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# The C(<sup>3</sup>P) + CH<sub>2</sub>(<sup>3</sup>B<sub>1</sub>) reaction: accurate electronic structure calculations and kinetics for astrochemical modeling

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In this work, we present a theoretical study of the C + CH<sub>2</sub> → H + CCH reaction, which is expected to play a key role in the formation of carbon-chain species in molecular clouds. We employ high-level *ab initio* electronic structure methods, including the HEAT-345Q composite scheme and multi-reference configuration interaction, to characterize the potential energy surface. Reaction kinetics are investigated through both conventional transition state theory for tight transition states and variational reaction coordinate transition state theory (VRC-TST) for barrierless pathways. The master equation technique is used to account for competing complex formation, isomerization, and dissociation processes, particularly under collisionless conditions relevant to astrochemistry. Rate constants for product formation are calculated over a wide temperature range (10–300 K), and fitted to extended Arrhenius expressions. The results reveal that both singlet and triplet pathways contribute significantly to the overall reaction rate, with the triplet surface dominating under typical ISM conditions.

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## 1 Introduction

To date, more than 300 molecules have been detected in the interstellar medium (ISM), and the number is continuously growing.<sup>1,2</sup> These molecules range from the simplest molecules that exist, such as methylenide (CH), the first molecule detected in the ISM in 1937,<sup>3</sup> to complex molecules such as fullerenes,<sup>4</sup> and cyanonaphthalene.<sup>5</sup> The ISM consists of diverse regions, where molecular abundances vary depending on local conditions.

To model the chemistry happening in different regions of the ISM, reaction networks such as Nautilus,<sup>6</sup> RATE22<sup>7</sup> and UCLCHEM<sup>8</sup> have been developed. These networks typically incorporate hundreds of species and thousands of reactions, occurring in both the gas phase and on dust grain surfaces. They are used to simulate the evolution of the abundances of different molecules over time and to compare them with observational data. In these models, rate constants for individual reactions are crucial, but due to the extreme conditions in the ISM, these rate constants are not easily measured. Indeed, in dense molecular clouds, temperatures can be as low as 10 K with pressures down to about 10<sup>-15</sup> bar.<sup>9</sup> These rate constants are tabulated in databases, such as the KInetic Database for Astrochemistry (KIDA).<sup>10</sup> The lack of data under conditions similar to those in the ISM results in many of the rate constants

having significant uncertainties, with values being extrapolated from similar reactions or experimental data from largely different conditions. Because these reaction networks encompass too many reactions to each be exhaustively studied, sensitivity analysis are used to determine the reactions that will have significant impacts on the abundances of the species of interest.<sup>11,12</sup>

On the experimental side, the CRESU technique<sup>13</sup> allows for the direct measurements of rate constants over a wide range of temperatures, but reactions between two radical species, such as atomic carbon (C) and methylene (CH<sub>2</sub>), are difficult to study experimentally. Additionally, the CRESU technique<sup>13</sup> is not always able to probe the products formed and can then not determine the branching ratios of the reaction. In these cases, computational chemistry is a precious tool for computing rate constants that will be included in reaction networks.

Among the numerous astrochemical reactions, the reaction C + CH<sub>2</sub> → C<sub>2</sub>H + H has not been studied before but has been shown to be a key reaction in astrochemical networks.<sup>12</sup> Atomic carbon is expected to be one of the most abundant species in molecular clouds, especially in the early and intermediate stages of cloud evolution, with an abundance possibly reaching up to 10<sup>-4</sup> with respect to H<sub>2</sub>.<sup>14–18</sup> CH<sub>2</sub> has been detected in various molecular clouds<sup>19–21</sup> and is expected to be formed mainly through the CH<sub>3</sub><sup>+</sup> + e<sup>-</sup> → CH<sub>2</sub> + H reaction.<sup>22</sup> It is also expected to play a role in the chemistry of Titan as a photo-dissociation product of methane.<sup>23,24</sup> The C + CH<sub>2</sub> reaction produces hydrogen atoms (H) and the ethynyl radical (C<sub>2</sub>H), the latter being involved in the growth of polycyclic aromatic

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hydrocarbons (PAHs)<sup>25</sup> and was first detected in 1974.<sup>26</sup> Acetylene (HCCH), which is an intermediate in the reaction pathway, was detected in 1989<sup>27</sup> and is an important molecule in extraterrestrial chemistry.<sup>28</sup> Vinylidene (CCH<sub>2</sub>), another intermediate, remains undetected,<sup>29</sup> in part due to the short lifetime of its singlet ground state.<sup>30</sup>

In this work, we present high-accuracy electronic structure calculations for the C + CH<sub>2</sub> reaction. We employ the high-accuracy extrapolated *ab initio* thermochemistry (HEAT) scheme,<sup>31</sup> along with the multi-reference configuration interaction (MRCI) method,<sup>32</sup> to obtain accurate information regarding the stationary points on the potential energy surface (PES) of the system. These electronic structure calculations allow us to characterize intermediates and transition states, which are necessary to take into account when studying the reaction kinetics. To investigate the reaction kinetics, we apply a statistical rate theory based master equation method, allowing us to obtain rate constants for the C + CH<sub>2</sub> → H + C<sub>2</sub>H reaction.

## 2 Methodology

In typical chemical kinetics calculations, it is necessary to obtain accurate information on the stationary points of the PES. These can be used to compute microcanonical rate constants that are then input in the master equation (ME) to obtain phenomenological rate constants. This section will describe each step of these processes.

