



## Machine learning of the architecture–property relationship in graft polymers†

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**Graft polymers are promising in energy and biomedical applications. However, the diverse architectures make it challenging to establish their structure–property relationships. We systematically investigate how backbone and side-chain architectures influence four key properties: glass transition temperature ( $T_g$ ), self-diffusion coefficient ( $D$ ), radius of gyration ( $R_g$ ), and packing density ( $\rho$ ). Using molecular dynamics simulations, we analyze a dataset of 500 graft polymers with randomly positioned side chains.  $T_g$  and  $D$  exhibit decoupled relationships due to the distinct topological effects. Furthermore, we develop dense neural networks (DNNs) and convolutional neural networks (CNNs) to pave the way to polymer design with desired properties.**

Graft polymers consist of a main backbone with one or more side chains, giving them combined or novel properties not found in linear or block copolymers.<sup>1–3</sup> Their architecture enables enhanced or unique material functionalities. Bottlebrush architectures, a special class of graft polymers, feature highly grafted side chains that suppress molecular entanglements, yielding materials softer than conventional elastomers. These polymers have emerged as pivotal materials in advanced 3D printing, enabling solvent-free fabrication of ultra-soft elastomers with biomimetic mechanical properties that mimic biological tissues.<sup>4</sup> To optimize printability, shape retention, and post-print functionality, precise engineering of their thermal properties and dynamics is essential.

The glass transition temperature ( $T_g$ ) is a fundamental thermal property of graft polymers that governs their printability.<sup>5</sup> It defines the temperature at which a polymer transitions from a rigid to a rubbery state, influencing the flow behavior, shape

retention, and post-print structural integrity in 3D printing.<sup>6</sup> Previous experimental studies have shown that  $T_g$  depends on both the chemical composition and the architectural arrangement of the backbone ( $N_{bb}$ ) and side chain ( $N_{sc}$ ) lengths.<sup>7,8</sup> Additionally, recent advances based on the generalized entropy theory (GET)<sup>9</sup> have demonstrated that the relative rigidities of the backbone and side chains critically influence the glass formation behavior in graft polymers.<sup>10</sup> These theoretical predictions, supported by molecular dynamics (MD) simulations<sup>11</sup> and experimental studies,<sup>12</sup> reveal the nontrivial trends in  $T_g$ .

Besides the thermodynamic property  $T_g$ , the dynamical property, such as polymer diffusion in the melt state, is crucial to their processing, *e.g.* governing interlayer bonding in 3D printing, material homogeneity, and mechanical performance.<sup>13,14</sup> During extrusion-based 3D printing, molten polymer layers must interdiffuse to form entangled molecular networks and strong interlayer bonds.<sup>5</sup> The self-diffusion coefficient ( $D$ ) of a polymer is influenced by molecular weight, backbone rigidity, and side-chain length.<sup>15,16</sup> Shorter, flexible side chains generally promote faster diffusion by reducing entanglements, while longer, rigid side chains hinder diffusivity, increasing viscosity and reducing chain relaxation dynamics.<sup>15</sup>

