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# Boron-doped scandium clusters $B@Sc_{n-1}^{-/0/+}$ with $n = 2-13$ : uncovering the smallest endohedrally doped cages†

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A comprehensive study using density functional theory with the PBE functional and the Def2-TZVP basis set investigates the pure  $Sc_n^{+/0/-}$  and doped  $Sc_{n-1}B^{+/0/-}$  clusters with  $n = 1-13$  in three charged states.  $B@Sc_6^{+/0/-}$  clusters emerge as the smallest doped cages identified so far, distinguished by their near-perfect octahedral geometry, with a B atom centrally enclosed in the  $Sc_6^{+/0/-}$  cages. Structural analysis reveals size-dependent trends, with a critical size at  $n = 6$ , marking a transition from exohedral to endohedral configuration, and a shift in the substitution-addition pattern of the B atom within the pure Sc host. Incorporation of a B atom induces electron redistribution, stabilizes high spin states and reduces energetic degeneracy. B-doping enhances the stability of the initial  $Sc_n^{+/0/-}$  clusters, showing a consistent preference for cationic isomers. A molecular orbital (MO) analysis provides a detailed explanation for the observed energy degeneracy among various stable spin states by delving into their electronic configurations.

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## 1. Introduction

There has been a remarkable surge of interest in small transition metal (TM) clusters, both in their pure form and when they are modified by other elements. This continuing enthusiasm is due not only to their well-known optical<sup>1</sup> and magnetic properties,<sup>2,3</sup> that are all size-dependent,<sup>1,4</sup> but also because of their versatility as catalysts in various chemical processes including the current challenges of renewable energy such as hydrogen storage<sup>5-8</sup> and CO<sub>2</sub> reduction.<sup>9,10</sup>

However, identification of the global ground state of a TM cluster, even for a lighter element such as scandium, presents

a considerable challenge for both theoretical and experimental approaches.<sup>11,12</sup> This difficulty arises from the presence of multiple quasi-degenerate isomers, each having a distinct spin magnetic moment, but which are closely matched in energy.

The scandium atom, despite its relatively simple electron configuration of [4s<sup>2</sup> 3d<sup>1</sup>], where it features just one unpaired 3d electron, reveals unexpected complexity in the spin states of scandium clusters (Sc<sub>n</sub>), even at very small sizes, such as the Sc<sub>2</sub> dimer,<sup>11,13-21</sup> and Sc<sub>3</sub> trimer.<sup>14,22</sup> This complexity becomes more pronounced as the number of flexible open-shell 3d electrons increases with the growing size of scandium clusters, leading to multiple high-spin states possessing different geometric structures but similar energy levels.<sup>18</sup>

In the field of atomic clusters, one effective strategy to potentially enhance or modify their properties, or to address inherent challenges, is the doping, wherein other elements are introduced into the cluster.<sup>23,24</sup> Doping can fundamentally influence the properties and behavior of nanoclusters, making it a valuable technique for customizing their characteristics to suit some specific applications or to overcome intrinsic limitations of the pure clusters.<sup>23,25</sup> For TM clusters, a doping can involve the incorporation of both metal and non-metal elements. Concerning the scandium clusters, as far as we know, only a limited number of studies, both experimental and theoretical, have been reported on pure and doped scandium clusters. Such a relative lack of investigation implies an insufficient understanding on this class of atomic clusters.

In previous studies, the potential applications of scandium-boron combinations have been explored, specifically in the

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† Electronic supplementary information (ESI) available: (i) The structures, multiplicities and relative energies (rE, kcal mol<sup>-1</sup>) of the lowest-lying  $Sc_n^{+/0/-}$  ( $n = 2-13$ ), (ii) the molecular orbital (MO) diagram of the  $Sc_6^{+/0/-}$ ,  $B@Sc_6^{+/0/-}$  and  $Sc_{11}^{+/0/-}$  at different spin states, and (iii) calculated density of states (DOS) for the lowest-lying neutral clusters of the  $Sc_6$ ,  $Sc_7$ ,  $B@Sc_6$  and  $B@Sc_7$  isomers. (iv) Coordinates of the lowest-lying  $Sc_n^{+/0/-}$  and  $Sc_{n-1}B^{+/0/-}$  ( $n = 2-13$ ) clusters. See DOI: <https://doi.org/10.1039/d4ra06541g>



form of scandium-doped boron clusters, with a particular emphasis on their possible use in hydrogen storage.<sup>8,26</sup> Furthermore, inclusion of scandium as a dopant induces a remarkable ability to stabilize the geometric configurations with high symmetry of boron cages. The structural arrangement of Sc-doped boron clusters  $\text{Sc}@\text{B}_n^{0/-}$  with  $n$  going from 10 to 20 undergoes a remarkable transition from a half-sandwich configuration to a drum-like shape, with a central location of the scandium atom.<sup>27</sup> These doped clusters usually adopt a cage-like topology. An intriguing discovery was the identification of the neutral  $\text{Sc}@\text{B}_{13}$  cluster which was assigned as a magic cluster.<sup>27</sup> Additionally, a larger and nearly perfect boron box  $\text{Sc}_2@\text{B}_{27}^+$  was characterized by its distinctive triple-ring tubular shape featuring a high  $D_{9h}$  point group symmetry.<sup>28</sup> This tubular structure is formed through an antiprism interconnection of three  $\text{B}_9$  strings, and the resulting box is capped by an Sc–Sc dimer, vertically placed at the center along the axis of the tubular box.<sup>28</sup>

In this context, the concept of introducing an inverse doping by placing a boron atom inside a  $\text{Sc}_n$  cage constitutes a legitimate idea. This raises the questions as to whether the boron dopant could occupy the interior of the  $\text{Sc}_n$  cage preferentially, and whether such an endohedral arrangement can thermodynamically stabilize the  $\text{Sc}_n$  cage. Given the number of valent electrons [ $2s^2$   $2p^1$ ] in a boron atom is quite similar to that of [ $4s^2$   $3d^1$ ] in a scandium atom, some intriguing properties are expected to emerge, reminiscent of the cases of the isovalent  $\text{B}_x@\text{Al}_y$  (ref. 29–31) and  $\text{Al}_x@\text{Sc}_y$  clusters.<sup>25,32,33</sup>

With the aim to delve deeper into this concept and identify the specific conditions under which boron atom would preferentially occupy a position inside a scandium cage, along with the necessary size criteria, we set out to carry out an extensive theoretical and computational study on the singly boron doped scandium clusters. Given that previous studies of Sajjad *et al.*, Bhunia *et al.* and Li *et al.* only theoretically investigated the neutral  $\text{Sc}_n$  clusters using less accurate quantum chemical methods by combining DFT functional with small basis sets such as CEP-121 G, LANL2DZ, and LANL2MB,<sup>19,20,34</sup> except for the dimer  $\text{Sc}_2$  and trimer  $\text{Sc}_3$ , we set out to provide in the present study a more comprehensive re-investigation. It focuses on scandium clusters  $\text{Sc}_n$  with  $n = 2$ –13 with across the cationic, neutral, and anionic charge states, utilizing a higher-level quantum chemical method. Subsequently, our study advances to determine the structures of singly boron-doped scandium clusters  $\text{Sc}_{n-1}\text{B}^{+/-}$  having the same size  $n = 2$ –13, also in three different charge states. This comprehensive investigation also takes the electronic and magnetic properties into account, as well as the growth patterns of both pure and boron-doped Sc clusters.

## 2. Computational methods

All standard electronic structure calculations are performed using the Gaussian 16 set of programs.<sup>35</sup> In previous investigations encompassing both pure scandium and boron systems, as well as mixed scandium-boron clusters, the utilization of the density functionals such as the PBE,<sup>36,37</sup> B3PW91,<sup>38,39</sup> BP86,<sup>40,41</sup>

TPSSh<sup>42</sup> and M05<sup>43,44</sup> has yielded consistent and appropriate results.<sup>8,11,19,20,28,34,45–50</sup> To maintain a consistency to enable meaningful comparisons with previous results, we now consider these five functionals in conjunction with the Def2-TZVP basis set<sup>51</sup> for the present study.

Preliminarily, we conduct a methods benchmark by re-evaluating the electronic and spin state of the  $\text{Sc}_3$  trimer. We thus employ the five functionals considered including PBE, B3PW91, BP86, TPSSh and M05 along with the Def2-TZVP basis set, followed by a comparison with the available experimental data.<sup>14</sup> Subsequently, we intend to undertake a comprehensive search for structures of a series of small  $\text{Sc}_n$  clusters and  $\text{Sc}_{n-1}\text{B}$  with  $n$  going from 2 to 13 across three charge states. For this extensive exploration, we use the PBE functional in conjunction with the Def2-TZVP basis set, as this functional has consistently demonstrated results in good agreement with experimental data as compared to the other functionals employed in this study (discussed in the next section “Some Benchmark Calculations on the  $\text{Sc}_3$  Trimer”).

In our global search procedure for the global energy minima, we employ two distinct methodologies. Firstly, we utilize an upgraded stochastic algorithm, building upon the previously reported random kick procedure,<sup>52</sup> to systematically generate diverse structures for both  $\text{Sc}_n^{+/-}$  and  $\text{Sc}_{n-1}\text{B}^{+/-}$  clusters. Simultaneously, we manually construct initial structures for the  $\text{Sc}_{n-1}\text{B}^{+/-}$  by strategically introducing a B atom into different positions within the local minimum structures of both neutral and charged states of the  $\text{Sc}_{n-1}^{+/-}$  species.<sup>18,34,45</sup> The process also involves a substitution of the B atoms with Sc atoms, taking inspiration from previous studies on the  $\text{B}_n\text{Sc}^{+/-}$  counterparts<sup>26</sup> and incorporating replacement of B or Sc atoms into the patterns observed in the Al–Sc systems<sup>25,32,33</sup> as well as  $\text{Al}_n\text{B}$  systems<sup>29,30,53,54</sup> taking a similar number of valent electrons into account. This comprehensive and intensive search approach ensures a thorough exploration of the potential energy landscapes for the clusters considered in various charge states.