### 2.1 Electronic structure calculations

Kinetic modeling requires highly accurate evaluation of reaction barriers and sometimes also reaction energies to obtain reliable results. Therefore, we employed the renowned HEAT scheme in its 345-Q form, hereafter referred to as HEAT345-Q.<sup>31</sup> This scheme has been shown to give reaction energies with errors lower than 1 kJ mol<sup>-1</sup>. The first step in HEAT345-Q is to perform a geometry optimization with coupled-cluster methods including single and double excitations and including triples in a perturbative way (CCSD(T)),<sup>33,34</sup> using the correlation-consistent cc-pVQZ basis set of Dunning *et al.*<sup>35,36</sup>

From the optimized geometry, several energy contributions are included to obtain accurate energies at a reasonable computational cost. In HEAT345-Q, the total energy is defined as a sum of contributions calculated for the obtained geometry, as given in eqn (1):

$$E = E_{\text{HF}}^{\infty} + \Delta E_{\text{CCSD(T)}}^{\infty} + \Delta E_{\text{CCSDT}} + \Delta E_{\text{CCSDTQ}} + \Delta E_{\text{rel}} + \Delta E_{\text{DBOC}} + \Delta E_{\text{ZPE}} \quad (1)$$

In eqn (1),  $E_{\text{HF}}^{\infty}$  is the complete basis set extrapolated Hartree-Fock energy,  $\Delta E_{\text{CCSD(T)}}^{\infty}$  is the complete basis set extrapolation of the correlation energy obtained from a CCSD(T) calculation. Further electron correlation terms ( $\Delta E_{\text{CCSDT}}$  and  $\Delta E_{\text{CCSDTQ}}$ ) are obtained through the use of frozen core calculations and smaller basis sets compared to  $\Delta E_{\text{CCSD(T)}}^{\infty}$ .  $\Delta E_{\text{rel}}$  includes relativistic corrections such as the Cowan-Griffin term and

the two-electron Darwin energy.<sup>37-39</sup>  $\Delta E_{\text{DBOC}}$  is the diagonal Born-Oppenheimer correction (DBOC), which is added to account for the Born-Oppenheimer approximation.<sup>40</sup>  $\Delta E_{\text{ZPE}}$  is finally the ZPE term corrected for anharmonicity employing VPT2, obtained at the same level of theory as the geometry optimization (*i.e.* CCSD(T)/cc-pVQZ).<sup>41</sup> A more thorough description of the HEAT scheme and each term involved in eqn (1), along with the basis set used in the calculation of each term can be found in the paper by Bomble *et al.*<sup>31</sup>

Geometries, relativistic corrections, DBOC and anharmonic-ZPE have been obtained using the CFOUR code.<sup>42</sup> CCSD and CCSD(T) calculations have been performed with the MOLPRO 2024.3 computational chemistry package.<sup>43-45</sup> Calculations including complete treatment of triples and further (*i.e.* CCSDT and CCSDTQ) have been carried out using the MRCC code.<sup>46,47</sup>

Due to their single-reference nature, coupled cluster methods are expected to fail for the processes of bond-forming and bond-breaking. As will be detailed in Section 2.2, our kinetics calculations require energy and frequency calculations along the bond dissociation or formation. Therefore, additional calculations are necessary to describe the breaking and forming of bonds. To this effect, geometry optimizations and energy calculations were carried out at the MRCI<sup>32</sup> level using a multiconfiguration self-consistent field (MCSCF)<sup>48</sup> wavefunction as the reference. We used a full valence complete active space, *i.e.* 10 electrons in 10 orbitals. Davidson corrections (+Q)<sup>49</sup> were applied to the MRCI energies to improve the accuracy of the total electronic energies calculated. The correlation-consistent aug-cc-pVTZ basis set of Dunning *et al.*<sup>35,36</sup> was used. This level of calculation is denoted as MRCI+Q/aug-cc-pVTZ and has been used for each bond scan *vide infra*. The multireference calculations were performed using MOLPRO 2024.3.<sup>43-45</sup> For each stationary point, a harmonic frequency calculation was performed to confirm its nature. The minima were identified by the absence of imaginary frequencies, whereas the transition states were confirmed by the presence of exactly one imaginary frequency along the reaction coordinate.

### 2.2 Kinetics treatment

The C + CH<sub>2</sub> reaction is expected to show two important properties that need to be taken into account when considering the kinetics of the system: first, the possibility for the isomerization of the formed adduct to compete with the hydrogen abstraction that leads to C<sub>2</sub>H + H formation. Second, simple bond-forming and bond-breaking processes can be expected to proceed without passing through a saddle point on the PES, making it challenging to determine the kinetic bottleneck.

To accurately describe systems where several chemical reactions compete with collisional (de-)energization processes, the ME<sup>50,51</sup> is used in conjunction with RRKM theory. The ME is a probabilistic model of energy transfer. A two-dimensional master equation is used to take both energy and total angular momentum into account. In this model, the time evolution of the probability of finding species A in an



energy state  $E_i$  and angular momentum quantum number  $J_i$  is given by:

$$\begin{aligned} \frac{d}{dt} p_A(E_i, J_i, t) = & \omega \left( \int_0^\infty \sum_{J_j=0}^\infty P(E_i, J_i | E_j, J_j) p_A(E_j, J_j, t) dE_j \right. \\ & - p_A(E_i, J_i, t) + \sum_{B \neq A} k_{AB}(E_i, J_i) p_B(E_i, J_i, t) \\ & \left. - k_{BA}(E_i, J_i) p_A(E_i, J_i, t) + Rf \right) \end{aligned} \quad (2)$$

In eqn (2), four terms appear. The first two are concerned with collisional energy transfer. Specifically, the first term is the increase in population of the state  $E_i, J_i$  from collisional excitation or deexcitation of molecules of  $A$  in all energy and angular momentum states  $E_j, J_j$  (including  $E_i, J_i$ ), while the second one is the decrease in population of that same state due to collisions. For the evaluation of these terms, a collisional model has to be chosen. The collisional frequency ( $\omega$ ) used here comes from the Lennard-Jones collision frequency model.<sup>52</sup> The Lennard-Jones collision parameters for the intermediates CCH<sub>2</sub> and HCCH were assumed to be equal and obtained from the work of Hippler *et al.*<sup>53</sup> Those for the bath gas, H<sub>2</sub>, have been obtained from the work of Weaver *et al.*<sup>54</sup> The energy transfer model also has to be chosen and is in our case a simple down-exponential model.<sup>55</sup>

The third term of eqn (2) relates to specie  $B$  forming  $A$ , and *vice versa* for the fourth term. The reactions are governed by microcanonical rate constants  $k(E, J)$  and conservation of the total angular momentum is accounted for.

