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# Mechanisms and selectivity of methanol oxidation on PtRuM<sub>3</sub>/C-MWCNT (M = Fe and Co) electrocatalysts†

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Methanol oxidation efficiency and resistance to CO poisoning are the most challenging issues associated with direct methanol fuel cells. Much experimental effort has been undertaken, such as generating Pt-based binary and ternary nanoparticles, creating composite substrates, and fabricating nanoparticles with special shapes, to overcome these drawbacks. Our previous experiment showed that ternary PtRuM<sub>3</sub>/C-MWCNT (M = Fe and Co; C-MWCNT = carbon Vulcan-multiwalled carbon nanotube) electrocatalysts exhibited high methanol oxidation activity and tolerance to CO poisoning. However, reaction mechanisms on ternary PtRuM<sub>3</sub>/C-MWCNT (M = Fe and Co) electrocatalysts remain unknown. Therefore, this work is devoted to elucidating the problem using density functional theory calculations and thermodynamic models. Our present study showed that methanol oxidation proceeds *via* four possible reaction pathways on the surface of PtRuM<sub>3</sub>/C-MWCNTs, where the most favourable one follows a series of steps converting CH<sub>3</sub>OH → CH<sub>3</sub>OH\* → CH<sub>2</sub>OH\* → CH<sub>2</sub>O\*/CHOH\* → CHO\* → CHOOH\* → CHOO\*/COOH\* → CO<sub>2</sub>\* with a thermodynamic barrier of 0.513 eV for applied potentials of *U* = 0 V and 1.005 V on PtRuFe<sub>3</sub>/C-MWCNTs and 0.404 eV for *U* = 0 V and 0.167 eV for *U* = 1.005 V on PtRuCo<sub>3</sub>/C-MWCNTs. We also provide physical insights into the interaction between methanol oxidation intermediates and substrates' surface by analysing electronic properties. Our findings support the results of our previous experiment. The results of this study can be useful for rationally designing the anode for fuel cells.

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## 1 Introduction

Today, global energy shortages and environmental pollution problems have been increasing tremendously. Therefore, research on novel energy sources and technologies is an urgent requirement. Direct methanol fuel cells (DMFCs) are regarded as one of the most promising energy technologies owing to their high conversion efficiencies, low operating temperatures, and short recharge time.<sup>1,2</sup> Platinum is hitherto the best electrocatalyst for methanol oxidation on the anode of DMFCs because of its outstanding catalytic efficiency, excellent electrical properties, and high corrosion resistance; however, CO poisoning is the major obstacle in increasing the performance of DMFCs to a practical level.<sup>1,2</sup> Alloying is an effective way to enhance the

activity of methanol oxidation and reduce the cost of DMFCs because of bifunctional mechanisms or electronic effects. Especially, the methanol oxidation ability of PtM (M = Fe, Co, Ni, Cu, Ru, *etc.*) binary alloys is higher than that of pure Pt,<sup>3–10</sup> where PtRu exhibits the highest electrocatalytic performance due to its improved tolerances to CO poisoning. From the theoretical viewpoint, adding a third metal could change PtRu electronic properties and surface structure as well as improve catalytic performance.<sup>11,12</sup> To date, many studies have shown that ternary Pt-based nanocrystals formed from various metals (Ru, Fe, Co, Ni, Pd, Rh, Cu, *etc.*) and support materials (carbon, carbon nanotubes, graphene, metal oxides, *etc.*) significantly enhance methanol oxidation activity and the durability of the anode of DMFCs.<sup>13–20</sup> Among the inexpensive metals combined with PtRu alloy, earth-abundant transition metals with low cost and good catalytic performance, such as iron (Fe), cobalt (Co), and nickel (Ni), are superior candidates for developing the anode of DMFCs.<sup>21–30</sup> Specifically, PtRuFe alloy displayed a higher onset potential and current intensity than PtRu and PtFe alloys.<sup>22–24</sup> PtRuNi alloy on Vulcan carbon and carbon nanotubes can significantly improve the methanol oxidation performance and tolerance to CO poisoning compared to PtRu alloy.<sup>25–27</sup> Meanwhile, PtRuCo alloy without supports also exhibited a superior ability to oxidize methanol and prevent CO poisoning compared to the PtRu alloy.<sup>28,29</sup> Our research recently

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showed that the third metal component, M, enhanced the electrocatalytic activity of PtRuM<sub>x</sub>/C-MWCNTs (M = Fe, Co, Ni; x = 1, 3) compared to the binary PtRu/C-MWCNTs system. Moreover, PtRuCo<sub>x</sub>/C-MWCNTs exhibited the best methanol oxidation activity, while PtRuFe<sub>x</sub>/C-MWCNTs showed the highest tolerance to CO poisoning.<sup>31</sup>

Many theoretical studies on the interaction between methanol and catalysts have been carried out along with experiments. Using density functional theory (DFT) calculations, Zhao's group investigated the methanol oxidation on PtRu(111).<sup>32</sup> They found that the most favourable reaction pathway of methanol oxidation on PtRu(111) is CH<sub>3</sub>OH → CH<sub>3</sub>O → CH<sub>2</sub>O → CHO → CHOOH → COOH → CO<sub>2</sub>. Moreover, on the PtRu(111) surface, most of the intermediates adsorbed around the Ru sites due to the lower electronegativity of Ru atoms. According to Orazi *et al.*, the methanol molecule adsorbs most stably *via* its O atom on the top Co site of the PtCo(111) surface.<sup>33</sup> The charge transfer from the C atom to the O atom of the methanol molecule and finally to the Co atoms changed the charge distribution around the adsorption site of methanol. Du *et al.* analysed the possible mechanisms of methanol decomposition on the Pt<sub>3</sub>Ni(111) surface by examining the initial scission of O–H, C–H, and C–O bonds.<sup>34</sup> The DFT investigation of the reaction pathway for methanol on different Pt crystal planes and PtNi surface also suggested the Ni site as the favourable adsorption position for methanol oxidation.<sup>35</sup> Furthermore, the density functional studies of the CO adsorption energy on Fe<sub>1-x</sub>PtRu<sub>x</sub> nanocrystal surfaces showed that the Fe<sub>1-x</sub>PtRu<sub>x</sub> alloy weakens the CO–Pt bond to enhance the anti-CO poisoning ability.<sup>36</sup> Notably, the DFT calculations have focused only on studying the methanol oxidation on binary alloys, while there are only a few works for ternary alloy catalysts.

The experimental works confirmed that ternary PtRuM alloys without carbon supports exhibited higher methanol oxidation efficiency and CO poisoning resistance over binary Pt-based and pure metal catalysts.<sup>22–29,31</sup> Remarkably, our previous experiment revealed an excellent catalytic activity of PtRuM<sub>x</sub>/C-MWCNTs (M = Fe, Ni, Co) and the atomic ratio of Pt:Ru:M = 1:1:3 showed a better performance than that of 1:1:1, for the methanol oxidation.<sup>31</sup> However, no studies are available to elucidate the methanol oxidation mechanisms of PtRuM<sub>x</sub>/C-MWCNTs, particularly for Pt:Ru:M = 1:1:3. Therefore, the present work is devoted to solving this issue by systematically searching for the possible intermediates and then clarifying the reaction pathways of methanol oxidation on PtRuM<sub>3</sub>/C-MWCNTs (M = Fe, Co) catalysts. Here, we selected two representatives of the electrocatalysts with M = Fe and Co because PtRuCo<sub>3</sub>/C-MWCNTs showed the best reaction activity, while PtRuFe<sub>3</sub>/C-MWCNTs exhibited the highest tolerance to CO poisoning among the considered third metal (Fe, Co, and Ni).<sup>31</sup> The results of this work are completely new and will be valuable for optimally designing ternary Pt-based catalysts. To achieve the target, we used density functional theory calculations and the thermodynamic model.<sup>37,38</sup>

## 2 Catalyst model and computational details

PtRuFe<sub>3</sub>/C-MWCNTs and PtRuCo<sub>3</sub>/C-MWCNTs substrates were designed using the slab model with the (111) crystal surface framework and the (4 × 4) unit cell of five atomic layers. Furthermore, to maximize the role of precious metals (Pt and Ru), we designed the supercell with the layers of these metals close to the surface of the slab. As depicted in Fig. 1a and b (top and side views), the topmost and second layers consist of sixteen Pt and sixteen Ru atoms, respectively. The underneath three layers were composed of inexpensive Fe or Co metals. The above five atomic layers are grown on the support, which consists of the graphene nanosheet with a few extra C atoms adsorbed on the bottom side of the graphene to mimic the C-MWCNTs support of the PtRuM<sub>3</sub>/C-MWCNTs substrates (M = Fe and Co). The total number of atoms in each substrate is 116. We set up the substrates as described because the high-resolution transmission electron microscopy of our previous experiment exhibited that the scale of the MWCNTs is much broader than that of the nanoparticles dispersed on them. Therefore, the nanoparticle is regarded as located approximately on a nearly flat area on the surface of the MWCNT. Also, by ignoring the effects of the multiple walls, we can use a graphene sheet to mimic the MWCNT. The decorated C atoms on the bottom side of the graphene sheet mimic the Vulcan carbon in our previous experiment.<sup>31</sup> We expect that our supercell model can capture the main physics of the methanol oxidation on the surface of the PtRuM<sub>3</sub>/C-MWCNTs catalysts. We have to emphasize that we do not intend to fully describe the MWCNTs, even though there were not many DFT calculations concerning the complexity of the model as in the present study. The *ab initio* studies have usually ignored carbon supports.<sup>32–34,39,40</sup> The atomic positions and the unit cell size for the designed substrates were first optimized, and the structure of possible intermediates of methanol oxidation on the optimized substrates was then fully relaxed using the density functional theory calculations with the aid of the Vienna *Ab initio* Simulation Package (VASP).<sup>41</sup> Our model does not include van der Waals interactions because the contribution toward chemical reactions on metal surfaces is usually ignorable.<sup>42,43</sup> To optimize the unit cell size, we varied the lattice constant and calculated the total energy for each variation. The minimum point in the parabolic curve of the total energy *versus* the lattice constant determines the optimized size of the unit cell, as shown in Fig. S1 in ESI.† The optimized lattice constant of both substrates is 2.61 Å. Therefore, the dimensions of the unit cell in the slab model are 10.4 Å and 10.4 Å in the x and y axes and 23.4 Å in the surface normal direction with a vacuum space of about 12 Å. In all the optimization processes for the atomic positions, the atoms were allowed to move freely in all dimensions until the force acting on each atom reached 0.001 eV Å<sup>-1</sup>. We used a plane-wave basis set with a kinetic cut-off energy of 400 eV, the Perdew–Burke–Ernzerhof generalized gradient approximation for the exchange–correlation energy,<sup>44,45</sup> and the projector augmented wave pseudopotentials for the ion–valence electron interaction.<sup>46</sup> The k-point mesh sample of 5 × 5 × 1 with the special-point sampling



