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Co-electrolysis SOEC and internal reforming SOFC for achieving a carbon-neutral society

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Solid oxide electrolysis cells (SOECs) can produce carbon monoxide (CO) from carbon dioxide (CO₂) in addition to hydrogen (H₂) from steam using renewable energy sources such as solar and wind power. Methanol (MeOH) and dimethyl ether (DME) are industrially synthesized from syngas (H₂ + CO mixture) with an H₂/CO ratio of 2. Solid oxide fuel cells (SOFCs) can generate power using MeOH and DME in addition to H₂. To achieve a carbon-neutral society, H₂O/CO₂ co-electrolysis SOECs and internal reforming SOFCs using MeOH and DME were investigated using the same negatrode-supported microtubular cells. As a result of quantitative analysis of the gas composition, the H₂/CO ratios of the product gases were identical to the H₂O/CO₂ ratios of the input gases during the co-electrolysis. The gas diffusion resistance increased with decreasing H₂O/CO₂ ratios for co-electrolysis SOECs, and increased with time during co-electrolysis at H₂O/CO₂ = 2 and internal reforming of MeOH and DME. H₂O/CO₂ co-electrolysis SOECs and internal reforming SOFCs using MeOH and DME were successfully operated for 100 h.

Sustainability spotlight

To achieve a carbon-neutral society, converting carbon dioxide (CO_2) into raw materials and synthetic fuels (e-fuel) is very important. Solid oxide electrolysis cells (SOECs) can produce syngas ($H_2 + CO$ mixture) from steam and CO_2 using renewable energy sources such as solar and wind power. Syngas can be converted into methanol (MeOH) and dimethyl ether (DME) in addition to e-fuel such as gasoline, kerosene, and diesel *via* Fischer–Tropsch synthesis. MeOH and DME are fuels for solid oxide fuel cells (SOFCs) in addition to raw materials for commodity plastics (e-chemical). The reversible SOECs and SOFCs using carbon-containing fuels contribute to the following UN sustainable development goals: affordable and clean energy (SDG 7), responsible consumption and production (SDC 12), and climate action (SDG 13).

1. Introduction

Solid oxide fuel cells (SOFCs) are expected to be power generation systems with high energy conversion efficiencies. SOFCs can directly use hydrocarbon and alcohol fuels in addition to hydrogen (H₂), because oxide ions (O²⁻) conduct through an electrolyte and the electrochemical oxidation occurs at the negatrode (fuel electrode) at high temperatures above 600 °C.¹⁻³ Power generation with internal partial oxidation reforming of butane and steam reforming of ethanol has been investigated using microtubular SOFCs supported on a Ni-Gd-doped ceria (GDC) negatrode.⁴ A long-term flight of a drone (UAV; unmanned aerial vehicle) was demonstrated using a portable SOFC system powered by liquefied petroleum gas (LPG) cartridges.⁵ Because LPG is a fossil fuel, replacing LPG with carbon-neutral fuels is desirable. Although bio-ethanol helps to reduce carbon dioxide (CO₂) emissions, sulfur-containing bio-

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fuels deteriorate Ni-based SOFC negatrodes by promoting carbon deposition.⁶

Solid oxide cells can be used as electrolyzers as shown in Fig. 1. Solid oxide electrolysis cells (SOECs) can produce carbon monoxide (CO) from CO₂ in addition to H₂ from steam *via* the reverse reaction of SOFCs with O²⁻ conduction through the electrolyte. Alkaline and polymer electrolyte membrane (PEM) electrolysis are widely demonstrated for H₂ production.⁷ Some researchers have investigated low-temperature CO₂ electrolysis using alkaline aqueous electrolytes and PEMs. However, these require a high cell voltage above 2.5 V, and these exhibit a low faradaic efficiency.⁸ On the contrary, SOECs can produce CO at 1.4 V *via* high-temperature CO₂ electrolysis, resulting in faradaic and energy efficiencies of 100% in principle. If external thermal energy can compensate for the latent heat of water vaporization and endothermic electrolysis, a further decrease in cell voltage and an increase in efficiency are possible.

CO₂ capture is one of the most important technologies for achieving a carbon-neutral society. Chemical adsorption method involving monoethanolamine and gas separation membranes have been demonstrated for CO₂ capture. The initial target is treating the exhaust gases from plants, which

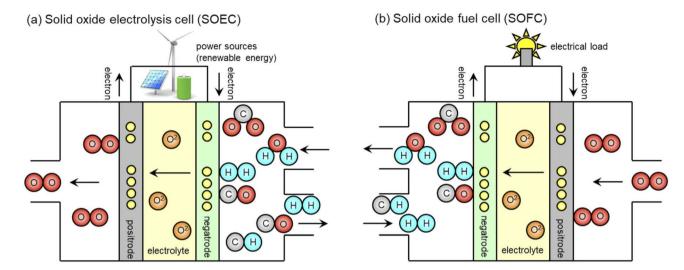


Fig. 1 Schematics of (a) co-electrolysis SOEC and (b) internal reforming SOFC.

contain 4–14 vol% CO₂. Recently, direct air capture (DAC), which extracts CO₂ directly from the atmosphere at any location, has been investigated. Mixed ionic liquid membranes exhibit a high CO₂ permeability of 2.5983 \times 10⁻⁶ cm³(STP)·cm cm $^{-2}$ s $^{-1}$ cm $_{\rm Hg}^{-1}$ and a high CO₂/N₂ selectivity of 1.0059 \times 10⁴ at 400 ppm CO₂. 11

SOECs can simultaneously perform steam and CO_2 electrolysis, known as co-electrolysis. ^{12–16} Syngas, a mixture of H_2 and CO_3 , is produced via the co-electrolysis SOECs. Syngas can be converted into many useful sources and fuels as follows:

Methanation:
$$3H_2 + CO \rightarrow CH_4 + H_2O$$
 (1)

Fischer–Tropsch synthesis:
$$(2n + 1)H_2 + nCO \rightarrow C_nH_{2n+2} + nH_2O$$
 (2)

