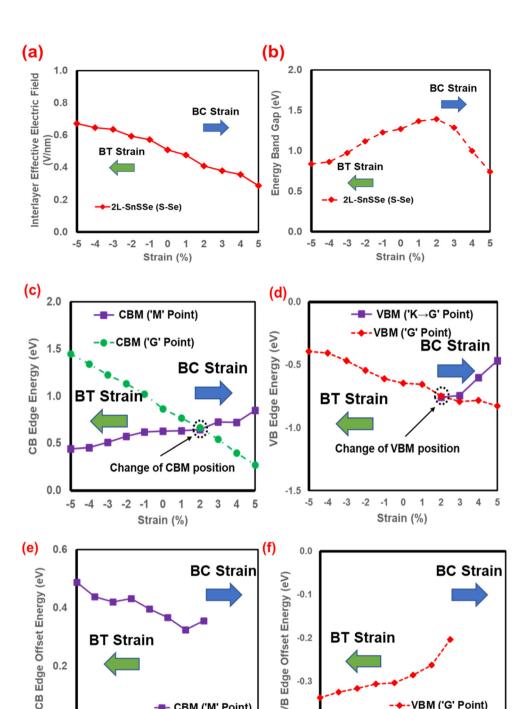


Fig. 11 Plots of (a) interlayer effective electric field, (b) electronic band structure, (c) conduction band edge energies, (d) valence band edge energies. gies, (e) CB edge offset energy, and (f) VB edge offset energy with varying biaxial strain in S-Se configuration of bilayer SnSSe.

CBM ('M' Point)

NB

-0.4

-5 -4 -3 -2

Strain (%)

Se atom (Fig. S6†), which leads to stronger localization of the VBM Bloch states around the Se atom (Fig. 10b) and subsequently also possibly contributes to the shift of the VBM towards the Fermi level. Interestingly, the $E_{\rm g}$ initially increases following monotonically reducing $E_{\rm eff}$ with increasing BC strain, as illustrated in Fig. 11b. However, with increasing BC

-2

0

Strain (%)

-4 -3

-5

0.0

strain, the ILD also reduces and eventually starts modulating the nature of interlayer atomic orbital hybridization (Fig. S5†), leading to delocalization of the CBM and VBM Bloch states over the bilayer, as observed for 5% BC strain (Fig. 10b). The delocalization tends to reduce the energy of the CBM and VBM, and this effect starts dominating the overall E_g variation

VBM ('G' Point)

beyond a certain BC strain. Subsequently, a steep reduction in E_{σ} is observed at higher BC strains.

Fig. 11c shows that the CB edge energy at the 'M' point ('G' point) decreases (increases) with increasing BT and increases (reduces) with increasing BC. This further leads to a shift in the CBM from the 'M' point to the 'G' point at a higher BC strain. Similarly, Fig. 11d indicates that the VB edge energy at the 'G' point increases with increasing BT and reduces with increasing BC. The VBM shifts from the 'G' point to an intermediate point between the 'K' and 'G' point at a higher BC strain, and the VB edge energy between the 'K' to 'G' point keeps increasing with BC strain.

Next, for the type-2 band alignment, the CB and VB edge separation (offset) between the top and bottom SnSSe layers is considered as a function of biaxial strain, as illustrated in Fig. 11e and f. The type-2 band alignment is annihilated at a larger BC strain, and therefore, the band edge offset is not considered from that point onwards. The results indicate that both the CB and VB offsets are increasing (decreasing) with increasing BT (BC) strain. This suggests that the BT strain is a highly promising material engineering technique for increasing the band edge offset while retaining type-2 band alignment in the S–Se configuration. This indicates that stable interlayer excitons can be realized through suitable optical excitation at room temperature (offsets $\gg KT \sim 0.026$ eV at T = 300 K) in a tensile-strained S–Se configuration of the SnSSe bilayer.

