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First principles investigation of electron mobility enhancement of β -Ga₂O₃ doped with indium†

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β -Ga₂O₃ is one of the new-generation wide-bandgap semiconductor materials that has attracted much attention in recent years. However, the reported room-temperature electron mobility of β -Ga₂O₃ is much lower than GaN and SiC. Alloying Ga₂O₃ is expected to endow the material with superior carrier transport properties. Herein, we mainly investigate the electron mobility of pure Ga₂O₃, In-doped Ga₂O₃, and Al-doped Ga₂O₃ from first-principles considering acoustic deformation potential (ADP) scattering, polar optical phonon (POP) scattering and ionized impurity (IMP) scattering. The structure optimization, electronic band structure, and temperature-dependent and concentration-dependent electron mobility are investigated. The results show that the mobility of In-Ga₂O₃ is always the highest at 105–650 K, and POP scattering is the dominant factor limiting the electron mobility from 150–650 K. The mobility enhancement by In-doping is attributed to the smaller effective mass caused by the In 5s state despite its slightly increased electron–phonon coupling strength. The predicted electron mobilities for Ga₂O₃, Al-Ga₂O₃ and In-Ga₂O₃ at an electron concentration of $1.0 \times 10^{17} \text{ cm}^{-3}$ are $151.5 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$, $137.8 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$ and $184.9 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$ at room temperature, respectively. This work provides an alternative route to enhance the electron mobility of Ga₂O₃ and guides in engineering their electronic transport properties for high-power electronics.

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1. Introduction

Wide bandgap semiconductor materials, represented by gallium oxide (β -Ga₂O₃),¹ aluminum nitride (AlN),² and diamond,³ have become the most promising materials for the new generation of semiconductors. Their high bandgap ($> 4.5 \text{ eV}$)⁴ and high breakdown voltage ($> 1800 \text{ V}$)^{5,6} significantly expand the depth and breadth of applications in electronic and optical devices. β -Ga₂O₃ has gained market favor due to its high-quality substrates and large-scale substrate production capabilities,⁷ prompting in-depth exploration of performance optimization by the academic and commercial communities. In semiconductor devices, carrier transport properties are crucial as they determine the electrical performance. However, the reported room-temperature electron mobility of β -Ga₂O₃ remains below $200 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$,^{8–12} which is 1 to 2 orders of magnitude lower

than that of third-generation semiconductors like SiC, GaN, etc.,^{13,14} hindering the efficiency and application range of Ga₂O₃ devices. Alloying Ga₂O₃ is expected to endow the material with superior carrier transport properties.

Existing research showed that doping could change the carrier mobility of semiconductors. Considering only acoustic phonon (rather than polar phonon) scattering, Zhang found that by doping with Cu and Sn, the electron mobility of Ga₂O₃ was enhanced significantly from $847 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$ to $12409 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$ and $4217 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$,¹⁵ respectively. Focusing on a simplified model based on deformation potential scattering, Yu found that the electron mobility of Ga₂O₃ was reduced from intrinsic $283.8 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$ to $207.7 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$, $212.6 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$, and $187.3 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$ by doping with Si, Ge and Sn.¹⁶ Typically, the structure cells chosen for first principles calculation contain only several dozen atoms, in which even doping with one atom could result in heavy doping, leading to a band structure similar to that of metals or semimetals, when doping with elements that are not isoelectronic with Ga or O. In such cases, using a semiconductor model to calculate its electrical transport properties might not be accurate. Isoelectronic doping does not present this issue. Li calculated the impact of indium doping on the electrical properties of single-layer Ga₂O₃ metal–oxide–semiconductor field-effect transistors (MOSFETs) and discovered

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that the on-current for high-performance and low-power achieved great improvement at In doping concentrations of 5% and 20%.¹⁷ Using a chemical vapor deposition method, Tian found that In-doping enhanced the mobility of Ga₂O₃ nanobelts compared to pure Ga₂O₃, thereby improving the sensitivity and responsiveness of Ga₂O₃ photodetectors,¹⁸ consistent with Ji's experimental results.¹⁹ Both theoretical and experimental studies have shown that the electron mobility of Ga₂O₃ could be improved by doping with indium. However, the scattering mechanisms in In-doped Ga₂O₃ have not been thoroughly studied yet. Moreover, literature has indicated that Al, which belongs to the same group as In, reduced the mobility when doped in Ga₂O₃.^{20,21} It is worth noting that these two elements belonging to the same group contribute to completely different effects on Ga₂O₃. Therefore, this research aims to compare various properties of In-doped Ga₂O₃, pure Ga₂O₃ and Al-doped Ga₂O₃, and then to investigate the reasons behind In-doping enhancing the mobility of Ga₂O₃.

In this work, we emphasize the scattering mechanisms determining the electron mobility of Ga₂O₃, In-Ga₂O₃, and Al-Ga₂O₃, taking acoustic deformation potential (ADP) scattering, polar optical phonon (POP) scattering and ionized impurity (IMP) scattering fully into account. We computed the band structures and density of states for three different structures, as well as the necessary parameters for ADP, POP and IMP scattering. Additionally, we calculated the variations in ADP, POP, and IMP scattering between 105 and 650 K and their respective contributions to the total mobility. Lastly, we investigated the mobility enhancement mechanism of In-doped Ga₂O₃.

2. Computational methodology

There are two kinds of unequal Ga atoms in the lattice structure of β -Ga₂O₃, namely Ga_I with tetrahedral coordination and Ga_{II} with octahedral coordination, as shown in Fig. 1. We have calculated the doping formation energy of In and Al atoms substituting for Ga_I and Ga_{II}, from which we could conclude that Al atoms preferentially substitute for Ga_{II} atoms, while In atoms preferentially substitute for Ga_I atoms. All the DFT calculations were performed in the $1 \times 2 \times 1$ monoclinic Ga₂O₃ supercell using the Vienna *ab initio* simulation package (VASP) code.^{22,23} The generalized gradient approximation (GGA) involving the Perdew–

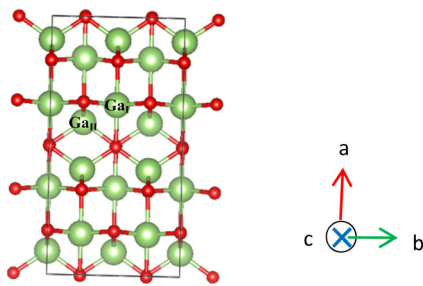


Fig. 1 Crystal structure of the Ga₂O₃ computational model. Green spheres represent cation antimony, and red spheres represent anion oxygen.

Burke–Ernzerhof (PBE)²⁴ functional was employed to describe the exchange correlation potential. The plane wave cutoff energy was set to 400 eV for all calculations. For the optimization and other property calculations, $3 \times 6 \times 7$ and $4 \times 7 \times 8$ Monkhorst–Pack k -points sampling were applied. These calculations were performed with 1×10^{-8} eV per atom energy tolerance and 0.01 eV Å⁻¹ force tolerance. To counteract the underestimation on the band gaps of GGA, and reproduce the correct band-structure of β -Ga₂O₃, the Heyd–Scuseria–Ernzerhof (HSE06) screened hybrid functional²⁵ was adopted to acquire the band structure as well, and the mixing parameter of 0.39 was set.