Methanol synthesis:
$$2H_2 + CO \rightarrow CH_3OH$$
 (3)

Dimethyl ether (DME) synthesis:
$$4H_2 + 2CO \rightarrow CH_3OCH_3 + H_2O$$
 (4)

Methanation is used to produce synthetic natural gas,17 with the advantage of utilizing existing pipelines and infrastructure. However, the SOFCs using synthetic natural gas require a high temperature of 790 °C for methane reforming. Fischer-Tropsch (FT) synthesis is used to produce synthetic fuels (e-fuel) such as gasoline, kerosene, and diesel for airplanes, vessels, and large vehicles. 18 A Co/SiO₂ catalyst yields 1500 and 815 g kg_{-cat}⁻¹ h⁻¹ of C₅₊ and C₁₀₋₂₀ hydrocarbons, respectively, via FT synthesis at 776 °C and 1.1 MPa.19 However, SOFCs easily deteriorate because of carbon deposition, when hydrocarbons with high carbon number are used as fuels. Therefore, the author focuses on methanol (MeOH) and dimethyl ether (DME). MeOH is industrially produced from syngas generated by natural gas reforming using Cu/ZnO-based catalysts.20-22 Direct methanol fuel cells (DMFCs) using PEM electrolyte have been investigated owing to their low reforming temperatures below 150 °C.²³ However, DMFCs suffer from CO poisoning on a negatrode and

MeOH crossover through an electrolyte. For SOFCs, MeOH is a promising fuel, because it does not cause CO poisoning and MeOH crossover.²⁴⁻²⁷ In addition, DME can be easily produced by the dehydration of methanol.²⁸

DME synthesis:
$$2CH_3OH \rightarrow CH_3OCH_3 + H_2O$$
 (5)

The reforming temperature of DME is less than 180 °C, and its characteristics are similar to those of LPG, because it is easily liquified at 0.6 MPa. Thus, DME is a possible alternative to LPG as a fuel for portable SOFC systems.^{29,30}

In the present work, co-electrolysis SOECs and internal reforming SOFCs were investigated using microtubular negatrode-supported cells with the same cell configuration. Numerous researchers have demonstrated reversible SOFC/SOEC operation using H₂ and steam.³¹⁻³³ However, there have been few demonstrations of reversible operation using carbon-containing fuels. The H₂/CO ratio of the syngas should be 2 for MeOH, DME, and FT syntheses. To investigate the effect of CO₂ concentration on electrochemical characteristics, co-electrolysis was performed with varying H₂O/CO₂ ratios from 0 to infinity (∞). The compositions of the product gases after co-electrolysis were analyzed using gas chromatography. Assuming that MeOH and DME are synthesized from syngas, internal reforming SOFCs were demonstrated using MeOH and DME. Steam reforming was investigated for MeOH, because it is a liquid with water solubility. Partial oxidation reforming was investigated for DME in addition to steam reforming, since it easily mixes with ambient air at ordinary temperatures and pressures. Short-term durability tests of the co-electrolysis SOECs using an input gas at $H_2O/CO_2 = 2$ and internal reforming SOFCs using MeOH and DME were conducted for 100 h.

2. Experimental

2.1 Cell preparation

Similar to previously reported internal reforming of butane and ethanol, an egatrode-supported microtubular cells with the same

cell configuration were used for co-electrolysis SOECs and internal reforming SOFCs using MeOH and DME. Negatrode microtube substrates were constructed using 60 wt% NiO (Sumitomo Metal Mining)-40 wt% Ce_{0.9}Gd_{0.1}O_{1.95} (GDC; Shin-Etsu Chemical) adding pore former (acrylic resin; Sekisui Plastic) and binder (cellulose; Yuken Kogyo) powders. These powders were mixed using a kneading machine with adding an appropriate amount of water, and the negatrode microtubes were extruded using a piston cylinder. After extrusion, the microtubes were dried overnight in air at room temperature. A slurry was prepared by mixing (Y₂O₃)_{0.08}(ZrO₂)_{0.92} (YSZ; Tosoh), binder (polyvinyl butyral; Sekisui Chemical) dispersant (tallow propylene diamine, Kao Chemicals) and plasticizer (dioctyl adipate; Wako Pure Chemical Industries) with ethanol and toluene solvents. The YSZ electrolyte was formed by dip-coating. The YSZ electrolyte thin-film and the NiO-GDC negatrode microtube were co-sintered in air for 3 h at 1400 °C. The GDC interlayer and the positrode (air electrode) of 70 wt% La_{0.6}-Sr_{0.4}Co_{0.2}Fe_{0.8}O_{3−δ} (LSCF; Kusaka Rare Metal)-30 wt% GDC were coated in a similar manner. The interlayer and positrode thinfilm layers were sintered sequentially in air for 2 h at 1200 °C and for 1 h at 1050 °C, respectively. The microtube diameter and positrode area after sintering were 2.8 mm and 2.6 cm², respectively. The thicknesses of the negatrode, electrolyte, interlayer, and positrode were 640, 10, 1, and 20 µm, respectively.

2.2 Evaluation of co-electrolysis SOECs and internal reforming SOFCs

Table 1 and Fig. 2 show the experimental conditions and setup for evaluating the co-electrolysis SOECs and internal reforming SOFCs. For internal steam reforming of MeOH, an aqueous MeOH solution (82 vol% at S/C = 0.5 and 69 vol% at S/C = 1.0) was supplied to the negatrode using a pump and vaporizer heated at 250 °C. For co-electrolysis and internal steam reforming of DME, steam was fed to the negatrode using a temperature-controlled bubbler. Before evaluation, a mixture of 20% H₂-3% H₂O-77% N₂ was supplied to the negatrode for 2 h at 700 °C for Ni catalyst reduction. Subsequently, the input gases were adjusted to the flow rates listed in Table 1, and air was supplied to the positrode at a rate of 100 mL min $^{-1}$. Hydrogen was supplied during co-electrolysis SOEC to prevent Ni catalyst oxidation in the negatrode under open circuit voltage (OCV). Current-voltage (I-V) characteristics were evaluated using a potentiostat/galvanostat (Solartron Analytical 1470E) by varying the voltage from OCV to 0.4 and 1.4 V for SOECs and SOFCs, respectively, at a sweep rate of 5 mV s⁻¹. Using a frequency response analyzer (Solartron Analytical 1455), the electrochemical impedance between the negatrode and positrode was measured in the frequency range of 100 kHz-0.1 Hz with 20 steps per logarithmic decade. The polarization impedance can be deconvoluted using the distribution of relaxation times (DRT) analysis.34,35 The DRT analysis was performed using