Microcanonical rate constants  $k(E, J)$  can be obtained by RRKM theory. In such work, the rate constant for a unimolecular reaction is given by eqn (3):<sup>56</sup>

$$k(E, J) = L \frac{N^\ddagger(E, J)}{h \rho(E, J)} \quad (3)$$

$E$  is the total nonfixed energy available to the molecule,  $J$  the angular momentum quantum number,  $L$  the statistical factor, and  $h$  is Planck's constant,  $N^\ddagger(E, J)$  is the sum of active vibrational and internal rotation states for the transition state, and  $\rho(E, J)$  is the density of quantum states of the reactant.

The last term of eqn (2) is a source term accounting for the bimolecular association step.  $R$  is the total rate of the entrance flux leading to the formation of the energized adduct, and  $f$  is the initial energy distribution function of the energized adduct formed by the association reaction and is given by

$$f(E, J) = \frac{(2J+1)N^\ddagger(E, J) \exp\left(-\frac{E}{RT}\right)}{\sum_J \int_0^\infty (2J+1)N^\ddagger(E, J) \exp\left(-\frac{E}{RT}\right) dE} \quad (4)$$

with  $N^\ddagger(E, J)$  here being the rovibrational sum of states of the entrance TS,  $T$  the temperature and  $R$  the ideal gas constant.

In the present work, some reactions proceed through well defined transition states, which are saddle points on the potential energy surface. On the other hand, some simple bond

formation or bond breaking occur without existence of a saddle point on the potential energy surface. The first type of transition states, also called tight transition states can be treated easily. Their sum of states can be computed from the geometry and vibrational frequencies calculated at the saddle point, treating it as a rigid rotor harmonic oscillator. The densum module of the MultiWell package<sup>57,58</sup> was used in such cases, as well as for the computation of the density of states of the different intermediates considered. In contrast, for the second type of transition states, or loose transition states, the kinetic bottleneck is located at the point along the reaction coordinate for which the sum of states is the smallest. A suitable method to treat loose transition states is the variable reaction coordinate transition state theory (VRC-TST) approach.<sup>59-61</sup>

In VRC-TST, the vibrational modes, perpendicular to the reaction coordinate in a bond cleavage process, are separated into two groups: conserved modes are those that remain of the same nature along the reaction coordinate, whereas transitional modes undergo a change in nature during the reaction. The former can be identified by their vibrational frequencies remaining almost constant as the interfragment distance is changed, while the latter will see their values tend to zero as the interfragment distance is increased. This is expected, as two separate fragments will have overall less vibrational modes and more rotational modes than the adduct formed by combining these two fragments. These two categories of modes are considered to be uncoupled and their overall sum of states  $N(E, J)$  is then given by a convolution as in eqn (5):

$$N(E, J) = \int_0^E N_v(E - \varepsilon) \Omega_J(\varepsilon) d\varepsilon \quad (5)$$

In eqn (5),  $E$  is the accessible energy and  $\varepsilon$  is the energy available for the transitional modes.  $N_v$  is the sum of states for the conserved vibrational modes, and is computed by a direct-count algorithms, while  $\Omega_J d\varepsilon$  is the number of states for the transitional modes at a given  $J$ , which is computed by Monte Carlo integration.<sup>60</sup>

To compute  $N(E, J)$ , a proper potential model describing the interactions between both fragments involved is necessary. The potential energy of the system was evaluated as a function of the distance between the bonding atoms of each fragment, keeping the relative geometries of the fragments fixed, and was then fitted to a Varshni potential.<sup>62,63</sup> Then, an additional 6-12 Lennard-Jones potential was added between the non-bonding atoms to account for the relative orientation of the fragments. The kinetic bottleneck was then found at the inter-fragment distance which has the smallest value of  $N(E, J)$ . The Variflex code<sup>64</sup> was used to compute the sum of states for the loose transition states. Alternatively, the variational RRKM approach implemented in the KTOOLS module of the MultiWell suite<sup>57,58</sup> can be employed to compute the sum of states for the loose transition state channels.

Branching ratios for individual reaction channels were then computed at the  $E/J$  resolved level using the pTS code, which solves a 2D master equation under the steady-state



approximation,<sup>65</sup> provided the sums of states and densities of states for transition states and minima are known.

The bimolecular association step rate constant was calculated using bimolecular transition state theory as given in eqn (6):<sup>56</sup>

$$k_{\text{bi}}(T) = \frac{k_{\text{B}}T}{h} \frac{Q_{\text{complex}^{\ddagger}}^{\text{el,trans}} Q_{\text{complex}^{\ddagger}}^{\text{vib,rot}}}{Q_{\text{frag}}^{\text{el,trans}} Q_{\text{frag}}^{\text{vib,rot}}} \quad (6)$$

At lower temperatures, numerical issues arise from the  $\exp\left(-\frac{E}{kT}\right)$  terms present in the ME model, see eqn (4). To circumvent this limitation, we decided to study the system in the collisionless limit. For that case, a computer code was developed to compute  $E/J$  resolved rate constants, provided the sums of states for the transition states are known.<sup>66</sup>

Considering an intermediate  $W_i$ , one can write the evolution of its concentration with respect to time as:

$$\frac{d[W_i(E, J)]}{dt} = \sum_{j \neq i} N_{ij}^{\ddagger} \left( \frac{\sigma_j}{\sigma_{ij}^{\ddagger}} [W_j] - \frac{\sigma_i}{\sigma_{ij}^{\ddagger}} [W_i] \right) - \sum_l \frac{\sigma_i}{\sigma_{iP_l}^{\ddagger}} N_{iP_l}^{\ddagger} [W_i] + \frac{\sigma_R}{\sigma_{iR}^{\ddagger}} N_{iR}^{\ddagger} \times c \quad (7)$$