Based on the momentum relaxation time approximation, the electron mobility, μ_e , can be computed through the linearized Boltzmann transport equation (BTE),^{26–29}

$$\mu_{e,\alpha\beta}^{\text{MRTA}} = \frac{e}{n_e \Omega} \sum_{n\mathbf{k}} \int \frac{d\mathbf{k}}{\Omega_{\text{BZ}}} \frac{\partial f_{n\mathbf{k}}^0}{\partial \varepsilon_{n\mathbf{k}}} v_{n\mathbf{k},\alpha} v_{n\mathbf{k},\beta} \tau_{n\mathbf{k}} \quad (1)$$

where α and β denote Cartesian coordinates, n_e is the electron concentration, Ω and Ω_{BZ} are the volumes of the unit cell and first Brillouin zone, respectively, $v_{n\mathbf{k},\alpha}$ and $v_{n\mathbf{k},\beta}$ are the group velocity weight of band index n and wave vector \mathbf{k} , “ cb ” stands for conduction bands, $f_{n\mathbf{k}}^0$ is the Fermi–Dirac distribution function, $\varepsilon_{n\mathbf{k}}$ is the electron energy, and $\tau_{n\mathbf{k}}$ is the electron lifetime. Based on the self-energy relaxation time approximation (SERTA),²⁷ the electron lifetimes can be obtained according to

$$\tau_{n\mathbf{k}}^{-1} = \sum_m \int \frac{d\mathbf{q}}{\Omega_{\text{BZ}}} \tau_{n\mathbf{k} \rightarrow m\mathbf{k}+\mathbf{q}}^{-1} \quad (2)$$

where $\tau_{n\mathbf{k} \rightarrow m\mathbf{k}+\mathbf{q}}^{-1}$ is the scattering rate of the transition from state $|n\mathbf{k}\rangle$ to state $|m\mathbf{k}+\mathbf{q}\rangle$. Two classes of scattering are implemented in the work: (i) inelastic scattering which occurs *via* emission or absorption of a phonon and (ii) perfectly elastic scattering in which no energy is gained or lost. In the case of inelastic scattering, the partial decay rate can be written as^{30,31}

$$\tau_{n\mathbf{k} \rightarrow m\mathbf{k}+\mathbf{q}}^{-1} = \frac{2\pi}{\hbar} |g_{nm}(\mathbf{k}, \mathbf{q})|^2 \times \left[(n_{\mathbf{q}} + 1 - f_{m\mathbf{k}+\mathbf{q}}^0) \delta(\Delta \varepsilon_{\mathbf{k},\mathbf{q}}^{nm} - \hbar\omega_{\mathbf{q}}) + (n_{\mathbf{q}} + f_{m\mathbf{k}+\mathbf{q}}^0) \delta(\Delta \varepsilon_{\mathbf{k},\mathbf{q}}^{nm} + \hbar\omega_{\mathbf{q}}) \right] \quad (3)$$

where \hbar is the reduced Planck constant, $n_{\mathbf{q}}$ is the Bose–Einstein occupation, δ is the Dirac delta function, $\Delta \varepsilon_{\mathbf{k},\mathbf{q}}^{nm} = \varepsilon_{n\mathbf{k}} - \varepsilon_{m\mathbf{k}+\mathbf{q}}$, $|g_{nm}(\mathbf{k}, \mathbf{q})|^2$ represents the matrix element of the interaction, which measures the probability amplitude of the transition from an initial state $n\mathbf{k}$ to final state $m\mathbf{k}+\mathbf{q}$ *via* a phonon with wave vector \mathbf{q} and frequency $\omega_{\mathbf{q}}$. The $-\hbar\omega_{\mathbf{q}}$ and $+\hbar\omega_{\mathbf{q}}$ terms correspond to scattering by emission and absorption of a phonon, respectively. The scattering mechanism of POP belongs to inelastic scattering.³²

For elastic scattering, the partial decay rate can be written as

$$\tau_{n\mathbf{k} \rightarrow m\mathbf{k}+\mathbf{q}}^{-1} = \frac{2\pi}{\hbar} |g_{nm}(\mathbf{k}, \mathbf{q})|^2 \delta(\Delta \varepsilon_{\mathbf{k},\mathbf{q}}^{nm}) \quad (4)$$

The scattering mechanisms of IMP^{33,34} and ADP^{35–38} belong to elastic scattering. The matrix elements for ADP, IMP and POP are calculated, respectively. Before the total mobility can be obtained, the basic parameters are calculated firstly. These



include the ADP matrix parameters of the fully anisotropic acoustic deformation potential and elastic constants, POP matrix parameters including static (ϵ_s), high-frequency (ϵ_∞) dielectric constants and effective phonon frequency (ω_{po}), etc. Through Fourier interpolation in the first Brillouin zone to compute electron mobility by AMSET,²⁹ we can accurately evaluate the contribution of individual scattering mechanisms on a much-denser mesh of dimensions $13 \times 25 \times 27$ after convergence tests.

3. Results and discussion

3.1. Electronic band structure

The lattice parameters of Ga_2O_3 , $\text{Al-Ga}_2\text{O}_3$ and $\text{In-Ga}_2\text{O}_3$ are listed in Table 1. The calculated Ga_2O_3 lattice parameter results are in good agreement with the experimental data³⁹ (deviation less than 1.8%) and previous calculations,⁴⁰ demonstrating reliability of the employed theoretical methodology. $\text{Al-Ga}_2\text{O}_3$ has a slightly smaller lattice parameter, while $\text{In-Ga}_2\text{O}_3$ has a slightly larger lattice parameter, as Al atoms are smaller than Ga atoms while In atoms are larger than Ga atoms.

To explore the differences in energy band, electronic occupancy states, and effective electron mass between pure Ga_2O_3 and doped Ga_2O_3 , we performed calculations of the band structure, total density of states (TDOS), and partial density of states (PDOS). Fig. 2(a)–(c) present the electronic band structures of Ga_2O_3 , $\text{Al-Ga}_2\text{O}_3$ and $\text{In-Ga}_2\text{O}_3$ with a Brillouin zone path of G–F–Q–Z–G calculated using PBE (orange lines) and HSE (blue lines), respectively. This reveals that the electronic band structures predicted using PBE and HSE demonstrate the same dispersion shape, except for the bandgap values, which means that they have the equivalent effective mass closely related to the curvature of the band at the high symmetry point. The band gap of Ga_2O_3 (Fig. 2a) obtained using HSE and

PBE is 4.91 and 2.05 eV respectively. The gap between the bandgap calculated by HSE and the experimental results of 4.86 eV⁴¹ is very small. For $\text{Al-Ga}_2\text{O}_3$ (Fig. 2b), the band gap is 5.05 and 2.18 eV, respectively, while for $\text{In-Ga}_2\text{O}_3$ (Fig. 2c), the band gap is 4.77 and 1.93 eV, respectively. As HSE requires heavy computational resources, PBE is chosen to predict the carrier transport properties of these three Ga_2O_3 structures.

