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Critical role of precursor flux in modulating nucleation density in 2D material synthesis revealed by a digital twin[†]

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Chemical vapor deposition (CVD) is the most widespread approach for two-dimensional (2D) material synthesis, yet control of nucleation density remains a major hurdle towards large-area growth. We find that precursor flux, a function of gas velocity and precursor concentration, is the critical parameter controlling nucleation. We observe that for a vertically aligned substrate, the presence of a cavity/slot in the substrate-supporting plate creates an enhanced growth zone for 2D-MoS₂. The effect of this confined space on nucleation density is experimentally verified by electron microscopy. To understand this intriguing observation, we developed a hyper-realistic multiphysics computational fluid dynamics model, *i.e.*, a digital twin of our CVD reactor, which reveals that space confinement achieves nearly-zero gas velocities. Digital twin-informed calculations indicate a significantly lower metal precursor flux at the confined space during the initial stages of growth, while precursor concentration is uniform across the substrate. The digital twin also makes an important prediction regarding a large time-lag between the set temperature, reactor environmental temperature, and substrate temperature, with implications for nucleation and growth. We offer a framework for designing confined spaces to control nucleation *via* regulating precursor flux, and for simulating reactor parameters for rapid optimization *via* the digital-twin model.

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Introduction

Transition metal dichalcogenides (TMDs) are exemplary two-dimensional (2D) materials, promising for electronic and optoelectronic applications,^{1–3} as well as for catalysis, including carbon dioxide reduction⁴ and hydrogen evolution reactions.⁵ Mechanical exfoliation⁶ and chemical vapor deposition (CVD)^{7–9} are the most common methods used for the synthesis of TMD monolayers (MLs). CVD can potentially provide high uniformity, repeatability, control of layer number, and scalability to large areas. However, CVD is a complex multiscale process involving heating precursors (gaseous or solid), vapor-phase transport by an inert carrier gas to the substrate, and subsequent reaction and deposition. Obtaining high-quality MLs using CVD is challenging due to reactor-to-reactor variability and local changes in temperature, concentration, and flow fields.^{10,11} Even a seemingly minor variation in these

experimental parameters can significantly impact the quality of the growth.^{12–14} However, multiphysics simulation studies that model the complex transport phenomena occurring in a CVD reactor and use them to develop new growth strategies are lacking.

There is a critical need to connect experimental parameters, such as the set temperature and gas flow rate, to mesoscopic variables such as the local temperature, concentration, and fluid flow profiles, and finally to thermodynamic variables and experimental observations of growth. For example, temperature impacts evaporation rates of the precursors,^{15,16} growth rate, and shape of the synthesized 2D material.^{17,18} However, the temperature profile inside a CVD reactor is expected to be non-uniform, with implications for non-stoichiometric growth. Similarly, obtaining a quantitative model of the vapor pressure (concentration) profile is critical for modifying nucleation and growth kinetics. Furthermore, the velocity profile of the carrier gas influences the concentration profile at the substrate,^{19,20} as well as sticking coefficients.²¹ Therefore, developing a digital twin (*in silico* CVD reactor) for a real CVD system will lead to an informed modification of experimental parameters and improve reproducibility, thus going beyond the currently practiced experimental trial-and-error paradigm. Previous simulation studies have mostly aimed at understanding the reaction pathways controlling growth *via* density functional theory^{22,23}

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(DFT), though some recent studies focus on computational fluid dynamics (CFD) aspects.^{24–26} However, the effect of the complete reactor geometry in modulating gas flow dynamics, along with precursor concentration and temperature models in a multiple temperature zone setup, is still critically missing.

Importantly, the combined role of local velocity and concentration, *i.e.* a treatment of precursor flux, is critically missing. For example, confined space geometries have been utilized in CVD processes to modulate precursor concentration and velocity profiles.^{27–30} Gas flow velocity and temperature field simulations have been performed for the case of single heating zone reactors,³¹ and limited to horizontally positioned substrates.^{32,33} However, velocity, concentration, and temperature profiles have been treated separately, leading to an incomplete understanding of the CVD process, including nucleation and growth.

Large-scale device fabrication requires large-area growth of superior quality 2D materials. Reducing nucleation density proportionally increases the edge lengths, and results in fewer and sparsely occurring grain boundaries, hence improving optoelectronic and electronic properties. Furthermore, a comprehensive understanding of the dynamics of nucleation, controlled by the dynamics of temperature, is critically important. Random, uninhibited nucleation results in a high nucleation density, limiting the size of the obtained flakes.^{34,35} A higher precursor concentration at the substrate initiates a “self-seeding” nucleation mechanism, which may also result in multi-layer growth.³⁶ Thus, a controlled nucleation density is the key to achieving desired ML growth and flake size.³⁴

