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# Efficient state-interaction approach for the $g$ -matrix analysis in high-spin molecules†

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We present an efficient state-interaction approach for evaluating  $g$ -shifts in high-spin molecular systems. Using a spin-orbit-coupled effective Hamiltonian with a restricted active space configuration interaction wavefunction, this method captures key excited-state contributions to  $g$ -shifts without requiring large orbital spaces, maintaining computational efficiency. Additionally, we introduce a property-driven algorithm to automatically select relevant orbitals, optimizing the active space selection. Application to diatomic and conjugated organic molecules demonstrates accuracy comparable to advanced methods, providing detailed insight into the origins of  $g$ -shifts. This methodology offers a flexible, efficient tool for exploring magnetic properties in complex molecules.

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## 1 Introduction

The understanding and prediction of magnetic properties in high-spin molecules are crucial for advancing applications in catalysis, magnetic materials, and biochemical processes.<sup>1–7</sup> High-spin, open-shell systems—characterized by an unpaired number of electrons and distinct populations of  $\alpha$  and  $\beta$  electrons in their outer orbitals—are found across many fields, including organic synthesis, organometallic catalysis, and materials science.<sup>8</sup> These reactive species are often studied using electron paramagnetic resonance (EPR) or electron spin resonance (ESR) spectroscopy, techniques that provide insights into molecular geometry and electronic configuration by probing interactions between unpaired electrons and external magnetic fields. Central to EPR analysis is the  $g$ -matrix, which defines the Zeeman splitting of spin states in an applied magnetic field, offering a window into the electronic structure and local environment of these molecules.<sup>9,10</sup>

The  $g$ -matrix encodes the effects of relativistic interactions, including contributions from spin-orbit coupling (SOC) and the electronic structure of the molecule, which collectively influence the response of electronic spins to an external magnetic field. Accurate determination of  $g$ -values is crucial for effectively characterizing complex systems. In the past,  $g$ -matrix calculations relied on semiempirical methods limited

to simplified models, with limited validity across system types. Since the 1990s, *ab initio* approaches, such as density functional theory (DFT) and wavefunction theory (WFT), have been increasingly applied to open-shell systems.<sup>11,12</sup> DFT methods typically treat the magnetic field perturbatively and offer efficiency, though they often depend heavily on functional choice and tend to underestimate  $g$ -values in transition-metal complexes.<sup>9,13,14</sup> In contrast, WFT methods can potentially handle high-spin states and transition metals with great accuracy by incorporating extensive electron correlation and relativistic effects, though at a higher computational cost.

Early work in WFT calculations at the Hartree-Fock (HF) level paved the way for increasingly sophisticated approaches in computing  $g$ -matrix parameters.<sup>15–19</sup> This initial work facilitated the extension of  $g$ -matrix calculations to post-HF methods, such as coupled-cluster (CC) response theory,<sup>20,21</sup> equations-of-motion coupled-cluster (EOM-CC),<sup>22</sup> and multi-configuration techniques including complete active space self-consistent field (CASSCF)<sup>23–25</sup> and restricted active space configuration interaction (RASCI).<sup>22</sup> These methods enable a targeted treatment of specific orbital spaces and capture essential electron correlation effects. Recent advancements, such as combining CASSCF with second-order perturbation theory (CASPT2), have shown that sum-over-states (SOS) techniques, when paired with high-quality wavefunctions, can produce reliable  $g$ -values for complex transition-metal systems.<sup>26,27</sup> Multi-reference configuration interaction (MR-CI) methods have similarly improved  $g$ -matrix accuracy by expanding state interactions through SOS formulations.<sup>28</sup> However, due to their computational intensity, MR-CI methods often become impractical for medium to large molecular systems.

Despite these advances, challenges remain, however, for high-spin systems with multiplicities beyond  $S = 3/2$ , where

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zero-field splitting effects might become significant and are challenging to capture using traditional DFT or low-level WFT approaches.<sup>29</sup> Addressing these systems requires sophisticated treatments of both dynamic correlation and SOC, particularly for heavy-element complexes where scalar-relativistic approximations are insufficient. For these cases, dynamic correlation and state-interaction approaches, capable of capturing spin-dependent interactions more comprehensively, are critical for accurately calculating the  $g$ -matrix. Consequently, as far as we are aware, few studies have attempted to evaluate the  $g$ -matrix computationally in high-spin molecules.<sup>29–31</sup>

In this study, we aim to advance  $g$ -matrix calculations in high-spin molecules by leveraging the advantages of state-interaction approaches. Unlike traditional response theory-based methods, state-interaction techniques allow for a more detailed decomposition of  $g$ -matrix shifts, offering unique insights into the underlying mechanisms. Specifically, they provide a granular analysis of contributions from SOC and transitions to excited states, making it possible to disentangle how each factor influences magnetic behavior. This capability is especially beneficial for high-spin compounds, where understanding the precise contributions from SOC and excitation energies is critical for accurate magnetic property predictions. By applying these methods across a series of systems with diverse electronic and SOC characteristics, we aim to refine computational strategies for  $g$ -matrix determinations, enhancing our understanding of the molecular factors driving magnetic properties in complex high-spin systems.

## 2 Theoretical background

### 2.1 Mapping between Zeeman and pseudospin Hamiltonians

Parametrization of the interaction between a high-spin molecular electronic state with an external magnetic field is typically done either by evaluating second order derivatives of the Zeeman splitting<sup>11,32</sup> or by mapping the real Zeeman Hamiltonian (eqn (1)) to an effective spin (or pseudospin) Hamiltonian (eqn (2)).<sup>26,31,33</sup>

$$\mathbf{H}_{\text{Zeeman}} = \beta_e \mathbf{B}^t (\mathbf{L} + g_e \mathbf{S}) \quad (1)$$

where  $\beta_e$  is the Bohr magneton,  $g_e$  is the free-electron isotropic  $g$ -factor,  $\mathbf{B}$  is the external magnetic field vector, and  $\mathbf{L}$  and  $\mathbf{S}$  are the electronic orbital and spin vector operators, respectively. In the high-field approach, *i.e.*, disregarding zero-field splitting contributions, and neglecting the interaction with nuclear spins, the pseudospin Hamiltonian is written as:

$$\tilde{\mathbf{H}}_{\text{spin}} = \beta_e \mathbf{B}^t \tilde{\mathbf{g}} \tilde{\mathbf{S}} \quad (2)$$

where  $\tilde{\mathbf{S}}$  is a pseudospin vector operator and the  $3 \times 3$  matrix  $\tilde{\mathbf{g}}$  contains the strength and anisotropy of the Zeeman splitting.