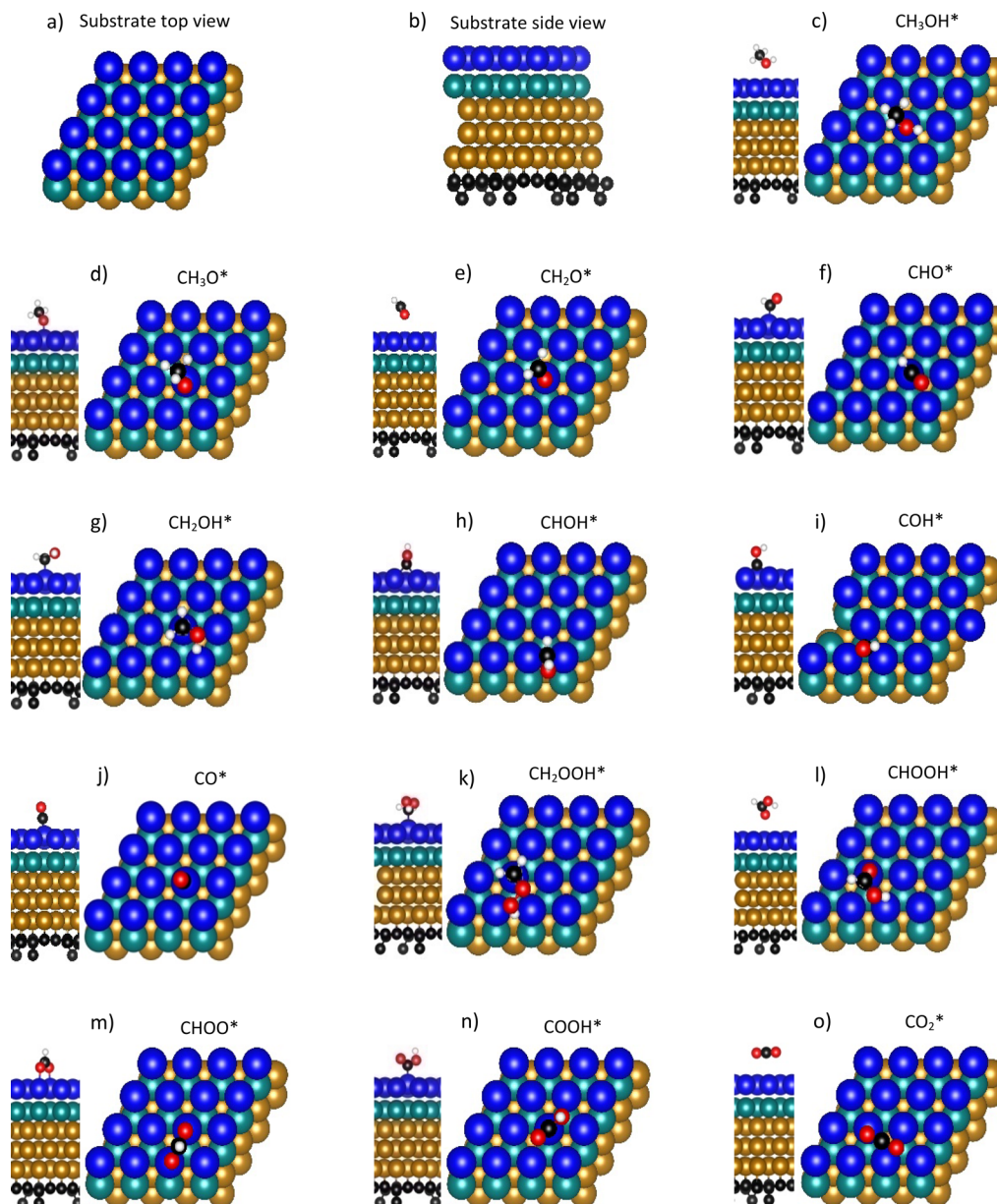


Fig. 1 The top and side views of the substrates (a and b) and the most stable configurations for the adsorption of methanol oxidation intermediates on the surface of PtRuM<sub>3</sub>/C-MWCNTs (M = Fe and Co) catalysts (c–o). Topmost-layer Pt (blue), Ru (green), Fe (golden), C (black), O (red), and H (white).

technique of Monkhorst and Pack was used for the Brillouin zone integration.<sup>47</sup> The cut-off energy and the *k*-point mesh sample have been tested for the convergence of the total energy. Spin polarization was appropriately constructed. To simulate periodic supercells, dipole corrections were set. The convergence speed of the calculations was supported by Methfessel–Paxton smearing<sup>48</sup> of first order with the sigma value of 0.2 eV for geometry optimization and 0.05 eV for obtaining electronic properties.

## 2.1 Adsorption energy

The binding strength of the various reaction intermediates on the possible adsorption sites of the substrates is expressed *via* the adsorption energy according to the following formula:

$$E_a = E_{[\text{sub+ads}]} - (E_{\text{sub}} + E_{\text{ads}}), \quad (1)$$

where  $E_{[\text{sub+ads}]}$ ,  $E_{\text{sub}}$ , and  $E_{\text{ads}}$  are the total energy of the substrate–adsorbate system, the clean substrate, and the isolated adsorbate, respectively. This work ignored the influences of water medium on the adsorption of the methanol oxidation intermediates.

## 2.2 Charge density difference

The charge density difference ( $\Delta\rho$ ) is studied to elucidate the interaction between the adsorbent and adsorbate using the following equation:<sup>33,38</sup>

$$\Delta\rho = \rho_{[\text{sub+ads}]} - \rho_{\text{sub}} - \rho_{\text{ads}}, \quad (2)$$



where  $\rho_{[\text{sub+ads}]}$ ,  $\rho_{\text{sub}}$ , and  $\rho_{\text{ads}}$  are the charge density of the adsorbent/adsorbate system, substrate with the adsorbed state, and the adsorbed molecule, respectively.

### 2.3 Gibbs free energy

Free energy diagrams following the thermodynamic model<sup>37,49,50</sup> were constructed to understand the thermodynamic stability of the reaction intermediates. The Gibbs free energy with electrode potential corrections was calculated as follows:

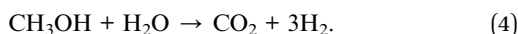
$$\Delta G(U) = \Delta G(0) + neU. \quad (3)$$

Here,  $\Delta G(0) = \Delta E + \Delta \text{ZPE} - T\Delta S$  with  $\Delta E$  and  $\Delta \text{ZPE}$  are reaction energy and the change of zero-point energies of intermediate reactions, estimated from the total energies and vibrational energies of our DFT calculations. The change in entropies ( $\Delta S$ ) was calculated from our DFT calculations using VASPKIT;<sup>51</sup>  $n$  and  $U$  are the number of electrons in each reaction step and the electrode potential relative to the standard hydrogen electrode, respectively. According to our previous experimental results,<sup>31</sup> the working potential of methanol oxidation was 0.8 V for the PtRuM<sub>3</sub>/C-MWCNTs (M = Fe, Co) electrocatalysts relative to an Ag/AgCl (3.5 M KCl) reference electrode. Therefore, the value of  $U$  for methanol oxidation in formula (3) is equivalent to 1.005 V, *i.e.*,  $E_{\text{RHE}} = E_{\text{Ag/AgCl}} + 0.205 \text{ V}$ , relative to the standard hydrogen electrode in our thermodynamic model. For comparison, we also studied the reaction mechanisms with  $U = 0 \text{ V}$ . The standard atmospheric pressure of 1 bar, room temperature of 300 K, and pH = 0 were used in this study. With the pH = 0 level, we can replace the proton and electron transfer by  $\text{H}^+ + \text{e}^- = \frac{1}{2}\text{H}_2$ , which is adequate with the hydrogen standard electrode model.

## 3 Results and discussion

### 3.1 Adsorption configurations of intermediates

The total methanol oxidation reaction generates carbon dioxide as the following equation:



This equation can proceed in many possible pathways (see Fig. 2) with multi-intermediate steps from (1)–(18) and involve thirteen reaction intermediates. The intermediates of methanol oxidation are proposed by a continuous dehydrogenation

process from the previously formed intermediates starting from  $\text{CH}_3\text{OH}^*$ , where the asterisk denotes the adsorbed state of the intermediates on the substrates' surface. The dehydrogenation can take place at the hydrogen atom near the O or C atoms of each intermediate. For example, in steps (1) and (2),  $\text{CH}_3\text{OH}^*$  can detach a hydrogen atom near the O atom to form  $\text{CH}_3\text{O}^*$  and near the C atom to generate  $\text{CH}_2\text{OH}^*$ , respectively. The other intermediates are also formed in the same manner. Noticeably, forming the double-oxygen intermediates such as  $\text{CH}_2\text{OOH}^*$ ,  $\text{CHOOH}^*$ , and  $\text{COOH}^*$  in steps (6), (11), and (16) require the involvement of a water molecule, *i.e.*,  $\text{CH}_2\text{O}^* + \text{H}_2\text{O} \rightarrow \text{CH}_2\text{OOH}^* + \frac{1}{2}\text{H}_2$ ,  $\text{CHO}^* + \text{H}_2\text{O} \rightarrow \text{CHOOH}^* + \frac{1}{2}\text{H}_2$ , and  $\text{CO}^* + \text{H}_2\text{O} \rightarrow \text{COOH}^*$ , respectively. Here,  $\text{CH}_2\text{OOH}^*$ ,  $\text{CHOOH}^*$ , and  $\text{COOH}^*$  were formed by combining  $\text{CH}_2\text{O}^*$ ,  $\text{CHO}^*$ , and  $\text{CO}^*$  with the OH group, which stemmed from the water splitting reaction,  $\text{H}_2\text{O} \rightarrow \text{OH} + \frac{1}{2}\text{H}_2$ , respectively. To explore the possible intermediates of methanol oxidation reaction, we designed the structure of each intermediate on the topmost surface of the substrate with the initial position of the intermediate of about 3 Å with various directions above the surface. We then optimized all the atomic positions of the designed structure and obtained the adsorption energy. For each intermediate, we compared its adsorption energies at various adsorption sites and configurations to gauge the most favourable adsorption configuration with the most negative adsorption energy. Fig. 1c–o shows the most stable configuration for various adsorbed intermediates of the methanol oxidation reaction, *i.e.*, methanol ( $\text{CH}_3\text{OH}^*$ ), methoxy ( $\text{CH}_3\text{O}^*$ ), hydroxymethyl ( $\text{CH}_2\text{OH}^*$ ), formaldehyde ( $\text{CH}_2\text{O}^*$ ), hydroxymethylene ( $\text{CHOH}^*$ ), hydroperoxymethyl ( $\text{CH}_2\text{OOH}^*$ ), formyl ( $\text{CHO}^*$ ), isoformyl ( $\text{COH}^*$ ), formic acid ( $\text{CHOOH}^*$ ), carbon monoxide ( $\text{CO}^*$ ), formate ( $\text{CHOO}^*$ ), carboxyl ( $\text{COOH}^*$ ), and carbon dioxide ( $\text{CO}_2^*$ ), on the surface of the PtRuM<sub>3</sub>/C-MWCNTs (M = Fe, Co) substrates. Particularly, the adsorption site, the bond distance ( $d_{\text{ads-sur}}$ ) from the nearest atom (carbon or oxygen atom, see Fig. 1c–o for each case) of the intermediates to the surface of the substrate, the adsorption energy ( $E_{\text{ads}}$ ), the zero-point energy (ZPE), and the total energy ( $E_{\text{total}}$ , *i.e.*,  $E_{\text{ads}}$  plus ZPE) are also listed in Table 1. As shown in Fig. 1c–o, several intermediates such as  $\text{CH}_3\text{OH}^*$ ,  $\text{CH}_3\text{O}^*$ ,  $\text{CH}_2\text{O}^*$ , and  $\text{CHOOH}^*$  adsorb most favourably with the end-on configuration on the top (T) site of the Pt atom, where the O atom is the nearest atom to the substrates' surface. The adsorption of the other intermediates, *i.e.*,  $\text{CH}_2\text{OH}^*$ ,  $\text{CHOH}^*$ ,  $\text{CH}_2\text{OOH}^*$ ,  $\text{CHO}^*$ ,  $\text{COH}^*$ ,  $\text{CO}^*$ , and  $\text{COOH}^*$ , is also the most

