



Cite this: *Soft Matter*, 2024,
20, 4291

Methyl- β -cyclodextrin asymmetrically extracts phospholipid from bilayers, granting tunable control over differential stress in lipid vesicles†

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Lipid asymmetry – that is, a nonuniform lipid distribution between the leaflets of a bilayer – is a ubiquitous feature of biomembranes and is implicated in several cellular phenomena. Differential tension – that is, unequal lateral monolayer tensions comparing the leaflets of a bilayer – is closely associated with lipid asymmetry underlying these varied roles. Because differential tension is not directly measurable in combination with the fact that common methods to adjust this quantity grant only semi-quantitative control over it, a detailed understanding of lipid asymmetry and differential tension are impeded. To overcome these challenges, we leveraged reversible complexation of phospholipid by methyl- β -cyclodextrin (mbCD) to tune the direction and magnitude of lipid asymmetry in synthetic vesicles. Lipid asymmetry generated in our study induced (i) vesicle shape changes and (ii) gel–liquid phase coexistence in 1-component vesicles. By applying mass-action considerations to interpret our findings, we discuss how this approach provides access to phospholipid thermodynamic potentials in bilayers containing lipid asymmetry (which are coupled to the differential tension of a bilayer). Because lipid asymmetry yielded by our approach is (i) tunable and (ii) maintained over minute to hour timescales, we anticipate that this approach will be a valuable addition to the experimental toolbox for systematic investigation into the biophysical role(s) of lipid asymmetry (and differential tension).

Received 31st December 2023,
Accepted 1st May 2024

DOI: 10.1039/d3sm01772a

rsc.li/soft-matter-journal

Introduction

Interest in membrane lipid asymmetry dates back to the 1970s.^{1,2} In the time since, its relevance for lipid-mediated signaling,³ lipid phase separation,^{4,5} membrane shape change/bending,^{6,7} and coupling with transmembrane protein structure/activity⁸ has been considered. The lipid asymmetry of a membrane can be broken down into two contributions: (i) area asymmetry⁹/area difference^{6,7}/packing asymmetry¹⁰ – that is, unequal monolayer surface areas that two apposed leaflets would tend to favor were they uncoupled and (ii) compositional asymmetry – that is, different lipid compositions between the leaflets.¹¹ Mechanical consequences of lipid asymmetry include bending stress and differential tension.^{10,12,13} Differential tension accumulates within an asymmetric bilayer when the apposed leaflets comprising it contain unequal lateral tensions. Though differential tension may underlie a general importance of lipid asymmetry for membrane biology,^{14,15} this quantity cannot be directly measured by micromechanical techniques (such as micropipette

aspiration). This impedes investigation into the biological role of lipid asymmetry.

To this end, the molecule methyl- β -cyclodextrin (mbCD) has been an important experimental tool. mbCD reversibly forms inclusion complexes with phospholipids¹⁶ which has been leveraged for preparation of compositionally asymmetric vesicles¹⁷ and for studying activation of mechanosensitive ion channels.^{18,19} Several studies have also demonstrated the utility of mbCD for investigating the chemical activity of cholesterol.^{20–22} Motivated by these studies, we used mbCD to investigate the mechanics and thermodynamics of area asymmetry generation in 1-component bilayers.

First, we confirmed that mbCD asymmetrically extracts lipid from intact vesicles thereby generating area asymmetry. Next, we show that mbCD can be kinetically trapped with supersaturating amounts of lipid and thereby used to tune the area asymmetries of giant unilamellar vesicles (GUVs). Generation of area asymmetry in these GUVs resulted in (i) membrane bending and (ii) the generation of gel–liquid phase coexistence from a laterally homogeneous membrane. Finally, we provide estimates of the chemical activity of lipid in the outer leaflets of 1-component bilayers undergoing mbCD-mediated collapse/solubilization. We find two different values for this quantity depending on the osmotic conditions to which vesicles are

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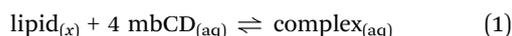
† Electronic supplementary information (ESI) available. See DOI: <https://doi.org/10.1039/d3sm01772a>



subjected. We use both values to determine microscopic/mechanical quantities in these vesicles. We begin by reviewing some details of mbCD–lipid complexation.

Description of mbCD–lipid equilibrium

A model for complexation between mbCD and bilayer-forming phospholipids was first proposed by Anderson *et al.*²³ These authors suggested that the complexes formed between monomeric phospholipid and mbCD have an average stoichiometry of 1 : 4, respectively (agreeing with structure–activity predictions drawn from complexes formed between cyclodextrins and various surfactants).^{16,24} The Anderson model maps this complexation in an mbCD–lipid phase diagram. Large enough concentrations of mbCD can solubilize all self-assembled lipid particles (vesicles) and the concentrations of mbCD and lipid at which this occurs constitute a solubilization boundary. This boundary divides phase space into two regions: (i) the coexistence region in which vesicles coexist with complexes and (ii) the solubilization region in which no vesicles persist. mbCD–lipid complexation is thought to proceed *via*:



Subscripts in eqn (1) indicate the phase of the species. The subscript (*x*) denotes that uncomplexed lipid can be present either in a bilayer (indicated by the subscript (mem)) or the solution-phase (indicated by the subscript (aq)) depending on whether a mixture lies in the coexistence or solubilization region.

Anderson *et al.* treated each bilayer according to the lipid partition model,²⁵ assuming that lipid in 1-component bilayers remains in its reference state throughout the coexistence region. This is based on the rationale that the mole fraction of the lipid component in the bilayer is fixed (regardless of extraction). However, because (i) the free energy of a lipid molecule residing within a bilayer is intimately coupled to its local chemical/mechanical environment^{26–28} combined with (ii) evidence that mbCD-mediated extraction/insertion of lipids alters membrane mechanics,^{18,29} we propose that (iii) lipid in bilayers deviate from their reference state when exposed to mbCD. We now discuss how this feature could contribute to mbCD–lipid equilibria.

To do so, we first define the equilibrium constant for mbCD–lipid complexation, K_{total} . According to eqn (1), K_{total} is given by:

$$K_{\text{total}} = \frac{\alpha_{\phi}}{\alpha_{\text{L}} \alpha_{\text{CD}}^4} \approx \frac{[\text{complex}]}{\alpha_{\text{L}} [\text{mbCD}]_{\text{free}}^4} \quad (2)$$

In eqn (2), α_{L} , α_{CD} , and α_{ϕ} are chemical activities of uncomplexed lipid, free mbCD, and complex at chemical equilibrium, respectively. α_{CD} and α_{ϕ} were approximated as molar concentrations of complex and free mbCD, denoted as $[\text{mbCD}]_{\text{free}}$ and $[\text{complex}]$; reference concentrations of 1 M are used for these aqueous species. The state which lipid molecules adopt within a pure, mechanically relaxed bilayer is taken as the reference state for uncomplexed, bilayer-resident lipid. An aqueous solution of monomeric lipid with a concentration equal to its

critical bilayer concentration ($< 0.46 \text{ nM}$)³⁰ is taken as the reference state for uncomplexed lipid in the solution-phase. Anderson *et al.* fixed $\alpha_{\text{L}} = 1$ in the coexistence region due to their assumption that a 1-component bilayer remains in its reference state irrespective of mbCD-mediated extraction. However, if this process does cause such bilayers to vary from this state, then this would cause variation of α_{L} such that $\alpha_{\text{L}} \neq 1$ in the coexistence region.

To highlight the supposed variation of α_{L} and its contribution to an experimentally accessible parameter, we define an effective equilibrium constant, K_{eff} (*i.e.* a ratio of concentrations raised to some powers, being more reminiscent of the standard form of equilibrium constants in biochemical/biophysical literature); this quantity is obtained by rearranging eqn (2):

$$K_{\text{eff}} = K_{\text{total}} \alpha_{\text{L}} = \frac{[\text{complex}]}{[\text{mbCD}]_{\text{free}}^4} \quad (3)$$

The relevance of K_{eff} is two-fold: (1) it captures any variation of α_{L} throughout phase space and (2) its value at the solubilization boundary is obtained by mapping this boundary. We will now explain how K_{eff} is obtained and suggest how variation of this parameter could affect quantitative interpretations of mbCD–lipid complexation.

Experimentally, the solubilization boundary is located by identifying so-called breakpoints. These are defined as the endpoints of mbCD–lipid titrations (identified *via* isothermal titration calorimetry^{23,31,32} and light scattering^{23,31,33} measurements). mbCD–lipid mixtures falling along the solubilization boundary are identified by total lipid concentrations, denoted by $[\text{lipid}]_{\text{total}}$, and $[\text{mbCD}]_{\text{total}}$ at which vesicles no longer coexist with complexes. These unique values of $[\text{mbCD}]_{\text{total}}$ are denoted as $[\text{mbCD}]_{\text{end}}$, being the total mbCD concentrations at which such breakpoints (or endpoints) occur. The solubilization boundary is mapped by fitting multiple determinations of $[\text{mbCD}]_{\text{end}}$ for various $[\text{lipid}]_{\text{total}}$.

To obtain the fitting equation for the solubilization boundary, Anderson *et al.* noted that essentially all lipid (except for a negligible portion $< 0.46 \text{ nM}$)³⁰ is complexed by mbCD at a breakpoint. Therefore, at the solubilization boundary, $[\text{mbCD}]_{\text{free}}$ in eqn (2) and (3) is given by:

$$\begin{aligned} [\text{mbCD}]_{\text{free}} &= [\text{mbCD}]_{\text{total}} - 4[\text{complex}] \\ &\cong [\text{mbCD}]_{\text{total}} - 4[\text{lipid}]_{\text{total}} \end{aligned} \quad (4)$$

Then, the fitting equation is obtained by substituting eqn (4) into eqn (2) and solving for $[\text{mbCD}]_{\text{end}}$, yielding:

$$\begin{aligned} [\text{mbCD}]_{\text{end}} &= 4[\text{lipid}]_{\text{total}} + \left[\frac{[\text{lipid}]_{\text{total}}}{K_{\text{total}} \alpha_{\text{L}}} \right]^{\frac{1}{4}} \\ &= 4[\text{lipid}]_{\text{total}} + \left(\frac{[\text{lipid}]_{\text{total}}}{K_{\text{eff}}} \right)^{\frac{1}{4}} \end{aligned} \quad (5)$$

For their model, Anderson *et al.* invoked $\alpha_{\text{L}} = 1$ throughout the coexistence region. If this substitution is introduced into eqn (5), the resulting expression becomes identical to the fitting equation used by Anderson *et al.* (eqn (9) in their study)²³ and



then by others.^{31,32} This fitting equation (with $\alpha_L = 1$) was thereafter used to obtain a fitting parameter which was thought to be K_{total} . However, if $\alpha_L = 1$ is omitted and eqn (5) (as written above) is used for fitting, the parameter obtained is K_{eff} (and not K_{total}). If α_L is subject to variation in the vicinity of the solubilization boundary, then this could mean that literature estimates^{23,31,32} of K_{total} are biased in some unknown way.