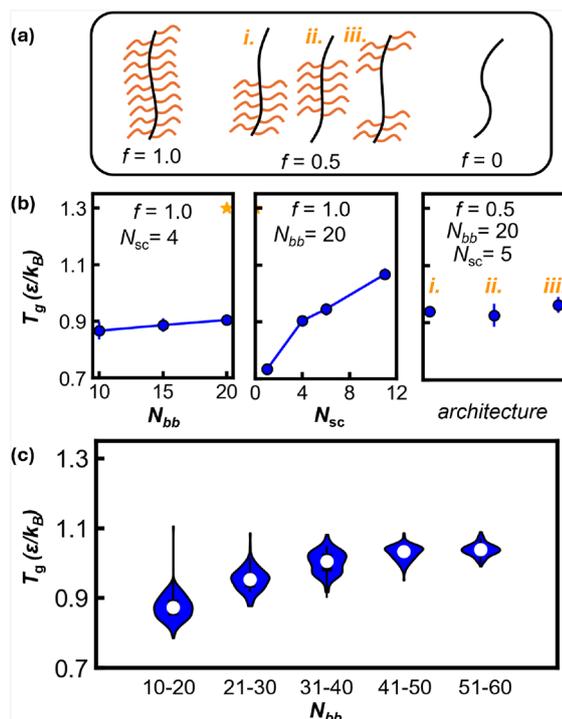
However, a comprehensive understanding of  $T_g$  and the diffusion of graft polymers is still lacking due to their diverse structures.<sup>7,17</sup> In this study, we address the long-standing challenge of predicting polymer thermal and dynamical properties based on their molecular architectures, driven by the highly nonlinear and complex structure–property relationships in polymers.<sup>18</sup> Despite extensive experimental and computational efforts,<sup>19–21</sup> the vast combinatorial space of backbone and side-chain configurations makes it difficult to establish generalizable design principles. The design parameters such as  $N_{bb}$ ,  $N_{sc}$ , grafting density ( $f$ ), and spatial positioning of side chains play a crucial role in shaping polymer behavior. A thorough investigation is carried out here by investigating 500 graft polymers with randomly placed side chains to understand how graft polymer architectures impact thermal and dynamic properties. By identifying key trends, we aim to establish a

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**Fig. 1** (a) Schematic representation of graft polymers is shown here for fully grafted ( $f = 1.0$ ) and partially grafted polymers ( $f = 0.5$ ) along with a linear polymer ( $f = 0$ ). For  $f = 0.5$ , three distinct side-chain architectures (*i.*, *ii.*, and *iii.*) are illustrated. (b) The variation of  $T_g$  is shown for  $f = 1.0$  and  $0.5$  with respect to backbone length ( $N_{bb}$ ), side-chain length ( $N_{sc}$ ), and side-chain architecture. The  $T_g$  of a classical linear polymer ( $f = 0$ ) is included as a reference (orange star). (c) The glass transition temperatures of 500 randomly generated graft polymers are plotted as a function of  $N_{bb}$ , capturing the broader distribution of  $T_g$  values across various molecular architectures.

framework for designing graft polymers with optimal thermal and dynamic performance.

We began by examining polymers with different grafting densities, including fully grafted bottlebrush polymers ( $f = 1.0$ ), partially grafted polymers ( $f = 0.5$ ), and classical linear polymers ( $f = 0$ ), as illustrated in Fig. 1(a). To investigate the influence of  $N_{bb}$  and  $N_{sc}$  on  $T_g$ , we simulated a total of 500 graft polymers, with 10 polymers at each value of  $f$  from 0.1 to 1.0 across five backbone-length blocks (10–20, 21–30, 31–40, 41–50, 51–60). The side-chain length is randomly generated. The value of  $T_g$  is obtained from density analysis as a function of temperature. More computational details are provided in Section S1 of the ESI.†

As shown in Fig. 1(b), left panel, the variation of  $T_g$  with backbone length is minimal for bottlebrush polymers with  $N_{sc} = 4$ , increasing only slightly from  $0.87$  to  $0.9 \epsilon/k_B$  as  $N_{bb}$  increases from 10 to 20. The slight impact of  $N_{bb}$  on  $T_g$  may be attributed to the narrow range of  $N_{bb}$  from 10 to 20. Besides,  $N_{sc}$  has a pronounced effect, as seen in Fig. 1(b), middle panel, where  $T_g$  increases from  $0.73$  to  $1.07 \epsilon/k_B$  as  $N_{sc}$  increases from 1 to 11 for a bottlebrush polymer with  $N_{bb} = 20$ . To establish a baseline comparison, we also computed  $T_g$  for a linear polymer, which is significantly higher ( $T_g = 1.3 \epsilon/k_B$ ) than that of

bottlebrush ones. This is consistent with the trend observed in experimentally synthesized bottlebrush polystyrene,<sup>7</sup> where, the  $T_g$  of bottlebrush polystyrene increases from  $37 \text{ }^\circ\text{C}$  to  $87 \text{ }^\circ\text{C}$  as  $N_{sc}$  increases from 2 to 8. The  $T_g$  values are found to be much smaller than those of linear polystyrene ( $90\text{--}110 \text{ }^\circ\text{C}$ ).<sup>22</sup>

