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Design principles for 3D thermoelectric materials in power generators

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Thermoelectric power generation, which converts waste heat into electricity, represents a promising approach toward sustainable energy harvesting. While geometric regulation of thermoelectric materials has shown significant potential for enhancing device performance, existing theoretical and computational approaches typically rely on simplified, case-specific designs under constrained conditions. This limitation primarily stems from theoretical challenges in comprehensively understanding thermoelectric transport in three-dimensional (3D) materials in varied thermal environments. Here, we develop an analytical theoretical framework to rigorously examines power generation in 3D thermoelectric materials across diverse thermal boundary conditions. Based on this framework, we propose a universal geometric design principle to optimize 3D materials for maximum power generation and introduce a universal figure of merit that comprehensively integrates material properties, geometry, and boundary conditions. Experimental validation using optimized 3D-printed (Bi,Sb)₂Te₃ legs demonstrates significant enhancements in performance. This study establishes a robust theoretical foundation and practical design strategy, advancing thermoelectric energy harvesting beyond traditional material–property-based optimizations.

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Broader context

As the global transition toward sustainable energy systems accelerates, waste heat recovery is gaining attention as a practical and effective strategy. Thermoelectric generators, which directly convert heat into electrical energy, offer a promising solution for harvesting low-grade waste heat from sources such as industrial exhaust, automotive engines, and even the human body. However, despite decades of innovation in thermoelectric materials, rational device-level design remains challenging due to a lack of comprehensive understanding of how the geometry of 3D thermoelectric materials affects device performance under varied thermal environments. In this work, we establish a universal theoretical framework that systematically analyzes the relationship between geometry and thermoelectric performance across diverse boundary conditions. Based on this framework, we propose a universal design principle for optimizing thermoelectric leg geometry, along with a new figure of merit that integrates material properties, geometric factor, and boundary effects. Experimental validation using optimized 3D-printed (Bi,Sb)₂Te₃ legs confirms the effectiveness and generality of the proposed design approach, demonstrating up to a 466% improvement in efficiency. This study provides a broadly applicable and practical strategy for enhancing thermoelectric device performance, supporting global efforts in waste heat recovery across industrial, automotive, and wearable applications.

1. Introduction

Thermoelectric (TE) devices, which enable direct conversion between thermal and electrical energies, have gained substantial attention as eco-friendly and sustainable energy harvesters from waste heat, offering a promising solution to the global energy crisis and environmental challenges in energy production.¹ The

energy conversion efficiency of TE materials is evaluated using the figure of merit $ZT = S^2T/\rho\kappa$, where ρ is the electrical resistivity, S is the Seebeck coefficient, κ is the thermal conductivity, and T is the absolute temperature.² Accordingly, over the past two decades, researchers have focused on enhancing ZT through various strategies, including nanostructuring, band engineering, high-entropy alloying, and defect engineering.^{3–9} These approaches predominantly aim to optimize the intrinsic properties of materials by tuning the charge carrier concentrations, modifying the electronic structures, and increasing phonon scattering, thereby modulating both the electrical and thermal transport properties of the materials.^{10–12}

Beyond material-level ZT enhancement, geometric design has recently emerged as a promising extrinsic strategy for

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enhancing device-level performance. By tailoring the geometry of TE materials, effective and flexible regulation of electrical and thermal transport within the TE legs can be achieved, thereby improving the device performances and operational adaptability.^{13–23} Computational methodologies, such as finite element methods, computational fluid dynamics, and multi-physics coupling, have been utilized for predicting and optimizing the performance of TE generators (TEGs) through geometric adjustments in materials.^{24,25} However, existing computational approaches are largely constrained to specific case studies, typically relying on predefined two- or three-dimensional (2D or 3D) geometries such as trapezoidal or hourglass shapes, and arbitrary thermal conditions, predominantly fixed T boundaries. Consequently, the resulting designs often exhibit irregular, case-specific characteristics without clear, generalizable trends—thereby hindering the development of broader insights into optimal geometric designs.

More fundamentally, the theoretical understanding of geometry-driven performance enhancement remains unclear. Conventional TE theories are primarily based on 1D thermal and electrical transport under fixed T boundary conditions.^{26–29} Although this simplified theory has successfully guided the optimization of material properties in conventional 1D cuboidal TE materials, they often fail to capture the complex interplay between thermal and electrical transport within 3D TE materials subjected to dynamic thermal environments. To fully leverage the potential of geometric design for TE performance enhancement, two critical questions must be addressed: (1) How does TE leg 3D geometry fundamentally influence the TE transport under diverse thermal boundary conditions? (2) What is the universally applicable design principle for an optimal design?

Here, we answer the above questions by establishing a theoretical framework that systematically analyzes the power generation in 3D TE materials across diverse thermal boundary conditions. We developed theoretical models for 3D TE systems under eight operating conditions, incorporating combinations of the Dirichlet, Neumann, and Robin boundary conditions. Based on this framework, we introduce a geometric factor (G factor) as a universal parameter to guide the optimization of the TE leg design. Moreover, we propose a universal figure of merit incorporating the geometric effect to predict the power generation performances. We fabricated $(\text{Bi,Sb})_2\text{Te}_3$ -based legs with optimized geometries using 3D printing and validated our design principles in various thermal environments. The optimized 3D geometry demonstrated a 466% increase in TE conversion efficiency compared to the conventional 1D cylinder, while utilizing 67% less TE materials. The proposed framework offers a comprehensive guide for optimizing the TE leg geometry as a practical and broadly applicable strategy, offering new directions for advancing device-level TE performance.

2. Results and discussion

2.1 Thermal boundary conditions

The operation of a TEG is governed by thermal boundary conditions classified into three categories: Dirichlet (fixed T),

Neumann (fixed heat flux), and Robin (convective heat transfer) (Fig. 1a).³⁰ The Dirichlet conditions are satisfied when the heat source or sink functions as a thermal reservoir, ensuring a fixed boundary T irrespective of the heat transfer dynamics. At $x = 0$, the T of a TEG is the boundary T , denoted as T_b and described as eqn (1)

$$T_b = T_{x=0}. \quad (1)$$

The Neumann conditions impose a constraint on the heat flux at the boundary, specifying the T gradient rather than the T itself. This condition appears most commonly in heat sources such as radioisotopes, combustion engines, and solar thermal absorbers, which provide a steady energy input.^{31–33} The heat flux condition at the boundary is given by eqn (2)

$$Q_b = -\kappa \frac{dT}{dx} \Big|_{x=0} + SJT_{x=0}, \quad (2)$$

where Q_b is the heat flux at the boundary surface, J is the current density, and dT/dx is the T gradient. The second term of $SJT_{x=0}$ indicates the Peltier heat.