These initial structures generated are then subjected to geometry optimizations in different multiplicities using the PBE functional in conjunction with the small LANL2DZ basis set. Subsequently, the local energy minima identified from both search approaches, with relative energies of <5 eV with respect to the lowest-lying minimum of each size and charge, are subjected to a re-optimization using the same functional but with the larger Def2-TZVP basis set. Harmonic vibrational frequencies are then calculated at the same level to identify equilibrium geometries and evaluate their zero-point energy (ZPE) corrections. This process allows a reliable identification to be carried out for the structural and energetic characteristics of the lowest-lying isomers.

To further analyze the properties, the natural bond orbital (NBO) analysis is conducted using the NBO 5.0 program.<sup>55</sup> This aims to emphasize the electronic populations, and, consequently, the chemical bonding and magnetic properties, allowing for a detailed examination of the charge transfer and electron contribution. Besides, the relative stability of different geometries and spin states of the studied clusters are rationalized using the jellium shell model (JSM).<sup>56</sup> This popular model



was successful in providing some simple but reasonable interpretations for stability patterns observed in other similar atomic clusters.<sup>52,57</sup>

### 3. Results and discussion

#### 3.1 Some benchmark calculations on the $\text{Sc}_3$ trimer

As mentioned above, debates have arisen, both experimentally and theoretically, concerning the most stable spin state of the neutral  $\text{Sc}_2$  cluster. Calculated results disagree with each other on the ground state of the dimer. While CASPT2 computations carried out in 2008<sup>21</sup> suggested that  $\text{Sc}_2$  has a triplet  ${}^3\Sigma_u^-$  ground state, the following results using MRCI(Q) and multi-reference perturbation theory NEVPT3 methods reported in 2010<sup>16,17</sup> pointed out a quintet  ${}^5\Sigma_u^-$  ground state. Results obtained in 2017<sup>19</sup> from coupled-cluster theory (U)CCSD(T) computations revealed a closed-shell  ${}^1\Sigma_g^+$  ground state which was not seriously considered in previous theoretical studies. On the other hand, most DFT results obtained using several functionals converged to a quintet  ${}^5\Sigma_u^-$  ground state. Such a discrepancy is reflected by the inherent difficulty for treatment of transition metal dimers by quantum chemical methods. In fact, the debate over the ground state of the chromium dimer  $\text{Cr}_2$  lasted several decades.<sup>58</sup> In this context the dimer is not suitable for a benchmarking of DFT functionals for Sc clusters. In this section, our objective is to present an overview and assessment of the benchmark calculations by considering the global energy, spin state, and vibrational frequencies of the neutral  $\text{Sc}_3$  trimer. The calculations involve the use of several density functionals including the PBE, B3PW91, BP86, TPSSh, and M05, along with the Def2-TZVP basis set.

The experimental resonance Raman spectrum of  $\text{Sc}_3$  trimer was well documented.<sup>14</sup> The trimer is characterized as a near-equilateral triangle, demonstrating a symmetric stretching vibrational frequency of  $\sim 248 \text{ cm}^{-1}$  and two vibrational frequencies of nearly degenerate asymmetric stretch-bends, both around  $150 \text{ cm}^{-1}$ . Furthermore, the ground state of the  $\text{Sc}_3$  trimer has been assigned by a  ${}^2\text{A}_1$  electron state based on a finding employed the electron paramagnetic resonance (ESR) spectroscopy's technique.<sup>59</sup>

A previous theoretical study using CASSCF followed by contracted CI calculations reported the ground state of  $\text{Sc}_3$  to be

${}^2\text{A}_2''$ .<sup>60</sup> However, this finding did not align with the ESR experiment results, and the symmetric stretching frequency ( $513 \text{ cm}^{-1}$ ) was significantly different from the Raman experimental data. Subsequent studies demonstrated that the BP86 functional, in conjunction with different basis sets, produced reasonable results, showing agreement with the  ${}^2\text{A}_1$  ground state and providing vibrational frequencies close to the experimental values.<sup>50,61,62</sup>

When combined with the Def2-TZVP basis set, all functionals used in this study yield results consistent with the experimental findings, confirming the ground state of the  $\text{Sc}_3$  trimer as  ${}^2\text{A}_1$ . Additionally, across the different functionals, the  $\text{Sc}_3$  trimer at its  ${}^2\text{A}_1$  state exhibits the same electron configuration, with an unpaired electron occupying the 2S molecular orbital (MO) (cf. Table S1†), indicating that the choice of a density functional induces little impact on the electronic structure. However, the results presented in Table 1 reveal that calculations employing the PBE functional provide better agreement with experiments compared to the other functionals used. For the calculated  $\text{Sc}_3$  trimer, only the vibrations at the  ${}^2\text{A}_1$  electronic state employing the PBE functional yield signals closely resembling the experimental findings, with a pair of degenerate vibrations at  $\sim 140 \text{ cm}^{-1}$  ( $\sim 140$  and  $\sim 145 \text{ cm}^{-1}$  when relaxing the symmetry) describing the nearly degenerate asymmetric signals at around  $145$  and  $150 \text{ cm}^{-1}$ , and a symmetric vibration at  $\sim 260 \text{ cm}^{-1}$  ( $\sim 268 \text{ cm}^{-1}$  when relaxing the symmetry) corresponding to the  $\sim 250 \text{ cm}^{-1}$  observed in the experiment.

Given the relatively accurate result in vibrational frequencies for the  $\text{Sc}_3$  trimer, the PBE functional is thus further utilized in this study.

#### 3.2 Structural evolution and the smallest size of exohedral–endostructural transition

For the pure  $\text{Sc}_n^{+/0/-}$  and doped  $\text{Sc}_{n-1}\text{B}^{+/0/-}$  ( $n = 2-13$ ) clusters, our selection process focuses on the lowest-lying isomers with relative energies closely aligned to the most stable structure with a difference of  $\sim 12 \text{ kcal mol}^{-1}$  ( $\sim 0.5 \text{ eV}$ ) in relative energy. This approach is necessary due to the abundance of local minima on the potential energy surface, along with the presence of energetically degenerate isomers in both

**Table 1** Relative energy (rE), electronic state (S), and Raman frequencies (Freq) of the  $\text{Sc}_3$  trimer computed using the PBE, B3PW91, PB86, TPSSh and M05 functionals with the def2-TZVP basis set

Functional	PBE			B3PW91			PB86			TPSSh			M05		
	${}^2\text{A}_1'$	${}^4\text{A}'$	${}^6\text{A}'$	${}^2\text{A}_1'$	${}^4\text{B}_2$	${}^6\text{A}_1$	${}^2\text{A}_1'$	${}^4\text{A}_1$	${}^6\text{A}'$	${}^2\text{A}_1'$	${}^4\text{B}_2$	${}^6\text{A}'$	${}^2\text{A}_1'$	${}^4\text{A}_2$	${}^6\text{A}'$
S <sup>b</sup>	${}^2\text{A}_1'$	${}^4\text{A}'$	${}^6\text{A}'$	${}^2\text{A}_1'$	${}^4\text{B}_2$	${}^6\text{A}_1$	${}^2\text{A}_1'$	${}^4\text{A}_1$	${}^6\text{A}'$	${}^2\text{A}_1'$	${}^4\text{B}_2$	${}^6\text{A}'$	${}^2\text{A}_1'$	${}^4\text{A}_2$	${}^6\text{A}'$
rE (kcal mol <sup>-1</sup> )	0.0	5.3	6.4	0.0	2.5	3.5	0.0	13.6	6.5	0.0	3.0	5.2	0.0	16.2	24.8
Freq (cm <sup>-1</sup> )	138	145	66	192	131	131	133	105	65.1	102	132	105	157	149	112
	138	181	185	192	142	146	133	232	186	102	141	136	157	250	190
	264	209	214	283	248	254	263	255	208	282	249	256	290	263	280
Expt <sup>a</sup> (cm <sup>-1</sup> )	145, 151, 248 (ref. 14)														

<sup>a</sup> Results are compared with the experimental Raman signals (Exp) of the  $\text{Sc}_3$  trimer reported in ref. 14. <sup>b</sup> Due to geometric distortions, several optimized structures do not have any symmetry; the others have low symmetry point group, but it is rather confusing to assign the symmetry of their electronic state. For the sake of simplicity, we consider the lowest-lying state in each multiplicity.