Materials and methods

Solvents and reagents

HPLC-grade methanol and chloroform were purchased from Fisher Scientific. Ultrapure water (Millipore Milli-Q) was used for all aqueous solutions. mbCD was purchased from Sigma-Aldrich. Chloroform solutions of 1-palmitoyl-2-oleoyl-glycero-3-phosphocholine (POPC), 1,2-dipalmitoyl-*sn*-glycero-3-phosphoethanolamine-*N*-(7-nitro-2-1,3-benzoxadiazol-4-yl) (NBD-PE; head-group-labelled) were obtained from Avanti Polar Lipids. Texas Red 1,2-dihexadecanoyl-*sn*-glycero-3-phosphoethanolamine (Texas Red DHPE) was dissolved in methanol before use. All lipid stock solutions were stored in sealed vials at $-20\text{ }^{\circ}\text{C}$. Vials containing POPC and NBD-PE stock solutions were flushed with research-grade Argon before sealing to prevent oxidation. 2-(*N*-(7-Nitrobenz-2-oxa-1,3-diazol-4-yl)amino)-2-deoxyglucose (NBD-Gluc), sucrose, glucose, HEPES, and sodium chloride were purchased from Fisher Scientific. β -casein from bovine milk was purchased from Sigma-Aldrich. All reagents were used without further purification.

Solution preparation and characterization

Stock solutions of mbCD and sucrose were prepared in ultrapure water or in buffer (20 mM HEPES, 100 mM sodium chloride, pH 7.4). All solutions were filtered through 0.22 μm filters (bottle-top; polystyrene; corning or syringe-top; PVDF; Millipore). We determined osmolalities using an automated osmometer (Advanced Instruments; Model 3300).

Preparation of large unilamellar vesicle (LUV) dispersions

LUV dispersions containing vesicles of defined average diameter were obtained by extrusion as described elsewhere.⁹ The only difference from this prior procedure was that the resuspended lipid film was vortexed to resuspend the lipid before 4 freeze-thaw cycles, performed by rapidly transferring the dispersion between liquid nitrogen and a hot water bath ($50\text{ }^{\circ}\text{C}$). The size distributions of the LUVs were determined *via* dynamic light scattering (Zetasizer Nano ZS; Malvern; ZEN3500). The average hydrodynamic diameters of LUVs extruded through 100 nm pores were 137 nm.

Preparation of giant unilamellar vesicle (GUV) dispersions

GUVs were prepared *via* electroformation using conductive Indium Tin Oxide (ITO) glass slides ($R_s = 4\text{--}8\ \Omega$; Delta Technologies; CG-40IN-S115) as described elsewhere.³⁴ For all preparations, a lipid composition of 99.6% POPC and 0.4% Texas Red-DHPE (mole percentages) in 150 mM sucrose was exposed

to a sinusoidal alternating current of 4 Hz and 4 V_{pp} for 2 hours at room temperature using a function generator (Rigol; DG1000Z). GUV dispersions were annealed at $50\text{ }^{\circ}\text{C}$ overnight and then kept at room temperature with no agitation. GUVs were used within 72 hours after annealing. Lipid concentrations of the GUV dispersions were quantified *via* direct injection onto a single quadrupole mass detector (ACQUITY SQ Detector; Waters; SQD). A calibration curve was prepared from POPC standards of various concentrations (Fig. S2a in the ESI†). For each standard, intensities from peaks corresponding to 760 m/z and 761 m/z were summed, averaged among triplicates, and plotted *versus* POPC concentration. GUV samples for this purpose were prepared by diluting GUV dispersions 1 : 50 (v : v) with methanol (POPC standards were measured in 1 : 50 (v : v) diluted sucrose : methanol matching these samples); quadruplicate measurements were made for each GUV dispersion. Additional assessment of the lipid accessibility and morphologies of GUVs in these dispersions were also made (see Fig. S2b–d and associated discussion in the ESI†).

LUV–mbCD titrations

Multiple titrations were performed in which mbCD was titrated into POPC and *vice versa*. Identical titration series were performed in unbuffered and buffered solutions under 400 rpm stirring. Pure POPC LUVs were used in these titration series. Breakpoints were identified in these mixtures by measuring the intensity of 285 nm light scattered at a 90° angle relative to the incident beam using a fluorometer (“Synchronous” scanning mode; JASCO; FP-8300).³⁵ Each breakpoint came from a single titration (except for one which was performed in duplicate) performed in one of two ways: (1) in separate, equal volume mixtures or (2) in a single cuvette containing titrand into which titrant was incrementally added. When mbCD was titrated with POPC, breakpoints were identified as the intersection of two linear fits of scattering signal *versus* total POPC concentration for distinct regimes within a single titration. When POPC was titrated with mbCD, light scattering signal *versus* total mbCD concentration was fit to a Boltzmann sigmoidal function using Origin. From these fitted titration curves, breakpoints were identified as concentrations of mbCD where the scattering signal approached the baseline (*i.e.* the lower plateau for large concentrations of mbCD). For single-cuvette titrations, the effects of dilution from added titrant were accounted for during breakpoint determination.

Fluorescence quenching measurements

NBD-based quenching experiments were carried out as described elsewhere.³⁶ LUVs composed of 99.7% POPC and 0.3% NBD-PE (mole percentages) were prepared in buffered sucrose solution (150 mM). LUVs composed of pure POPC with encapsulated NBD-Gluc were prepared by suspending the lipid films in the same solution supplemented with NBD-Gluc (100 μM). Quencher solutions were prepared by dissolving sodium dithionite (AKA quencher; 10 mM) in the same buffered sucrose solutions. Due to rapid decomposition of quencher under our conditions,³⁷ these solutions were used within



10 minutes of preparation. The fluorescence signal from NBD-PE and NBD-Gluc in these mixtures was monitored at 541 nm with excitation at 463 nm ("Emission" scanning mode; JASCO; FP-8300). After addition of quencher, LUVs remaining in these mixtures were solubilized by addition of 10% (v/v) Triton X-100 detergent solution (Sigma-Aldrich; X100) to observe complete loss of fluorescence after addition of quencher solution.

Temperature-cycling measurements and evaluation of vesicle re-nucleation

Temperature-dependent 90° light scattering measurements were performed using a temperature-controller/stirrer attachment (JASCO; ETC-815). POPC–mbCD mixtures were continuously stirred at 400 rpm. Pure POPC LUVs and mbCD were first mixed at room temperature. Then, the mixture was heated until all POPC became complexed by mbCD. This mixture was cycled between 10 and 70 °C at least two times while light scattering measurements were made. The temperature was varied in 2 °C increments and held for a specified amount of time (75 seconds, 130 seconds, and 360 seconds in separate measurements). Hysteresis was quantified as the difference between the solubilization and re-nucleation temperatures in these cycles. Transition temperatures were identified where scattering was 50% of the maximal signal observed during each measurement.

Kinetic trapping of mbCD–POPC complexes

Mixtures of POPC, mbCD, and sucrose were prepared in plastic tubes (0.2 mL; Brandtech; 781300). The concentration of sucrose was adjusted to ensure that the summed concentrations of mbCD/sucrose matched the concentration of sucrose encapsulated within GUVs (150 mM). These mixtures were heated to 85 °C for 20 minutes and then cooled to 25 °C for 10 minutes using a thermocycler (Bio-RAD; T100). Subsequently, mechanical agitation of these mixtures was avoided because this accelerated lipid re-nucleation. Care was taken to avoid transfer of condensation back into these solutions as, similarly, dilution accelerated lipid re-nucleation. These solutions were used for several hours after kinetic trapping.

Bulk GUV–mbCD incubation and evaluation

For incubating free-floating GUVs with mbCD, equal volumes of GUV dispersions and mbCD/sucrose solutions (in which the sum of the concentrations of these solutes were 150 mM, matching the encapsulated sucrose concentration inside the GUVs) were mixed in 0.2 mL plastic tubes. Upon addition, the GUV–mbCD mixtures were gently pipetted to ensure mixing; then, the mixtures were kept with no agitation. At the end of incubation, 10 µL of each mixture was added to 90 µL of osmotically balanced glucose solution. GUVs were concentrated in the bottom of the glucose medium whereas all solutes were diluted ten-fold throughout the whole volume. The bottommost 10 µL containing GUVs was added into a closed imaging chamber for observation. The GUVs rapidly settled onto the lower coverslip and were observed *via* confocal microscopy (Olympus; IX83) with a 60× objective (UPlanSApo; Olympus).

During observation, a 561 nm laser was used for excitation and emission of 618 nm light was collected to generate images. Closed imaging chambers were made by sandwiching small-volume samples between two 25 × 25 mm glass coverslips (Fisherbrand; 12542C) separated by a thin layer of grease (Dow-Corning). These coverslips were passivated with 5 µL of 1 mg mL⁻¹ β-casein dissolved in ultrapure water. Passivation was accomplished by spreading this solution on the coverslip surface with a plastic pipette, evaporating it to dryness, and rinsing the excess protein with ultrapure water. Passivated coverslips were air-dried before use.

During observation, the frequencies of GUVs containing at least one instance of various bending protrusions (either buds, pearls, or tubes; see Results section) and their direction (inward or outward) of these structures were tabulated. Additionally, the frequencies of GUVs containing at least one instance of a high-curvature protrusion (of any type) directed towards its interior and/or exterior and those containing no protrusions were tabulated. At least one image showing a representative cross-section of each GUV contributing to these statistics were collected; in some cases, short videos were obtained to properly show the bending protrusions which fluctuated in-and-out of the focal plane. Some dispersions contained a high density of vine-like tendrils with lengths spanning several hundreds of micrometers, resembling intermediate structures of electroformation³⁸ which form during electroosmotic deformation of lipid films.³⁹ These structures were usually entangled in networks composed of several other tendrils/GUVs. Because these structures were independent of exposure to mbCD, the following criteria were implemented to minimize the contribution of these structures to morphological statistics: protrusions were only tabulated if they (1) could be associated with a single GUV and (2) had a length less than the diameter of the associated GUV.

Local delivery of mbCD to single GUVs

Single GUVs were exposed to mbCD by injecting mbCD solution from a micropipette held closely to the vesicles. Micropipettes were fabricated as described elsewhere³⁴ using 1.0 mm OD, 0.78 mm ID, 100 mm L glass capillaries. Micropipettes were filled with mbCD solutions and then affixed into a stainless-steel dosing unit (Luigs and Neumann) held by a micromanipulator (Luigs and Neumann; SM 7). Local delivery of mbCD solutions to single GUVs was performed as described elsewhere;⁴⁰ a water reservoir mounted onto a stepper motor (Thor Labs; LTS150) was used to regulate the direction and speed of solution-flow through the tip of the micropipette. Experiments were performed in open-air imaging chambers (described elsewhere)⁴¹ which were filled with unbuffered, osmotically balanced glucose solution (approximately 700 µL). Then, a small volume of GUV dispersion (between 0.2–0.6 µL, depending on GUV density) was pipetted into the chamber to distribute the vesicles throughout the chamber before they settled on the lower coverslip. Because the outward solution-flow from micropipettes pushed GUVs away, the stage was manually adjusted to keep the GUV in focus and near the



micropipette tip. Videos were captured on an EM-CCD camera (Hamamatsu; C9000-13).

