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1. Introduction

Dielectric surfaces in contact with aqueous electrolytes may charge up by dissociation of ionogenic surface groups or by adsorption of ions, and develop an electric double layer (EDL) by counterion accumulation.¹ Due to pH-driven charge regulation,² this process depends on the surface chemistry and the pH of the adjacent electrolyte solution.³⁻⁵ Further, the type of added electrolytes and its concentration influence the charge state.⁶⁻⁹ In addition, it varies with the degree of double layer overlap between suspended dielectric particles.^{10–13} Constituting a many-body soft matter system, the charging process and the structure of the EDL are of fundamental interest but at the same time are quite complex.^{1,2} Approaches on different levels of sophistication have been developed for theoretical calculations of the charge state of dielectric surfaces¹⁴⁻²² as well as for the determination of electro-kinetic properties and their interpretation.²³⁻³² Moreover, charging bears important implications for the functioning of dielectric surfaces in many contexts

CO₂-induced drastic decharging of dielectric surfaces in aqueous suspensions[†]

Peter Vogel, 🕑 *^a David Beyer, 🕑 ^b Christian Holm 🕑 ^b and Thomas Palberg 问 ^a

We study the influence of airborne CO₂ on the charge state of carboxylate stabilized polymer latex particles suspended in aqueous electrolytes. We combine conductometric experiments interpreted in terms of Hessinger's conductivity model with Poisson-Boltzmann cell (PBC) model calculations with charge regulation boundary conditions. Without CO₂, a minority of the weakly acidic surface groups are dissociated and only a fraction of the total number of counter-ions actually contribute to conductivity. The remaining counter-ions exchange freely with added other ions like Na⁺, K⁺ or Cs⁺. From the PBCcalculations we infer a corresponding pK_a of 4.26 as well as a renormalized charge in reasonably good agreement with the number of freely mobile counter-ions. Equilibration of salt- and CO₂-free suspensions against ambient air leads to a drastic de-charging, which exceeds by far the expected effects of to dissolved CO₂ and its dissociation products. Further, no counter-ion-exchange is observed. To reproduce the experimental findings, we have to assume an effective pK_a of 6.48. This direct influence of CO₂ on the state of surface group dissociation explains our recent finding of a CO₂-induced decrease of the ζ -potential and supports the suggestion of an additional charge regulation caused by molecular CO₂. Given the importance of charged surfaces in contact with aqueous electrolytes, we anticipate that our observations bear substantial theoretical challenges and important implications for applications ranging from desalination to bio-membranes

ranging from biology over climate physics to waste water treatment.^{33–37}

A particularly interesting class of potentially chargeregulating additives are dissolved molecular gases like O2, N2 and CO₂. These are inevitably present in any system allowed to have contact with ambient air^{38,39} including standard doubly distilled water or dialyzed systems, but can be efficiently removed by degassing. Molecular gases may adsorb reversibly on dielectric surfaces,40,41 alter the surface structure,42 and influence the colloid stability.^{43,44} Unlike its inert counterparts, CO₂ partially dissociates to form carbonic acid,^{38,39,45} which in turn provides additional screening electrolyte and shifts the pH.46 Increasing the electrolyte content affects double layer extension leading to a drop in the Debye screening length. At the same time, a decrease in bulk pH affects the charge state by a shift in the surface group dissociation equilibrium⁴⁷⁻⁴⁹ thus resulting in altered suspension properties.^{50,51} It therefore is paramount to work at well-defined CO_2 -concentrations,⁵² e.g., by initial selective CO2-removal via exhaustive ion exchange in air-tight vessels or closed conditioning circuits and subsequent addition via contact with ambient air.23,53,54

Recently, we performed electrophoretic experiments at constant background concentrations of the inert gases but various concentrations of molecular CO_2 .⁵⁵ There, we found the effects of molecular CO_2 on the charge state of dielectric surfaces to go

^a Institute of Physics, Johannes Gutenberg University, 55128 Mainz, Germany. E-mail: petvogel@uni-mainz.de

^b Institut für Computerphysik (ICP), Universität Stuttgart, 70569 Stuttgart, Germany † Electronic supplementary information (ESI) available. See DOI: https://doi.org/

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way beyond the expected effects of screening and pHvariation.^{10,47,48,56} In particular, upon equilibration in contact with ambient air, the magnitudes of the electrokinetic ζ -potential dropped significantly. The process could be driven even further towards full decharging by equilibrating the suspension against pure CO₂-atmospheres.⁵⁷ Accompanying MD simulations revealed the formation of a thin, diffuse layer of molecular CO₂ very close to the surface for both hydrophobic and hydrophilic dielectric materials. From that, we proposed dielectric charge regulation as the underlying mechanism:⁵⁵ the presence of CO_2 lowers the local dielectric constant and thus enhances the electrostatic interaction at and/or between dissociated surface groups. The corresponding Coulombenergy causes an increase of the dissociation energy and/or introduces an energetic penalty for closely spaced surface groups. In effect this leads to a decrease of the ζ -potential. However, no direct information on the degree of dissociation, the bare charge, the effective charge or the surface chemistry is obtained from electrophoretic experiments.

The present study therefore complements our previous investigations by a comprehensive conductometric charge characterization as well as by Poisson-Boltzmann cell (PBC) model calculations with charge regulation boundary conditions. As a model system, we use negatively charged polystyrene particles of low size dispersity carrying ionizable carboxylate groups from synthesis. Specifically, we perform conductivity experiments in dependence on different variables, like number density, n, or type and concentration c of added 1:1 electrolyte (NaCl, HCl, NaOH). Our results are interpreted within Hessinger's model of independent ion migration.⁵⁸ The model gives access to three complementary charge numbers: the number of ionogenic surface groups N, the bare charge, Z, and the number of freely mobile counter-ions, *i.e.*, the effective conductivity charge Z_{a} . It successfully described the density and temperature dependent conductivity of deionized and decarbonized suspensions,⁵⁹ it applies to single component suspensions as well as mixtures thereof.54 While a rigorous theoretical description of the relation between different effective charges is still under discussion^{60–62} experimentally determined effective conductivity charges generally agree rather well with effective electrokinetic charges and with renormalized charges, at least as long highly charged particles in 1:1 electrolytes are considered.^{8,25}

We compare experiments in the absence and presence of CO_2 to isolate and discuss the effects of carbonization. We show that the presence of CO_2 has significant quantitative and even qualitative effects on the resulting density- and concentration-dependent conductivities which go way beyond the effects expected for dissolved CO_2 and its dissociation products. Next to an overall CO_2 -induced decharging, manifest *via* decreased bare and effective charges, we observe the absence of ion-exchange between the immobile and mobile EDL populations. This unexpected finding is shown by the PBC-calculations to relate to a significant increase of the effective surface group pK_a . Our results therefore confirm and extend the results of our previous electrophoretic experiments in several ways. We anticipate that our findings will stir further

theoretical interest in the structure and properties of the EDL at charged dielectric surfaces under ambient conditions and may contribute to a fundamentally improved understanding of the resulting performance of dielectric surfaces.

In what follows, we first shortly introduce the experimental system and our conditioning procedure techniques before describing the actual conductivity measurements and recalling Hessinger's conductivity model. The results section shows the obtained conductivities and interprets these in terms of characteristic charge numbers. We rationalize our findings using complementary Poisson–Boltzmann cell model calculations. We then discuss our findings in relation to the recently proposed decharging of dielectric surfaces by adsorbed molecular CO_2 . We conclude with a short outlook on further experiments and some practical consequences of our results.

