


 Cite this: *RSC Adv.*, 2024, 14, 20735

Study of optical rotation based on the molecular structure in fused oligomers of macrocycles†

 Ryo Katoono, * Yudai Obara, Kazuki Sakamoto and Rei Miyashita

We designed a unique oligomer form in which several helically twisted macrocycles (*M*- or *P*-helicity) are arranged through fusion. We investigated the optical rotation of a series of fused oligomers of macrocycles with a difference in the number and arrangement of elements associated with point-chiral auxiliary. Some oligomers cooperatively attained a situation where an identical sense of twisting was preferred throughout the entire molecule. On the basis of these results, we estimated diastereomeric excess induced in each oligomer. We revealed that the molar optical rotation per element was modulated with a rotational angle between elements: an increase *via* 0° rotational arrangement, a decrease *via* 180° rotational arrangement, or a decrease *via* cyclic arrangement. Alternatively, for other oligomers in which several diastereomeric conformers coexist, we uniquely attempted to consider the optical rotation based on the molecular structure through the assessment of a change ratio of the absorption dissymmetry factor before and after complexation with an achiral guest. We found that molar optical rotation could be different based on the arrangement, although actual measured values were similar.

 Received 20th May 2024
 Accepted 16th June 2024

DOI: 10.1039/d4ra03709j

rsc.li/rsc-advances

Introduction

The term oligomer refers to a molecule composed of multiple repeats of a small molecule (monomer). A typical case is known as so-called linear-chained oligomers (Scheme 1a),^{1–4} in which the structure of a small molecule is invariant and a rotatable bond is used to link the monomers. The conformational control of such a linear-chained oligomer is attained by an accumulative result of multiple controls of local conformation (*e.g.*, dihedral angle) about the rotatable linkage since the monomer is invariant. The term can cover another form of oligomers,^{5–8} for example, in which the monomer is a macrocycle arranged in a rotation-restrained manner.^{6–8} We are particularly interested in a unique case in which the macrocyclic monomer is variant in terms of chirality^{9–13} (Scheme 1b). The conformational control of such a fused oligomer of macrocycles would be attained by an accumulative result of multiple controls of local conformation (*e.g.*, dynamic chiral sense of twisting) in each macrocyclic element since the linkage is invariant. In such fused oligomers of macrocycles, there are cases where all elements prefer the same sense throughout the entire molecule (for descriptive purposes, we call this a “homochiral” situation)^{10–12} or different senses coexist (“heterochiral”

situations)¹³ in a molecule. Such conformational interinfluence could be a driving force for a molecule to predominantly adopt a particular conformation among multiple conformations.^{14,15} It should be noted that conformational interinfluence can lead to a homochiral situation and sometimes a specific heterochiral situation (Scheme 1b, controlled). If each macrocyclic element has no preference for a particular sense of twisting and no interinfluence could work between elements, multiple conformers with an identical and different sense of twisting would be statistically populated in the solution (Scheme 1b, less controlled).

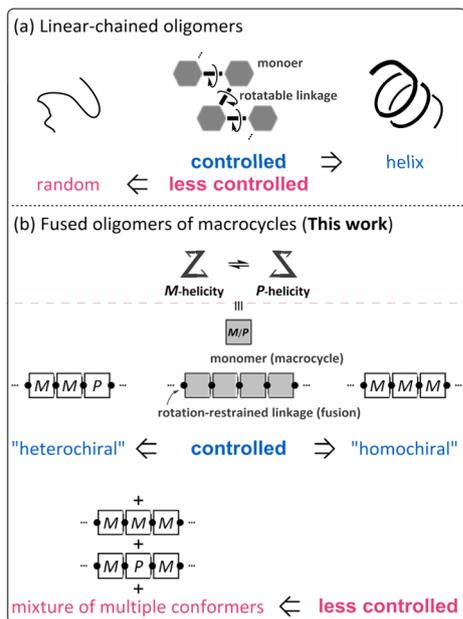
We assumed diverse arrangements of elements: rotational, acyclic, and cyclic (Scheme 2), which present diverse chiral architectures. This point would be an advantage of this oligomer system for studying optical rotation based on the molecular structure. This work investigated the molar optical rotation per element ($[M]_D/N$, *N*: number of macrocyclic elements) of a series of fused oligomers with a difference in the number and arrangement of elements. Attention should be paid to the fact that the correlation between the chiroptical values of a monomer and its oligomers is not settled on solid ground. The chiroptical value would be affected by molecular size, shape (number and arrangement of chromophores), and diastereomeric ratios. Therefore, discussing the chiroptical values would not be valid based solely on how an actual measured value is larger or smaller than a monomer. We should pay more attention to both minor and the most major conformers for dynamic chiral molecules, especially in less controlled cases (Scheme 1b).