Beyond  $N_{bb}$  and  $N_{sc}$ , we analyzed the effects of another key design parameter, the side-chain positioning, as illustrated in Fig. 1(b), right panel. The side chains are positioned at one end (*i.*), the center (*ii.*), and both ends (*iii.*), while keeping  $N_{bb} = 20$  and  $N_{sc} = 5$  constant. Differences in  $T_g$  among these architectures are minimal, consistent with experimental findings by Dearman *et al.*<sup>7</sup> Their synthesized bottlebrush polystyrene analogs, including types (*i.*), (*ii.*), and (*iii.*), showed a  $T_g$  variation of  $\leq 5 \text{ K}$ , supporting our results.

To examine the global trend in  $T_g$ , we plotted the variation of the average  $T_g$  as a function of  $N_{bb}$  in Fig. 1(c). The results show that  $T_g$  increases progressively as  $N_{bb}$  increases from 10 to 40, beyond which it reaches a plateau (from 41 to 60), indicating that further backbone elongation has little impact on  $T_g$ . These results demonstrate that the glass transition temperature of graft polymers is strongly influenced by both  $N_{sc}$  and  $N_{bb}$ , with  $N_{sc}$  playing a more dominant role at low  $N_{bb}$ . While increasing  $N_{bb}$  leads to a moderate rise in  $T_g$ , this effect saturates beyond  $N_{bb} = 40$ . In contrast, longer side chains significantly enhance  $T_g$ , suggesting that side-chain flexibility and steric effects play a crucial role in determining the thermal behavior of these polymers, as evident from literature based on the GET framework.<sup>10,11</sup> The influence of chain rigidity on  $T_g$  was further investigated by varying the angular force constant  $k_\theta$ , as detailed in Section S2 of the ESI.† Next, we examine the diffusivity of graft polymers in the melt state.

In classical polymer physics,  $D$  is inversely related to the hydrodynamic radius ( $R_h$ ) through the Stokes–Einstein relation.<sup>15</sup> Since  $R_h$  is proportional to the radius of gyration ( $R_g$ ) in polymeric systems ( $R_h/R_g \approx 0.9\text{--}1.0$ ),<sup>16</sup> we focus on the relationship between  $D$  and  $R_g$  here. These values are obtained from simulations run at  $T = 2.0 \epsilon/k_B$  specifically at the melt state of polymers.

Fig. 2(a) presents the variation of  $R_g$  for graft polymers compared to linear ones, where the backbone length of linear polymers varies from 10 to 90. By plotting the  $x$ - and  $y$ -axes of Fig. 2(a) in logarithmic scale, we computed the slope of the variation of  $R_g$  of linear polymers with changes in  $N_{bb}$ , resulting in a value of 0.66. This observed exponent is larger than that of an ideal random-walk polymer ( $R_g \propto N_{bb}^{0.5}$ ),<sup>15</sup> which can be attributed to the increased rigidity of the bead-spring model used in this work.