In this study, we only focus on the electron mobility. From the band diagram, it can be seen that the conduction band minimum (CBM) is located at the gamma point. The electron effective mass (m_c^*) is defined as:

$$\left(\frac{1}{m_c^*}\right)_{ij} = \frac{1}{\hbar^2} \frac{\partial^2 E_n(\vec{k})}{\partial k_i \partial k_j}, \quad i, j = x, y, z \quad (5)$$

where x , y , and z are the directions in the reciprocal space ($2\pi/a$), $E_n(\vec{k})$ is the dispersion relationship for the n -th electronic band. Using the effective mass calculator (EMC)⁴² and finite difference method, we have calculated the effective mass at CBM, as shown in Table 2. The effective masses of pure Ga_2O_3 along x , y , and z are 0.22, 0.23, and 0.21, which are close to the values reported in the literature of 0.22, 0.22, and 0.21.⁴⁰ The electron effective mass distributions reveal that the electron effective mass m_c^* is basically isotropic, consistent with the subsequent mobility calculations. The effective masses of $\text{Al-Ga}_2\text{O}_3$ are 0.24, 0.24, and 0.23, slightly higher than pure Ga_2O_3 , which is unfavorable for carrier transport; meanwhile the effective masses of $\text{In-Ga}_2\text{O}_3$ are 0.21, 0.22, and 0.21, slightly lower than pure Ga_2O_3 , which is beneficial for carrier transport.

The total density of states (TDOS) curves for pure Ga_2O_3 , $\text{Al-Ga}_2\text{O}_3$, and $\text{In-Ga}_2\text{O}_3$ are similar, as shown in Fig. 3. Near the valence band maximum (VBM), the states are mainly contributed by O 2p and Ga 3p states. The O 2p states are localized below VBM, leading to a flat valence band, bringing about large hole effective mass. The DOS near the CBM is very low, resulting in a steep conduction band, meaning Ga_2O_3 has small electron effective mass. Al 3s and Al 3p states have minimal contribution to CBM as shown in Fig. 3(b) and (d). In contrast, $\text{In-Ga}_2\text{O}_3$ shows slightly higher In 5s states near the CBM (3.5–5 eV), resulting in a higher TDOS, as shown in Fig. 3(c) and (e). However, in the region that determines the electron effective mass at the CBM (1.93–2.05 eV for $\text{In-Ga}_2\text{O}_3$, 2.06–2.15 eV for Ga_2O_3 , circled in red), the TDOS of $\text{In-Ga}_2\text{O}_3$ is

Table 1 Lattice constants of $\beta\text{-Ga}_2\text{O}_3$ compared with literature data

Lattice constant	<i>A</i>	<i>b</i>	<i>c</i>	β
Ga_2O_3 -expt. ³⁹	12.23	3.04	5.80	103.7
Ga_2O_3 -theory ⁴⁰	12.45	3.08	5.87	103.7
Ga_2O_3	12.32	3.07	5.70	103.69
$\text{Al-Ga}_2\text{O}_3$	12.30	3.07	5.68	103.64
$\text{In-Ga}_2\text{O}_3$	12.40	3.10	5.73	103.61

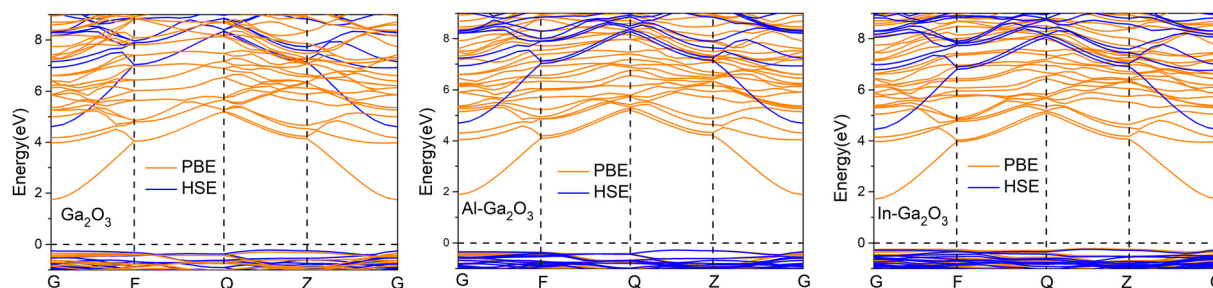


Fig. 2 Electronic band structures of pure Ga_2O_3 , $\text{Al-Ga}_2\text{O}_3$, and $\text{In-Ga}_2\text{O}_3$ calculated using PBE (orange lines) and HSE (blue lines) functionals.



Table 2 Electron effective mass of Ga₂O₃, Al-Ga₂O₃ and In-Ga₂O₃ compared with literature data

Structure	Electron effective mass (m_e^*/m_0)		
	m_{xx}^*	m_{yy}^*	m_{zz}^*
Ga ₂ O ₃ ⁴⁰	0.22	0.22	0.21
Ga ₂ O ₃	0.22	0.23	0.21
Al-Ga ₂ O ₃	0.24	0.24	0.23
In-Ga ₂ O ₃	0.21	0.22	0.21

the lowest caused main by the In 5s state, with less localization and a steeper CBM, resulting in a lower electron effective mass. The detailed TDOS of Ga₂O₃ and In-Ga₂O₃ near the CBM is shown in Table S1 (ESI[†]).

3.2. Electrical transport properties caused by ADP

Based on the electronic band structure, the scattering rate from ADP, POP, and IMP and the electron mobility could be calculated. Piezoelectric scattering was not considered as its proportion is very small. The electron mobility is calculated at moderate electron concentrations ($1 \times 10^{17} \text{ cm}^{-3}$). The methodology is introduced firstly for computing the transport properties, which enable us to discuss various factors influencing the electron mobility.