The Robin conditions describe the convective heat transfer based on Newton's law of cooling, which is commonly observed in air- or liquid-cooled TEGs.³⁴ This condition defines the relationship between the surface T and its gradient, ensuring a balance between conduction and convective heat transfer, expressed as eqn (3)

$$h(T_{\text{fluid}} - T_{x=0}) = -\kappa \frac{dT}{dx} \Big|_{x=0} + SJT_{x=0}, \quad (3)$$

where h is the heat transfer coefficient of the fluid and T_{fluid} is the free-stream fluid T .

Applying these conditions to both the heat source and sink leads to nine thermal boundary combinations. The Neumann–Neumann case was excluded in this study because specifying heat fluxes at both boundaries fixes the net heat flow ($Q_h - Q_c$) and thus, by energy conservation, predefines the TEG power ($P = Q_h - Q_c$), leaving no degrees of freedom for performance analysis. Consequently, eight feasible boundary configurations were used to comprehensively represent the thermal environments of the TEG across diverse real-world applications. Under these conditions, we analytically computed the resulting difference in T (ΔT), P , and efficiency (η) by establishing the energy balance equations (SI1–SI9). A constant property model (CPM) was used for a simple evaluation of the TEG performance.²⁶ The validity of the CPM within our theoretical framework was confirmed through comparison with the temperature-dependent material model (TPM) (Fig. S1). Both models demonstrated nearly identical energy conversion efficiencies across a diverse range of materials within the device. Further details are provided in SI10.

2.2 Theoretical framework for 3D geometry

To investigate the effect of the TE leg geometry on the device performance, we analyzed the heat and charge transport within the TE leg in a closed circuit with a load resistance (R_L). We established a 3D symmetric model with a parabolic cross-sectional variation along the TE length (L) (Fig. 1b and SI11).



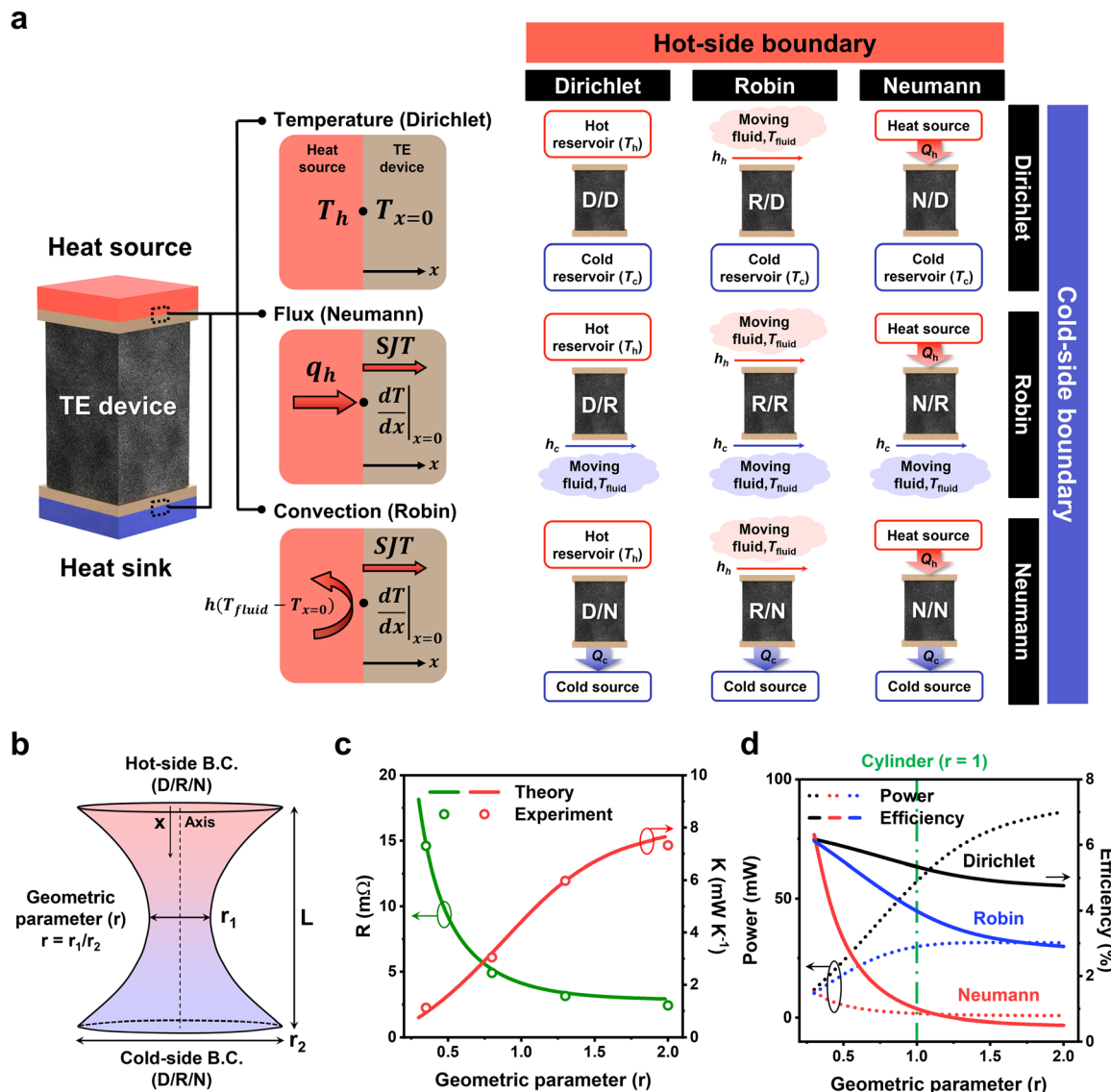


Fig. 1 Theoretical modeling of TE leg geometry under diverse boundary conditions. (a) Schematic of the thermal boundary conditions (Dirichlet, Neumann, and Robin) and feasible boundary configurations of the TEG operating system. (b) 3D symmetric model of the TE leg with a parabolic cross-sectional variation. The bottom-to-central radius ratio (r) determines the shape ($r = 0.3-2$). (c) Comparison between theoretical and experimental trends of K and R of a 3D-printed $(\text{Bi,Sb})_2\text{Te}_3$ material. (d) Theoretical analyses of variations in P and η with r under diverse boundary conditions ($T_h = 475 \text{ K}$ & $T_c = 300 \text{ K}$, $Q_h = 4750 \text{ W m}^{-2}$ & $T_c = 300 \text{ K}$, $h_h = 250 \text{ W m}^{-2} \text{ K}^{-1}$ & $T_{\text{fluid}} = 475 \text{ K}$ & $T_c = 300 \text{ K}$) using a $(\text{Bi,Sb})_2\text{Te}_3$ CPM with $\rho_c = 2.3 \times 10^{-8} \Omega \text{ m}^2$, bottom and top areas of $36 \times 10^{-6} \text{ m}^2$, and a height of $6 \times 10^{-3} \text{ m}$. B.C.: Boundary condition.