Here, we experimentally perform oxygen-assisted three-zone atmospheric pressure CVD (AP-CVD) of ML MoS₂ and create the corresponding digital twin: a comprehensive computational fluid dynamics (CFD) model including heat, mass, and momentum transport equations. For a vertically aligned substrate (normal to the incoming gas flow), we find that the presence of a slot (cavity) in the supporting plate creates an excellent growth zone for MoS₂, compared to no growth observed on the rest of the substrate, and on the substrate which does not have a slot. We create a COMSOL Multiphysics® finite element model by accounting for fluid flow dynamics, evaporation of chalcogen and metal oxide precursors, realistic substrate geometries, and temperature profiles. Using this hyper-realistic model, we observed no significant concentration gradients for the vertically aligned substrate. However, a velocity dead-zone is created in the slot area, wherein we find direct evidence of reduced nucleation density *via* electron microscopy. Thus, precursor flux, which is a function of gas velocity, precursor concentration and concentration gradient, emerges as the critical parameter controlling nucleation density. Furthermore, informed by our digital twin, we observed a large time lag between the set temperature, reactor temperature, and substrate temperature, with consequences on growth uniformity and nucleation. Thus, using this model, we make several critical observations on nucleation density, spatial temperature profiles, and gas flow. The deep study of precursor flux, enabled by the digital twin, will lead to the synthesis of higher quality 2D

materials and faster optimization of the nucleation/growth process.

Results and discussion

The setup used for ML MoS₂ growth (on SiO₂/Si substrates) is shown in Fig. 1a. The reactor is a quartz tube (60 mm diameter). Three heated zones provide independent control over the evaporation temperature of the precursors and growth temperature at the substrate, with the zones separated by 75 mm wide insulation barriers. Inert carrier gas (Ar or N₂) transports the vaporized precursors to the substrate placed downstream. We also introduce a small amount of oxygen (O₂) into the system (see Methods for details of the growth process), as it is shown to improve the growth.³⁷ Before heating, the reactor is flushed with high-purity inert gas to obtain reduced levels of residual moisture and O₂ (see ESI Section I and Video V1† for corresponding simulations of the tube environment). Fig. 1b shows a model of the reactor, as used for the simulations with appropriate boundary conditions and sources. Chalcogen (sulfur) powder and transition metal oxide (MoO₃) powders are placed in alumina boats in the first and second heating zones, respectively.

To ensure maximum precursor impingement on the growing surface, the substrate is placed vertically in the third heating zone. As we will see later, vertical placement also enables minimum spatial variation in the precursor concentration, providing a more uniform growth environment. In contrast, for a horizontally placed substrate, even with small dimensions (1 × 1 cm²), a concentration gradient is expected^{32,33} (also see ESI Section II†). This gradient is most pronounced during the nucleation stage and critically affects the type of growth obtained. To support the substrate in a vertical configuration, we created a slot (a groove, 1 mm deep, 1–2 mm wide) in the bottom supporting alumina plate, and supported it at the back using an alumina boat (see Fig. 1b, lower left).

Remarkably, the presence of the slot is decisive toward obtaining ML MoS₂ growth under similar growth conditions across different growth runs and substrates. Fig. 1c and d show optical microscopy images of 300 nm SiO₂/Si substrates after CVD growth, when the substrate is placed inside the slot, and without the slot, respectively. A Raman peak shift of ~20 cm⁻¹, along with typical optical contrast, confirms the presence of ML MoS₂ (ref. 38) (see ESI Section III† for optical spectroscopy and SEM characterization). The presence of ML MoS₂ flakes only in the case of the slotted configuration is striking and points toward the significant effect of the slot on modifying the local growth environment.

Development of the multiphysics digital twin

We used COMSOL Multiphysics® to develop a coupled 3D model of gas-flow, precursor concentration, and temperature distribution for a realistic simulation of the CVD process. To understand the gas flow dynamics and the precursor concentration inside the slot, we carefully modeled the source geometry, substrate supports, and specific materials of various

