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## Introduction

The nematic (N) phase is the simplest liquid crystalline state, consisting of molecules or particles that have long-range orientational order but lack translational order. Despite this orientational order, the bulk nematic phase is apolar as there are an equal number of molecules oriented parallel and antiparallel.

In the recently discovered ferroelectric nematic  $(N_F)$  phase,<sup>1-6</sup> the orientational order of the conventional nematic state is augmented by so-called polar order which arises due to parallel alignment of molecular electric dipole moments. This parallel alignment distinguishes it from the nematic phase, and virtually all other fluid states of matter. Depictions of nematic and polar nematic phases are given in Fig. 1.

Having been the subject of some speculation,<sup>7–9</sup> the  $N_F$  phase has been now experimentally realised in several classes of materials, having originally been observed in RM734 and

# Room-temperature ferroelectric nematic liquid crystal showing a large and diverging density;

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The ferroelectric nematic phase  $(N_F)$  is a recently discovered phase of matter in which the orientational order of the conventional nematic liquid crystal state is augmented with polar order. Atomistic simulations suggest that the polar N<sub>F</sub> phase would be denser than conventional nematics owing to contributions from polar order. Using an oscillating U-tube densitometer, we obtain detailed temperature-dependent density values for a selection of conventional liquid crystals with excellent agreement with earlier reports. Having demonstrated the validity of our method, we then record density as a function of temperature for M5, a novel room-temperature ferroelectric nematic material. We present the first experimental density data for a N<sub>F</sub> material as well as density data for a nematic that has not previously been reported. We find that the room-temperature N<sub>F</sub> material shows a large (>1.3 g cm<sup>-3</sup>) density at all temperatures studied, notably including phases without polar order. An increase in density at phase transitions is observed. The magnitude of the increase for the intermediate-to-ferroelectric nematic  $(N_X - N_F)$  transition is an order of magnitude smaller than the isotropic-nematic (I-N) transition. We then probe potential consequences that may result from an elevated density through measurement of the refractive indices ( $n_o$  and  $n_e$ ). The  $n_{avg}$  of M5 is compared with 5CB and polar smectic liquid crystals. We observe how the highly polar nature of the system counteracts the effects of an increase in density. With knowledge of experimental density, we are able to derive an approximation that yields the polar order parameter, (P1), from polarisation measurements. Present results may be typical of ferroelectric nematic materials, potentially guiding material development, and is especially relevant for informing ongoing studies into this emerging class of materials.

DIO, (Fig. 1(c) and (d)), both reported in 2017. In recent years the number of  $N_F$  materials has been increased significantly as derivatives of RM734 and DIO<sup>10–14</sup> have been developed, including those exhibiting a direct I– $N_F$  transition.<sup>15</sup>

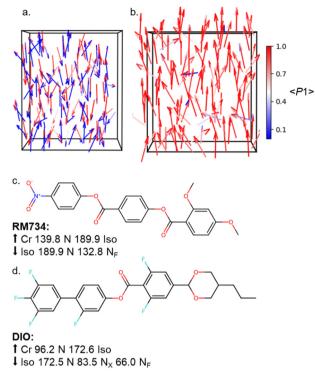
In RM734<sup>1,2</sup> the N-N<sub>F</sub> transition is accompanied by a softening of the K<sub>1</sub> splay constant, and a growth of ferroelectric ordering.<sup>4,6</sup> DIO<sup>3</sup> behaves slightly differently, with an intermediate phase between the N and N<sub>F</sub>; crucially however, DIO was also shown to possess these same characteristic macroscopic domains of ferroelectric ordering in the low temperature nematic phase.<sup>5</sup> When studied by DSC, there is a small enthalpy associated with the transition from nematic to polar nematic phase(s). Dielectric measurements have reported large dielectric permittivity values on the order of 10<sup>4</sup> for RM734<sup>16</sup> and for DIO,<sup>3,17</sup> although the validity of these has been questioned.<sup>18,19</sup> Polarisation investigations have found values of spontaneous polarisation for RM734  $(6 \ \mu C \ cm^{-2})^{5,20}$  and DIO  $(2.5-6 \ \mu C \ cm^{-2})^{3,17}$  which are comparable with polar columnar  $(5.8 \ \mu C \ cm^{-2})^{21}$  and bent core liquid crystals (LCs) (0.5–0.8  $\mu$ C cm<sup>-2</sup>).<sup>22</sup> The measured N<sub>F</sub> spontaneous polarisation values is far larger than typical chiral smectic C materials (e.g. DOBAMBAC, 42.0 nC  $\text{cm}^{-2}$ )<sup>23</sup> and somewhat smaller than that achieved by inorganic materials - e.g. the inorganic material  $PbSc_{0.5}Ta_{0.5}O_3$  (30.0 µC cm<sup>-2</sup>).<sup>24</sup>