Results

Characterizing osmotic effects on solubilization equilibria between mbCD and phospholipid

In vesicles, both membrane bending and lateral stresses are coupled to osmotic differentials across the bilayer.⁴² Previous experiments characterizing vesicle solubilization by mbCD were carried out under conditions of large, variable osmotic differentials (*i.e.* hypertonicity). This is because mbCD was present in the external solutions with no secondary osmolyte encapsulated inside vesicles to offset the osmotic pressure of mbCD. Because this balance was neglected, vesicles exposed to mbCD in earlier studies were subjected to extensive osmotic stress (from unbalanced mbCD in the external solution). This could have influenced the solubilization behavior of mbCD. To evaluate the consequences of this coupling, we introduced sucrose as a secondary, balancing osmolyte to perform measurements under conditions of minimal osmotic stress. By simultaneously adjusting mbCD/sucrose concentrations in the external solution to maintain a total concentration equivalent to the encapsulated sucrose inside the vesicles (150 mM sucrose), we minimized osmotic differentials in our experiments (by maintaining approximate isotonicity; see Fig. S1a–f in the ESI†).

To evaluate solubilization behavior under minimal osmotic differentials, we carried out 90° light scattering titrations of lipid and mbCD at room-temperature (RT; *i.e.* 23 ± 2 °C). The goal of these titrations was the determination of breakpoints (see background section),^{23,31} each breakpoint was identified by bulk concentrations of mbCD and POPC denoted by [mbCD]_{end} and [POPC]_{total}, respectively. We determined breakpoints by titrating POPC with mbCD (see Fig. 1a) and *vice versa* (see Fig. 1b), constituting two trajectories by which the solubilization boundary could be approached at fixed RT. Sets of [mbCD]_{end} and [POPC]_{total} characterizing these breakpoints resulted in a two-dimensional phase diagram. The solubilization boundary and associated estimate of K_{eff} at RT under isotonicity were obtained by fitting the experimental boundary to eqn (5) (see Fig. 1c).

Six breakpoints were obtained by titrating mbCD with POPC and two were determined by titrating POPC with mbCD. The fact that breakpoints from both titration schemes fell along a single boundary implies that chemical equilibrium was suitably approached. We found that chemical equilibrium was approached within 20 minutes but we typically incubated these mixtures for 1 hour or more. Our fit of the solubilization boundary at RT under isotonic conditions provided an estimate of $K_{\text{eff}} = 214 \pm 5 \text{ M}^{-3}$ (fitted value ± uncertainty using eqn (5)). The area below the solid curve in Fig. 1c is the coexistence regime, where vesicles and mbCD complexes coexist (see background section).

Table 1 summarizes all estimates of K_{eff} currently available in the literature and the osmotic conditions (*i.e.* tonicity) under

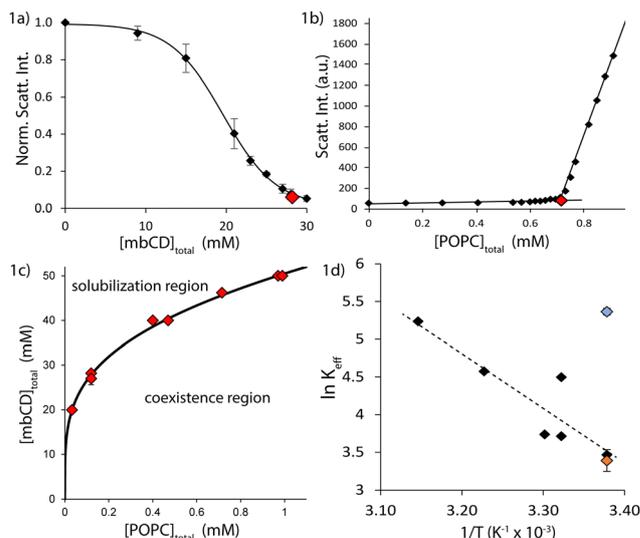


Fig. 1 The mbCD–POPC solubilization boundary is affected by osmotic differentials. (a) Titrating a POPC dispersion with mbCD at a fixed concentration of [POPC]_{total} = 0.12 mM. POPC LUVs were 90 nm in diameter. Vertical axis = intensity of 285 nm light scattered at an angle of 90° normalized by the signal of the 0 mM mbCD mixture. Red diamond = location of breakpoint. Error bars = SEMs from triplicate titrations. The line is a fitting of this data. (b) Titrating a mbCD solution in a single cuvette. 1.8 mL of mbCD solution initially containing [mbCD]_{total} = 49 mM was titrated with a dispersion of 137 nm POPC LUVs of [POPC]_{total} = 0.13 mM. Effect of dilution upon the initial [mbCD]_{total} was accounted for to provide the plot. Vertical axis = absolute intensity of scattered 285 nm light. Red diamond = location of breakpoint. Dotted lines = linear fits before and after the breakpoint. (c) mbCD–POPC phase diagram for isotonic conditions at 23 °C. Red diamond = location of breakpoint. Error bar on one breakpoint = SEM from triplicate titrations performed by a single experimenter. Solid black line = fitting of the breakpoints to eqn (5) with $\nu = 4$; $K_{\text{eff}} = 214 \text{ M}^{-3}$ was provided from this fit. (d) K_{eff} at different temperatures and osmotic conditions. Black diamonds = literature estimates under hypertonic conditions (see text). Blue diamond = our estimate at 23 °C under isotonic conditions. Orange diamond = our estimate of K_{eff} at 23 °C under hypertonic conditions. Dotted line = fitting of literature data. Error bars = uncertainty from fitting. 150 mM sucrose solutions were used for background correction in the above measurements.

Table 1 K_{eff} of mbCD–POPC complexation at different temperatures

$K_{\text{eff}} (\text{M}^{-3})$	$\ln[K_{\text{eff}}]$	$T (^\circ\text{C})$	$1/T (\text{K}^{-1})$	Source	Tonicity
90	4.50	28	0.00332	Anderson <i>et al.</i>	Hypertonic
42	3.74	30	0.00330	Bozelli <i>et al.</i>	
97	4.57	37	0.00323	Bozelli <i>et al.</i>	
188	5.24	45	0.00314	Bozelli <i>et al.</i>	
41	3.71	28	0.00332	Markones <i>et al.</i>	
32	3.47	23	0.00338	Huang <i>et al.</i>	
30	3.39	23	0.00338	This study	
214	5.37	23	0.00338	This study	Isotonic

which they were determined;^{23,31–33} Fig. 1d plots these estimates. Our estimate of K_{eff} at RT under isotonic conditions is significantly larger than the value predicted from literature data (in which osmotic balance of mbCD was neglected). We hypothesized that differences between this estimate of K_{eff} and earlier values could be due to osmotic effects.



To test the above hypothesis, we performed duplicate titrations without adjusting the external sucrose concentration to offset the osmotic pressure applied by mbCD. Restated, a fixed 150 mM sucrose concentration was maintained inside/outside the LUVs while the mbCD concentration was adjusted; thereby, a hypertonic differential was applied to the LUVs. This scheme matched the osmotic conditions used in earlier studies.^{23,31–33} From these titrations, we obtained $K_{\text{eff}} = 30 \pm 1 \text{ M}^{-3}$ (average value \pm standard error of the mean [SEM]) at RT in good agreement with literature data³³ at the same temperature, confirming our hypothesis. This finding also suggests that the interaction between sucrose and the headgroups of phospholipids^{43,44} (which is thought to alter mechanical properties of bilayers)^{45,46} does not seem to influence mbCD–lipid equilibrium.

Assessing lipid flipping and vesicle leakage in response to lipid extraction

Having identified the solubilization boundary, we next asked if transmembrane leaflet area asymmetry was maintained within the coexistence regime in vesicles exposed to mbCD on our experimental timescales (1–2 hours). While mbCD is thought to interact with lipids in the outer leaflets of vesicles only, we asked if loss of lipid from outer leaflets results in an extensive, spontaneous flow of lipid from the inner leaflets to compensate for depletion of the outer leaflet (through directional/biased lipid flipping, driven by mechanical stress).^{47,48} We asked if this process occurs detectably and on a similar timescale as lipid extraction.

Whereas mbCD-mediated extraction plateaus within minutes,^{49,50} flip-flop is generally regarded as a much slower process.^{51,52} If that is the case here, mbCD and inclusion complexes would rapidly achieve a preequilibrium⁵³/metastable state^{48,54} with lipid in the outer leaflets before appreciable lipid flip-flop occurred (thereby allowing accumulation of area asymmetry). However, recent observation of accelerated flip-flop in experimental^{55,56} and simulated⁵⁴ bilayers containing area asymmetry suggest that biased flip-flop could occur on a similar timescale as lipid extraction. In these cases, it is likely that rapid flipping occurred *via* bilayer defects,⁵⁷ including pre-pores⁵⁸ or micelle-like defects.⁵⁴ Therefore, we monitored lipid flipping as well as vesicle leakage (to monitor pre-pore formation) in mbCD–lipid mixtures.

To do so, we probed the accessibility of NBD-labelled compounds to the exterior solution *via* irreversible quenching of NBD fluorescence by the membrane-impermeant salt, sodium dithionite (quencher).³⁶ NBD-labelled molecules on the interior of vesicles (*i.e.* inner leaflets or encapsulated solution) are inaccessible to the quencher whereas molecules on the exterior of vesicles (*i.e.* outer leaflets or exterior solution) are accessible. We added sodium dithionite to mbCD–vesicle mixtures, reaching a final concentration of 5 mM (matching optimal conditions recently reported for this experiment).⁵⁹ We monitored changes in the accessibility of a lipid probe (*i.e.* NBD-PE) and an encapsulated, aqueous probe NBD-Gluc (*i.e.* an aqueous fluorescent probe) after exposing our LUVs to

mbCD for 1–2 hours. After these incubations, we performed quenching measurements.

An example set of NBD-PE quenching measurements is shown in Fig. 2a. The fractional reduction in the dilution-corrected fluorescence (plateaus occurring after the time point marked by “+ quencher” in Fig. 2a) allowed us to monitor the accessibility of the labelled compounds to the exterior solution (*i.e.* NBD-PE in the outer leaflets and in-complex with mbCD; NBD-Gluc in the external solution). The appearance of stable plateaus in NBD-PE signal after addition of quencher implies that scrambling (*i.e.* flip-flop which is uncoupled to mechanical stress and, instead, equilibrates compositional gradients) did not occur detectably during quenching reactions.⁶⁰ Only after addition of detergent (at the time-point marked by “+ Triton-X” in Fig. 2a) was fluorescence completely abrogated. We assessed the accessible fractions of both NBD-PE and NBD-Gluc in separate mbCD–LUV mixtures of fixed $[\text{POPC}]_{\text{total}}$ and increasing $[\text{mbCD}]_{\text{total}}$ (see Fig. 2b and c).