3.6. Comparative analysis

The key findings of this study are compared with previously reported theoretical findings on SnSSe and Janus TMD bilayers. Previous theoretical reports on SnSSe bilayers also reported a notably small energy bandgap in the S-Se configuration compared to S-S and Se-Se configurations. 29,30 Moreover, a non-zero interlayer dipole moment and interlayer electric field were previously reported in the S-Se configuration of the SnSSe bilayer, which is consistent with the findings of this study.^{29,30} On the other hand, a previous theoretical study on Janus WSSe bilayer shows comparable interlayer interaction energies at different interlayer chalcogen pair configurations,²⁸ consistent with that of the SnSSe bilayers reported in this study. Next, as observed for relaxed SnSSe bilayers in this study, both Janus MoSSe41 and WSSe28 bilayers show the lowest bandgap at S-Se interlayer chalcogen pairs at different interlayer stacking orientations, which is consistent with the findings of this study. Moreover, similar to the S-Se configuration of the SnSSe bilayer reported in this study, the asymmetrical interlayer chalcogen pairing in MoSSe leads to a finite interlayer charge transfer⁴¹ and subsequent interlayer dipole moment⁴² and electric field.⁴¹ On the other hand, for MoSeTe and WSeTe bilayers in asymmetrical interlayer chalcogen pairing with in AA interlayer stacking, the decreasing ILD shows a drastic reduction of energy bandgaps and eventually semiconducting to metallic transformations, wherein a small reduction in energy bandgap can be observed with increasing ILD. 43 These trends are in good agreement with the qualitative trend of bandgap variations, with the ILD variation study of this work. Interestingly, in the S-Se configuration of the Janus WSSe bilayer, the application of both BC and BT strain reduces the energy bandgap, as also observed in this study for the S-Se configuration of the SnSSe bilayer. 28 Finally, the previously reported interlayer electric fields and dipole moment values for different Janus TMD bilayers in their asymmetric interlayer chalcogen pairing configurations are compared with the findings of this study in Table 3.

Therefore, the comparative analysis emphatically suggests that the asymmetric interfacial chalcogen pairing in Janus TMD bilayers can induce finite interlayer charge transfer, interlayer dipole moment and a built-in interlayer electric field. The presence of an interlayer electric field is expected to induce a type-2 band alignment with interlayer excitons and simultaneously a bandgap reduction in Janus TMD bilayers with asymmetric interfacial chalcogen pairing. Moreover, the S–Se stacking configuration of Janus SnSSe exhibits a comparable interlayer dipole moment and intrinsic interlayer electric field to those previously observed in MoSSe.

Finally, to date, a number of Janus monolayer TMDs, including SnSSe, have been successfully synthesized using CVD using selenization or sulfurization of the top chalcogen layer, 12,13 selective epitaxy atomic replacement, 4 hot injection of Se precursor and S precursor solutions into the Sn precursor15 and plasma-driven selenization.16 However, the controlled synthesis of few-layered Janus TMDs using precise interfacial chalcogen combinations is a significant challenge. To the best of the authors' knowledge, to date, the closest attempt in this direction has reported the heterostructure of MoSSe with MoS2 with S-Se and S-S interfacial chalcogen combinations. 82 Specifically, monolayer MoSSe is prepared by selenization of CVD-synthesized monolayer MoS2, followed by its transfer onto the as-grown monolayer MoS₂ using poly-methyl methacrylate (PMMA) to form either S-S or Se-S interfacial chalcogen combinations at the hetero-interfaces.82 Therefore, adapting these synthesis strategies for bilayer SnSSe, particu-

Table 3 Comparative study of theoretically calculated interlayer dipole moments and interlayer electric fields in bilayer Janus TMDs

Material	Dipole moment (Debye)	Intrinsic electric field (V \mathring{A}^{-1})
S–Se configuration of 2L-MoSSe ⁴¹	_	0.45
S–Se configuration of 2L-MoSSe ⁴²	0.34	_
S–Se configuration of 2L SnSSe ³⁰	0.34	_
S–Se configuration of 2L SnSSe ²⁹	_	0.18
S-Se configuration of 2L SnSSe (this work)	0.27	0.14

larly to realize well-defined S-Se interlayer configurations, is likely to require an integrated approach combining vertical layer-by-layer transfer with plasma-assisted chalcogen-substitution techniques. These methods require precise control over stacking order and interfacial cleanliness. Specifically, achieving selective alignment of S and Se atoms across layers without significant lattice distortion remains a formidable challenge. Nevertheless, overcoming these obstacles can pave the way for high-performance optoelectronic devices based on SnSSe bilayers.