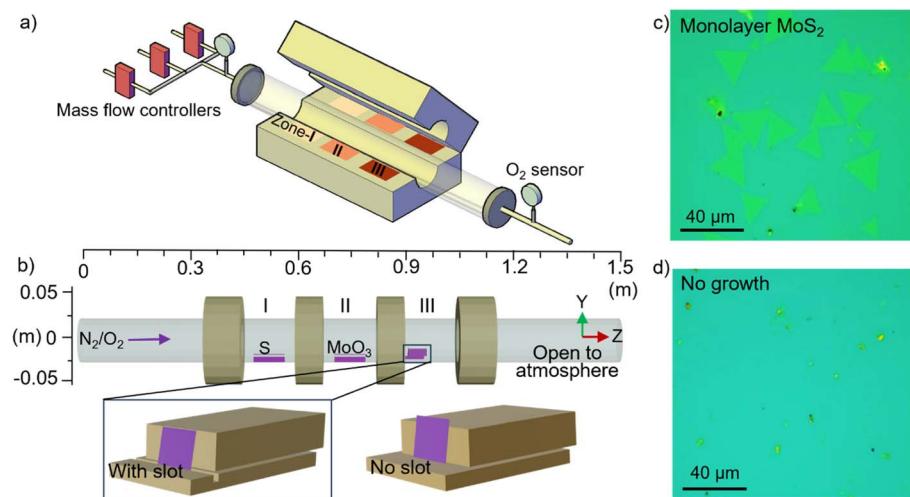


Fig. 1 Schematic of the CVD setup and growth of monolayer MoS₂. (a) Schematic of the 3-zone furnace and experimental setup used for atmospheric pressure CVD (AP-CVD) of monolayer MoS₂. (b) Schematic of the reactor geometry setup in COMSOL Multiphysics®. Heating zones are labeled as I, II and III, separated by insulation zones. Boundary conditions at reactor ends are indicated. S and MoO₃ powder precursors are placed in zones I and II, while the substrate is placed vertically in zone III. Carrier gas is introduced from the left and the reactor is in an ambient environment at $t = 0$. Schematics of slotted and non-slotted substrate configurations are shown in the lower panel. Optical microscopy images of CVD grown triangular monolayer MoS₂ on SiO₂/Si for (c) slotted and (d) non-slotted configurations.

assemblies. The synthesis process can be divided into four broad parts: nitrogen flushing, reactor heating, precursor vaporization, and reaction and deposition. We developed an integrated model for the first three of the mentioned processes, simulating the actual experimental conditions as closely as possible (see Methods for mesh sizes for simulations and specific COMSOL modules used). The deposition process is modeled by considering evaporation and downstream transport of the powder precursors to the substrate.

In the context of CVD, transfer of physical quantities inside a physical system is a combination of convection (due to inert carrier gas flow) and diffusion^{25,26} (due to concentration gradients). The governing equation for describing such a physical phenomenon is the diffusion-convection equation (DCE):

$$\frac{\partial C(x, y, z, t)}{\partial t} = \vec{\nabla} \cdot \left(D \vec{\nabla} C(x, y, z, t) - \vec{v} C(x, y, z, t) \right) \quad (1)$$

where C is the local fluid concentration (mol m⁻³), \vec{v} is the carrier gas velocity (m s⁻¹), D is the precursor diffusivity in the carrier gas (m² s⁻¹),³⁹ and x (m) is the coordinate along the reactor. Using the DCE, we can also model precursor evaporation with the addition of a source term:

$$\frac{\partial C(x, y, z, t)}{\partial t} = \vec{\nabla} \cdot \left(D \vec{\nabla} C(x, y, z, t) - \vec{v} C(x, y, z, t) \right) + r_v(x, y, z, t) \quad (2)$$

where r_v is the precursor source term, *i.e.*, molar production rate per unit volume (mol m⁻³ s⁻¹). The saturation vapor pressure (P_s) for a given species is primarily a function of temperature (T).^{40,41} We used the Knudsen–Langmuir equation⁴² to model the temperature-dependent evaporation of the precursors, as detailed in ESI Section IV.[†]

Understanding concentration profiles and fluid flow inside the reactor

We first examine precursor and O₂ spatiotemporal profiles at the substrate. We note that our synthesis process minimizes precursor evaporation prior to the set temperature being realized (see ESI Section IV[†] for corresponding axial simulations of MoO₃ and O₂). Hence, for the purpose of modeling precursor evaporation, we allow the precursors to evaporate only after heating is completed (30 min).

Fig. 2 shows the MoO₃/S₈ ratio and O₂ profiles at the substrate after 5 minutes of the beginning of growth, with and without the slot. Elemental sulfur (S) in its vaporized form exists as S₈ (octa-sulfur) molecules.⁴³ Hence, the concentrations of sulfur and oxygen depicted are those of S₈ and O₂ species, respectively, and are discussed as such in the rest of the manuscript. Elemental concentrations may be obtained by multiplying S₈ and O₂ concentrations by a factor of 8 and 2, respectively. Importantly, the presence of the slot does not result in a spatially varying precursor profile at the substrate for any of the simulated species, and thus, we have indicated the average values of precursor concentration. Furthermore, the slot does not affect the average surface concentration of the reacting species compared with the non-slotted configuration (MoO₃/S₈ ratio (Fig. 2a and c) and O₂ (Fig. 2b and d)). A similar trend was observed throughout the growth time (see ESI Section IV and Videos V2, V3, and V4[†] for simulated profiles along the length of the reactor and at other time steps during growth).

Precursor concentration gradients are not the underlying reason for the observed drastic changes in growth between slotted and non-slotted configurations. Concentration, velocity fields, and temperature are the primary parameters affecting nucleation and growth, amongst which concentration and