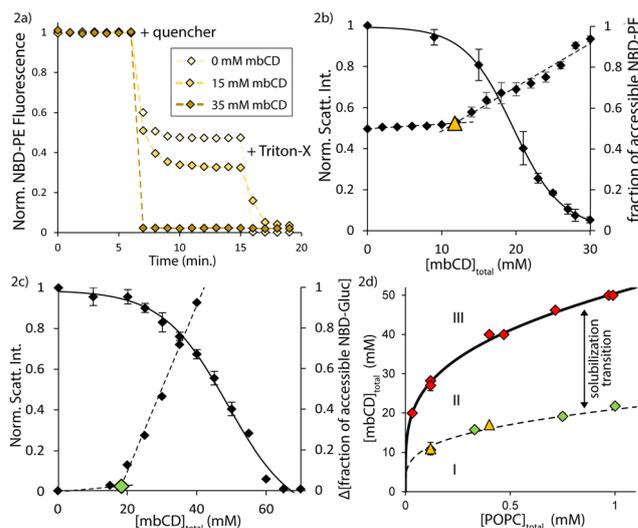


Fig. 2 Vesicle rupture/collapse occurs over a mbCD concentration range that is enclosed by two boundaries. (a) Primary NBD-PE quenching measurements for $[\text{POPC}]_{\text{total}} = 0.12 \text{ mM}$. Vertical axis = dilution-corrected, normalized fluorescence from NBD-PE. (b) Overlay of NBD-PE quenching measurements onto light scattering titration data with fixed $[\text{POPC}]_{\text{total}} = 0.12 \text{ mM}$. Left vertical axis = normalized light scattering signal. Right vertical axis = fraction of quenched NBD-PE. Dotted lines = linear fits from both quenching regimes (see text). Triangle = discontinuity in NBD-PE quenching. Error bars = SEMs from triplicates. (c) Overlay of NBD-Gluc quenching measurements onto light scattering titration data with fixed $[\text{POPC}]_{\text{total}} = 0.75 \text{ mM}$. Left vertical axis = normalized light scattering signal. Right vertical axis = change in fraction of quenched NBD-Gluc compared to 0 mM mbCD mixture. Dotted lines = linear fits from both quenching regimes. Diamond = discontinuity in NBD-PE quenching. (d) Summary of results from NBD-PE and NBD-Gluc quenching measurements on the mbCD–POPC phase diagram under isotonic conditions at RT. Triangles = discontinuities from NBD-PE quenching. Green diamonds = discontinuities from NBD-Gluc quenching. Red diamonds = breakpoints from light scattering titrations. Dotted line = onset boundary (see text). Solid line = isotonic solubilization boundary at RT. Error bars = SEMs from triplicate (triangles and red diamonds) or duplicate (green diamonds). Discontinuities from NBD-PE and NBD-Gluc quenching for $[\text{POPC}]_{\text{total}} = 0.12 \text{ mM}$ are overlapping.



According to Fig. 2b, half of the total NBD-PE was accessible to quencher before exposure to mbCD. This showed that our vesicle preparations were unilamellar.⁶¹ As $[\text{mbCD}]_{\text{total}}$ was increased initially, Fig. 2b and c show only slight increases in the fraction of accessible NBD-PE and NBD-Gluc (we refer to this as the shallow regime). Then, as $[\text{mbCD}]_{\text{total}}$ was increased further, the accessible fractions of both probes increased steeply until nearly all the NBD-compounds became accessible (we refer to this as the steep regime). We identified transitions from shallow to steep regimes by determining the intersection of linear fits to the data in these regions (AKA discontinuities).

From multiple quenching series for NBD-PE and NBD-Gluc for various $[\text{POPC}]_{\text{total}}$, we found that discontinuities between the shallow and steep regimes occurred at significantly lower mbCD concentrations than associated breakpoints (falling along the solubilization boundary). Specifically, we found that discontinuities in NBD-PE and NBD-Gluc accessibilities occurred at $41 \pm 2\%$ and $41 \pm 1\%$ of $[\text{mbCD}]_{\text{end}}$ (average \pm SEM). Fig. 2d shows that the discontinuities identified in NBD-PE and NBD-Gluc quenching series fall along a common boundary within the coexistence region. This means that, for a given $[\text{POPC}]_{\text{total}}$, steep increases in NBD-Gluc and NBD-PE accessibility coincide at a single threshold concentration of mbCD. Since these discontinuities occurred with rapid decreases in light scattering intensity (which, to a first approximation, is proportional to vesicle concentration),³⁵ this suggested that vesicle solubilization accounted for the pronounced changes in lipid accessibility in the steep regime.

We denote the concentration of mbCD associated with a discontinuity in NBD-PE/NBD-Gluc quenching as $[\text{mbCD}]_{\text{onset}}$; $[\text{mbCD}]_{\text{onset}}$ and $[\text{mbCD}]_{\text{end}}$ are related by $[\text{mbCD}]_{\text{onset}} = 0.4 \times [\text{mbCD}]_{\text{end}}$. Each discontinuity is classified by paired $[\text{mbCD}]_{\text{onset}}$ and $[\text{POPC}]_{\text{total}}$. Because these discontinuities identify the onset of vesicle collapse/solubilization as lipid is titrated with mbCD, we therefore refer to the line formed by the unity of all such discontinuities as the onset boundary (dotted line in Fig. 2d). This boundary divides the coexistence region. The onset and solubilization boundaries trace-out a third region of the mbCD–lipid phase diagram (labelled as region II in Fig. 2d; AKA the solubilization transition).

Generating area asymmetry in GUVs with increasing concentrations of mbCD

The shallow regime in Fig. 2b suggests a small but detectable increase in lipid accessibility and vesicle leakage (though not exceeding a 3% change in either case) as the onset boundary is approached. This suggests that defect-mediated, biased flip-flop within intact vesicles occurred on a similar timescale as lipid extraction. We hypothesized that this could relax the area asymmetries of LUVs in the previous measurements. To assess this hypothesis, we turned to GUVs whose large diameters (10–100 μm) allow them to be observed *via* optical microscopy in a native, fluid environment (in contrast to electron microscopy which involves staining, fixation, and/or freezing to observe the LUVs). If mbCD-mediated lipid extraction generates area asymmetry in vesicles, then this would induce bending

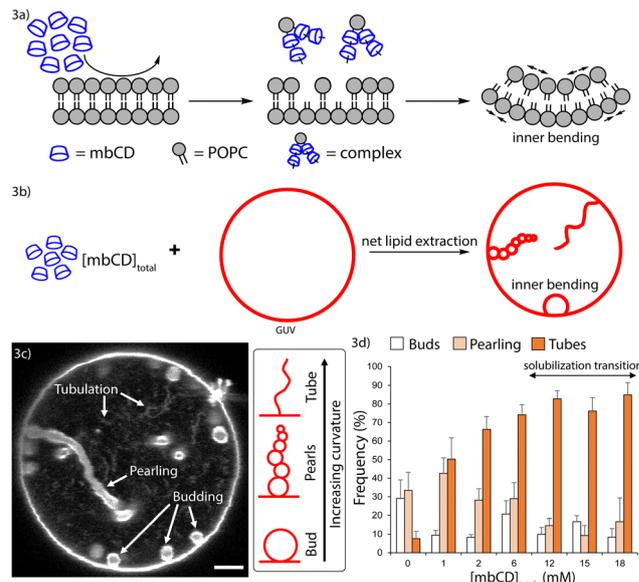


Fig. 3 Asymmetric lipid extraction generated by mbCD induces negative curvature in GUVs in a concentration-dependent manner (a) mbCD asymmetrically extracts lipids from the outer leaflet of a bilayer and generates membrane bending. The bilayer bends away from the leaflet from which lipids are extracted. Arrows show whether lipids are stretched/compressed relative to their optimal molecular area. (b) Work-flow for mbCD–GUV incubation and evaluation of bending. (c) Cross-section of a GUV from a 6 mM mbCD mixture observed *via* confocal microscopy. Examples of inner tubulation, pearling/unduloid, and budding are shown. Scale bar = 5 μm . (d) Inner bending morphologies in GUVs incubated with different $[\text{mbCD}]_{\text{total}}$ for 30 minutes prior to observation. Vertical axis = average frequencies of GUVs containing at least one instance of each morphology. GUVs used in this dataset were obtained from 3 separate dispersions. Error bars = SEMs from six replicates. Between 15–40 single GUVs were observed from each mixture.

(a schematic of this phenomenon at the molecular-scale is shown in Fig. 3a).⁶⁷ Therefore, to address whether biased lipid flip-flop precludes accumulation of area asymmetry in vesicles, we monitored mbCD-mediated bending transitions in GUVs.

Fig. 3b shows the GUV shape changes induced by asymmetric lipid extraction (emerging from the molecular-scale phenomenon shown in Fig. 3a). If area asymmetry was rapidly dissipated by biased flip-flop, then only spherical GUVs would persist (because the bilayer has no tendency to bend). If area asymmetry was maintained for longer timescales, then GUV shapes like that shown in Fig. 3b would persist. By this logic, we assessed generation of area asymmetry in GUVs by identifying high curvature bending protrusions directed towards their interiors after exposure to mbCD for 30 minutes. The kinds of high-curvature protrusions that we observed (such as those shown in Fig. 3c) have been ubiquitously associated with area asymmetry generation^{29,34,62} and reflect that negative curvature was generated in these GUVs. We increased $[\text{mbCD}]_{\text{total}}$ in this series while holding $[\text{POPC}]_{\text{total}}$ constant (contributed from the GUVs added to these mixtures) (at $22 \pm 2 \mu\text{M}$ [mean \pm SEM] from eleven separate GUV dispersions; see Table S1 in the ESI†).

Fig. 3d shows statistics generated from observation of multiple GUVs incubated with increasing $[\text{mbCD}]_{\text{total}}$. GUVs exposed



to increasing $[\text{mbCD}]_{\text{total}}$ up to 6 mM showed an increase in the frequency of high-curvature tubes (with diameters below the optical resolution); after this concentration, the frequency of these tubes plateaued. The frequencies of lower-curvature morphologies (buds and pearls) underwent a continual decrease for $[\text{mbCD}]_{\text{total}}$ greater than 1 mM. These observations imply an increase in the negative curvature and area asymmetry of GUVs from 0–6 mM mbCD followed by an apparent plateau. These trends confirm that area asymmetry was generated within the intact GUVs exposed to mbCD.

Earlier definitions of $[\text{mbCD}]_{\text{end}}$ and $[\text{mbCD}]_{\text{onset}}$ can be used to contextualize this behavior in the mbCD–POPC phase diagram of Fig. 2d. Since GUV–mbCD mixtures contain $[\text{POPC}]_{\text{total}} = 22 \mu\text{M}$, we can use eqn (5) with $K_{\text{eff}} = 214 \text{ M}^{-3}$ to obtain $[\text{mbCD}]_{\text{end}} = 18 \text{ mM}$ and $[\text{mbCD}]_{\text{onset}} = 0.4 \times [\text{mbCD}]_{\text{end}} = 7 \text{ mM}$. The similarity between $[\text{mbCD}]_{\text{onset}} = 7 \text{ mM}$ for the mbCD–GUV mixtures and the start of the plateau in Fig. 3d (occurring in the vicinity of 6 mM mbCD) implies that the plateau falls within the onset and solubilization boundaries (*i.e.* region II of Fig. 2d). Increasing $[\text{mbCD}]_{\text{total}}$ prior to the onset boundary (*i.e.* within region I of Fig. 2d) generates area asymmetry in a concentration-dependent manner. This confirms that biased lipid flip-flop (which would have abrogated area asymmetry generation and shape changes in this region) must be slower than lipid extraction by mbCD.

Supercooling of mbCD–lipid complexes to control lipid delivery to/from GUVs

In the experiments described above, we showed that increasing $[\text{mbCD}]_{\text{total}}$ generated a concentration-dependent increase in the negative area asymmetry and negative curvature of GUVs. We next asked if we could generate positive curvature by driving excess lipid into the outer leaflets of vesicles (*i.e.* positive area asymmetry) *via* mbCD-complexed lipids.