This model has identical top and bottom surface areas at the TE leg and electrodes, which can prevent the influences of the surface areas, such as the convection area and heat flux area, and contact resistance (R_c) on the power performance. The geometric parameter (r), defined as the ratio of the central radius (r_1) to the bottom radius (r_2) ($r = r_1/r_2$), is utilized as the design variable in this model. When $r = 1$, the geometry corresponds to that of the conventional cylindrical model. Concave and convex shapes have $r < 1$ and $r > 1$, respectively.

P and η of a TEG under Dirichlet, Neumann, and Robin conditions are derived from the heat flow and P equations (Table S1). These equations show that P and η of the TEG are strongly dependent on the variables, thermal conductance (K)

and electrical resistance (R), which are inherently determined by the leg geometry.

In a conventional cuboidal or cylindrical model, K and R are given by $K = \kappa A/L$ and $R = \rho L/A$, respectively, which are valid only for structures with uniform cross sections. For 3D structures with varying cross sections, these properties are determined through integration over infinitesimal elements³⁵ (4):

$$K = \kappa \cdot \left(\int_0^L \frac{dx}{A(x)} \right)^{-1} \text{ and } R = \rho \cdot \int_0^L \frac{dx}{A(x)} \quad (4)$$

where $A(x)$ denotes the cross-sectional area at position x . These equations assume flat equipotential surfaces, where heat and



charge transport occur in the x direction.³⁵ However, in practice, the flow lines deviate from the ideal straight paths, leading to distortions in the equipotential surfaces.^{35,36} To account for this deviation, we introduce a correction factor β , which accounts for the reduction in the effective equipotential surface area (Fig. S2 and S112). This correction improves the accuracy of analytical performance prediction by properly incorporating the geometric influence on the transport properties (Fig. S3). To simplify the equations, we further reduced the equations to $K = \kappa/R_g$ and $R = \rho R_g$ by defining the geometric resistance (R_g) (5):

$$R_g = \beta \int_0^L \frac{dx}{A(x)} \quad (5)$$

Moreover, considering the R_c between the TE leg and electrodes, the total resistance of the TEG is expressed as $R = \rho R_g + R_c$, where $R_c = 2\rho_c/A$, with ρ_c representing the electrical contact resistivity. Because the thermal contact resistance can be modelled *via* the Robin boundary condition, it is not included in the TEG's K .

As expected, both K and R exhibit strong dependencies on the geometry as r varies, a trend further validated by the experimental measurements with 3D-printed $(\text{Bi,Sb})_2\text{Te}_3$ (Fig. 1c). To investigate the influence of the variations in K and R on η and P , we conducted a theoretical analysis and formulated their relationships under eight boundary conditions (Tables S1, S2 and Fig. S4–S11). Here, we illustrate three representative cases with the hot-side boundary conditions set to the Dirichlet, Neumann, and Robin conditions, whereas the cold-side follows the Dirichlet condition.

Under the Dirichlet–Dirichlet condition, P and η are proportional to $1/R$ and $1/(RK)$, respectively. The parameter RK represents the ratio between thermal and electrical transport in the TE leg, where a smaller RK indicates a more efficient TE effect. In the absence of R_c , RK converges to the intrinsic material property ($\rho\kappa$), making η independent of the geometry (Fig. S12). However, in practical TEG modules, R_c is inevitable at the metal–semiconductor junction,^{37,38} making RK dependent on both the material properties and geometry.

To quantitatively evaluate how variations in R_c affect the optimal geometry and the resulting thermoelectric performance (P and η), we conducted a comprehensive parametric analysis under eight boundary conditions (provided in Fig. S13 and S14). The results show that, irrespective of the geometry, lowering ρ_c consistently enhances both P and η , indicating the importance of minimizing R_c in all cases. At the same time, changes in ρ_c influence geometry, since ρ_c alters the total R , which consequently shifts the optimal geometric resistance. Importantly, while the degree to which geometric optimization contributes to performance improvements varies, the geometric designs consistently enhance the power-generating performances.

Consequently, geometric variations affect both P and η : decreasing R enhances P but degrades η . Under the Neumann–Dirichlet condition, P and η scale as $1/(RK^2)$, emphasizing the importance of minimizing K for enhancing performance, regardless of R_c . Accordingly, the optimal geometry is determined by K to maximize ΔT . To prevent divergence in ΔT , we constrain it

within the TEG's stable T range. Under the Robin–Dirichlet system, P follows $1/R \cdot 1/(K(1 + ZT')/hA + 1)^2$, whereas η scales as $1/(RK) \cdot 1/(K(1 + ZT') + hA)$. P is maximized when the thermal resistance of the fluid matches that of the TE leg, ensuring optimal heat and charge transfer. In contrast, η improves as K decreases, without a single optimal point. Owing to this diverse interplay between the geometry and TE performance, P and η exhibit distinct dependencies on r under each boundary condition (Fig. 1d and Fig. S15). Thus, in practical applications involving diverse boundary conditions, geometric effects are critical, necessitating tailored design strategies to optimize P and η .

2.3 Design principle for optimal 3D geometry

Based on the theoretical framework, we developed a systematic design principle to guide the 3D geometry design for maximizing P and η under eight different boundary conditions. Fig. 2 shows the systematic flowchart illustrating the overall design process. The first step for design is to establish an initial geometric model, typically, in a cuboidal or cylindrical shape. Next, the thermal boundary conditions of the initial model are specified, considering the Dirichlet, Neumann, or Robin boundary condition at both the hot- and cold-sides. Following this, the primary optimization objective is defined, that is, whether to maximize P and η , as each objective results in a different optimal geometry. Based on these predefined parameters, the G factor is calculated using the formulations provided in Table 1. The G factor, proposed in this study, is a dimensionless metric for evaluating the geometric optimality of the TE leg. It is defined as the ratio of R_g between the initial and optimized designs, as shown in eqn (6):

$$G = \frac{R_g^{\text{initial}}}{R_g^{\text{optimal}}} \quad (6)$$

The G factor is a quantitative measurement of the deviation from the optimal design, thus serving as a critical guide in the design process. A detailed methodology for determining R_g^{optimal} is provided in the SI Notes.