For polymers with  $f$  values of 0.5 and 1.0, the relationship between  $R_g$  and  $N_{bb}$  deviates significantly from the power-law trend observed for linear polymers. The dependence of  $R_g$  on polymer side-chain architecture is found to be scattered with no definite trend, particularly with respect to  $N_{sc}$  and its spatial distribution along the backbone. When  $N_{sc}$  is short (1 and 4), the  $R_g$  of bottlebrush polymers is smaller than that of a linear polymer with  $N_{bb} = 20$ , indicating a more collapsed polymer conformation due to attractive interactions between short side chains. As  $N_{sc}$  increases to 6,  $R_g$  becomes comparable to that of

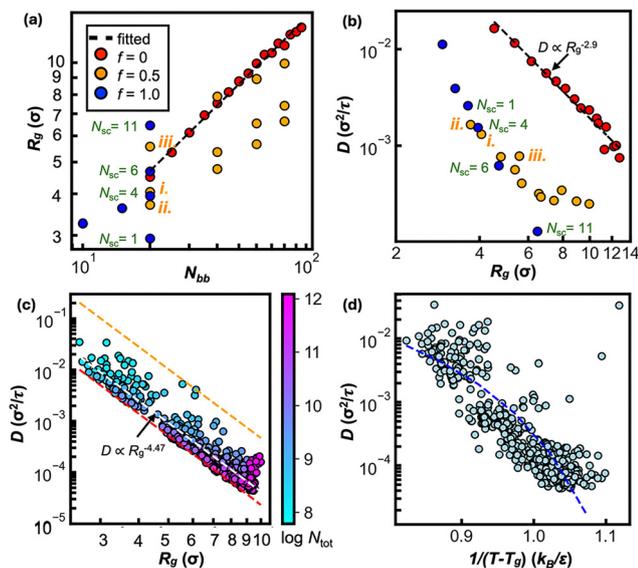


Fig. 2 (a) Radius of gyration ( $R_g$ ) of linear polymers ( $f = 0$ ) and graft polymers ( $f = 0.5, 1.0$ ). The dashed line represents a power law scaling as  $N_{bb}^{0.66}$ . (b) Self-diffusion coefficient ( $D$ ) of linear and graft polymers. The dashed line represents a power law scaling as  $R_g^{-2.9}$ . (c) The relationship between  $D$  and  $R_g$  of all the 500 graft polymers. The white dashed line represents the power scaling,  $R_g^{-4.47}$ . The red and yellow dashed lines are the lower and upper boundaries of the 500 data points. (d) The  $D$  vs.  $1/(T - T_g)$  relationship deviates far from the WLF equation with  $T_1 = 0$  (the blue dashed line).

a linear polymer, suggesting a transition from a collapsed to an expanded state. When  $N_{sc}$  further increases to 11, steric hindrance between the long side chains leads to an expanded conformation, where  $R_g$  exceeds that of a linear polymer. Apart from  $N_{sc}$ , the spatial placement of side chains also affects  $R_g$ . Among the three configurations analyzed in Fig. 1(a), graft polymers with configuration (ii.) exhibit the most collapsed structure, followed by configuration (i.), while configuration (iii.), where side chains are positioned at both ends, resulting in the most extended backbone conformation.

Next, we examine the relationship between  $R_g$  and  $D$  for linear and graft polymers. Note that the diffusion coefficient is computed from the mean-squared displacement of the polymer chain's center of mass, indicating that the diffusion discussed here refers to chain-level motion. We assume the behaviors of polymers in this study are in the unentangled regime because the maximum backbone length ( $N_{bb} = 60$ ) is less than the reported entanglement length  $N_e$  of 86.<sup>16,23</sup> As shown in Fig. 2(b), for linear polymers,  $D$  follows a power-law scaling as  $D \propto R_g^{-2.9}$ , which is comparable to  $D \propto R_h^{-2.7}$  reported in ref. 16. For graft polymers,  $D$  is significantly lower than that of linear polymers at the same  $R_g$ . While  $D$  decreases with increasing  $R_g$ , similar to linear polymers, the data points for graft polymers do not collapse onto a single power-law trend, indicating that a simple scaling relationship does not adequately describe their diffusivity. Fig. 2(c) and (d) reveal key deviations from classical scaling and transport theories in graft polymers. In Fig. 2(c), although an overall trend of  $D \propto R_g^{-4.47}$  is