To test if excess lipid could be delivered to the outer leaflets of vesicles, we adapted previously reported methods for delivery of cholesterol²⁰ and fatty acids⁶³ between membranes and external solutions using cyclodextrins. These methods utilized heating to facilitate complexation between the cyclodextrins and corresponding guest molecules followed by cooling to yield solutions containing the corresponding complexes. These solutions were then used to drive the guest molecules into membranes. Here, we asked if kinetic trapping of mbCD with supersaturated concentrations of lipid (“loaded” mbCD solutions) could provide a driving force through which vesicles would accept excess lipid into their outer leaflets.

It was previously shown that K_{eff} increases when the temperature of a mbCD–POPC mixture is elevated.³¹ We exploited this behavior to solubilize vesicles in mbCD–POPC mixtures *via* heating to 70 °C. Then, we rapidly cooled these complex solutions back to 25 °C (*i.e.* with negligible times at each intermediate temperature) under continuous stirring. The process of re-nucleation was monitored *via* 90° light scattering, resulting in an increase in the amount of scattered light over time. We classified each mixture based on re-nucleation behaviors upon cooling (see Fig. 4a): (i) no re-nucleation

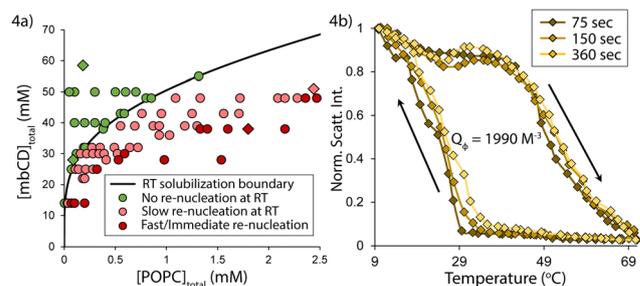


Fig. 4 mbCD can be kinetically trapped with supersaturating concentrations of POPC by supercooling. (a) Re-nucleation behavior of mbCD–lipid solutions cooled to 25 °C mapped onto the phase diagram. Black line = isotonic solubilization boundary at RT from Fig. 1c. Each point summarizes results from a single mixture after cooling from 70 °C (see text about the three groups used to classify these solutions). Diamonds show states that were also surveyed in dilution experiments as shown in Fig. S3a in the ESI.† (b) Three thermal cycles measured for a mbCD–POPC mixture of $Q_\phi = 1990 \text{ M}^{-3}$ with $[\text{mbCD}]_{\text{total}} = 38 \text{ mM}$. The amount of time the mixtures were held at each temperature is specified for each dataset. Vertical axis = normalized light scattering intensity (at 285 nm) relative to maximal scattering intensity at 10 °C from that measurement.

(green datapoints), (ii) slow re-nucleation (*i.e.* detectable increase in light scattering was delayed and did not plateau within 5 minutes) (pink datapoints), or (iii) immediate re-nucleation (*i.e.* achieving a plateau within 5 minutes after cooling) (red datapoints). Fig. 4a shows the results of these tests mapped onto the mbCD–POPC phase diagram. We interpreted the re-nucleation behavior of these cooled solutions through the lens of mass-action.

A lipid–mbCD mixture in the coexistence region is a biphasic mixture consisting of a mesophase of all free-floating vesicles and a solution-phase (which we refer to as a “complex solution”). Contained in the complex solution are inclusion complexes, free mbCD, and a negligible concentration of lipid at its critical bilayer concentration (CBC; $< 0.46 \text{ nM}$).³⁰ The complex solution is free to exchange lipid with the vesicles in which it is held in contact; the tendency for such a complex solution to donate lipid to such vesicles is defined as the following (denoted as Q_ϕ ; AKA the mass-action quotient):

$$Q_\phi = \frac{[\text{complex}]}{\alpha_L [\text{mbCD}]_{\text{free}}^4} = \frac{[\text{POPC}]_{\text{total}}}{([\text{mbCD}]_{\text{total}} - 4[\text{POPC}]_{\text{total}})^4} \quad (6)$$

Eqn (6) is based on the definition of the equilibrium constant for mbCD–lipid complexation, denoted by K_{total} , shown in eqn (2).⁶⁴ The second expression relies on the assumption that the majority of lipid contained in a complex solution is complexed by mbCD (valid in all our experiments because the CBC of POPC is much smaller than various $[\text{POPC}]_{\text{total}}$). A complex solution which tends to donate lipid into a pre-formed vesicle mesophase also possesses a tendency to generate a new mesophase in the absence of a pre-existing one (AKA nucleation). This agrees with our hypothesis that loaded mbCD should spontaneously shed lipid through any pathways which allow Q_ϕ to approach the value of 214 M^{-3} (*i.e.* the value of K_{eff} corresponding to the RT, isotonic solubilization boundary).



The process of lipid re-nucleation is relevant for data in Fig. 4a and b.

For $Q_\phi < 214 \text{ M}^{-3}$ we observed no vesicle re-nucleation after cooling (*i.e.* all mixtures in Fig. 4a falling above the solubilization boundary correspond to a green datapoint). For values of $Q_\phi < 214 \text{ M}^{-3}$ at 25°C , lipid re-nucleation occurred after cooling (*i.e.* all mixtures in Fig. 4a falling below the solubilization boundary).⁶⁵ We found that delayed re-nucleation was observed increasingly in cooled mixtures falling closer to the solubilization boundary. A separate boundary, at approximately $Q_\phi \cong 1000 \text{ M}^{-3}$, divided slow/delayed and fast/immediate re-nucleation (*i.e.* regions formed by all pink and red datapoints, respectively, in Fig. 4a). Without stirring or any other agitation, loaded mbCD solutions with Q_ϕ values between 214 M^{-3} and roughly 1000 M^{-3} were metastable for >20 hours at RT with no detectable re-nucleation (*i.e.* pink datapoints in Fig. 4a). We hypothesized that complex solutions that mapped to this region of mbCD–lipid phase space were kinetically trapped as a result of supercooling.

The notion of supercooling implies hysteresis and we thus sought further evidence for this phenomenon. To do so, we cycled three, identical mixtures between two temperatures above and below RT; these mixtures were characterized by $Q_\phi = 1990 \text{ M}^{-3}$ and $[\text{mbCD}]_{\text{total}} = 38 \text{ mM}$ after lipid complexation (see eqn (6)). Each mixture was held at a temperature for a specified waiting time before proceeding to the next temperature. 90° light scattering readings were taken at each temperature after these waiting times. We varied the waiting times used for each mixture.

Fig. 4b shows three hysteresis loops resulting from the above measurements. In each hysteresis loop, we identified the occurrence of solubilization/re-nucleation as states that gave half maximal scattering signal (identified by linear interpolation); the temperatures associated with these locations were taken as transition temperatures. The extent of hysteresis was quantified as the difference between transition temperatures ($\Delta T = T_{\text{solubilize}} - T_{\text{nucleate}}$). There was minimal change with respect to the surveyed waiting times. The large degree of undercooling required for re-nucleation in these experiments confirms that loaded mbCD solutions with Q_ϕ values of 214 M^{-3} and roughly 1000 M^{-3} were kinetically trapped *via* supercooling.

We also characterized lipid release behavior of loaded mbCD solutions in response to dilution (see Fig. S3a and b and associated text in the ESI[†]). Observations from these experiments (1) suggest that re-nucleation of lipid from loaded mbCD is path-independent and (2) demonstrated that dilution of a complex solution causes an instantaneous increase in Q_ϕ (which is related to the dilution-factor). Both points are relevant for using loaded mbCD solutions to insert lipid into GUVs (and interpret other behaviors in these experiments).

Tuning the area asymmetries of GUVs from bulk mixing with loaded mbCD

We next evaluated whether loaded mbCD could control net lipid delivery between the external solution and intact vesicles.

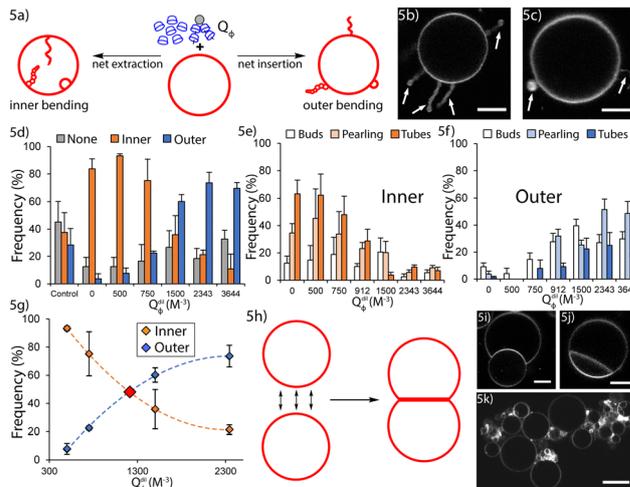


Fig. 5 Adjusting POPC–mbCD mass-action controls direction of net lipid exchange between GUVs and the external solution. (a) Emergence of high-curvature bending morphologies relates to net lipid exchange between GUVs and loaded mbCD (controlled by the value of Q_ϕ^{dil}). (b) Example image of a GUV with outer pearling morphologies (arrows). Scale bar = $10 \mu\text{m}$. (c) Example image of a GUV with an outer bud (left arrow) and an outer tube (right arrow). Scale bar = $10 \mu\text{m}$. (d) Statistics obtained from GUVs incubated with loaded mbCD; incubation time = 1.5 minutes before observation (see text). Vertical axis = frequencies of GUVs containing at least one instance of inner/outer bending protrusions of any kind. (e) Frequencies of single GUVs containing at least one instance of various inner morphologies observed in GUVs incubated with loaded mbCD. (f) Frequencies of single GUVs containing at least one instance of various outer morphologies observed in GUVs incubated with loaded mbCD. (g) Frequencies of inner/outer bending morphologies replotted from 5d over the range Q_ϕ^{dil} : [500 M^{-3} , 2343 M^{-3}]. Dotted lines = 2nd-order polynomial fits of the corresponding dataset. Red diamond = intersection of both fits at $Q_\phi^{\text{cross}} = 1200 \text{ M}^{-3}$. (h) Proposed mechanism for formation of composite GUV structures. These structures formed alongside the GUV shapes shown in (a). (i) and (j) Example images of composite GUV structures formed between two GUVs. Scale bars = $10 \mu\text{m}$. (k) Example image of a GUV aggregate (see text). Scale bar = $20 \mu\text{m}$. Error bars in (d)–(f) = SEMs; between 15–40 individual GUVs were observed in each replicate and each datapoint is averaged from between 2–9 replicates from separate GUV preparations.

To do so, we once again utilized GUVs to monitor generation of membrane curvature. This was accomplished by mixing loaded mbCD solutions and GUV dispersions in a 1 : 1 (v : v) ratio and incubating for 1.5 minutes. Fig. 5a is a schematic showing inward and outward bending transitions of GUVs (example images of GUVs with outer bending protrusions are shown in Fig. 5b and c). Identification of these structures provided information about the direction of net curvature-generation which we related to area asymmetry generation: negative curvature corresponded to lipid extraction from the GUVs (resulting in negative area asymmetry) whereas positive curvature corresponded to lipid insertion into the GUVs (resulting in positive area asymmetry).