Geometric optimization becomes necessary if the G factor deviates from unity, specifically falling below 0.9 or exceeding 1.1. In such cases, the optimal geometric parameter (r_{opt}) can be identified using the G factor – optimal geometry (GO) plot, which depicts the relationship between the G factor and r_{opt} , thereby enabling engineers to determine the optimal value without complex calculations (Fig. 2, Table S3 and S113). However, if manufacturing constraints limit the feasibility of a 3D design, alternative GO plots for a 2.5D model, which can be realized using conventional manufacturing techniques such as dicing, pressing and molding, are available^{39–42} (Fig. S16).

The symmetric model presented in this design principle is a simplified case used solely to facilitate the analytical derivation of the G factor in 3D TE materials. The theoretical framework and design principle themselves are not limited to convex or concave geometries with parabolic profiles and do not limit the ranges of r . Importantly, R_g serves as a physical descriptor that captures the relative resistances of thermal and electrical



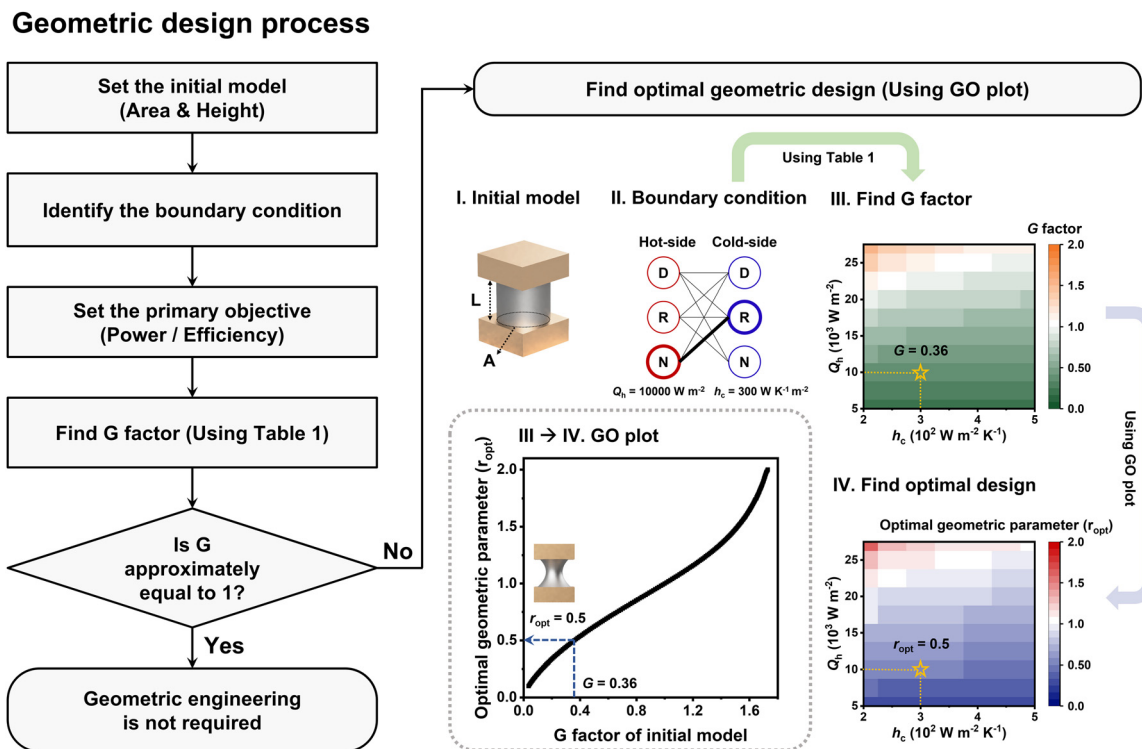


Fig. 2 Geometric design principle of a TE leg. Systematic flowchart illustrating the overall design process.

transport paths in arbitrary 3D geometries. Our design principle is thus generalizable: any geometries of 3D TE materials can be analyzed within our framework by calculating their corresponding R_g and G factor. To further demonstrate this generalizability, we extended our model to include multi-radius geometries, in which multiple radii along the leg are independently defined and integrated into a higher-order area function $A(x)$ (Fig. S17). For instance, materials with differing 3D geometries but identical R_g values are predicted to yield equivalent power generation performance, as validated by numerical simulations (Fig. S18 and Table S4).

2.4 Experimental validation of design principles

We validated our design principles by comparing theoretically computed performances with the experimentally measured values using the fabricated single-leg devices across four distinct boundary conditions: (1) Dirichlet–Dirichlet (T_h & T_c), (2) Neumann–Dirichlet (Q_h & T_c), (3) Neumann–Robin (Q_h & h_c), and (4) Dirichlet–Robin (T_h & h_c) on the hot- and cold-sides. These conditions were chosen considering real-world applications, including an industrial TEG with thermal reservoirs (T_h & T_c), a solar TEG utilizing constant heat from an absorber and cooled by a coolant (Q_h & T_c), an automotive TEG harnessing continuous heat from the vehicle exhaust and dissipating it *via* a heat sink (Q_h & h_c), and a wearable TEG operating at a constant body T with air cooling (T_h & h_c).^{43–47} The optimized TE legs were fabricated *via* a high-precision 3D-printing process using (Bi,Sb)₂Te₃-based TE ink, and subsequently integrated into a TE device sandwiched with Cu plate electrodes by

soldering (Fig. 3a and Fig. S19–S22).^{14,48–50} Fracture surface scanning electron microscopy (SEM) analysis and measurements of κ reveal that the printed samples exhibited uniform microstructures and thermal properties across varying in-plane printing patterns (Fig. S23 and S24). Furthermore, directional heat flow measurements along the x , y , and z directions for the 3D-printed sample clearly confirm the isotropic nature of their thermal properties independent of the printing direction (Fig. S25).