In eqn (7),  $N_{ij}^{\ddagger}$  is the sum of states for the TS connecting species  $i$  and  $j$ , and it depends on  $E$  and  $J$ . The first term of the first sum corresponds to isomerization from the other intermediates  $W_j$  to  $W_i$ , while the second term corresponds to isomerization from  $W_i$  to  $W_j$ . The second sum corresponds to forming the product  $P_k$  from  $W_i$ , and  $N_{iR}^{\ddagger} \times c$  corresponds to the formation of  $W_i$  from the reactants, with  $c$  a constant related to the reactants partition function, but also to the reactants' concentration. The

various  $\sigma$ 's are the rotational symmetry numbers. Since in the collisionless case the energy levels are uncoupled, the system is solved for each  $(E, J)$  pair. The contributions from each pair are summed in order to obtain rate constants for each product channel. Note that all microcanonical rate constants are replaced by sum of states and rotational symmetry numbers, as all densities of states will vanish.<sup>56</sup> In the steady-state approximation, eqn (7) is equal to 0 and one can rewrite it as

$$\sum_{j \neq i} \frac{\sigma_j}{\sigma_{ij}^{\ddagger}} N_{ij}^{\ddagger} [W_j] - \left( \sum_{j \neq i} \frac{\sigma_i}{\sigma_{ij}^{\ddagger}} N_{ij}^{\ddagger} + \sum_l \frac{\sigma_i}{\sigma_{iP_l}^{\ddagger}} N_{iP_l}^{\ddagger} \right) [W_i] = -\frac{\sigma_R}{\sigma_{iR}^{\ddagger}} N_{iR}^{\ddagger} \times c \quad (8)$$

or in matrix form:

$$\mathbb{A}X = B \Rightarrow X = \mathbb{A}^{-1}B \quad (9)$$

In eqn (9),  $A_{ij} = \frac{\sigma_j}{\sigma_{ij}^{\ddagger}} N_{ij}^{\ddagger}$ ,  $A_{ii} = -\sum_{j \neq i} \frac{\sigma_i}{\sigma_{ij}^{\ddagger}} N_{ij}^{\ddagger} - \sum_l \frac{\sigma_i}{\sigma_{iP_l}^{\ddagger}} N_{iP_l}^{\ddagger}$ ,  $B_i = -\frac{\sigma_R}{\sigma_{iR}^{\ddagger}} N_{iR}^{\ddagger} \times c$  if  $i$  is the first intermediate formed by the association reaction,  $B_i = 0$  otherwise. Finally,  $X$  is the vector of steady-state concentrations for all intermediates. Then, the product formation rate constant for each product channel  $l$  is given by

$$k(T, P_l \text{ from } W)_i = \sum_n [W_i]_n k_{il}(E_n) \quad (10)$$

### 3 Results and discussion

In this section we will first report results from our electronic structure calculations and discuss them. Thereafter we turn to our kinetics calculations.

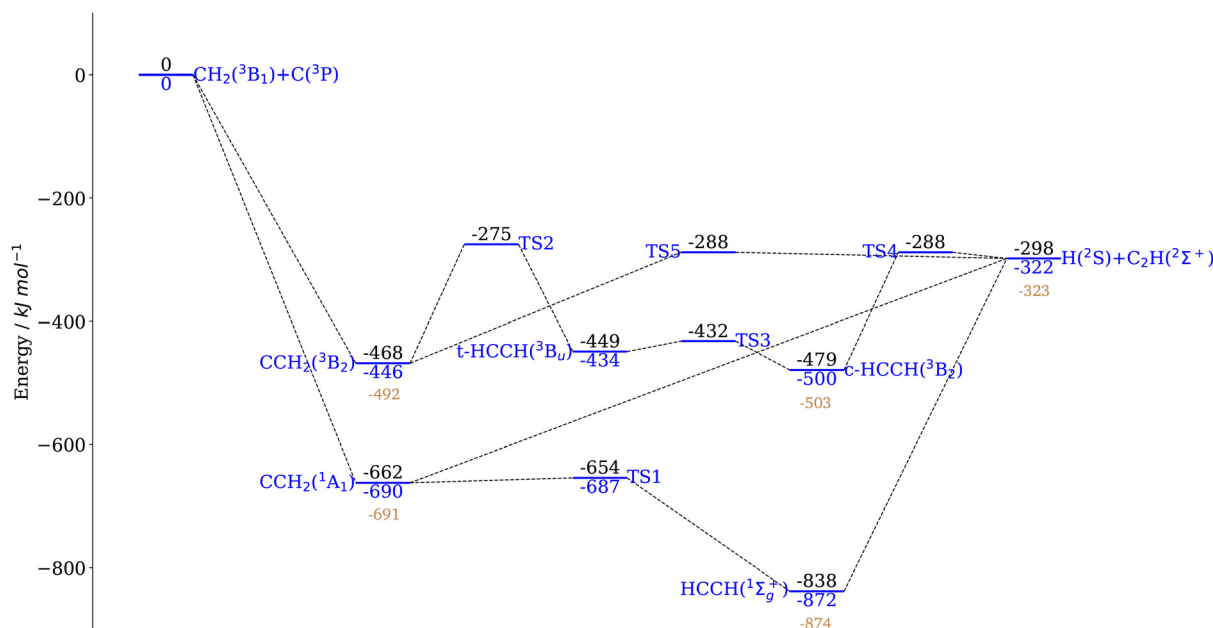


Fig. 1 Stationary points on the PES for the C + CH<sub>2</sub> system. In blue, energies at the HEAT345-Q level. In black, energies at the MRCI+Q/aug-cc-pVTZ level, corrected for harmonic ZPE. In brown, associated reaction enthalpy at 0 K calculated from the ATcT database values.