We introduced the parameter Q_ϕ^{dil} for these experiments; this quantity describes the instantaneous mass-action quotient of the external solution after mixing GUVs and loaded mbCD; these values were calculated using eqn (6) as described in the



ESI† (see Fig. S3a and b and associated discussion). Briefly, values of Q_{ϕ}^{dil} for these experiments were calculated by multiplying the initial values of Q_{ϕ} for the undiluted loaded mbCD solutions (*i.e.* prior to mixing) by a factor of $2^3 = 8$, corresponding to the two-fold dilution during mixing of loaded mbCD solutions with GUV dispersions in a 1:1 (v:v) ratio. We prepared a series of loaded mbCD solutions spanning a range of Q_{ϕ} : $[0 \text{ M}^{-3}, 456 \text{ M}^{-3}]$ with $[\text{mbCD}]_{\text{total}} = 28 \text{ mM}$. Thus, after accounting for dilution, the range spanned in the mbCD–GUV mixtures was Q_{ϕ}^{dil} : $[0 \text{ M}^{-3}, 3644 \text{ M}^{-3}]$ with $[\text{mbCD}]_{\text{total}} = 14 \text{ mM}$.

Because the concentration of uncomplexed lipid was negligible (approximately 0.46 nM)³⁰ compared to the millimolar concentrations of lipid complexed by mbCD, lipid exchange between GUVs and the complexes was likely to be the most relevant contribution to GUV shape changes. After incubating the GUVs with loaded mbCD, we generated the statistics contained in Fig. 5d–f by monitoring the frequencies of GUVs containing at least one instance of various high-curvature protrusions. GUVs containing no bending protrusions were also tabulated (these contributed to the “None” classification). From Fig. 5d, the frequency of GUVs displaying at least one inward protrusion (of any kind) in these mixtures decreased with increasing Q_{ϕ}^{dil} . Simultaneously, the frequency of GUVs containing at least one outward protrusion (of any kind) increased with increasing Q_{ϕ}^{dil} .

Among inner bending morphologies, Fig. 5e shows that GUVs containing high-curvature tubules were the dominant inner morphology for Q_{ϕ}^{dil} : $[0 \text{ M}^{-3}, 912 \text{ M}^{-3}]$, coinciding with a decrease in the frequencies of GUVs containing inner morphologies (of any kind) along Q_{ϕ}^{dil} : $[0 \text{ M}^{-3}, 1500 \text{ M}^{-3}]$. This suggests a decrease in the magnitude of negative area asymmetry/curvature along these ranges. Analogously, for outer bending morphologies, Fig. 5f shows that GUVs containing low-curvature morphologies (buds and pearls) were the dominant outer structures for Q_{ϕ}^{dil} : $[912 \text{ M}^{-3}, 3644 \text{ M}^{-3}]$, coinciding with an increase in the frequencies of GUVs containing outer morphologies (of any kind) along Q_{ϕ}^{dil} : $[750 \text{ M}^{-3}, 3644 \text{ M}^{-3}]$. This suggests an increase in the magnitude of positive area asymmetry/curvature along these ranges.

The findings above provide qualitative evidence that loaded mbCD of suitable Q_{ϕ} drives lipid insertion into intact GUVs. We asked whether these findings agreed with the formalism proposed by Anderson *et al.*²³—*i.e.*, $\alpha_L = 1$, implying that K_{eff} at the RT, isotonic solubilization boundary should dictate the direction of net lipid exchange between mbCD and GUVs with respect to Q_{ϕ}^{dil} . The above trends reveal that there is a value of Q_{ϕ}^{dil} (which we refer to as Q_{ϕ}^{cross}) at which neither inner nor outer bending protrusions are favored. We identified Q_{ϕ}^{cross} as the location at which empirically chosen, quadratic fits to the inner/outer bending frequencies intersected (see Fig. 5g). From these fits, we found that $Q_{\phi}^{\text{cross}} = 1200 \pm 109 \text{ M}^{-3}$ (intersection \pm propagated uncertainty). This value is significantly larger than $K_{\text{eff}} = 214 \text{ M}^{-3}$, illustrating disagreement between our findings and implications of the Anderson formalism.

We speculated that the increased appearance of composite GUV structures (*i.e.* those composed of two or more adhered

GUVs; see schematic in Fig. 5h) in the loaded mbCD–GUV mixtures might relate to this disagreement. These structures coexisted with isolated GUVs containing bending protrusions used to collect the bending statistics in Fig. 5d–f. Fig. 5i and j are examples of composite structures formed between two GUVs whereas Fig. 5k is an example of a so-called GUV aggregate, being composed of many adhered GUVs. Composite GUV structures appeared more frequently when $Q_{\phi}^{\text{dil}} \geq 912 \text{ M}^{-3}$, falling near the boundary separating delayed/rapid lipid re-nucleation (*i.e.* $Q_{\phi} \cong 1000 \text{ M}^{-3}$; see Fig. 4a). This also fell near $Q_{\phi}^{\text{cross}} = 1200 \pm 109 \text{ M}^{-3}$, supporting the above premise.

It is conceivable that rapid re-nucleation of nascent lipid assemblies (from release of lipid from complexes) could drive GUV aggregation as a means of cloaking the hydrophobic areas of lipids with suboptimal packing in re-nucleated assemblies.^{66,67} Indeed, composite GUV structures similar to those in Fig. 5i and j have been considered previously,⁶⁸ concluding that substantial adhesive energies are required for their formation. Highly strained lipids with tails embedded between GUVs and re-nucleated lipid particles (similar conformations observed in simulations)⁶⁹ could provide such adhesive forces. Such bridging interactions could even underly heterogeneous nucleation on the surfaces of GUVs. If the above phenomena preferentially drew de-complexed lipid into nascent lipid assemblies as opposed to pre-formed GUVs, then the data in Fig. 5d–f might convey the delivery-tendency of the nucleates (and not loaded mbCD).^{53,70} Accordingly, we devised our next experiments to limit unconstrained lipid re-nucleation and assess whether this process explains $Q_{\phi}^{\text{cross}} \neq 214 \text{ M}^{-3}$.

Local delivery of loaded mbCD to monitor remodelling of single GUVs in real-time

We thought that local delivery of mbCD to single GUVs might minimize the occurrence of re-nucleation and subsequent adhesion/aggregation events (described above). We accomplished this by using micropipettes to locally administer mbCD solutions of different Q_{ϕ} to single GUVs (see schematic in Fig. 6a). This scheme contrasted with bulk mixing experiments where loaded mbCD was homogeneously distributed throughout the entire external solution (*i.e.* those experiments leading to data in the panels of Fig. 5).

We anticipated that these experiments would either (i) yield a more accurate estimate of Q_{ϕ}^{cross} (thereby addressing why $Q_{\phi}^{\text{cross}} \neq 214 \text{ M}^{-3}$ in bulk mixing experiments) or (ii) validate our estimate of Q_{ϕ}^{cross} from bulk mixing. We flushed single GUVs with mbCD solutions of $Q_{\phi} = 0, 100, 550, 1100 \text{ M}^{-3}$ and $[\text{mbCD}]_{\text{total}} = 10 \text{ mM}$ to observe generation of area asymmetry in real-time. These mbCD solutions spanned the entire range of Q_{ϕ} for which mbCD could be kinetically trapped at RT. For single GUVs treated with $Q_{\phi} = 0, 100, 550 \text{ M}^{-3}$, we observed inner bending protrusions emerge from GUVs, agreeing with observations from bulk mixing. Fig. 6b shows a time-lapse of a GUV flushed with loaded mbCD of $Q_{\phi} = 100 \text{ M}^{-3}$. These findings confirmed that $Q_{\phi}^{\text{cross}} \neq 214 \text{ M}^{-3}$ because Q_{ϕ} above and below 214 M^{-3} induced inner bending protrusions



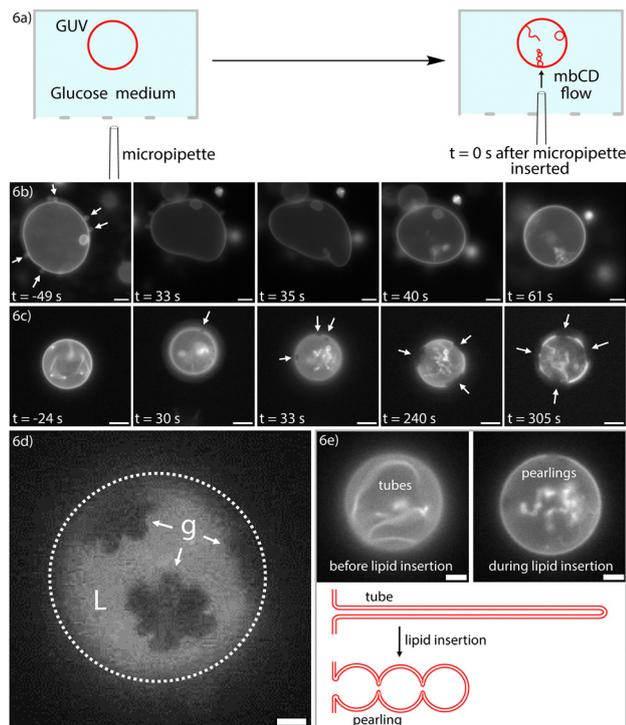


Fig. 6 Local delivery of loaded mbCD achieves morphological remodeling and gel-liquid phase coexistence in 1-component POPC GUVs (a) A schematic of how single GUVs were treated with locally-delivered mbCD. A micropipette was filled with mbCD solution and inserted into an open imaging chamber containing GUVs settled onto the lower surface. A positive pressure was maintained in the micropipette to achieve an outward flow of mbCD solution from the micropipette tip. (b) Timelapse of a GUV treated with a loaded mbCD solution of $Q_\phi = 100 \text{ M}^{-3}$ and $[\text{mbCD}]_{\text{total}} = 10 \text{ mM}$. White arrows in the first frame (prior to micropipette insertion) highlight outward buds on the GUV. Over the course of treatment, the outward buds are retracted, the GUV becomes more tense, and inner bending protrusions emerge. Frame 3 shows the time at which the first inward protrusion began to emerge. Scale bar = $10 \mu\text{m}$. (c) Timelapse of a GUV treated with a loaded mbCD solution of $Q_\phi = 1100 \text{ M}^{-3}$ and $[\text{mbCD}]_{\text{total}} = 10 \text{ mM}$. White arrows show domains within the GUV bilayer. Frame 2 shows the point at which the first domain could be identified. Scale bar = $10 \mu\text{m}$. (d) An example epifluorescence image of a GUV that underwent gel-liquid (g and L, respectively) coexistence after local delivery to $Q_\phi = 1100 \text{ M}^{-3}$ and $[\text{mbCD}]_{\text{total}} = 10 \text{ mM}$ solution. This image was obtained after 6 minutes of exposure to loaded mbCD. Scale bar = $5 \mu\text{m}$. (e) Tube-to-pearl transformation from the timelapse of Fig. 6c with a schematic of this process. Scale bars = $5 \mu\text{m}$.

exclusively. If $Q_\phi^{\text{cross}} = 214 \text{ M}^{-3}$, then lipid insertion would have occurred during $Q_\phi = 550 \text{ M}^{-3}$ delivery. These observations are therefore consistent with the occurrence of negative area asymmetry when $Q_\phi < \sim 1200 \text{ M}^{-3}$ (as determined from bulk mixing experiments; see Fig. 5d and g).