In the present work, we map the  $\tilde{\mathbf{H}}_{\text{spin}}$  to the Zeeman Hamiltonian expressed in the basis of electronic states belonging to the target multiplet of dimension  $M$ . Therefore, equating eqn (1) and (2) in the matrix representation of the pseudospin,

$\mathbf{S}$  and  $\mathbf{L}$  operators results in:

$$\tilde{\mathbf{g}} \tilde{\mathbf{S}} = \mathbf{L} + g_e \mathbf{S} = \mathbf{J} \quad (3)$$

Importantly, these multiplet states are obtained following a state-interaction approach<sup>22</sup> through the diagonalization of a SOC-dressed effective Hamiltonian (eqn (4)),

$$H_{IJ}^{\text{eff}} = E_I \delta_{IJ} + H_{IJ}^{\text{SO}} \quad (4)$$

where  $I$  and  $J$  denote nonrelativistic states with  $\{E_I\}$  eigenenergies, and  $H_{IJ}^{\text{SO}} = \langle I | H^{\text{SO}} | J \rangle$  is the SOC between  $I$  and  $J$  states. Such a state-interaction approach, also referred as quasi-degenerate perturbation theory (QDPT),<sup>9,25</sup> is limited by the truncation in the number of nonrelativistic states considered, that is, the dimension of the effective Hamiltonian. On the other hand, diagonalization of eqn (4) implies that second and higher order spin-orbit effects are included. The spin-orbit contribution to the perturbed Hamiltonian in eqn (4) can be incorporated using various approximations. Moreover, the state-interaction methodology enables the enhancement of results by refining the transition energies in eqn (4), either through the use of highly accurate computational methods or experimental values, as shown by Kähler *et al.*<sup>22</sup>

Extraction of the terms of the  $g$ -matrix is pursued by applying the projection technique introduced by Tatchen and coworkers,<sup>31</sup> which involves the projection of eqn (3) to individual components of the pseudospin,  $\tilde{\mathbf{S}}_i$ ,  $i = X, Y, Z$ ,

$$g_{ki} = \frac{\text{Tr}(\mathbf{J}_k \cdot \tilde{\mathbf{S}}_i)}{\text{Tr}(\tilde{\mathbf{S}}_i \cdot \tilde{\mathbf{S}}_i)} \quad (5)$$

where  $k = x, y, z$  indicate spatial indices, and by fixing the pseudospin operators to:

$$g_{zz} \tilde{\mathbf{S}}_Z = \mathbf{J}_z \quad (6)$$

$$g_{yy} \tilde{\mathbf{S}}_Y + g_{yz} \tilde{\mathbf{S}}_Z = \mathbf{J}_y \quad (7)$$

$$g_{xx} \tilde{\mathbf{S}}_X + g_{xy} \tilde{\mathbf{S}}_Y + g_{xz} \tilde{\mathbf{S}}_Z = \mathbf{J}_x \quad (8)$$

Details of the use of eqn (5)–(8) and the procedure to obtain the principal values of the  $g$ -matrix can be found elsewhere.<sup>31</sup>

### 2.2 Nonrelativistic wavefunction

Finally, selecting an appropriate electronic structure method to approximate the eigenstates of the nonrelativistic Hamiltonian and construct  $H^{\text{eff}}$  is crucial. For this purpose, we employ the RASCI method.<sup>34,35</sup> In RASCI, the electronic wavefunctions are generated by applying an excitation operator to a reference configuration, typically a Hartree–Fock determinant. In RASCI, the molecular orbital space is divided into three subspaces: RAS1, RAS2, and RAS3. The RAS2 subspace contains the key orbitals and electrons necessary to describe the ground and low-lying excited states of the molecule. RAS1 corresponds to the doubly occupied orbitals below the RAS2 space, while RAS3 represents the virtual orbitals above RAS2. The excitation operator acting on the reference configuration is expressed as:

$$\hat{R} = \hat{r}_0 + \hat{r}_h + \hat{r}_p + \hat{r}_{hp} + \hat{r}_{2h} + \hat{r}_{2p} + \dots \quad (9)$$



where  $\hat{r}_0$  accounts for all possible configurations of electrons within RAS2, while the remaining terms describe configurations involving an increasing number of holes (h) in RAS1 and particles (p) in RAS3. This framework allows for a natural and flexible description of the ground and low-lying states with different spin multiplicities, making it especially suitable for strongly correlated systems such as open-shell molecules or systems with near-degenerate states. The accuracy and computational efficiency of the RASCI wavefunction are determined by the size of the RAS2 space and the truncation of the excitation operator in eqn (9).

For the feasible application of RASCI in the calculation of  $g$ -shifts within the state-interaction framework, it is essential that the wavefunction accurately captures those nonrelativistic states contributing to the target electron spin multiplet while maintaining a moderate computational cost. Therefore, we chose a minimal RAS2 space, designed to describe the target spin multiplet  $M$  (where  $M = 2S + 1$ ), using  $M - 1$  electrons in  $M - 1$  orbitals. Additionally, we truncate the excitation operator to include only the first three terms on the right-hand side of eqn (9). We expect that including hole and particle excitations will efficiently account for the influence of the full set of molecular orbitals, allowing us to construct large effective Hamiltonians, *i.e.*, considering a wide range of excitations, without a significant increase in computational cost. The computational efficiency of the proposed method stems from employing a compact RAS2 space and truncating the excitation operator in eqn (9). As a result, the computational cost scales linearly with the size of the molecule and the basis set. This streamlined approach, which balances accuracy and efficiency, is more challenging to achieve in other multiconfigurational methods such as CASSCF.

Additionally, to optimize the RASCI wavefunction for calculating the  $g$ -matrix, we have developed an automated scheme to enhance the RAS2 space by identifying the most important states contributing to the shifts in the  $g$ -matrix relative to the free-electron spin ( $\mathbf{g} = g\mathbf{I} + \Delta\mathbf{g}$ ). Starting from a minimal RAS2 space, we expand it by incorporating relevant orbitals from RAS1 and/or RAS3. This is guided by the perturbative sum-over-states expression for evaluating the Zeeman/spin-orbit contributions to the  $\Delta g$  elements:<sup>13,36</sup>

$$\Delta g_{ki} = -\frac{2}{S} \sum_{I \neq 0} \frac{\langle 0 | L_k | I \rangle \langle 0 | h_i^{\text{SO}} | I \rangle}{E_I - E_0} \quad (10)$$

where  $S$  is the spin of the target state 0,  $\{I\}$  represents the set of nonrelativistic states spanning  $H^{\text{eff}}$ ,  $L_k$  is the  $k$ -th component of the angular momentum operator, and  $h_i^{\text{SO}}$  is the  $i$ -th Cartesian component of the mean-field SOC operator.<sup>37</sup> To facilitate the identification of relevant states, we estimate the contribution of individual states to the  $g$ -shifts using the following expression:

$$|\Delta g_{k \cdot}| = \frac{|\langle 0 | L_k | I \rangle| |\text{SOCC}(0, I)|}{E_I - E_0}, \quad k = x, y, z \quad (11)$$

where the dot ( $\cdot$ ) indicates an average over the second index *via*

the SOC constant (SOCC):

$$|\text{SOCC}(0, I)|^2 = \sum_{M_S, M'_S} |\langle 0 S M_S | H^{\text{SO}} | I S' M'_S \rangle|^2 \quad (12)$$

where  $H^{\text{SO}}$  is the total spin-orbit operator. The SOCCs enable us to account for the contributions from all microstates of the ground and excited states, effectively averaging over the pseudospin directions. In this study, we identify relevant excited states as those satisfying the criterion  $|\Delta g_{k \cdot}| \geq |\Delta g_{k \cdot}^{\text{max}}|/2$ , where  $|\Delta g_{k \cdot}^{\text{max}}|$  represents the maximum  $g$ -shift along the  $k$ -direction. Additional details regarding the selection threshold  $|\Delta g_{k \cdot}^{\text{max}}|$  are provided in Section 1.4 of the ESI†. Once these states are identified, the critical orbitals are selected based on their single-electron occupancies in configurations with the highest weights. Relevant configurations are defined as those with amplitudes at least 75% of the amplitude of the configuration with the largest value, ensuring that only the most significant contributions are considered in the analysis. Perturbative expansions have been previously utilized in CI wavefunctions to efficiently lower state energies, as in CIPSI and SORCI methods.<sup>38,39</sup>

