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# Local structure, zero field splitting and optical absorption of Mn<sup>2+</sup> doped ZnK<sub>2</sub>(SO<sub>4</sub>)<sub>2</sub>·6H<sub>2</sub>O single crystals

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The Mn<sup>2+</sup> doped ZnK<sub>2</sub>(SO<sub>4</sub>)<sub>2</sub>·6H<sub>2</sub>O (ZKS) single crystal zero field splitting parameters are obtained using the superposition model. The evaluated parameters agree well with those found from EPR. The conclusion of the experiment that in ZKS, the Mn<sup>2+</sup> ion takes the place of the Zn<sup>2+</sup> site is verified by theoretical analysis. The crystals' optical spectra are estimated by utilizing the crystal field parameters obtained from the superposition model and the crystal field analysis computer program. A good agreement between the calculated and experimental band positions is found. Thus, the experimental results are confirmed by the theoretical studies.

## 1. Introduction

The EPR of the Mn<sup>2+</sup> impurity has been widely studied in a variety of single crystals due to the sensitivity of its zero field splitting values to small structural distortions in the lattice.<sup>1,2</sup> A number of studies have been reported on impurities doped into diamagnetic host lattices at room temperature.<sup>3–5</sup>

The superposition model (SPM) can be used to model the zero field splitting (ZFS) and crystal field (CF) parameters for use in other studies.<sup>6–10</sup> SPM and the point-charge model<sup>11–13</sup> are commonly used to determine the parameters of the crystal field (CF). SPM was proposed for CF under certain assumptions.<sup>14</sup> (1) The CF at a paramagnetic ion is expressible as an algebraic sum of contributions, from other ions in the crystal. (2) When the paramagnetic ion is located at the origin of a chosen coordinate frame, all the major CF contributions from every single ion in the crystal are axially symmetric with respect to its position vector. (3) Only neighboring or coordinated ions (ligands) need to be counted for their CF contributions. (4) CF contributions from single ligands are transferable across different host crystals. Finding a steady spherical polar coordinate system ( $R_L$ ,  $\theta_L$ ,  $\Phi_L$ ) for each ligand or ion from the host crystal's X-ray data is crucial for carrying out an SPM analysis on the CF. Ionic charge, ionic size, and inter-ionic bonding mismatches are likely to cause some local distortion

when transition metal ions are infused. Critical analysis of the experimental spin-Hamiltonian parameters for Mn<sup>2+</sup> and Fe<sup>3+</sup> in CaO and MgO crystals has been done<sup>15</sup> providing the SPM parameters for the EPR data and showing that the CF for 3d ions satisfies the superposition principle. For the alkali earth oxides, sets of SPM intrinsic parameters based on reliable ligand distances have been determined.<sup>16</sup>

The crystals with the general formula A<sub>2</sub><sup>+</sup>B<sup>2+</sup>(XO<sub>4</sub>)<sub>2</sub>·6H<sub>2</sub>O are known as Tutton single crystals, where A is a monovalent cation, B is a divalent cation usually a transition metal and X can be sulfur or selenium.<sup>17,18</sup> Tutton salts are a famous isostructural crystal family which shares the same monoclinic symmetry and the space group *P*2<sub>1</sub>/*a* with two formula units per unit cell *Z* = 2.<sup>19</sup> The Tutton salts are valuable crystals as they are used extensively in UV filters.<sup>20</sup>

Zinc potassium sulfate hexahydrate crystals (ZKS) are crystallized in the monoclinic crystal system and belong to the Tutton crystalline salts. These crystals, because of their growth with high purity and suitable crystal sizes and small transparency in the UV region, could be potential candidates for optoelectronic applications.<sup>21</sup>

EPR study of Mn<sup>2+</sup> doped ZKS has been done at 293.7 K and the spin-Hamiltonian parameters have been obtained.<sup>22</sup> From angular variation studies, it is determined that magnetic [Mn(H<sub>2</sub>O)<sub>6</sub>]<sup>2+</sup> complexes are created when the Mn<sup>2+</sup> ion enters the divalent sites of the Tutton salt lattice. The *a*<sup>\*</sup>*bc* axis system, where *b* and *c* are the crystal axes and *a*<sup>\*</sup> is perpendicular to *b* and *c*, is used to discuss the orientations. The EPR *x* and *z* axes deviate by 9° from both the Zn–O(7) and Zn–O(9) directions in ZKS.