The ADP matrix element is given by²⁹

$$g_{nm}^{\text{ad}}(\mathbf{k}, \mathbf{q}) = \sqrt{k_B T} \sum_{\mathbf{G} \neq -\mathbf{q}} \left[\frac{\tilde{\mathbf{D}}_{nk} \cdot \hat{\mathbf{S}}_l}{c_l \sqrt{\rho}} + \frac{\tilde{\mathbf{D}}_{nk} \cdot \hat{\mathbf{S}}_{t1}}{c_{t1} \sqrt{\rho}} + \frac{\tilde{\mathbf{D}}_{nk} \cdot \hat{\mathbf{S}}_{t2}}{c_{t2} \sqrt{\rho}} \right] \times \langle m\mathbf{k} + \mathbf{q} | e^{i(\mathbf{q}+\mathbf{G}) \cdot \mathbf{r}} | n\mathbf{k} \rangle \quad (6)$$

where $\tilde{\mathbf{D}}_{nk}$ is a deformation potential tensor that describes how the electronic states respond to lattice vibrations, $\hat{\mathbf{S}}_l$, $\hat{\mathbf{S}}_{t1}$ and $\hat{\mathbf{S}}_{t2}$ represent the unit polarization vectors for the longitudinal acoustic mode (l) and two transverse acoustic modes ($t1$, and $t2$), respectively, and ρ represents the density of the material. The amplitude of the strain at any temperature T can be

obtained from the potential energy of the acoustic phonon as $\sqrt{k_B T / \rho c^2}$, where k_B is the Boltzmann constant. $\langle m\mathbf{k} + \mathbf{q} | e^{i(\mathbf{q}+\mathbf{G}) \cdot \mathbf{r}} | n\mathbf{k} \rangle$ is the overlap integral between state $|n\mathbf{k}\rangle$ and state $|m\mathbf{k} + \mathbf{q}\rangle$, where the factor $e^{i(\mathbf{q}+\mathbf{G}) \cdot \mathbf{r}}$ accounts for the phase factor associated with the phonon wavevector and reciprocal lattice vector.

The elastic constants (C) of pure Ga₂O₃ calculated in this study are 288.4 GPa, 412.6 GPa, and 401.7 GPa, slightly higher than the experimental values⁴³, as shown in Table 3. The deformation potential (D_A) and elastic constants of In-Ga₂O₃ are the smallest, while those of Al-Ga₂O₃ are the largest, with pure Ga₂O₃ falling in the middle. The value of D_A/C of In-Ga₂O₃ is the smallest, while in Al-Ga₂O₃ it is the largest. According to formula (6), g_{nm}^{ad} is proportional to D_A/C , indicating that In-Ga₂O₃ might have the smallest g_{nm}^{ad} . Detailed matrix of elastic constants and deformation potential are listed in the ESI[†].

Fig. 4a shows the temperature-dependent anisotropic mobility caused by only ADP scattering. The calculated mobilities differ by about 30% for the different directions, equivalent to the values observed in ref. 44. Besides, the mobility caused by ADP decreases with increasing temperature. According to formula (6), the scattering caused by deformation potential is positively correlated with temperature; as the temperature rises, deformation potential scattering increases, leading to a decrease in mobility. Fig. 4b shows the isotropically averaged mobility variation of Ga₂O₃, Al-Ga₂O₃, and In-Ga₂O₃ with temperature. The mobility of In-Ga₂O₃ is the highest when only ADP scattering is considered.

3.3. Electrical transport properties caused by POP

The POP differential scattering rate is given by:

$$g_{nm}^{\text{po}}(\mathbf{k}, \mathbf{q}) = \left[\frac{\hbar \omega_{\text{po}}}{2} \right]^{\frac{1}{2}} \sum_{\mathbf{G} \neq -\mathbf{q}} \left(\frac{1}{\hat{\mathbf{n}} \cdot \boldsymbol{\varepsilon}_{\infty} \cdot \hat{\mathbf{n}}} - \frac{1}{\hat{\mathbf{n}} \cdot \boldsymbol{\varepsilon}_s \cdot \hat{\mathbf{n}}} \right)^{\frac{1}{2}} \times \frac{\langle m\mathbf{k} + \mathbf{q} | e^{i(\mathbf{q}+\mathbf{G}) \cdot \mathbf{r}} | n\mathbf{k} \rangle}{|\mathbf{q} + \mathbf{G}|} \quad (7)$$

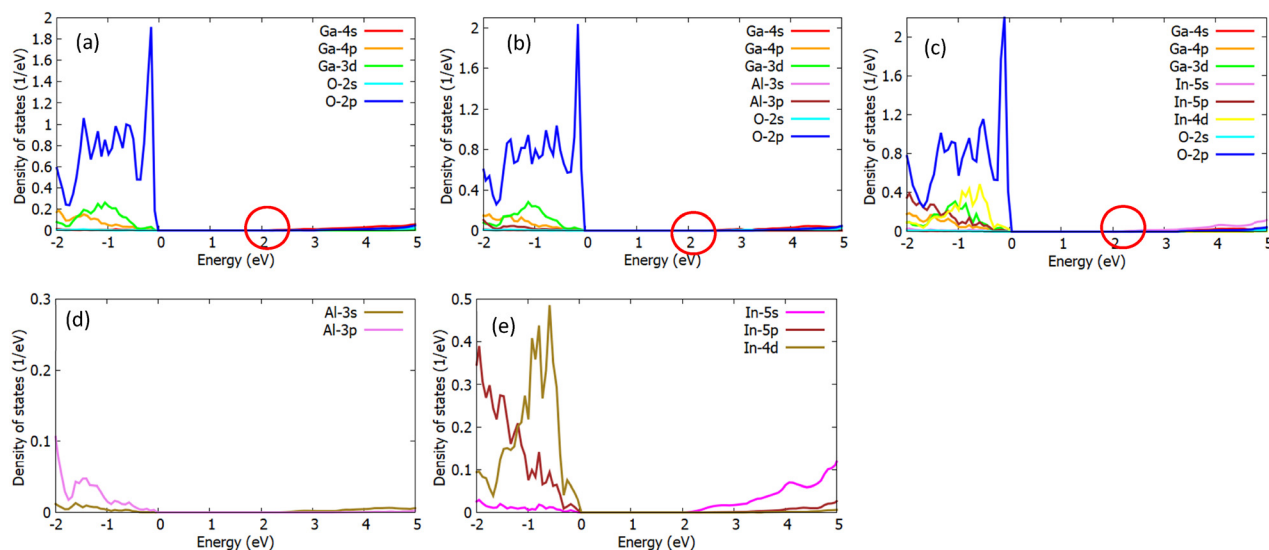
**Fig. 3** TDOS of pure Ga₂O₃ (a), Al-Ga₂O₃ (b), and In-Ga₂O₃ (c); PDOS of Al in Al-Ga₂O₃ (d) and PDOS of In in In-Ga₂O₃ (e).

Table 3 Elastic constants and deformation potential of Ga₂O₃, Al–Ga₂O₃ and In–Ga₂O₃ compared with literature data

	<i>C</i> (GPa)			<i>D_A</i> (eV)		
	<i>A</i>	<i>b</i>	<i>c</i>	<i>a</i>	<i>b</i>	<i>c</i>
Ga ₂ O ₃ -expt ⁴³	242.8	343.8	347.4	—	—	—
Ga ₂ O ₃	288.4	412.6	401.7	3.15	2.16	3.27
Al–Ga ₂ O ₃	295.8	419.0	406.5	3.29	2.36	3.30
In–Ga ₂ O ₃	281.8	403.9	385.2	2.88	2.17	2.93

where $\hbar\omega_{\text{po}}$ represents the frequency of the polar optical phonon mode, \hat{n} is a unit vector describing the direction of the phonon wavevector, while ϵ_{∞} and ϵ_s are the high-frequency and static dielectric tensors of the material, respectively. The

expression $\left(\frac{1}{\hat{n} \cdot \epsilon_{\infty} \cdot \hat{n}} - \frac{1}{\hat{n} \cdot \epsilon_s \cdot \hat{n}}\right)^{\frac{1}{2}}$ characterizes the difference in dielectric screening between high and low frequencies, influencing the strength of the long-range Coulomb interactions between electrons and phonons in polar materials.