2. Materials and sample preparation

We used spherical copolymer particles synthesized by radical emulsion-polymerization from 60% w/w butylacrylamide, 38% w/w styrene, 2% w/w acrylic acid, and 0.5% w/w sodiumperoxodisulfate, kindly provided by BASF, Ludwigshafen (Lab code PNBAPS359, manufacturer batch number 2168/7390). Their diameter of 2a = 359 nm was determined by the manufacturer using analytical ultracentrifugation. Stock suspensions of particle number densities $n \approx 1 \times 10^{18} \text{ m}^{-3}$ were prepared by dilution with deionized (DI) water. Subsequently, mixed-bed ion exchange resin (IEX) (Amberjet, Carl Roth GmbH + Co. KG, Karlsruhe, Germany) was added and the suspensions were left to stand under occasional stirring for some weeks. They were then coarsely filtered using Sartorius 5 µm syringe-driven membrane filters to remove dust, ion-exchange debris, and coagulate regularly occurring upon first contact with IEX. All further sample preparation/conditioning steps including the conductivity measurements were performed in a peristaltically driven circuit described in detail elsewhere.54

Briefly, appropriately diluted stock suspensions were loaded into the circuit under filtering with Sartorius 1.2 µm and 0.8 µm filters. Then, the suspension is pumped through the air-tight tubings connecting (i) the IEX filled ion exchange chamber, (ii) a reservoir under inert gas atmosphere (Ar) to add suspension, water, or electrolyte solutions, (iii) the conductivity measurement cell and (iv) a rectangular quartz-cell (5 mm × 10 mm) for turbidity measurements⁵² for *in situ* control of the number density, $n = 3\Phi/(4\pi a^3)$, respectively the particle volume fraction, Φ .

3. Conductivity experiments

Bulk conductivities, σ , were measured at a frequency of ω = 400 Hz (electrodes LTA01 and LR325/01 with bridge LF538 or electrode LR325/001 with bridge LF340, WTW, Germany). This frequency is low enough to stay in the DC-limit, but large enough to avoid electrode polarization effects.

For measurements starting from the thoroughly deionized and decarbonized reference state, the sample is cycled until after about an hour a stable minimum conductivity is reached. Control experiments with pure water yield a background conductivity of $\sigma_{\rm B} = (55-60)$ nS cm⁻¹ due to auto-dissociation of water. For experiments in presence of CO₂, thoroughly deionized and decarbonized suspensions are brought into contact with ambient air by opening the reservoir while cycling under bypass of the IEX column. After about half an hour, the CO₂ dissolving and dissociation reactions have equilibrated increasing $\sigma_{\rm B}$ by the amount of carbonic acid present in solution. In the electrolyte concentration dependent measurements, starting from either state, the IEX column was bypassed and electrolyte solution (Titrisol 0.1 mol L⁻¹ NaCl, HCl or NaOH, Merck, Germany) was added in small quantities under conductometric control.

Measured conductivities are interpreted using Hessinger's conductivity model and reported in terms of charge numbers. This model approximates the radial dependence of micro-ionic diffusivities¹² by considering a bimodal distribution of either zero or bulk mobility for the counter-ions. The composition of both fractions is assumed to be identical. Assuming Drude-type conductivity, the model sums over the conductivity contributions of all ionic species *i*:

$$\sigma = \sum_{i} n_{i} e z_{i} \mu_{i} \tag{1}$$

Here, *e* is the elementary charge, n_i is the number density, μ_i the mobility, and z_i the valency of any species, respectively. Note that the sum includes the contributions of particles, counter-ions, ions from water auto-protolysis, added (and reacted) electrolyte ions as well as the dissociation products of CO₂. The respective micro-ionic mobilities μ_i are taken from literature,⁶³ while the particle mobilities $\mu_{\rm P}$ are determined in independent experiments.52 To be specific, we consider a 1:1 electrolyte at T = 298.15 K, where the valence is $z_i = 1$, and the number density of each micro-ionic species is $n_i = c_i 1000 N_A$, with c_i being the electrolyte molar concentration. At ambient conditions, the saturation concentration of ambient CO2 dissolved in water amounts to $c_{\rm CO_2}$ = 1.18 \times 10⁻⁵ mol L⁻¹ ($n_{\rm CO_2}$ = 7.1 \times 10^{21} m⁻³). Due to partial dissociation of its reaction product carbonic acid, $c_{\text{HCO}_3^-} = c_{\text{H}^+} = 3.16 \text{ }\mu\text{mol }\text{L}^{-1}$, and we have $pH = 5.5.^{46}$ Further, at 298.15 K, the bulk mobilities of particles, H⁺, OH⁻, CO₃H⁻, Na⁺, and Cl⁻ are $\mu_{\rm P} \approx (2-5) \times 10^{-8} \, {\rm m}^2 \, {\rm s}^{-1} \, {\rm V}^{-1}, {}^{52}$
$$\begin{split} & \mu_{\rm H^+} = 36.23 \times 10^{-8} \text{ m}^2 \text{ s}^{-1} \text{ V}^{-1}, \ \mu_{\rm OH^-} = 20.52 \times 10^{-8} \text{ m}^2 \text{ s}^{-1} \text{ V}^{-1}, \\ & \mu_{\rm HCO_3^-} = 4.61 \times 10^{-8} \text{ m}^2 \text{ s}^{-1} \text{ V}^{-1}, \ \mu_{\rm Na^+} = 5.19 \times 10^{-8} \text{ m}^2 \text{ s}^{-1} \text{ V}^{-1}, \\ & \text{and} \ \mu_{\rm CI^-} = 7.91 \times 10^{-8} \text{ m}^2 \text{ s}^{-1} \text{ V}^{-1}, \text{ respectively.}^{63} \end{split}$$

This yields a general expression to describe the conductivity of suspensions containing negatively charged particles with their counter-ions and additional non-reacting 1:1 electrolyte:

$$\sigma = ne(\mu_{\rm P} + \langle \mu^+ \rangle) + M(\langle \mu^+ \rangle + \langle \mu^- \rangle) + \sigma_{\rm B}$$
(2)

Here, we used the arithmetic means of all cationic (+), respectively anionic (-) micro-ionic mobilities:

$$\langle \mu^+ \rangle = \frac{\sum_i \mu_i M_i^+}{\sum_i M_i^+}$$
(3a)

$$\langle \mu^{-} \rangle = \frac{\sum_{i} \mu_{i} M_{i}^{-}}{\sum_{i} M_{i}^{-}}$$
(3b)

including the Z protonic counter-ions in eqn (3a). We further introduced the number of added micro-ions of species *i* per particle, $M_i = n_i/n = c1000N_A/n$. Their total number then is $M = \sigma M_i$. The background concentration of micro-ions, $\sigma_{\rm B}$, is composed of contributions of ions from water autodissociation, from residual ions e.g., leaking from the container walls, and from partially dissociating CO2. In deionized, decarbonized water, the contribution to the micro-ionic concentration from auto-dissociation is $c \approx 2 \times 10^{-7}$ mol L⁻¹, yielding $\sigma_{\rm H_2O}$ = 55 nS cm⁻¹. This contribution is important in systems of very small n.⁵² The level of unidentified small ions typically does not exceed $c \approx 10^{-8}$ mol L⁻¹,⁶⁴ and its conductivity contribution can usually be neglected. However, suspensions equilibrated against ambient air contain small amounts of carbonic acid, and we use $\sigma_{CO,H_2} = 3.16 \ \mu mol \ L^{-1} \ 1000 N_A e$ $(\mu_{\rm H^+} + \mu_{\rm HCO_2^-}).^{65}$