As a monomer of fused oligomers, we used a macrocycle (**1**)⁹ that can adopt two chiral forms with *P*- or *M*-helicity by twisting

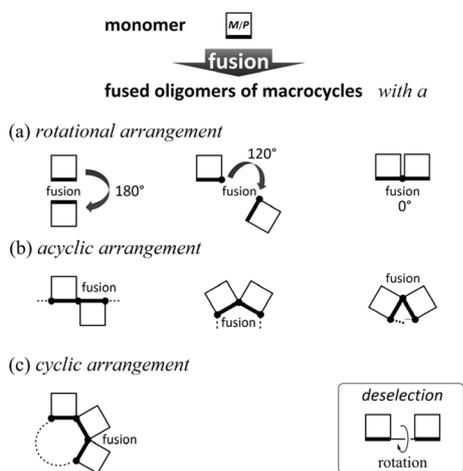
Department of Chemistry, Faculty of Science, Hokkaido University, Sapporo 060-0810, Japan. E-mail: katoono@sci.hokudai.ac.jp; Tel: +81 11 706-4616

† Electronic supplementary information (ESI) available: [ESI_1] details of conformational searches, spectroscopic measurements (NMR, UV, and CD) and complexation experiments (Fig. S1–S27), and experimental details of new compound synthesis (Schemes S1–S3); [ESI_2] copies of ¹H/¹³C NMR spectra and LRMS of new compounds. See DOI: <https://doi.org/10.1039/d4ra03709j>





Scheme 1 Types of oligomers: (a) linear-chained oligomers and (b) fused oligomers of macrocycles.



Scheme 2 Diverse arrangements of dynamic chiral macrocyclic elements: (a) rotational, (b) acyclic, and (c) cyclic.

clockwise or counterclockwise (Fig. 1). As previously reported, these two helical forms are conformationally interconvertible in solution. The population can be estimated using a diastereomeric ratio by NMR spectroscopy. Thus, we arranged the macrocyclic element covalently in a single molecule through ring fusion of a part of the element (2–11) (Fig. 2). These fused oligomers would exist as a mixture of multiple conformers in solution according to the helical sense of each element (e.g., M_2 , M_1P_1 , and P_2 from two elements; M_3 , M_2P_1 , M_1P_2 , and P_3 from three elements, etc.). If we could determine the population of multiple conformers that coexist in a solution, a measured value would be interpreted according to the population. However, it is not always easy when the number of elements increases.

If only a single pair of diastereomeric (pseudo-enantiomeric) conformers with M - or P -helicity could be present in the solution (Scheme 1b, controlled), that would be suitable for estimating the population as a diastereomeric ratio (M_N/P_N), as with a monomeric case ($N = 1$). This was the case for 2,¹⁰ 4,¹¹ 5, 10,¹² and 11.¹² Fortunately, the diastereomeric ratio was quantitatively estimated for 2, 4, and 5. This allowed us to discuss their optical rotations based on their molecular structure and found that the molar optical rotation could be modulated at a rotational angle between elements.

Alternatively, multiple pairs of diastereomers can be present in equilibrium (3 and 6–8¹²) (Scheme 1b, less controlled). In such a solution, chiroptical values would be obtained as an average property resulting from contributions from all conformations, for which it is impossible to consider as-measured values based solely on a particular conformation. Here, we uniquely attempted to evaluate optical rotations emerging from even such an indefinite system due to the coexistence of multiple conformers, suggesting that a rotational angle between elements could contribute to a difference in the molar optical rotation of tris(macrocycle)s 6–8.