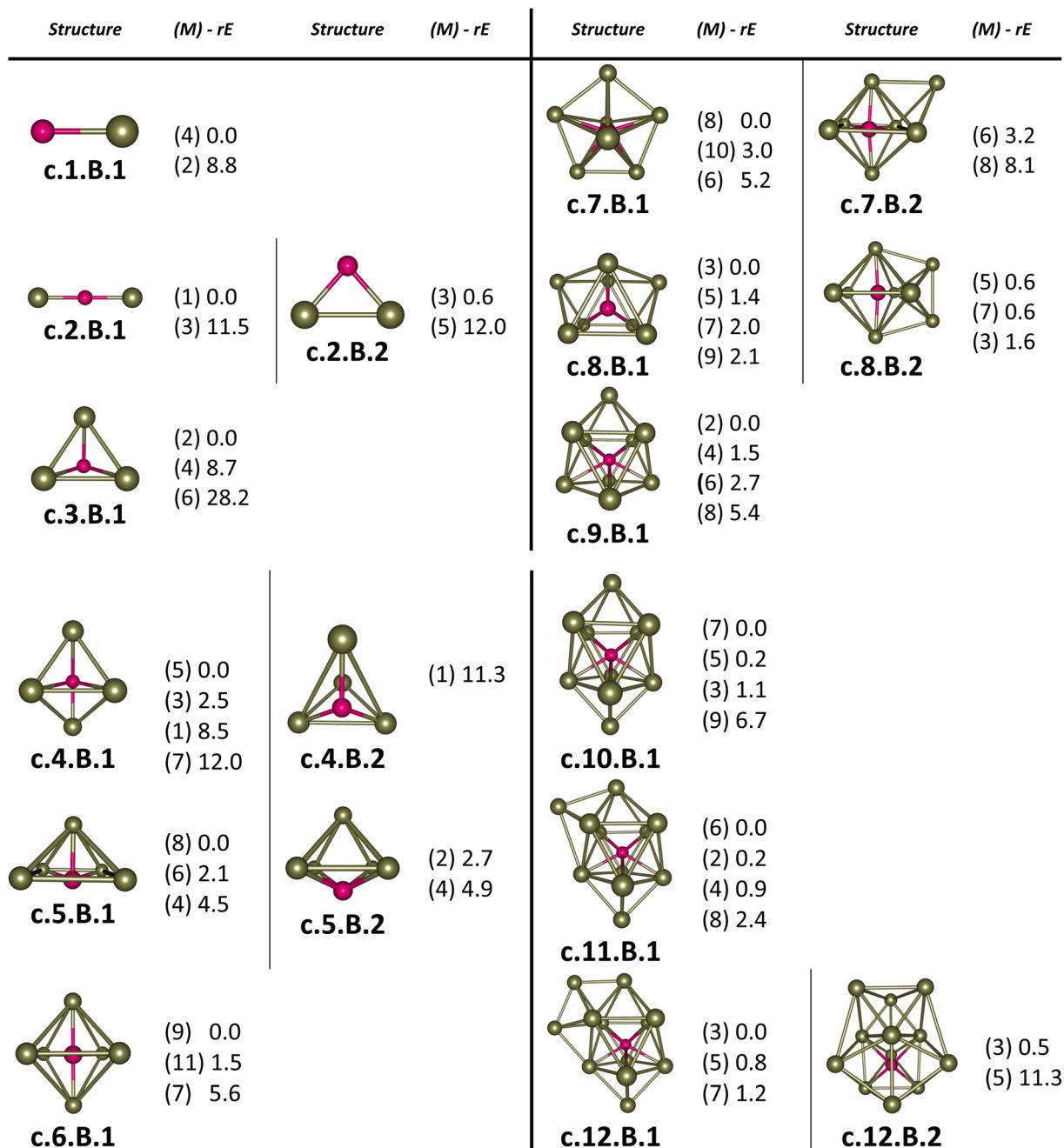


Fig. 1 Structures, multiplicities (M, in bracket) and relative energies (rE, kcal mol<sup>-1</sup>) of the lowest-lying cationic  $\text{Sc}_{n-1}\text{B}^+$  ( $n = 2-13$ ) clusters calculated using the PBE functional with the def2-TZVP basis set.

structures and spin states for each cluster size. The shapes, spin states, and relative energies of the pure  $\text{Sc}_n^{+/0/-}$  in three charge states are represented in Fig. S1 (S stands for the ESI file).<sup>†</sup> The shapes, spin states, and relative energies of the boron doped  $\text{Sc}_{n-1}\text{B}^{+/0/-}$  structures are depicted in Fig. 1-3, corresponding to the cationic, neutral and anionic charges, respectively.

In our labeling convention, the x.N.Z.y notation is employed for pure  $\text{Sc}_n^{+/0/-}$  isomers, where x = c, a, and n represent cationic, anionic and neutral isomers, respectively; N denotes the number of Sc atoms, and Z = A designates pure  $\text{Sc}_n^{+/0/-}$

clusters. The subscript y = 1, 2, 3, etc... indicates isomers with increasing relative energy. For example, **c.5.A.1** consistently identifies the most stable isomer of the  $\text{Sc}_5^+$  cation.

Similarly, the x.M.Z.y label is utilized for doped  $\text{Sc}_{n-1}\text{B}^{+/0/-}$  isomers in which x = a, c and n indicate the anionic, cationic and neutral isomers, respectively. M = N-1 with N = 2-13 denotes the number of Sc atoms, and Z = B corresponds to the series of doped  $\text{Sc}_{n-1}\text{B}^{+/0/-}$  clusters. Again, the subscript y = 1, 2, 3, etc... stands for isomers with increasing relative energy. Accordingly, **c.5.B.1** consistently denotes the most stable isomer of the  $\text{Sc}_5\text{B}^+$  cation.



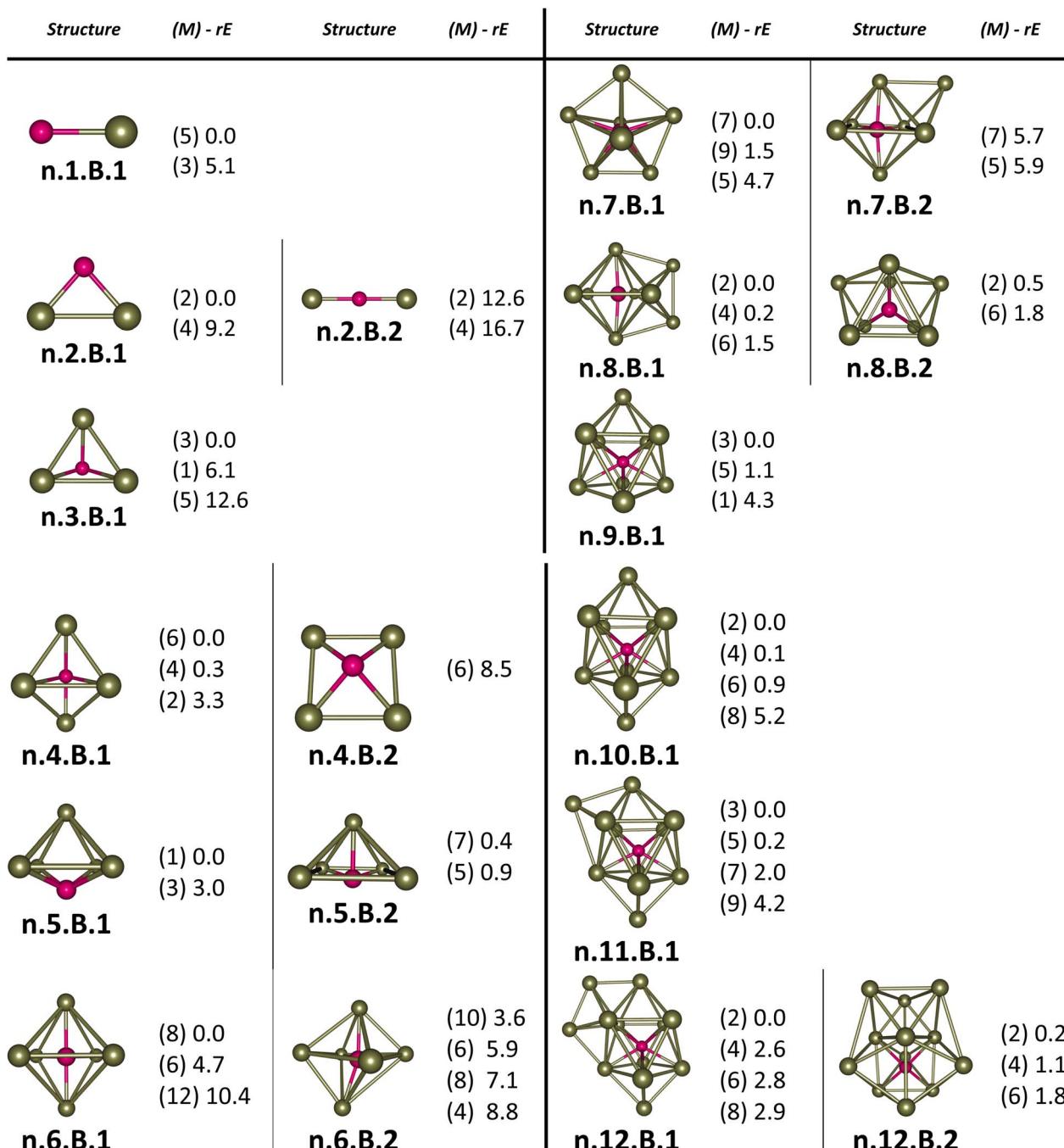


Fig. 2 Structures, multiplicities (M, in bracket) and relative energies (rE, kcal mol<sup>-1</sup>) of the lowest-lying neutral  $\text{Sc}_{n-1}\text{B}$  ( $n = 2-13$ ) clusters calculated using the PBE functional with the def2-TZVP basis set.

The critical size of the  $\text{Sc}_{n-1}\text{B}^{+/0/-}$  clusters with  $n = 2-11$  occurs at  $n = 6$ , marking the point at which an exohedral-endohedral rearrangement takes place, accompanied by a transition in the substitution-addition trend of the B atom. Across all three charge states considered, particularly for smaller sizes, those are characterized by very small number of Sc atoms having shapes such as a line, a triangle, a tetrahedron and a triangular bipyramidal, respectively, corresponding to the doped  $\text{Sc}_{n-1}\text{B}^{+/0/-}$  clusters with  $n = 2-6$ . A distinct preference emerges for the exohedral trend of boron substitution into the corresponding

original shapes of  $\text{Sc}_n^{+/0/-}$  ( $n = 2-6$ ) clusters. This trend undergoes a notable shift, however, as the cluster size increases, accompanied with the expansion of Sc<sub>n</sub> cage, favoring an endohedral trend of boron addition into the larger  $\text{Sc}_n^{+/0/-}$  ( $n = 6-10$ ) clusters, as illustrated in Fig. 4. The trend of addition is initiated with a B atom attaching to the bottom face of a distorted triangular bipyramidal composed of the  $\text{Sc}_5^{+/0/-}$  cages. This results in the formation of a nearly pyramidal structure in the  $\text{B}@\text{Sc}_5^{+/0/-}$  clusters in which the B atom is positioned at the center, slightly angled downward from the square bottom surface.