### 3.1 Electronic structure calculations

Unless explicitly stated, the energy values mentioned in this section correspond to the MRCI+Q/aug-cc-pVTZ values. These are given relative to the energy of the separated reactants  $C(^3P) + CH_2(^3B_1)$  and have been corrected for vibrational zero-point energy (ZPE).

The calculated stationary points on the PES associated with the  $C + CH_2$  reaction are shown in Fig. 1, along with reaction enthalpies associated to the formation of intermediates and products at 0 K, using benchmark values from the active thermochemical tables (ATcT).<sup>67</sup> Each reactant has a triplet spin state as its electronic ground state. This can result in the reaction occurring on a singlet, triplet, or quintet surface. In all three cases, C and  $CH_2$  can form  $CCH_2$  without passing an energy barrier.  $CCH_2(^1A_1)$  is with an energy of  $-662 \text{ kJ mol}^{-1}$  more stable than  $CCH_2(^3B_2)$  which has an energy of  $-468 \text{ kJ mol}^{-1}$ .  $CCH_2(^5A)$  has an energy of  $-141 \text{ kJ mol}^{-1}$ . On the singlet surface,  $CCH_2$  can undergo H-loss to form  $H + C_2H$  without going through a saddle point, or isomerize into  $HCCH$  through TS1 which has an energy of  $-654 \text{ kJ mol}^{-1}$ , the latter option being more energetically favorable.  $HCCH$ , at an energy of  $-838 \text{ kJ mol}^{-1}$ , can also dissociate into  $H + C_2H$  without going through a saddle point. The products  $H + C_2H$  have an energy of  $-298 \text{ kJ mol}^{-1}$ , and all of the species involved on the singlet surface are therefore lower in energy than the reactants.

The individual contributions to the total energy in the HEAT scheme described in Section 2.1 are reported in Table 1 for the singlet surface for reactants, products, and some intermediates. In addition to stationary point calculations, surface scans were performed for the entrance ( $C + CH_2 \rightarrow CCH_2(^1A_1)$ ) and exit ( $CCH_2(^1A_1) \rightarrow C_2H + H$  and  $HCCH(^1\Sigma_g^+) \rightarrow C_2H + H$ ) channels. Since these steps are expected to proceed without an intrinsic energy barrier, a series of single-point energy (SPE) and frequency calculations were carried out along the reaction coordinate to accurately characterize the potential energy surface. This provides essential data to fit the potential energy used as input in VRC-TST calculations.

Previous works on the singlet potential energy surface of acetylene have discussed the presence or absence of an intermediate in the isomerization path between  $CCH_2(^1A_1)$  and  $HCCH(^1\Sigma_g^+)$ .<sup>68–71</sup> While we have not been able to find such an intermediate in our calculations, we infer that even if existing it would not be important to include it in our kinetics calculations as it should sit in a shallow well between two small transition states. From comparing energetic data and structure,

it appears that our TS1 corresponds to the higher energy one of those two TSs and therefore TS1 should be sufficient to assess the kinetics of the system.

The initial HEAT paper reports energies for both  $C_2H$  and  $CH_2$ .<sup>72</sup> For  $C_2H$ , our results are in accordance with theirs. A difference of  $\sim 6 \text{ kJ mol}^{-1}$  mainly comes from our inclusion of the 2-electrons Darwin energy in the HEAT345-Q scheme that was not included in the initial HEAT scheme. Removing that contribution from our calculations lowers the energy difference to  $0.4 \text{ kJ mol}^{-1}$ . A similar observation is made for  $CH_2$ . Baraban *et al.*<sup>73</sup> also reported values for  $HCCH(^1\Sigma_g^+)$  and  $CCH_2(^1A_1)$  using the HEAT-456QP scheme.<sup>31</sup> Our total energies differ by  $1.4 \text{ kJ mol}^{-1}$  for  $HCCH(^1\Sigma_g^+)$  and by  $2.2 \text{ kJ mol}^{-1}$  for  $CCH_2(^1A_1)$ , with each individual term being very close between the calculations reported by Baraban *et al.* and ours. We can conclude that the results are in good agreement, with energy differences being attributed to the slight differences between the two HEAT schemes.

The triplet surface behaves very similar to the singlet one.  $CCH_2$  can undergo H-loss to form the products  $H + CCH$  through TS5 or isomerization to *trans*- $HCCH$  through TS2, which can itself isomerize to *cis*- $HCCH$  through TS3. *cis*- $HCCH$  can then dissociate into the products  $H + C_2H$  through TS4. A surface scan was performed for the entrance channel  $C + CH_2 \rightarrow CCH_2(^3B_2)$  to fit the energies to a Varshni potential. Similarly as for the singlet surface, this association proceeds without an intrinsic energy barrier.

Few studies have reported results for the triplet PES of the system,<sup>74,75</sup> and we could not find any existing data following the HEAT scheme. While we were able to obtain HEAT data for the minima on the triplet spin surface, our coupled-cluster calculations indicated a multireference nature of these structures through high T1 diagnostic values ( $\sim 0.08$ ). The T1 diagnostic is regularly used to assess the reliability of coupled-cluster calculations and for any value higher than 0.02 the results should be treated as unreliable.<sup>76</sup> The high values obtained for the transition state calculations therefore prevent us from calculating reliable HEAT energies. Nevertheless, HEAT results are reported for the minima in Table 2, and are in general agreement with our MRCI energies as well as with energies reported in the work by Vacek *et al.*<sup>74</sup> We however note a significant difference for the ATcT value obtained for the formation of  $CCH_2(^3B_2)$  and our own results which can not be easily explained.