### 3 Computational procedure

Calculations for the triplet states of diatomic molecules  $\text{O}_2$ ,  $\text{S}_2$ ,  $\text{NH}$ ,  $\text{NF}$ ,  $\text{NCl}$ , and  $\text{NBr}$  were conducted using experimental bond lengths.<sup>40</sup> For the remaining high-spin diatomic molecules, geometries were optimized using DFT with the BP86 exchange-correlation functional.<sup>29</sup> Molecular coordinates for the conjugated cyclic organic compounds, optimized at the B3LYP level and discussed in Section 4.2, were taken from ref. 31. Additionally, triplet state geometries of linear acenes, ranging from anthracene to hexacene, were optimized using the M06-2X energy functional<sup>41</sup> (ESI†).

The choice of molecular orbitals for constructing RASCI wavefunctions is a critical factor. In this study, RASCI calculations have been performed using the high-spin ROHF wavefunction corresponding to the target state as the reference configuration. Details of the employed RAS2 spaces are indicated in Section 4 and in the ESI† (in particular those following the  $g$ -driven automatic strategy in eqn (11)). Unless otherwise specified, the RASCI calculations utilize the full set of occupied and virtual orbitals, with no frozen orbitals. The only exception is for polyatomic conjugated organic molecules, where the 1s core electrons of carbon, oxygen, and nitrogen atoms were frozen, meaning they were excluded from the RAS1 orbital space. Second-order perturbative corrections to RASCI excitation energies, *i.e.*, RASCI(2),<sup>42</sup> of diatomic molecules in Table S2 (ESI†) have been computed with the Davidson-Kapuy partition of the Hamiltonian.

Spin-orbit interactions have been introduced by means of the Breit-Pauli spin-orbit Hamiltonian,<sup>43,44</sup> with a mean-field treatment of the two-electron terms,<sup>45</sup> following a recent implementation.<sup>46</sup> Scalar relativistic effects were not incorporated in the RASCI calculations.



Accurate calculation of  $g$ -matrix parameters necessitates the use of, at least, triple- $\zeta$  sets to give reliable results<sup>20</sup> and the inclusion of polarization functions to address the gauge dependence problem.<sup>17</sup> Consequently, the def2-TZVP basis set was employed for all  $g$ -shift calculations. Gauge dependency arises in  $g$ -matrix calculations due to the origin dependence of the angular momentum operator for finite basis sets. It is usually treated with gauge including atomic orbitals<sup>47</sup> or the selection of the center of electronic charge as the gauge origin,<sup>48</sup> being the latter a simple and effective way to treat this dependence. In our case, the gauge origin is placed at the center of nuclear charge, which, in non-ionic systems, appears to provide a reasonable approximation to the electronic charge center.<sup>26,33</sup> Unless indicated, all  $g$ -values are reported as  $g$ -shifts ( $\Delta g$ ) in parts per thousand (ppt). As indicated by eqn (5), within the state-interaction framework, the sign of the  $g$ -shift parameters is governed by the signs of the SOC and orbital angular momentum contributions. While a detailed exploration of this topic is beyond the scope of this work, the origin and uniqueness of the  $g$ -matrix sign are thoroughly discussed in the existing literature.<sup>49–53</sup>

Electronic structure calculations have been carried out using a developers version of Q-Chem 6.0.<sup>54</sup> CP-DFT calculations have been performed with ORCA 6.0.<sup>55–58</sup> Evaluation of the  $g$ -matrix parameters was carried out with in-house codes integrated within the PyQChem interface.<sup>59</sup>

## 4 Results and discussion

In the following, we apply our state-interaction approach to evaluate the  $g$ -matrix in a range of high-spin molecular species. Specifically, we assess the performance of RASCI in calculating  $g$ -shifts for diatomic molecules with high-spin ground states, as well as for spin-triplet states in conjugated polycyclic organic molecules.

### 4.1 Diatomic molecules

We begin our analysis by evaluating the impact of using a  $g$ -driven selected RAS2 orbital space ( $g$ -RAS2) and investigating the dependence of the results on the number of states included in the effective Hamiltonian. To this end, we consider a small set of diatomic molecules with a triplet ground state: O<sub>2</sub>, S<sub>2</sub>, NH, NF, NCl, and NBr. Table 1 presents the  $g$ -tensor shifts computed using various RASCI state-interaction approaches for

the selected ground-state spin-triplet diatomic molecules. The results are compared with experimental data and theoretical values obtained from MRSOCI,<sup>31</sup> coupled-perturbed CASSCF (CP-CASSCF)<sup>25</sup> and BP86<sup>29</sup> calculations, all of which also utilize a mean-field approximation to the full Breit–Pauli operator. RASCI and MRSOCI computations were performed using experimental bond lengths,<sup>40</sup> while CP-CASSCF and BP86 values were obtained at geometries optimized with the BP86 exchange–correlation functional.<sup>29</sup> Our focus is on the doubly degenerate  $g$ -tensor component perpendicular to the molecular axis ( $\Delta g_{\perp}$ ), which is typically reported in experiments. The parallel component is symmetry-forbidden in homonuclear diatomic molecules,<sup>60</sup> and tends to be small in heteronuclear diatomic compounds.

The homoatomic molecules O<sub>2</sub> and S<sub>2</sub> belong to the  $D_{\infty h}$  point group, with a triplet ground state  $X^3\Sigma_g^-$  characterized by two unpaired electrons in the degenerate  $\pi_x^*, \pi_y^*$  orbitals. Consistent with symmetry selection rules, the primary contribution to  $\Delta g_{\perp}$  arises from the interaction between the ground state and the lowest two-fold degenerate  $^3\Pi_g$  excited states. The RASCI-computed  $g$ -shifts for O<sub>2</sub> show excellent agreement with experimental results, while the computed shifts for S<sub>2</sub> are slightly lower than experimental values. In O<sub>2</sub>, only the lowest doubly-degenerated  $^3\Pi_g$  state significantly contributes to  $\Delta g_{\perp}$ , as convergence is achieved with just three states ( $X^3\Sigma_g^-$  and  $1^3\Pi_g$ ). Increasing the number of states in the effective Hamiltonian does not alter the results, as confirmed by the individual state contributions shown in Fig. 3. In contrast, expanding the RAS2 space by including additional orbitals to better describe the  $X^3\Sigma_g^-$  and  $1^3\Pi_g$  states using the  $g$ -driven RAS2 expansion technique leads to a slight improvement in the computed values. Starting with the minimal RAS2 orbital space required to describe the ground state triplet, consisting of two electrons in the two  $\pi$ -orbitals (min-RAS2), we employ the  $g$ -driven RAS2 expansion technique to automatically generate an improved fully correlated orbital space (Fig. 1). In this case, the primary contributions to  $\Delta g_{\perp}$  (in the  $x$ - and  $y$ -directions) arise from  $\sigma_{p_z} \rightarrow (\pi_x^*, \pi_y^*)$  excitations. Consequently, the  $g$ -driven RAS2 space is extended to include four electrons within the  $\pi_x^*, \pi_y^*$ , and  $\sigma_{p_z}$  orbitals.