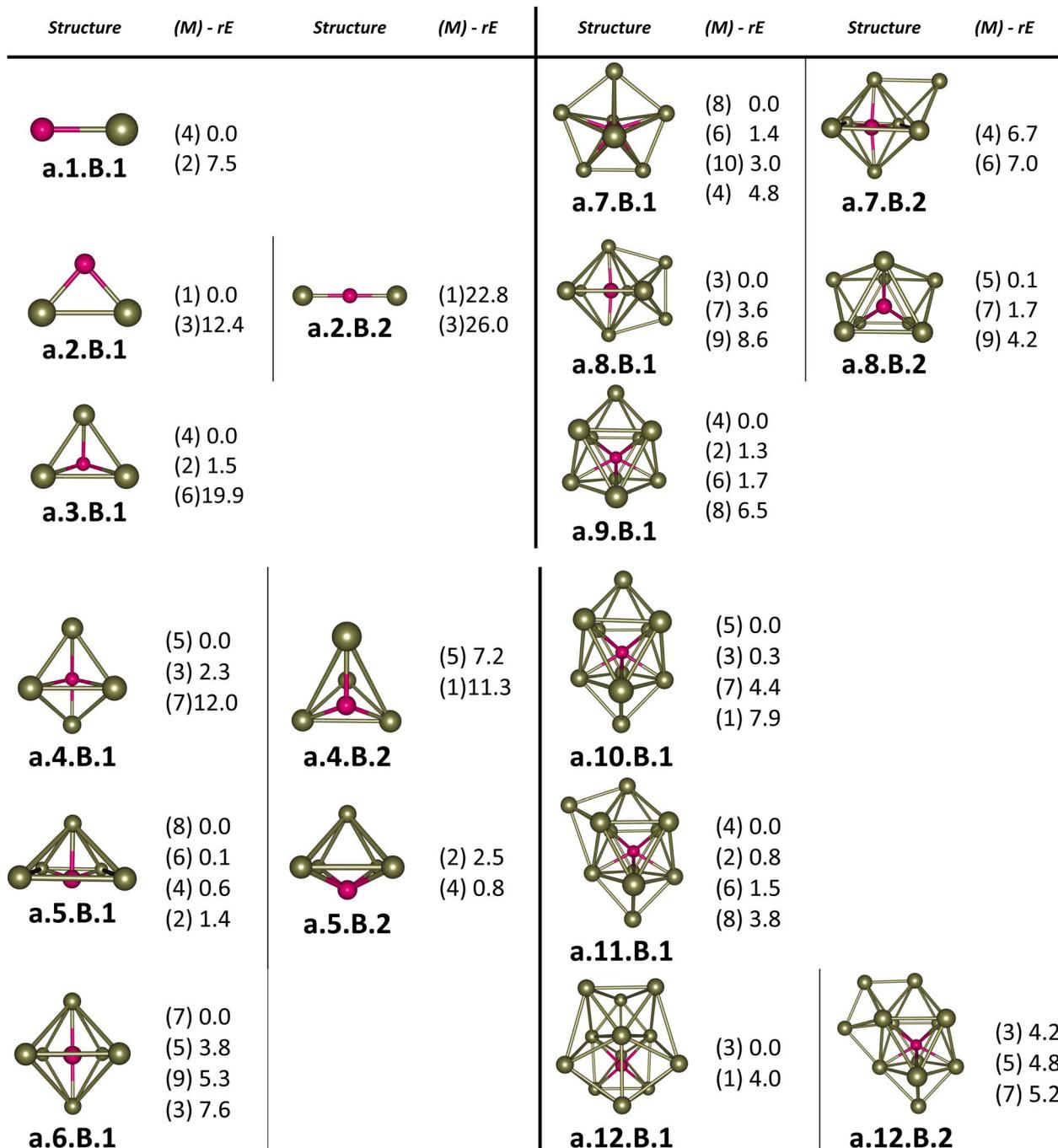
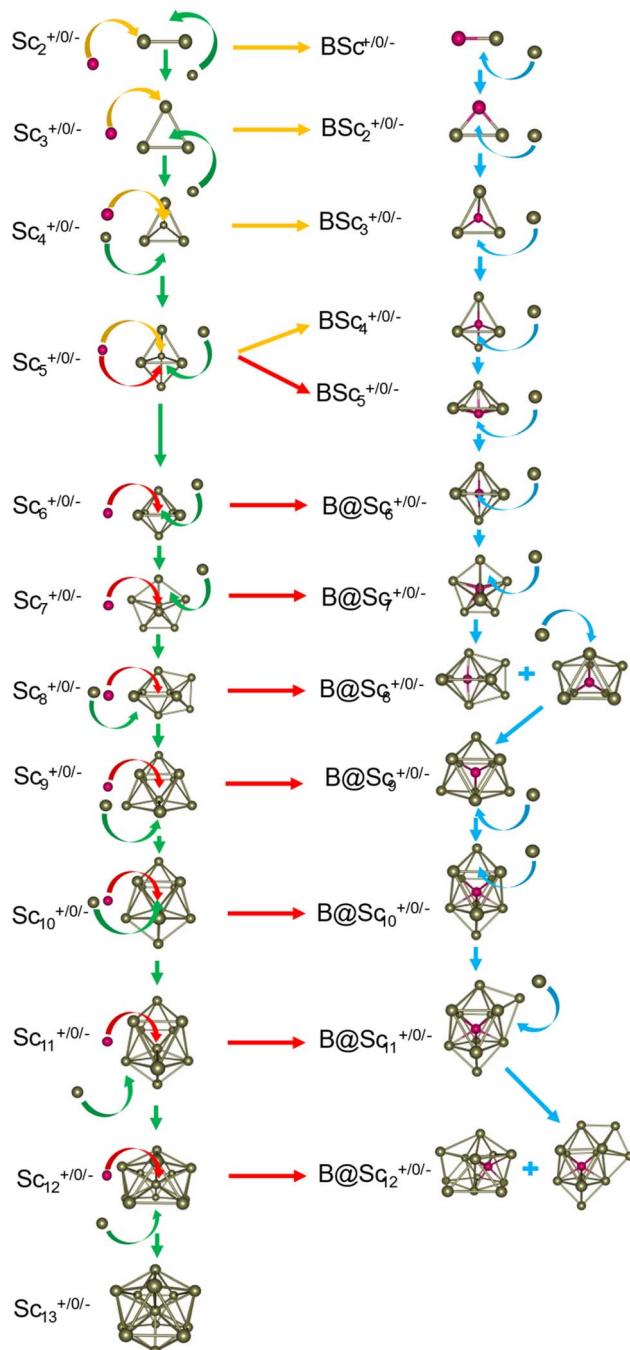


Fig. 3 Structures, multiplicities (M, in bracket) and relative energies (rE, kcal mol<sup>-1</sup>) of the lowest-lying anionic  $\text{Sc}_{n-1}\text{B}^-$  ( $n = 2-13$ ) clusters calculated using the PBE functional with the def2-TZVP basis set.

Particularly striking is the stable and aesthetically pleasing lowest-lying structure of the  $\text{B}@\text{Sc}_6^{+0/-}$  clusters, standing out as the smallest doped cage observed thus far.<sup>53,57,63</sup> Noteworthy for their nearly perfect octahedral shape, each of these clusters encapsulates a B atom at its centre within the confined space of a  $\text{Sc}_6^{+0/-}$  cage. The specific size of the  $\text{Sc}_6^{+0/-}$  cage provides snugly sufficient space, allowing a B atom to be centrally positioned, forming six B-Sc bonds, and enhancing the condensation of the initially loosely structured  $\text{Sc}_6^{+0/-}$  cage (cf. Fig. 1–4

and S1 of the ESI file†). In fact, the doped B atom connects six Sc atoms together giving rise to six additional B-Sc bonds, thus stabilizing the initial  $\text{Sc}_6^{+0/-}$  configurations and thereby solidifying the overall structure (cf. the next section “Thermodynamic stability”).

In line with the prevailing trend of additive design, the  $\text{B}@\text{Sc}_7^{+0/-}$  enclosures also showcase a visually appealing structure, highlighting a central B atom positioned within the pentagonal bipyramidal  $\text{Sc}_7^{+0/-}$  cage, revealing almost a  $C_{2v}$



**Fig. 4** Structural evolution of the pure  $\text{Sc}_n^{+/-}$  and doped  $\text{Sc}_{n-1}\text{B}^{+/-}$  clusters with  $n$  going from 2 to 13. Green and blue arrows illustrate the stepwise structural changes by adding one Sc atom in the  $\text{Sc}_n^{+/-}$  and  $\text{Sc}_{n-1}\text{B}^{+/-}$  clusters, respectively. Yellow and red arrows present trends in substitution and addition of B into pure Sc clusters, respectively.

symmetry. However, given their rather large size with respect to the modest atomic radius of B, the  $\text{Sc}_7^{+/-}$  crates are relatively spacious for accommodating the B atom, leading to their loosely distorted structures.

As the size of the crates increases, they progressively experience significant expansion, resulting in a loosening that

prompts structural reorganization for enhanced condensation and effective bonding. For the next  $\text{B}@\text{Sc}_8^{+/-}$ , a notable energetic degeneracy is observed between the two most stable geometric configurations (*cf.* Fig. 1–4). In the first, the B atom occupies the central position of the octahedron belonging to the adjacently double face-capped octahedral  $\text{Sc}_8^{+/-}$  cages. In the second configuration, the B atom centrally resides in a  $\text{Sc}_8$  rectangular antiprism. Such a rectangular antiprism  $\text{B}@\text{Sc}_8^{+/-}$ , in and of itself, serves as the basic building block for larger sizes, highlighting its own structural significance.

Building upon the structural block of the rectangular antiprism observed in  $\text{B}@\text{Sc}_8^{+/-}$ , the most stable configurations of  $\text{B}@\text{Sc}_9^{+/-}$  and  $\text{B}@\text{Sc}_{10}^{+/-}$  clusters integrate one and two additional Sc atoms onto the rectangular faces of the antiprism, respectively (*cf.* Fig. 4). The B atom consistently serves as a central point of connection, bringing the outer Sc atoms together. Such a cohesive effect results in the structures of  $\text{B}@\text{Sc}_9^{+/-}$  and  $\text{B}@\text{Sc}_{10}^{+/-}$  that are fixed and much more compact than the initially loosely distorted  $\text{Sc}_9^{+/-}$  and  $\text{Sc}_{10}^{+/-}$  cages.