We comparatively analyzed the initial model (cylinder) and optimized geometry (Fig. S26). Across all boundary conditions, the measured I , V , P and η trends show excellent agreement with the theoretical predictions, with minor discrepancies (Fig. S27–S43). The deviations were primarily attributed to T -dependent variations in the TE properties, as the theoretical models are based on the CPM model.⁵¹ Under the Dirichlet–Dirichlet condition (Fig. 3b), the optimal geometries for maximization of P and η were found to be convex and concave geometries, respectively (Fig. 3c and d). The optimized geometry achieved a P of 40.4 mW and η of 4.68% at $\Delta T = 125$ K, which were 59.4% and 28.1% higher than those of the cylindrical model, respectively (Fig. 3e). The power enhancement resulted from the minimization of R due to the wider cross-sectional area of the optimal geometry, whereas the η gain was attributed to a larger R in the narrower cross-section. In the Neumann–Dirichlet condition (Fig. 3f), the concave geometry was optimal for both P and η (Fig. 3g and h). The greatest performance enhancement was observed at $Q_h = 3500 \text{ W m}^{-2}$, where the optimized geometry produced 5.91 mW P and 4.56% η ,





Table 1 G factor and universal figure of merit. This table lists the equations used to determine the G factor for P and η under eight boundary conditions. The G values 1.73 and 0.17 represent the maximum and minimum within the designable range in our 3D model. Similarly, these values can be interpreted as the G factor limits when applied to other design models. The G factor is calculated using several parameters, including L (initial model height, m), q'' (heat flux, $W m^{-2}$), h (heat transfer coefficient, $W m^{-2} K^{-1}$), κ (thermal conductivity of the TE material, $W m^{-1} K^{-1}$), ρ (electrical resistivity of the TE material, Ωm), ρ_c (electrical contact resistivity, K^{-1}), and Z_c (TEG efficiency index, K^{-1}), which is defined as $\frac{S^2}{RK}$. The table also includes T_p , T_{max} , and T^* with the unit of K. T_c^{min} and T_p^{max} represent the operational T limits of the TEGs. m is approximately calculated as $\sqrt{1 + Z_c \frac{T_{max}}{2}}$. The precise equations are listed in Table S2. This table also provides the equation for the universal figure of merit, which is calculated using G_p

Boundary condition (H/C)	G factor for P , G_p	G factor for η , G_η	T_p (K)	T_{max} (K)	T^* (K)	Universal figure of merit ($Z_c T_{max}$)
Dirichlet/Dirichlet	$\begin{cases} 1 & \text{if } \frac{\rho_c}{L\rho} < 4 \\ 1.73 & \text{if } \frac{\rho_c}{L\rho} \geq 4 \end{cases}$	$\begin{cases} 1 & \text{if } \frac{\rho_c}{L\rho} < 0.005 \\ 0.17 & \text{if } \frac{\rho_c}{L\rho} \geq 0.005 \end{cases}$	—	$T_h - T_c$	—	$Z_c T_{max}$
Dirichlet/Robin	$\frac{2Lh}{\kappa(1 + Z_c T^*)}$ $1 + \sqrt{1 + 16 \frac{h}{\kappa(1 + Z_c T^*)} \frac{\rho_c}{\rho}}$	0.17 (this model) lower limit of design constraints $\frac{\kappa \rho J_{max}}{1 + \sqrt{1 + 16 \frac{h}{\kappa} \frac{\rho_c}{\rho} J_{max}}}$	$1 + \sqrt{1 + 16 \frac{h}{\kappa} \frac{\rho_c}{\rho} J_{max}}$ $3 + \sqrt{1 + 16 \frac{h}{\kappa} \frac{\rho_c}{\rho} J_{max}}$	$T_h - T_{fluid}$	$\frac{T_h - T_p}{(m+1)} + \frac{T_p}{2(m+1)^2}$	$\frac{G_p - Z_c T_{max}}{1 + G_p}$
Dirichlet/Neumann	$\frac{L}{1 + Z_c T^* \kappa T_{max}}$	$\frac{L}{1 + Z_c T^* \kappa T_{max}}$	—	$T_h - T_c^{min}$	$\frac{T_c^{min}}{(m+1)} + \frac{T_{max}}{2(m+1)^2}$	$G_p Z_c T_{max}$
Robin/Dirichlet	$\frac{2Lh}{\kappa(1 + Z_c T^*)}$ $1 + \sqrt{1 + 16 \frac{h}{\kappa(1 + Z_c T^*)} \frac{\rho_c}{\rho}}$	0.17 (this model) lower limit of design constraints $\frac{\kappa \rho J_{max}}{1 + \sqrt{1 + 16 \frac{h}{\kappa} \frac{\rho_c}{\rho} J_{max}}}$	$1 + \sqrt{1 + 16 \frac{h}{\kappa} \frac{\rho_c}{\rho} J_{max}}$ $3 + \sqrt{1 + 16 \frac{h}{\kappa} \frac{\rho_c}{\rho} J_{max}}$	$T_{fluid} - T_c$	$\frac{T_p + T_c}{(m+1)} - \frac{T_p}{2(m+1)^2}$	$\frac{G_p - Z_c T_{max}}{1 + G_p}$
Robin/Robin	$\frac{L}{1 + Z_c T^* \kappa \left(\frac{1}{h_h} + \frac{1}{h_c} \right)}$ $1 + \sqrt{1 + \frac{16}{\kappa \left(\frac{1}{h_h} + \frac{1}{h_c} \right)} \frac{\rho_c}{\rho}}$	0.17 (this model) lower limit of design constraints $\frac{\kappa \rho J_{max}}{1 + \sqrt{1 + 16 \frac{h}{\kappa} \frac{\rho_c}{\rho} J_{max}}}$	$1 + \sqrt{1 + 16 \frac{h}{\kappa} \frac{\rho_c}{\rho} J_{max}}$ $3 + \sqrt{1 + 16 \frac{h}{\kappa} \frac{\rho_c}{\rho} J_{max}}$	$T_{h,fluid} - T_{c,fluid}$	$T_{h,fluid} - (T_{max} - T_p) \frac{h_c}{h_h + h_c} - \frac{T_p}{2(m+1)^2}$	$\frac{G_p - Z_c T_{max}}{1 + G_p}$
Robin/Neumann	$\frac{L}{1 + Z_c T^* \kappa T_{max}}$	$\frac{L}{1 + Z_c T^* \kappa T_{max}}$	—	$T_{fluid} - T_c^{min} - \frac{q''}{h}$	$\frac{T_c^{min}}{(m+1)} + \frac{T_{max}}{2(m+1)^2}$	$G_p Z_c T_{max}$
Neumann/Dirichlet	$\frac{L}{1 + Z_c T^* \kappa T_{max}}$	$\frac{L}{1 + Z_c T^* \kappa T_{max}}$	—	$T_h^{max} - T_c$	$\frac{T_h^{max}}{(m+1)} - \frac{T_{max}}{2(m+1)^2}$	$G_p Z_c T_{max}$
Neumann/Robin	$\frac{L}{1 + Z_c T^* \kappa T_{max}}$	$\frac{L}{1 + Z_c T^* \kappa T_{max}}$	—	$T_h^{max} - T_{fluid} - \frac{q''}{h}$	$\frac{T_h^{max}}{(m+1)} - \frac{T_{max}}{2(m+1)^2}$	$G_p Z_c T_{max}$

representing improvements of 422% and 466%, respectively, over the cylindrical model (Fig. 3i). These enhancements were achieved by minimizing K , thereby maximizing ΔT within the operable T range. When evaluated at the same T_h , concave geometries will exhibit a lower P due to its higher R (Fig. S44). However, the enhancement of η was consistently observed in the concave optimal geometry, implying that the geometry with smaller K requires less Q_h for creating the same ΔT than the cylinder (Fig. S45). Interestingly, with increasing Q_h , the

optimal geometry became gradually thicker and cylindrical, resulting in reduced performance enhancements. This result can be understood by considering the changes in Q_h under the Neumann condition, where the increase in Q_h increases T_h to bring it close to the limit T of 475 K in our model, regardless of the geometry.