The magnitude of  $\Delta g_{\perp}$  in S<sub>2</sub> is significantly larger than in O<sub>2</sub>, due to the stronger SOC arising from the higher atomic number of sulfur. The minimal RASCI approach, which uses a three-state Hamiltonian and a restricted RAS2 space (two electrons in

**Table 1** Calculated  $\Delta g_{\perp}$  values (in ppt) for diatomic molecules obtained with the RASCI methodology using a different number of states (indicated as  $[N]$ , with  $N \times N$  the size of the effective Hamiltonian) and active spaces, and compared to MRSOCI,<sup>31</sup> CP-CASSCF,<sup>25</sup> BP86<sup>29</sup> and experimental<sup>29</sup> values. In all cases,  $g$ -driven RAS2 space contains 4 electrons in 3 orbitals

Molecule	min-RAS2[3]	min-RAS2[100]	$g$ -RAS2[3]	$g$ -RAS2[100]	MRSOCI	CP-CASSCF	BP86	Exp.
O <sub>2</sub>	2.8	2.8	2.9	2.9	2.7	2.9	3.1	2.9
S <sub>2</sub>	11.2	11.8	11.8	12.5	12.9	13.0	12.1	14.5
NH	1.4	1.4	1.4	1.4	1.3	1.2	1.5	1.7
NF	0.9	1.0	1.2	1.3	1.8	1.7	2.0	2.0
NCl	3.2	3.4	3.8	4.0	4.8	4.4	5.0	5.4
NBr	11.0	11.1	14.0	13.1	16.4	14.6	21.8	19.3



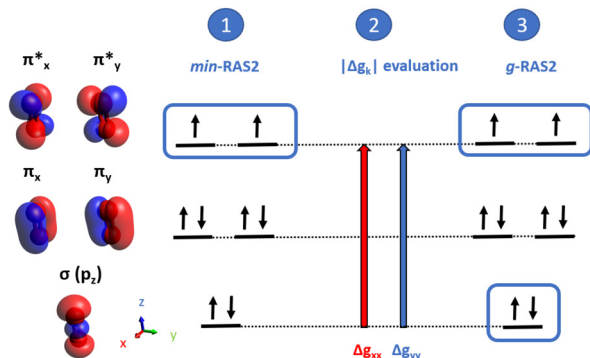


Fig. 1 Scheme of the  $g$ -driven RAS2 expansion technique in  $O_2$ , using (2,2) active space in min-RAS2 and increasing it to (4,3) in  $g$ -RAS2.

the  $\pi_x^* \pi_y^*$  orbitals), underestimates the experimental value by 23%. However, increasing the size of the RAS2 space and including additional electronic states in the effective Hamiltonian substantially improves the accuracy, yielding results comparable to those from MRSOCI and CP-CASSCF calculations.

Heteroatomic molecules NH, NF, NCl, and NBr belong to the  $C_{\infty v}$  point group and have a  $X^3\Sigma^-$  spin-triplet ground state. Deviations from the free-electron Landé factor in the direction perpendicular to the molecular bond axis are induced by SOC with the doubly degenerate  $^3\Pi$  state. RASCI-computed  $g$ -shifts follow the experimental trend along the NX series ( $H \sim F < Cl < Br$ ), but systematically underestimate the magnitude of the  $\Delta g_{\perp}$  values. Similar to the case of  $S_2$ , both the expansion of the RAS2 space and the inclusion of more electronic states in the SOC-dressed Hamiltonian in general lead to improved results compared to the minimal scheme (RAS2 with two electrons in two orbitals and a three-state SOC Hamiltonian). The expansion of the RAS2 space, however, has a more significant impact. The absolute error in the RASCI-predicted  $\Delta g_{\perp}$  increases with the atomic number of X, likely due to inaccuracies in the computed excitation energies and/or SOCs, and possibly to the increasing influence of scalar relativistic effects.

To further investigate the parameters determining the magnitude of the  $g$ -values in nitrogen monohalides, we analyze the excitation energies and SOCCs between the ground-state triplet and the excited triplet state  $^3\Pi$  that primarily contribute to  $\Delta g_{\perp}$  (Table 2). The increase in the computed  $g$ -shifts is driven by the simultaneous decrease in excitation energies and the increase

Table 2 Excitation energies to the  $^3\Pi$  state ( $\Delta E$  in eV) computed with B3LYP, EOM-CCSD and RASCI. RASCI  $X^3\Sigma^-/{}^3\Pi$  SOC constant (SOCC in  $\text{cm}^{-1}$ ) and perpendicular  $g$ -shifts (in ppt) calculated with the one-electron and total parts of the BP SOC Hamiltonian ( $\Delta g_{\perp}^1$  and  $\Delta g_{\perp}$ , respectively). All RASCI calculations have been done with a  $g$ -expanded RAS2 space (4 electrons in 3 orbitals) and with a three-state effective Hamiltonian

Molecule	$\Delta E$			SOCC	$\Delta g_{\perp}^1$	$\Delta g_{\perp}$
	B3LYP	EOM-CCSD	RASCI			
NF	7.70	7.07	7.13	56	1.9	1.2
NCl	5.52	5.10	5.04	102	5.2	3.8
NBr	4.89	4.50	4.35	315	16.2	14.0

in SOCs with the atomic number of the halogen atom. The RASCI excitation energies are generally lower than those obtained from TDDFT using the B3LYP functional and from equation-of-motion coupled-cluster singles and doubles (EOM-CCSD). This suggests that inaccuracies in the relative energies of triplet–triplet states are unlikely to be the primary cause of the systematic underestimation of  $g$ -shifts. Table 2 also presents  $g$ -matrix parameters obtained by considering only the one-electron part of the BP Hamiltonian ( $\Delta g_{\perp}^1$ ). A comparison of the total  $g$ -shifts reveals a decreasing two-electron contribution along the NF, NCl, and NBr series, consistent with the linear dependence of the one-electron SOC term on the atomic number  $Z$ . Since the two-electron SOC terms partially cancel the one-electron contribution,<sup>61</sup>  $\Delta g_{\perp}^1$  is consistently larger than the full  $\Delta g_{\perp}$ . Excluding the two-electron SOC terms yields  $g$ -values that are closer to the experimental results, likely due to a fortuitous cancellation of errors.