It is noteworthy that the structures of  $\text{B}@\text{Sc}_{10}^{+/-}$  and  $\text{Sc}_{11}^{+/-}$  are quite similar to each other, featuring a quasi  $D_{4d}$  gyroelongated square bipyramid with a central connection point formed by a B and Sc atom, respectively.

However, in going beyond  $n = 11$ , the doping a B atom at a central point of the Sc cage to connect and shape the outer Sc cage is no longer effective. This is because the  $\text{Sc}_n^{+/-}$  cage has reached a sufficient size, and a Sc atom, with its larger radius, becomes more efficient in playing the central connecting role with other outer Sc atoms as compared to the smaller-radius B atom.

In contrast to boron-doped  $\text{B}@\text{Al}_{12}^{0/-}$  those preserve the icosahedral shape of the  $\text{Al}_{13}$  cluster,<sup>29,54</sup> their isovalent  $\text{B}@\text{Sc}_{12}^{+/-}$  isomers cannot retain the icosahedron of the  $\text{Sc}_{13}$  cluster. For larger sizes with  $n = 12$  and 13, the  $\text{Sc}_{n-1}\text{B}^{+/-}$  clusters shift away from the earlier addition as well as substitution rules into the  $\text{Sc}_n^{+/-}$  host. Instead, a gradual addition of Sc atoms onto the outer faces of the  $\text{B}@\text{Sc}_{10}^{+/-}$  is observed. Meanwhile,  $\text{Sc}_{12}^{+/-}$  undergoes a rearrangement into a mono-capped pentagonal antiprism, followed by a well-known icosahedron of the  $\text{Sc}_{13}^{+/-}$  in which a Sc atom plays the role of an endohedral stabilizing center.

### 3.3 Energetic degeneracy and high magnetic moment

As the size expands, the intricacies of energetic degeneracy become more pronounced,<sup>18</sup> that can be attributed to two primary factors. On the one hand, energetic degeneracy is triggered by a geometric competition for the global minimum, a consequence of the inherent flexibility and fluxionality within the clusters. With increasing size, numerous structural rearrangements and transformations occur, resulting in multiple energetic degeneracy.

On the other hand, the increasing number of unpaired electrons invariably induces energetic degeneracy among the high spin states. These electrons, closely packed in energy, particularly the 3d electrons, coupled with a strong Jahn–Teller effect, contribute to the small differences or even overlap in energy levels of the 1F, 2D, and even 2P shell orbitals, further



complicating the energy landscape. In this complex scenario, the shapes of these shell orbitals become distorted due to the merging of different orbital types, disrupting molecular symmetry and making them difficult to be identified. Hereafter, we refer to the range encompassing these intricate energy levels as the “mixed band”. Within the mixed band, the HOMO-LUMO gap, or the HOMO-SOMO gap, is characterized with a very small energy, facilitating an easier traversal of electrons which continues until the mixed band becomes unoccupied. As a result, the HOMO level now shifts to the orbitals located at significantly lower energy levels, such as 2S, 1P, or 1D orbitals,

ultimately establishing a notably large HOMO-LUMO (HOMO-SOMO) gap.

The energy degeneracy of the pure  $\text{Sc}_n^{+/0/-}$  tends to escalate as its size  $n$  increases and attains the pivotal magic number, namely  $n = 13$ . At this critical size, the  $\text{Sc}_{13}^{+/0/-}$  isomers enjoy a synergistic interplay between electronic and geometric structures within the cluster. This synergy culminates in the emergence of both an icosahedral structure and very high spin electronic states, with a  $^{19}\text{A}_1$  state for the cationic, a  $^{20}\text{A}$  state for the neutral, and a  $^{19}\text{B}_{3u}$  state for the anionic  $\text{Sc}_{13}$  isomer. These isomers are characterized by their electron shells in cationic,

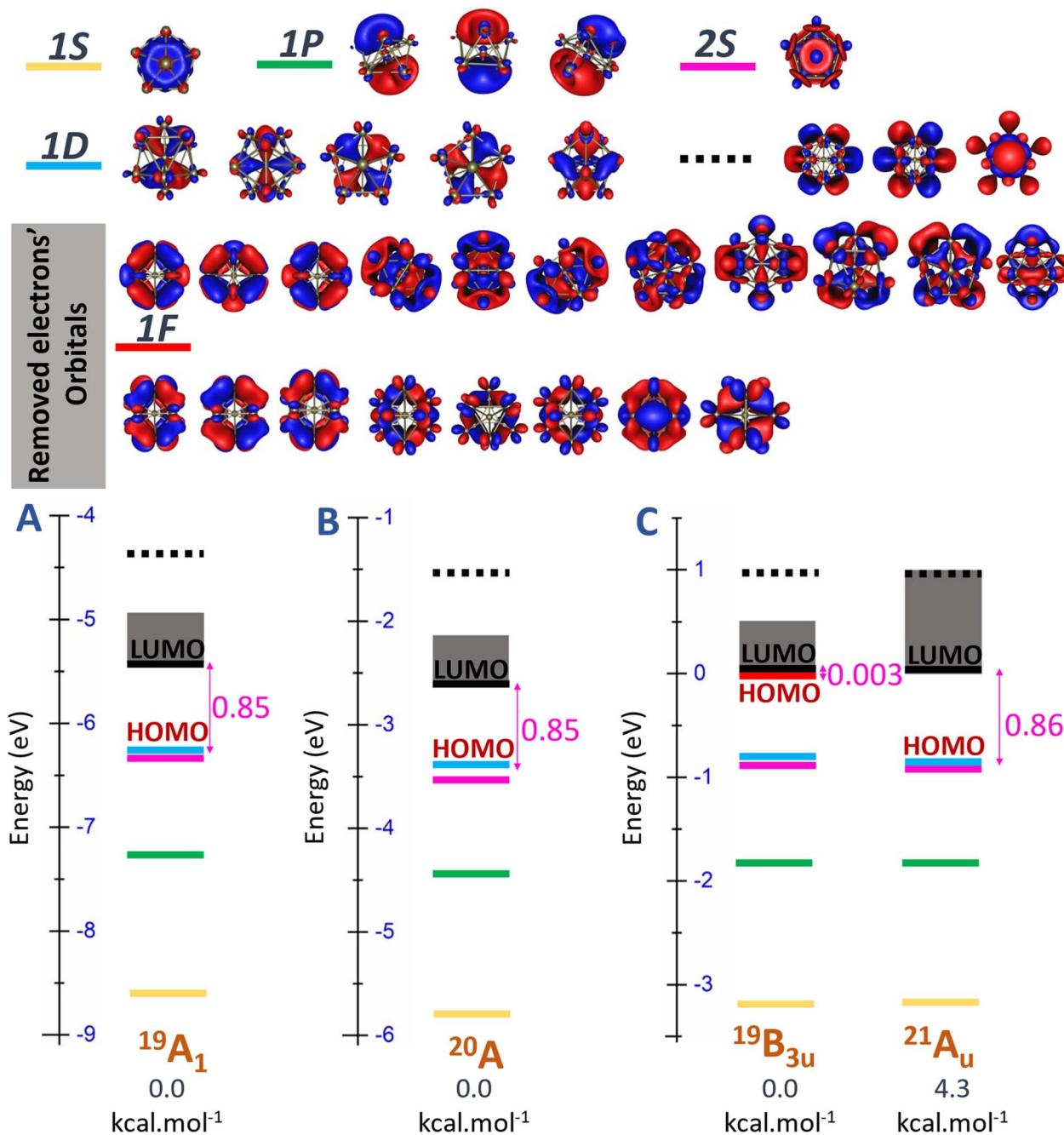


Fig. 5 Molecular orbital (MO) diagram on the beta side of (A) cationic  $\text{Sc}_{13}^+$ , (B) neutral  $\text{Sc}_{13}$ , and (C) anionic  $\text{Sc}_{13}^-$  clusters, using the PBE/Def2-TZVP theory method.

neutral, and anionic states expressed as  $[1S^21P^62S^21D^{10}\text{SOMO}^{18}]$ ,  $[1S^21P^62S^21D^{10}\text{SOMO}^{19}]$  and  $[1S^21P^62S^21D^{10}2F^2\text{SOMO}^{18}]$ , respectively.

In Fig. 5, a uniform energy level pattern is depicted among these isomers, emphasizing three key regions: the core levels associated with the  $[1S^21P^62S^21D^{10}]$  electron configuration, the [mixed band] comprising 19 closely spaced energy levels, and the “other” levels, which extend beyond the mixed band, exhibiting distinct orbital shapes and significantly higher energy levels—approximately 0.6 eV above those in the mixed band. On the beta side of these isomers, both cationic and neutral isomers exhibit a HOMO level of  $1D_{xy}$  and a LUMO level corresponding to the first level of 1F in the mixed band, with a HOMO–LUMO gap of approximately 0.85 eV.

However, the anionic  $\text{Sc}_{13}^-$  isomer, having 40 valence electrons, behaves differently. Here, the beta HOMO aligns with the first level of the [mixed band] rather than with the 1D level, while the LUMO aligns with the second level, creating a  $^{19}\text{B}_{3u}$  state with a nearly zero HOMO–LUMO gap, instead of maintaining the  $^{21}\text{A}_u$  state with an empty beta [mix band] seen in the neutral and cationic forms. This behavior is due to the added electron exceeding the capacity of the [mixed band], which destabilizes the cluster when attempting to occupy a significantly higher “other” level in the case of  $^{21}\text{A}_u$  electronic state. Consequently, this extra electron is more favorably placed in a beta 1F orbital within the [mixed band], resulting in an electron configuration of  $[1S^21P^62S^21D^{10}2F^2\text{SOMO}^{18}]$  at the 19-electron spin state, which is consistent with previous findings,<sup>32</sup> rather than the  $[1S^21P^62S^21D^{10}\text{SOMO}^{20}]$  configuration seen in the 21-electron spin state.