Because observations for $Q_\phi = 0, 100, \text{ and } 550 \text{ M}^{-3}$ validated the bending statistics from bulk mixing experiments, we next asked if delivery of $Q_\phi = 1100 \text{ M}^{-3}$ loaded mbCD would induce outer bending protrusions in single GUVs. Surprisingly, we did not observe outer bending. Instead, we observed phase separation at RT in 99.7% POPC//0.4% Texas Red-DHPE GUVs (mole percentages) (in three GUVs from a total of five). A timelapse

showing emergence and ripening of these domains (dark spots indicated by white arrows) is contained in Fig. 6c. Texas Red-DHPE is known to partition strongly to more disordered phases,⁷¹ suggesting that these domains were more ordered compared to the enriched phase. The domains were initially circular but then ripened into more complex shapes (such as the example shown in Fig. 6d). This behavior suggests that these domains were initially fluid-like but became gel-like the longer GUVs were exposed to loaded mbCD of $Q_\phi = 1100 \text{ M}^{-3}$. These observations agree with recent theoretical predictions that area asymmetry can induce gel-liquid phase coexistence at temperatures above typical transition temperatures determined in symmetric bilayers (*i.e.* $-5 \text{ }^\circ\text{C}$ for POPC, well-below the temperature of these experiments).^{5,10,72}

In all cases, the morphological transformation shown in Fig. 6e preceded emergence of these domains (they can also be seen by close-inspection of the time-lapse in Fig. 6c). These tube-to-pearl transformations are consistent with a reduction in the magnitude of negative spontaneous curvature (from lipid insertion) under the constraint of fixed volume.^{73,74} We are uncertain why these inward bending protrusions were not retracted into the flat portions of these GUVs (a phenomenon implied by the bending statistics in Fig. 5d-f); this finding might relate to the metastability of closed necks in these vesicles.⁷⁵ Occurrence of lipid insertion for $Q_\phi = 1100 \text{ M}^{-3}$ agrees with our estimate of $Q_\phi^{\text{cross}} = 1200 \pm 109 \text{ M}^{-3}$ (within associated uncertainty) (please see indicated note).⁷⁶ The significance of this finding will be emphasized in the Discussion section.

Discussion

mbCD-lipid equilibrium shares some characteristics with that between “slow” solubilizing detergents and lipids

During our characterization of the chemical equilibrium between mbCD and lipid, we identified a new boundary in mbCD-lipid phase space: *i.e.*, the onset boundary (refer to Fig. 2d). The onset and solubilization boundaries enclose an additional region in mbCD-lipid phase space. Interestingly, this region seems to be analogous to regions in detergent-lipid phase diagrams in which bilayers coexist with mixed detergent-lipid micelles.⁷⁷

Proceeding with this analogy, the scrambling/leakage behaviors leading to the onset boundary are reminiscent of so-called “slow” solubilizing detergents.^{78,79} These amphiphiles are thought to possess a limited capacity to rapidly flip-flop between the leaflets of intact vesicles (AKA “crack in”);⁸⁰ this matches the long timescales (hours to days) associated with phospholipid flip-flop.^{51,52} Our finding that intact, POPC vesicles exposed to mbCD had (i) minimal changes in NBD-PE and NBD-Gluc accessibility ($< 3\%$ in both cases; refer to Fig. 2b and c) and (ii) could support long-lived morphological/phase transformations (see GUV experiments) mimics the behaviors attributed to detergents in this category.

Our observations contrast with scrambling/leakage behaviors attributed to “fast” detergents.^{81,82} Such amphiphiles



rapidly penetrate across bilayers, possibly *via* pre-pores.^{58,83} “Fast” detergents readily dissipate area asymmetry on minute timescales (as shown in this study),⁸² differing from long-lived (hour timescales) asymmetries generated by mbCD.³² The metastability of area asymmetry in our study is likely owed to the fact that the molecular shape of POPC^{27,84} is not expected to facilitate pre-pore formation (differing from conical amphiphiles which do serve this role).^{85–87}

mbCD-mediated lipid extraction generates differential tension and net bilayer tension

Our observations of GUVs exposed to mbCD (in both the bulk mixing and local delivery schemes) provide evidence that lipid is asymmetrically extracted from the outer leaflets of intact vesicles in a concentration-dependent manner (throughout region I of Fig. 2d). This process appears to induce differential tension (denoted by $\Delta\Sigma$). $\Delta\Sigma$ is defined as the difference between the mechanical tensions of the outer and inner leaflets (denoted by σ_{out} and σ_{in} , respectively) given by $\Delta\Sigma = \sigma_{\text{out}} - \sigma_{\text{in}}$.^{5,54} Asymmetric lipid extraction accumulates $\Delta\Sigma$ by causing lipids in the depleted, outer leaflets to be relatively stretched compared to those contained in the inner leaflets (as in Fig. 3a).

When $\Delta\Sigma$ accumulates within a bilayer, the bilayer possesses an increased tendency to undergo bending/shape transitions.^{5,7,88} Thus, our observation of an increase in the average negative curvature of GUVs with respect to $[\text{mbCD}]_{\text{total}}$ implies an increase in $\Delta\Sigma$ as the onset boundary is approached (see bending statistics in Fig. 3d). Likewise, our observation of a plateau in negative curvature during the solubilization transition (region II of Fig. 2d) indicates that $\Delta\Sigma$ seems to approach a fixed value between the onset and solubilization boundaries. By extension, this implies that lipids in the outer leaflets of intact vesicles during the solubilization transition experience similar degrees of stretching (and similar values of σ_{out}) in this region of phase space.

Along with $\Delta\Sigma$, real-time observation of asymmetric lipid extraction from GUVs during local delivery experiments (refer to Fig. 6b) revealed a tensing effect. This observation implies that vesicles exposed to mbCD also accumulated net bilayer tension (denoted by σ_{net}) distributed uniformly across the bilayer; this is consistent with reports of the mbCD-mediated activation of mechanosensitive ion channels.¹⁸ Nonzero σ_{net} must result from (i) net loss of lipid from the GUVs and (ii) impedance to bending (from osmotic constraints) as $\Delta\Sigma$ is accumulated. The former contribution pertains to tension from osmotic/hydrostatic pressure whereas the latter pertains to the so-called spontaneous tension.^{42,74,89}

We propose that the combination of nonzero $\Delta\Sigma$ and σ_{net} distributed within these vesicles drove mbCD-mediated collapse/solubilization. Though the exact events involved in vesicle collapse are unclear at this time, one hypothesis is that the onset boundary corresponds to a location in mbCD–lipid phase space at which biased flipping (possibly *via* bilayer defects) was initiated on short timescales. If this process occurred in coordination with mbCD-mediated extraction, then vesicle collapse could result. Possible candidates for the bilayer-defects

involved in this process include pre-pores⁵⁸ or micelle-like defects.⁵⁴ As $[\text{mbCD}]_{\text{total}}$ is continually increased beyond the onset boundary, we propose that different subpopulations of vesicles (harboring relatively similar $\Delta\Sigma$ and σ_{net}) undergo collapse/solubilization until no vesicles persist in the mixture (occurring at the breakpoint of a titration, along the solubilization boundary). Further increase of $[\text{mbCD}]_{\text{total}}$ (into region III of Fig. 2d) drives additional, undetectable complexation of lipid monomers in the solution.

Hypertonic deflation enhances the survivability of vesicles exposed to mbCD

We found that hypertonic conditions lead to a smaller K_{eff} during the solubilization transition under hypertonic conditions compared to osmotic balance. Phenomenologically, this means that larger $[\text{mbCD}]_{\text{total}}$ are required to achieve solubilization under hypertonic conditions for equivalent $[\text{POPC}]_{\text{total}}$. We determined $K_{\text{eff}} = 214 \pm 5 \text{ M}^{-3}$ under isotonic conditions and $K_{\text{eff}} = 30 \pm 1 \text{ M}^{-3}$ under hypertonic conditions. Using eqn (3) and (5) with these values of K_{eff} (and the relation $[\text{mbCD}]_{\text{onset}} = 0.4 \times [\text{mbCD}]_{\text{break}}$), we can predict the percentage of extracted lipid in the vicinity of the onset boundary under both osmotic conditions. Performing this calculation over the complete range of $[\text{POPC}]_{\text{total}}$ used in both cases, we report that 3% and 5% lipid extraction (of the total lipid) led to collapse/solubilization in the isotonic and hypertonic cases, respectively. This reveals that hypertonicity allows vesicles to sustain a greater amount of asymmetric extraction prior to collapse.

One hypothesis for this finding is that hypertonic stress partially alleviates osmotic constraints and thereby facilitates vesicle shape transitions (as in these studies).^{73,90} Hypertonic deflation would thereby allow a greater fraction of a bilayer to undergo bending transitions in response to asymmetric extraction (compared to vesicles in the isotonic case). This would minimize the fraction of the bilayer that is unable to match its preferred or spontaneous curvature (from area asymmetry generation).^{34,91,92} Failure to adapt in such a fashion results in accumulation of large, nonzero σ_{net} (from spontaneous tension, referred to earlier)^{74,89} within these portions of the bilayer. Osmotic deflation (as in the hypertonic case could (i) reduce the fraction of the bilayer subjected to this large, nonzero σ_{net} and (ii) thereby reduce the free energy density of the bilayer. Both effects could oppose defect-formation underlying vesicle collapse/solubilization. Ultimately, this could allow vesicles in the hypertonic case to survive to a greater degree of lipid extraction compared to vesicles under isotonic conditions.

Changes in lipid chemical activity due to area asymmetry can be detected through mbCD–lipid chemical equilibrium

Based on the Anderson formalism (*i.e.* that $\alpha_L = 1$ throughout the coexistence region),²³ we hypothesized that Q_{ϕ}^{cross} from loaded mbCD experiments should match the value of K_{eff} at the RT solubilization boundary under corresponding osmotic conditions. We found that the value of $K_{\text{eff}} = 214 \pm 5 \text{ M}^{-3}$ disagrees with our estimate of $Q_{\phi}^{\text{cross}} = 1200 \pm 109 \text{ M}^{-3}$ from



GUV experiments. We propose that this disagreement can be explained by variation of α_L in 1-component bilayers containing area asymmetry. This implies that the assumption proposed by Anderson *et al.* for mbCD–lipid complexation (*i.e.* that $\alpha_L = 1$ in intact, 1-component vesicles) is invalid. To demonstrate this, we will make use of the definitions for K_{total} and K_{eff} (from eqn (2) and (3); see background section).

We propose that identification of Q_ϕ^{cross} provides an estimate of the equilibrium constant for mbCD–POPC complexation (that is, K_{total}). By Le Chatelier's Principle, when $Q_\phi < K_{\text{total}}$, asymmetric extraction will be driven spontaneously (yielding net negative curvature in the GUVs); when $Q_\phi > K_{\text{total}}$ asymmetric insertion will be driven spontaneously (yielding net positive curvature in the GUVs). When $Q_\phi = K_{\text{total}}$, however, there is no net tendency for extraction or insertion. Since we have defined Q_ϕ^{cross} as the value of Q_ϕ at which neither inward nor outward bending is favored, it follows that $Q_\phi^{\text{cross}} = K_{\text{total}}$. Therefore, we report an estimate of $K_{\text{total}} = 1200 \pm 109 \text{ M}^{-3}$ for the complexation of POPC by mbCD. Importantly, this constant is different from the parameters obtained by fitting solubilization boundaries in mbCD–lipid phase space.