4. Experimental results

4.1 Particle number density dependent conductivities in the deionized state

Fig. 1 compares the particle number density dependence of the background-corrected conductivity of deionized suspensions in the decarbonized state and the CO₂-equilibrated state. In both cases, we obtain a strictly linear dependence of the background corrected conductivity on the particle number density (dashed lines). However, in the presence of ambient CO₂, we observed a significantly lower slope. For evaluation, we rewrite eqn (2) to read:

$$\sigma = \sigma_0 + \sigma_{\rm B} = neZ_{\sigma}(\mu_{\rm P} + \mu_{\rm H^+}) + \sigma_{\rm B}.$$
 (4)

Least squares fits of eqn (4) to the data in Fig. 1 (dashed lines) yield $Z_{\sigma} = (2.35 \pm 0.04) \times 10^3$ for the decarbonized and $Z_{\sigma} = (1.30 \pm 0.07) \times 10^3$ for the CO₂-saturated state. Where not indicated otherwise, quoted errors denote the standard error at a confidence level of 0.95. The corresponding diffuse layer charge-densities are: $|\sigma_{\rm el}| = (9.3 \pm 0.1) \times 10^{-2} \,\mu{\rm C \ cm^{-2}}$ and $|\sigma_{\rm el}| = (5.1 \pm 0.1) \times 10^{-2} \,\mu{\rm C \ cm^{-2}}$, respectively, where $|\sigma_{\rm el}| = Z_{\sigma}e/4\pi a^2$.³⁷ We thus see a 45% reduction of the conductivity charge in the presence of CO₂.

4.2 Conductivity titration with NaOH

Upon adding a reactive species like NaOH to thoroughly deionized and decarbonized suspensions, we observe the well-known non-monotonic conductivity dependence in Fig. 2a.^{3,5} Each background-corrected data set shows an initial, roughly linear descent. Past the minimum we observe a moderate, again roughly linear ascent, which steepens past the equivalence point. For increasing *n*, the minima shift upward and further to the right. In Fig. 2b, we replot the data *versus M*⁺.



Fig. 1 Density-dependent conductivity of deionized colloidal suspensions. Background-corrected conductivities as a function of number density *n* for the two representative states as indicated in the key. The upper scale shows the volume fraction, $\Phi = (4/3)\pi a^3 n$ with 2a = 359 nm being the particle diameter. The dashed lines are least squares fits of eqn (4) returning values of $Z_{\sigma} = (2.35 \pm 0.04) \times 10^3$ and $Z_{\sigma} = (1.30 \pm 0.07) \times 10^3$ for the CO₂-free and the CO₂-saturated cases, respectively.

Now the minima are at the same salt concentration. From fits of linear functions to the middle and final parts we infer the total number of surface groups to be $N = (134 \pm 2) \times 10^3$. During the initial, *n*-dependent decrease of conductivity, only dissociated ions are exchanged. Eqn (2) reads:

$$\sigma - \sigma_{\rm B} = \sigma_0 + ne\Delta\mu M^+ \frac{Z_\sigma}{Z} \tag{5}$$

Here the mobility difference $\Delta \mu = \mu_{\text{Na}^+} - \mu_{\text{H}^+}$ has been introduced. The initial slope is $d\sigma/dM^+ = ne\Delta\mu Z_{\sigma}/Z$. With Z_{σ} taken from the density dependent experiment at no added salt, fits of eqn (5) to the initial descent yield the charge ratio Z_{σ}/Z , respectively the bare charge *Z*. From the fits shown in Fig. 2b as red solid lines, we obtain an average charge ratio of $Z_{\sigma}/Z = 0.23$ (Fig. S1 in the ESI†) and an average value for the bare charge of $Z = (10.4 \pm 0.5) \times 10^3$.

4.3 Addition of non-reacting electrolyte

For the addition of 1:1 electrolytes to our suspensions of negatively charged colloidal spheres, we started from either a thoroughly deionized, salt and CO_2 -free, or from a thoroughly deionized state subsequently equilibrated against ambient air. Fig. 3 compares the background-corrected conductivities for different *n* upon addition of a simple strong acid (HCl) and a simple electrolyte (NaCl). For HCl, we observe a linear increase irrespective of the state of carbonization (Fig. 3a and b). For NaCl, the situation is qualitatively different in the absence and presence of CO_2 . In the decarbonized state (Fig. 3c), the curves initially show a steep increase. They then bend over and continue in a linear fashion at lesser slope. With increasing *n*, the cross-over region between the two characteristic slopes shifts towards higher *c*. In the presence of CO_2 , the dependence is again linear (Fig. 3d).

For each situation, the data collapse on single master curves, when scaled by the particle number density and plotted *versus* number of added cations per particle, M (Fig. S2 and S3 in the ESI†). To isolate the conductivity contribution of added electrolyte per particle, $(\sigma - \sigma_0 - \sigma_B)/n$, data are additionally corrected for the particle contribution to conductivity, σ_0 (Fig. S4 and S5 in the ESI†). In Fig. 4, we show the collapsed data for the addition of NaCl to CO₂-free and to CO₂-equilibrated suspensions. Fig. 4a and c focus on the initial stages of the titrations



Fig. 2 CO₂-free conductometric titration with NaOH. (a) Background-corrected conductivities in dependence on the concentration of added NaOH. Data are taken for different number densities as indicated in the key. (b) The same, now plotted in dependence on the number of cations added per particle. Dashed and dotted black lines denote fits of linear functions to the middle and final part of the curves, respectively. From their crossing point, we infer a total number of ionizable surface groups of $N_{CO_2H} = (134 \pm 2) \times 10^3$. The red solid lines are least squares fits of eqn (5) to the data. From these, we obtain an average value for the bare charge of $Z = (10.4 \pm 0.5) \times 10^3$.



Fig. 3 Electrolyte concentration dependent conductivities of initially deionized suspensions. Background corrected conductivities for CO₂-free (left) and CO₂-equilibrated (right) conditions and different number densities as indicated in the key. (a) and (b) Addition of a monoprotic strong acid: HCL. (c) and (d) Addition of a monovalent simple electrolyte: NaCL.

and emphasize the different shapes of the master curves. Without CO_2 , the addition of small amounts of NaCl yields a bent curve initially following the limiting conductivity contribution of HCl. At larger *M*, the curve straightens and runs parallel to the limiting conductivity contribution of NaCl. In the presence of CO_2 , we obtain a linear increase with a slope corresponding to the limiting conductivity contribution of NaCl. Fig. 4b and d highlight the collapse of data taken at different *n* over several orders of magnitude in salt concentration. In the absence of CO_2 we see a well-defined transition between the two linear regimes with its turning point occurring around $M \approx 1 \times 10^4$.

To describe the data quantitatively, we rewrite eqn (2) to read:

$$(\sigma - \sigma_0 - \sigma_{\rm B})/n = e(Z_{\sigma}(\langle \mu^+ \rangle - \mu_{\rm H^+}) + M(\langle \mu^+ \rangle + \mu_{\rm Cl^-}))$$
(6)

Note that with Z_{σ} known from the previous experiment, the only free parameter in eqn (6) is the charge ratio Z_{σ}/Z , respectively the bare charge *Z* entering *via* $\langle \mu^+ \rangle$ (see also Fig. S8 of the ESI†). Fits of eqn (6) to the data use the conductivity charges $Z_{\sigma} = (2.35 \pm 0.04) \times 10^3$ and $Z_{\sigma} = (1.30 \pm 0.07) \times 10^3$ as input for the CO₂-free and the CO₂-saturated state, respectively.