Table 1 Flow rates (mL min⁻¹) of the input gases for co-electrolysis SOECs and internal steam (SR) and partial oxidation (POx) reforming SOFCs

| | $\rm H_2O/CO_2$ | H_2 | $\rm H_2O$ | CO_2 | O_2 | MeOH or DME | N_2 |
|-----------------|----------------------|-------|------------|-----------------|-------|-------------|-------|
| Co-electrolysis | $H_2O/CO_2=0$ | 3.0 | 0.0 | 20.0 | | | 77.0 |
| | $H_2O/CO_2 = 1/3$ | 3.0 | 5.0 | 15.0 | | | 77.0 |
| | $H_2O/CO_2 = 1$ | 3.0 | 10.0 | 10.0 | | | 77.0 |
| | $H_2O/CO_2 = 2$ | 3.0 | 13.3 | 6.7 | | | 77.0 |
| | $H_2O/CO_2 = 3$ | 3.0 | 15.0 | 5.0 | | | 77.0 |
| | $H_2O/CO_2 = \infty$ | 3.0 | 20.0 | 0.0 | | | 77.0 |
| MeOH SR | S/C = 0.5 | | 5.0 | | | 10.0 | 85.0 |
| | S/C = 1.0 | | 10.0 | | | 10.0 | 80.0 |
| DME SR | S/C = 1.0 | | 10.0 | | | 5.0 | 85.0 |
| | S/C = 1.5 | | 15.0 | | | 5.0 | 80.0 |
| DME POx | O/C = 1.0 | | | | 10.0 | 10.0 | 61.4 |
| | O/C = 1.5 | | | | 15.0 | 10.0 | 56.4 |

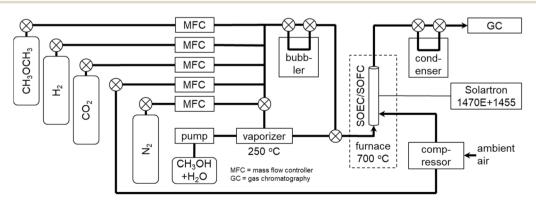


Fig. 2 Schematic of experimental setup for evaluation of co-electrolysis SOECs and internal reforming SOFCs.

Z-Assist software (Toyo Corp.).36 It used FTIKREG software37 to solve an ill-posed inverse problem in the DRT analysis via Tikhonov regularization. Real impedance was used for the DRT analysis because the impact of measurement errors and inductive components was lower than that with imaginary impedance.³⁸ Kramers-Kronig validation was performed using K-K test39 and Lin-KK Tool40 software. Residuals between measured and Kramers-Kronig transformed impedances were within 0.5%. The parameters obtained DRT analysis were refined by complex non-linear least squares (CNLS) fitting using ZView software (Scribner Associates), assuming an equivalent circuit model with a series connection of resistance (R_0) and parallel resistance-capacitance (R_kC_k) elements. The thermodynamic equilibrium compositions were calculated using HSC Chemistry 5.11 (Outokumpu). During co-electrolysis, the flow rates of the product gases were analyzed with a thermal conductivity detector (TCD) in a micro gas chromatograph (Agilent Technologies 490; Molsieve 5A column with Ar as the carrier gas for H2, N2, CH4, and CO, and PoraPLOT Q column with He as the carrier gas for CO₂). Steam flow rates in the product gases were not measured by micro gas chromatography, because steam was removed using a condenser as shown in Fig. 2. The steam flow rates of the product gases were estimated by considering the mass balance of the hydrogen, oxygen and carbon species. Unfortunately, the flow rates of the reformate gases during internal reforming could not be analyzed, because MeOH and DME are soluble in water. Short-term durability tests of co-electrolysis SOECs and internal reforming SOFCs were conducted for 100 h at a constant voltage of 1.28 V and a constant current density of 0.3 A cm⁻², respectively.

Results and discussion

3.1 Co-electrolysis SOECs

Fig. 3 shows the equilibrium amounts of the product gases as a function of $H_2O + CO_2$ utilization at (a) $H_2O/CO_2 = 0$ and (b) $H_2O/CO_2 = 2$ at 700 °C. The input gases are 0.2 mol of H_2O/CO_2 and 0.03 mol of H_2 . The product amounts of the H_2/CO mixtures

are assumed to obey faradaic law. At $H_2O/CO_2=0$, carbon is deposited, when H_2O+CO_2 utilization exceeds 0.8. At low temperatures, carbon is easily deposited, even at lower H_2O/CO_2 ratios. Moreover, methane is slightly produced, when H_2O+CO_2 utilization is above 0.6 at $H_2O/CO_2=2$. When carbon and/or methane are not produced, the amounts of H_2 and CO produced increase linearly with the H_2O+CO_2 utilization, and the H_2/CO ratios of the product gases are identical to the H_2O/CO_2 ratios of the input gases. Co-electrolysis is desirable to be operated at high temperatures to prevent carbon and methane production.