The density functional theory (DFT) studies elucidate the electronic structure regulation in Ru–NiCo<sub>2</sub>O<sub>4</sub> and the

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modification of the d-band center optimizes H\* adsorption energy, which considerably increased the hydrogen production efficiency.<sup>23</sup> A Mo-doped CoN is coupled with NiFe-LDH for preparing a Mott-Schottky heterojunction, addressing the enhanced hydrogen evolution reaction (HER), oxygen evolution reaction (OER), and urea oxidation reaction (UOR) compared with the individual counterparts.<sup>24</sup> This process for varying the local electron density could be a promising route to obtain low-energy consumption green hydrogen generation. DFT calculations were performed to further understand the catalytic mechanism and to assess the influence of Mo doping and heterointerfaces on the HER and OER performance of Mo-CoN coupled with NiFe-LDH. The incorporation of Mo and the fabrication of the composite with NiFe-LDH improve the electrocatalytic activity by modulating the electronic structure [JEC]. The above studies motivated us to perform a theoretical study on the local structure, zero field splitting and optical absorption of Mn<sup>2+</sup> doped ZKS.

In this study, the ZFS parameters *D* and *E* are determined for the Mn<sup>2+</sup> ion in ZKS at 293.7 K (room temperature, RT) taking CF parameters obtained from SPM and perturbation equations.<sup>25</sup> The goal is to locate the Mn<sup>2+</sup> ion and the distortion that is taking place in the ZKS crystal. The results obtained for the Mn<sup>2+</sup> ion at the substitutional Zn<sup>2+</sup> site in the ZKS crystal with local distortion show good agreement with the EPR experimental values. The crystal field analysis (CFA) program and CF parameters are used to calculate the optical spectra of the Mn<sup>2+</sup> doped ZKS single crystals. The calculated positions of the optical energy bands agree reasonably well with those obtained from the experiment. A further aim of the study is to find the extent to which CF theory and SPM analysis can be applied to Mn<sup>2+</sup> ions in ZKS crystals in order to generate an SPM parameter database. This will determine molecular nanomagnet (MNM) design and computer simulation of their magnetic and spectroscopic characteristics. The transition ion-based MNM class currently includes single-molecule magnets (SMMs),<sup>26</sup> single-chain magnets (SCMs),<sup>27</sup> and single ion magnets (SIMs).<sup>28</sup> Because of the interesting magnetic properties of MNMs, such as magnetization's macroscopic quantum tunneling and possible uses in high-density information storage and quantum computing, the above systems have attracted large attention from scientists and researchers.<sup>26,27</sup> There are several synthesized SCM or SMM systems with Mn<sup>2+</sup> and Cr<sup>3+</sup> ions.<sup>29</sup> Since model calculations for simpler crystal systems can be used as a basis for more complex ones, the parameters of the model obtained in this case may be used for ZFS parameter calculations for Mn<sup>2+</sup> ions at similar sites in MNM. This work's modeling can be extended to investigate various crystals of scientific and industrial interest in a number of other ion-host systems.

## 2. Crystal structure

The crystal structure of Tutton salt ZKS is monoclinic with space group *P*2<sub>1</sub>/*a*.<sup>21,30</sup> The unit cell's parameters are as follows: *Z* = 2, *β* = 104.78°, *a* = 9.044, *b* = 12.194 and *c* = 6.151 Å. All other