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**Fig. 1** Depictions of the orientations of the molecular electric dipole moments in the (a) nematic and (b) ferroelectric nematic phases; the arrows are color-coded to represent the contribution to the bulk value of the polar order parameter,  $\langle P1 \rangle$  which is 0.08 for (a) and 0.86 for (b), respectively, while  $\langle P2 \rangle$  is 0.66 and 0.66 for (a) and (b), respectively. In both cases the director is oriented perfectly with the box height (*z*-axis). The molecular structures of the first reported N<sub>F</sub> materials; (c) RM734,<sup>1,2</sup> and (d) DIO<sup>3</sup> along with their transition temperatures (*T*, °C) on heating ( $\uparrow$ ) and cooling ( $\downarrow$ ).

Our investigations were driven by the predictions of atomistic molecular dynamics (MD) simulations. MD simulations can reproduce the polar nematic ordering and calculate mean densities from atomic scale interactions.<sup>25</sup> Simulations predicted a high mass density,  $\rho$  of 1.3 g cm<sup>-3 25</sup> in RM734. Considering the oft-used assumption that  $\rho$  in liquid crystals  $\approx 1 \text{ cm}^{-3}$ , known to be an approximation for some LCs and is unjustified for many others, this raises a potential defining property of N<sub>F</sub> materials.

As LCs undergo a first-order phase transition, they exhibit a density change that can be discontinuous.<sup>26</sup> The temperature dependence of density,  $\rho(T)$  in a discrete liquid crystal phase can be described by a linear thermal expansion of its specific volume,  $v_{sp}$  as described in eqn (1) and (2)

$$\nu_{\rm sp}(T) = 1/\rho(T) \tag{1}$$

$$v_{\rm sp}(T) = v_{\rm sp}^* + \alpha T \tag{2}$$

where  $v_{sp}^*$  is the specific volume at 0 °C,  $\alpha$  is an empirical expansion coefficient describing how the material behaves with temperature changes, and *T* is the temperature.

The density of LCs has previously been measured by several methods including the capillary tube technique,<sup>25</sup> the weight

change of a submerged glass cylinder<sup>27</sup> and a dilatometer measuring the height of a mercury interface.<sup>28</sup> These methods all suffer from a difficulty in obtaining the precise temperature control that detailed study over phase transitions demands. Moreover, the lack of experimental density data for all but a handful of common LCs has led to the incorrect (*vide infra*) assumption about  $\rho$  being propagated.

Density data were available for 5CB,<sup>29–33</sup> 8CB,<sup>34–36</sup> and (NCS)PCH6.<sup>37</sup> A comprehensive list of the data and their properties are given in section 4 of the supplementary information. The 5CB dataset<sup>30</sup> was chosen for comparison with high resolution data (between 5 °C and 0.2 °C) over a large temperature range. The available data for 8CB consisted of either sparse measurements<sup>35</sup> or data taken over a temperature range near a single transition.<sup>34</sup> The (NCS)PCH6 literature data<sup>37</sup> were used out of necessity as no other data were available. We analyse the agreement of the experimental and literature data through Bland–Altman<sup>38</sup> type plots (ESI,† Section S4). We find limits of agreement, *l* through eqn (3) where  $\tilde{d}$  is the mean difference between our experimental data and its corresponding literature data.  $\sigma_d$  is the standard deviation  $\tilde{d}$ . Its agreement can then be judged through the data's vicinity to  $\tilde{d}$ .

$$l = \bar{d} \pm 1.96\sigma_d \tag{3}$$

The largest difference between the agreement comes from a systematic differences between the methods in the capillary tube investigation of  $5CB^{32}$  and  $8CB^{36}$  where a dilatometer is used. These methods have a systematic difference of approximately 1% and 3% respectively compared to  $0.02\%^{30}$  and  $0.04\%^{35}$  of the density meters. This is calculated from the average of the differences used in the Bland–Altman plots (Fig. S9–S17 in ESI†).