Fig. 4 shows the I–V characteristics for co-electrolysis SOEC at various $\rm H_2O/CO_2$ ratios and 700 °C. The flow rates of the input gases are listed in Table 1. The theoretical electromotive forces (EMFs) are 0.910, 0.906, 0.902, 0.899, 0.898, and 0.894 V at $\rm H_2O/CO_2=0$, 1/3, 1, 2, 3, and ∞ , respectively. The OCVs were 20–30 mV lower than the theoretical EMFs under all conditions, owing to slight gas leakage. The slopes of I–V curves increased with decreasing $\rm H_2O/CO_2$ ratios. The $\rm H_2O$ + $\rm CO_2$ utilizations were 0.27–0.32 under 1.28 V at $\rm H_2O/CO_2=0$ – ∞ . The performances during $\rm H_2O/CO_2$ co-electrolysis and $\rm CO_2$ electrolysis

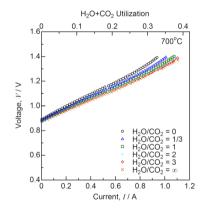
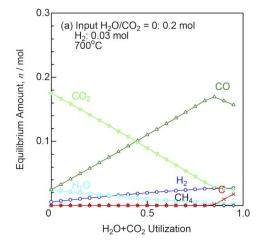


Fig. 4 Current–voltage characteristics for co-electrolysis SOEC at various H_2O/CO_2 ratios and 700 °C.



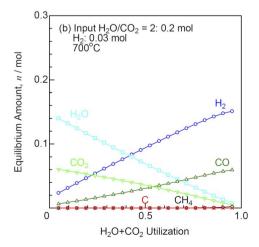


Fig. 3 Equilibrium amounts of the product gases as a function of $H_2O + CO_2$ utilization at (a) $H_2O/CO_2 = 0$ and (b) $H_2O/CO_2 = 2$ (input $H_2O/CO_2 = 0$) and (b) $H_2O/CO_2 = 0$ and (c) $H_2O/CO_2 = 0$ and (d) $H_2O/CO_2 = 0$ and (e) $H_2O/CO_2 = 0$ and (f) $H_2O/CO_2 = 0$ and (h) $H_$

were lower than that during steam electrolysis. 12,13,15,16 The performance of the co-electrolysis SOEC decreased with increasing CO_2 concentrations in the input gases.

Fig. 5(a) and (b) show the Nyquist plots of impedance spectra for co-electrolysis SOEC under OCV and 1.28 V, respectively, at various H_2O/CO_2 ratios and 700 °C. The ohmic losses (R_0) derived from the intersections of the impedance arcs at high frequencies with the real axis remained unchanged with the H₂O/CO₂ ratios. The ohmic losses under 1.28 V were slightly larger than those under OCV, because endothermic reaction of H₂O/CO₂ co-electrolysis decreased the local temperature at the interface between electrolyte and electrode. The polarization resistances at low frequencies below 10 Hz increased with decreasing H₂O/CO₂ ratios. DRT analysis was performed to deconvolute the impedance spectra as shown in Fig. 5(c) and (d). Six DRT peaks were observed under all the conditions, corresponding to the following physicochemical origins of the rate-determining elementary processes for negatrode-supported microtubular SOECs:36

 P_1 (10–100 kHz): physical impedance originating from the grain boundaries, pores, and reaction products between the electrolyte and positrode

 P_2 , P_3 (20 Hz–10 kHz): charge transfer and ionic conduction processes at the negatrode

 P_4 (2–200 Hz): oxygen surface exchange and diffusion processes at the positrode

 P_5 , P_6 (0.1–20 Hz): gas diffusion and nonstoichiometric oxygen variation processes at the Ni-GDC negatrode

Fig. 5(e) and (f) show the resistance against H_2O/CO_2 ratios derived from the CNLS fitting using the equivalent circuit model with a series connection of R_0 and six R_kC_k (k=1–6) elements. R_5 and R_6 increased with decreasing H_2O/CO_2 ratios. Graves $et\ al.^{12}$ reported that the polarization resistance resulting from gas diffusion process at the negatrode increased at high CO_2 concentrations. This suggests that the CO/CO_2 mixture diffuses more difficultly than the H_2/H_2O mixture in the SOEC negatrode.

Syngas with an H_2/CO ratio of 2 is desirable for methanol, DME, and FT syntheses. Therefore, a quantitative analysis of

Table 2 Estimated flow rates ($mL \, min^{-1}$) of the product gases for coelectrolysis SOEC under equilibrium, OCV, and 1.28 V using gas chromatography. The steam flow rates of the product gases were estimated in consideration for mass balance of hydrogen, oxygen and carbon species

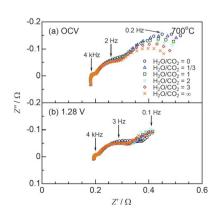
| H ₂ O/CO ₂ | V | I | H_2 | H_2O | CO | CO_2 | CH_4 | N_2 |
|----------------------------------|-------------|---------|-------|--------|-------|--------|--------------------|-------|
| 0 | Equilibrium | | 0.543 | 2.46 | 2.46 | 17.5 | $1 	imes 10^{-6}$ | 77.0 |
| | OCV | 0 A | 0.947 | 1.65 | 2.72 | 17.7 | 0 | 77.0 |
| | 1.28 V | 0.770 A | 1.12 | 2.43 | 7.70 | 11.7 | 0 | 77.0 |
| 1/3 | Equilibrium | | 1.33 | 6.68 | 1.68 | 13.3 | 5×10^{-6} | 77.0 |
| | OCV | 0 A | 1.58 | 6.74 | 1.21 | 13.5 | 0 | 77.0 |
| | 1.28 V | 0.830 A | 3.13 | 5.33 | 5.51 | 9.03 | 0 | 77.0 |
| 1 | Equilibrium | | 1.98 | 11.0 | 1.02 | 8.98 | 6×10^{-6} | 77.0 |
| | OCV | 0 A | 1.86 | 10.7 | 0.720 | 9.70 | 0 | 77.0 |
| | 1.28 V | 0.871 A | 4.96 | 7.61 | 3.80 | 6.63 | 0 | 77.0 |
| 2 | Equilibrium | | 2.35 | 14.0 | 0.647 | 6.05 | 5×10^{-6} | 77.0 |
| | OCV | 0 A | 2.13 | 13.4 | 0.538 | 6.91 | 0 | 77.0 |
| | 1.28 V | 0.886 A | 6.22 | 10.0 | 2.44 | 4.31 | 0 | 77.0 |
| 3 | Equilib | rium | 2.53 | 15.5 | 0.469 | 4.53 | 4×10^{-6} | 77.0 |
| | OCV | 0 A | 2.38 | 15.3 | 0.394 | 4.95 | 0 | 77.0 |
| | 1.28 V | 0.902 A | 7.22 | 10.6 | 1.84 | 3.39 | 0 | 77.0 |
| ∞ | Equilib | rium | 3.00 | 20.0 | 0 | 0 | 0 | 77.0 |
| | OCV | 0 A | 3.08 | 19.9 | 0 | 0 | 0 | 77.0 |
| | 1.28 V | 0.909 A | 9.46 | 13.5 | 0 | 0 | 0 | 77.0 |