They return $Z = (9.92 \pm 0.05) \times 10^3$ and $Z = (1.34 \pm 0.06) \times 10^3$. In the absence of CO₂, the derived bare charge is in good agreement with the result from the titrations with NaOH. However, the presence of CO₂ reduces the bare charge to about 14% of its value under CO₂-free conditions.

Within Hessinger's model, our results signify the exchange of low-mobility Na⁺ added to the mobile part of the EDL for highly mobile H⁺ stemming from the stagnant part of the EDL.⁵⁸ Initially, practically all Na⁺ are exchanged for protons and the bulk conductivity increases strongly with a slope similar to the limiting conductivity contribution of HCl. The increase slows as the compositions in the mobile and stagnant parts of the EDL approach each other. After completion of the exchange, the slope is determined solely by the addition of NaCl to water. The situation is strikingly different in the CO₂saturated case. Here, any curve bending effect is practically absent. This signifies the absence of any ion exchange between the mobile and the immobile fractions of the micro-ionic population. This can be rationalized considering the here observed coincidence of Z_{σ} and Z. The total number of freely mobile counter-ions coincides with the total number of counterions: practically all counter-ions are freely mobile at this low bare charge. The same behavior is seen for the addition of KCl



Fig. 4 Conductivity contribution of added electrolytes per particle under ideal (no CO_2) and environmental conditions (with CO_2). The data are plotted in dependence on the number of Na⁺ added per particle, *M*. The red solid lines are least squares fits of eqn (6) to obtain the corresponding particle bare charge, *Z*, as indicated in the keys. For comparison, we also show the limiting conductivity contributions HCl (das-dotted) and NaCl (short dashed). (a) No CO_2 . The fit of eqn (6) returns $Z = (9.92 \pm 0.05) \times 10^3$, with the error denoting the standard error at a confidence level of 0.95. (b) Double logarithmic rendering of the same data. A transition between two linear regimes is observed at $M \approx 1 \times 10^4$. (c) and (d) With CO_2 . The fit of eqn (6) now returns $Z = (1.34 \pm 0.06) \times 10^3$.

and CsCl. This shows that the presence of exchange in the CO_2 -free state and its absence in the CO_2 -saturated state are well reproducible and independent of the type of cation used (Fig. S7 of the ESI†).

The absence of exchange seen in Fig. 4c and d is different to its non-observability upon the addition of HCl (*cf.* Fig. S4a, b and S6 of the ESI†). There, we have an identity of counter-ions and added cations. No change in average cation mobility occurs and thus no change of slope.

5. Charge renormalization of charge-regulating colloids – Poisson–Boltzmann theory

To rationalize our experimental observations, we utilize Poisson– Boltzmann theory. We employ the cell-model approximation⁶⁶ to reduce the complicated many-body system of a colloidal solution to a computationally tractable problem. Thus, we consider a single spherical colloid of radius *a*, centered in a spherical cell of radius $R = a\Phi^{-1/3}$ that is overall electroneutral. For computational convenience, we couple the cell at its outside to a reservoir at a given pH-value. Note that the reservoir is a purely theoretical construct which has no analogue in the experimental setup. Due to the spherical symmetry, the problem reduces to a onedimensional problem in the radial coordinate $r \in [a, R]$. In order to obtain the (reduced) electrostatic potential Ψ and the distribution of ions, we solve the Poisson–Boltzmann equation

$$\left(\frac{\mathrm{d}^2}{\mathrm{d}r^2} + \frac{2}{r}\frac{\mathrm{d}}{\mathrm{d}r}\right)\Psi(r) = \kappa_0^2\sinh(\Psi(r)),\tag{7}$$

where $\kappa_0 \equiv \sqrt{8\pi\lambda_{\rm B}n_0}$ is the inverse Debye length of the reservoir with $\lambda_{\rm B} = e^2/(4\pi\varepsilon_0\varepsilon_{\rm r}k_{\rm B}T)$ denoting the Bjerrum length. In the

1

salt-free (apart from the autoionization) case considered here, n_0 and thus κ_0 is fully determined by the pH-value of the reservoir:

$$n_0 = \max(10^{-pH_{\rm res}}, 10^{-(14-pH_{\rm res})}) \bmod L^{-1}N_{\rm A}.$$
 (8)

The PB equation given in eqn (7) is a second-order ODE that has to be supplemented with two boundary conditions. At the cell boundary, the electric field has to vanish due to the overall electroneutrality, resulting in the Neumann boundary condition

$$\Psi'(R) = 0. \tag{9}$$

At the surface of the colloidal particle, the condition

$$\Psi'(a) = \frac{-Z\lambda_{\rm B}}{a^2} \tag{10}$$

has to hold, where Z is the (dimensionless) charge of the colloid. However, due to the charge regulating nature of the surface groups, Z is not fixed but also depends on the potential:

$$Z = -N\alpha(pH_{surface}, pK_a) = -N\alpha(pH_{res} + \log_{10}(e)\Psi(a)pK_a).$$
(11)

Here, *N* is the total number of ionizable surface groups and α is the average degree of their ionization and *e* is Euler's number. The specific functional form of α depends on the employed model of charge regulation. In our calculations, we employ the Henderson–Hasselbalch equation

$$\alpha_{\rm HH} = \frac{1}{1 + 10^{pK_{\rm a} - pH_{\rm surface}}},\tag{12}$$

which is equivalent to the Langmuir isotherm.²⁰ Eqn (10)–(12) form the self-consistent charge regulation boundary condition of Ninham and Parsegian.⁶⁷ Note that the Langmuir isotherm in the Ninham–Parsegian theory neglects correlation effects between nearby sites on the colloidal surface.^{20,22} Consequently, the pK_a -values reported in the following are understood to be "effective" pK_a -values that approximately account for the electrostatic interactions between the surface groups.

the open-source library SciPy.68 To solve the PB equation with the specified boundary conditions for a given value of pH_{res} numerically, we use an iterative procedure, where the charge Zof the colloid is adjusted until self-consistency is achieved. Because the colloidal particle cannot leave the cell, there emerges a Donnan potential $\Psi(R)$ between the reservoir and the cell, leading to a concentration difference of protons. In order to obtain the bare charge of the colloid for a desired bulk pH-value (which we identify with the local pH-value at the cell boundary, $pH_{bulk} = pH_{res} + \Psi(R)\log_{10}(e)$ we solve the PB equation for a range of reservoir pH-values, calculate the bulk pH for each of them and linearly interpolate the result to the desired bulk pH-value. Similarly, we obtain the renormalized/ effective charge of the colloid, which we calculate from our numerical solution using the analytical prescription of Trizac et al.¹⁷ Note that there exist several distinct charge renormalization schemes, which result in slightly differently effective charges.⁶¹ However, given the inherent uncertainty of the experimental system, we argue that the choice of the method is only of secondary importance and we opt for the most popular one. To ensure numerical stability of the solver, we start at a very low pH-value, where the colloid is barely charged, and increase the pH-value only in small steps. In each step, the numerical solution of the previous pH-value is used as initial guess, which leads to rapid convergence and avoids numerical instabilities. Fig. 5 displays the results obtained for the present particles of a = 179.5 nm, $N = 134 \times 10^3$ and $\Phi = 4 \times 10^{-3}$.