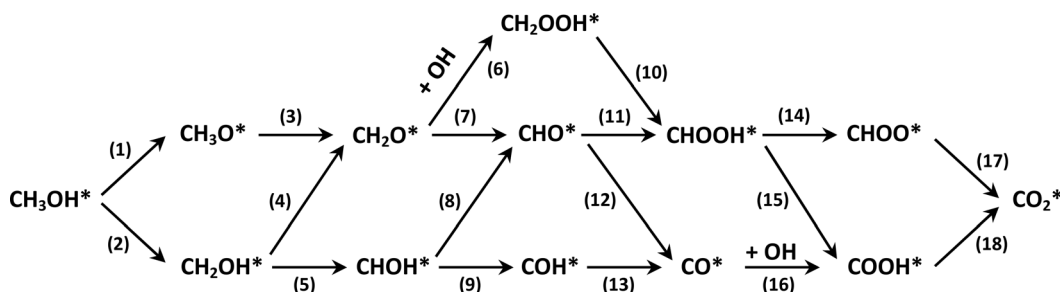


Fig. 2 Possible methanol decomposition pathways on catalyst surfaces.



**Table 1** The bond distance ( $d_{\text{ads-sur}}$ ) from the nearest atom (carbon or oxygen atom) of adsorbate molecules to the surface; adsorption energy ( $E_{\text{ads}}$ ), zero-point energy (ZPE), and total energy ( $E_{\text{total}}$ , i.e.,  $E_{\text{ads}}$  plus ZPE) of the intermediates on the PtRuM<sub>3</sub>/C-MWCNT (M = Fe and Co) substrates. The top site of a Pt atom (T), the bridge of two Pt atoms (B), and the hollow with an underneath Ru atom (H)

Molecule	Chemical formula	$d_{\text{ads-sur}}$ (Å)		$E_{\text{ads}}$ (eV)		ZPE (eV)		$E_{\text{total}}$ (eV)	
		M = Fe (site)	M = Co (site)	M = Fe	M = Co	M = Fe	M = Co	M = Fe	M = Co
Methanol	CH <sub>3</sub> OH*	2.76 (T)	2.66 (T)	0.017	-0.305	1.375	1.379	1.392	1.074
Methoxy	CH <sub>3</sub> O*	2.17 (T)	2.15 (T)	-1.194	-1.483	1.061	1.060	-0.133	-0.423
Formaldehyde	CH <sub>2</sub> O*	2.97 (T)	3.07 (T)	0.072	-0.230	0.721	0.724	0.793	0.494
Formyl	CHO*	2.36 (T)	2.37 (T)	-1.948	-2.129	0.470	0.471	-1.478	-1.658
Carbon monoxide	CO*	2.17 (T)	2.25 (T)	-1.097	-1.335	0.203	0.205	-0.894	-1.130
Hydroxymethyl	CH <sub>2</sub> OH*	2.45 (T)	2.51 (T)	-1.541	-1.793	1.109	1.106	-0.432	-0.687
Hydroxymethylene	CHOH*	1.88 (B)	1.94 (B)	-3.650	-3.785	0.800	0.801	-2.850	-2.984
Isoformyl	COH*	1.47 (H)	1.47 (H)	-3.516	-3.684	0.492	0.492	-3.024	-3.192
Hydroperoxymethyl	CH <sub>2</sub> OOH*	2.52 (T)	2.50 (T)	-1.657	-1.835	1.162	1.171	-0.495	-0.664
Formic acid	CHOOH*	2.93 (T)	3.07 (T)	0.038	-0.246	0.902	0.901	0.940	0.655
Carboxyl	COOH*	2.35 (T)	2.36 (T)	-1.874	-2.139	0.616	0.616	-1.258	-1.523
Formate	CHOO*	2.29 (T-T)	2.32 (T-T)	-1.947	-2.309	0.611	0.615	-1.336	-1.694
Carbon dioxide	CO <sub>2</sub> *	3.34 (T-B)	3.45 (T-B)	0.024	-0.206	0.316	0.316	0.340	0.110

stable with the end-on configuration *via* their C atom; however, while CH<sub>2</sub>OH\*, CH<sub>2</sub>OOH\*, CHO\*, COH\*, CO\*, and COOH\* are on the top site, CHOH\* is on the bridge (B) and COH\* is on the hollow (H) with an underneath Ru atom. Exceptions are for CHOO\* and CO<sub>2</sub>\*, where they adsorb stably in the side-on configurations with the double top (T-T) site (each O atom on a T site) for CHOO\* and the T-B site (one O atom on top and the other O atom on B) for CO<sub>2</sub>\*. Especially, the CO<sub>2</sub>\* structure is in a straight configuration with an O-C-O angle of about 180°, parallel to the surface of the substrate. Table 1 also summarizes the most favourable adsorption site on the substrates' surface and the bond distance  $d_{\text{ads-sur}}$  (in columns 3 & 4). We found that the bond distance from the nearest atom of the intermediates to the surface is in the following order: hollow < bridge < top or top-top < top-bridge. The CO<sub>2</sub>\* intermediate is located at the largest distance of about 3.4 Å from the surface of the PtRuM<sub>3</sub>/C-MWCNTs (M = Fe, Co) substrates. The adsorption energy of CH<sub>3</sub>OH\*, CH<sub>2</sub>O\*, CHOOH\*, and CO<sub>2</sub>\* is positive (in column 5), which implies that these intermediates unfavourably adsorb and the other intermediates favourably adsorb with their negative adsorption energy on the surface of the PtRuFe<sub>3</sub>/C-MWCNTs. Particularly, the adsorption energy of all the intermediates (column 6) is negative on the PtRuCo<sub>3</sub>/C-MWCNTs catalyst. For each intermediate, it is more stable on PtRuCo<sub>3</sub>/C-MWCNTs than on PtRuFe<sub>3</sub>/C-MWCNTs because its adsorption energy is always more negative on M = Co than M = Fe in the range of about -0.135 eV (CHOH\*) to -0.362 eV (CHOO\*). The positive zero-point energy (in columns 7 & 8) competes with the negative adsorption energy and hence influences the stability of the intermediates adsorbed on the catalytic surface. We found the fluctuation (or zero-point energy) of each adsorption intermediate is rather large. Particularly, the fluctuation is stronger than the adsorption strength for CH<sub>3</sub>OH\*, CH<sub>2</sub>O\*, CHOOH\*, and CO<sub>2</sub>\*. Therefore, the total energy  $E_{\text{total}}$  of these intermediates becomes positive, which implies that CH<sub>3</sub>OH\*, CH<sub>2</sub>O\*, CHOOH\*, and CO<sub>2</sub>\* are unstable and subject

to desorption from the substrates' surface. Emphasizing that the intermediates in the end-on *via* O configuration, such as CH<sub>3</sub>OH\*, CH<sub>3</sub>O\*, CH<sub>2</sub>O\*, CHOOH\*, and CO<sub>2</sub>\* in the parallel structure have positive or least negative adsorption energy, indicating the adsorption *via* the O atom is not favourable, except for CHOO\*. In contrast, the other intermediates remain in a stable state even after including the fluctuation on both substrates because of the negative  $E_{\text{total}}$ . The isoformyl (COH\*) is the most stable compared to all the other intermediates, with the most negative total energy on both substrates. We also found that, generally, the trend of the adsorption positions, bond distances, and adsorption energy of the intermediates are similar for both substrates, with the adsorption being more favourable on PtRuCo<sub>3</sub>/C-MWCNTs than on PtRuFe<sub>3</sub>/C-MWCNTs. Furthermore, the adsorption energy ( $E_{\text{ads}}$ ) of formaldehyde (CH<sub>2</sub>O\*) on PtRuFe<sub>3</sub>/C-MWCNTs is insignificant, which is similar to the previous study for the adsorption of this intermediate on Pt(111).<sup>32,52</sup> Also, the adsorption strength of carbon monoxide (CO\*) is better on the PtRuCo<sub>3</sub>/C-MWCNTs surface with an adsorption energy of -1.335 eV compared to that of -1.097 eV on the PtRuFe<sub>3</sub>/C-MWCNTs surface. Interestingly, this result supports our previous experimental study, i.e., the  $j_{\text{F}}/j_{\text{r}}$  ratio of peak currents in forward and reverse directions demonstrated that the resistance to CO poisoning of PtRuFe<sub>3</sub>/C-MWCNTs is higher than that of PtRuCo<sub>3</sub>/C-MWCNTs, with  $j_{\text{F}}/j_{\text{r}}$  values of 6.9 and 4.3, respectively.<sup>31</sup> The CO\* adsorption *via* the C atom on the top of the Pt atom was also found in the experiment, which investigated the CO adsorption on the Pt(111) surface by the scanning tunnelling microscopy technique.<sup>53,54</sup>

Furthermore, we also explored the ORR intermediates on PtRuM<sub>3</sub> substrates without C-MWCNTs support. The obtained results for the adsorption site and energy, Table S1 in ESI,† are similar to those of the PtRuM<sub>3</sub>/C-MWCNTs. The most noticeable finding for the role of the C-MWCNTs support is that it enhanced the adsorption energy of the less stable intermediates



like  $\text{CH}_3\text{OH}^*$ ,  $\text{CH}_2\text{O}^*$ ,  $\text{CHOOH}^*$ , and  $\text{CO}_2^*$ , where the adsorption energy of these intermediates becomes more negative on PtRuM<sub>3</sub>/C-MWCNTs (Table 1) compared to the PtRuM<sub>3</sub> substrates (Table S1†), respectively.