Conformational analyses of the fused oligomers of macrocycles in solution were primarily based on NMR spectroscopy, and we measured optical rotation^{5,16–22} and electronic circular dichroism (CD).^{5,16}

Results and discussion

Synthesis of fused oligomers of macrocycles

We synthesized a series of fused oligomers of macrocycles 2–11 (Fig. 2) based on a simple and versatile strategy that involved a multi-fold ring-closing condensation reaction of a couple of anilines with terephthaloyl chloride (Scheme 3). The precursor anilines were obtained in a TFA-protected form, which was used as a control of the corresponding macrocycle in optical rotation measurements (pr-1–pr-11). Bis-, tris- or tetrakis(macrocycle) 3, 5, 6, and 8 were newly synthesized here (ESI_1, Schemes S1–S3) (ESI_2)† and analyzed along with other analogs.

¹H NMR spectra of fused oligomers of macrocycles

To consider an innate conformational preference (homochiral or heterochiral) in each framework without any chiral auxiliary, we implemented conformational searches with model molecules 2M–11M [$X = \text{CH}_3$] using software summarized in the ESI (ESI_1, Fig. S1–S6).† In solution, conformational preferences of 2–11 with chiral auxiliaries [$X = (R)\text{-CH}(\text{CH}_3)(\text{cHex})$] would be modulated by cooperation or competition between such an innate preference of the framework and accumulative helical-sense preferences induced in each macrocyclic element by the intramolecular transmission of point chirality (R).

NMR spectroscopy would be an effective tool for estimating a ratio of conformers when both major and minor peaks could stand separately within an NMR timescale. The ¹H NMR spectrum of 1, measured at room temperature, showed only one set of averaged resonances, indicating that two twisted forms (M -1 and P -1) interconverted within the timescale (Fig. 3, S7, and



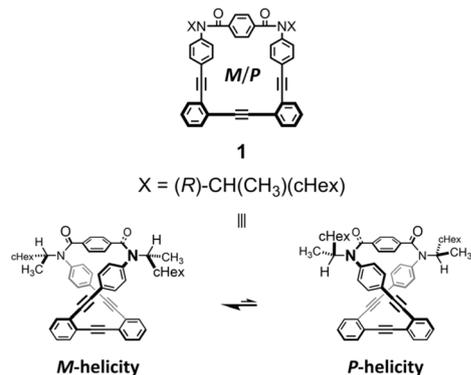


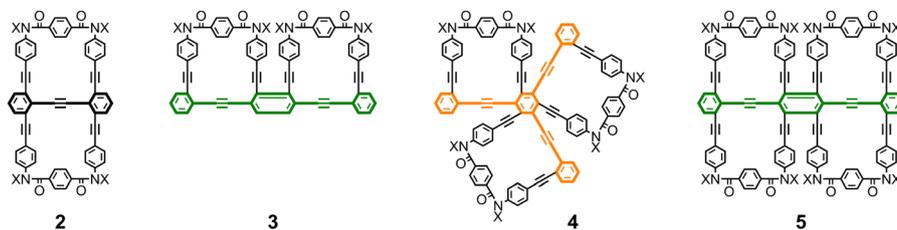
Fig. 1 Chemical structure of chiral macrocyclic element **1**⁹ ($N = 1$) and conformational interconversion between two chiral forms with M - or P -helicity.

S8†). Alternatively, in the spectrum of **2** (Fig. 3, S7, and S9†), two sets of resonances ($\alpha + \beta$) were present and assigned to diastereomeric conformers of MM -**2** (α) and PP -**2** (β). These independent chemical shifts for methine protons ($H\alpha$: 4.588 ppm and