In this article we report an unusually large density (>1.3 g cm<sup>3</sup>) for a ferroelectric nematic liquid crystal, **M5** (Merck Electronics KGaA). A density increase resulting from polar ordering on transition to an N<sub>F</sub> state is also shown. We benchmark our results against a set of standard liquid crystals, which we find to be in excellent agreement with the available literature data. Finally, we evaluate potential implications of a large density for liquid crystals by comparing its average refractive index with polar smectic liquid crystals and **5CB**. Spontaneous polarisation measurements and an approximation of the polar order of DIO are examined with consideration of the experimentally confirmed N<sub>F</sub> density.

### Methods and experimental

Density measurements were performed using an Anton-Paar DMA 4100M densitometer which operates on the oscillating U-tube principle (Fig. 2). A U-shaped borosilicate glass tube is filled with  $\approx 1$  mL material. Samples were loaded using a SGE precision syringe. A syringe heater was used for samples with above-ambient melting points; the syringe outlet was interfaced with the DMA 4100M inlet port using a short section of PTFE tubing with appropriate PEEK/ETFE microfluidic connectors (purchased from Darwin Microfluidics). The presence of bubbles within the tube was assessed through visual inspection.

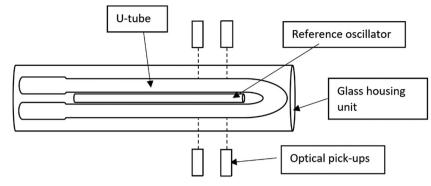


Fig. 2 Schematic diagram of the oscillating U-tube setup used to measure density. The optical pickups determine the LC sample's characteristic frequency which corresponds to a density value.

This experimental method requires a large amount of material; however, it can be largely recovered on the completion of the measurements. Recovered material was subjected to purification with a Teledyne Combiflash NextGen 300+ Flash chromatography system and filtration over a 0.2 micron PTFE filter.

Once filled, the tube is excited to oscillate at its characteristic frequency in the direction of the normal to the tube. The density is calculated from eqn (4)

$$\rho = A \cdot Q^2 \cdot f_1 - B \cdot f_2 \tag{4}$$

with *Q* being the quotient of the characteristic frequencies of the measuring tube and a reference tube. *A* and *B* are constants specific to the instrument and are calculated by calibrating against substances with a precisely known value for density.  $f_1$  and  $f_2$  are corrections factors. The  $f_1$  and  $f_2$  correction factors possess contributions from the viscosity of the sample in the form of damping. An increase in viscosity has an increased damping effect on the characteristic frequency of the oscillating tube, resulting in a greater magnitude of corrections needed. A valid measurement for this machine is three successive measurements that do not deviate beyond 0.0001 g cm<sup>-3</sup>. The repeatability of the temperature during measurement is 0.02 °C.

Refractive indices measurements were performed on a Bellingham + Stanley Abbe 60/DR refractometer. The refractometer finds the critical angle of total reflection of an LC sample at a wavelength of 589 nm. A polariser is used to differentiate between the ordinary and extraordinary refractive indices. Temperature control is achieved by circulating water with a temperature range from room temperature to ~70 °C and an accuracy of ~0.2 °C.