We next extend our study to a broader set of diatomic molecules with high-spin ground states ( $S = 3, 4, 6, 7$ , and 12). Table 3 presents the RASCI  $g$ -shifts obtained using a high-spin ROHF reference configuration, a  $g$ -driven RAS2 space and incorporating 30 electronic states in the SOC-dressed Hamiltonian. These results are compared to BP86 calculations<sup>29</sup> and experimental measurements. The excitation energies and the percentage of each configuration in each excited state using the min-RAS2, and the  $g$ -RAS2 approach with and without hole and particle configurations, are provided in the ESI† (Tables S2 and S3). Excluding hole and particle configurations systematically results in blue-shifted excitation energies, leading to reduced  $g$ -shifts. Furthermore, while min-RAS2 states predominantly exhibit contributions from hole and particle configurations,  $g$ -RAS2 states are mainly characterized by active configurations.

Table 3  $\Delta g$  values (in ppt) for high-spin molecules computed with RASCI methodology compared to BP86 and experimental values.<sup>29</sup> Absolute percent errors in parenthesis

Molecule	$2S + 1$	$g$ -RAS2[30]	BP86	Exp.
$O_2$	3	2.9 (0)	3.1 (7)	2.9
$S_2$	3	13.9 (4)	12.1 (17)	14.5
SeO	3	15.1 (54)	17.9 (45)	32.7
NH	3	1.4 (18)	1.5 (12)	1.7
NF	3	1.2 (40)	2.0 (0)	2.0
NCl	3	4.0 (26)	5.0 (7)	5.4
NBr	3	14.3 (26)	21.8 (13)	19.3
NI	3	1.8 (94)	38.9 (25)	31.0
$Ge_2^+$	4	-39.4 (38)	-49.2 (22)	-63.2
$GaAs^+$	4	-13.8 (189)	-20.3 (351)	-4.5
$V_2^+$	4	-54.7 (17)	-11.3 (76)	-46.3
CrH	6	-1.5 (44)	-4.6 (270)	2.7
CrF	6	-1.1 (15)	-11.0 (746)	-1.3
MnO	6	-3.2 (56)	2.5 (134)	-7.3
MnS	6	2.4 (64)	10.2 (52)	6.7
MnH	7	-1.9 (46)	-2.0 (54)	-1.3
MnF	7	-1.0 (23)	0.1 (108)	-1.3
MnCl	7	-1.8 (75)	0.9 (112)	-7.3
MnBr	7	-3.3 (65)	5.1 (155)	-9.3
MnI	7	-2.4 (74)	10.7 (215)	-9.3
$Mn_2^+$	12	-0.7 (79)	2.0 (161)	-3.3



In general, the RASCI errors are comparable to those obtained with BP86. However, an interesting trend emerges: for molecules with a triplet-spin ground state, the DFT errors are smaller than those from RASCI. Conversely, for higher-spin ground states ( $S \geq 6$ ), the RASCI results show better agreement with experimental data. This discrepancy may be attributed to the known limitations of KS-DFT functionals in accurately describing systems with near-degenerate ground states, whereas the optimized active space in our RASCI calculations helps capture these effects more effectively.

Certain systems exhibit significant deviations from the reference experimental values. Notably, for SeO, both RASCI and BP86 substantially underestimate  $\Delta g_{\perp}$ . Similar underestimations have been reported using the VWN local density approximation, the RPBE gradient-corrected functional,<sup>29</sup> and the PBE functional implemented with the effective potential method.<sup>30</sup>

The underestimation is even more pronounced in the case of NI, although the BP86 value slightly exceeds the experimental shift. Notably, the BP86 calculations by Patchkovskii and Ziegler<sup>29</sup> utilized Slater-type orbitals and incorporated scalar relativistic effects *via* relativistic frozen core potentials and the first-order Pauli Hamiltonian. To investigate the origin of this discrepancy, we performed additional CP-DFT/BP86 calculations. Using the same atomic basis set as in our RASCI computations (def2-TZVP), CP-DFT/BP86 yields a significant underestimation of  $\Delta g_{\perp}$  (1.9 ppt). However, the value increases substantially to 35.2 ppt when the ANO-RCC basis set is employed.<sup>62</sup> Analysis of the contributions to  $\Delta g$  reveals that this increase arises from the cross term between the orbital Zeeman and spin-orbit coupling interactions,<sup>63</sup> a contribution also captured in our approach. These results underscore the crucial role of the basis set in accurately calculating  $g$ -shifts, particularly for molecules containing heavy elements such as iodine.

In GaAs<sup>+</sup>, the ground state  $X^4\Sigma^-$  exhibits the strongest spin-orbit interaction with the doubly degenerate  $^4\Pi$  state, which have an excitation energy of 3.42 eV. Considering only these three states ( $g$ -RAS2[3]) yields  $\Delta g_{\perp} = -9.6$  ppt. Replacing the  $g$ -RAS2 computed energy (3.42 eV) with the CASSCF energy reported by Balasubramanian (6.46 eV)<sup>64</sup> in the 3-state effective SOC-dressed Hamiltonian reduces the shift to  $\Delta g_{\perp} = -5.1$  ppt. This indicates that the overestimation of the  $g$ -shift in this case arises primarily from an underestimation of the quartet-quartet excitation energy.

## 4.2 Conjugated cyclic organic molecules

We next apply our methodology to the characterization of  $g$ -parameters in the lowest triplet state of neutral organic conjugated molecules. In these larger systems, the increased density of electronic states compared to diatomic molecules means that higher-energy or multiple excited states can significantly influence the interaction between electronic spins and an external magnetic field. To begin, we analyze three conjugated carbonyl compounds: 1,4-benzoquinone (also known as *p*-benzoquinone), benzophenone, and fluorenone. These molecules feature low-lying  $\pi\pi^*$  and  $n\pi^*$  states with significant SOCs, in agreement with the El-Sayed rules.<sup>65</sup> Following this, we explore the triplet state of the simplest polycyclic aromatic hydrocarbon, naphthalene, and examine the effects of nitrogen substitution in quinoline. The computed  $g$ -values are presented in Table 4, alongside DFT/MRSOCI results<sup>31</sup> and experimental data, when available, for comparison.