In polar semiconductors, the charge carriers and the surrounding lattice deformation form a so-called polaron,⁴⁵ which determines the nature of carrier transport. Polarons can be classified into small and large ones based on the strength of electron phonon coupling. The lattice deformation in a large polaron is usually moderate and spreads over multiple unit cells, resulting in a larger mobility. The electron–phonon interaction is usually dominated by the coupling of charge carriers to the longitudinal optical phonons, which can be described within the Fröhlich model.⁴⁶ The coupling strength between electrons and polar optical phonons is quantified using the Fröhlich coupling constants^{32,47}

$$\alpha = \frac{1}{2} \frac{1}{4\pi\epsilon_0} \left(\frac{1}{\epsilon_{\infty}} - \frac{1}{\epsilon_s} \right) \frac{e^2}{\hbar\omega_{\text{po}}} \sqrt{\frac{2m_c^* \omega}{\hbar}} \quad (8)$$

where m_c^* is the CBM electron effective mass, and ϵ_0 is the vacuum permittivity. The above relevant material parameters of Ga₂O₃ are listed in Tables 2 and 5. The calculated α (shown in Table 4) shows the averaged value of 1.16, 1.25 and 1.17 for Ga₂O₃, Al–Ga₂O₃ and In–Ga₂O₃, which falls in the intermediate

electron–phonon coupling regime (defined as $0.5 \leq \alpha \leq 6$). The magnitudes of α for Ga₂O₃ and In–Ga₂O₃ are quite close, suggesting similar electron–phonon interaction strengths. We further estimate the size of polarons in Ga₂O₃, Al–Ga₂O₃ and In–Ga₂O₃, by the Schultz polaron radius (r_f).⁴⁷ The large values of electron polaron radius (which extend over multiple structural units) indicate that the polarons are delocalized in these Ga₂O₃. Al–Ga₂O₃ has the smallest Schultz Polaron radius while Ga₂O₃ has the largest one, suggesting that the Fröhlich coupling strength of In–Ga₂O₃ is slightly larger than Ga₂O₃, and smaller than that of Al–Ga₂O₃.

$g_{nm}^{\text{po}}(k, q)$ is proportional to the frequency of the polar optical phonon mode, ω_{po} , and inversely proportional to the electronic high-frequency dielectric constant, ϵ_{∞} . As ϵ_{∞} is much smaller than ϵ_s , the value of $\frac{1}{\hat{n} \cdot \epsilon_{\infty} \cdot \hat{n}} - \frac{1}{\hat{n} \cdot \epsilon_s \cdot \hat{n}}$ is almost equal to $\frac{1}{\hat{n} \cdot \epsilon_{\infty} \cdot \hat{n}}$.

For purposes of the screening, we assume that the high-frequency dielectric constant is isotropic. Indeed, our DFPT calculations (see Table 5) show that the high-frequency part of the dielectric tensor is nearly isotropic, with values ranging between 3.98 and 4.10 depending on the direction, close to the theoretical value.^{11,12} In contrast, the static dielectric tensor (ϵ_s) shows a stronger directional dependence, which is attributed to the anisotropic ionic contributions to the dielectric tensor in the monoclinic lattice. An averaged value of the computed ϵ_{∞} (4.05) is used for calculating $g_{nm}^{\text{po}}(k, q)$ of Ga₂O₃. This value is close to the experimental value of $\epsilon_{\infty} = 3.60$.⁴⁸ Besides, it is obvious that the ϵ_{∞} of In–Ga₂O₃ is the largest, and the ω_{po} of In–Ga₂O₃ is the smallest, indicating g_{nm}^{po} of In–Ga₂O₃ might be the smallest among these three structures according to formula (7).

We further analyze the individual contribution of POP scattering, as shown in Fig. 5. The mobility of Ga₂O₃, Al–Ga₂O₃, and In–Ga₂O₃ exhibits similar variation curves with temperature, in which the mobility of In–Ga₂O₃ by POP individual scattering is always the highest. μ_{POP} reduces monotonically as the temperature increases. Since as temperature further increases, more polar optical phonons are excited which can

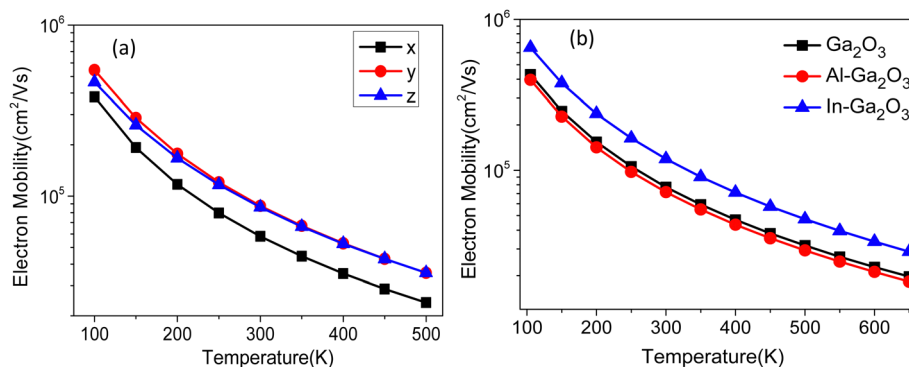
**Fig. 4** Temperature-dependent electron mobility of Ga₂O₃ along x, y, and z directions (a) and the isotropically averaged mobility variation of Ga₂O₃, Al–Ga₂O₃ and In–Ga₂O₃ (b) when only ADP scattering is considered.

Table 4 Calculated Fröhlich parameter (α) and Schultz polaron radius (r_f) for electrons in Ga₂O₃, Al-Ga₂O₃, and In-Ga₂O₃ at $T = 300$ K

	α			r_f (Å)		
	Ga ₂ O ₃	Al-Ga ₂ O ₃	In-Ga ₂ O ₃	Ga ₂ O ₃	Al-Ga ₂ O ₃	In-Ga ₂ O ₃
Average	1.16	1.25	1.17	145.8	138.1	142.3

induce a macroscopic electric field, thus strengthening the electron-phonon coupling.