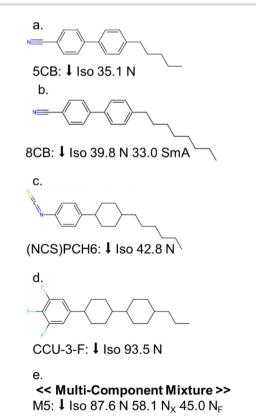
The temperature dependence of polarisation is measured through its switching current response.<sup>39</sup> A triangular wave voltage with  $V_{\text{RMS}} = 5$  V and frequency = 63 Hz was produced by an Agilent 33220A waveform generator and applied to DIO in a 4 µm INSTEC cell with no alignment layer. Temperature control was achieved with a LINKAM THM600 hot stage. The output signal was recorded on RIGOL DHO 4204 oscilloscope. Integration of the current response peaks calculates the  $P_{\rm s}$  through eqn (5)

$$P_{\rm s} = \int \frac{I_{\rm p}}{2AG} {\rm d}t \tag{5}$$

where  $I_p$  is the current due to polarisation reversal, A is the area of the cell and G is the gain of the current-to-voltage amplifier used in the experimental method.

#### Materials

The materials selected were **M5** (Merck Electronics KGaA), 4-*cyano*-4-pentylbiphenyl (**5CB**, Fluorochem), 4-*cyano*-4-octylbiphenyl (8CB, Fluorochem), 1-(*trans*-4-hexylcyclohexyl)-4-isothiocyanatobenzene ((NCS)PCH6), (Sigma-Aldrich) and *trans*-4-(*trans*-4'-*n*-propylcyclohexyl)-cyclohexyl-3,4,5-trifluorobenzene



**Fig. 3** Chemical structures of the materials for which density measurements were undertaken. Transition temperatures (T, °C) on cooling ( $\downarrow$ ) were determined from density measurements and are in good agreement with DSC data (ESI,† Section S1). For single component materials (a)–(d) molecular structures are given.

(CCU-3-F, prepared according to ref. 40). Both **M5** and commercial materials were used as received. Fig. 3 presents the transition temperatures for the materials investigated in this work, and chemical structures in the case of single-component materials (Fig. 3(a)–(d)). The limits of the density meter's operating temperature range did not allow for measurements of RM734 and DIO.

## Results

#### Apolar liquid crystals

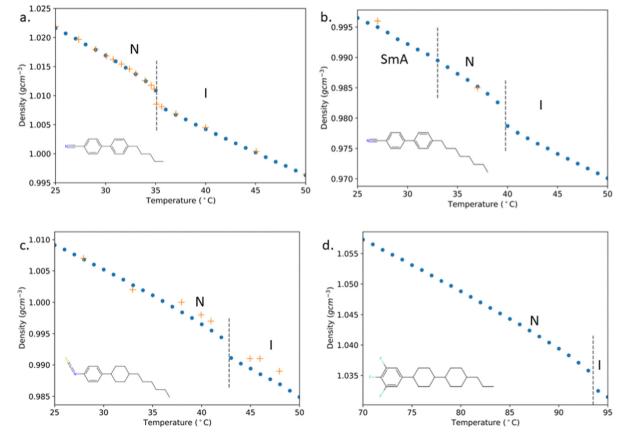
Our initial investigations focused on a set of relatively well-known materials, for some of which density data was available. We selected **5CB** as it is an ambient temperature nematic; 8CB as it exhibits a transition between two LC phases (smectic A (SmA), a layered structure and N) and has a high viscosity at ambient temperature; (NCS)PCH6 as a non-nitrile room-temperature nematic LC; CCU-3-F as a fluorinated LC with an above-ambient melting point which enabled us to refine our technique for handling materials with elevated melting points. The temperature-dependent densities for the selected materials are given in Fig. 4.

The measurement runs for all materials began in the isotropic phase and were cooled through the phase range into their lowest temperature phase above crystallisation. The present results compare very favourably with available literature data for **5CB**, 8CB and (NCS)PCH6. In all cases, the density of the LC materials is around 1 g cm<sup>-3</sup>. The I–N transitions for each material can be clearly observed as discontinuous increase in  $\rho$ . At the N–SmA transition (Fig. 4(b)) we do not find a discernible increase in density.