Through such fitting, K_{eff} is obtained and not K_{total} (see background section). Whereas K_{total} is constant, $K_{\text{eff}} = K_{\text{total}} \times \alpha_L$. Therefore, K_{eff} captures variation from α_L . For example, if $\alpha_L < 1$, then $K_{\text{eff}} < K_{\text{total}}$. By fitting the RT solubilization boundary under different osmotic conditions, we obtained estimates of $K_{\text{eff}} = 214 \pm 5 \text{ M}^{-3}$ (isotonicity) and $K_{\text{eff}} = 30 \pm 1 \text{ M}^{-3}$ (hypertonicity). Comparison of these values to $K_{\text{total}} = 1200 \pm 109 \text{ M}^{-3}$ shows that $\alpha_L < 1$ at these boundaries. Using our estimates of K_{total} and K_{eff} under both osmotic conditions yields $\alpha_L = 0.18 \pm 0.02$ (isotonicity) and $\alpha_L = 0.025 \pm 0.002$ (hypertonicity) (estimates \pm propagated uncertainties) in the outer leaflets of vesicles on the verge of collapse. These estimates of α_L can be related to microscopic and mechanical quantities in vesicles.

Lipid chemical activity allows estimation of area-per-lipid values and the differential tension in vesicles exposed to mbCD

Jähnig proposed an equation for the chemical potential of lipid in the outer leaflets of vesicles (eqn (9) in the reference).⁵³ From this equation, α_L is found to be:⁹³

$$\alpha_L = \exp\left[\frac{\gamma(a_0^2 - a_{\text{out}}^2)}{k_B T a_0}\right] \quad (7)$$

where γ is the interfacial energy density of the monolayer–water interface ($\gamma \approx 40 \text{ mN m}^{-1}$ for POPC);^{94,95} a_0 is the optimal or preferred area-per-lipid ($a_0 = 0.63 \text{ nm}^2$ for POPC at 23 °C);⁹⁶ k_B is the Boltzmann constant; T is the temperature (23 °C in our experiments); and a_{out} is the actual area-per-lipid of vesicles in the outer leaflets of vesicles exposed to mbCD.

Using eqn (7), we can use our estimates of α_L for vesicles on the verge of collapse (*i.e.* during the solubilization transition) to predict associated values of a_{out} . Doing so, we obtain $a_{\text{out}} = 0.71 \pm 0.01 \text{ nm}^2$ (isotonicity) and $a_{\text{out}} = 0.80 \pm 0.01 \text{ nm}^2$ (hypertonicity) (estimate \pm propagated uncertainty); these estimates correspond to 13% and 26% relative lipid expansion,

respectively. Recalling our earlier calculation, the larger relative expansion in the hypertonic case is associated with a larger percentage of lipid extraction (5%) compared to the isotonic case (3%). These relative lipid expansions found above are comparable to the 18% relative expansion in the underfilled leaflet of planar bilayers containing the maximal amount of area asymmetry for which this assembly remained metastable/defect-free during microsecond simulations.⁵⁴ The fact that our real-world bilayers seemed to contain $\sigma_{\text{net}} > 0 \text{ mN m}^{-1}$ (see earlier discussion) whereas the simulated bilayers were tensionless (*i.e.* $\sigma_{\text{net}} = 0 \text{ mN m}^{-1}$) could explain the differences between our estimates and this literature value.

Using the above estimates of a_{out} , it is also possible to predict associated values of σ_{out} and $\Delta\Sigma$ in this location of phase space. By extending a model proposed by Israelachvili,²⁷ Levadnyy *et al.* described σ_{out} using the following equation:⁹⁷

$$\sigma_{\text{out}} = \gamma \left(1 - \frac{a_0^2}{a_{\text{out}}^2}\right) \quad (8)$$

Substituting the above values of a_{out} into eqn (8) yields $\sigma_{\text{out}} = 8.5 \pm 0.2 \text{ mN m}^{-1}$ (isotonicity) and $\sigma_{\text{out}} = 15.2 \pm 0.2 \text{ mN m}^{-1}$ (hypertonicity) (estimate \pm propagated uncertainty). These values are similar in magnitude to the rupture tensions reported for phosphatidylcholine vesicles subjected to micropipette aspiration.⁹⁸ If we assume that vesicles are tensionless (*i.e.* $\sigma_{\text{net}} = \sigma_{\text{out}} + \sigma_{\text{in}} = 0 \text{ mN m}^{-1}$), then $\sigma_{\text{in}} = -\sigma_{\text{out}}$ and $\Delta\Sigma = 2\sigma_{\text{out}}$.^{10,48} Using this assumption, we obtain estimates of $\Delta\Sigma = 17.0 \pm 0.4 \text{ mN m}^{-1}$ (isotonicity) and $\Delta\Sigma = 30.4 \pm 0.4 \text{ mN m}^{-1}$ (hypertonicity) (estimate \pm propagated uncertainty). Each of the parameters estimated from our experimental determinations of α_L are summarized in Table 2.

We note the following caveat to the above estimates of $\Delta\Sigma$. Even though asymmetric bilayers are typically simulated under the constraint of $\sigma_{\text{net}} = 0 \text{ mN m}^{-1}$,^{54,99–101} we reiterate that real-world vesicles exposed to mbCD appear to contain $\sigma_{\text{net}} > 0 \text{ mN m}^{-1}$ (from contributions explained above). Nonzero σ_{net} results in additional stretching contributions distributed between both leaflets which contribute to α_L , a_{out} , and σ_{out} but which drop out of $\Delta\Sigma$ (because they are evenly distributed between the leaflets). Accordingly, the tensionless condition probably provides an upper limit to $\Delta\Sigma$ in vesicles on the verge of collapse: *i.e.* $\Delta\Sigma \leq 2\sigma_{\text{out}}$. In other words, estimates of $\Delta\Sigma$ reported above are probably overestimates.

Relating to the above, bilayer stiffening and gel–liquid phase coexistence from accumulation of $\Delta\Sigma$ has been studied for $\sigma_{\text{net}} = 0 \text{ mN m}^{-1}$ only.^{5,102} We observed such transitions in the

Table 2 Selected parameters characterizing vesicles during mbCD-mediated solubilization under different osmotic conditions at 23 °C

	Isotonicity	Hypertonicity
α_L	0.18 ± 0.02	0.025 ± 0.002
Extracted lipid (%)	3%	5%
a_{out} (nm ² per lipid)	0.71 ± 0.01	0.80 ± 0.01
σ_{out} (mN m ⁻¹)	8.5 ± 0.2	15.2 ± 0.2
$\Delta\Sigma$ (mN m ⁻¹)	17.0 ± 0.4	30.4 ± 0.4



flat portions of GUVs which were studded with high-curvature, inward protrusions (see time-lapse of Fig. 6c), revealing that these GUVs possessed nonzero, negative spontaneous curvatures during exposure to loaded mbCD. Accordingly, the flat portions of these GUVs in which the gel domains formed must have harbored a nonzero spontaneous tension (which applies an additional stretching contribution to lipids within these regions).^{74,89} This contribution was presumably opposed by a compressive contribution due to net lipid insertion into the bilayer (under the constraint of fixed encapsulated volume). The direction and magnitude of σ_{net} is unclear because the magnitudes of the above contributions are unknown.

Because application of mechanical tensions alters coexistence in bilayers,^{103,104} the above contributions are likely to be relevant for understanding phase behaviors^{4,105} associated with lipid asymmetry. Therefore, these contributions should be considered in future experiments and theory. The fact that $\sigma_{\text{net}} \neq 0 \text{ mN m}^{-1}$ before/during lipid insertion might relate to why we were unable to induce outward bending during local delivery (which was expected based on bulk mixing experiments) and, instead, induced gel domains.

Carbohydrate asymmetries did not bias our assessment of mbCD-mediated transformations in GUVs

Because we diluted GUVs with encapsulated sucrose solutions into osmotically-balanced glucose solutions at different stages of our experiments, we must consider the effects of carbohydrate asymmetry upon our study.⁴⁵ Shape changes associated with this phenomenon could have confounded our determination of Q_{ϕ}^{cross} , for example, since this was based on assessment of GUV bending transitions. This does not seem to have occurred because we observed (i) similar frequencies of GUVs containing inner/outer bending protrusions in the absence of mbCD and (ii) almost half of the GUVs contained no bending protrusions in the absence of mbCD (see Fig. 5d). Therefore, the electroformed GUVs used in the bulk mixing experiments were flat, on average, across the eleven dispersions. If solution asymmetry had a more pronounced effect on our study, then outer bending protrusions would have dominated in the control (due to the larger size of sucrose compared to glucose) (as in this study).⁴⁵

Moreover, the striking outer pearling morphologies associated with carbohydrate asymmetry are associated with more extensive deflation ($>10\%$ deflation)⁴⁵ compared to that experienced by GUVs in our study (no more than 2% deflation; see ESI†). Finally, we note that GUVs used in our study appeared to be mechanically relaxed – on average, across all vesicles within each dispersion – in the absence of mbCD (see Fig. 5d and Fig. S2/associated discussion in the ESI†).^{7,106} This implies that the GUVs occupied their reference states (characterized by $\alpha_{\text{L}} = 1$) prior to lipid exchange with mbCD. Since the GUVs appeared to occupy their reference state, this validates $Q_{\phi}^{\text{cross}} = K_{\text{total}}$ (which requires that the GUVs exposed to the corresponding mbCD solution are characterized by $\alpha_{\text{L}} = 1$).

Conclusions

We have leveraged mbCD–lipid complexation to generate area asymmetry in 1-component vesicles. This conclusion reiterates the bases of important preparatory schemes for *in vitro* membrane asymmetry research^{17,32} and highlights the synthetic utility gained by kinetic trapping of mbCD–lipid complexes. Specifically, kinetic trapping was required to achieve net lipid insertion into GUVs, yielding (i) tunable curvature-generation and (ii) gel–liquid coexistence at 23 °C. It is already established that compositional asymmetry influences phase coexistence in multicomponent bilayers,^{4,105} but here we have studied the effect of area asymmetry/differential tension in isolation (in confirmation of recent theoretical predictions).^{5,102}

We also showed that (1) neglecting variation in lipid chemical activity underestimates equilibrium constants for mbCD–lipid complexation and (2) this variation is related to mechanical stresses in vesicles. Practically, this indicates that a re-evaluation of reported equilibrium constants^{23,31,32} is warranted. Furthermore, our study highlights the usefulness of lipid chemical activity (accessible through systematic treatment of mbCD–lipid equilibrium) for quantitative study of lipid asymmetry. To this end, we applied a basic thermodynamic model to calculate microscopic/mechanical parameters using two estimates of lipid chemical activity yielded by our study.

In the future, mbCD–lipid equilibrium could be used to validate models for transmembrane protein allostery with respect to lipid asymmetry.⁸ These ideas are relevant, for example, in the mbCD-mediated opening of mechanosensitive ion channels which has received recent attention.^{18,19} Based on our findings, the allosteric bias applied by mbCD in these experiments seems to result from a combination of differential tension and net bilayer tension. Similarly, it is likely that allosteric bias and adjustment of lipid thermodynamic gradients due to differential tension is relevant for the activities of lipid flippases and scramblases.¹⁰⁷

Author contributions

T. R. and T. B. designed research. T. R., Y. X., Z. A., and W. C. performed research. T. R. and T. B. wrote the article.

Conflicts of interest

There are no conflicts to declare.

Acknowledgements

We acknowledge funding through NIH grant NIGMS 097552.

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