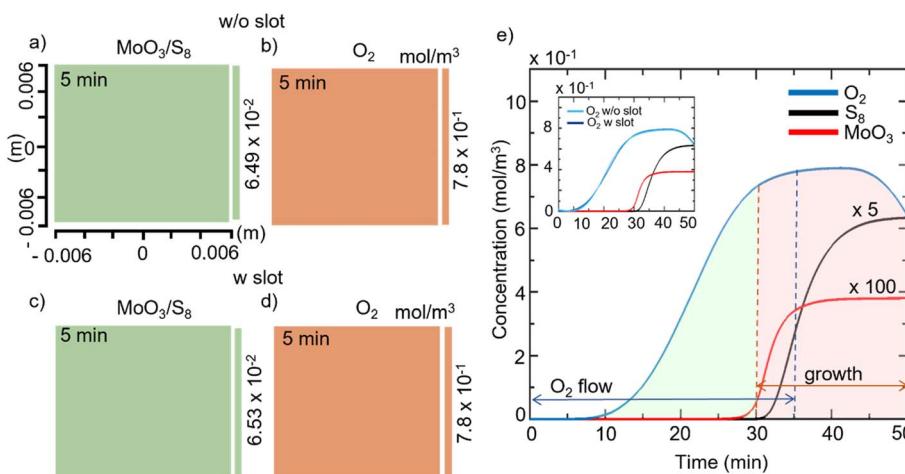


Fig. 2 Comparison of concentration profiles at a vertically placed substrate. MoO_3/S_8 ratio profiles for (a) non-slotted and (c) slotted substrate configurations. O_2 profiles for (b) non-slotted and (d) slotted substrate configurations. The coordinate system is defined w. r. t. the substrate, with $(0, 0, 0)$ being the substrate center. Y coordinates in (b) and (d) are the same as those in (a) and (c). All profiles are shown at the beginning of the growth process. (e) Concentration profiles of O_2 , S_8 and MoO_3 at the substrate throughout the deposition process. Heating and growth periods are shaded in green and orange, respectively. The inset shows the same profiles with and without slotted configurations. Profiles for S_8 and MoO_3 are almost similar for the two configurations and represented by a single line. Inset axes have the same units as (e).

temperature are similar for both slotted and non-slotted configurations. Hence, we must take a careful look at the velocity profiles near the substrate.

First, we calculate the Reynolds and Mach numbers to understand the type of carrier gas flow (laminar *vs.* turbulent and incompressible *vs.* compressible, respectively) in our reactor. The Reynolds number (Re) is a nondimensional number that quantifies the ratio of inertial to viscous forces in a flow field, calculated as

$$\text{Re} = \frac{\rho u L}{\mu} \quad (3)$$

where ρ is the carrier gas density (kg m^{-3}), u is the carrier gas speed (m s^{-1}), L is the characteristic length (m) (the diameter of the tube here), and μ is the carrier gas dynamic viscosity ($\text{kg m}^{-1} \text{s}^{-1}$). A lower value of Re (typically $<10^3$) predicts the flow to be laminar.^{44,45} Furthermore, the Mach number is defined as

$$M = \frac{u}{c} \quad (4)$$

where u is the carrier gas flow speed (m s^{-1}) and c is the speed of sound in the inert carrier gas (m s^{-1}). Typical gas flow speeds in our CVD reactor are on the order of 10^{-2} – 10^{-3} m s^{-1} , and with ambient viscosity. The above equations lead to $\text{Re} \sim 1$ and Mach number $\sim 10^{-6}$ – 10^{-7} , and thus, the carrier gas flow should be laminar and incompressible. Although the calculated Mach number is low, we have employed the compressible fluid flow sub-module, because large temperature variations in the system (as revealed by our multiphysics simulations) can cause significant density changes inside the CVD reactor.

Now, we simulate the carrier gas velocity streamlines (while accounting for simulated temperature profiles), representative of the fluid flow direction at any given point. In any given volume element, the evaporated precursor atoms will be

imparted momentum in the direction tangential to the nearby streamlines. Hence, streamlines serve as useful tools for visualizing and understanding the local growth environment near the substrate. Note that the ratio of substrate area and reactor cross section is very small (~ 0.04), and hence only streamlines within a small radial cross section interact with the substrate. For discussion, we have indicated (Fig. 3) only those sets of streamlines that impinge on the surface of the substrate, and ignored the ones that fall outside or go around.

A comparison between Fig. 3a (slotted) and 3b (non-slotted) reveals that the carrier gas, upon encountering the substrate, is pushed down toward the slot, whereby its velocity decreases due to the slot geometry. Thus, a region of very low velocity, hereafter referred to as a “velocity dead-zone” (stationary zone), is

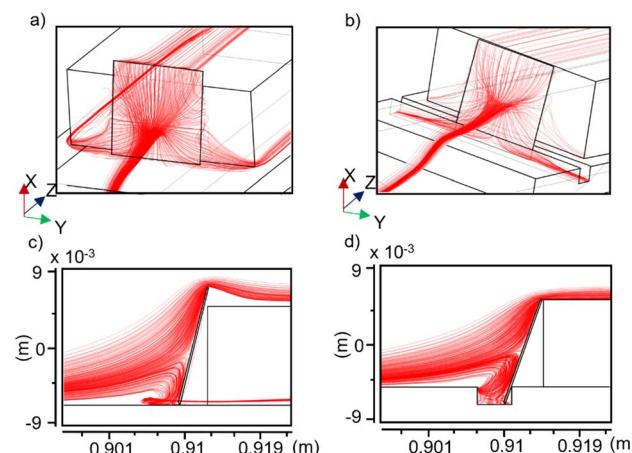


Fig. 3 Comparison of the velocity profiles at the substrate. Carrier gas velocity streamlines near the substrate are plotted for (a) non-slotted and (b) slotted configurations. Axial carrier gas velocity streamlines near the substrate for (c) non-slotted and (d) slotted configurations.



created near the slot. Due to the lower flow velocity and laminar nature of fluid flow, streamlines bend inside the slot (Fig. 3d). For the non-slotted configuration (Fig. 3c), streamlines show a reversal of the flow at the bottom of the substrate, leading the flow away from the surface before turning sideways to continue the forward flow. This reverse current is suppressed in Fig. 3d due to the slot geometry confining the flow inside it. This can directly affect the nucleation density at the substrate, as we will see later.