#### Ferroelectric nematic liquid crystal M5

Having shown our ability to reproduce and expand upon literature densities of common liquid crystals, we next performed density measurements on the room-temperature  $N_F$  material **M5**, a multi-component mixture produced by Merck Electronics KGaA. A cursory inspection of the data in Fig. 5 reveals that, even in the isotropic liquid, the density of **M5** is remarkably high, being ~30% larger than **5CB** and of the same magnitude as dichloromethane (1.33 g cm<sup>3</sup> at 25 °C).

In **M5** there is a constant decrease in the expansion coefficients as it is cooled through its phase range (Table 1). This can also be observed in the rate of density change within the linear regimes of Fig. 5. As with the other materials investigated, an increase in the density can be seen at  $T_{\rm IN}$  and this feature is also clear at  $T_{\rm N_XN_F}$  though the  $T_{\rm NN_X}$  density change appears to be continuous. Fig. 5 presents data obtained at an increased temperature resolution (0.15 °C compared to the 1 °C given in Fig. 4).



**Fig. 4** Densities of the liquid crystal materials at 1 °C intervals. Dashed lines denote transition temperatures as defined by the temperature of the largest density gradient. The density increases at the phase transition are readily observable for the I–N transitions, but more subtle for the N–SmA transition. Comparison is made with literature data where possible (orange plus points) for (a) **5CB**,<sup>30</sup> (b) 8CB<sup>35</sup> and (c) (NCS)PCH6.<sup>37</sup> (d) The CCU-3-F figure is representative of the scarcity of LC density data.

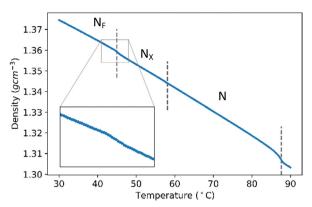


Fig. 5 Temperature-dependent density behaviour for the N<sub>F</sub> material M5 across its phase range. The initial increase with first nematic ordering is on cooling from the isotropic phase at 87.6 °C similar to the other selected materials. There is no discernible change in density at the N-N<sub>X</sub> phase transition. There is a small increase at 45 °C that can be attributed to the effects of polar ordering. The high average density of M5 should also be noted. Inset: N<sub>x</sub>-N<sub>F</sub> transition.

The inset facilitates a more detailed look at the behaviour over the  $N_x$ - $N_F$  transition where the density increase can be seen.

The linear relationship between density and temperature in a discrete phase can be explored through eqn (2). From this,  $v_{sp}(T)$  is separated into discrete phases using the transition temperatures in Fig. 4 as their temperature ranges. The gradient of a linear fit of  $v_{\rm sp}(T)$  for each phase (see also Fig. S18 in ESI<sup>+</sup>) is taken to be the expansion coefficient. Expansion coefficients for the selected materials can be found in Table 1. The expansion coefficients are similar, although we do not find an explicit relationship between coefficient and LC phase type as the coefficient can be seen to either increase (5CB, 8CB) or decrease (CCU-3-F, (NCS)PCH6) through the I-N transition.

Table 2 gives the density increases for the selected materials. A linear fit of the higher temperature phase  $\rho^{\text{highT}}$  was extrapolated into the lower temperature phase and used to calculate the density deviation of the lower temperature phase as it cools. The magnitude of change in density that occurs in the non-linear period between two linear regimes is then taken to be the density deviation of that transition. A representative example of this process is given in Fig. S6 (ESI<sup>†</sup>). The density deviation at (NCS)PCH6's I-N transition can be seen in Fig. 6(a). We find  $\Delta \rho$  of the I–N transitions for all materials studied to be of the same order of magnitude,

Table 1 Expansion coefficients,  $\alpha$  of  $v_{sp}$  calculated for each material in each phase. These parameters are analogous to the thermal expansion coefficient describing how a material's volume changes with temperature. The parameters are obtained through linear fits to  $v_{sp}(T)$  within each specific LC phase

	$\alpha \ 10^4 \ (\text{cm}^3 \ \text{g}^{-1} \ \text{K}^{-1})$					
Material	$N_{\rm F}$	$N_X$	SmA	Ν	Ι	
M5	5.30	6.08	_	6.57	7.09	
5CB	—	—		9.18	7.96	
8CB	—	—	8.16	11.5	8.76	
CCU-3-F	—	—		7.81	9.00	
(NCS)PCH6	—	—	—	8.08	8.80	