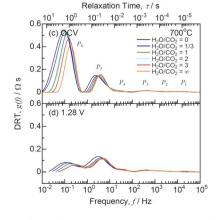
product gas compositions is important for the co-electrolysis SOEC evaluation. Table 2 shows the estimated flow rates of the product gases for co-electrolysis SOEC under equilibrium, OCV and 1.28 V using gas chromatography. The steam flow rates were estimated in consideration for mass balance of hydrogen, oxygen and carbon species assuming no carbon deposition. The faradaic law for electrolysis is as follows:

$$I = \dot{n}zF \tag{6}$$

where *I* is the current (A), \dot{n} is the molar product rate (mol s⁻¹), *z* is the valency of the ions (2), and *F* is the faradaic constant (96 485C mol⁻¹). The ideal gas law is as follows:

$$p\dot{v} = 60\dot{n}R_{\rm g}T\tag{7}$$





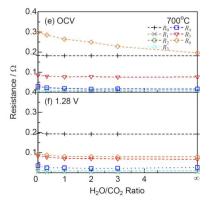


Fig. 5 (a and b) Impedance, (c and d) DRT spectra, and (e and f) resistances for co-electrolysis SOEC under (a, c and e) OCV and (b, d and f)1.28 V at various H_2O/CO_2 ratios and 700 °C.

where p is the pressure (kPa), \dot{v} is the flow rate of the product gas (L min⁻¹), R_{α} is the gas constant (8.3145 J mol⁻¹ K⁻¹), and T is the absolute temperature (K). In the standard state (p = 101.325kPa and T = 273.15 K), \dot{v} is derived from the following equation:

$$\dot{v} = 6.9652 \times 10^{-3} I \tag{8}$$

This indicates the production of approximately 7 mL min⁻¹ of syngas per 1 A current. Under OCV, the equilibrium compositions differed from the input gas compositions owing to the reverse water gas shift reaction.

$$H_2 + CO_2 \leftrightarrow H_2O + CO$$
 (9

The differences between the equilibrium and measured gas flow rates were less than 1 mL min⁻¹ under OCV. Under 1.28 V, the H₂ + CO flow rates in the range of 5.15-6.38 mL min⁻¹ increased, when the current was 0.770-0.909 A at $H_2O/CO_2 =$ $0 - \infty$. The faradaic efficiencies were 0.96-1, because carbon

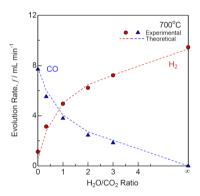
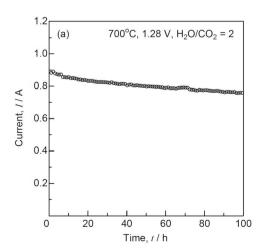


Fig. 6 Evolution rates of the product gases for co-electrolysis SOEC at various H₂O/CO₂ ratios and 700 °C

and methane were not produced in the H₂O + CO₂ utilizations ranges of 0.27-0.32. Fig. 6 shows the evolution rates of the product gases for co-electrolysis SOEC at various H2O/CO2 ratios and 700 °C. The H₂/CO ratios of the product gases were almost the identical to the H₂O/CO₂ ratios of the input gases. CO₂ electrolysis was slightly more difficult than steam electrolysis, because the polarization resistances increased with decreasing H₂O/CO₂ ratios as shown in Fig. 5. However, CO was produced via the reverse water gas shift reaction (eqn (9)) in addition to co-electrolysis. Thus, the product gas compositions easily reached equilibrium compositions.

The short-term durability test was performed under a constant voltage of 1.28 V at H₂O/CO₂ = 2 and 700 °C as shown in Fig. 7. Under 1.28 V, the initial current was 0.886 A, which decreased to 0.756 A after 100 h. The slope of the I-V curves increased, although the OCV remained unchanged during the durability test for 100 h. Fig. 8 shows the (a) impedance, (b) DRT spectra, and (c) resistances for co-electrolysis SOEC during the durability test under a constant voltage of 1.28 V at $H_2O/CO_2 = 2$ and 700 °C. The ohmic loss remained unchanged, whereas the polarization resistances at low frequencies below 10 Hz increased after 100 h. The DRT analysis suggested that R_5 and R_6 related to the gas diffusion process at the negatrode increased with time. The gas diffusion resistance should be decreased to improve durability in addition to the initial performance for co-electrolysis SOECs. Fig. 9 shows the evolution rates of the product gases during the durability test of the co-electrolysis SOEC under a constant voltage of 1.28 V at H₂O/ $CO_2 = 2$ and 700 °C. The evolution rates of H_2 and CO decreased with time, because the current decreased from 0.886 A to 0.756 A under 1.28 V after 100 h. The faradaic efficiency was remained above 0.95, confirming that the co-electrolysis SOEC produced syngas with a constant H₂/CO ratio of 2. MeOH and DME syntheses from syngas have been industrially established. Internal reforming SOFCs using MeOH and DME are discussed in the next section.