Conclusion

In this study, the effects of different interfacial chalcogen pair configurations on the structural and electronic properties of Janus SnSSe bilayers were extensively investigated, emphasizing the interlayer energy band alignment. This is followed by a detailed study of interlayer band alignments with respect to interlayer distance and biaxial strain variations. The results indicate that three distinct interlayer chalcogen pair configurations, i.e. S-S, S-Se, Se-Se, can be realized in bilayer SnSSe, where each configuration is energetically and dynamically stable and is equally likely to form. The breaking of out-ofplane mirror symmetry in the S-Se configuration results in unique properties, including finite interlayer transferred charge density (~2.2 μC cm⁻²), finite interlayer dipole moment density (\sim 1.81 \times 10¹⁴ D cm⁻²), finite effective interlayer electric field ($\sim 0.5 \text{ V nm}^{-1}$), reduced energy bandgap ($\sim 14\% - 15\% E_{\text{g}}$ reduction), and type-2 band alignment compared to other two interlayer chalcogen pair configurations. Moreover, S-Se configuration demonstrates clear interlayer separations between the CBM and VBM Bloch state with CB offset ~0.36 eV and VB offset ~0.29 eV in its type-2 band alignment, suggesting the unique possibility of realizing interlayer excitons in a homogeneous bilayer. The results further suggest that the variation in the interlayer separations and applied biaxial strain can be used to effectively tune the electronic properties of the S-Se configuration of the SnSSe bilayer. Typically, both smaller ILDs and larger BC strains can annihilate the type-2 band alignment while causing a drastic reduction in E_g (~43% at 5% BC strain from 2% BC strain) in the S-Se configuration. In contrast, in S-Se configuration, increasing ILD slightly reduces the E_{g} (~8% with 1.5 Å increase in ILD), retaining the type-2 band alignment, with a slight increase in VB offset (~6% with 1.5 Å increase in ILD) and comparable CB offset, while expecting to improve the interlayer exciton radiative lifetime owing to reducing electron-hole wave function overlap. However, increasing the BT strain retains the type-2 band alignment, and at the same time, notably reduces the $E_{\rm g}$ (~42% at 5% BT strain from relaxed configuration) and increases the CB/VB offset (~33% increase in CB and 19% increase in VB at 5% BT strain from relaxed configuration), while expecting to slightly degrade the interlayer exciton radiative lifetime in S-Se configuration owing to increasing conduction band spread in energy. In summary, this study demonstrated that dissimilar chalcogen

pairing in the Janus SnSSe bilayer is a potential homogeneous 2D material system for realizing type-2 band alignment, which can be further efficiently tuned by applying BT strain and increasing ILD. The generation of interlayer excitons in such strain-engineered S-Se configuration of SnSSe bilayers can lead to the realization of tuneable electron-hole separation in real and reciprocal spaces. The presence of interlayer exciton in S-Se configuration of SnSSe bilayers and their tunability with increasing ILD and BT strain can offer significant advantages for electronic and optoelectronic applications, including exciton-based transistors, ultra-low threshold lasers, excitonic transistors, ultra-sensitive broadband photodetectors, and tuneable LED designs. Moreover, the realization and manipulation of interlayer excitons are expected to play a transformative role in valleytronics for low-power information processing, including energy-efficient data manipulation and storage.

Author contributions

Naresh Bahadursha: visualization, validation, software, methodology, writing - original draft, preparation, investigation, and data curation. Chanda Bhavitha Sri: validation, software, methodology, and data curation. Kuna Krishna Ruthvik: validation, software, methodology, and data curation. Swastik Bhattacharya: writing - review and editing, investigation, and formal analysis. Sayan Kanungo: writing - review and editing, writing - original draft, validation, supervision, investigation, formal analysis, and conceptualization.

Data availability

The data supporting this article have been included as part of the ESI.†

The code for ab initio DFT simulations can be found at https://www.synopsys.com/manufacturing/quantumatk.html and is described in J. Phys.: Condens. Matter (APS), vol. 32, p. 015901 (2020). The code used in this study was the QuantumATK version V-2023.12.

Conflicts of interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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