A similar trend was observed for the Neumann–Robin condition (Fig. 3j). The greatest performance enhancement was observed at $Q_h = 4750 \text{ W m}^{-2}$, with a measured P of 11.0 mW

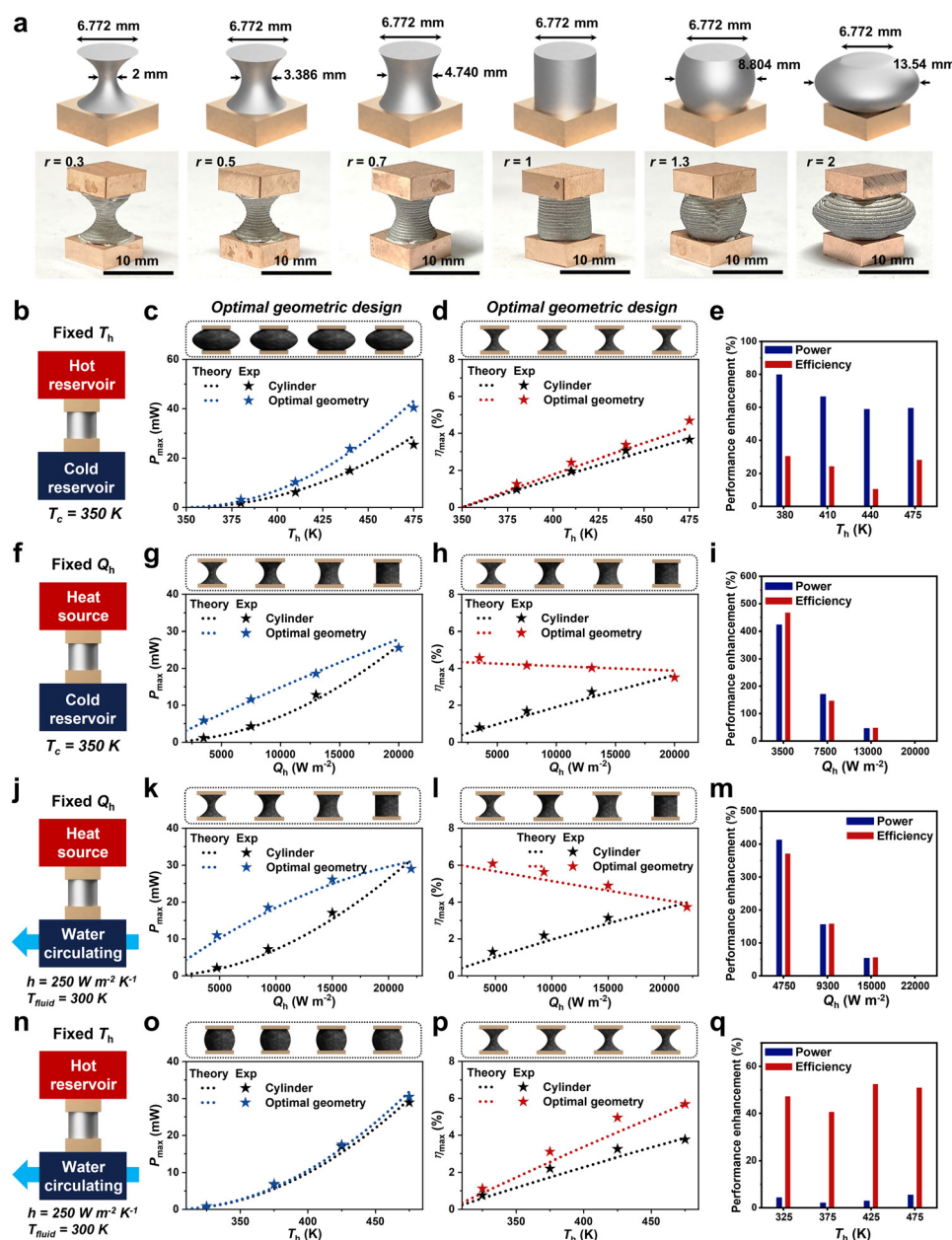


Fig. 3 Power generation performances of optimized 3D geometries and cylinders. (a) 3D models and photographs of TEGs with optimized geometries, fabricated *via* 3D printing. Results for (b)–(e) Dirichlet–Dirichlet boundary system, (f)–(i) Neumann–Dirichlet boundary system, (j)–(m) Neumann–Robin boundary system, and (n)–(q) Dirichlet–Robin boundary system. (b), (f), (j) and (n) Schematic of the setup, (c), (g), (k) and (o) P_{\max} and (d), (h), (l) and (p) η_{\max} as functions of the hot-side boundary condition for cylindrical and optimized TEGs. (e), (i), (m) and (q) Bar graphs showing the performance enhancement of the optimized 3D geometries relative to the cylinder. The device images positioned above each performance graph represent the optimal geometry corresponding to each data point. The points and dashed lines in the graphs correspond to the measured and theoretically predicted data, respectively.



(Fig. 3k) and η of 6.08% (Fig. 3l) for the optimized geometry, representing improvements of 412% and 370% over the results of the cylindrical model (Fig. 3m). In both conditions, geometry engineering is more efficient under a low heat flow. The high heat flow in both the Neumann and Robin conditions results in thermal boundary conditions approaching the limit T , behaving like the Dirichlet condition. Under the Dirichlet–Robin condition (Fig. 3n), the optimized geometries demonstrated average enhancements of 3.6% in P and 47% in η when compared with the results of the cylindrical model (Fig. 3o–q). Although the improvement in P is minimal, the η gain from an increased ΔT due to the reduction in K is significant. These experimental results validate our proposed design principle across diverse boundary conditions.