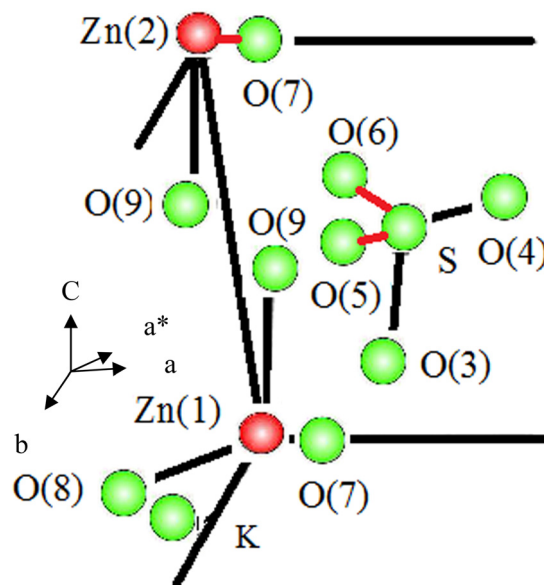


Fig. 1 The room-temperature ZKS crystal structure and the symmetry-adopted axis system (SAAS).

divalent cations in the unit cell are in general positions, with the two inequivalent ones located at points (0, 0, 0) and (1/2, 1/2, 0). Each divalent cation is surrounded by a slightly distorted octahedron of water molecules.<sup>30</sup> Fig. 1 shows the symmetry adopted axis system (SAAS) and ZKS crystal structure.

## 3. Crystal field and zero field splitting parameter calculations

The EPR spectra can be analyzed with the spin Hamiltonian:<sup>7</sup>

$$E(S_x^2 - S_y^2) + D\left\{S_z^2 - \frac{1}{3}S(S+1)\right\} + \mu_B B \cdot g \cdot S = \mathcal{H} \quad (1)$$

where *B*, *μ<sub>B</sub>*, *g*, *D* and *E* are the applied magnetic field, Bohr magneton, splitting factor, second rank axial, and second rank rhombic ZFS parameters.<sup>31,32</sup> The modified crystallographic *a\**, *b* and *c* axes (*a\** is normal to axes *b* and *c*) and the (*x*, *y*, *z*) laboratory axes are shown in Fig. 1. The directions of metal-ligand bonds being mutually perpendicular are referred to as the symmetry adopted axes (SAA) or the local symmetry axes of the site. As shown in Fig. 1, the axis-*Z* of SAAS is along the crystal axis-*c*, and (*X*, *Y*) are perpendicular to the axis-*Z*. When Mn<sup>2+</sup> ions are introduced in the ZKS crystal, they substitute at Zn<sup>2+</sup> (1) sites with some local distortion in the lattice.<sup>33</sup>

The Mn<sup>2+</sup> ion spin Hamiltonian can be written as,<sup>34</sup>

$$\mathcal{H} = \mathcal{H}_o + \mathcal{H}_{so} + \mathcal{H}_{ss} + \mathcal{H}_c \quad (2)$$

$$\mathcal{H}_c = \sum B_{kq} C_q^{(k)} \quad (3)$$

where *B<sub>kq</sub>*, in Wybourne notation, represent the CF parameters and *C<sub>q</sub><sup>(k)</sup>*, the spherical tensor operators. *B<sub>kq</sub>* ≠ 0 in the orthorhombic symmetry crystal field only for *k* = 2, 4; *q* = 0, 2, 4. Employing SPM, the CF parameters *B<sub>kq</sub>* are computed.<sup>34</sup>



The symmetry of the local field about  $\text{Mn}^{2+}$  ions in the ZKS crystal is taken to be orthorhombic (OR-type I),<sup>7</sup> where the ZFS parameters  $D$  and  $E$  are found as follows:<sup>35</sup>

$$D = \left( \frac{3\zeta^2}{70P^2D'} \right) [-B_{20}^2 - 21\zeta B_{20} + 2B_{22}^2] + \left( \frac{\zeta^2}{63P^2G} \right) [-5B_{40}^2 - 4B_{42}^2 + 14B_{44}^2] \quad (4)$$

$$E = \left( \frac{\sqrt{6}\zeta^2}{70P^2D'} \right) [2B_{20} - 21\zeta] B_{22} + \left( \frac{\zeta^2}{63P^2G} \right) [3\sqrt{10}B_{40} + 2\sqrt{7}B_{44}] B_{42} \quad (5)$$