Another detailed examination of Fig. S2 (ESI file)† focusing on the  $\text{Sc}_{11}$  species reveals a pronounced energy degeneracy in all three charge states, characterized by an energy degeneracy among several high spin states. Importantly, the energy differences between these states are mostly smaller than 0.1 eV that ranges within the error margin of  $\pm 0.2$  eV of the DFT methods employed. This implies that their relative positions can be changed with respect to the methods employed. In the case of the cationic  $\text{Sc}_{11}^+$ , spin states of energy degeneracy’s isomers extend from triplet state and persist until reaching the 13-*et* spin state. At this point, electrons situated on the “mixed band” at beta side have already been removed, resulting in the electron shells of  $[1S^21P^61D^{10}2S^2\text{SOMO}^{12}]$  as illustrated in Fig. S2A (ESI file).† Consequently, in the 13-*et* state of cationic  $\text{Sc}_{11}^+$ , the beta HOMO is identified as the 2S-MO, contributing to a significant beta HOMO–LUMO gap specified by 0.7 eV. Similarly, in the case of the neutral  $\text{Sc}_{11}$ , the energetic degeneracy spans from the doublet to the 14-*et* spin states, where the HOMO on the beta side is also identified by 2S-MO, forming the electron shells of  $[1S^21P^61D^{10}2S^2\text{SOMO}^{13}]$ , with the beta HOMO–LUMO gap specified by 0.7 eV as well (cf. Fig. S2B, ESI file†).

Additionally, Fig. 6 and S2 (ESI file)† offer a clearer illustration of the significant reduction in the number of energy-degenerate states following replacement of the central Sc atom of  $\text{Sc}_{11}^{+/0/-}$  by a B atom. The variation in electron levels leads to a modification of electron shells between the pure and doped B clusters (discussed in the next section “Electron contribution of boron dopant and its effect to scandium hosts”). Specifically,

the electron shell undergoes a shift from  $[1S^21P^61D^{10}2S^2] + [\text{mixed band}]$  of the  $\text{Sc}_{11}^{+/0/-}$  to  $[1S^21P^62S^22P^61D^{10}] + [\text{mixed band}]$  for  $\text{B}@\text{Sc}_{10}^{+/0/-}$ . This alteration is marked by an increase in the number of electrons at the “core” level and a corresponding decrease in the number of electrons in the [mixed band]. Consequently, this shift reduces the number of closely spaced energy levels in the [mixed band], resulting in a noteworthy reduction in the degeneracy of energy states.

### 3.4 Electron contribution of boron dopant and its effect to scandium hosts

As mentioned above, the doping of boron atom not only influences the geometry but also triggers an electronic structure readjustment, significantly impacting on the spin state of the studied clusters, playing a crucial role in mitigating the energetic degeneracy among the extensive range of spin states in the initially pure Sc clusters.

To delve into a more profound understanding of the impact of boron doping on the scandium host, we now employ the NBO method<sup>55</sup> to scrutinize the natural electron configurations (NEC) and spin densities. On the one hand, the density of states (DOS) maps depicted in Fig. 7, S6 and S7 (ESI file)† reveals a difference in electron contributions when comparing scenarios with and without a B doping into the Sc host. Introduction of B into an Sc host involves its s and p electrons, contributing to the overall electron count, and consequently reducing the energy levels of the S and P molecular orbitals.

On the other hand, an intriguing observation is emerged across nearly all  $\text{Sc}_{n-1}\text{B}$  clusters, that is, the number of valence electrons in boron dopant increases by an electron donation from  $\text{Sc}_{n-1}$  host, approximately 1.5 times more (totaling around 4.5 electrons on 2s and 2p) as compared to the standard 3 electrons (2 electrons in 2s and 1 electron in 2p) of a typical boron atom. This augmented contribution significantly influences the electron configuration of the entire cluster by causing a downward shift in the 2P levels below the 1D levels.

This influence is prominently evident when examining the MO diagram of  $\text{Sc}_6^{+/0/-}$  clusters (Fig. S3–S5, respectively, ESI file†), where the 2P orbitals extend over the 1D orbitals’ levels and beyond. Introducing boron into these clusters, as illustrated in the case of  $\text{B}@\text{Sc}_6^{+/0/-}$  (Fig. S6 and S7†), the 2P orbitals gradually shift below these 1D levels.

In a different context as mentioned in a paragraph above, examination of  $\text{Sc}_{11}^{+/0/-}$  (Fig. S2, ESI file†) reveals a general electronic structure of  $[1S^21P^61D^{10}2S^2] + [\text{mixed band}]$ , where the 2P orbitals extend beyond the LUMO level. In contrast, the  $\text{B}@\text{Sc}_{10}^{+/0/-}$  scenario which mirrors the structure of the  $\text{Sc}_{11}^{+/0/-}$  but substitutes the central Sc atom with a B atom, showcases a distinct shell, namely, the 2P orbitals are lowered below the 1D levels, forming electron shells such as  $[1S^21P^62S^22P^61D^{10}] + [\text{mixed band}]$  (Fig. 6).

Additionally, due to the smaller radius of B as compared to Sc, the bonds between the central atom and those at the vertices of the square antiprism in the  $\text{B}@\text{Sc}_{10}^{+/0/-}$  are shorter than those in the  $\text{Sc}_{11}^{+/0/-}$  (approximately 2.5 and 2.8 Å, respectively). This tends to elongate the  $\text{B}@\text{Sc}_{10}^{+/0/-}$  structure along the z-axis,



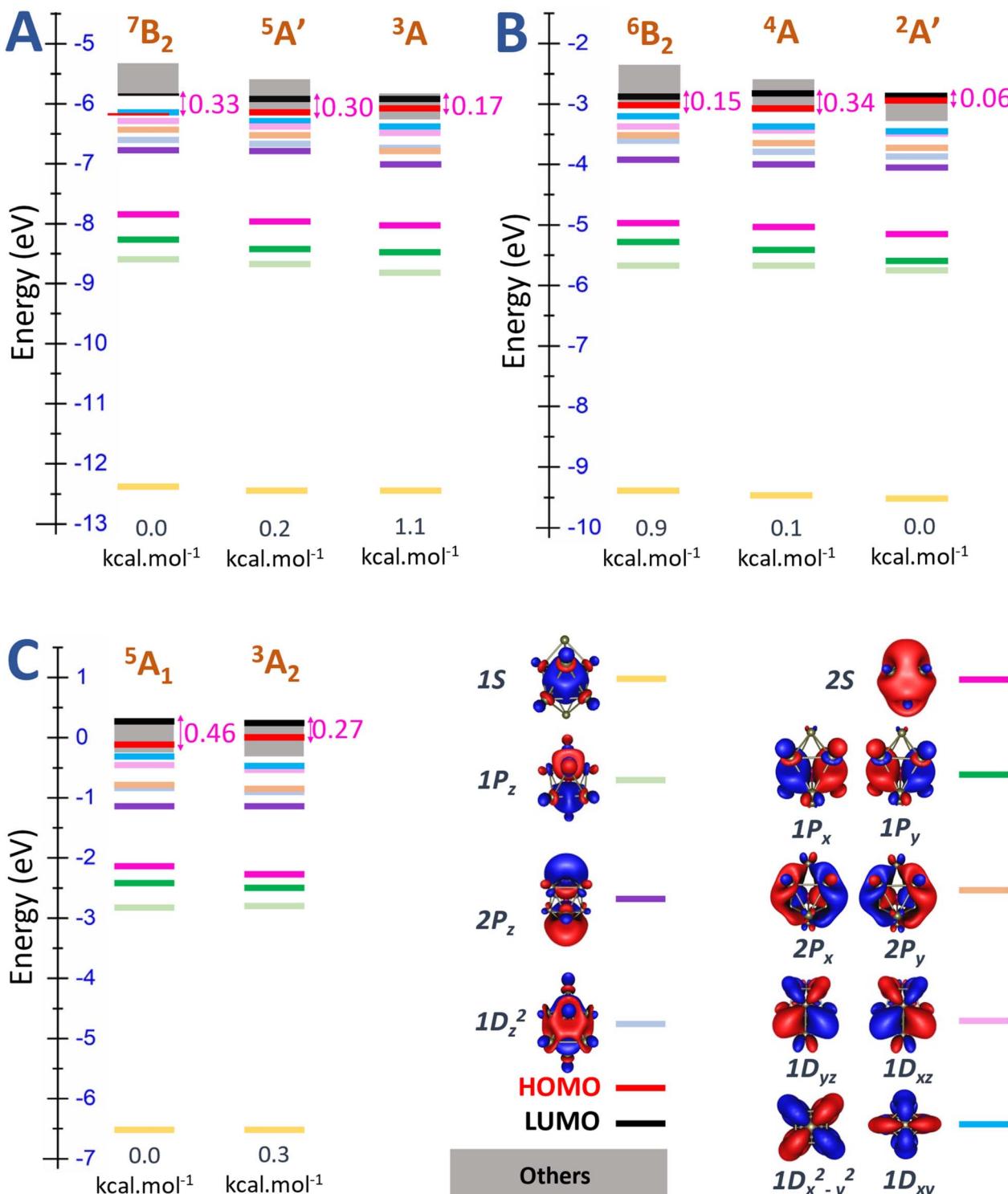


Fig. 6 Molecular orbital (MO) diagram on the beta side of (A) cationic  $\text{B@Sc}_{10}^+$ , (B) neutral  $\text{B@Sc}_{10}$ , and (C) anionic  $\text{B@Sc}_{10}^-$  clusters, using the PBE/Def2-TZVP method.

passing through the B center and the two Sc apexes of equilateral square pyramids in the gyroelongated square bipyramidal structure. As a result, the energies of  $\text{P}_z$  and  $\text{D}_z^2$  orbitals along the  $z$ -axis are significantly lower as compared to the similar  $\text{P}$  or  $\text{D}$  orbital types in other directions (*cf.* Fig. 6).

### 3.5 Thermodynamic stability

In this study, thermodynamic stability of the lowest-lying pure  $\text{Sc}_n^{+/0/-}$  and doped  $\text{Sc}_{n-1}\text{B}^{+/0/-}$  ( $n = 2-13$ ) clusters in three charged states is evaluated by the average binding energies ( $E_b$ ).