3.4. Electrical transport properties caused by IMP

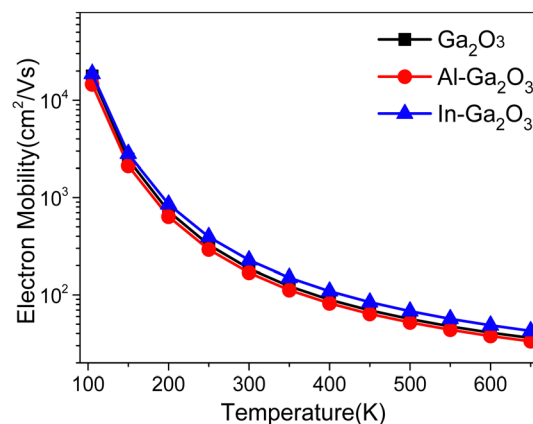
The ionized impurity matrix element is given by

$$g_{nm}^{ii}(\mathbf{k}, \mathbf{q}) = \sum_{\mathbf{G} \neq -\mathbf{q}} \frac{n_{ii}^{1/2} Ze \langle m\mathbf{k} + \mathbf{q} | e^{i(\mathbf{q}+\mathbf{G})\cdot\mathbf{r}} | n\mathbf{k} \rangle}{\hat{\mathbf{n}} \cdot \boldsymbol{\varepsilon}_s \cdot \hat{\mathbf{n}} |\mathbf{q} + \mathbf{G}|^2 + \beta^2} \quad (9)$$

where n_{ii} is the ionized impurity density, representing the concentration of the electron that contributes to the interaction. Ze is the charge of the ionized impurity, where Z is the atomic number of the impurity (or the number of charges), and e is the elementary charge. The factor $\hat{\mathbf{n}} \cdot \boldsymbol{\varepsilon}_s \cdot \hat{\mathbf{n}}$ modulates the strength of the Coulomb interaction due to screening effects. The denominator $|\mathbf{q} + \mathbf{G}|^2 + \beta^2$ accounts for the momentum transfer $\mathbf{q} + \mathbf{G}$ during scattering, with β representing a screening length parameter that modulates the range of the interaction.

As shown in Fig. 6a, the mobility due to IMP slightly increases with rising temperature because, as the temperature increases, the kinetic energy of electrons increases, causing them to move faster and spend less time near recombination centers, thereby reducing the probability of scattering. Besides, our research has shown that the mobility of In-Ga₂O₃ is always higher than that of pure Ga₂O₃ and Al-Ga₂O₃. This might be partly attributed to the larger ε_s of In-Ga₂O₃.

The electron concentration is varied from 10^{13} cm^{-3} to 10^{18} cm^{-3} to explore the concentration dependent electron mobility of Ga₂O₃, Al-Ga₂O₃ and In-Ga₂O₃, respectively, as shown in Fig. 6b. With electron concentration increasing from 10^{13} to 10^{16} cm^{-3} , the electron mobility of In-Ga₂O₃ slightly drops from $228.9 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$ to $211.7 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$ at 300 K, respectively, which indicates the electron mobility of In-Ga₂O₃ remains essentially stable. After that, a further increase in electron concentration (from 10^{16} to 10^{18} cm^{-3}) rapidly deteriorates electron mobility, from $211.7 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$ to $138.4 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$ at 300 K. This is caused by the strong scattering of excessive carrier concentration with electrons and phonons. According to formula (9), the scattering intensity is positively correlated with impurity

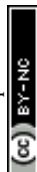
**Fig. 5** Temperature-dependent electron mobility of Ga₂O₃, Al-doped Ga₂O₃ and In-doped Ga₂O₃, where only POP scattering is considered.

concentration n_{ii} : the higher the impurity (electron) concentration, the greater the electron scattering intensity, which hinders movement and decreases mobility.

Based on Fig. 4b, 5 and 6a, in the temperature range of 105–150 K, μ_{IMP} is the lowest, indicating IMP scattering dominates the electron transport. In the temperature range of 150–650 K, μ_{ADP} and μ_{IMP} are much higher than μ_{POP} , indicating that POP scattering dominates the carrier transport of these three Ga₂O₃. Fig. 7 shows the effect of temperature on overall mobility, considering ADP, IMP, and POP together. Following Matthiessen's rule,⁵⁰ the total mobility μ_{total} is determined from $\mu_{\text{total}}^{-1} = \mu_{\text{ADP}}^{-1} + \mu_{\text{IMP}}^{-1} + \mu_{\text{POP}}^{-1}$. The total mobility is primarily determined by the smallest partial mobility. Overall, ADP has little effect on the total electron mobility. At low temperatures, impurity scattering significantly impacts the total electron mobility; as the temperature increases, optical phonon scattering gradually becomes the dominant scattering mechanism. The magenta curve in Fig. 7 shows the experimentally measured Hall mobility of pure Ga₂O₃,⁹ while the black curve represents the mobility of pure Ga₂O₃ calculated in this study. The high degree of overlap between these two curves indicates the reliability of the calculation method employed in this research. The overall mobility of In-Ga₂O₃ (blue curve) is the highest from 105 to 650 K, and the electron mobilities of Ga₂O₃, Al-Ga₂O₃ and In-Ga₂O₃ are $151.5 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$, $137.8 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$ and $184.9 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$ at 300 K. Since the effective mass of In-Ga₂O₃ is smaller than that of Ga₂O₃ and Al-Ga₂O₃, it still possesses higher mobility despite its slightly larger electron-phonon coupling strength.

Table 5 The parameters of POP scattering of β -Ga₂O₃ compared with literature data

Materials	ε_{∞}				ε_s				ω_{po} (THz)
	a	b	c	Average	a	b	c	Average	
Ga ₂ O ₃ ¹¹	4.07	4.14	4.19	4.13	10.99	10.50	13.91	11.80	12.08, 8.46–11.60 ⁴⁹
Ga ₂ O ₃ ¹²	4.02	4.03	4.15	4.10	11.88	9.22	12.61	11.24	
Ga ₂ O ₃	3.98	4.06	4.10	4.05	10.20	9.55	13.71	11.15	
Al-Ga ₂ O ₃	3.91	3.99	4.00	3.97	10.09	9.48	13.04	10.87	12.75
In-Ga ₂ O ₃	4.01	4.10	4.12	4.08	10.32	9.49	13.90	11.24	12.71



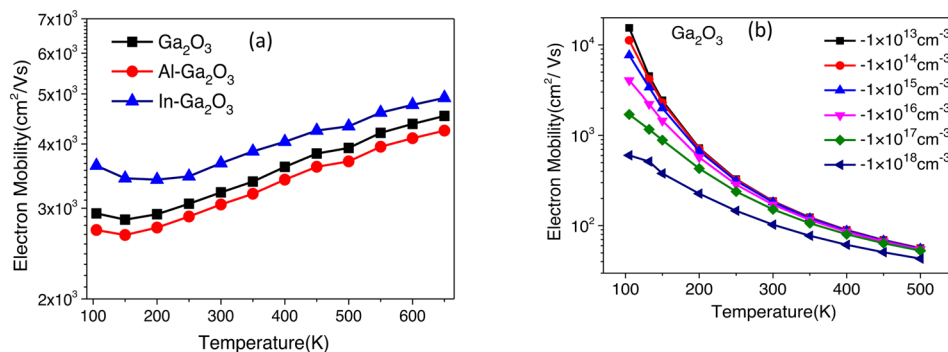


Fig. 6 Temperature-dependent electron mobility of Ga_2O_3 at electron concentrations ($1 \times 10^{17} \text{ cm}^{-3}$) where only IMP scattering is considered (a). Temperature-dependent electron mobility of Ga_2O_3 at various electron concentrations where ADP, IMP and POP scattering are considered together (b).