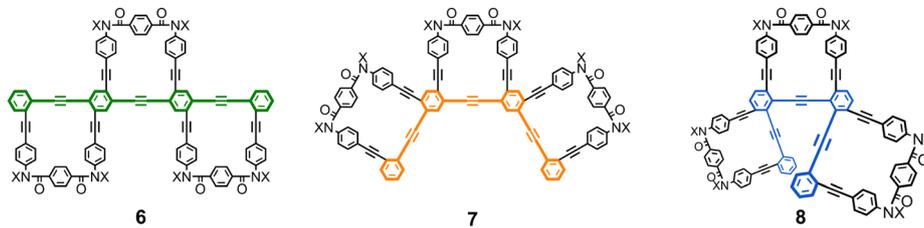
$H\beta$: 4.375 ppm)²³ were revealed to assume a central value. According to this value, we found an averaged signal for the corresponding protons in **1** that appeared downfield. This was also the case for other fused macrocycles **3**, **4**, **6**, **7**, and **9**, indicative of fast interconversions among conformers. While for **5** (Fig. 3, S7, S10, and S11†) and partly for **8** (Fig. 3, S7, S12, and S13†), such interconversion slowed, such as in **2**. Though it could not be assigned to a particular (homochiral or heterochiral) conformation of **10** or **11**, the coexistence of two forms with M - or P -helicity (in a conformer or among conformers) was confirmed at room temperature. Based on chemical exchanges in ¹H NMR spectroscopy (Fig. S14†), we reported that the diastereomeric ratio (α/β) induced at 223 K in chloroform was estimated to be 2.3 for M -**1** and P -**1**, 4.7 for MM -**2** and PP -**2**, and 9.9 for MMM -**4** and PPP -**4** by linear extrapolation.¹¹ In a similar manner, the value of α/β was estimated to be ca. 51 for $MMMM$ -**5** and $PPPP$ -**5** (Fig. S10 and Table S1†).

Alternatively, in the VT-NMR spectra of bis(macrocyclic) **3** (Fig. S15 and S16†), lowering temperatures revealed that a heterochiral conformer (MP), as well as a diastereomeric pair of homochiral conformers (MM and PP), was involved in the

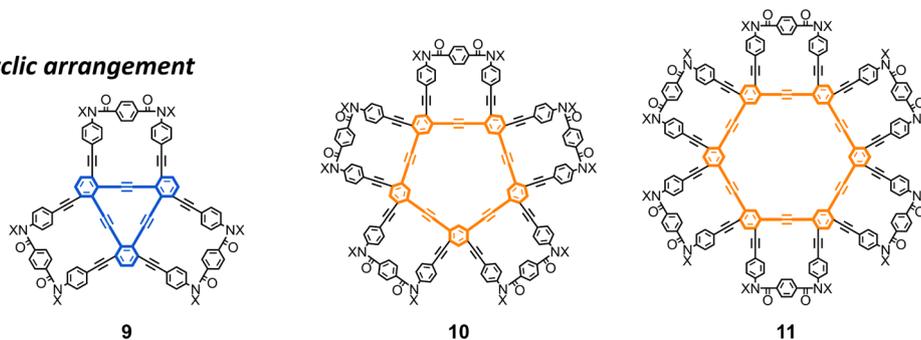
rotational arrangement



acyclic arrangement



cyclic arrangement

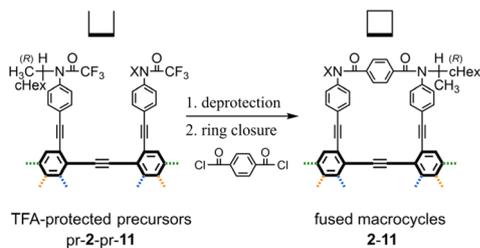


$N = 2-6$
para-PEs
meta-PEs
ortho-PEs

X = (R)-CH(CH₃)(cHex)

Fig. 2 Chemical structures of fused oligomers of macrocycles **2–11** ($N = 2–6$). PE: phenylene-ethynylene. Bis-, tris- or tetrakis(macrocyclic) **3**, **5**, **6**, and **8** were newly synthesized.





Scheme 3 Synthetic strategy based on a multi-fold ring closure.

equilibrium (Fig. S14†). Participation of heterochiral conformer(s) in the equilibrium was similarly observed in the spectra of tris(macrocycle)s 6–8 with an acyclic arrangement (Fig. S12, S17 and S18†), where the conformational distribution was indeterminate due to broadening and overlapping.