Table 2 The magnitude of the density increases of each transition through the non-linear  $\rho(T)$  region. The I–N transitions for all materials are of a similar magnitude as the same sort of ordering takes place. The density change corresponding to M5's N<sub>X</sub>-N<sub>F</sub> transition is an order of magnitude larger than its N-N<sub>X</sub> transition and three times the size of the N-SmA transition of 8CB

Material	$\Delta ho 10^3 \ ({ m g \ cm}^{-3})$					
	I–N	N–N <sub>X</sub>	$N_X - N_F$	N–SmA		
M5	3.1	0.05	0.75			
5CB	2.2	_	_	_		
8CB	2.5	_	_	0.20		
CCU-3-F	2.0	_	_	_		
(NCS)PCH6	2.8	—	—	_		

presumably a consequence the fact the same type of molecular reorganisation takes place for each material at  $T_{IN}$ . For 8CB we find the N-SmA transition is ten times smaller than its I-N transition indicating that the change in molecular packing at the smectic transition is not as a drastic as a nematic one.

M5's increase in density from its I-N and N<sub>x</sub>-N<sub>F</sub> phase transitions can be seen in Fig. 6(b) and (c). The N<sub>X</sub>-N<sub>F</sub> transition is accompanied by a much smaller density change than that associated with the I-N transition, approximately 0.00075 g cm $^{-3}$ vs. 0.0031 g cm $^{-3}$  (Table 2). The size of this I–N density change is the largest of the investigated materials. The density deviation of the Nx-N<sub>F</sub> transition has been calculated at more than three times larger than that of the N-SmA transition. This suggests a significant structural reorganisation taking place through polar ordering when compared to that of the positional ordering of the N-SmA transition. It is interesting to note that M5 does not follow the loose positive correlation between density increase and transitional enthalpy (ESI,† Table S2), perhaps due to its composition as a mixture.

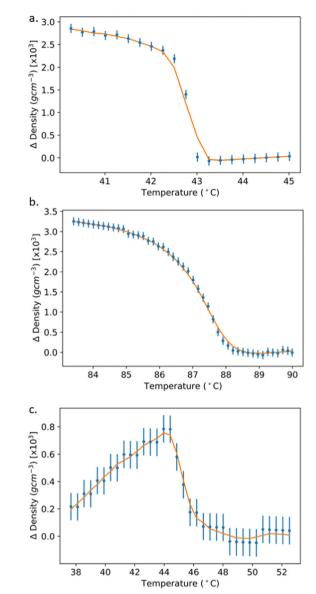
#### Implications of a large liquid crystal density

As the refractive index (or indices) of a material with induced dipoles depends significantly upon the density according to the Lorentz-Lorenz equation,<sup>46</sup> it is interesting to explore whether the anomalously high density and the highly polar nature of M5 (and potentially other NF materials) impacts their optical properties. We measured the refractive indices and birefringence of M5, finding the latter to be comparable to  $DIO^{47}$  (but smaller than RM734<sup>5,25</sup>); see Fig. 7. Due to the temperature limits of the experimental method employed in this work, measurements were performed a significant distance from the I-N transition. Therefore, a pretransitional monotonic reduction is not observed in the extraordinary,  $n_{\rm e}$ , and ordinary,  $n_0$ , refractive indices as the system is heated towards the isotropic phase. Here, we focus on  $n_{avg}$  as  $n_o$ ,  $n_e$ and  $\Delta n$  are more strongly linked to the order parameter. Fig. 7(c) shows the  $n_{\text{avg}}$  as calculated by eqn (6) for M5.

$$n_{\rm avg} = \sqrt{\frac{2n_{\rm o}^2 + n_{\rm e}^2}{3}}$$
(6)

We find that  $n_{avg}$  is smaller than the equivalent values for the standard nematogen 5CB, a material  $\approx$  30% less dense than M5.<sup>42</sup> Here we see direct evidence of contributions from the