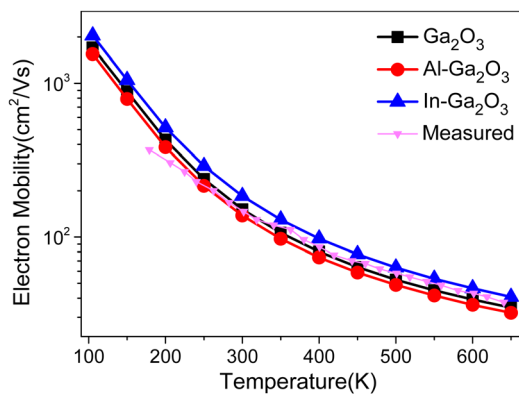


Fig. 7 Temperature-dependent electron mobility of Ga_2O_3 , Al-doped Ga_2O_3 and In-doped Ga_2O_3 , where ADP, IMP and POP scattering are considered together.

4. Conclusions

To summarize, we have investigated the temperature-dependent electron mobility of Ga_2O_3 , Al- Ga_2O_3 and In- Ga_2O_3 from first-principles by fully considering the scattering mechanisms of ADP, IMP, and POP. The results show that POP scattering is the dominant factor limiting the electron mobility of Ga_2O_3 , Al- Ga_2O_3 and In- Ga_2O_3 between 150 and 650 K. Combining these three scattering mechanisms, the electron mobilities of Ga_2O_3 , Al- Ga_2O_3 and In- Ga_2O_3 are $151.5 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$, $137.8 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$ and $184.9 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$ at 300 K. Furthermore, as temperature increases, the electron mobility of three Ga_2O_3 reduces due to more excited optical phonons, thus enhancing the electron-phonon coupling. With electron concentration increasing, the electron mobility of three Ga_2O_3 reduces due to more scattering probabilities. The electron mobility of In- Ga_2O_3 is the highest among these three structures for the decreased effective mass caused by the In 5s state. This work offers an alternative method to boost the electron mobility of Ga_2O_3 and serves as a guide for engineering the electronic transport properties tailored for high-power electronic applications.

Author contributions

L. Z.: conceptualization, software, writing – original draft. J. H.: validation. Y. S.: writing – review & editing. F. L. and P. Z.: formal analysis, visualization. D. W.: visualization. K. W.: writing – review & editing, supervision. Y. W.: writing – original draft, supervision.

Data availability

The data that support the findings of this study are available within the article and the ESI.†

Conflicts of interest

There are no conflicts to declare.

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References

- 1 X. He, J. Hu and Z. Zhang, *et al.*, Study on the interface electronic properties of AlN(0001)/ β - Ga_2O_3 (100), *Surf. Interfaces*, 2022, **28**, 101585.
- 2 N. Pant, W. Lee and N. Sanders, *et al.*, Increasing the mobility and power-electronics figure of merit of AlGaN with atomically thin AlN/GaN digital-alloy superlattices, *Appl. Phys. Lett.*, 2022, **121**(3), 032105.
- 3 C. J. H. Wort and R. S. Balmer, Diamond as an electronic material, *Mater. Today*, 2008, **11**, 22–28.