**Table 1** HEAT345-Q contributions for stationary points on the singlet PES. All values are given in Hartrees

	$CH_2(^3B_1)$	$C(^3P)$	$CCH_2(^1A_1)$	TS1	$HCCH(^1\Sigma_g^+)$	$H(^2S)$	$C_2H(^2\Sigma^+)$
$E_{HF}^\infty$	-38.935334	-37.688648	-76.800053	-76.780535	-76.855469	-0.499994	-76.167291
$\Delta E_{CCSD(T)}^\infty$	-0.213427	-0.156099	-0.462735	-0.478655	-0.480411		-0.446052
$\Delta E_{CCSDT}$	-0.000470	-0.000562	-0.000703	-0.000205	0.000225		-0.000181
$\Delta E_{CCSDTQ}$	-0.000082	-0.000029	-0.000620	-0.000791	-0.000911		-0.000939
$\Delta E_{rel}$	-0.016051	-0.016285	-0.032230	-0.032257	-0.032142	-0.000006	-0.032363
$\Delta E_{DBOC}$	0.002160	0.001660	0.003766	0.003728	0.003673	0.000272	0.003522
$\Delta E_{ZPE}$	0.016478		0.023011	0.021042	0.026349		0.013993
$E_{HEAT}$	-39.146727	-37.859966	-77.269566	-77.267674	-77.338685	-0.499729	-76.629309



**Table 2** HEAT345-Q contributions for minima on the triplet PES. All values are given in Hartrees

	$\text{CCH}_2(^3\text{B}_2)$	<i>trans</i> - $\text{HCCH}(^3\text{B}_u)$	<i>cis</i> - $\text{HCCH}(^3\text{B}_2)$
$E_{\text{HF}}^\infty$	-76.747189	-76.717941	-76.751199
$\Delta E_{\text{CCSD(T)}}^\infty$	-0.439916	-0.449692	-0.439837
$\Delta E_{\text{CCSDT}}$	0.0123715	-0.001046	-0.001237
$\Delta E_{\text{CCSDTQ}}$	-0.000310	-0.000890	-0.000616
$\Delta E_{\text{rel}}$	-0.0320931	-0.032212	-0.032138
$\Delta E_{\text{DBOC}}$	0.003804	0.004264	0.003849
$\Delta E_{\text{ZPE}}$	0.030450	0.025690	0.023995
$E_{\text{HEAT}}$	-77.172884	-77.171827	-77.197184

Finally, the quintet surface was only briefly studied. While the association of C and  $\text{CH}_2$  occurs without an intrinsic energy barrier, both hydrogen abstraction and isomerization to HCCH involve energy barriers of about  $\sim 200 \text{ kJ mol}^{-1}$  so the quintet surface is not expected to play a significant role in the kinetics of the reaction.

All the energies and geometries calculated are available in the SI, as well as the harmonic frequencies used to compute the densities and sums of states necessary for the kinetics calculations. Parameters obtained from the Varshni fits for the loose transition states are also included.

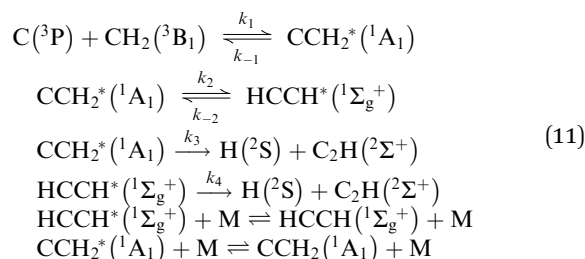
### 3.2 Kinetics calculations

As shown in Section 3.1, the reaction can occur without energy barrier on both the singlet and triplet surfaces. The bimolecular association rate constants for both the singlet and triplet surfaces are shown in Fig. 2. From this figure, it can be seen that the rate constant on the triplet surface is about twice as large as the one on the singlet surface. While the singlet spin surface is more attractive, the higher rate constant on the triplet spin surface is explained by the difference in electronic degeneracy between the two surfaces. Thus both surfaces may contribute significantly to the overall rate constant. We study the rate constants on the singlet and the triplet surface independently and sum them to obtain the overall results.

In this section, kinetics calculations reported were performed using MRCI energies. The calculations were performed using both HEAT345-Q and MRCI methods on the singlet surface and no significant difference arose. Studying the system

in the collisionless limit allows us to get analytical results for the rate constants for individual channels. We argue that this approximation is relevant, as pressures relevant to astrochemistry are very low, and we will show that at higher temperatures, the unimolecular products are negligible for any pressure lower than atmospheric pressure. Master equation calculations have been performed for all angular momentum quantum numbers up to 80, with a maximum energy of  $80\,000 \text{ cm}^{-1}$  and energy bins of  $10 \text{ cm}^{-1}$ .

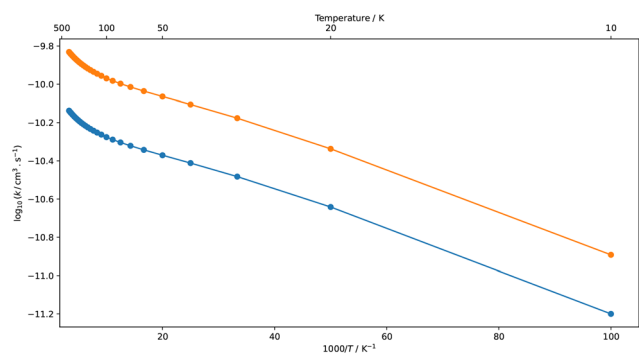
**3.2.1 Singlet surface.** On the singlet surface, the reaction  $\text{C} + \text{CH}_2 \rightarrow \text{H} + \text{C}_2\text{H}$  is expected to proceed following the mechanism:



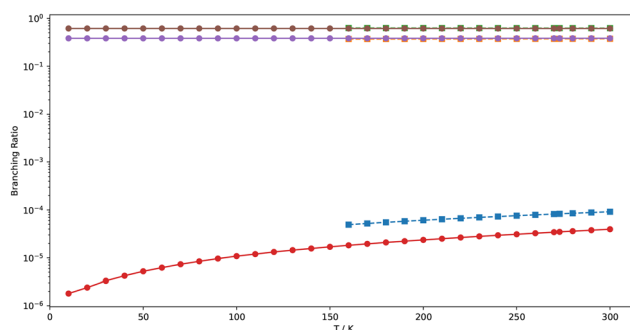
In the collisionless limit, the last 2 processes relating to collisional (de)excitation are ignored.