**Fig. 6** The density deviation  $(\Delta \rho = \rho(T) - \rho^{\text{highT}}(T))$  through the I–N transition (a), (b) of (NCS)PCH6 and **M5** respectively. The behaviour in (a) and (b) is the result of a conventional nematic ordering taking place. (C) Shows how the density changes in **M5** as a result of polar ordering. Data are presented as scatter points whereas the solid line is a Savitzky–Golay filter<sup>41</sup> smoothing intended to show the trend of  $\Delta \rho$ .

permanent dipole moments of a highly polar system influencing the refractive indices of a material. The observations of **M5** and **5CB** where an increased density does not result in a larger  $n_{\rm avg}$  confirms that Lorentz–Lorenz equation does not adequately explain/should not be used in the explaining the behaviour of polar liquid crystal materials. To identify any relationship between  $n_{\rm avg}$  and spontaneous polarisation **M5** is compared with literature  $n_{\rm avg}$  data for the polar smectics **SCE8** ( $P_{\rm s} \approx 50$  nC cm<sup>-2</sup>)<sup>43</sup> and compounds **1** and **3** ( $P_{\rm s} \approx$ 150 nC cm<sup>-2</sup>) from ref. 44 and 45 (structures and phase sequences are given in ESI,† Section S6). There is a scattering of values with **M5** and its polarisation magnitude

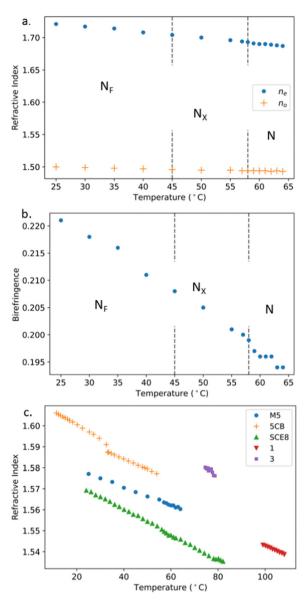


Fig. 7 (a) The  $n_0$  and  $n_e$  measurements of **M5** at 589 nm as the sample is cooled through its  $N-N_X-N_F$  phase sequence. (b) The resulting birefringence ( $\Delta n = n_e - n_o$ ) values of **M5**. (c) A comparison is made of  $n_{avg}$  for **M5** and **5CB**<sup>42</sup> as well as the polar smectics, **SCE8**<sup>43</sup> and compounds **1** and **3** from ref. 44 and 45.

of  $\approx 5.5 \ \mu\text{C cm}^{-2.48}$  resulting in a lower  $n_{\text{avg}}$  than the less polar compound 3 indicating there is no such relationship.

It is possible to use measurements of the density and spontaneous polarisation in a ferroelectric material, together with knowledge of the molecular dipole moment to deduce a value for the polar order parameter  $\langle P1 \rangle$ . In this case, as **M5** is a multicomponent material of unknown composition it was impossible to measure the polar order. However, as there is a clear indication from simulations that DIO also has a density of 1.3 g cm<sup>-3</sup>, and our measurements of **M5**, show that such a high value is indeed realistic, the approach was used for that pure material in approximating the polar order parameter. If we consider polarisation as the number density of electric dipoles

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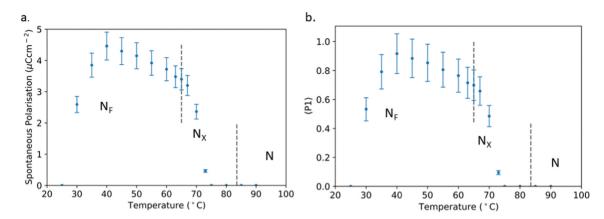


Fig. 8 (a) Spontaneous polarisation measurements of DIO (see Fig. 1 for DIO's structure and phase sequence) on cooling through its  $N_F - N_X - N$  phase sequence until crystallisation. Switching current response peaks are integrated to gives the magnitude of polarisation. (b) An approximation of  $\langle P1 \rangle$  for DIO from the contribution of average molecular dipole alignment to the polarisation.