Here  $P = 7B + 7C$ ,  $G = 10B + 5C$ ,  $D' = 17B + 5C$ .  $B$  and  $C$  represent Racah parameters and  $\zeta$  is the spin-orbit coupling parameter. In terms of average covalency parameter  $N$ ,  $B = N^4B_0$ ,  $C = N^4C_0$ ,  $\zeta = N^2\zeta_0$ , where  $\zeta_0$  gives the free ion spin-orbit coupling parameter and  $B_0$  and  $C_0$  are Racah parameters for the free ion.<sup>34,36</sup>  $\zeta_0 = 336 \text{ cm}^{-1}$ ,  $B_0 = 960 \text{ cm}^{-1}$  and  $C_0 = 3325 \text{ cm}^{-1}$  for free  $\text{Mn}^{2+}$  ions.<sup>7</sup>

The covalency parameter  $N$  is found from  $N = \left( \sqrt{\frac{B}{B_0}} + \sqrt{\frac{C}{C_0}} \right) / 2$  using Racah parameters ( $B = 850 \text{ cm}^{-1}$ ,  $C = 2970 \text{ cm}^{-1}$ ) obtained from optical analysis of the  $\text{Mn}^{2+}$  ion in zinc cesium sulphate hexahydrate where ligands are oxygens,<sup>37</sup> as no optical absorption of  $\text{Mn}^{2+}$  doped ZKS has been reported.

The CF parameters using SPM are determined,<sup>14,35</sup> in terms of co-ordination factor  $K_{kq}(\theta_j, \varphi_j)$  and intrinsic parameter  $\overline{A}_k(R_j)$ , as

$$B_{kq} = \sum_j \overline{A}_k(R_j) K_{kq}(\theta_j, \varphi_j) \quad (6)$$

$\overline{A}_k(R_j)$  is found from

$$\overline{A}_k(R_0) \left( \frac{R_0}{R_j} \right)^{t_k} = \overline{A}_k(R_j) \quad (7)$$

where the ligand's distance from the  $d^n$  ion is denoted by  $R_j$ ,  $\overline{A}_k(R_0)$  is the intrinsic parameter,  $R_0$  is the reference distance of the ligand from the metal ion and  $t_k$  gives the power law exponent. For  $\text{Mn}^{2+}$  doped crystals,  $t_2 = 3$  and  $t_4 = 7$  were used earlier,<sup>35</sup> the same values are taken here. Since the co-ordination about the  $\text{Mn}^{2+}$  ion is octahedral,  $\overline{A}_4$  is obtained from the relation<sup>38</sup>

$$\overline{A}_4(R_0) = \frac{3}{4} Dq \quad (8)$$

From optical study,<sup>37</sup>  $Dq = 790 \text{ cm}^{-1}$ . Therefore,  $\overline{A}_4(R_0) = 592.5 \text{ cm}^{-1}$ . For  $3d^5$  ions the ratio  $\frac{\overline{A}_2}{\overline{A}_4}$  falls in the range 8–12.<sup>34,39,40</sup> With  $\overline{A}_2 = 10\overline{A}_4$ ,  $\overline{A}_2 = 5925 \text{ cm}^{-1}$ .