We use the boundary value problem solver implemented in

In Fig. 5a we show the calculated bare charge as a function of the surface-group pK_a -value for the two experimentally realized situations. The corresponding average bare charges from the experiments are indicated as dashed lines of the same color. In the CO₂-free state, we consider pH_{bulk} = 7.0. Within the considered charge regulation model, we can identify a value of $pK_a \approx 4.26$ leading to the dissociation of $Z \approx 10\,000$ surface groups. In the CO₂-equilibrated state we consider pH_{bulk} = 5.5 and $c_B = 3.16 \,\mu$ mol L⁻¹ and the experimentally determined bare



Fig. 5 Results from PBC-calculations. Comparison of results for the two different situations indicated in the key: salt and CO_2 -free state at pH_{bulk} = 7 (blue) and CO_2 -equilibrated state at pH_{bulk} = 5.5 (orange). (a) Bare charges obtained for different surface group pK_a (solid lines) to the experimentally observed bare charges (dashed horizontal lines). The crossing point yields surface pK_a of 4.26 and 6.48, respectively. (b) Renormalized charge as a function of the bare charge. The black dashed line indicates the condition $Z_{PBC} = Z$.

charge is $Z \approx 1340$. We observe a drastic change in the surfacegroup pK_a needed to realize this bare charge. In fact, the pK_a shifts to an effective value of $pK_a \approx 6.48$.

The decrease of bare charge is mirrored by the accompanying decrease of the renormalized charge. Fig. 5b shows the theoretically calculated renormalized charge as a function of the bare charge for both considered bulk pH-values. Initially following the relation $Z_{PBC} = Z$, it bends over and approaches a limiting value. Note that with CO₂, there are overall more ions in the cell, and, consistent with the results of Alexander *et al.*,¹⁵ the renormalized charge shows a larger saturation value. At pH_{bulk} = 7.0, where the experimentally determined average bare charge was $Z = (10.4 \pm 0.5) \times 10^3$, the theory predicts a renormalized charge of $Z_{PBC} = 2100$. For pH_{bulk} = 5.5, where the experimentally determined bare charge was Z = 1340, the theory predicts a renormalized charge of $Z_{PBC} = 1170$.

6. Discussion

We summarize our findings in Fig. 6. Fig. 6a shows the results for the CO₂-free cases. The average values of $N = (134 \pm 2) \times 10^3$, $Z = (10.4 \pm 0.5) \times 10^3$ and $Z_{\sigma} = (2.35 \pm 0.04) \times 10^3$ reflect the well-known sequence of charge number magnitudes: $N \gg Z > Z_{\sigma}$. Only a very small part of the weakly acidic surface groups is dissociated and only a fraction of the total number of counter-ions is actually mobile. From the PBC-calculations with pH-driven charge regulation (Fig. 5a) we infer a corresponding pK_a of 4.26. This is slightly lower than previously reported values for carboxylate stabilized particles.³ However, it appears well-compatible with a dominance of carboxylate surface groups and a small admixture of a few sulfate groups stemming from the initiator. The calculations further predict a renormalized charge of $Z_{\rm PBC} = 2.1 \times 10^3$. This figure is in reasonable agreement with the experimentally obtained value. The small deviation is attributed to the simplifications made in the present theoretical approach, *e.g.*, the neglect of microscopic surface geometry and of ion correlations. Overall, the comparison demonstrates the excellent performance of Hessinger's conductivity model.

In Fig. 6b, we replot the Z- and Z_{σ} -data from the CO₂-free experiments on an enlarged scale and compare them to the results obtained in the presence of CO_2 (reddish symbols). For the latter, we found an average bare charge of $Z = (1.34 \pm 0.06) \times 10^3$ and an average conductivity charge of Z_{σ} = (1.30 \pm 0.06) \times 10³. If CO_2 had no influence on the p K_a , we would expect a bare charge of $Z \approx 6 \times 10^3$. However, the much smaller experimental bare charge is observed in the charge regulating PBC-calculations for an effective surface pK_a of $pK_a \approx 6.48$. The PBC-prediction for the renormalized charge at pH = 5.5 then is Z_{PBC} = 1200 in reasonable agreement with the experimentally obtained value (the small deviation is, again, attributed to the neglect of ion correlations). At such low bare charge numbers, there is no substantial charge renormalization. If we follow previous work and identify Z_{PBC} with Z_{σ} , this finding explains the absence of ion exchange in the presence of CO₂. There are, simply speaking, hardly any immobile ions to be exchanged. The final charge number magnitude sequence reads: $Z_{\sigma}^{+\mathrm{CO}_2} \approx Z^{+\mathrm{CO}_2} < Z_{\sigma}^{-\mathrm{CO}_2} \ll Z^{-\mathrm{CO}_2} \ll N.$

The drastic reduction of the effective conductivity charge and the renormalized charge in the presence of CO_2 is in line



Fig. 6 Comparison of charge numbers for different particle number densities. Here we display the individual fit results obtained at different densities for the different experiments (symbols as indicated in the keys) and the corresponding averages thereof (dashed lines). The upper scale represents the corresponding particle volume fraction, $\Phi = (4/3)\pi a^3 n$. (a) Comparison of different types of charge for the salt- and CO₂-free systems. We obtained the following averages with quoted errors denoting the standard deviation: number of dissociable surface groups $N = (134 \pm 2) \times 10^3$, average bare charge number from titration with NaOH: $Z = (10.7 \pm 0.5) \times 10^3$, average bare charge number from titration with NaOI: $Z = (10.0 \pm 0.3) \times 10^3$, barge charge number from titration with CCl: $Z = (10.5 \pm 0.1) \times 10^3$, bare charge number from titration with CCl: $Z = (10.5 \pm 0.1) \times 10^3$, bare charge number from titration with CCl: $Z = (10.5 \pm 0.1) \times 10^3$, bare charge number from titration with CCl: $Z = (10.5 \pm 0.1) \times 10^3$, bare charge number from titration with CCl: $Z = (10.5 \pm 0.1) \times 10^3$, bare charge number from titration with CCl: $Z = (10.5 \pm 0.1) \times 10^3$, bare charge number from titration with CCl: $Z = (10.5 \pm 0.1) \times 10^3$, average effective charges for CO₂-free systems (replotted from (a)) and CO₂-equilibrated systems on an enlarge scale. For the CO₂-equilibrated systems, we find the average bare charge number from titration with NaCl, $Z = (1.34 \pm 0.04) \times 10^3$ and the average effective conductivity charge, $Z_{\sigma} = (1.30 \pm 0.07) \times 10^3$.

with the previous electrophoretic results,^{55,57} where we had reported a decrease of the ζ -potential from $\zeta = (61 \pm 4)$ mV to $\zeta = (35 \pm 2)$ mV after equilibration to ambient air and even further to $\zeta = (3 \pm 2)$ mV after equilibration to a CO₂ atmosphere. These experiments could, however, not directly demonstrate an underlying decrease of the bare surface charge. The present combination of conductivity experiments under various conditions with charge-regulating PBC-calculations unequivocally revealed that CO₂ directly exerts a strong decharging effect on the bare surface charge. The reduction in ζ -potential and conductivity charge, respectively renormalized charge simply follows suit, and the absence of ion exchange effects upon the addition of pH neutral 1:1 electrolytes to CO₂-equilibrated systems is readily explained by the negligible amount of charge renormalization under these conditions.