Next, we examined the velocity profiles directly at the substrate surface. Note that during heating and growth, the velocity inside the reactor is in a steady state, and hence we plot the steady-state magnitudes of the velocity components. Fig. 4a and d show the transverse velocity profiles over the substrate, distinctly showing an overall reduction in magnitude in the case when a slot is present. This effect is more pronounced in the region of the substrate physically inside the slot, where the velocity is almost two orders of magnitude lower than in the

nearby region (physically outside the slot). Fig. 4b and e show surface plots of the normal component of the velocity at the substrate. It can be seen in Fig. 4b that a lower velocity region exists toward the bottom of the substrate where it is in contact with the alumina plate. With the slotted configuration in Fig. 4e, this area extends out. The significant changes in the local growth environment due to modified gas flow dynamics should directly affect the delivery of the precursor on the substrate.

To corroborate our understanding of the non-trivial influence of the carrier gas velocity profile and precursor concentration, we calculated the incoming precursor flux (J , at the substrate) analytically. The steady-state nucleation rate⁴⁶ goes as $Q_0 \propto J^2$ (see ESI Section V† for a detailed derivation). Hence, a decreased precursor flux to the substrate would result in an overall reduction in the nucleation density.

Using data obtained from the multiphysics simulations, particularly precursor concentration, surface temperature

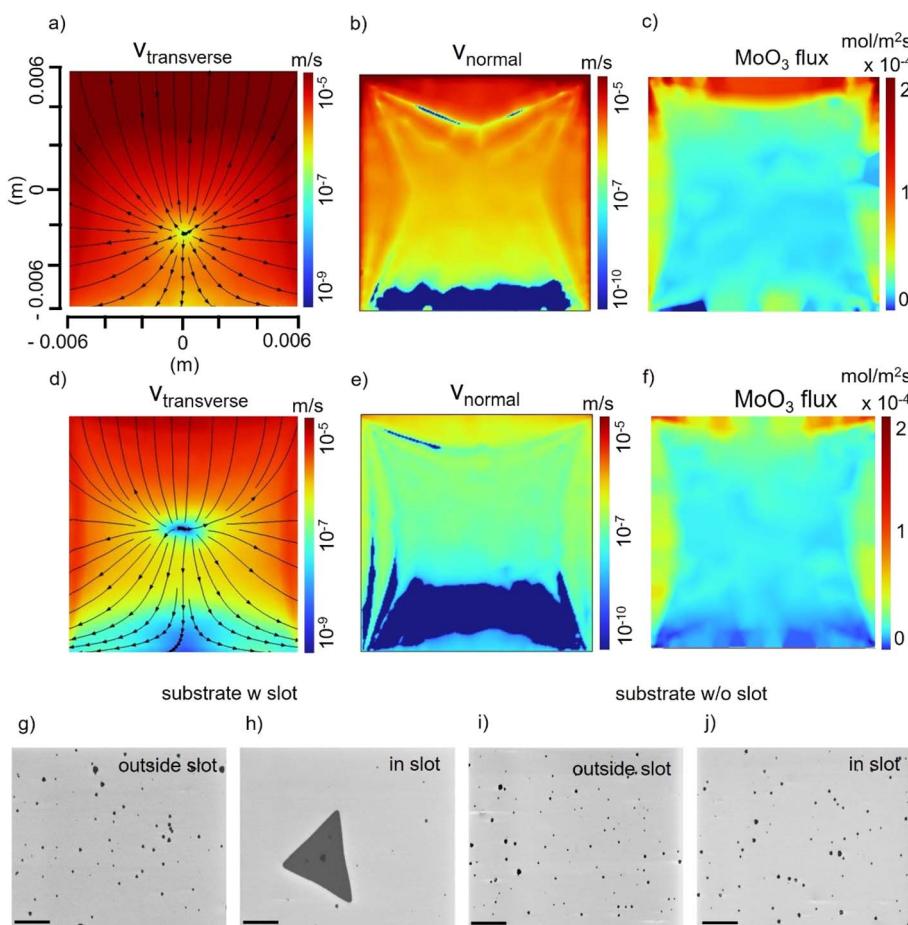


Fig. 4 Simulated velocity surface plots at the substrate and experimental observation of nucleation densities. Transverse component of the carrier gas velocity at the substrate for (a) non-slotted and (d) slotted configurations, respectively. Lines on the substrate denote gas flow streamlines. Normal component of the carrier gas velocity at the substrate for (b) non-slotted and (e) slotted configurations, respectively. Transition metal precursor flux at the substrate for (c) non-slotted and (f) slotted configurations, respectively. Flux is plotted for 5 minutes after growth starts. Axes coordinates in (b–f) are the same as those in (a). Scanning electron microscopy (SEM) images of the region of the substrate (g) away from and (h) inside the slot. (i and j) SEM images of the substrate in the non-slotted configuration at regions similar to (g) and (h). Labels “outside slot” and “in slot” in (i) and (j), respectively, represent similar vertical positions as (g) and (h) for comparison with the substrate placed without a slot. The scale bar is 10 μ m.