## 4. Results and discussion

Using SPM and the ligand configuration about the  $\text{Mn}^{2+}$  ion shown in Fig. 1, the CF parameters of the  $\text{Mn}^{2+}$  ion at the  $\text{Zn}^{2+}$  (1) sites are estimated. Table 1 provides atoms' coordinates in the ZKS single crystal with bond length  $R$  (both with and without distortion) and angles  $\theta$ ,  $\varphi$  for site I. The ZFS and CF parameters together with reference distance  $R_0$  are presented in Table 2. Table 2 shows that  $R_0 = 0.200 \text{ nm}$ , being slightly less than the sum of the radii of the ions ( $0.223 \text{ nm}$ ) of  $\text{Mn}^{2+} = 0.083 \text{ nm}$  and  $\text{O}^{2-} = 0.140 \text{ nm}$  with no distortion and  $\frac{\overline{A}_2}{\overline{A}_4} = 8, 10, 12$  provide ZFS parameter values at octahedral substitutional site I different from the EPR experimental ones.<sup>22</sup> Experimental parameters of ZFS  $|D|$  and  $|E|$  (in unit of  $10^{-4} \text{ cm}^{-1}$ ) for site I from EPR are 355.8, 57.2, respectively.  $|E|/|D|$  is obtained as 0.160 being smaller than the standard value 0.33.<sup>32</sup>  $|D|$  and  $|E|$  estimated theoretically without distortion are larger than the EPR experimental values. The value of  $|E|/|D|$  is also larger than the standard value 0.33.<sup>32</sup> Therefore, local distortion is included into the calculation. For local distortion an iterative procedure has been used by changing  $R$ ,  $\theta$  and  $\varphi$  to minimize the difference between calculated and experimental  $D$  and  $E$  and  $E/D$  near to

**Table 1** Atoms' coordinates, bond length  $R$  (both with and without distortion) and angles  $\theta$ ,  $\varphi$  in the ZKS single crystal (site I)

Mn <sup>2+</sup> position	Ligands	$x$ (Å)	$y$ (Å)	$z$ (Å)	Spherical polar coordinates of ligands					
					$R$ (nm)	$\theta^\circ$	$\varphi^\circ$			
Without distortion										
Site: substitutional	O7	0.1723	0.1080	0.1683	0.20741	$R_1$	85.34	$\theta_1$	85.22	$\varphi_1$
Zn(1)	O8	-0.1629	0.1113	0.0351	0.20598	$R_2$	89.02	$\theta_2$	94.53	$\varphi_2$
(0.0000, 0.0000, 0.0000)	O9	-0.0007	-0.0676	0.3024	0.20362	$R_3$	81.46	$\theta_3$	90.02	$\varphi_3$
	O7'	-0.1723	-0.1080	-0.1683	0.20741	$R_4$	94.65	$\theta_4$	94.78	$\varphi_4$
	O8'	-0.1723	0.3920	0.6683	0.67733	$R_5$	84.34	$\theta_5$	91.46	$\varphi_5$
	O9'	0.1723	0.6080	0.3317	0.77278	$R_6$	87.54	$\theta_6$	88.72	$\varphi_6$
With distortion										
I	O7				0.28741		66.34		86.72	
	O8				0.28598		70.02		92.53	
	O9				0.26007		62.46		88.02	
	O7'				0.30901		86.65		90.78	
	O8'				0.79733		82.34		91.46	
	O9'				0.85778		89.54		90.72	



Table 2 The Mn<sup>2+</sup> doped ZKS crystal's CF and ZFS parameters

Site	Crystal-field parameters (cm <sup>-1</sup> )						Zero-field splitting parameters (× 10 <sup>-4</sup> cm <sup>-1</sup> )		
	R <sub>0</sub> (nm)	B <sub>20</sub>	B <sub>22</sub>	B <sub>40</sub>	B <sub>42</sub>	B <sub>44</sub>	D	E	E / D
Without distortion site I									
$\frac{\overline{A_2}}{\overline{A_4}} = 8$	0.200	-17 062.3	-21 071.6	5249.723	5583.833	8072.755	3295.6	1679.4	0.509
$\frac{\overline{A_2}}{\overline{A_4}} = 10$	0.200	-21 327.9	-26 339.5	5249.723	5583.833	8072.755	4724.9	2421.1	0.512
$\frac{\overline{A_2}}{\overline{A_4}} = 12$	0.200	-25 593.5	-31 607.4	5249.723	5583.833	8072.755	6458.7	3314.3	0.513
With distortion site I									
$\frac{\overline{A_2}}{\overline{A_4}} = 8$	0.200	-5618.94	2495.683	-133.084	-19.7999	2948.929	285.2	75.7	0.265
$\frac{\overline{A_2}}{\overline{A_4}} = 10$	0.200	-7023.67	3119.604	-133.084	-19.7999	2948.929	355.8	109.3	0.307
Exp.							355.8	57.2	0.160
$\frac{\overline{A_2}}{\overline{A_4}} = 12$	0.200	-8428.4	3743.524	-133.084	-19.7999	2948.929	437.7	148.9	0.340