The branching ratios obtained from the analytical results in the collisionless limit and for low pressure ( $10^{-6} \text{ atm}$ ) between 10 K and 300 K are shown in Fig. 3. The two sets of results are in good agreement, with differences under 0.005% in the product branching ratios.

For temperatures higher than 150 K, branching ratios for each channel were calculated at various pressures. Results are presented in the SI for pressures of 1,  $10^3$ ,  $10^6$  and  $10^9 \text{ atm}$ . No significant changes are observed at pressures lower than 1 atm or higher than  $10^9 \text{ atm}$ . At pressures lower than 1 atm, product formation is the major channel, while backdissociation and complex stabilization can be neglected. With increasing pressure, complex formation becomes gradually more important. The formation of HCCH competes with formation of bimolecular products at  $10^3 \text{ atm}$ , and with the formation of  $\text{CCH}_2$  at  $10^6 \text{ atm}$ . At extremely high pressures,  $\text{CCH}_2$  becomes the only



**Fig. 2** Bimolecular association rate constant as a function of temperature for the  $\text{C} + \text{CH}_2$  reaction. In blue, for the singlet state. In orange, for the triplet state.



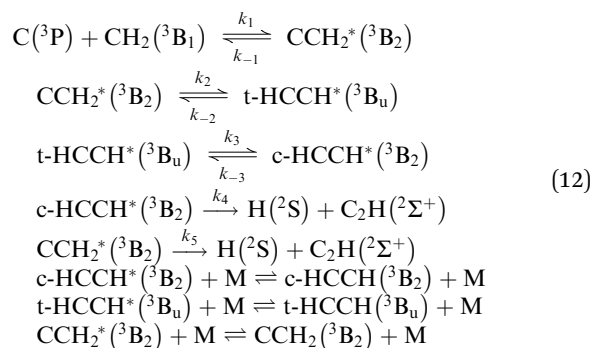
**Fig. 3** Branching ratios at  $P = 10^{-6} \text{ atm}$  (dotted lines) and in the collisionless case (full lines) on the singlet spin surface. In brown and green:  $\text{H} + \text{C}_2\text{H}$  formation from the dissociation of  $\text{CCH}_2$ , in purple and pink:  $\text{H} + \text{C}_2\text{H}$  formation from the dissociation of  $\text{HCCH}$ , in red and blue: backdissociation to reactants from  $\text{CCH}_2$ .



relevant product as any  $\text{CCH}_2^*$  adduct formed is thermalized by collisions before having time to react further.

The negligible amount of intermediates stabilized at low pressures along with the strong agreement for branching ratios between the collisionless and low pressure results, shown in Fig. 3 for the temperature range 150–300 K, justify the use of the collisionless approximation to obtain results also at temperatures below 150 K. At pressures of the order of  $10^6$  atm, H-loss from  $\text{CCH}_2$  has a significant impact on the formation of  $\text{H} + \text{C}_2\text{H}$ , which is thus an important channel to include in order to have a proper description of the system. In the collisionless case, we expect that the inclusion of this channel is not important, as the isomerization and subsequent dissociation as seen in Fig. 3 dominates over the backdissociation.

**3.2.2 Triplet surface.** Based on our calculated stationary points for the triplet surface, the reaction  $\text{C} + \text{CH}_2 \rightarrow \text{C}_2\text{H} + \text{H}$  is expected to proceed following the mechanism:



In the collisionless limit, the last 3 processes relating to collisional (de)excitation are ignored.

As in the singlet case, at any pressure relevant for astrochemistry, the stabilization of intermediates is negligible and the results in the collisionless case are used for all temperatures. The branching ratios for product formation and backdissociation are shown in Fig. 4. The results are similar to those observed on the singlet spin surface. H-loss from  $\text{CCH}_2(^3\text{B}_2)$  is the main product channel, followed by loss from  $\text{c-HCCH}(^3\text{B}_2)$ . The higher yield from  $\text{CCH}_2(^3\text{B}_2)$  is explained by the lower

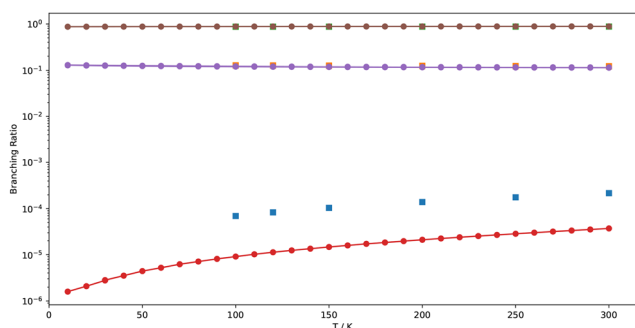


Fig. 4 Branching ratios at  $P = 10^{-6}$  atm (dotted lines) and in the collisionless case (full lines) on the triplet surface. In brown and green:  $\text{H} + \text{C}_2\text{H}$  formation from the dissociation of  $\text{CCH}_2$ , in purple and pink:  $\text{H} + \text{C}_2\text{H}$  formation from the dissociation of  $\text{HCCH}$ , in red and blue: backdissociation to reactants from the dissociation of  $\text{CCH}_2$ .

barrier to dissociate than the barrier to isomerize to  $\text{t-HCCH}(^3\text{B}_u)$ . Dissociation back to the reactants is again negligible.

**3.2.3 Overall results and astrochemical modeling.** As shown in the previous sections, backdissociation is negligible over the temperature range of interest, and the product formation rate constant is almost equal to the bimolecular association rate constant. Fig. 5 shows that around two-thirds of the product formation comes from the reaction on the triplet spin surface. The rate constant does not show any negative temperature dependence at lower temperatures as can be seen in some radical–radical reactions.<sup>61,77,78</sup>

The overall product formation rate constant was fitted to the modified Arrhenius expression

$$k(T) = \alpha \times 10^{-10}(T/300)^\beta \exp(-\gamma/T) \text{ cm}^3 \text{ s}^{-1} \quad (13)$$

for three different temperature ranges: 10–100 K, 100–200 K, and 200–300 K. Parameters corresponding to the best fits are given in Table 3.