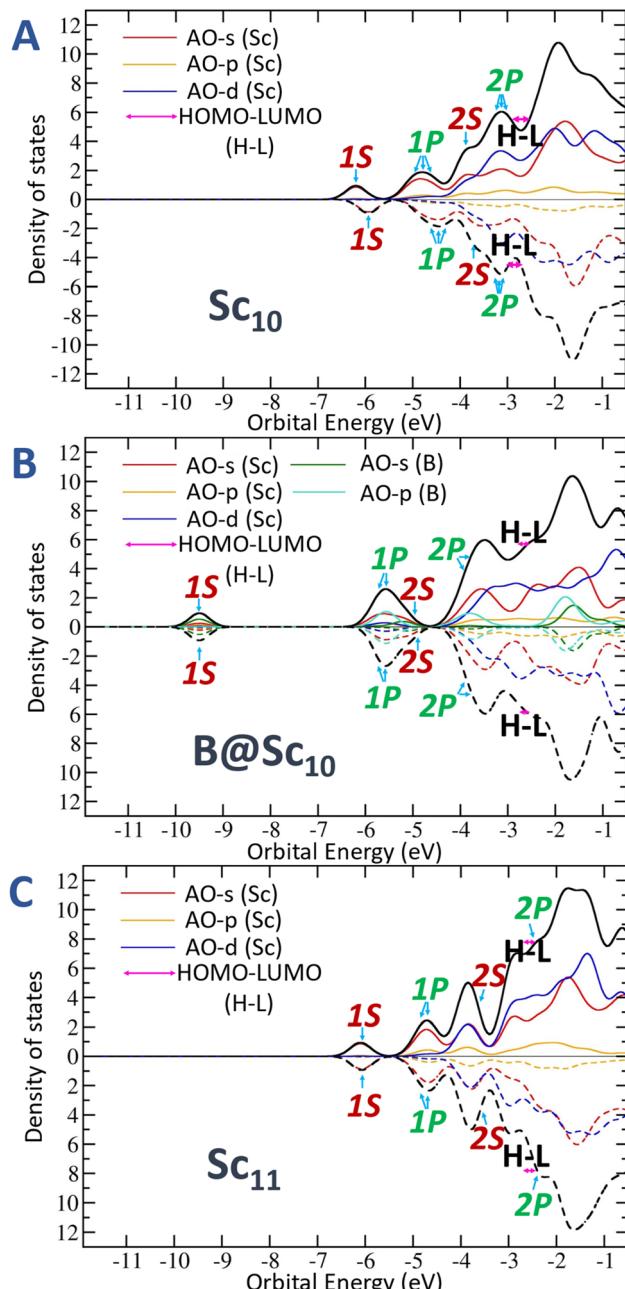


Fig. 7 Calculated density of states (DOS) for the lowest-lying neutral clusters of (A):  $\text{Sc}_{10}$ , (B):  $\text{B}@\text{Sc}_{10}$ , and (C):  $\text{Sc}_{11}$ . Positive and negative DOS represent spin-up and spin-down electrons, respectively.

The formulas used for calculating the average binding energies of these clusters are defined as follows (eqn (1)–(6)):

- For cationic pure clusters  $\text{Sc}_n^+$ :

$$E_b(\text{Sc}_n^+) = [(n-1)E(\text{Sc}) + E(\text{Sc}^+) - E(\text{Sc}_n^+)/n] \quad (1)$$

- For neutral pure clusters  $\text{Sc}_n$ :

$$E_b(\text{Sc}_n) = [nE(\text{Sc}) - E(\text{Sc}_n)]/n \quad (2)$$

- For anionic pure clusters  $\text{Sc}_n^-$ :

$$E_b(\text{Sc}_n^-) = [(n-1)E(\text{Sc}) + E(\text{Sc}^-) - E(\text{Sc}_n^-)]/n \quad (3)$$

- For cationic doped clusters  $\text{Sc}_{n-1}\text{B}^+$ :

$$E_b(\text{Sc}_{n-1}\text{B}^+) = [(n-2)E(\text{Sc}) + E(\text{Sc}^+) + E(\text{B}) - E(\text{Sc}_{n-1}\text{B}^+)/n] \quad (4)$$

- For neutral doped clusters  $\text{Sc}_{n-1}\text{B}$ :

$$E_b(\text{Sc}_{n-1}\text{B}) = [(n-1)E(\text{Sc}) + E(\text{B}) - E(\text{Sc}_{n-1}\text{B})]/n \quad (5)$$

- For anionic doped clusters  $\text{Sc}_{n-1}\text{B}^-$ :

$$E_b(\text{Sc}_{n-1}\text{B}^-) = [(n-1)E(\text{Sc}) + E(\text{B}^-) - E(\text{Sc}_{n-1}\text{B}^-)]/n \quad (6)$$

In these equations:

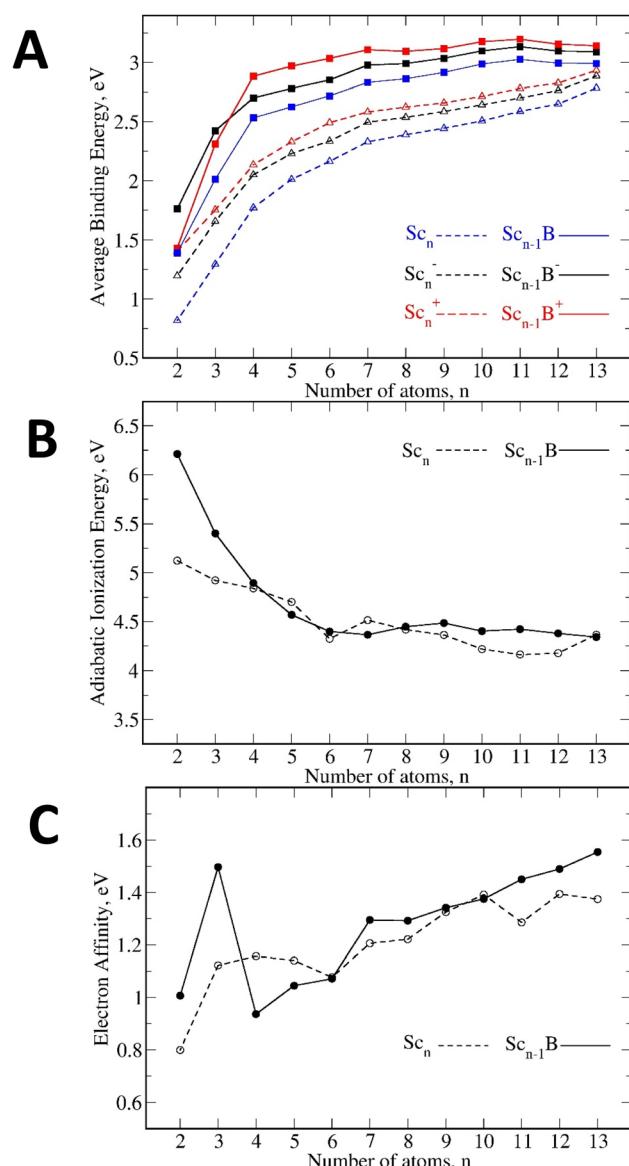


Fig. 8 (A): Average binding energy of  $\text{Sc}_n^{+/0-}$  and  $\text{Sc}_{n-1}\text{B}^{+/0-}$ , (B): adiabatic ionization energy and (C): adiabatic electron affinity C of the lowest-lying energy  $\text{Sc}_n$  and  $\text{Sc}_{n-1}\text{B}$  clusters including  $n = 2-13$  using the PBE/def2-TZVP method.



•  $E(\text{Sc})$ ,  $E(\text{Sc}^+)$  and  $E(\text{Sc}^-)$  represent the total energies of a single scandium atom, scandium cation, and scandium anion, respectively.

•  $E(\text{Sc}_n^+)$ ,  $E(\text{Sc}_n)$  and  $E(\text{Sc}_n^-)$  represent the total energies of the lowest-lying cationic, neutral, and anionic  $\text{Sc}_n^{+/0/-}$ , respectively.

•  $E(\text{B})$  and  $E(\text{B}^-)$  denote the total energies of a single boron atom and boron anion, respectively.

•  $E(\text{Sc}_{n-1}\text{B}^+)$ ,  $E(\text{Sc}_{n-1}\text{B})$  and  $E(\text{Sc}_{n-1}\text{B}^-)$  represent the total energies of the lowest-lying cationic, neutral and anionic  $\text{Sc}_{n-1}\text{B}^{+/0/-}$ , respectively.

For cationic clusters, because the ionization energy of the Sc atom (6.30 eV) is significantly lower than that of the B atom (8.67 eV), we thus utilize only the total energies of the  $\text{Sc}^+$  cation  $E(\text{Sc}^+)$  for calculating the average binding energy of cationic clusters, instead of the total energies of the  $\text{B}^+$  cation  $E(\text{B}^+)$ . For anionic cluster, since the electron affinity of the B atom (0.27 eV) is larger than that of the Sc atom (0.04 eV), the total energies of the  $\text{B}^-$  anion  $E(\text{B}^-)$  is used for in the calculation of anionic cluster binding energies, instead of the total energies of the  $\text{Sc}^-$  anion  $E(\text{Sc}^-)$ .