To further analyze the results, we plotted the measured I_{opt} and output voltage (V_{cc}) (I and V at the maximum efficiency) versus hot-side temperature (T_{h}) or input heat flux (Q_{h}). Geometric modulation by lowering r reduces I_{opt} under Dirichlet/Dirichlet and Dirichlet/Robin boundary conditions (Fig. S30 and S33). In the meantime, V_{cc} values are maintained under the Dirichlet/Dirichlet condition due to the fixed ΔT , and are slightly enhanced with lowering r under the Dirichlet/Robin condition by the enhanced ΔT . In contrast, we observed that the I_{opt} was slightly enhanced with lowering r under Neumann/Dirichlet and Neumann/Robin conditions (Fig. S36 and S40). In Neumann-type systems, the increase in ΔT resulting from geometric modulation (lowering r) more than compensates for the rise in R —particularly when R_{c} is non-negligible. As a result, I_{opt} slightly increases with decreasing r . Similarly, V_{cc} exhibits a more pronounced increase with decreasing r compared to the Dirichlet/Robin condition, due to the stronger enhancement in ΔT under fixed heat flux boundaries.

For evaluating the optimal device durability, we conducted accelerated lifetime and thermal cycling tests. Under a representative Neumann–Robin boundary condition ($Q_{\text{h}} = 4000 \text{ W m}^{-2}$, $h = 250 \text{ W m}^{-2} \text{ K}^{-1}$) and a continuous current of 0.43 A, the device was tested over 170 hours, showing <5% degradation in output and maintaining a stable η of $\sim 5.5\%$ (Fig. S46). In thermal cycling tests with 100 rapid heating–cooling cycles (458–308 K), the device resistance and voltage remained stable within a 5% variation (Fig. S47). These results confirm that our optimized geometry, despite its non-uniform profile, maintains high thermoelectric performance and robustness under realistic operating conditions.

Furthermore, to verify the universality of our framework beyond a specific material system, we conducted an independent validation using PbTe-based devices.¹⁷ The performance trends observed in these PbTe devices showed strong agreement with theoretical predictions, confirming that our geometric optimization principle is applicable across different thermoelectric materials (Fig. S48–S53).

2.5 Universal figure of merit

The TEG performance is typically evaluated using several figures of merit, such as ZT_{mid} , $Z_{\text{eff}}T_{\text{mid}}$, $[ZT]_{\text{eng}}$, $Z_{\text{gen}}T_{\text{mid}}$, and $[ZT]_{\text{mod}}$, which serve as reliable criteria for the design and optimization

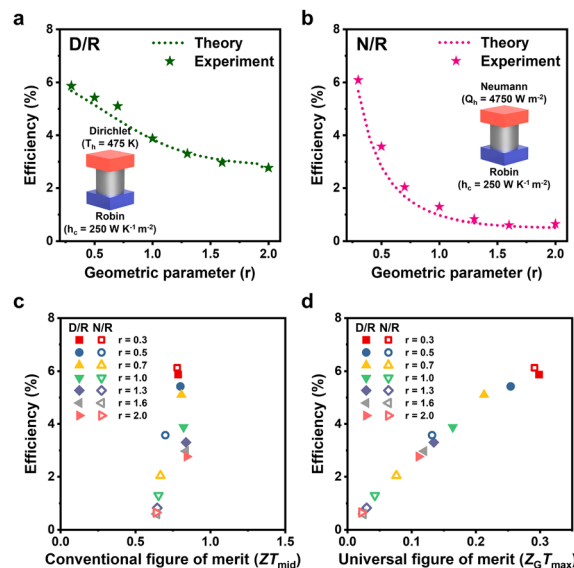


Fig. 4 Universal figure of merit incorporating geometric effects. (a) and (b) η_{max} as a function of r under (a) the Dirichlet–Robin boundary system and (b) the Neumann–Robin boundary system for seven different geometries ($r = 0.3$ – 2). (c) and (d) Plots of η_{max} versus (c) the conventional figure of merit (ZT_{mid}) and (d) the universal figure of merit ($Z_{\text{G}}T_{\text{max}}$).

of TE materials.^{26–29} However, these figures of merit assume a fixed ΔT (Dirichlet–Dirichlet condition), thereby restricting the practical evaluation of the TEG under the real-world environment. To address this limitation, we propose a new universal figure of merit ($Z_{\text{G}}T_{\text{max}}$) that comprehensively integrates intrinsic material properties, 3D geometry, and boundary conditions with the G factor (Table 1). When either the hot- or cold-side is under the Neumann or Robin condition, $Z_{\text{G}}T_{\text{max}}$ is given by $ZT_{\text{max}} \times G_{\text{p}}$ or $ZT_{\text{max}} \times G_{\text{p}}/(G_{\text{p}} + 1)$, respectively, where T_{max} represents the available maximum ΔT in the system. All these metrics are formulated using the G factor, which not only serves as a guide for 3D design but also plays a crucial role in integrating the geometric effects into the figure of merit.

To validate the effectiveness of the newly proposed $Z_{\text{G}}T_{\text{max}}$, we compared η trends with the conventional figure of merit (ZT_{mid}) across seven different geometries ($r = 0.3$ – 2) under the Neumann and Robin conditions (Fig. 4a, b and Fig. S42, S43). The results show that the conventional figure of merit, ZT_{mid} , does not maintain a proportional relationship with η (Fig. 4c). In contrast, $Z_{\text{G}}T_{\text{max}}$ exhibits a clear linear correlation with η , despite variations in geometry and boundary conditions (Fig. 4d), confirming its reliability for predicting TEG performance. Consequently, this metric can serve as a robust indicator for optimizing TEG design in practical applications.

3. Conclusions

We developed a comprehensive theoretical framework for designing the 3D TE materials in TEGs under diverse boundary conditions. By establishing theoretical models for the TE performance across eight distinct boundary systems, we proposed a universal



design principle, utilizing the G factor as a guiding parameter, to optimize the TE leg 3D geometry for enhanced performance. The validity of this design strategy was experimentally confirmed through 3D printing-based fabrication and performance evaluation of TE devices, demonstrating significant performance improvements across multiple boundary conditions. Additionally, we introduced universal figures of merit for 3D TE materials, integrating all critical parameters influencing device performance, enabling convenient and accurate predictions of power generation efficiency. Our proposed strategy offers a comprehensive design guide for maximizing the TEG power generation at the device level without relying on improvements in the material properties, thereby extending beyond conventional ZT -based optimization. Moreover, the integration of theoretical modelling and experimental validation advances the fundamental understanding of electrical and thermal transport in 3D TE materials. The demonstrated enhancement in power generation across diverse boundary conditions—representative of real-world operating environments—broadens the practical applicability of TE power generation technologies, accelerating their adoption in everyday applications. Moreover, most optimal designs correspond to high R_g (*i.e.*, small r), which significantly reduces material usage while achieving high thermoelectric performance—resulting in a highly efficient use of materials. Meanwhile, the current theoretical framework was developed under the assumption of isotropic thermoelectric behavior, but it can be extended to anisotropic systems in future studies. In particular, materials composed of inherently one-dimensional or two-dimensional building blocks,⁵² which exhibit directional transport characteristics, may offer potential to further improve thermoelectric performances of devices by tailored design strategies based on their anisotropic thermoelectric properties.