### 3.2 Electronic properties

One can reveal the nature of the interaction between the intermediates and the substrates *via* the electronic structure properties such as the Bader point charge, electronic density of states, and charge density difference. The point charge is determined by the Bader partition technique<sup>55,56</sup> for the atoms of the substrate/intermediate systems; then, subtract the neutral charge of the atoms from the obtained point charge. Table 2 provides the Bader point charge of the C, O, and H atoms for each intermediate (columns 3–5), five atomic layers of metals (columns 6–10), and carbon layers of the substrate (column 11), where layer 1 is the topmost layer with the intermediates adsorbed on it. The total charge of each intermediate (column 12) is the charge summation of the C, H, and O atoms, while the total charge of the substrate (column 13) is calculated by the charge summation of the five atomic layers of metals and carbon layers of the substrate.

As seen in Table 2, for all the intermediates on both substrates, the C and H atoms always donate, and the O atoms always accumulate the negative charge (in the  $e^-$  unit). Also, the

layer-resolved charge shows that, under the adsorption of the intermediates, layer 1 of the Pt atoms and carbon layers of both substrates always gain, and the other layers of Ru, Fe, and Co atoms always lose the charge. Although the charge accumulation and donation have such a simple rule, the total charge of the intermediate and substrate shows that the gain and loss vary for different systems. The charge exchange of  $\text{CH}_2\text{O}^*$  and  $\text{CHOOH}^*$  with the substrates is ignorable because of the same magnitude, with a calculation error of  $0.005e^-$ . The  $\text{CH}_3\text{O}^*$ ,  $\text{CO}^*$ ,  $\text{COH}^*$ ,  $\text{COOH}^*$ , and  $\text{CHOO}^*$  intermediates on both substrates and  $\text{CH}_2\text{OH}^*$  on the PtRuFe<sub>3</sub>/C-MWCNTs surface exhibit large charge exchanges with the substrates (more than 10% of  $e^-$  like  $\text{CO}^*$  and  $\text{COH}^*$ , to 36% of  $e^-$  as  $\text{CH}_3\text{O}^*$ , and up to 50% of  $e^-$  such as  $\text{CHOO}^*$ ), in the magnitude order:  $\text{CHOO}^* > \text{CH}_3\text{O}^* > \text{COOH}^* > \text{COH}^* > \text{CO}^* > \text{CH}_2\text{OH}^*$  for both substrates. Also, the small charge exchange (more than  $0.005e^-$  and less than 10% of  $e^-$ ) is found for the remaining molecules, *i.e.*,  $\text{CH}_3\text{OH}^*$ ,  $\text{CHO}^*$ ,  $\text{CHOH}^*$ ,  $\text{CH}_2\text{OOH}^*$ , and  $\text{CO}_2^*$  on both substrates and  $\text{CH}_2\text{OH}^*$  on the PtRuCo<sub>3</sub>/C-MWCNTs. Particularly, while  $\text{CH}_3\text{OH}^*$ ,  $\text{CH}_2\text{OH}^*$ ,  $\text{CHOH}^*$ , and  $\text{CH}_2\text{OOH}^*$  donate, the other intermediates gain the charge from the substrates. Notably, the weak charge exchange intermediates, *i.e.*,  $\text{CH}_3\text{OH}^*$ ,  $\text{CH}_2\text{O}^*$ ,  $\text{CHOOH}^*$ , and  $\text{CO}_2^*$ , have small adsorption energies, as shown in Table 1.

**Table 2** The Bader charge transfer ( $e^-$ ) of the substrate/intermediate systems. Positive and negative values indicate the charge gain and loss, respectively. The charge summation over all the atoms of each species in the intermediate is denoted by  $\Sigma$ . The error of the charge calculation is  $0.005e^-$

Radical	PtRuM <sub>3</sub> /C-MWCNTs	C	$\Sigma\text{O}$	$\Sigma\text{H}$	Layer 1 (Pt)	Layer 2 (Ru)	Layer 3 (Fe or Co)	Layer 4 (Fe or Co)	Layer 5 (Fe or Co)	Carbon layers	Intermediate	Substrate
$\text{CH}_3\text{OH}^*$	M = Fe	-0.572	1.647	-1.134	2.939	-0.519	-2.222	-0.381	-3.769	4.011	-0.059	0.059
	M = Co	-0.643	1.669	-1.066	2.929	-1.930	-0.898	-0.345	-2.619	2.903	-0.040	0.040
$\text{CH}_3\text{O}^*$	M = Fe	-0.692	1.159	-0.113	2.512	-0.493	-2.201	-0.373	-3.769	3.970	0.354	-0.354
	M = Co	-0.705	1.160	-0.079	2.517	-1.887	-0.906	-0.349	-2.622	2.871	0.376	-0.376
$\text{CH}_2\text{O}^*$	M = Fe	-1.580	1.734	-0.155	2.909	-0.545	-2.217	-0.384	-3.768	4.006	-0.001	0.001
	M = Co	-1.632	1.756	-0.121	2.883	-1.929	-0.895	-0.344	-2.620	2.902	0.003	-0.003
$\text{CHO}^*$	M = Fe	-1.671	1.793	-0.112	2.793	-0.387	-2.217	-0.396	-3.767	3.964	0.010	-0.010
	M = Co	-1.583	1.799	-0.138	2.731	-1.790	-0.907	-0.349	-2.621	2.858	0.078	-0.078
$\text{CO}^*$	M = Fe	-1.760	1.880	—	2.665	-0.394	-2.216	-0.368	-3.768	3.961	0.120	-0.120
	M = Co	-1.736	1.870	—	2.688	-1.825	-0.906	-0.334	-2.621	2.864	0.134	-0.134
$\text{CH}_2\text{OH}^*$	M = Fe	-0.773	1.810	-1.156	2.910	-0.403	-2.218	-0.391	-3.765	3.986	-0.119	0.119
	M = Co	-0.729	1.811	-1.127	2.839	-1.804	-0.902	-0.347	-2.620	2.879	-0.045	0.045
$\text{CHOH}^*$	M = Fe	-0.862	1.915	-1.112	2.776	-0.308	-2.225	-0.391	-3.766	3.973	-0.059	0.059
	M = Co	-0.846	1.937	-1.125	2.780	-1.733	-0.917	-0.345	-2.621	2.870	-0.034	0.034
$\text{COH}^*$	M = Fe	-0.921	2.042	-1.000	2.529	-0.250	-2.234	-0.395	-3.768	3.997	0.121	-0.121
	M = Co	-0.865	2.045	-1.000	2.512	-1.685	-0.937	-0.337	-2.623	2.890	0.180	-0.180
$\text{CH}_2\text{OOH}^*$	M = Fe	-0.741	1.850	-1.183	2.876	-0.392	-2.217	-0.386	-3.766	3.959	-0.074	0.074
	M = Co	-0.625	1.840	-1.234	2.833	-1.794	-0.909	-0.346	-2.620	2.855	-0.019	0.019
$\text{CHOOH}^*$	M = Fe	-2.723	3.802	-1.084	2.924	-0.547	-2.219	-0.380	-3.767	3.994	-0.005	0.005
	M = Co	-2.675	3.768	-1.089	2.898	-1.939	-0.891	-0.341	-2.621	2.890	0.004	-0.004
$\text{COOH}^*$	M = Fe	-2.691	3.870	-1.000	2.619	-0.407	-2.222	-0.377	-3.767	3.975	0.179	-0.179
	M = Co	-2.643	3.860	-1.000	2.599	-1.821	-0.902	-0.345	-2.620	2.872	0.217	-0.217
$\text{CHOO}^*$	M = Fe	-2.783	3.366	-0.093	2.412	-0.542	-2.201	-0.362	-3.768	3.971	0.490	-0.490
	M = Co	-2.742	3.369	-0.128	2.401	-1.906	-0.909	-0.337	-2.620	2.872	0.499	-0.499
$\text{CO}_2^*$	M = Fe	-4.000	4.024	—	2.922	-0.543	-2.220	-0.379	-3.767	3.963	0.024	-0.024
	M = Co	-4.000	4.030	—	2.891	-1.925	-0.896	-0.342	-2.622	2.864	0.030	-0.030



From the above analysis, we can state that the interaction between the methanol oxidation reaction intermediates and the substrates is the charge exchange; except for  $\text{CH}_2\text{O}^*$  and  $\text{CHOOH}^*$ , the interaction should be due to the charge attraction (no charge exchange).

The subtle physical insights into the interaction of the intermediates and the substrates are also revealed *via* analysing the electronic density of states (DOS). We first present the orbital-projected DOS of the isolated intermediates to identify the location of peaks (Fig. 3) before considering their interaction with the substrates. We then show the orbital-projected DOS of the adsorbed intermediates to determine at which peaks the modification occurs the most to understand the changes in the DOS due to the substrate–adsorbate interaction (Fig. 4).

Fig. 3 shows that all the isolated intermediates have a peak near or at the Fermi level, which can be the spin-up or spin-down components or both. The  $p_x$  orbital dominates this peak for the double O intermediates such as  $\text{CH}_2\text{OOH}$ ,  $\text{CHOOH}$ ,  $\text{CHOO}$ ,  $\text{COOH}$ , and  $\text{CO}_2$ . For the other intermediates, the dominated orbital can be the  $p_y$  orbital for  $\text{CH}_3\text{OH}$ ,  $\text{CH}_2\text{OH}$ ,  $\text{CHOH}$ ,  $\text{CH}_2\text{O}$ , and  $\text{CHO}$ , and the  $p_z$  orbital for  $\text{CH}_3\text{O}$ ,  $\text{COH}$ , and  $\text{CO}$ . The  $s$  orbital contributes to the peak at the Fermi level for most of the intermediates, except for  $\text{CO}$  and  $\text{CO}_2$ . However, this contribution is much smaller than the  $p$  orbitals.