The ground-state singlet of *p*-benzoquinone exhibits an optimized geometry that belongs to the  $D_{2h}$  symmetry point group. Upon geometry optimization on the lowest triplet state PES, the molecule retains its planarity but reduces its symmetry to  $C_{2v}$  due to a pseudo-Jahn-Teller distortion involving several nearly degenerate electronic states.<sup>70</sup> At the PES minimum, the  $T_1$  state belongs to the  $^3A_2$  irreducible representation and

**Table 4**  $\Delta g$  values (in ppt) for polyaromatic molecules computed with RASCI methodology and compared with the DFT/MRSOCI<sup>31</sup> and experimental values. Details of  $g$ -RAS2 can be found in the ESI

Molecule		min-RAS2[30]	$g$ -RAS2[30]	min-RAS2[500]	DFT/MRSOCI	Exp. <sup>a</sup>
<i>p</i> -Benzoquinone	$\Delta g_{xx}$	3.01	3.08	2.83	2.38	2.18
	$\Delta g_{yy}$	0.10	0.16	0.64	0.55	1.18
	$\Delta g_{zz}$	12.69	10.83	12.46	44.40	7.62
Benzophenone	$\Delta g_{xx}$	3.08	3.04	3.04	2.73	-0.22, -2.92
	$\Delta g_{yy}$	0.16	0.13	0.55	0.31	-1.42, -3.32
	$\Delta g_{zz}$	12.30	9.75	12.25	12.10	8.28, 7.38
Fluorenone	$\Delta g_{xx}$	0.01	0.01	0.01	0.01	—
	$\Delta g_{yy}$	0.04	0.29	0.66	0.94	—
	$\Delta g_{zz}$	0.40	1.29	0.79	2.30	—
Naphthalene	$\Delta g_{xx}$	0.09	0.48	0.40	0.21	0.68
	$\Delta g_{yy}$	0.01	0.08	0.45	0.29	0.68
	$\Delta g_{zz}$	0.03	0.02	0.03	0.03	0.58
Quinoline	$\Delta g_{xx}$	0.28	0.25	0.51	1.23	1.68
	$\Delta g_{yy}$	0.16	0.01	0.45	0.41	0.58
	$\Delta g_{zz}$	0.01	0.01	0.01	0.02	-0.42

<sup>a</sup> Experimental values for benzophenone (ref. 66 and 67), benzoquinone (ref. 68), naphthalene and in quinoline (ref. 69).



exhibits a  $n\pi^*$  character (Fig. S2, ESI†).<sup>71</sup> The strongest component of the  $g$ -matrix, both experimentally observed and computationally predicted, lies along the two carbonyls bond axis ( $\Delta g_{zz}$ ). RASCI calculations for the  $g_{zz}$  shift, using the minimal RAS2 space, slightly overestimate the experimental value,<sup>68</sup> and the shift remains nearly invariant as the number of states is increased. The relatively large  $\Delta g_{zz}$  arises from the coupling of  $T_1$  with low-lying  $\pi\pi^*$  triplet states (Fig. S2 and Section 2.2 in the ESI†). Modifying the RAS2 space *via* the  $g$ -driven procedure improves the description of these critical states, resulting in better agreement with experimental data. Notably, the RASCI calculations do not suffer from the large overestimation of  $\Delta g_{zz}$  observed in DFT/MRSOCI calculations. This discrepancy may be attributed to the underestimation of energy gaps to low-lying  $^3\pi\pi^*$  states in DFT/MRSOCI, which artificially amplifies the  $g$ -shift. The primary contribution to the  $xx$ -component of the  $g$ -matrix arises from a  $^3B_2$  ( $\sigma\pi^*$ ) state (Section 2.2 in the ESI†). RASCI calculations using the minimal RAS2 space overestimate the experimental  $\Delta g_{xx}$  value. Increasing the size of the RAS2 space *via* the  $g$ -driven procedure does not significantly improve the results, and only a slight reduction in the overestimation is observed when a large number of states are included in the effective Hamiltonian. Similarly, the best results for  $\Delta g_{yy}$  are obtained when a large number of states are included in the state-interaction scheme.

The  $T_1$  state of benzophenone adopts a non-planar structure with  $C_2$  symmetry, which can be attributed to an out-of-plane bending distortion caused by the pseudo-Jahn–Teller effect. This distortion arises from the interaction between the lowest  $^3n\pi^*$  state and a low-lying  $^3\pi\pi^*$  state.<sup>31</sup> Our RASCI calculations identify the lowest triplet state as belonging to the  $A_2$  irreducible representation, with a strong  $n\pi^*$  character, consistent with the experimental assignment.<sup>72</sup> The performance of different RASCI approaches in evaluating  $g$ -shifts is similar to that observed in *p*-benzoquinone. The  $g$ -shift along the carbonyl bond axis ( $\Delta g_{zz}$ ), arising from the interaction between the ( $n\pi^*$ )  $T_1$  state and low-lying  $^3\pi\pi^*$  states, improves with an expansion of the  $g$ -driven RAS2 space. On the other hand,  $\Delta g_{yy}$  is more sensitive to the size of the effective SOC-dressed Hamiltonian (Section 2.2 in the ESI†).

Fluorenone belongs to the  $C_{2v}$  point group, with the  $T_1$  state corresponding to the  $^3B_1$  irreducible representation and having a  $\pi\pi^*$  character, as confirmed by experimental results.<sup>73</sup> In RASCI calculations, the main  $g$ -shift,  $\Delta g_{zz}$ , occurs along the carbonyl bond axis and arises from the interaction of the ground state with the  $^1^3B_2$  state ( $n\pi^*$ ,  $\Delta E = 3.02$  eV, SOCC = 44  $\text{cm}^{-1}$ ). The  $\Delta g_{yy}$  component results from interactions with high-energy  $^3A_2$  states ( $\sigma\pi^*$ ), such as the  $17^3A_2$  state, with  $\Delta E = 10.32$  eV and SOCC = 22  $\text{cm}^{-1}$ .

The optimized geometry of naphthalene on the  $T_1$  potential energy surface retains the  $D_{2h}$  symmetry of the ground-state singlet. At its energy minimum, the lowest triplet state exhibits a pristine  $\pi\pi^*$  character and belongs to the  $B_{2u}$  irrep. Compared to the three conjugated ketone molecules studied, the absence of heteroatom lone pairs ( $n$ ) in naphthalene results in  $g$ -values that are closer to the free-electron value, in agreement with the

El-Sayed rules.<sup>65</sup> In-plane  $g$ -shifts ( $\Delta g_{xx}$  and  $\Delta g_{yy}$ ) arise from the coupling of  $T_1$  with  $^3B_{1u}$  and  $^3A_u$  states, respectively, both of which have  $\sigma\pi^*$  or  $\pi\sigma^*$  character. The computed  $g$ -shifts underestimate experimental values, consistent with previous MRSOCI calculations by Tatchen *et al.*,<sup>31</sup> who suggested that this discrepancy could stem from the absence of first-order corrections (relativistic mass correction to the spin-Zeeman interaction, and the one- and two-electron spin-orbit Zeeman gauge corrections). However, our results indicate that, to achieve  $\Delta g_{xx}$  and  $\Delta g_{yy}$  values closer to experimental measurements within a state-interaction framework, a large number of excited states must be included in the effective Hamiltonian (eqn (4)), as demonstrated by calculations using a minimal RAS2 space (2 electrons in 2 orbitals) and 500 states. Conversely, RASCI calculations with various RAS2 spaces, even when including many excited states, underestimate the  $g$ -shift along the axis normal to the molecular plane. The primary contributions to  $\Delta g_{zz}$  originate from low-lying  $^3\pi\pi^*$  states. We tentatively attribute this discrepancy to limitations in the chosen wavefunction method, particularly the lack of dynamic correlation in RASCI with hole and particle excitations, as recently discussed in the computation of  $g$ -parameters for spin-doublet molecules.<sup>22</sup> This deficiency likely leads to overly large energy gaps between the  $T_1$  state and other excited  $^3\pi\pi^*$  states. For instance, the energy gap between the lowest triplet state and the  $^3\pi\pi^*$  state that predominantly contributes to  $\Delta g_{zz}$ , identified as  $1^3B_{3u}$ , is 1.98 eV when computed at the TDDFT/B3LYP level, significantly smaller than the RASCI value of 2.87 eV. However, substituting the RASCI energy with the B3LYP value in the  $g$ -RAS2[30] SOC-dressed effective Hamiltonian results in only a slight increase in the magnitude of the  $g$ -shift ( $\Delta g_{zz} = 0.031$  ppt). This minor adjustment does not fully account for the discrepancy with the experimental value, suggesting other factors may also contribute to the observed differences. Furthermore, it has been suggested that the mean-field approximation to the two-electron term in the Breit–Pauli Hamiltonian is inadequate for accurately describing SOCs between  $\pi\pi^*$  states.<sup>74</sup>