during the estimated nucleation window (roughly between 1 and 5 minutes of growth, see ESI Section IV†), and the velocity components at the substrate, we obtained the precursor flux at each substrate surface element (governed by the mesh size employed for simulations). Earlier studies have indicated that TMD nucleation is governed primarily by the concentration and adsorption–desorption equilibrium of the transition metal precursor.^{15,47,48} With this in mind, Fig. 4c and f show the calculated MoO_3 flux, incoming at the substrate at 5 minutes of growth, for the non-slotted and slotted configurations, respectively (see ESI Section V† for MoO_3 flux profiles throughout the growth, S flux profiles, and details of the flux calculations). In the presence of a slot, the MoO_3 flux reduces to 1/3rd of the value compared to the case without a slot. Interestingly, the spatial variation in the precursor flux and the surface velocity follows a similar trend.

To directly measure the nucleation density, we performed scanning electron microscopy (SEM) of the substrates. Fig. 4g–j correspond to slotted and non-slotted configurations, respectively, under similar optimized growth conditions (see ESI Section VII† for comparison at other vertical distances from the slot). A comparison of Fig. 4g and i, which are taken at similar vertical positions on the substrate, well away from the slot, shows similar density, size and shape of nucleation sites. A more careful observation reveals the presence of small MoS_2 flakes with a triangular shape. Due to an increased rate of nucleation in this region, the growth of MoS_2 flakes is limited to a maximum edge length of $\sim 1\text{--}2\ \mu\text{m}$. On the contrary, Fig. 4h (in the slot) and 4j (without slot), which are at the same vertical positions on the substrate, show remarkably different depositions. In Fig. 4h, the nucleation density is reduced, and MoS_2 triangular flakes with edge length $\geq 30\ \mu\text{m}$ are observed. Interestingly, for the substrate placed without a slot (Fig. 4j),

a deposition similar to Fig. 4g and i is observed. This is direct evidence that a slot-induced, confined space reaction environment leads to a decrease in the nucleation density. Statistical analysis indicates an order of magnitude reduction in nucleation density in the slot region (ESI† Section VI). Hence, reduced precursor flux leads to reduced nucleation density in the slot. Thus, precursor flux, and not just the precursor concentration, is the decisive parameter controlling nucleation.

Predicting temperature variations in the CVD reactor

Temperature has a significant impact on nucleation and ML growth. Even in analytical calculations for the impingement rates discussed above, the rate of nucleation depends exponentially on the temperature of the substrate. Thus, a complete understanding of the dynamic heating process and local temperatures in a CVD reactor is necessary. In our COMSOL model, we accounted for the heating rate and heat diffusion between neighboring heating zones, as well as the realistic thermal conductivity of the materials in the reactor (alumina, quartz, and inert gas). Such a model is valuable even for simulating the post-deposition cooling process, with an effect on uncontrolled deposition.

Fig. 5 and Video V5† depict the time-dependent simulated axial temperature profile along the reactor. The set temperatures of all three zones are achieved in 30 minutes (onset of the growth time in our CVD process). We observe that there is finite heat leakage *via* the insulation zones, and the temperatures of the areas near the insulation zones are less than at the centers of the heating zones. Furthermore, due to the presence of heating sources at the radial boundaries, a radial temperature gradient forms in the reactor (see ESI Section VII†).

Remarkably, the temperature (Fig. 5c) of the substrate assembly (combination of the substrate, alumina boat, and plate)