Granting that the observed effect can be expressed as a significant shift of the surface pK_a , the observed shift is much larger than the known difference for COOH-groups in the bulk and at surfaces, which typically amounts to $\approx 0.5 \text{ pK}_{a}$ units. Further the observed shift by more than two units exceeds by far the expectable uncertainties in the theoretical calculations introduced by employing the PBC model. We therefore believe that this unforeseen observation poses a considerable challenge to explain, how dissolved molecular CO₂ could possibly influence the dissociation equilibrium. In our previous work, we had tentatively considered several alternatives regarding the underlying mechanisms. All of them were motivated by the results of our molecular dynamics simulations, where we observed the formation of a diffusely adsorbed monolayer of CO₂ very close to the surface.⁵⁵ In principle, such a layer could lead to surface modifications shifting the shear plane further outward and thus decrease the ζ -potential without influencing the particle charge.42,69 Since we here directly observed a decrease in the bare charge, we can now rule out this possibility. Alternatively, the layer could decrease the dielectric permittivity close to the surface and thus strengthen any electrostatic interactions. Enhanced attractive interactions could increase the dissociation energy. Stronger repulsion between neighboring surface charges could introduce a Coulomb penalty for dissociation. Both would counteract dissociation and the corresponding shift in effective surface pK_a would directly lower the bare charge. Which of these effects dominates the observed dielectric charge regulation cannot be decided within the present approach. A detailed treatment remains a theoretical challenge but should be accessible within recent analytic approaches accounting for spatially variable dielectric permittivities, hydrodynamics and finite ion size effects.^{32,70} It should also be in reach of computer simulations.⁷¹ Overall, we anticipate, that the present observations should motivate enhanced theoretical interest in an improved modelling of double layer properties.

On the experimental side, the CO_2 layer could be characterized further by X-ray and/or element selective neutron reflectometry.⁴⁰ Its consequences for colloid–colloid interactions could be determined with high distance resolution by colloidal probe experiments.^{2,10,11} But also the conductivity experiments could be extended to include a back-titration by HCl starting from the NaCl-saturated state. Up to now, we had studied polymer lattices stabilized by weak acids, hydrophilic silica surfaces, and super-hydrophobically coated surfaces, but also further surfaces should be addressed to firmly establish the CO_2 adsorption as general phenomenon.

A final remark addresses the implications of our findings for future experiments at low salt conditions. First, the significant influence of CO₂ on the charge state of dielectric surfaces in contact with aqueous electrolytes will require utmost care in characterizing and controlling its concentration in any precision measurement of suspension properties and surface characteristics. The techniques employed in the present paper may serve as a starting point. Second, the novel decharging effects exerted by molecular CO2 will certainly affect many surface and suspension properties. Occasional consequences of CO2contaminations have been reported.⁵¹ Möller et al. used treatment of surfaces with CO2-equilibrated DI water and subsequent partial CO₂-removal to improve control for writing and drawing in water via modified diffusiophoretic transport of the ink particles.⁷² Systematic experiments comparing the structure and phase behavior in dependence on electrolyte concentration and number density with and without CO2 are now under way and will be reported elsewhere. Overall, we believe that the controlled application of molecular CO₂ will open novel ways of manipulating the performance of functional colloidal systems and solid-water interfaces.

7. Conclusions

We demonstrated the direct influence of molecularly dissolved CO₂ on the state of surface group dissociation. We observe a drastic reduction of the number of dissociated surface groups and a halving of effective charges. Such a reduction is significantly stronger than the expected effects induced by the CO₂reaction products in salt-free water, i.e., an altered local pH and an increased salinity caused by the formation of carbonic acid which partially dissociates. The present study therefore confirmed and substantially extended previous investigations and further supported our suggestion of an additional charge regulation by CO₂. Given the relatively small concentration of CO_2 in ambient air of 421 ppm, the extent of decharging dielectric surfaces by a charge neutral molecule is equally impressive and surprising. In fact, while there existed some literature on the effects of degassing in general, the specific effects of CO₂ had been largely ignored. However, in view of the ubiquitous nature of water-solid interfaces and their importance in geology, meteorology, biology as well as in technical applications, we feel that much further research is needed to explain our unexpected findings.

Author contributions

P. V. performed the experiments and the evaluations. D. B. performed the PBC-calculations. C. H. supervised the theoretical and T. P. the experimental part. P. V. and T. P. wrote the

original manuscript. All authors contributed equally in discussing the data and finalizing the manuscript.

Data availability

Raw data are obtainable from the authors upon reasonable request. The source code used for the PB cell-model calculations is freely available on GitHub (https://github.com/davidb beyer/pb_solver).

Conflicts of interest

There are no conflicts to declare.

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References

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- 1 J. Lyklema, *Fundamentals of Interface and Colloid Science: Solid-Liquid Interfaces*, Academic Press, London, 1995, vol. II.
- 2 S. H. Behrens and M. Borkovec, Electrostatic Interaction of Colloidal Surfaces with Variable Charge, *J. Phys. Chem. B*, 1999, **103**, 2918–2928.
- 3 J. P. H. Zwetsloot and J. C. Leyte, Conductometric Titration of Latex with Acidic Surface Groups, *J. Colloid Interface Sci.*, 1994, 163, 362–371.
- 4 T. Gisler, S. F. Schulz, M. Borkovec, H. Sticher, P. Schurtenberger, B. D'Aguanno and R. Klein, Understanding colloidal charge renormalization from surface chemistry: Experiment and theory, *J. Chem. Phys.*, 1994, **101**, 9924–9936.
- 5 J. Yamanaka, Y. Hayashi, N. Ise and T. Yamaguchi, Control of the surface charge density of colloidal silica by sodium hydroxide in salt-freeand low-salt dispersions, *Phys. Rev. E: Stat. Phys., Plasmas, Fluids, Relat. Interdiscip. Top.*, 1997, 55, 3028–3036.
- 6 C. F. Zukoski and D. A. Saville, The interpretation of electrokinetic measurements using a dynamic model of the stern layer: I. The dynamic model, *J. Colloid Interface Sci.*, 1986, **114**, 32–44.
- 7 C. F. Zukoski and D. A. Saville, The interpretation of electrokinetic measurements using a dynamic model of the stern layer: II. Comparisons between theory and experiment, *J. Colloid Interface Sci.*, 1986, **114**, 45–53.