The orbital-projected electronic density of states of the substrate/intermediate systems in Fig. 4 and S2, ESI,† will assist in substantially understanding the nature of the interaction

between the intermediates and the substrates. In Fig. 4 and S2,† we plotted only the most significant orbitals near the Fermi level, in the energy range from  $-4.0$  to  $2.0$  eV. We presented the identical orbitals with the same colour, *i.e.*,  $d_{xz}$  and  $d_{yz}$  (green) and  $d_{xy}$  and  $d_{x^2-y^2}$  (black). We found that the spin-up  $d_{xz}$ ,  $d_{yz}$ , and  $d_{z^2}$  orbitals of the Pt, Ru, Co, and Fe metal atoms and all the spin-down  $d$  orbitals (*i.e.*,  $d_{xy}$ ,  $d_{x^2-y^2}$ ,  $d_{xz}$ ,  $d_{yz}$ ,  $d_{z^2}$ ) of the metal atoms dominate the DOS of the  $\text{PtRuCo}_3/\text{C-MWCNTs}$  and  $\text{PtRuFe}_3/\text{C-MWCNTs}$  substrates around the Fermi level. Notably, the orbitals of the carbon support are insignificant. The interaction between an adsorbate and an adsorbent is established by the attraction between the occupied states of the adsorbate and the unoccupied states of the adsorbent and *vice versa*. Comparing the orbital-projected DOS of the adsorbed intermediates in Fig. 4 and S2† to that of the isolated intermediates in Fig. 3, we found that the peak at the Fermi level of the isolated intermediates disappears in the adsorbed intermediates (Fig. 4) and rearranges clearly inside the valence and conduction bands. Tracking the DOS of the isolated intermediates at the Fermi level, we can conclude that the interaction between the  $p$  orbitals, *i.e.*, ( $p_x$ ,  $p_y$ ,  $p_z$ ) of all the intermediates with the  $z$ -axis projected spin-up  $d$  orbitals and all the spin-down  $d$  orbitals of the Pt, Ru, Co, and Fe atoms is the physical reason for the adsorption of the intermediates on the  $\text{PtRuM}_3/\text{C-MWCNTs}$  substrates.

Fig. 5 depicts the charge density difference of the substrate/intermediate systems, where the cyan and yellow colours present the charge depletion and accumulation, respectively.

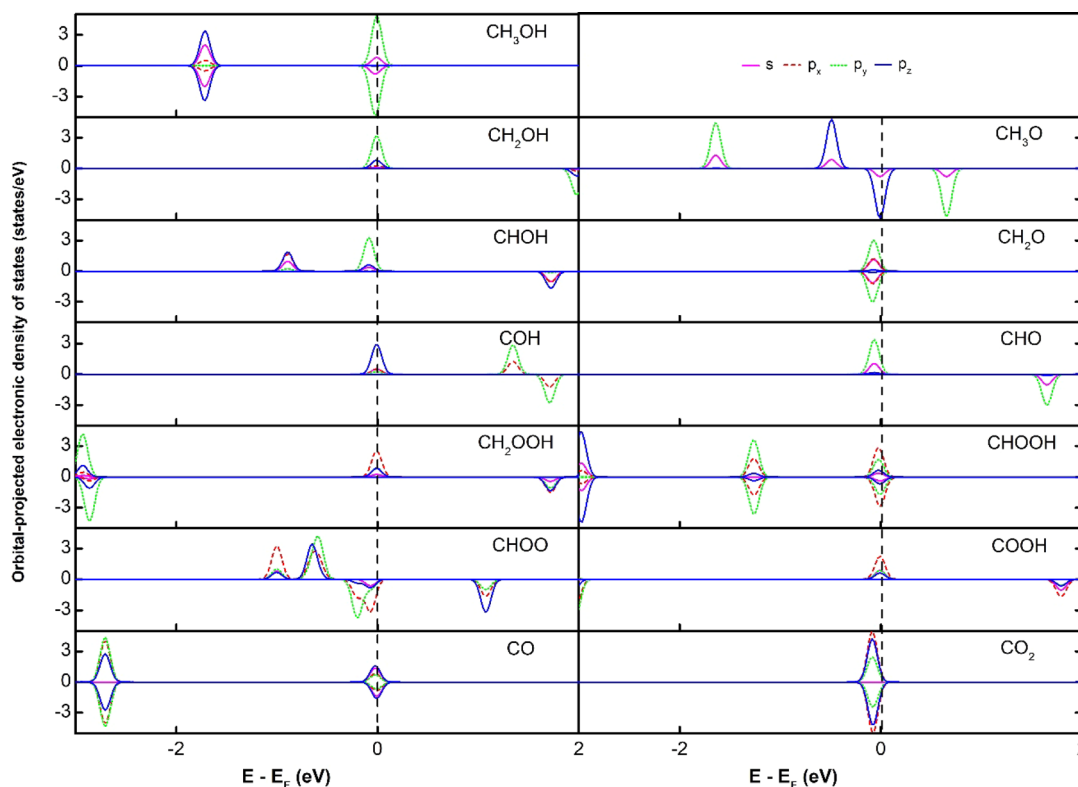


Fig. 3 The orbital-projected electronic density of states of the isolated adsorbates.



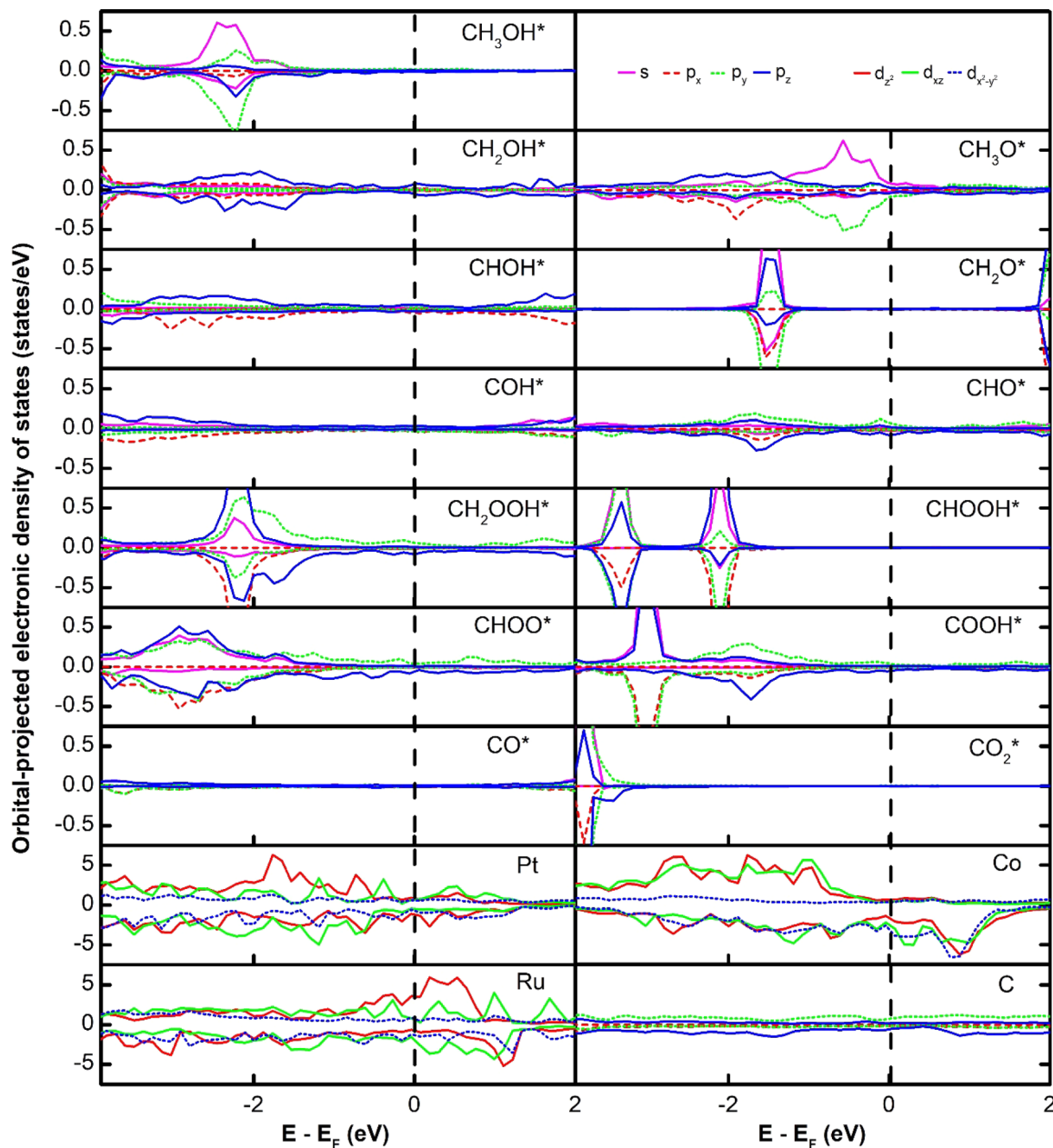


Fig. 4 The orbital-projected electronic density of states for the systems of the PtRuCo<sub>3</sub>/C-MWCNT substrate and the adsorbed intermediate:  $d_{xz}$  is identical to  $d_{yz}$ , and  $d_{xy}$  is identical to  $d_{x^2-y^2}$ . For the PtRuFe<sub>3</sub>/C-MWCNT substrate, see Fig. S2 in ESI.†

We found that the topmost Pt layer (layer 1 in Table 2) and the O atom of the intermediates always gain charge. Therefore, if the CH<sub>3</sub>OH\*, CH<sub>3</sub>O\*, CH<sub>2</sub>O\*, CHOOH\*, CO<sub>2</sub>\*, and CHOO\* intermediates approach the substrate surface, their O atom will compete with the Pt layer to gain the charge. Therefore, the interface region between the O atom and the surface will form the depletion cloud (cyan colour). This cyan cloud couples with the accumulation clouds to form charge dipoles while it simultaneously couples with the charge gain cloud of the O atom of the intermediates to form another charge dipole. Therefore, the intermediates and the substrates can establish the interaction *via* these dipoles. If the depletion cloud in the

interface region is broad, the intermediates such as CH<sub>3</sub>OH\*, CH<sub>3</sub>O\*, CH<sub>2</sub>O\*, CHOOH\*, and CO<sub>2</sub>\* compete strongly with the Pt layer. Hence, their interaction with the substrate surface becomes weak, resulting in unstable adsorption, as analysed in Subsection 3.1. Although CHOO\* also adsorbs *via* the O atoms, its charge dipoles are arranged more harmonically and equitably. The other strongly adsorbed intermediates also have characteristics similar to those of the charge arrangement of CHOO\*.