standard value 0.33<sup>32</sup> keeping in mind the minimum lattice strain. Using the above value of R<sub>0</sub> and local distortion, the ZFS parameters for substitutional octahedral sites I are determined for  $\frac{\overline{A_2}}{\overline{A_4}} = 8, 10, 12$  and are given in Table 2. The ZFS parameter values are smaller than the experimental ones (error 19.84%) for  $\frac{\overline{A_2}}{\overline{A_4}} = 8$  and larger for  $\frac{\overline{A_2}}{\overline{A_4}} = 12$  (error 23.02%, |E|/|D| is also larger than the standard value 0.33) while these are in good agreement with the EPR experimental values for  $\frac{\overline{A_2}}{\overline{A_4}} = 10$ .<sup>22</sup> Hence  $\frac{\overline{A_2}}{\overline{A_4}} = 10$  seems to be appropriate. The parameters t<sub>2</sub> = 3 and t<sub>4</sub> = 7 with transformation S2 for standardization<sup>32</sup> are employed to get an |E|/|D| ratio near to 0.33 and calculated ZFS parameters close to the experimental values from EPR. A similar value of  $\frac{\overline{A_2}}{\overline{A_4}}$  has been used for Mn<sup>2+</sup> doped diglycine calcium chloride tetrahydrate<sup>41</sup> and Fe<sup>3+</sup> doped BiVO<sub>4</sub>.<sup>34</sup>

The CFA program<sup>42</sup> and B<sub>kq</sub> parameters (with distortion) are used to calculate the optical spectra of Mn<sup>2+</sup> doped ZKS single crystals. By diagonalizing the full Hamiltonian, the positions of the energy bands of the Mn<sup>2+</sup> ion are evaluated. Table 3 shows the energy band positions (experimental and calculated) for substitutional site I.<sup>37</sup> From the position and the nature of the bands observed, they have been ascribed to a Mn<sup>2+</sup> ion in octahedral symmetry.<sup>37,43</sup> Ligand field bands are sharp when the energy expressions for the transitions are independent of Dq, since the number of t<sub>2g</sub> electrons is the same in both the excited and the ground states.<sup>43</sup> The sharp bands are therefore assigned to the [<sup>4</sup>A<sub>1g</sub>(G), <sup>4</sup>E<sub>g</sub>(G)] and the <sup>4</sup>E<sub>g</sub>(D) states, respectively. The broad bands are assigned to <sup>4</sup>T<sub>1g</sub>(G) and <sup>4</sup>T<sub>2g</sub>(G), respectively. These bands are broad as their transitions involve a change of configuration from (t<sub>2g</sub>)<sup>3</sup>(e<sub>g</sub>)<sup>2</sup> to (t<sub>2g</sub>)<sup>4</sup>(e<sub>g</sub>). The remaining bands are assigned to <sup>4</sup>T<sub>2g</sub>(G), <sup>4</sup>T<sub>1g</sub>(P) and <sup>4</sup>T<sub>1g</sub>(F) states, respectively. The CFA program<sup>42</sup> can perform diagonalization of the complete Hamiltonian within the 3d<sup>N</sup> basis of states in the intermediate

Table 3 Both calculated and experimental energy bands of the single crystal of ZKS doped Mn<sup>2+</sup>