Quinoline in its lowest triplet state adopts a planar structure with  $C_s$  symmetry. Similar to naphthalene, it exhibits a  $\pi\pi^*$  character, though with a slightly distorted distribution of the two unpaired electrons, as observed in Fig. 2. The results

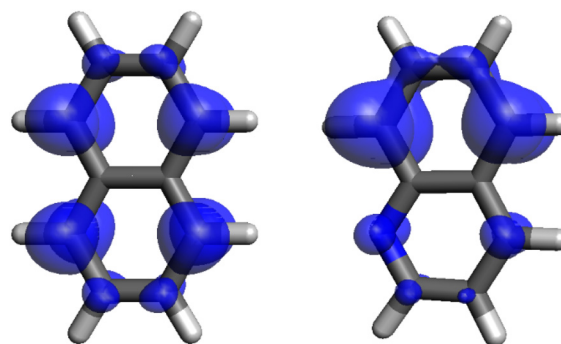


Fig. 2 Electron spin density distributions for the  $T_1$  state of naphthalene (left) and quinoline (right). Isosurface value: 0.005  $\text{Bohr}^{-3}$ .



obtained using various RASCI methods exhibit a performance comparable to that for naphthalene. As with naphthalene, accurately reproducing the magnitude of the  $g$ -shifts within the molecular plane requires the inclusion of high-lying triplet states with  $\sigma\pi^*$  and  $\pi\sigma^*$  character. However, the presence of a nitrogen atom in the quinoline backbone significantly increases the experimentally observed  $\Delta g_{xx}$  compared to naphthalene. This trend is only partially captured by the RASCI calculations (min-RAS2[500]). This discrepancy can be attributed to the overestimation of the energy gap between the  $T_1$  state and higher-energy contributing triplets. In RASCI, the lowest triplet state with notable  $\sigma\pi^*$  character and a sizable spin-orbit coupling constant (SOCC) of  $8.2 \text{ cm}^{-1}$  is calculated at an energy gap of  $7.3 \text{ eV}$ , while in DFT/MRSOCI, the first triplet above  $T_1$  appears at  $1.3 \text{ eV}$  with a larger SOCC of  $10 \text{ cm}^{-1}$ .

Benzophenone and *p*-benzoquinone exhibit their most significant contributions to the  $g$ -parameters in two states that are energetically closer to the ground state. As a result, an optimal description of these states, and consequently the  $g$ -shift, is achieved using the refined active space defined without requiring a large effective Hamiltonian. In contrast, fluorenone, naphthalene, and quinoline do not show a single dominant transition but rather a multitude of transitions that collectively influence  $\Delta g$ . For these molecules, the best description of the  $g$ -shift is attained within the initial active space, utilizing a larger number of states. Fig. 3 illustrates these transitions for benzophenone, naphthalene, and quinoline.

### 4.3 Linear acenes

Finally, we examine the performance of our approach in calculating  $g$ -values for linear acenes. This allows us to determine whether the trends observed in naphthalene extend to other polyaromatic hydrocarbons and to analyze the dependence of  $g$ -values on molecular size across the series from naphthalene to hexacene. Table 5 presents the  $g$ -tensor shifts for linear  $[n]$ acenes with  $n = 2-6$ , calculated using various RASCI approaches. We employed three orbital space configurations: a complete active space CI with 8 electrons in the 8 frontier  $\pi$ -orbitals (without additional hole or particle contributions), the minimal RAS2 space selection (2 electrons in 2 orbitals), and the system specific  $g$ -driven expanded RAS2 space. No comparable experimental or theoretical data is available, as studies on these molecules have focused only on their ionic structures.<sup>75-78</sup> Results are also compared with CPKS BP86 calculations,<sup>63</sup> which were performed variationally using a non-relativistic Hamiltonian. Scalar relativistic effects were not included, and the same basis set was used for consistency. For clarity, unlike previous sections, values in Table 5 are presented in part per million (ppm).

The DFT-computed  $g$ -shifts of naphthalene in the molecular plane,  $\Delta g_{xx}$  (short molecular axis) and  $\Delta g_{yy}$  (long molecular axis), show good agreement with experimental values (Table 4). Therefore, BP86 values for  $\Delta g_{xx}$  and  $\Delta g_{yy}$  will be used as reference points for evaluating our RASCI calculations in the remaining  $[n]$ acenes in the triplet state. Conversely, the DFT