Crystal orbital Hamilton population (COHP) can also provide a better understanding of the chemical bonding strength of the intermediates to the substrate surface.<sup>57–59</sup> Fig. 6 shows the



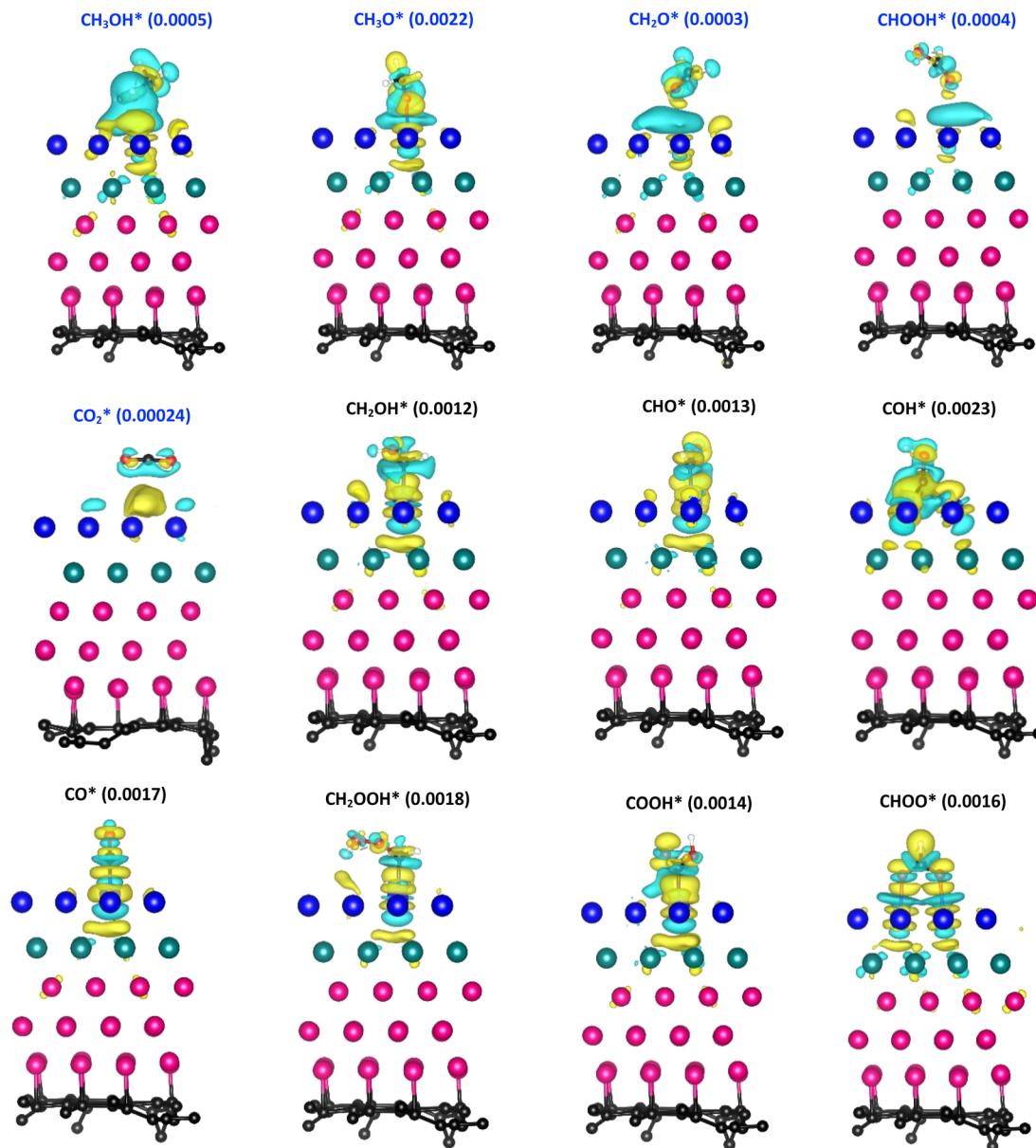
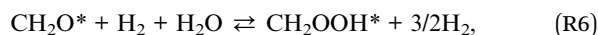
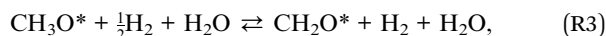
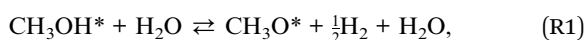


Fig. 5 The charge density difference of the systems of the adsorbed intermediate on the PtRuCo<sub>3</sub>/C-MWCNT substrate. The isosurface values are inside parentheses, with the unit being e<sup>-</sup> Å<sup>-3</sup>.

COHP, the O–Pt bond, between the oxygen atoms of the representative intermediates (CH<sub>3</sub>OH\*, CH<sub>3</sub>O\*, and CH<sub>2</sub>O\*) and the PtRuCo<sub>3</sub>/C-MWCNTs substrate. The positive and negative values of the COHP describe the binding and antibonding energy regions, respectively. The results implied that the O–Pt interaction is the strongest for CH<sub>3</sub>O\* and weakest for CH<sub>3</sub>OH\* and CH<sub>2</sub>O\*, which agrees well with the trend of their adsorption energies and the Bader charge transfers.

### 3.3 Methanol oxidation reaction mechanisms

Fig. 2 presents the possible reaction pathways on the surface of the PtRuM<sub>3</sub>/C-MWCNTs substrates, which are expressed in detail through the following intermediate reactions:



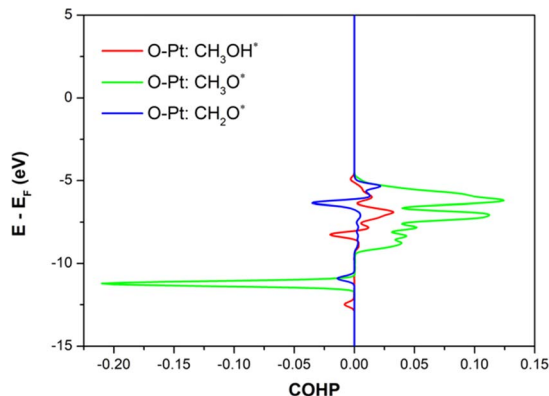
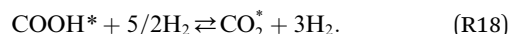
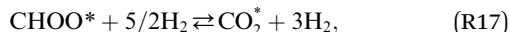
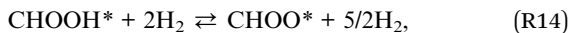


Fig. 6 The crystal orbital Hamilton population of the O–Pt bonding interaction between the intermediates ( $\text{CH}_3\text{OH}^*$ ,  $\text{CH}_3\text{O}^*$ , and  $\text{CH}_2\text{O}^*$ ) and the  $\text{PtRuCo}_3/\text{C-MWCNT}$  substrate.



The formula to calculate the Gibbs free energy for each intermediate step from (R1)–(R18) is presented as follows<sup>60</sup>

$$\Delta G_i(U) = G_{iR}(U) - G_{iL}(U) = \Delta G_i(0) + eU, \quad (5)$$

$$\Delta G_i(0) = G_{iR}(0) - G_{iL}(0). \quad (6)$$

where  $i$  runs from (R1)–(R18). L and R denote the left and right sides of each intermediate step, from (R1)–(R18).  $G_i$  and  $\Delta G_i$  indicate the Gibbs free energy for one side of the reaction and the whole intermediate step, respectively.

To identify the favourable reaction pathways, we calculated the Gibbs free energy ( $\Delta G$ )<sup>61</sup> for all intermediate steps from (R1)–(R18) with zero-point energies provided in Table 1. To do that, we first have to attain the values of the Gibbs free energy  $G_{iL}$  and  $G_{iR}$  as listed in Table 3 for the applied potential  $U = 0$  V. We then calculate  $\Delta G_i(0)$ , following eqn (6), for the applied potential  $U = 0$  V, and determine  $\Delta G_i(U)$ , following eqn (5), for  $U = 1.005$  V. Fig. 7 and 8 depict the Gibbs free energy diagrams for methanol oxidation reaction on the  $\text{PtRuFe}_3/\text{C-MWCNTs}$  and  $\text{PtRuCo}_3/\text{C-MWCNTs}$  substrates at the applied potentials  $U = 0$  and  $1.005$  V, respectively.

We first analyse the reaction mechanisms of methanol oxidation on the  $\text{PtRuFe}_3/\text{C-MWCNTs}$  substrate at the applied potential  $U = 0$  V, see Fig. 7a and Table 4. Note that we did not study transition states for the intermediate steps in the present work. In the forward direction, Fig. 7 shows the possible pathways: path 1 converts  $\text{CH}_3\text{OH} \rightarrow \text{CH}_3\text{OH}^* \rightarrow \text{CH}_2\text{OH}^* \rightarrow \text{CH}_2\text{O}^*/\text{CHOH}^* \rightarrow \text{CHO}^* \rightarrow \text{CHOOH}^* \rightarrow \text{CHOO}^*/\text{COOH}^* \rightarrow \text{CO}_2^*$  going uphill from  $\text{CH}_3\text{OH} \rightarrow \text{CH}_3\text{OH}^* \rightarrow \text{CH}_2\text{OH}^* \rightarrow \text{CH}_2\text{O}^*$  and  $\text{CHO}^* \rightarrow \text{CHOOH}^* \rightarrow \text{CHOO}^*$ , where the rate-limiting step occurs at the methanol adsorption step ( $\text{CH}_3\text{OH} \rightarrow \text{CH}_3\text{OH}^*$ ) with the thermodynamic barrier of 0.513 eV (see Table 4). Path 2 transforms  $\text{CH}_3\text{OH} \rightarrow \text{CH}_3\text{OH}^* \rightarrow \text{CH}_2\text{OH}^* \rightarrow \text{CH}_2\text{O}^*/\text{CHOH}^* \rightarrow \text{CHO}^*/\text{COH}^* \rightarrow \text{CO}^* \rightarrow \text{COOH}^* \rightarrow \text{CO}_2^*$ , which goes uphill from  $\text{CH}_3\text{OH} \rightarrow \text{CH}_3\text{OH}^* \rightarrow \text{CH}_2\text{OH}^* \rightarrow \text{CH}_2\text{O}^*/\text{CHOH}^*$  and  $\text{CO}^* \rightarrow \text{COOH}^*$ , where the rate-limiting step happens at the carbon monoxide to carboxyl converting step ( $\text{CO}^* \rightarrow \text{COOH}^*$ ) with the thermodynamic barrier of 0.786 eV on  $\text{PtRuFe}_3/\text{C-MWCNTs}$  (see Table 4). Path 3:  $\text{CH}_3\text{OH} \rightarrow \text{CH}_3\text{OH}^* \rightarrow \text{CH}_3\text{O}^* \rightarrow \text{CH}_2\text{O}^* \rightarrow \text{CHO}^*$