Transition from <sup>6</sup> A <sub>1g</sub> (S)	Observed band (cm <sup>-1</sup> )	Calculated band (cm <sup>-1</sup> ) I
<sup>4</sup> T <sub>1g</sub> (G)	18 436	23 327, 23 343, 23 513, 23 592, 23 759, 23 843
<sup>4</sup> T <sub>2g</sub> (G)	22 815	23 979, 24 000, 24 363, 24 402, 24 445, 24 485
<sup>4</sup> E <sub>g</sub> (G)	24 783	24 828, 24 856, 24 865, 24 872
<sup>4</sup> A <sub>1g</sub> (G)	24 850	24 880, 24 889
<sup>4</sup> T <sub>2g</sub> (D)	28 003	26 582, 26 639, 27 214, 27 274, 28 565, 28 578
<sup>4</sup> E <sub>g</sub> (D)	29 870	29 249, 29 305, 29 730, 29 828
<sup>4</sup> T <sub>1g</sub> (P)	32 435	31 477, 31 502, 34 913, 35 045, 35 148, 35 264
<sup>4</sup> A <sub>2g</sub> (F)		36 656, 36 961
<sup>4</sup> T <sub>1g</sub> (F)	41 460	40 843, 40 559, 40 678, 40 730, 40 790, 40 799

crystal field coupling scheme providing not only the CF energy levels but also the state vectors. The Hamiltonian incorporated in the CFA program contains the Coulomb interaction (in terms of the Racah parameters B and C), Trees correction (α), the spin-orbit interaction (ζ), the crystal field Hamiltonian, the spin-spin interaction (M<sub>0</sub>), and the spin-other orbit interaction (two parameters: M<sub>00</sub>, M<sub>22</sub>). The adjusted values of the free-ion parameters used in the CFA calculations are (in cm<sup>-1</sup>): B = 850 and C = 2970, α = 76, ζ<sub>0</sub> = 336 cm<sup>-1</sup>, M<sub>0</sub> = 0.2917, M<sub>2</sub> = 0.0229, M<sub>00</sub> = 0.2917, and M<sub>22</sub> = 0.0229. Though the whole Mn<sup>2+</sup> spectra consist of 120 degenerate states, we present only a few energy levels based on intensity.<sup>44</sup> The transitions associated with <sup>4</sup>E<sub>g</sub>(G), <sup>4</sup>A<sub>1g</sub>(G), <sup>4</sup>T<sub>2g</sub>(D), <sup>4</sup>E<sub>g</sub>(D) and <sup>4</sup>A<sub>2g</sub>(F) are well predicted while the transitions associated with <sup>4</sup>T<sub>1g</sub>(G), <sup>4</sup>T<sub>2g</sub>(G), <sup>4</sup>T<sub>1g</sub>(P) and <sup>4</sup>T<sub>1g</sub>(F) show larger deviation. The reasons for these deviations may be electron correlation effects, vibronic coupling or limitations of the CF model.<sup>33</sup>

It is evident from Table 3 that the calculated and experimental energy band positions agree fairly well. Therefore, the theoretical results verify the EPR experimental one<sup>22,37</sup> that Mn<sup>2+</sup> ions enter the ZKS crystal at the substitutional Zn<sup>2+</sup> (1) octahedral site. The model parameters determined may be utilized in ZFS parameter estimations for Mn<sup>2+</sup> ions at similar molecular nanomagnet sites.



## 5. Conclusions

To determine the zero field splitting parameters, the superposition model and perturbation theory are utilized for ZKS single crystals infused with  $Mn^{2+}$  ions. The calculated ZFS parameters match well with the experimental values from EPR for  $\frac{\overline{A_2}}{\overline{A_4}} = 10$ . The computed optical spectra are discussed.

The calculated positions of the optical energy bands agree reasonably well with those obtained from the experiment. Thus, the experimental result is supported by the theoretical analysis that  $Mn^{2+}$  ions substitute at  $Zn^{2+}$  (1) sites in ZKS. The model parameters evaluated in this study may be utilized for ZFS parameter determinations for  $Mn^{2+}$  ions at similar sites in MNM. The present modeling technique may be useful in finding various crystals of a number of scientific and industrial applications.

## Ethical approval

There were no human or animal subjects in this study, and it wasn't conducted in any protected or private locations. Corresponding locations did not require any special permissions.

## Author contributions

Vikram Singh and Maroj Bharati prepared the figure, wrote the manuscript, and carried out the computations. Ram Kripal: concept and oversight. The manuscript has been reviewed by all authors.

## Conflicts of interest

The authors affirm that no known conflicting financial interests or personal relationships could have influenced any of the work presented in this paper.

## Data availability

Data will be made available on request.

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