Molar optical rotation of fused oligomers of macrocycles

For dynamic chiral molecules,^{24–27} optical activities vary with the ratio of two enantiomeric forms. A purely isolated enantiomer obtained the greatest and specific value, and the value disappears in a racemate. To disrupt the equivalent balance, a point-

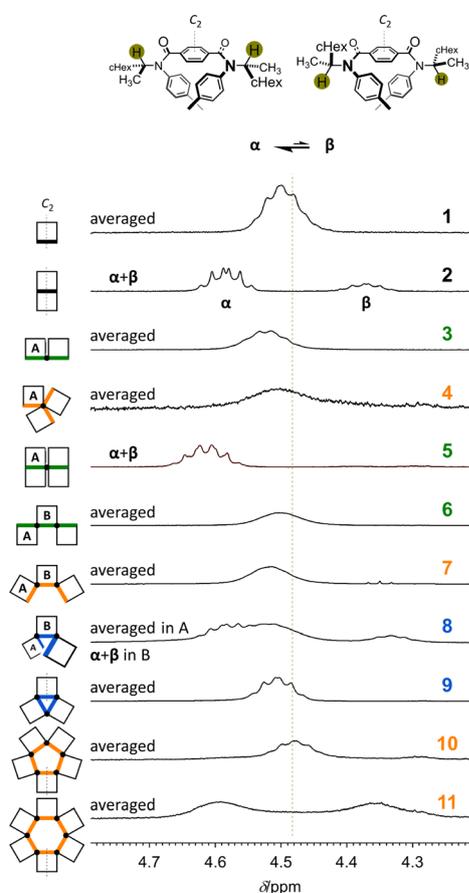


Fig. 3 Partial ^1H NMR spectra (400 MHz, methine protons) of 1–11, measured in CDCl_3 at room temperature. The lack of a two-fold axis led to non-equivalency within a macrocyclic element (A in 3–8) and non-equivalency between elements ($A \neq B$, ABA in 6–8).

chiral auxiliary [$X = (R)\text{-CH}(\text{CH}_3)(\text{cHex})$] was attached to the macrocyclic element. We can see an optical activity through the intramolecular transmission of the point chirality (R) to the macrocyclic element (M/P).

Although the monomeric element 1 ($N = 1$) and its acyclic analog pr-1 possess the same number of auxiliaries ($n = 2$), the value of the molar optical rotation $[M]_D$ of 1 was significantly greater than that of pr-1 (Fig. 4). This single-digit increase would be due to an imbalance induced between the two helically-twisted forms of the macrocycle since similar values of $[M]_D/n$ were recorded with pr-1 ($n = 2$) and 12²⁸ ($n = 1$) without any macrocyclic structure (Table 1). The signs of the optical rotations induced for fused macrocycles 2–11 were consistent with that of 1,²⁹ although there were differences in the number and arrangement of elements. This result was considered consistent with the observation of downfield shifts for methine protons with respect to the central value of $\text{H}\alpha$ and $\text{H}\beta$ in the ^1H NMR spectrum of 2 (Fig. 3).

The intensity of the optical rotation was considered as a value per element. The absolute values of $[M]_D/N$ increased for 6–8 (acyclic) and 3–5 (rotational), and decreased for 2 (rotational), 9–11 (cyclic), compared to that for 1 (upper, Fig. 4 and Table 1). These values should be considered an average property; therefore, a comparison in the intensity was allowed only for 1, 2, 4, and 5. Based on the measured values of $[M]_D$ and each diastereomeric excess at room temperature, the maximum value of $[M]_D/N$ at 100 de% was calculated to be 1311 deg for 1 (from 19 de% at room temperature), 552.9 for 2 (34 de%), 1138 for 4 (37 de%), and 1359 for 5 (64 de%). In comparing 1 and 2, a molecule that can be regarded as a doubled form, where a pair of motifs are arranged so that they are rotated 180° with respect to each other, could contribute to a decrease in intensity, at least in the current system. The comparison of 2 and 5 would support that a rotational arrangement with 0° could contribute to an increase in intensity (Cf. 1 and 3). Relatively small values of $[M]_D/N$ were obtained for 9–11 with a cyclic arrangement, indicating that the cyclic arrangement could be a reason for the decrease²¹ or canceled senses of twisting in a heterochiral conformation might lead to the decrease.