Table 3 The Gibbs free energy  $G_{iL}$  and  $G_{iR}$  (eV) of the intermediate steps on the  $\text{PtRuM}_3/\text{C-MWCNTs}$  ( $M = \text{Fe}$  and  $\text{Co}$ ) substrates at an applied potential ( $U$ ) of 0 V, pressure of 1 bar, and temperature of 300 K

Intermediate step	$\text{PtRuFe}_3/\text{C-MWCNTs}$	$\text{PtRuCo}_3/\text{C-MWCNTs}$
$\text{CH}_3\text{OH}^* + \text{H}_2\text{O}$	0.513	0.167
$\text{CH}_3\text{O}^* + 1/2\text{H}_2 + \text{H}_2\text{O}$	1.357	1.037
$\text{CH}_2\text{OH}^* + 1/2\text{H}_2 + \text{H}_2\text{O}$	0.653	0.388
$\text{CH}_2\text{O}^* + \text{H}_2 + \text{H}_2\text{O}$	1.084	0.792
$\text{CHOH}^* + \text{H}_2 + \text{H}_2\text{O}$	1.127	0.641
$\text{CHO}^* + 3/2\text{H}_2 + \text{H}_2\text{O}$	0.508	0.398
$\text{COH}^* + 3/2\text{H}_2 + \text{H}_2\text{O}$	0.879	0.716
$\text{CH}_2\text{OOH}^* + 3/2\text{H}_2$	3.696	3.503
$\text{CO}^* + 2\text{H}_2 + \text{H}_2\text{O}$	0.003	−0.260
$\text{CHOOH}^* + 2\text{H}_2$	0.835	0.548
$\text{CHOO}^* + 5/2\text{H}_2$	0.997	0.634
$\text{COOH}^* + 5/2\text{H}_2$	0.789	0.453
$\text{CO}_2^* + 3\text{H}_2$	0.329	0.033



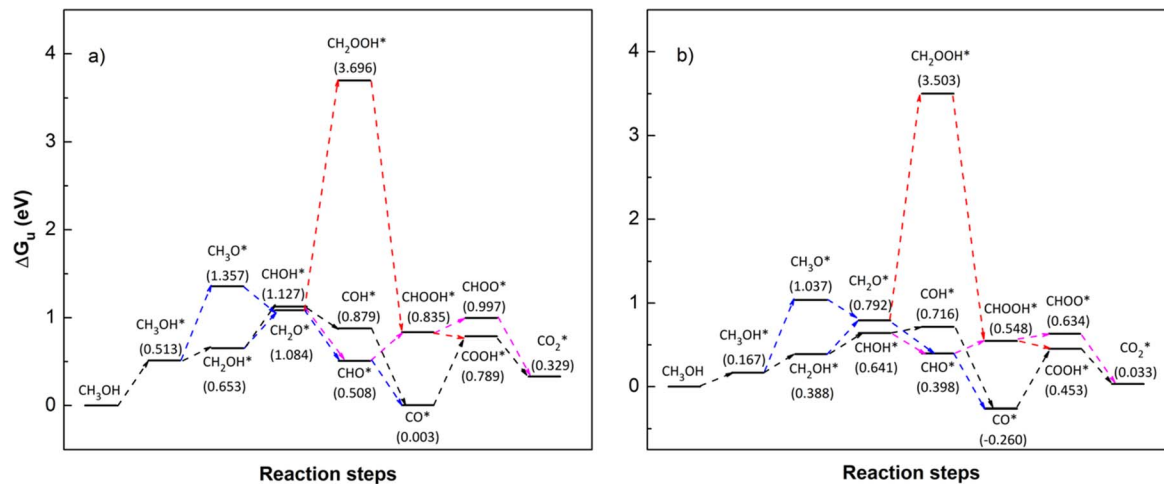


Fig. 7 Gibbs free energy diagram for the methanol oxidation reaction on (a) PtRuFe<sub>3</sub>/C-MWCNT and (b) PtRuCo<sub>3</sub>/C-MWCNT substrates at an applied potential ( $U$ ) of 0 V, a pressure of 1 bar, and a temperature of 300 K. For simplicity, the hydrogen and water molecules in each step have been omitted in the diagrams. Relative Gibbs free energy (eV) is in parenthesis.

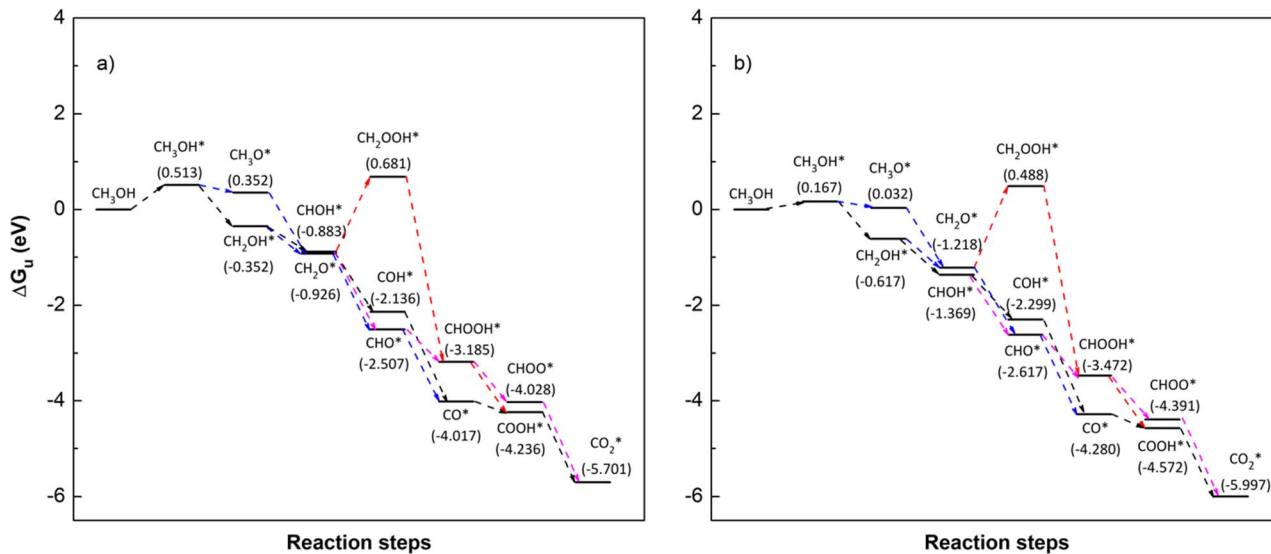


Fig. 8 Gibbs free energy diagram for the methanol oxidation reaction on (a) PtRuFe<sub>3</sub>/C-MWCNT and (b) PtRuCo<sub>3</sub>/C-MWCNT substrates at an applied potential ( $U$ ) of 1.005 V, pressure of 1 bar, and temperature of 300 K. For simplicity, the hydrogen and water molecules in the reaction equations have been omitted in the diagrams. Relative Gibbs free energy (eV) is in parenthesis.

$\rightarrow$ CHOOH\*/CO\* $\rightarrow$ CHOO\*/COOH\* $\rightarrow$ CO<sub>2</sub>\* with the rate-limiting step taking place at the methanol to methoxy transforming step (CH<sub>3</sub>OH\*  $\rightarrow$  CH<sub>3</sub>O\*) with a thermodynamic barrier of 0.844 eV (Table 4). Path 4: CH<sub>3</sub>OH $\rightarrow$ CH<sub>3</sub>OH\* $\rightarrow$ CH<sub>3</sub>O\*/CH<sub>2</sub>OH\* $\rightarrow$ CH<sub>2</sub>O\* $\rightarrow$ CH<sub>2</sub>OOH\* $\rightarrow$ CHOOH\* $\rightarrow$ CHOO\*/COOH\* $\rightarrow$ CO<sub>2</sub>\* with the rate-limiting step occurs at the formaldehyde to hydroperoxymethyl converting step (CH<sub>2</sub>O\*  $\rightarrow$  CH<sub>2</sub>OOH\*) with a thermodynamic barrier of 2.612 eV. We can see that the four reaction pathways are found not only on the PtRuFe<sub>3</sub>/C-MWCNTs but also on the PtRuCo<sub>3</sub>/C-MWCNTs substrate. However, the rate-limiting step of path 1 occurs at the hydroxymethyl to formaldehyde transforming step (CH<sub>2</sub>OH\*  $\rightarrow$  CH<sub>2</sub>O\*) on the PtRuCo<sub>3</sub>/C-MWCNTs substrate, which is

different from that on the PtRuFe<sub>3</sub>/C-MWCNTs surface. The highest thermodynamic barrier ( $E_b$ ) for path 1, path 2, path 3, and path 4 on the PtRuCo<sub>3</sub>/C-MWCNTs substrate is 0.404, 0.713, 0.870, and 2.711 eV, respectively. According to the Arrhenius equation for calculating the reaction-rate constant ( $R$ ),  $R \sim \exp(-E_b/RT)$ , the lower the barrier, the higher the favourable order of the reaction pathway should be. We found that the favourable order of reaction pathways is path 1 > path 2 > path 3 > path 4 for both substrates. By comparing the energy barrier for each path, we found that path 1 and path 2 of the methanol oxidation reaction are more favourable on PtRuCo<sub>3</sub>/C-MWCNTs than on PtRuFe<sub>3</sub>/C-MWCNTs, while path 3 and path 4 are slightly less favourable on PtRuCo<sub>3</sub>/C-MWCNTs. Notably, path 4 has a very high thermodynamic barrier, which perhaps



**Table 4** The thermodynamic barrier (eV) of the intermediate steps on the PtRuM<sub>3</sub>/C-MWCNTs (M = Fe, Co) substrates at the applied potential  $U = 0$  V, pressure of 1 bar, and temperature of 300 K. The rate-limiting step is marked by bold font. The highest thermodynamic barrier for each pathway is presented in parentheses