observed, the significant spread in  $D$  at fixed  $R_g$  demonstrates a breakdown of universal diffusion-size relationships due to topological factors. Fig. 2(d) shows that  $D$  does not follow the expected behavior from the Williams-Landel-Ferry (WLF) equation,  $\log D = -C_1 \log D(T_1)/(C_2/(T - T_g + T_1) + 1)$  where  $C_1$  and  $C_2$  are constants,<sup>24</sup> as polymers with similar  $T_g$  exhibit diffusion rates differing by orders of magnitude, highlighting a decoupling between dynamic and thermodynamic properties enabled by architectural control.

The structural diversity introduced by side chains in our MD simulations leads to substantial variations in chain mobility, highlighting the need for a more comprehensive model to describe the diffusion behavior of graft polymers in the melt state.

Accurately predicting the  $T_g$  and  $D$  is therefore challenging due to their nonlinear structure-property relationships. To overcome this, we developed machine learning (ML) models trained on simulated polymer datasets. A key aspect here is the featurization strategy, which plays a critical role in model performance. We tested three types of polymer representations: (1) six physical descriptors, (2) eleven graphical descriptors,<sup>25</sup> and (3) two-dimensional grayscale images. Dense neural network (DNN) models were implemented for the first two feature sets, while convolutional neural networks (CNN) were developed for image-based representations (see Section S3 of ESI† for model descriptions).

Before training the ML models, we examined the correlation between physical and graphical descriptors to assess feature relevance. Fig. S3 (ESI†) presents the Spearman's rank correlation coefficients, where most of the physical and graphical descriptors are highly correlated with the four properties.

By utilizing the physical descriptors or the graphical descriptors, we trained DNN models for each of these properties. The hyperparameters of DNN models are optimized, *i.e.* the number of hidden layers, the number of hidden nodes, and the learning rate to improve the accuracy (see Section S3.2 of ESI†). The DNN model consisted of 4 hidden layers and each hidden layer contained 512, 1024, 512, and 32 hidden nodes. The learning rate is 0.001 and the activation function is rectified linear unit. The 10-fold cross-validation is used to get the average values of the  $R^2$  scores on testing datasets. The  $R^2$  scores of the DNN models by using the physical descriptors for predicting  $T_g$ ,  $R_g$ ,  $D$ , and  $\rho$  are shown in Fig. 3. All the  $R^2$  scores are more than 0.9, except for  $T_g$ . However, it is noted that though the  $R^2$  score for predicting  $T_g$  is 0.85, the root mean square error is found to be 0.025 as obtained from MD simulations. Overall, the DNN models trained on graphical descriptors perform slightly better than those trained on physical descriptors. This is because physical descriptors are limited in differentiating the configurations of graft polymers. For example, the configurations of (i.) (ii.) and (iii.) in Fig. 1(a) are represented by the same six physical descriptors.

Besides the physical and graphical descriptors, we used  $26 \times 60$  pixels (corresponding to maximum  $N_{sc}$  and  $N_{bb}$  in the dataset) grayscale images to represent graft polymers. Pixels in the matrix indicated different types of beads: black pixels (grayscale value = 0) denoted backbone beads, gray pixels

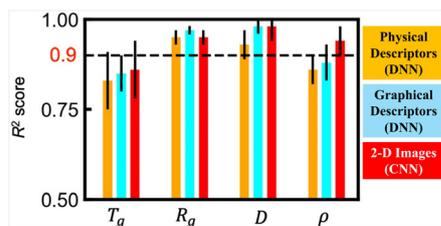


Fig. 3 The testing  $R^2$  scores for predicting  $T_g$ ,  $R_g$ ,  $D$ , and  $\rho$  are shown, with a dashed reference (in black) line at 0.9. Orange: DNN models trained on 6 physical descriptors; cyan: DNN models trained on 11 graphical descriptors; red: CNN trained against  $26 \times 60$  pixels grayscale images. Error bars indicate standard deviations from 10-fold cross-validation.