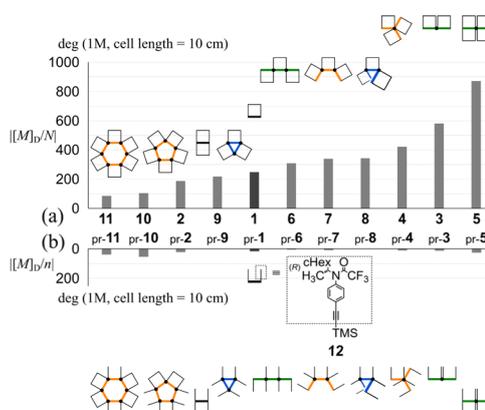


Fig. 4 Chemical structure of 12²⁸ and absolute values of $[M]_D$ per element (a) N : number of macrocyclic elements and (b) n : number of point-chiral elements.



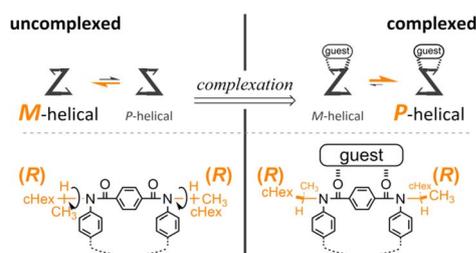
Table 1 Specific optical rotations ($[\alpha]_D$ [deg], c [g dL⁻¹]) and molar optical rotations ($[M]_D$ [deg], 1 M, cell length = 10 cm) measured in CHCl₃ at room temperature and absolute values of $[M]_D$ per element (N : number of macrocyclic elements and n : number of point-chiral elements)

Molecule	11	10	2	9	1	6	7	8	4	3	5	
$[\alpha]_D$	-126	-153	-280	-318	-328	-437	-482	-485	-596	-809	-1338	
$[M]_D$	-513	-519	-375	-650	-249	-928	-023	-029	-263	-165	-479	
$[M]_D/N$	85	104	188	217	249	309	341	343	421	582	870	
Molecule	12	pr-11 ^a	pr-10 ^a	pr-2	pr-9	pr-1	pr-6	pr-7	pr-8	pr-4	pr-3	pr-5
$[\alpha]_D$	-35	-108	-149	-59	-3.2	-39	-13	-23	+3.7	-27	-33	-72
$[M]_D$	-14	-454	-526	-86	-7.2	-32	-29	-53	+8.5	-63	-51	-206
$[M]_D/n$	14	38	53	22	1.2	16	4.8	8.8	1.4	10	13	26

^a Due to a difference in the synthetic strategy, three (out of five on 5PAM) and four (out of six on 6PAM) macrocycles were present in pr-10 and pr-11. Consequently, the values of $[M]_D/n$ were greater than those of pr-2-pr-9.

For a series of the corresponding acyclic analogs (pr-2-pr-9) (lower, Fig. 4 and Table 1), we observed similar values of $[M]_D/n$, which were comparable to the value for **12** ($n = 1$), regardless of the n and PE frameworks. These results indicated that the value was considered an additive property and the point-chiral element could work without regard to the location,²³ as it was associated with **12**, due to the high conformational flexibility of acyclic frameworks.²⁰

Attempt to consider optical rotation by assessment of a change ratio of dissymmetry ($\Delta\epsilon/\epsilon$) before and after complexation. Here, we attempt to consider the optical rotations of bis- or tris(macrocycle) **3** and **6–9**, for which multiple conformers coexist in solution (populations unknown), as shown by ¹H NMR spectra measured at low temperatures. For such an indefinite case, we conceived using a guest molecule to form a complex. We planned to assess a change ratio of the absorption dissymmetry factor ($\Delta\epsilon/\epsilon$) before and after complexation. This was inspired by and based on the complexation-induced reversal of helical-sense preferences (two-way intramolecular transmission of point chirality) (Scheme 4):^{9,10} (i) in the absence of a guest, an *M*-helical form is preferred due to an intramolecular transmission of point chirality (*R*), and (ii) in the presence of a guest, a *P*-helical form turns to be favorable due to an intramolecular transmission of the same point chirality (*R*). To be strict, we need to consider multiple conformations in terms of the local helicity (*m*, *n*, or *p*-helicity) as well as global helicity (*M*- or *P*-helicity) (Scheme 5) since a helical-sense preference would be related to an energy difference between two local *C*₂-symmetrical conformations with *m*- or *p*-helicity (*Mm* and *Pp*).