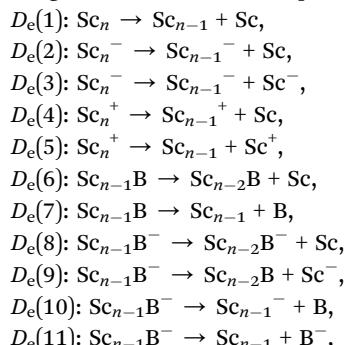
**Table 2** Dissociation energies ( $D_e$ , eV) obtained (PBE/Def2-TZVP + ZPE) for various fragmentation channels of  $\text{Sc}_n$  in neutral, cationic, and anionic states

<i>n</i>	Neutrals		Anion		Cation	
	$D_e(1)$	$D_e(2)$	$D_e(3)$	$D_e(4)$	$D_e(5)$	
2	1.63	2.39	2.39	2.81	2.81	
3	2.25	2.57	3.33	2.45	3.63	
4	3.2	3.23	4.32	3.28	4.66	
5	2.97	2.96	4.07	3.11	4.57	
6	2.92	2.86	3.96	3.3	4.9	
7	3.32	3.45	4.49	3.13	5.11	
8	2.81	2.83	3.99	2.91	4.69	
9	2.88	2.99	4.17	2.94	4.82	
10	3.08	3.14	4.43	3.22	5.16	
11	3.39	3.28	4.64	3.45	5.52	
12	3.34	3.45	4.69	3.32	5.46	
13	4.41	4.39	5.74	4.22	6.34	

Fig. 8A clearly indicates that the binding energy values of the doped  $\text{Sc}_{n-1}\text{B}^{+/0/-}$  are stronger than those of the pure  $\text{Sc}_n^{+/0/-}$ , suggesting that introduction of a B atom into the Sc clusters enhances the thermodynamic stability of the initial Sc hosts. In addition, Fig. 8A highlights another noteworthy observation emphasizing the significant role of the charge state in the overall stability. In both pure and B-doped Sc clusters, the charged clusters exhibit greater stability with respect to their neutral counterparts, with the cationic states displaying the highest level of stability.

Moreover, an analysis of the adiabatic ionization energies (IEa) and adiabatic electron affinities (EAa) for the lowest-lying neutral isomers in Fig. 8B and C, respectively, again shows a notable size dependence. The pattern of IEa exhibits its decrease with increasing size, as the clusters grow, detachment of an electron becomes more facile. Conversely, the trend of EAa rises along with size; as the clusters expand, reception of an electron also becomes more favorable. However, the EAa values are rather small (<1.6 eV) suggesting their instability with respect to electron addition. Hence, these observed trends suggest that the clusters considered predominantly exhibit a preference for the cationic states.

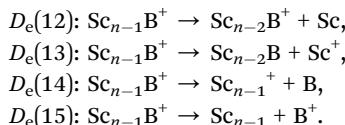
To enhance the assessment of thermodynamic stability, the dissociation energies ( $D_e$ ) for diverse fragmentation channels (*x*) of the lowest-lying clusters are calculated. The results are presented in Tables 2 and 3, and the corresponding formulas are outlined below, where (*x*) represents the number order of the fragmentation channels, spanning from  $D_e(1)$ – $D_e(15)$ :



**Table 3** Dissociation energies ( $D_e$ , eV) obtained (PBE/Def2-TZVP + ZPE) for various fragmentation channels of  $\text{Sc}_{n-1}\text{B}$  in neutral, cationic, and anionic states

<i>n</i>	Neutrals		Anions				Cations			
	$D_e(6)$	$D_e(7)$	$D_e(8)$	$D_e(9)$	$D_e(10)$	$D_e(11)$	$D_e(12)$	$D_e(13)$	$D_e(14)$	$D_e(15)$
2	2.78	2.78	3.52	3.75	3.75	3.48	5.24	2.86	2.86	5.24
3	3.26	4.41	3.75	4.72	5.10	4.84	4.21	4.30	4.27	7.82
4	4.09	6.25	3.53	4.99	6.07	5.80	4.46	5.50	6.28	10.03
5	2.99	6.04	3.10	4.00	5.93	5.67	3.32	4.72	6.31	10.14
6	3.19	6.26	3.21	4.22	6.19	5.92	3.36	5.09	6.56	10.53
7	3.51	6.84	3.73	4.76	7.06	6.79	3.54	5.44	6.80	11.15
8	3.09	6.60	3.08	4.34	6.69	6.42	3.00	4.93	6.67	10.83
9	3.34	7.13	3.39	4.64	7.25	6.98	3.30	5.15	7.06	11.32
10	3.63	7.87	3.66	4.96	7.92	7.66	3.71	5.52	7.83	12.14
11	3.42	8.22	3.50	4.83	8.28	8.01	3.40	5.30	8.01	12.47
12	2.64	7.47	2.68	4.09	7.68	7.41	2.69	4.56	7.26	11.76
13	2.96	7.09	3.02	4.47	7.25	6.99	3.00	4.91	6.93	11.42





Both pure and doped clusters display a tendency to favor the detachment of a neutral Sc atom over a charged Sc atom (Tables 2 and 3), indicating a consistent preference of charge retention within the clusters following dissociation. This preference aligns with the earlier discussion regarding a stability's tendency for the charged clusters over the neutral counterpart. Moreover, across all three charge states (Table 3), the dissociation energies for the  $\text{Sc}_{n-1}\text{B}^{+/0/-}$  clusters in the B-dissociation channel  $D_e(7)$ ,  $D_e(10)$  and  $D_e(14)$  are greater than those of the Sc-detachment channel  $D_e(6)$ ,  $D_e(8)$  and  $D_e(12)$ . This observation can be attributed to two main factors. Firstly, the B dopant has an intrinsic preference for reception of electrons from nearby Sc atoms (as the electron population in B is 1.5 times higher than normal), leading to formation of strong Sc-B bonds. Secondly, starting from  $n = 5$  onwards, B is situated inside the Sc cages, making it more challenging to be extracted from the cage, as compared to the cutting of an outer Sc atom.

## 4. Concluding remarks

In the present theoretical study, a comprehensive investigation of pure  $\text{Sc}_n^{+/0/-}$  and doped  $\text{Sc}_{n-1}\text{B}^{+/0/-}$  clusters ( $n = 1-13$ ) is conducted using DFT computations with the PBE/Def2-TZVP method, leading to several significant conclusions:

(i) A detailed structural analysis of the clusters in three charged states reveals a pronounced size dependency in their structures. However, the shape of a specific cluster size remains unchanged upon the removal or addition of an electron. The critical size for the  $\text{Sc}_{n-1}\text{B}^{+/0/-}$  clusters is determined to be  $n = 6$ , marking the point where an exohedral–endothedral transformation occurs. This transformation is also accompanied by a transition in the substitution-addition trend of the B atom into the pure Sc host. For doped  $\text{Sc}_{n-1}\text{B}^{+/0/-}$  clusters with  $n = 2-6$ , the boron atom prefers an exohedral substitution into the original shapes of the  $\text{Sc}_n^{+/0/-}$  clusters. Nevertheless, there is a shift towards a boron endohedral addition when the  $\text{Sc}_{n-1}\text{B}^{+/0/-}$  clusters reach a size of  $n = 6-11$ . In larger clusters,  $n = 12$  and 13 of  $\text{Sc}_{n-1}\text{B}^{+/0/-}$ , a departure from the earlier trends is observed. Instead of direct addition or substitution into the Sc host, Sc atoms are gradually added onto the outer faces of  $\text{Sc}_{n-1}\text{B}^{+/0/-}$ . Meanwhile,  $\text{Sc}_{12}^{+/0/-}$  transforms into a mono-capped pentagonal antiprism, and  $\text{Sc}_{13}^{+/0/-}$  forms a well-known icosahedron.

(ii) The  $\text{B}@\text{Sc}_6^{+/0/-}$  clusters are identified as the smallest doped cages observed thus far. They are notable for their nearly perfect octahedral shape, with a B atom centrally enclosed within the  $\text{Sc}_6^{+/0/-}$  cages. The size of the  $\text{Sc}_6^{+/0/-}$  cages is optimal, allowing the B atom to fit snugly in the center. This enhances the condensation of the initially loosely structured  $\text{Sc}_6^{+/0/-}$  cages, resulting in a more compact overall structure and stabilizing their geometric configurations.

(iii) A molecular orbital (MO) analysis provides a suitable explanation for the observed energy degeneracy between

various stable spin states, which arise from the closely packed 3d electrons influenced by the Jahn–Teller effect. This results in a mixed band with overlapping energy levels, where the small HOMO–LUMO gap facilitates easier electron traversal. The energy degeneracy is resolved when the HOMO level occupies distinct, lower-energy orbitals outside the mixed band, creating a noticeable HOMO–LUMO gap.

(iv) At the critical size of  $n = 13$ ,  $\text{Sc}_{13}^{+/0/-}$  exhibits a synergistic interplay that results in both an icosahedral structure and a stable high-spin electronic state with a  $^{19}\text{A}_1$  state for the cationic, a  $^{20}\text{A}$  state for the neutral, and a  $^{19}\text{B}_{3u}$  state for the anionic  $\text{Sc}_{13}$  isomer, all without any energetic degeneracy. The electron shells in these cationic, neutral, and anionic isomers are established as  $[1\text{S}^2 1\text{P}^6 2\text{S}^2 1\text{D}^{10} \text{SOMO}^{18}]$ ,  $[1\text{S}^2 1\text{P}^6 2\text{S}^2 1\text{D}^{10} \text{SOMO}^{19}]$  and  $[1\text{S}^2 1\text{P}^6 2\text{S}^2 1\text{D}^{10} 2\text{F}^2 \text{SOMO}^{18}]$ , respectively.

(v). The boron dopant unusually increases the number of valence electrons, approximately 1.5 times more than a regular boron atom due to electron donation from the Sc host. This heightened contribution significantly influences the electron configuration of the entire cluster, causing a downward shift in the 2P levels below the 1D levels. This adjustment in electron configuration plays a crucial role in stabilizing the spin state of the studied clusters, effectively mitigating the energetic degeneracy among the extensive range of spin states in the initially pure Sc clusters.

(vi). Overall, introduction of a B atom as dopant into the Sc clusters enhances the thermodynamic stability of the initial Sc hosts and displays a notable charge-dependent with a preference for stability in cationic isomers.

## Data availability

The quantum chemical program Gaussian 16 has been used. Reference of this program is given in the list of references. The datasets supporting this article are uploaded as part of the ESI file† that includes the Cartesian coordinates of the optimized geometries, information on the electronic structures of the structures considered.

## Conflicts of interest

There are no conflicts to declare.

## Acknowledgements

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