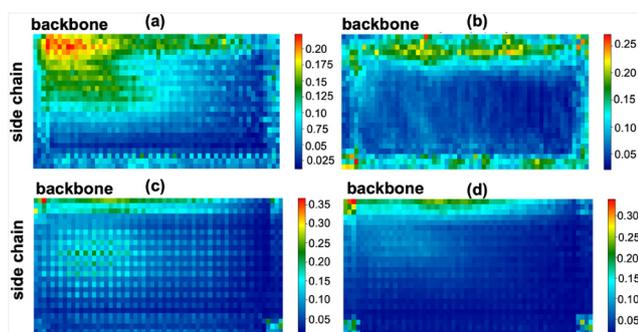


Fig. 4 The average saliency maps across all the 500 samples to show the consistent regions of the graft polymers critical for the four properties: (a)  $T_g$ , (b)  $R_g$ , (c)  $D$ , and (d)  $\rho$ . Colors in the colorbar denote the corresponding contribution values of each pixel in the graft polymer images.

(grayscale value = 127) represented side-chain beads, and white pixels (grayscale value = 255) indicated the absence of beads. A representative example of the image for a bottlebrush polymer ( $f = 1.0$ ) with a backbone length of 58 is shown in Fig. S4 of ESI.† The CNN models are trained on these images as the input. The convolutional and pooling layers are optimized (see Section S3.3 of ESI†). The  $R^2$  scores for  $D$ ,  $R_g$ , and  $T_g$  are comparable to that of DNN models (Fig. 3). The  $R^2$  score of the CNN model for predicting  $\rho$  is 0.94, much higher than that of the DNN model. The  $R^2$  score of our CNN model for predicting  $R_g$  is shown comparable to that of GNN models, employed in Jiang *et al.*<sup>25</sup>

To gain new insights and improve the interpretability of the CNN model, we plotted the saliency map (Fig. 4) highlighting the spatial regions most influential to the CNN model predictions. For  $T_g$ , contributions are concentrated at the backbone and nearby side chains, while  $R_g$  is driven by both backbone and terminal regions of long side chains. In contrast,  $D$  and  $\rho$  are primarily influenced by the backbone, reflecting its role in governing steric effects and free volume. A detailed description of the map is given in Section S4 of the ESI.† Further discussion of the general design rules is provided in Section S5 of the ESI.†

In conclusion, our systematic investigation of 500 graft polymers demonstrates that  $T_g$ ,  $D$ ,  $R_g$ , and  $\rho$  are strongly influenced by the nonlinear interplay between backbone and side-chain architectures. These dependencies extend beyond the predictive capabilities of traditional polymer physics models, such as power

scaling laws and WLF functions. Notably,  $T_g$  and  $D$  respond differently to topological variations:  $D$  is highly sensitive to the positioning of side chains, whereas  $T_g$  is only marginally affected. This differential sensitivity results in a decoupling of  $T_g$  and  $D$ , thereby overcoming the intrinsic coupling observed in linear polymers that typically constrains the processing of materials with high  $T_g$  and low  $D$ . The ability to decouple  $T_g$  and  $D$  enables the rational design of polymers with reduced  $T_g$  yet maintained low diffusivity (high viscosity), or *vice versa*. Additionally, the machine learning models developed in this study accurately and efficiently predict  $T_g$  and  $D$ , facilitating the topological design of graft polymers to achieve targeted thermodynamic and dynamic properties. In the future, chemically specific models will be developed to guide experimental efforts in validating the ML predictions and synthesizing new graft polymers.

## Conflicts of interest

There are no conflicts to declare.

## Data availability

The data supporting this article have been included as part of the ESI.†

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