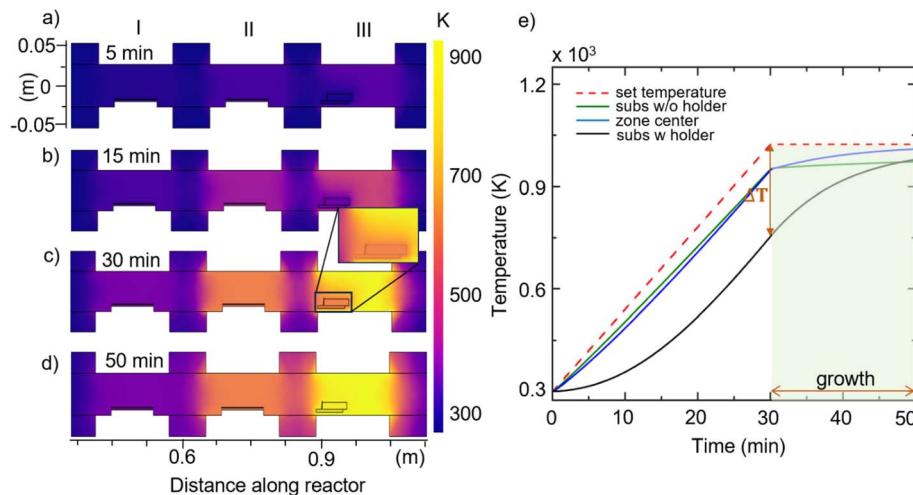


Fig. 5 Developing new insights with the developed digital-twin model. Simulated temperature profile of the reactor. Axial temperature profiles of the reactor are plotted at (a) 5, (b) 15, (c) 30, and (d) 50 minutes. The total heating time taken to achieve the set temperature is set to 30 minutes. The inset in (c) shows the temperature profile near the substrate. The view shows the reactor between the first and last insulation zones. Representation is not to scale, and the reactor is stretched vertically to highlight variations in the temperature profiles. (e) Comparison of time-dependent average temperature profiles of the source (set temperature), zone center, and the vertically placed substrate, with and without alumina supports (subs w/o holder and subs w holder, respectively). The growth window is shaded in green.



is much lower than the center of the heating zone. The set temperature and the substrate temperature show a lag of nearly ~ 250 °C. Furthermore, the zone-center temperature and the substrate temperature show a lag of nearly ~ 150 °C. This temperature difference is significant considering the above-mentioned exponential relation between nucleation and temperature, and can lead to markedly different types of growth. As a critical experimental insight, we observe that by the onset of growth, the substrate is still not at the desired temperature, and doesn't reach the set temperature even till the growth is finished (Fig. 5e and ESI Section VII†). We note that such an observation is very challenging to make experimentally and leads to a more comprehensive understanding of the observed growth. Through careful selection of holder materials and adjustment of the growth process, such effects may be minimized, or even tuned.

We attribute this significant time-lag to the large heat capacity of the substrate assembly, compared to the inert environment. The specific heat capacities of inert gas (N_2) and alumina are similar. However, the large difference in density leads to a larger heat capacity for alumina boats and supports, compared to that of the surrounding inert atmosphere (see ESI Section VII†). Fig. 5e shows time-dependent plots for the heat source and the average surface temperature at the substrate, with and without alumina supports. The average temperature at the substrate significantly lags behind the source due to the alumina supports, while it follows the source temperature closely in the absence of alumina (with air being replaced for alumina in the simulations) as the supporting material. We note that "without alumina supports" is a hypothetical setting used in the simulation, where the substrate is unsupported. In reality, such a system can be created by using a holder with one or a few contact points on the substrate.

We believe that such temperature differentials and dynamics will also arise in other CVD reactors depending upon the specific material used as the substrate holder, and especially since most reactors use alumina or quartz. Additionally, since nucleation occurs in the initial stages of growth in a very narrow time frame, nucleation is sensitive to the instantaneous temperature rather than the average temperature over the growth time scale. Similarly, such temperature variation could also be found in the precursor alumina boats, which implies that the actual temperature of precursor evaporation may be much lower than expected. Also, large temperature gradients might lead to deposition of the unreacted material and bulk/secondary deposition, resulting in poor quality of growth. In short, low temperature differentials are expected to lead to controllable film growth, and conversely, high temperature differentials can lead to particle formation and higher growth rates. The significant temperature differentials between the substrate and local inert gas environment may also give rise to thermo-diffusion or the Ludwig–Soret effect,^{49,50} which can lead to the aggregation of heavier (MoO_3) and lighter (S) precursors in the colder and warmer regions of the as-formed thermal boundary layer close to the substrate.^{51,52}

Conclusions

In summary, we report the non-trivial effect of transition metal precursor flux in modulating the 2D TMD nucleation density in

a confined-space microreactor (vertically placed substrate in a slot). This unique insight is enabled by the development of a hyper-realistic digital-twin CFD model, accounting for specific reactor and substrate holder geometries, evaporation and transport of precursor species, and reactor heating. Significant modifications in the carrier gas flow near the slot (velocity-dead zone), revealed by the digital twin, impact precursor delivery during the nucleation and growth stages. Thus, the precursor flux is the critical parameter controlling nucleation, wherein the reduction of nucleation density is experimentally verified by electron microscopy. Furthermore, we predict a significant time lag between the actual substrate temperature and the set temperature, explained by the high heat capacity of the substrate holder. Thus, such a multiscale model offers a better understanding of the actual growth temperature and local temperature variations at different places in the reactor, allowing local tunability and control.