Finally, the Nautilus simulation code<sup>6</sup> was used to visualize the impact of replacing the rate constant that is currently incorporated in the *kida.uva.2024* network<sup>10</sup> by the rate constant calculated in this work. Nautilus is a 3-phase (gas, dust grain ice surface and dust grain ice mantle) time dependent chemical model for astrochemistry. There are 800 individual species included in the network that are involved in approximately 9000 reactions. Elements are initially in either their neutral or ionic forms in this model (elements with an ionization potential  $< 13.6$  eV are considered to be fully ionized). This model is used to simulate the abundances of atoms and molecules with respect to hydrogen, in molecular clouds as a function of time.

Fig. 6 shows the relative abundances of  $\text{C}_2\text{H}$  and  $\text{CH}_2$  with the currently included value of  $k(T) = 10^{-10} \text{ cm}^3 \text{ s}^{-1}$  and our calculated value for a simulation at  $T = 10$  K. The effects on the abundances of the species involved in the reaction are rather small, which is explained by the fact that at  $T = 10$  K, the fitted

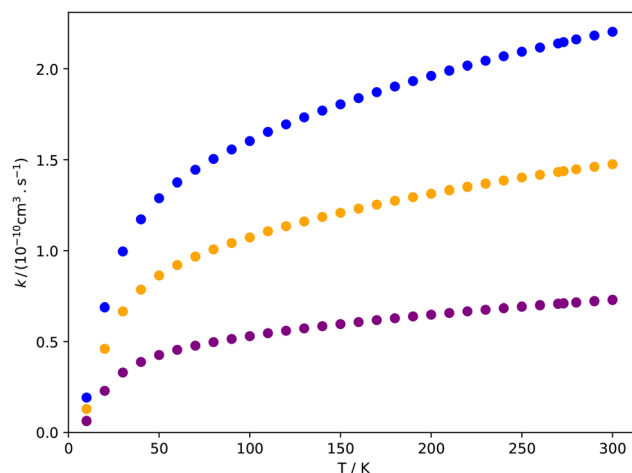
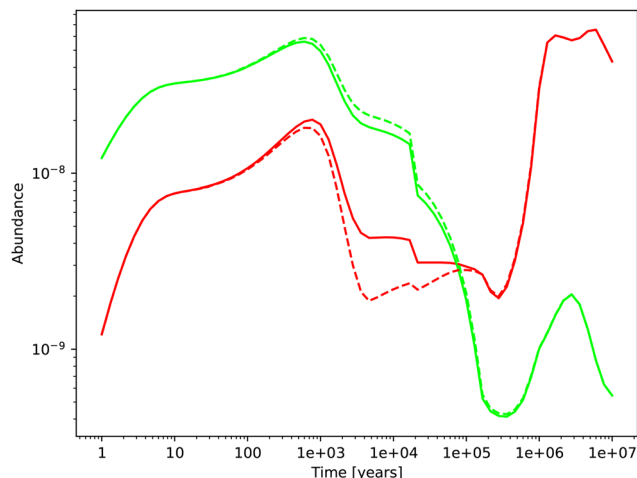


Fig. 5 Calculated product formation rate constants for the  $\text{CH}_2 + \text{C} \rightarrow \text{H} + \text{C}_2\text{H}$  reaction: singlet case (purple), triplet (orange), overall (blue).



**Table 3** Parameters obtained from the best fit for the overall product formation rate constant

Temperature range (K)	$\alpha$ (cm <sup>3</sup> s <sup>-1</sup> )	$\beta$	$\gamma$ (K)
10–100	$1.890 \times 10^{-10}$	-0.0052	23.432
100–200	$2.193 \times 10^{-10}$	0.303	-2.357
200–300	$2.280 \times 10^{-10}$	0.244	10.204



**Fig. 6** Abundances of C<sub>2</sub>H (red) and CH<sub>2</sub> (green) relative to H<sub>2</sub> with the rate constant currently in the kida.uva.2024 network (full lines) and the rate constant calculated in this work (dotted lines). The Nautilus simulation code was used with  $T = 10$  K.

rate constant obtained from the calculations in this work is  $k(10) = 2.168 \times 10^{-11} \text{ cm}^3 \text{ s}^{-1}$  which is less than one order of magnitude different from the value  $10^{-10} \text{ cm}^3 \text{ s}^{-1}$  used originally in the network.

Further kinetic results obtained in the collisionless case for the singlet and triplet spin surface, as well as the overall results are available in the SI.

## 4 Conclusion and outlook

In this work, we have conducted a comprehensive theoretical investigation of the  $\text{C} + \text{CH}_2 \rightarrow \text{H} + \text{C}_2\text{H}$  reaction, focusing on interstellar conditions. By combining high-accuracy *ab initio* calculations with kinetic modeling approaches, we have characterized the relevant stationary points on the potential energy surfaces for both singlet and triplet reaction pathways and derived reliable rate constants over a broad temperature range.

Notably, this work reports for the first time HEAT-scheme energy values for the minima on the triplet potential energy surface of the C<sub>2</sub>H<sub>2</sub> system, contributing new high-level reference data to the field.

The main outcome of this study for astrochemistry is the derivation of three fitted expressions between 10 K and 300 K for the rate constant for the  $\text{C} + \text{CH}_2 \rightarrow \text{H} + \text{C}_2\text{H}$  reaction.

Overall, this study highlights the value of theoretical chemistry in bridging experimental limitations, particularly for

radical–radical reactions. Future work could use these methods to explore pressure-dependent effects in planetary atmospheres or to investigate other key reactions that may not be experimentally unfeasible.

## Conflicts of interest

There are no conflicts to declare.

## Data availability

The data supporting this article have been included as part of the supplementary information (SI). Supplementary information is available. See DOI: <https://doi.org/10.1039/d5cp02644j>.

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