- 8 H. Reiber, T. Köller, T. Palberg, F. Carrique, E. Ruiz Reina and R. Piazza, Salt concentration and particle density dependence of electrophoretic mobilities of spherical colloids in aqueous suspension, *J. Colloid Interface Sci.*, 2007, **309**, 315–322.
- 9 I. Semenov, S. Raafatnia, M. Sega, V. Lobaskin, C. Holm and F. Kremer, Electrophoretic mobility and charge inversion of a colloidal particle studied by single-colloid electrophoresis and molecular dynamics simulations, *Phys. Rev. E: Stat., Nonlinear, Soft Matter Phys.*, 2013, **87**, 22302.
- 10 G. Trefalt, T. Palberg and M. Borkovec, Forces between colloidal particles in aqueous solutions containing monovalent and multivalent ions, *Curr. Opin. Colloid Interface Sci.*, 2017, 27, 9–17.
- 11 G. Trefalt, S. H. Behrens and M. Borkovec, Charge Regulation in the Electrical Double Layer: Ion Adsorption and Surface Interactions, *Langmuir*, 2016, **32**, 380–400.
- 12 V. Lobaskin, B. Dünweg and C. Holm, Electrophoretic mobility of a charged colloidal particle: a computer simulation study, *Phys. Rev. E: Stat., Nonlinear, Soft Matter Phys.*, 2004, 16, S4063–S4073.
- V. Lobaskin, B. Dünweg, M. Medebach, T. Palberg and C. Holm, Electrophoresis of colloidal dispersions in the low-salt regime, *Phys. Rev. Lett.*, 2007, 98, 176105.
- 14 E. J. W. Verwey, Theory of the stability of lyophobic colloids, *J. Phys. Colloid Chem.*, 1947, 51, 631–636.
- 15 S. Alexander, P. M. Chaikin, P. Grant, G. J. Morales, P. Pincus and D. Hone, Charge renormalization, osmotic pressure, and bulk modulus of colloidal crystals: Theory, *J. Chem. Phys.*, 1984, **80**, 5776–5781.
- 16 L. Belloni, Colloidal interactions, J. Phys.: Condens. Matter, 2000, 12, R549–R587.
- 17 E. Trizac, L. Bocquet, M. Aubouy and H. H. von Grünberg, Alexander's Prescription for Colloidal Charge Renormalization, *Langmuir*, 2003, **19**, 4027–4033.
- 18 Y. Levin, Electrostatic correlations: from plasma to biology, *Rep. Prog. Phys.*, 2002, **65**, 1577.
- 19 M. Heinen, E. Allahyarov and H. Löwen, Highly asymmetric electrolytes in the primitive model: hypernetted chain solution in arbitrary spatial dimensions, *J. Comput. Chem.*, 2014, **35**, 275–289.
- 20 R. Podgornik, General theory of charge regulation and surface differential capacitance, *J. Chem. Phys.*, 2018, 149.
- 21 N. Adžić and R. Podgornik, Field-theoretic description of charge regulation interaction, *Eur. Phys. J. E: Soft Matter Biol. Phys.*, 2014, 37, 5.
- 22 T. Colla, A. Bakhshandeh and Y. Levin, Charge regulation of nanoparticles in the presence of multivalent electrolytes, *J. Chem. Phys.*, 2024, 161.
- 23 N. Garbow, M. Evers, T. Palberg and T. Okubo, On the electrophoretic mobility of isolated colloidal spheres, *J. Phys.: Condens. Matter*, 2004, **16**, 3835–3842.
- 24 R. Galneder, V. Kahl, A. Arbuzova, M. Rebecchi, J. O. R\u00e4dler and S. McLaughlin, Microelectrophoresis of a Bilayer-Coated Silica Bead in an Optical Trap: Application to Enzymology, *Biophys. J.*, 2001, **80**, 2298–2309.

- 25 L. Shapran, M. Medebach, P. Wette, T. Palberg, H. J. Schöpe, J. Horbach, T. Kreer and A. Chatterji, Qualitative characterisation of effective interactions of charged spheres on different levels of organisation using Alexander's renormalised charge as reference, *Colloids Surf.*, A, 2005, 270–271, 220–225.
- 26 G. S. Roberts, T. A. Wood, W. J. Frith and P. Bartlett, Direct measurement of the effective charge in nonpolar suspensions by optical tracking of single particles, *J. Chem. Phys.*, 2007, **126**, 194503.
- 27 F. Strubbe, F. Beunis, M. Marescaux and K. Neyts, Charging mechanism in colloidal particles leading to a linear relation between charge and size, *Phys. Rev. E: Stat., Nonlinear, Soft Matter Phys.*, 2007, **75**, 31405.
- 28 A. V. Delgado, F. González-Caballero, R. J. Hunter, L. K. Koopal and J. Lyklema, Measurement and interpretation of electrokinetic phenomena, *J. Colloid Interface Sci.*, 2007, 309, 194–224.
- 29 F. Carrique, E. Ruiz-Reina, R. Roa, F. J. Arroyo and Á. V. Delgado, General electrokinetic model for concentrated suspensions in aqueous electrolyte solutions: Electrophoretic mobility and electrical conductivity in static electric fields, *J. Colloid Interface Sci.*, 2015, **455**, 46–54.
- 30 Á. V. Delgado, F. Carrique, R. Roa and E. Ruiz-Reina, Recent developments in electrokinetics of salt-free concentrated suspensions, *Curr. Opin. Colloid Interface Sci.*, 2016, 24, 32–43.
- 31 D. Botin, J. Wenzl, R. Niu and T. Palberg, Colloidal electrophoresis in the presence of symmetric and asymmetric electro-osmotic flow, *Soft Matter*, 2018, **14**, 8191–8204.
- 32 F. Carrique, E. Ruiz-Reina, F. J. Arroyo, J. J. López-García and A. V. Delgado, Effects of finite counterion size and nonhomogeneous permittivity and viscosity of the solution on the electrokinetics of a concentrated salt-free colloid, *Phys. Rev. E*, 2024, 110.
- 33 J. Gapinski, A. Wilk, A. Patkowski, W. Häussler, A. J. Banchio, R. Pecora and G. Nägele, Diffusion and microstructural properties of solutions of charged nanosized proteins: experiment versus theory, *J. Chem. Phys.*, 2005, 123, 54708.
- 34 A. Gulotta, M. Polimeni, S. Lenton, C. G. Starr, A. Stradner, E. Zaccarelli and P. Schurtenberger, Combining Scattering Experiments and Colloid Theory to Characterize Charge Effects in Concentrated Antibody Solutions, *Mol. Pharmaceutics*, 2024, 21, 2250–2271.
- 35 N. Maeda, Brief Overview of Ice Nucleation, *Molecules*, 2021, 26, 392.
- 36 M. Lukas, R. Schwidetzky, A. T. Kunert, U. Pöschl, J. Fröhlich-Nowoisky, M. Bonn and K. Meister, Electrostatic Interactions Control the Functionality of Bacterial Ice Nucleators, J. Am. Chem. Soc., 2020, 142, 6842–6846.
- 37 A. V. Delgado, M. L. Jiménez, G. R. Iglesias and S. Ahualli, Electrical double layers as ion reservoirs: applications to the deionization of solutions, *Curr. Opin. Colloid Interface Sci.*, 2019, 44, 72–84.
- 38 F. J. Millero, R. Feistel, D. G. Wright and T. J. McDougall, The composition of Standard Seawater and the definition of

the Reference-Composition Salinity Scale, *Deep Sea Res., Part I*, 2008, **55**, 50–72.