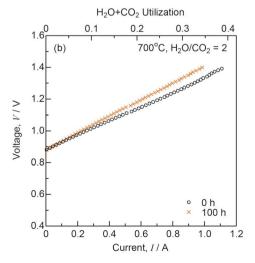


Fig. 7 (a) Time course of current under a constant voltage of 1.28 V and (b) current-voltage characteristics for co-electrolysis SOEC before and after the durability test at $H_2O/CO_2 = 2$ and 700 °C.

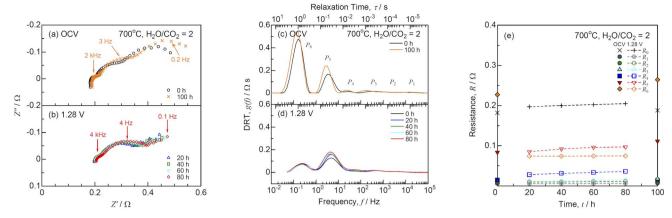


Fig. 8 (a and b) Impedance, (c and d) DRT spectra, and (e) resistances for co-electrolysis SOEC during the durability test under a constant voltage of 1.28 V at $H_2O/CO_2 = 2$ and 700 °C.

3.2 Internal reforming SOFCs

MeOH and DME are easily reformed at low temperatures. The conversion of MeOH and DME reaches 99% at 150 and 180 °C, respectively, in thermodynamic equilibrium. The stoichiometric reaction for MeOH decomposition is as follows:

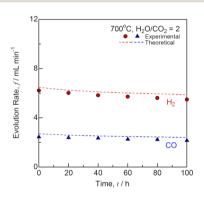


Fig. 9 Evolution rates of the product gases during the durability test of co-electrolysis SOEC under a constant voltage of 1.28 V at $\rm H_2O/CO_2=2$ and 700 °C.

$$CH_3OH \rightarrow 2H_2 + CO \Delta H_{25 \text{ °C}} = +90.5 \text{ kJ mol}^{-1}$$
 (10)

Fig. 10(a) shows the equilibrium amounts of the reformate gases as a function of S/C ratio during steam reforming of MeOH at 700 °C. Steam is not required stoichiometrically for MeOH decomposition as shown in eqn (10). However, steam reforming is required to prevent carbon deposition, because carbon is deposited at S/C ratios below 0.3 in equilibrium. Internal reforming SOFCs can be easily supplied with 82 vol% (S/C = 0.5) or 69 vol% (S/C = 1.0) MeOH water solutions. Meanwhile, DME can be reformed using partial oxidation (eqn (12)) in addition to steam (eqn (11)).

$$\text{CH}_3\text{OCH}_3 + \text{H}_2\text{O} \rightarrow 4\text{H}_2 + 2\text{CO} \Delta H_{25 \text{ °C}} = +205 \text{ kJ mol}^{-1} (11)$$

$$CH_3OCH_3 + \frac{1}{2}O_2 \rightarrow 3H_2 + 2CO \Delta H_{25 \text{ °C}} = -37.0 \text{ kJ mol}^{-1} (12)$$

Fig. 10(b) and (c) show the equilibrium amounts of the reformate gases as a function of S/C and O/C ratios during steam reforming and partial oxidation reforming of DME at 700 °C. The stoichiometric S/C and O/C ratios are 0.5 for steam reforming and partial oxidation reforming of DME. However,

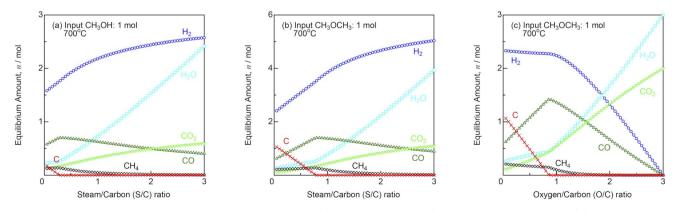


Fig. 10 Equilibrium amounts of the reformate gases as a function of S/C and O/C ratios for (a) steam reforming of MeOH, (b) steam reforming of DME, and (c) partial oxidation reforming of DME (input MeOH or DME: 1 mol) at 700 °C.

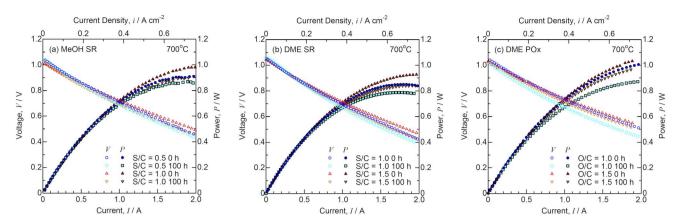


Fig. 11 Current–voltage characteristics for SOFCs during (a) steam reforming (SR) of MeOH, (b) SR of DME, and (c) partial oxidation reforming (POx) of DME before and after the durability tests at 700 °C.

carbon is deposited at S/C ratios <0.8 and O/C ratios <0.9 in equilibrium. The gas characteristics of DME are similar to those of LPG. Therefore, partial oxidation reforming can be easily performed by supplying DME/air mixture.

Fig. 11 shows the I-V characteristics for SOFCs during (a) steam reforming of MeOH, (b) steam reforming of DME, and (c) partial oxidation of DME before and after the durability tests at 700 °C. The theoretical EMFs, OCVs, and voltages at 0.3 A cm⁻² are summarized in Table 3. Unfortunately, the flow rate of the reformate gases during internal reforming could not be determined using the setup as shown in Fig. 2, because water-soluble MeOH and DME were removed from the condenser. The OCVs were almost identical to the theoretical EMFs under all the conditions, suggesting that MeOH and DME were reformed into H₂ and CO by steam and partial oxidation. The OCVs remained unchanged during the durability tests. The I-V characteristics were similar during internal reforming of MeOH and DME. Fig. 12 shows the time course of voltage for SOFCs during (a) steam reforming of MeOH, (b) steam reforming of DME, and (c) partial oxidation of DME during the durability test at a constant current density of 0.3 A cm⁻² and 700 °C. Internal reforming SOFCs using MeOH and DME were continuously operated for 100 h. The degradation rates at different S/C ratios were almost the same during steam reforming of MeOH and DME, whereas the degradation rate at O/C = 1.0 was larger than that at O/C =