Intermediate step	PtRuFe <sub>3</sub> /C-MWCNTs	PtRuCo <sub>3</sub> /C-MWCNTs
CH <sub>3</sub> OH + H <sub>2</sub> O → CH <sub>3</sub> OH* + H <sub>2</sub> O	<b>0.513 (path 1)</b>	0.167
CH <sub>3</sub> OH* + H <sub>2</sub> O → CH <sub>3</sub> O* + 1/2H <sub>2</sub> + H <sub>2</sub> O	<b>0.844 (path 3)</b>	<b>0.870 (path 3)</b>
CH <sub>3</sub> OH* + H <sub>2</sub> O → CH <sub>2</sub> OH* + 1/2H <sub>2</sub> + H <sub>2</sub> O	0.140	0.221
CH <sub>3</sub> O* + 1/2H <sub>2</sub> + H <sub>2</sub> O → CH <sub>2</sub> O* + H <sub>2</sub> + H <sub>2</sub> O	−0.273	−0.245
CH <sub>2</sub> OH* + 1/2H <sub>2</sub> + H <sub>2</sub> O → CH <sub>2</sub> O* + H <sub>2</sub> + H <sub>2</sub> O	0.431	<b>0.404 (path 1)</b>
CH <sub>2</sub> OH* + 1/2H <sub>2</sub> + H <sub>2</sub> O → CHO* + H <sub>2</sub> + H <sub>2</sub> O	0.474	0.253
CH <sub>2</sub> O* + H <sub>2</sub> + H <sub>2</sub> O → CH <sub>2</sub> OOH* + 3/2H <sub>2</sub>	<b>2.612 (path 4)</b>	<b>2.711 (path 4)</b>
CH <sub>2</sub> O* + H <sub>2</sub> + H <sub>2</sub> O → CHO* + 3/2H <sub>2</sub> + H <sub>2</sub> O	−0.576	−0.394
CHOH* + H <sub>2</sub> + H <sub>2</sub> O → CHO* + 3/2H <sub>2</sub> + H <sub>2</sub> O	−0.619	−0.243
CHOH* + H <sub>2</sub> + H <sub>2</sub> O → COH* + 3/2H <sub>2</sub> + H <sub>2</sub> O	−0.248	0.075
CH <sub>2</sub> OOH* + 3/2H <sub>2</sub> → CHOOH* + 2H <sub>2</sub>	−2.861	−2.955
CHO* + 3/2H <sub>2</sub> + H <sub>2</sub> O → CHOOH* + 2H <sub>2</sub>	0.327	0.150
CHO* + 3/2H <sub>2</sub> + H <sub>2</sub> O → CO* + 2H <sub>2</sub> + H <sub>2</sub> O	−0.505	−0.658
COH* + 3/2H <sub>2</sub> + H <sub>2</sub> O → CO* + 2H <sub>2</sub> + H <sub>2</sub> O	−0.876	−0.976
CHOOH* + 2H <sub>2</sub> → CHOO* + 5/2H <sub>2</sub>	0.162	0.086
CHOOH* + 2H <sub>2</sub> → COOH* + 5/2H <sub>2</sub>	−0.046	−0.095
CO* + 2H <sub>2</sub> + H <sub>2</sub> O → COOH* + 5/2H <sub>2</sub>	<b>0.786 (path 2)</b>	<b>0.713 (path 2)</b>
CHOO* + 5/2H <sub>2</sub> → CO <sub>2</sub> * + 3H <sub>2</sub>	−0.668	−0.601
COOH* + 5/2H <sub>2</sub> → CO <sub>2</sub> * + 3H <sub>2</sub>	−0.460	−0.420

prohibits the methanol oxidation reaction from proceeding on both substrates.

From the above analysis, our results exhibited that, for  $U = 0$  V, path 1 is the most favourable mechanism: CH<sub>3</sub>OH → CH<sub>3</sub>OH\* → CH<sub>2</sub>OH\* → CH<sub>2</sub>O\*/CHOH\* → CHO\* → CHOOH\* → CHOO\*/COOH\* → CO<sub>2</sub> on both substrates. Compared to the literature, our result is different from the work of Lv *et al.*,<sup>35</sup> where they found that the most favourable mechanism for the methanol oxidation on Pt and PtNi catalysts should proceed *via* the CO\* formation, *i.e.*, CH<sub>3</sub>OH\* → CH<sub>2</sub>OH\* → CHOH\* → COH\* → CO\* → COOH\* → CO<sub>2</sub>. Besides, the most favourable pathway on PtRu/Pt(111) in the research of Ding *et al.*,<sup>42</sup> is CH<sub>3</sub>OH\* → CH<sub>3</sub>O\* → CH<sub>2</sub>O\* → CHO\* → HCOOH\* → COOH\* → CO<sub>2</sub>, where forming CH<sub>3</sub>O\* does not result in the most favourable mechanism for the PtRuCo<sub>3</sub>/C-MWCNTs and PtRuFe<sub>3</sub>/C-MWCNTs substrates in our present work. The most favourable reaction pathway (path 1) in this study supports the previous experiments that PtRuCo<sub>3</sub>/C-MWCNTs and PtRuFe<sub>3</sub>/C-MWCNTs catalysts have higher tolerances to CO poisoning compared to the Pt-based bimetallic alloys.<sup>31,62</sup>

At the experimental condition,  $U = 1.005$  V relative to the hydrogen standard electrode, Fig. 8 shows that all of path 1, path 2, and path 3 are going downhill after the uphill step at CH<sub>3</sub>OH → CH<sub>3</sub>OH\*. Therefore, all three pathways have the same rate-limiting step at CH<sub>3</sub>OH → CH<sub>3</sub>OH\* and the same thermodynamic barrier of 0.513 eV and 0.167 eV on both PtRuCo<sub>3</sub>/C-MWCNTs and PtRuFe<sub>3</sub>/C-MWCNTs substrates, respectively. The barrier on PtRuCo<sub>3</sub>/C-MWCNTs is three times lower than that on PtRuFe<sub>3</sub>/C-MWCNTs, implying that the third metal component Co offers a significantly better performance over Fe. Interestingly, this result is consistent with our experiment,<sup>31</sup> where PtRuCo<sub>3</sub>/C-MWCNTs showed a considerably

higher methanol oxidation peak and significantly lower electron transfer resistance compared to PtRuFe<sub>3</sub>/C-MWCNTs. Besides, path 4 has the rate-limiting step occurring at the converting step from formaldehyde to hydroperoxymethyl (CH<sub>2</sub>O\* → CH<sub>2</sub>OOH\*), which is the same as that at the applied potential  $U = 0$  V; however, the activation barrier of 1.607 and 1.705 eV on the PtRuCo<sub>3</sub>/C-MWCNTs and PtRuFe<sub>3</sub>/C-MWCNTs surfaces, respectively. Also, the activation barrier for path 4 at  $U = 1.005$  V is significantly lower than that at  $U = 0$  V.

We also calculated the Gibbs free energy and studied Gibbs free energy diagrams at the applied potentials of  $U = 0$  V and 1.005 V for the methanol oxidation reaction on PtRuM<sub>3</sub> catalysts without the C-MWCNTs support. The Gibbs free energy diagrams are also similar to those on the PtRuM<sub>3</sub>/C-MWCNTs; however, the activation barrier differs. Comparing Tables 4 and S2† shows that, in the presence of the C-MWCNTs support, this value at  $U = 0$  V increases for path 1, path 2 and decreases for path 3, path 4 on PtRuM<sub>3</sub>/C-MWCNTs (M = Fe and Co). At  $U = 1.005$  V, the energy barrier for the three most favourable pathways (path 1, path 2, and path 3; three paths have the same energy barrier for each metal M = Fe and Co) on PtRuM<sub>3</sub> substrates is 0.417 eV (Fe) and 0.376 eV (Co), and that for the most unfavourable one (*via* CH<sub>2</sub>OOH\*) is 1.732 eV (Fe) and 1.953 eV (Co). We found that the C-MWCNTs support increases the activation barrier for the three most favourable paths on PtRuFe<sub>3</sub>/C-MWCNTs, while it decreases for all the other cases. Therefore, the C-MWCNTs support plays a better role for the PtRuCo<sub>3</sub>/C-MWCNTs.

## 4 Conclusions

Using density functional theory calculations, we searched for the possible intermediates of methanol oxidation reaction on



the surface of PtRuM<sub>3</sub>/C-MWCNTs (M = Fe and Co) substrates. Most intermediates stably adsorb except for methanol, formaldehyde, formic acid, and carbon dioxide. The interaction between the intermediates and the substrates is due to the charge exchange for all intermediates, excluding the electrostatic attraction with CH<sub>2</sub>O and CHOOH, which mainly stems from the p orbitals of the intermediates interacting with the z-axis projected spin-up components of and all the spin-down component of the d orbitals of the Pt, Ru, Co, and Fe atoms. The Gibbs free energy diagram showed four possible reaction pathways for the methanol oxidation on the PtRuM<sub>3</sub>/C-MWCNTs (M = Fe and Co) substrates. At the applied potential of 0 V, three most favourable mechanisms with different activation barriers on each substrate are (path 1) CH<sub>3</sub>OH → CH<sub>3</sub>OH\* → CH<sub>2</sub>OH\* → CH<sub>2</sub>O\*/CHOH\* → CHO\* → CHOOH\* → CHOO\*/COOH\* → CO<sub>2</sub>, (path 2) CH<sub>3</sub>OH → CH<sub>3</sub>OH\* → CH<sub>2</sub>OH\* → CH<sub>2</sub>O\*/CHOH\* → CHO\*/COH\* → CO\* → COOH\* → CO<sub>2</sub>, and (path 3) CH<sub>3</sub>OH → CH<sub>3</sub>OH\* → CH<sub>2</sub>OH\* → CH<sub>2</sub>O\*/CHOH\* → CHO\*/COH\* → CO\* → COOH\* → CO<sub>2</sub>. However, at the working potential of 1.005 V, these pathways have the same downhill behaviour, with the highest thermodynamic barrier occurring at the methanol adsorption step, CH<sub>3</sub>OH → CH<sub>3</sub>OH\*. Three pathways have the same energy barrier of 0.513 and 0.167 eV for the PtRuFe<sub>3</sub>/C-MWCNTs and PtRuCo<sub>3</sub>/C-MWCNTs substrates, respectively. This result implied that the performance of PtRuCo<sub>3</sub>/C-MWCNTs is better than that of PtRuFe<sub>3</sub>/C-MWCNTs. This study only considered the low coverage of reaction intermediates. However, further investigation of the effects of coverages is necessary for understanding a full physical picture of the interaction between the intermediates and the substrate surface, which will be a research topic for future studies.

## Data availability

The data supporting this article have been included as part of the ESI.†

## Author contributions

Conceptualization (DNS), formal analysis (DNS, DLQ), investigation (DLQ, DNS), resources (DNS, VC), supervision (DNS, VC), validation (DNS, DLQ, VC), visualization (DLQ), writing manuscript (DNS, DLQ), reviewing and editing (DNS, VC).

## Conflicts of interest

There are no conflicts of interest to declare.

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