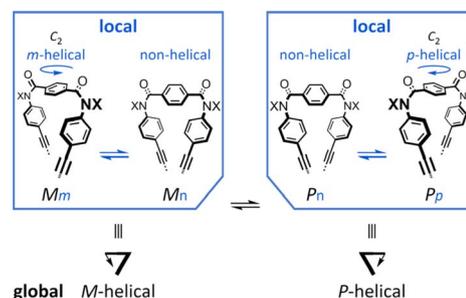


Scheme 4 Complexation-induced reversal of helical-sense preferences (two-way intramolecular transmission of point chirality).

The proximity of a guest through the formation of hydrogen bonds at the terephthaloyl bridge would lead to some change in the local conformation (*e.g.*, the dihedral angle of the carbonyl group with respect to the central phenylene ring in the terephthaloyl bridge and the spatial location in the chiral auxiliary). That is, the population of local non-helical conformers (*M_n* and *P_n*) would be reduced in a complex state. Consequently, an intramolecular point-chirality transmission would work relatively more efficiently than an uncomplexed state.

Thus, we assumed that such a homochiral situation could be enforcedly preferred in a complex state of fused oligomers even in any number and arrangement of elements (Scheme 6), which might help simplify an indefinite system. In some cases, there would be no change in the preferred forms before and after complexation (**2**), or complexation could accompany a change in the population of conformers from multiple pairs to a single pair of diastereomers (**3**, **6–9**). In the former case, the change ratio (complexed/uncomplexed) would be close to 1 if a macrocyclic element did not significantly change local conformations upon complexation. In the latter case, the change ratio would be relatively more excellent since the chiroptical values obtained from an original solution (in the absence of a guest) could be underestimated due to the coexistence of multiple conformers containing heterochiral ones.

To consider the original state, we first implemented VT-CD measurements of **3**, **6–9** without a guest (Fig. S19A†). In the absorption region of each fused macrocycle (Fig. S20†), the Cotton effects involving several extreme values were induced



Scheme 5 Multiple conformations in the global helicity (*M*- and *P*-helical) and local helicity (non-, *m*- and *p*-helical).



Table 2 Changes in $\Delta\epsilon/\epsilon$ at extreme wavelengths: 1–9 before and after complexation with **13**

Molecule	Uncomplexed		Complexed		Equiv. of 13	Change ratio (complexed/uncomplexed)
	λ/nm	$ \Delta\epsilon/\epsilon $	λ/nm	$ \Delta\epsilon/\epsilon $		
1	350	0.00325	353	0.00480	2	1.5
	301	0.00114	301	0.00139		
2	337	0.00097	333	0.00103	4	1.1
	310	0.00168	310	0.00181		
3	351	0.00150	348	0.00354	4	2.4
	308	0.00063	308	0.00197		
6	390	0.00060	391	0.00101	6	1.7
	341	0.00033	340	0.00078		
	323	0.00072	321	0.00169		
7	401	0.00068	400	0.00121	6	1.8
	347	0.00025	345	0.00092		
	327	0.00018	325	0.00060		
8	388	0.00215	385	0.00493	6	2.3
	320	0.00051	323	0.00076		
9	386	0.00069	388	0.00350	6	5.1
	323	0.00026	321	0.00083		

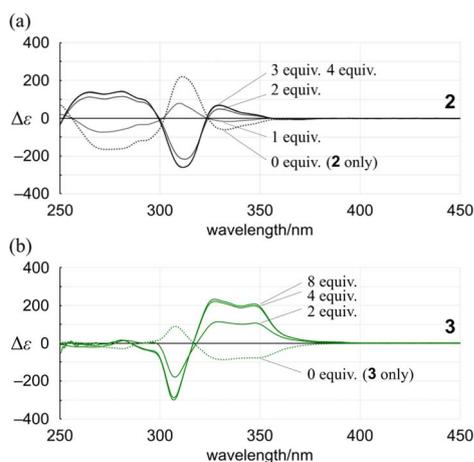


Fig. 6 CD spectra of (a) **2** (8.37×10^{-5} M) and (b) **3** (1.23×10^{-4} M) in the presence of **13** [0 equiv. (**2** or **3** only, dashed line); 1, 2, 3 and 4 equiv. for **2**; 2, 4 and 8 equiv. for **3**]. All spectra were measured in CH_2Cl_2 at 293 K. $\Delta\epsilon$ [$\text{mol}^{-1}\cdot\text{cm}^{-1}$].