1.5 during partial oxidation reforming of DME. Previously, the voltage rapidly dropped during internal reforming of butane at O/C \leq 1.0 and ethanol at S/C \leq 1.5,⁴ although Ni-ceria based negatrodes exhibit high tolerance against carbon deposition.^{3,24} The voltage was stable during internal reforming of MeOH and DME, and no carbon deposition was detected at the Ni-GDC negatrode after the durability test. MeOH and DME contain C–O bonds but no C–C bonds, making carbon deposition difficult.²⁵

The impedance spectra before and after the durability tests at 700 °C are shown in Fig. 13. Table 3 lists the ohmic losses (R_0) and total polarization resistances (R_p) before and after 100 h. The R₀ values almost remained unchanged during the durability test, whereas those of R_p increased with time. The DRT analysis was performed to deconvolute the impedance spectra as shown in Fig. 14. Four DRT peaks corresponding to P_2-P_5 were detected under all the conditions. Fig. 15 shows the time course of the resistances derived from CNLS fitting using the equivalent circuit model with a series connection of R_0 and four $R_k C_k$ (k = 2-5) elements. The values of R_3 and R_5 , which were ascribed to charge transfer and ionic conduction processes, and gas diffusion processes in the negatrode, respectively, increased with time. The DRT peaks of P_3 and P_5 shifted to lower frequencies as shown in Fig. 14. The gas diffusion resistance of the negatrode-supported microtubular cells used in this work

Table 3 Theoretical EMFs, OCVs, voltages at 0.3 A cm^{-2} , ohmic losses and total polarization resistances under OCV for SOFCs during steam reforming (SR) of MeOH, SR of DME, and partial oxidation reforming (POx) of DME before and after the durability test at a constant current density of 0.3 A cm^{-2} and $700 \text{ }^{\circ}\text{C}$

| | MeOH SR | | DME SR | | DME POx | _ |
|---|----------------|----------------|----------------|----------------|----------------|----------------|
| Ratio | S/C = 0.5 | S/C = 1.0 | S/C = 1.0 | S/C = 1.5 | O/C = 1.0 | O/C = 1.5 |
| Theoretical EMF | 1.04 V | 1.02 V | 1.04 V | 1.02 V | 1.03 V | 0.997 V |
| OCV | 1.05 V | 1.02 V | 1.05 V | 1.04 V | 1.05 V | 1.03 V |
| $V_{0 \text{ h}} @ 0.3 \text{ A cm}^{-2}$ | 0.764 V | 0.772 V | 0.758 V | 0.754 V | 0.777 V | 0.780 V |
| $V_{100 \text{ h}} @ 0.3 \text{ A cm}^{-2}$ | 0.749 V | 0.748 V | 0.734 V | 0.733 V | 0.730 V | 0.761 V |
| $R_{0,0 \text{ h}}$ | $0.182~\Omega$ | $0.160~\Omega$ | $0.200~\Omega$ | $0.180~\Omega$ | $0.184~\Omega$ | $0.165~\Omega$ |
| R _{0,100 h} | $0.182~\Omega$ | $0.166~\Omega$ | $0.202~\Omega$ | $0.179~\Omega$ | $0.186~\Omega$ | $0.163~\Omega$ |
| $R_{\rm p,0~h}$ | $0.114~\Omega$ | $0.115~\Omega$ | $0.114~\Omega$ | $0.121~\Omega$ | $0.122~\Omega$ | $0.115~\Omega$ |
| R _{p,100 h} | $0.137~\Omega$ | $0.145~\Omega$ | $0.151~\Omega$ | $0.154~\Omega$ | $0.162~\Omega$ | $0.145~\Omega$ |

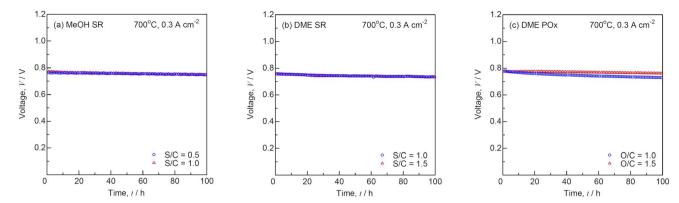


Fig. 12 Time courses of voltage for SOFCs during (a) steam reforming (SR) of MeOH, (b) SR of DME, and (c) partial oxidation reforming (POx) of DME during the durability test at a constant current density of 0.3 A cm⁻² and 700 °C.

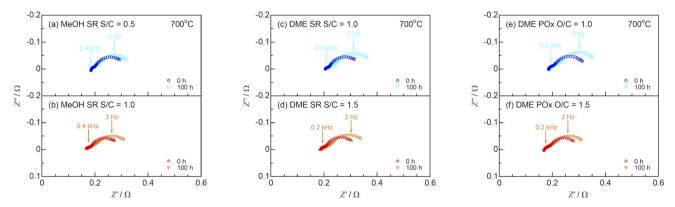


Fig. 13 Impedance spectra for SOFCs during (a and b) steam reforming (SR) of MeOH, (c and d) SR of DME, and (e and f) partial oxidation reforming (POx) of DME before and after the durability tests at 700 °C.

was large, degrading the negatrode performance in charge transfer and gas diffusion processes during internal reforming of MeOH and DME. Thus, optimizing the negatrode microstructure is important for improving the initial performance and durability of co-electrolysis SOECs and internal reforming SOFCs.