Laminar flow (present in our system) is universally preferred for vapor deposition techniques including CVD,^{25,53} Metal Organic CVD (MOCVD)^{54,55} and even physical vapor deposition systems.⁵⁶ In contrast, turbulent flow can lead to non-uniform thickness and degrade film quality.^{57,58} For such widely used laminar flow systems, our conclusions, which are based on modified gas flow dynamics due to geometrical confinement, will be valid. The exact modification of streamlines in a smooth, laminar flow of carrier gas would, of course, depend on the specific holder assembly in question but can be predicted in a similar manner to our CVD system. It should be noted that the digital-twin model is centered on transport phenomena (heat/mass transfer and fluid flow) and is independent of specific reaction kinetics. This allows for a generally applicable understanding of how macroscopic experimental parameters may affect microscopic variables such as the residence time and nucleation density. This digital-twin model may also be integrated with density functional theory (DFT) calculations and reactive molecular dynamics (MD) simulations to relate a set of macroscopic growth parameters to microscopic physical quantities. These simulations can be used to relate optical and structural properties (such as defects) to growth conditions and reactor configurations. This study motivates exploration of complex substrate holder geometries and introduction of additional physical features to the reactor to controllably modify the local growth environment for high-quality material synthesis. Since such studies are challenging to conduct in practice, the as-simulated profiles will lead to informed decision making. Scalable and reproducible synthesis of 2D-TMDs is crucial for reliable technological applications. However, a proportional scaling of the reactor is expected to alter the type of growth obtained. In this case, the precursor flux emerges as a tuning knob to directly control nucleation density, leading to well-controlled growth. Additionally, for wafer-scale growths, due to the large wafer diameter, temperature inhomogeneities can occur across a wafer. Such temperature variations can be significant and can alter vapor pressure and precursor delivery across the wafer. Detailed modelling of wafer-scale reactors can be performed *via* the digital twin and lead to practically useful insights. Overall, our combined experimental-theoretical work paves the way for informed, predictive, and reproducible growth of high-quality and large-area 2D materials *via* regulating precursor flux,



direct control of nucleation density, and the development of a hyper-realistic digital-twin model.

Methods

Experimental details

Monolayer MoS₂ was grown in a split tube type, horizontal, three-zone furnace. Sulfur (Sigma-Aldrich, CAS no. 7704-34-9, 99.98%) and MoO₃ (Sigma-Aldrich, CAS no. 1313-27-5, 99.97%) powder precursors were used and placed in the first and second zone, respectively. The substrates are sonicated in acetone, IPA, and DI water at 50 °C for 10 minutes each and nitrogen-dried. The substrate was placed vertically inside a slot (groove/cavity) in an alumina plate, supported by another alumina block. Ultra-high purity inert gas (N₂) was used to flush the reactor of ambient air, moisture, and other contaminants. The exhaust is open to the atmosphere, and the process takes place at atmospheric pressure with a constant N₂ flow.

The three zones were individually heated to 200 °C, 530 °C, and 750 °C in 30 minutes with a 100/2 sccm N₂/O₂ flow. Ultra-high purity N₂ (impurity <10 ppm) and O₂ (impurity <5 ppm) were used throughout the complete process. During growth, the flow rate is 100/2 sccm (N₂/O₂) for the first 5 minutes and 100 sccm (N₂) for 15 minutes. After 20 minutes of growth, the flow rate is increased to 100 sccm to flush out unreacted precursors and prevent secondary growth during the cooling phase. The furnace lid is opened for rapid cooling, assisted by a wall-mounted fan. After cooling down using UHP N₂ flow, we evacuate the reactor for ~2 hours before taking out the sample. Surface coverage and morphology of the as-grown ML MoS₂ were observed using a scanning electron microscope (Ultra55 FE-SEM Karl Zeiss) at 5 kV accelerating voltage. Raman and photoluminescence (PL) measurements were carried out on a HORIBA LabRamHR Raman/PL setup using a 532 nm laser.

Multiphysics simulations

Simulations were performed using COMSOL Multiphysics, which utilized the CFD, heat transfer, and chemical reaction engineering modules. The submodules, laminar flow, heat transfer for fluids, transport of diluted species, and transport of concentrated species were used to model the physics inside the CVD tube. Tables S-I in the ESI† provide information about the materials used for modelling individual components of the digital twin. The simulation was performed on a mesh termed “Coarser” in COMSOL with a total of 101 905 elements within the volume of the tube and with an average element quality of 0.6268 in skewness (0 being the worst and 1 being the best). The mesh was fine enough to realize the slot in the model. Running each simulation on a workstation with a 12th Gen Intel i9 with 16 cores took three and a half hours.

Abbreviations

2D	Two-dimensional
TMD	Transition metal dichalcogenide
ML	Monolayer

CVD	Chemical vapor deposition
CFD	Computational fluid dynamics
MoS ₂	Molybdenum disulfide
DFT	Density functional theory
MOCVD	Metal-organic chemical vapor deposition
AP-CVD	Atmospheric pressure chemical vapor deposition
SEM	Scanning electron microscopy
DCE	Diffusion-convection equation
RMD	Reactive molecular dynamics

Data availability

Data and codes for the manuscript are uploaded to the link <https://osf.io/xjqy6/>?view_only=d0d31958b0db434995875c44d7c4a3b6.

Author contributions

Abhinav Sinha (ABS), MV, AS, and AGR developed the overall modeling framework. The inert gas flushing and precursor evaporation model was developed by MV, ABS, AS, and AGR. The temperature model was developed by ABS, KSK, and AS. All simulations were performed by ABS and NK. MV, KSK, and AS developed the experimental framework. MV and KSK performed chemical vapor deposition. MV and KSK carried out optical microscopy, scanning electron microscopy and optical spectroscopy characterization. MV, ABS, AS, and AGR discussed and prepared the manuscript with contributions from all authors.

Conflicts of interest

There are no conflicts to declare.

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