per unit volume, then we can infer that a larger density will increase the measured polarisation. Following this, we have approximated the polar order parameter of DIO,  $\langle P1 \rangle$  through temperature-dependent spontaneous polarisation measurements (Fig. 8). We define  $\langle P1 \rangle$  in eqn (7).

$$\langle P1 \rangle = \frac{P_{\rm s}}{P_{\rm max}} \tag{7}$$

where  $P_{\rm s}$  is the spontaneous polarisation.  $P_{\rm max}$  is given in eqn (8)

$$P_{\max} = \frac{\mu_{\text{calc}} \rho N_{\text{A}}}{M} \tag{8}$$

where  $\mu_{\text{calc}}$  is the dipole moment calculated at the B3LYP/6-31G(d,p) level of DFT,<sup>49,50</sup> M is the molecular mass,  $\rho$  is the density (1.3 g cm<sup>-3</sup>) and  $N_A$  is Avogadro's number. Calculating  $\langle P1 \rangle$  from a  $P_s$  measurement approximates the average contribution of the molecular dipole alignment to the  $P_s$  where a bulk material with perfect polar order ( $\langle P1 \rangle = 1$ ) gives  $P_{\text{max}}$ .

As can be seen in Fig. 8, DIO's N phase produces zero measured polarisation values and thus possesses no polar order. On cooling through the  $N_{\rm X}$  phase, some average polar order begins to grow at and below 73 °C, resulting in net polarisation. Within the  $N_F$  phase the polarisation can be seen to increase until it saturates at a 4.5  $\mu C$  cm $^{-2} \pm 10\%$ . This produces a  $\langle P1 \rangle$  of 0.91  $\pm$  15% with the increased error accounting for any density changes due to a temperature change. As this material is being supercooled, the polarisation decreases past the saturation point until crystallisation and it no longer provides any measured response.

Recalculating with a conventional density assumption of 1 g cm<sup>-3</sup> results in an unphysical  $\langle P1 \rangle$  of 1.19. It may be of note that reliable density and polarisation measurements as well a realistic assumption for a maximum  $\langle P1 \rangle$  order parameter would provide a method for the experimental approximation of dipole moments. From a material design perspective, eqn (8) provides a means to estimate  $P_s$  directly from electronic structure calculations, although this does not mean that a given

material will generate and sustain polar ordering. Additionally, knowledge of the density of a typical  $N_F$  material enables the use of eqn (8) to check the physical validity of measured  $P_s$  values which, for a given material, are limited by the dipole moment and density.

## Conclusions

We have shown that the density of the  $N_F$  material **M5** is significantly larger than conventional liquid crystals, a finding that is in keeping with that determined in the atomistic MD simulations.<sup>25</sup> Here, we find that the  $N_F$  material **M5** possesses a much higher density (~1.3 g cm<sup>-3</sup>) than that of conventional nematic systems where the density is assumed (and found) to be ~1 g cm<sup>-3</sup>. We also observe experimentally an increase in density on entering the  $N_F$  phase which is comparable to that seen *in silico*.<sup>25</sup>

Refractive indices measurements of **M5** were used to examine the relationship between density, polarisation magnitude and  $n_{\text{avg}}$ . **M5**, while being  $\approx 30\%$  denser than **5CB**, possesses a lower  $n_{\text{avg}}$ . We believe this to be a result of **M5**'s highly polar nature. **M5** was compared to polar smectic liquid crystals with the polarisation magnitude possessing no direction correlation with  $n_{\text{avg}}$ . The  $\langle P1 \rangle$ of DIO is approximated from temperature-dependent spontaneous polarisation measurements. The calculation of  $\langle P1 \rangle$  includes the simulation supported and now experimentally verified density value for an N<sub>F</sub> material.

For classical apolar liquid crystals it is customary to assume a density of 1 g cm<sup>-3</sup> if required for measurement or analysis. In the case of N<sub>F</sub> materials, we suggest that, in the absence of data for a specific material, a value of 1.3 g cm<sup>-3</sup> be used.

## Data availability

The data collected in this work has been made publicly available at the University of Leeds Research Data Archive https:// doi.org/10.5518/1343.

#### Paper

## Conflicts of interest

There are no conflicts to declare.

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