3.3 Carbon-neutral energy system using co-electrolysis SOECs and internal reforming SOFCs

Fig. 16 shows a schematic of the carbon-neutral energy system using co-electrolysis SOECs and internal reforming SOFCs. CO₂ is captured from the exhaust gas of plants and directly from the air (DAC).⁹⁻¹¹ Renewable energy sources such as solar and wind

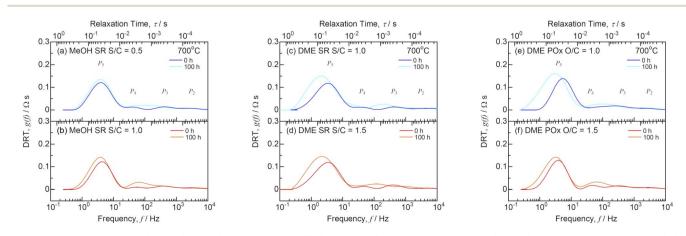


Fig. 14 DRT spectra for SOFCs with (a and b) steam reforming (SR) of MeOH, (c and d) SR of DME, and (e and f) partial oxidation reforming (POx) of DME before and after the durability tests at 700 °C.

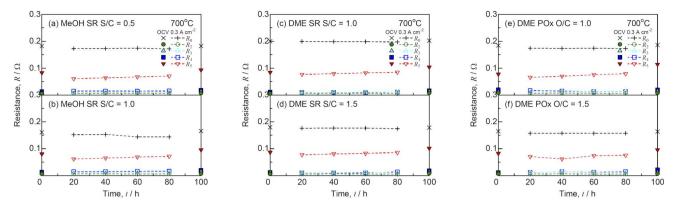


Fig. 15 Time courses of resistances for SOFCs with (a and b) steam reforming (SR) of MeOH, (c and d) SR of DME, and (e and f) partial oxidation reforming (POx) of DME during the durability test at a constant current density of 0.3 A cm⁻² and 700 °C.

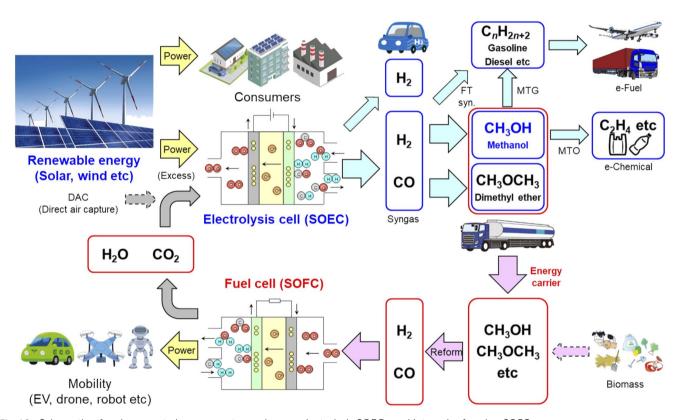


Fig. 16 Schematic of carbon-neutral energy system using co-electrolysis SOECs and internal reforming SOFCs

power are supplied to consumers such as houses, buildings, and plants. The excess electric power is converted into chemical energy. Hydrogen is produced using SOECs in addition to alkaline and PEM electrolysis, and can be used in stationary fuel cells and fuel cell vehicles.7 Syngas is also produced using SOECs, and converted into MeOH and DME.20-22,28 Synthetic gasoline, kerosene, and diesel (e-fuel) are produced from syngas via FT synthesis, and can be used for airplanes, vessels, and large vehicles. 18,19 Methanol can be converted into gasoline (MTG; methanol to gasoline), olefin (MTO; methanol to olefins) such as ethylene and propylene, and aromatics (MTA; methanol to aromatics) such as benzene, toluene, and xylene. MTO widely

contributes to carbon-neutral manufacturing processes for commodity plastics (e-chemical), whereas the raw materials of engineering plastics such as polycarbonate and polyurethane are directly synthesized from CO2.41 MeOH is a liquid at ordinary temperatures and pressures, and DME is easily liquified at 0.6 MPa. Therefore, MeOH and DME are promising energy carriers and fuels for internal reforming SOFCs. Biomass is also used as a fuel in SOFCs after desulfurization and reforming. Although CO2 is exhausted from internal reforming SOFCs, it can be used for co-electrolysis SOECs. Mass and heat balance should be considered to achieve carbon neutrality. Thus, coelectrolysis SOECs and internal reforming SOFCs significantly contribute to achieving a carbon-neutral society.

4. Conclusion

In the present work, $\rm H_2O/CO_2$ co-electrolysis SOECs and internal reforming SOFCs using MeOH and DME were investigated using negatrode-supported microtubular cells with the same cell configuration. The co-electrolysis performance decreased with increasing $\rm CO_2$ concentration in the input gas owing to an increase in polarization resistance related to gas diffusion process at the negatrode. The diffusion of $\rm CO/CO_2$ mixture was more difficult than that of $\rm H_2/H_2O$ mixture in the SOEC negatrode. The gas diffusion resistance increased with time during co-electrolysis SOECs at $\rm H_2O/CO_2 = 2$ and 700 °C. At various $\rm H_2O/CO_2$ ratios, the faradaic efficiencies exceeded 96%, and the $\rm H_2/CO$ ratios of the product gases were almost identical to the $\rm H_2O/CO_2 = 2$, the faradaic efficiency and $\rm H_2/CO$ ratio of the product gas were stable for 100 h.

MeOH and DME can be produced industrially from syngas with an H₂/CO ratio of 2. The I-V characteristics were similar during internal reforming of MeOH and DME. The polarization resistances related to charge transfer and gas diffusion processes increased with time during internal reforming of MeOH and DME. Thus, the gas diffusion resistance should be decreased to improve the initial performance and durability of co-electrolysis SOECs and internal reforming SOFCs. In thermodynamic equilibrium, carbon is deposited at S/C <0.3 for MeOH, and at S/C <0.8 and O/C <0.9 for DME during steam and partial oxidation reforming, respectively. The internal reforming SOFCs successfully operated for 100 h at S/C ≥0.5 for MeOH, S/C \geq 1.0 and O/C \geq 1.0 for DME. Therefore, MeOH and DME syntheses from syngas via co-electrolysis SOECs and power generation via internal reforming SOFCs using MeOH and DME will contribute to achieving a carbon-neutral society.

Author contributions

Hirofumi Sumi: conceptualization, methodology, resources, data curation, investigation, writing – original draft preparation.

Conflicts of interest

There are no conflicts to declare.

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