- 39 K. Gilbert, P. C. Bennett, W. Wolfe, T. Zhang and K. D. Romanak, CO₂ solubility in aqueous solutions containing Na⁺, Ca²⁺, Cl⁻, SO₄₂⁻ and HCO₃⁻: The effects of electrostricted water and ion hydration thermodynamics, *Appl. Geochem.*, 2016, **67**, 59–67.
- 40 D. A. Doshi, E. B. Watkins, J. N. Israelachvili and J. Majewski, Reduced water density at hydrophobic surfaces: Effect of dissolved gases, *Proc. Natl. Acad. Sci. U. S. A.*, 2005, **102**, 9458–9462.
- 41 S. M. Dammer and D. Lohse, Gas Enrichment at Liquid-Wall Interfaces, *Phys. Rev. Lett.*, 2006, **96**, 206101.
- 42 B. İlhan, C. Annink, D. V. Nguyen, F. Mugele, I. Siretanu and M. H. G. Duits, A method for reversible control over nanoroughness of colloidal particles, *Colloids Surf.*, A, 2019, 560, 50–58.
- 43 R. M. Pashley, Effect of Degassing on the Formation and Stability of Surfactant-Free Emulsions and Fine Teflon Dispersions, *J. Phys. Chem. B*, 2003, **107**, 1714–1720.
- 44 N. Maeda, K. J. Rosenberg, J. N. Israelachvili and R. M. Pashley, Further Studies on the Effect of Degassing on the Dispersion and Stability of Surfactant-Free Emulsions, *Langmuir*, 2004, **20**, 3129–3137.
- 45 F. J. Millero, Thermodynamics of the carbon dioxide system in the oceans, *Geochim. Cosmochim. Acta*, 1995, **59**, 661–677.
- 46 Aqion freeware program, *Aqion 8.4.1 (release 9.23)*, available at: https://www.aqion.de/, accessed 18 August 2022.
- 47 F. Carrique, E. Ruiz-Reina, F. J. Arroyo and A. V. Delgado, Dynamic electrophoretic mobility of spherical colloidal particles in realistic aqueous salt-free concentrated suspensions, *J. Phys. Chem. B*, 2010, **114**, 6134–6143.
- 48 M. Heinen, T. Palberg and H. Löwen, Coupling between bulk- and surface chemistry in suspensions of charged colloids, *J. Chem. Phys.*, 2014, **140**, 124904.
- 49 A. Bakhshandeh, D. Frydel and Y. Levin, Theory of Charge Regulation of Colloidal Particles in Electrolyte Solutions, *Langmuir*, 2022, **38**, 13963–13971.
- 50 N. Lorenz, I. Gupta and T. Palberg, Microstructural diversity, nucleation paths, and phase behavior in binary mixtures of charged colloidal spheres, *J. Chem. Phys.*, 2023, **158**, 114902.
- 51 N. Lorenz, C. Wittenberg and T. Palberg, Porous crystals in charged sphere suspensions by aggregate-driven phase separation, *Soft Matter*, 2023, **19**, 5076–5091.
- 52 D. Botin, F. Carrique, E. Ruiz-Reina and T. Palberg, Nonmonotonic concentration dependence of the electrophoretic mobility of charged spheres in realistic salt free suspensions, *J. Chem. Phys.*, 2020, **152**, 244902.
- 53 T. Okubo and H. Fujita, Phase diagram of alloy crystal in the exhaustively deionized suspensions of binary mixtures of colloidal spheres, *Colloid Polym. Sci.*, 1996, **274**, 368–374.
- 54 P. Wette, H. J. Schöpe, R. Biehl and T. Palberg, Conductivity of deionized two-component colloidal suspensions, *J. Chem. Phys.*, 2001, **114**, 7556.
- 55 P. Vogel, N. Möller, M. N. Qaisrani, P. Bista, S. A. L. Weber, H.-J. Butt, B. Liebchen, M. Sulpizi and T. Palberg, Charging

of Dielectric Surfaces in Contact with Aqueous Electrolytes – the Influence of CO₂, *J. Am. Chem. Soc.*, 2022, **144**, 21080–21087.

- 56 F. Carrique and E. Ruiz-Reina, Effects of water dissociation and CO₂ contamination on the electrophoretic mobility of a spherical particle in aqueous salt-free concentrated suspensions, *J. Phys. Chem. B*, 2009, **113**, 8613–8625.
- 57 P. Vogel and T. Palberg, Electrokinetic effects of ambient and excess carbonization of dielectric surfaces in aqueous environments, *J. Colloid Interface Sci.*, 2024, **656**, 280–288.
- 58 D. Hessinger, M. Evers and T. Palberg, Independent ion migration in suspensions of strongly interacting charged colloidal spheres, *Phys. Rev. E: Stat. Phys., Plasmas, Fluids, Relat. Interdiscip. Top.*, 2000, **61**, 5493–5506.
- 59 M. Medebach, R. C. Jordán, H. Reiber, H.-J. Schöpe, R. Biehl, M. Evers, D. Hessinger, J. Olah, T. Palberg, E. Schönberger and P. Wette, Drude-type conductivity of charged sphere colloidal crystals: Density and temperature dependence, *J. Chem. Phys.*, 2005, **123**, 104903.
- 60 A. Diehl and Y. Levin, Smoluchowski equation and the colloidal charge reversal, *J. Chem. Phys.*, 2006, **125**, 54902.
- 61 M. E. Brito, G. Nägele and A. R. Denton, Effective interactions, structure, and pressure in charge-stabilized colloidal suspensions: Critical assessment of charge renormalization methods, *J. Chem. Phys.*, 2023, 159.
- 62 T. Colla, I. M. Telles, M. Arfan, A. P. Dos Santos and Y. Levin, Spiers Memorial Lecture: Towards understanding of iontronic systems: electroosmotic flow of monovalent and divalent electrolyte through charged cylindrical nanopores, *Faraday Discuss.*, 2023, **246**, 11–46.
- 63 CRC handbook of chemistry and physics, A ready-reference book of chemical and physical data, ed. D. R. Lide, CRC Press, Boca Raton, 76th edn, 1996.
- 64 R. Niu, P. Kreissl, A. T. Brown, G. Rempfer, D. Botin, C. Holm, T. Palberg and J. de Graaf, Microfluidic pumping by micromolar salt concentrations, *Soft Matter*, 2017, 13, 1505–1518.

- 65 Electrostatic Effects in Soft Matter and Biophysics. Proceedings of the NATO Advanced Research Workshop on Electrostatic Effects in Soft Matter and Biophysics Les Houches, France 1–13 October 2000, ed. C. Holm, P. Kékicheff and R. Podgornik, Springer Netherlands; Imprint: Springer, Dordrecht, 1st edn, 2001, vol. 46.
- 66 M. Deserno and C. Holm, in *Electrostatic Effects in Soft Matter and Biophysics. Proceedings of the NATO Advanced Research Workshop on Electrostatic Effects in Soft Matter and Biophysics Les Houches, France 1–13 October 2000*, ed. C. Holm, P. Kékicheff and R. Podgornik, Springer Netherlands; Imprint: Springer, Dordrecht, 1st edn, 2001, pp. 27–52.
- 67 B. W. Ninham and V. A. Parsegian, Electrostatic potential between surfaces bearing ionizable groups in ionic equilibrium with physiologic saline solution, *J. Theor. Biol.*, 1971, **31**, 405–428.
- 68 P. Virtanen, R. Gommers, T. E. Oliphant, M. Haberland, T. Reddy, D. Cournapeau, E. Burovski, P. Peterson, W. Weckesser, J. Bright, S. J. van der Walt, M. Brett, J. Wilson, K. J. Millman, N. Mayorov, A. R. J. Nelson, E. Jones, R. Kern, E. Larson, C. J. Carey, İ. Polat, Y. Feng, E. W. Moore, J. VanderPlas, D. Laxalde, J. Perktold, R. Cimrman, I. Henriksen, E. A. Quintero, C. R. Harris, A. M. Archibald, A. H. Ribeiro, F. Pedregosa and P. van Mulbregt, SciPy 1.0: fundamental algorithms for scientific computing in Python, *Nat. Methods*, 2020, 17, 261–272.
- 69 J. E. Seebergh and J. C. Berg, Evidence of a hairy layer at the surface of polystyrene latex particles, *Colloids Surf.*, A, 1995, 100, 139–153.
- 70 J. J. López-García, J. Horno and C. Grosse, Ionic size, permittivity, and viscosity-related effects on the electrophoretic mobility: A modified electrokinetic model, *Phys. Rev. Fluids*, 2019, 4, 103702.
- N. Aho, P. Buslaev, A. Jansen, P. Bauer, G. Groenhof and B. Hess, Scalable Constant pH Molecular Dynamics in GROMACS, *J. Chem. Theory Comput.*, 2022, 18, 6148–6160.
- 72 N. Möller, L. Hecht, R. Niu, B. Liebchen and T. Palberg, Writing Into Water, *Small*, 2023, **19**, e2303741.