4. Methods

4.1 Materials

High-purity granules (99.999%) of bismuth (Bi), antimony (Sb), and tellurium (Te) were obtained from 5 N Plus. Ethanethiol (>97%), ethylenediamine (>99.5%), acetonitrile (>99.8%), and glycerol (>99.5%) were supplied by Aldrich. All substances were used in their original state without further treatment.

4.2 Synthesis of (Bi,Sb)₂Te₃-based TE particles

High-energy ball milling was employed to prepare Bi_{0.55}Sb_{1.45}Te₃ TE powders. A zirconia milling jar (80 mL) was loaded with 5 mm zirconia grinding balls, with a fixed ball-to-powder weight ratio of 5:1 (Fritsch Monomill, Pulverisette, Germany). The alloying process was performed at a rotational speed of 450 rpm for 11 hours. To ensure uniform particle distribution, agglomerates were removed by sieving to a size of <45 μm.

4.3 Formulation of all-inorganic (Bi,Sb)₂Te₃-based ink

To synthesize Sb₂Te₄²⁻ ChaM, 0.32 g of Sb powder and 0.64 g of Te powder were dissolved in a co-solvent comprising 2 mL of ethanethiol and 8 mL of ethylenediamine at room temperature

inside a nitrogen-purged glove box. The solution was stirred for more than 24 hours until complete dissolution. Acetonitrile was introduced as an anti-solvent at an 8:1 volume ratio, followed by centrifugation at 10 000 rpm for 10 minutes to precipitate the precursor. The precipitate was subsequently dried under vacuum for 1 hour to obtain Sb₂Te₄²⁻ ChaM powder. A mixture of 10 g of TE powder and 2.5 g of ChaM was then dispersed in 10 g of glycerol, followed by mixing in a planetary centrifugal mixer (ARM-100, Thinky) for 2 hours to ensure thorough homogenization.

4.4 3D printing and sintering process of (Bi,Sb)₂Te₃ samples

A custom-designed extrusion-based 3D printer with programmable air pressure and temperature control was employed for the printing process. The prepared ink was loaded into a 5 ml syringe (Saejong), which was equipped with a metal nozzle featuring an inner diameter of 520 μm. A graphite substrate with a thickness of 3 mm was used as the substrate for printing. The printing path was generated using design software, with a circular pattern programmed for deposition. To prevent uneven material distribution in a single direction, successive layers were stacked in an alternating crosswise orientation. The printing procedure was conducted at room temperature, with a 1-second pause between each layer deposition. The printed structure was then dried at 423 K for 24 hours before undergoing annealing in a nitrogen atmosphere at 723 K for 3 hours.

4.5 Measurement of TE properties

Electrical conductivity and Seebeck coefficient measurements were performed using a commercial system (LSR3, Linseis, Germany) in a helium environment over the temperature range of 300 K to 525 K. The thermal conductivity (κ) was determined using the equation $\kappa = dC_pD$, where d is the density, C_p represents the specific heat capacity, and D denotes thermal diffusivity. Thermal diffusivity was obtained through laser flash analysis (LFA, Linseis, Germany) within the same temperature range. The sample density was calculated from weight and volume measurements, while the specific heat capacity was derived using the Dulong–Petit equation. The measurements were conducted on cuboid-shaped 3D-printed (Bi,Sb)₂Te₃ samples.

4.6 Fabrication and performance measurement of a TEG

To facilitate the integration of TE legs (Fig. 3a), copper electrodes with dimensions of 8 mm × 8 mm × 3 mm were prepared. The samples were joined to the electrodes using a Sn/Ag/Cu solder at 623 K. The contact resistivity was determined using a four-probe direct current setup with three TEGs having varying heights but identical cross-sectional areas (Fig. S19). To avoid unintended oxidation and air side-convection, the output power (P) and conversion efficiency (η) were measured in a vacuum environment (Fig. S26). The hot-side temperature and input heat flow were regulated using a ceramic heater (10 mm × 10 mm), while the cold-side temperature and convective heat transfer were maintained *via* a water-cooled chiller system. A stainless-steel column (10 mm × 10 mm × 25 mm) was employed as a heat flow meter to quantify cold-side heat flow (Q_c) based on Fourier's law. Four K-type thermocouples (0.3 mm diameter) were employed for



temperature monitoring, connected to a Keithley 2000 multi-meter. To mitigate contact thermal resistance, a thermal interface material was applied between adjacent components. The P was determined using a Keithley 2400 source meter with the equation, $P = I \times (V_{oc} - IR)$, where I is the current in the closed circuit, V_{oc} is the open-circuit voltage, and R is the TEG resistance. To measure R without parasitic resistances such as wire resistance, equipment resistance, and wire contact resistance, a four-probe direct current setup was employed, with an ammeter connected in series and a voltmeter in parallel. The system was considered thermally stabilized when temperature fluctuations remained below 0.1 K over 20 minutes. By adjusting I and repeating the process, the maximum P and η of the generator were determined, where η was calculated as $\eta = P/(P + Q_c)$. Additionally, the heat transfer coefficient (h_c) was derived using the relation, $h_c = Q_c/((T_c - T_{fluid}) \times A)$, where Q_c is the measured heat flow, T_c is the cold-side temperature, T_{fluid} is the fluid temperature, and A is the cross-sectional area of the module exposed to the fluid.

Author contributions

S. E. Y.: conceptualization, formal analysis, investigation, methodology, validation, visualization, writing – original draft, and writing – review & editing. J. L.: conceptualization, software, and formal analysis. H. L.: software and formal analysis. B. R.: writing – supervision and review & editing. J. S. S.: conceptualization, supervision, funding acquisition, project administration, writing – original draft, and writing – review & editing.

Conflicts of interest

There are no conflicts to declare.

Data availability

The data supporting this article have been included as part of the SI. It includes the theoretical formulation and derivation, theoretical analysis, TE property data, SEM images, TE module fabrication process, and performance measurement results. See DOI: <https://doi.org/10.1039/d5ee03225c>

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