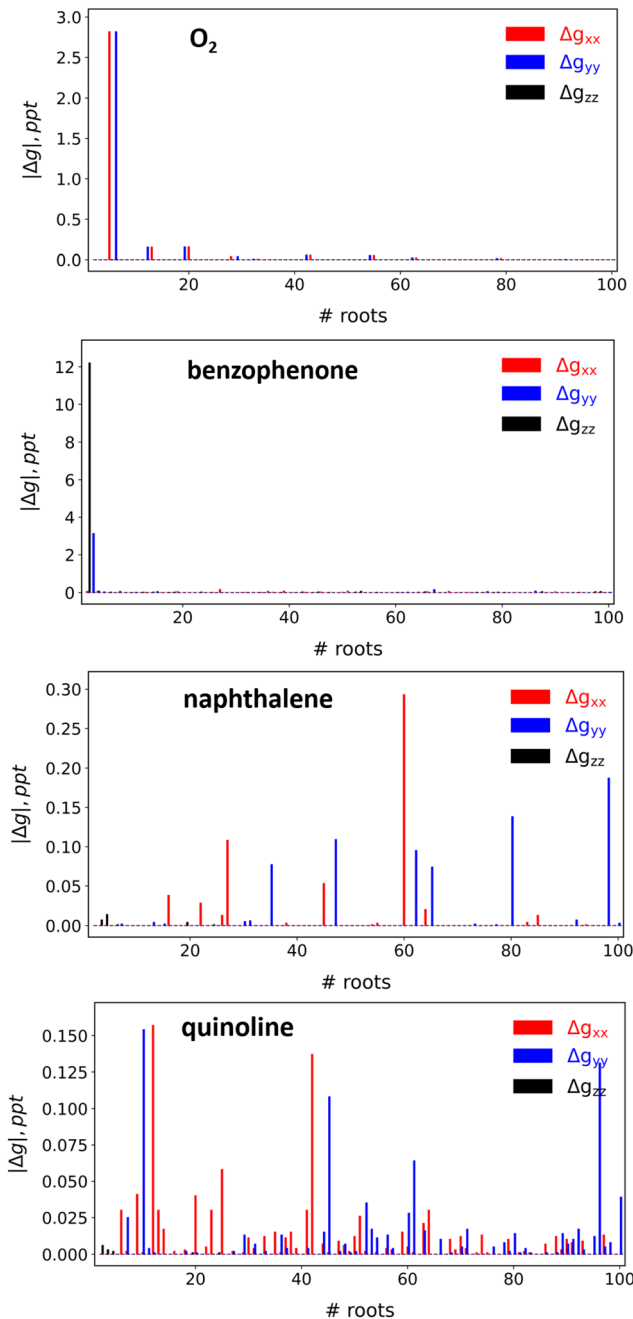


Fig. 3 Absolute values of the  $\Delta g$  components in two-state SOC-dressed Hamiltonians, the ground and a single excited state (# roots in the x-axis) for  $O_2$ , benzophenone, naphthalene and quinoline.

result for  $\Delta g_{zz}$  in naphthalene has an opposite sign to the experimental value and is an order of magnitude smaller.

As discussed for naphthalene, the  $g$ -shift component perpendicular to the molecular plane ( $\Delta g_{zz}$ ) is primarily influenced by interactions between  $T_1$  and other low-lying  $^3\pi\pi^*$  nonrelativistic states. Consequently, the CASCI values obtained with an active space limited to  $\pi$ -orbitals cannot be enhanced through the  $g$ -driven automatic orbital selection strategy or by expanding the effective Hamiltonian. The requirement to include states with  $\sigma\pi^*$  and  $\pi\sigma^*$  character to achieve significant



**Table 5** Main component  $\Delta g$  values (in ppm) for lowest triplet state of linear acenes computed with RASCI with various RAS2 spaces and number of states, and with the BP86 exchange–correlation functional

<i>n</i>		$\pi$ -CASCI[30]	min-RAS2[30]	<i>g</i> -RAS2[30] <sup>a</sup>	min-RAS2[500]	BP86
2	$\Delta g_{xx}$	1	192	25	475	664
	$\Delta g_{yy}$	−1	159	−3	430	563
	$\Delta g_{zz}$	18	14	20	14	−56
3	$\Delta g_{xx}$	0	145	13	445	665
	$\Delta g_{yy}$	0	122	6	409	560
	$\Delta g_{zz}$	17	12	8	13	−41
4	$\Delta g_{xx}$	0	8	1	449	672
	$\Delta g_{yy}$	0	−20	−1	383	561
	$\Delta g_{zz}$	22	17	11	22	−31
5	$\Delta g_{xx}$	0	84	2	425	677
	$\Delta g_{yy}$	0	89	2	406	545
	$\Delta g_{zz}$	18	11	9	15	−26
6	$\Delta g_{xx}$	0	6	1	508	686
	$\Delta g_{yy}$	0	−14	−0	382	541
	$\Delta g_{zz}$	19	12	1	17	−24

<sup>a</sup> Details on the RAS2 space given in the ESI.

$xx$  and  $yy$  shifts becomes evident in the vanishing CASCI values and the results from a minimal RAS2 space (min-RAS2[30] and min-RAS2[500] in Table 5). To fully capture these contributions, a broad manifold of excited states is essential. Additionally, the convergence of the state-interaction approach may necessitate an even larger number of excited states as molecular size increases (Fig. S13, ESI<sup>†</sup>), owing to the higher density of states.

Notably, the difference between  $\Delta g_{xx}$  and  $\Delta g_{yy}$  relative to BP86 shifts grows with the increasing number of six-membered rings. Specifically,  $\Delta g_{xx}$  increases with the length of the molecules, while  $\Delta g_{yy}$  remains relatively constant across the series. This trend aligns with the expected rise in anisotropy between the  $x$  and  $y$  directions as the molecular length increases. The RASCI method, using a minimal RAS2 space and a large-dimension state interaction scheme, yields in-plane  $g$ -shifts of similar magnitude to those obtained with DFT. However, it does not capture the increasing anisotropy between the short and long molecular axes with the molecular size.

## 5 Conclusions

We have developed a general methodology for efficiently evaluating  $g$ -shifts in molecular systems with any spin multiplicity, leveraging a state-interaction approach to construct a SOC-dressed (effective) Hamiltonian from nonrelativistic states obtained with the RASCI wavefunction. Our method incorporates both hole and particle configurations, allowing for a focused analysis of excited-state contributions to the  $g$ -matrix. By circumventing the need for extensive complete active spaces, this approach maintains computational efficiency while achieving accurate results. Importantly, our method enables a detailed dissection of  $g$ -shifts by analyzing the couplings between target nonrelativistic spin multiplets in terms of excitation energies, SOC effects, and transition angular moments.

Overall, our strategy has proven to be a viable approach for evaluating and characterizing  $g$ -shifts. Our results for a range of diatomic molecules show very good agreement with both high-

accuracy methods and experimental data, demonstrating the effectiveness of our approach. In these systems,  $g$ -values depend on contributions from a limited set of excited states, simplifying their computational characterization. Larger molecules, such as conjugated organic compounds, however, often feature numerous low-lying electronic excited states with significant spin–orbit interactions with the ground state, and a broader set of excited states might substantially contribute to the overall  $g$ -shifts. In these cases, the methodology benefits from larger effective Hamiltonians, as the  $g$ -shifts are the cumulative result of numerous contributions. We observed that discrepancies in accuracy of  $g$ -values of conjugated organic molecules in the  $T_1$  state may arise from errors in the computed energy gaps between nonrelativistic states and from variations in SOC magnitudes. For instance, the underestimation of  $\Delta g$  in some molecules primarily stems from overestimated energy gaps between the lowest triplet state and  $^3\pi\pi^*$  excited states.

While various strategies and algorithms have been developed for automatic active-orbital-space selection in multi-configurational wavefunctions, this work, to the best of our knowledge, represents the first instance of a property-driven automatic approach for constructing an active orbital space tailored for magnetic property calculations. This selection targets those orbitals critical for capturing the dominant contributions to the  $\Delta g$  values, further reducing computational demands. The RASCI framework is particularly well-suited to this approach, as it enables the exploration of orbitals' impact on electronic properties through hole and particle excitations beyond the RAS2 space. This property-driven scheme holds promise for extension to other electronic properties, an area we are actively investigating in our lab.

## Author contributions

A. C.-G. and D. C. jointly conceived and designed the project and developed the computational methodologies. A. C.-G. conducted the calculations and performed data analysis. Both authors collaborated in drafting and revising the manuscript, providing critical insights and edits throughout the writing process.

## Data availability

The data that supports the findings of this study are available within the article and its ESI.<sup>†</sup>

## Conflicts of interest

There are no conflicts to declare.

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