- 4 H. H. Tippins, Optical absorption and photoconductivity in the band edge of β -Ga₂O₃, *Phys. Rev.*, 1965, **140**(1A), A316–A319.
- 5 K. Wu, L. Zhang, F. Li, L. Sang, M. Liao, K. Tang, J. Ye and S. Gu, Enhancement of interfacial thermal conductance by introducing carbon vacancy at the Cu/diamond interface, *Carbon*, 2024, **223**, 119021.
- 6 M. Higashiwaki, K. Sasaki and A. Kuramata, *et al.*, Gallium oxide Ga₂O₃ metal-semiconductor field-effect transistors on single-crystal β -Ga₂O₃ substrates, *J. Appl. Phys. Lett.*, 2012, **100**(1), 013504.
- 7 Z. Galazka, R. Uecker and K. Lrnscher, *et al.*, Czochralski growth and characterization of β -Ga₂O₃ single crystals, *Cryst. Res. Technol.*, 2010, **45**(12), 1229–1236.
- 8 Encarnación G. Villora, Kiyoshi Shimamura, Takekazu Ujiie and Kazuo Aoki, Electrical conductivity and lattice expansion of β -Ga₂O₃ below room temperature, *Appl. Phys. Lett.*, 2008, **92**, 202118.
- 9 N. Ma, N. Tanen, A. Verma, Z. Guo, T. Luo, H. (Grace) Xing and D. Jena, Intrinsic Electron Mobility Limits in β -Ga₂O₃, *Appl. Phys. Lett.*, 2016, **109**, 212101.
- 10 Z. Zhang, Y. Wu, C. Lu and S. Ahmed, Electron mobility in β -Ga₂O₃: an ensemble Monte Carlo study, *Appl. Phys. A*, 2018, **124**, 637.
- 11 X. Duan, T. Wang, Z. Fu, L. Liu and J. Yang, Nontrivial role of polar optical phonons in limiting electron mobility of two-dimensional Ga₂O₃ from first-principles, *Phys. Chem. Chem. Phys.*, 2023, **25**, 10175–10183.
- 12 Y. Kang, K. Krishnaswamy, H. Peelaers and C. G. Van de Walle, Fundamental limits on the electron mobility of β -Ga₂O₃, *J. Phys.: Condens. Matter*, 2017, **29**, 234001.
- 13 F. Roccaforte, P. Fiorenza, G. Greco, R. L. Nigro, F. Giannazzo, F. Iucolano and M. Saggio, Emerging trends in wide band gap semiconductors (SiC and GaN) technology for power devices, *Microelectro. Eng.*, 2018, **187–188**, 66–77.
- 14 B. K. Ridley, B. E. Foutz and L. F. Eastman, Mobility of electrons in bulk GaN and Al_xGa_{1-x}N/GaN heterostructures, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 2000, **61**, 16862–16869.
- 15 C. Zhang, F. Liao, X. Liang, H. Gong, Q. Liu, L. Li, X. Qin, X. Huang and C. Huang, Electronic transport properties in metal doped beta-Ga₂O₃: A first principles study, *Phys. B*, 2019, **562**, 124–130.
- 16 M. Yu, B. Peng, K. Sun, J. Yu, L. Yuan, J. Hu, Y. Zhang and R. Jia, First principles investigation of photoelectric properties of Ga₂O₃ Doped with group IV elements (Si, Ge, Sn), *Mater. Today Commun.*, 2023, **34**, 105127.
- 17 P. Li, L. Dong, C. Li, B. Lu, C. Yang, B. Peng, W. Wang, Y. Miao and W. Liu, Indium doping-assisted monolayer Ga₂O₃ exfoliation for performance-enhanced MOSFETs, *Nanoscale*, 2023, **15**, 12105–12115.
- 18 W. Tian, C. Zhi, T. Zhai, S. Chen, X. Wang, M. Liao, D. Golberg and Y. Bando, In-doped Ga₂O₃ nanobelt based photodetector with high sensitivity and wide-range photo-response, *J. Mater. Chem.*, 2012, **22**, 17984–17991.
- 19 L. Ji, X. Chen, X. Su, J. Wan, Z. Tu, H. Wu and C. Liu, Influence of indium doping on electrical performance of gallium oxide thin-film transistors, *Appl. Phys. Lett.*, 2023, **122**, 202105.
- 20 J. Rehm, T. Chou, S. B. Anooz, P. Seyidov, A. Fiedler, Z. Galazka and A. Popp, Perspectives on MOVPE-grown (100) β -Ga₂O₃ thin films and its Al-alloy for power electronics application, *Appl. Phys. Lett.*, 2022, **121**, 240503.
- 21 Z. Xi, N. Chen, J. Cai, C. Xu, S. Li and S. Zheng, Modulation of electronic structures and transport properties in 2D TM_{0.5}Ga_{1.5}O₃ (TM = Al, Ga, In), *Phys. Lett. A*, 2024, **525**, 129914.
- 22 G. Kresse and J. Furthmüller, Efficient iterative schemes for ab initio total energy calculations using a plane-wave basis set, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 1996, **54**, 11169.
- 23 G. Kresse and J. Furthmüller, Efficiency of ab-initio total energy calculations for metals and semiconductors using a plane-wave basis set, *Comput. Mater. Sci.*, 1996, **6**, 15.
- 24 J. P. Perdew, K. Burke and M. Ernzerhof, Generalized gradient approximation made simple, *Phys. Rev. Lett.*, 1996, **77**, 3865.
- 25 J. Heyd, G. E. Scuseria and M. Ernzerhof, Hybrid functionals based on a screened Coulomb potential, *J. Chem. Phys.*, 2003, **118**, 8207.
- 26 S. Poncé, W. Li, S. Reichardt and F. Giustino, First-principles calculations of charge carrier mobility and conductivity in bulk semiconductors and two-dimensional materials, *Rep. Prog. Phys.*, 2020, **83**, 036501.
- 27 S. Poncé, E. R. Margine and F. Giustino, Towards predictive many-body calculations of phonon-limited carrier mobilities in semiconductors, *Phys. Rev. B*, 2018, **97**, 121201.
- 28 W. Li, Electrical transport limited by electron-phonon coupling from Boltzmann transport equation: An ab initio study of Si, Al, and MoS₂, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 2015, **92**, 075405.
- 29 A. M. Ganose, J. Park, A. Faghaninia, R. Woods-Robinson, K. A. Persson and A. Jain, Efficient calculation of carrier scattering rates from first principles, *Nat. Commun.*, 2021, **12**, 2222.
- 30 G. Grimvall, *The Electron-Phonon interaction in metals*, North-Holland, Amsterdam, 1981.
- 31 F. Giustino, M. L. Cohen and S. G. Louie, Electron-phonon interaction using Wannier functions, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 2007, **76**, 165108.
- 32 H. Fröhlich, Electrons in lattice fields, *Adv. Phys.*, 1954, **3**, 325–361.
- 33 H. Brooks, Scattering by ionized impurities in semiconductors, *Phys. Rev.*, 1951, **83**, 879.
- 34 C. Herring and E. Vogt, Transport and deformation-potential theory for many-valley semiconductors with anisotropic scattering, *Phys. Rev.*, 1956, **101**, 944.
- 35 J. Bardeen and W. Shockley, Deformation potentials and mobilities in non-polar crystals, *Phys. Rev.*, 1950, **80**, 72.
- 36 F. S. Khan and P. B. Allen, Deformation potentials and electron-phonon scattering: Two new theorems, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 1984, **29**, 3341.
- 37 E. Kartheuser and S. Rodriguez, Deformation potentials and the electron-phonon interaction in metals, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 1986, **33**, 772.



- 38 R. Resta, Deformation-potential theorem in metals and in dielectrics, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 1991, **44**, 11035.
- 39 S. Geller, Crystal Structure of β -Ga₂O₃, *J. Chem. Phys.*, 1960, **33**, 676–684.
- 40 Q. Fan, R. Zhao, W. Zhang, Y. Song, M. Sun and U. Schwingenschlögl, Low-energy Ga₂O₃ polymorphs with low electron effective masses, *Phys. Chem. Chem. Phys.*, 2022, **24**, 7045–7049.
- 41 S. J. Pearton, J. Yang, P. H. Cary, F. Ren, J. Kim, M. J. Tadjer and M. A. Mastro, A review of Ga₂O₃ materials, processing, and devices, *Appl. Phys. Lett.*, 2018, **5**, 011301.
- 42 Effective Mass Calculator for Semiconductors, Fonari A, Sutton C, <https://github.com/afonari/emc2013-3-18>.
- 43 K. Adachi, H. Ogi, N. Takeuchi, N. Nakamura, H. Watanabe, T. Ito and Y. Ozaki, Unusual elasticity of monoclinic β -Ga₂O₃, *J. Appl. Phys.*, 2018, **124**, 085102.
- 44 M. H. Wong, K. Sasak, A. Kuramata, S. Yamakoshi and M. Higashiwaki, Electron channel mobility in silicon-doped Ga₂O₃ MOSFETs with a resistive buffer layer, *Jpn. J. Appl. Phys.*, 2016, **55**, 1202B9.
- 45 D. Emin, *Polarons*, Cambridge University Press, 2013.
- 46 H. Fröhlich, Interaction of electrons with lattice vibrations, *Proc. Math. Phys. Eng.*, 1952, **215**, 291–298.
- 47 J. M. Frost, Calculating polaron mobility in halide perovskites, *Phys. Rev. B*, 2017, **96**, 195202.
- 48 G. Schmitz, P. Gassmann and R. Franchy, A combined scanning tunneling microscopy and electron energy loss spectroscopy study on the formation of thin, well-ordered β -Ga₂O₃ films on CoGa (001), *J. Appl. Phys.*, 1998, **83**, 2533–2538.
- 49 T. Onuma, S. Saito, K. Sasaki, K. Goto, T. Masui, T. Yamaguchi, T. Honda, A. Kuramata and M. Higashiwaki, Temperature-dependent exciton resonance energies and their correlation with IR-active optical phonon modes in β -Ga₂O₃ single crystals, *App. Phys. Lett.*, 2016, **108**, 101904.
- 50 B. R. Nag, *Electron Transport in Compound Semiconductors*, Springer Berlin Heidelberg, Berlin, Heidelberg, 1980, vol. 11.