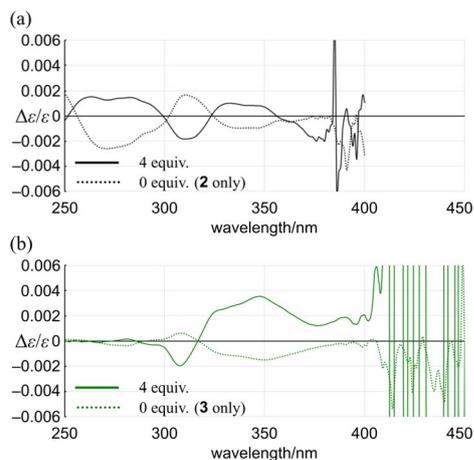


Fig. 7 Plots of $\Delta\epsilon/\epsilon$ for (a) **2** and (b) **3** versus wavelength in the presence (solid line) or absence (dashed line) of **13**.

spectroscopy (Fig. S15b†), would also be explained by this ratio (Fig. 7b and Table 2), indicating that the actual measured value for **3** was underestimated (Fig. 4).

Conclusions

We have demonstrated a series of fused oligomers of macrocycles (**2–11**), in which a dynamic chiral macrocycle (**1**) (*M*- or *P*-helicity) is repeatedly arranged through fusion. A diversity of arrangements (rotational, acyclic, and cyclic) provided a variety of chiral architectures, which led us to consider optical rotation based on the molecular structure.

In particular, a diastereomeric excess was fortunately estimated for **2**, **4**, and **5** with a rotational arrangement under an innate or induced preference for a homochiral situation. The rotational angle could modulate the molar optical rotation. The arrangement of elements rotated 180° relative to each other could be responsible for decreased optical rotation, at least in the current system.

Though a diastereomeric ratio for **9–11** could not be estimated at room temperature,³¹ their optical rotations seemed relatively small in a cyclic arrangement.

For bis(macrocycle) **3** and tris(macrocycle)s **6–8**, in which multiple conformers coexisted (populations unknown), we uniquely assessed a change ratio of dissymmetry ($\Delta\epsilon/\epsilon$) before and after complexation with an achiral guest. Based on a difference in the change ratio, we found that a rotational angle between elements could contribute to a difference in the optical rotation, even though a similar value of $[M]_D/N$ was observed for three isomeric macrocycles **6–8** with an acyclic arrangement, in which the conformational distribution (degree of mixing, *e.g.*, *MMM* and *MMP* in each original state) was different.

Conflicts of interest

There are no conflicts to declare.



Acknowledgements

This work was supported by JSPS KAKENHI Grants (15K17818 and 21K05031) and is based in part on previous efforts by Yuki Tanaka and Keiichi Kusaka (1), Shunsuke Kawai (2), and Takaaki Kudo (4). We are grateful for their contributions (Hokkaido University).

Notes and references

- 1 S. Ando, E. Ohta, A. Kosaka, D. Hashizume, H. Koshino, T. Fukushima and T. Aida, *J. Am. Chem. Soc.*, 2012, **134**, 11084.
- 2 J. Jiang, M. M. Slutsky, T. V. Jones and G. N. Tew, *New J. Chem.*, 2010, **34**, 307.
- 3 P. Rivera-Fuentes, J. L. Alonso-Gómez, A. G. Petrovic, F. Santoro, N. Harada, N. Berova and F. Diederich, *Angew. Chem., Int. Ed.*, 2010, **49**, 2247.
- 4 J. C. Nelson, J. G. Saven, J. S. Moore and P. G. Wolynes, *Science*, 1997, **277**, 1793.
- 5 T. Mori, *Chem. Rev.*, 2021, **121**, 2373.
- 6 J. A. Marsden and M. M. Haley, *J. Org. Chem.*, 2005, **70**, 10213.
- 7 K. Tahara, Y. Yamamoto, D. E. Gross, H. Kozuma, Y. Arikuma, K. Ohta, Y. Koizumi, Y. Gao, Y. Shimizu, S. Seki, K. Kamada, J. S. Moore and Y. Tobe, *Chem.-Eur. J.*, 2013, **19**, 11251.
- 8 L. A. Baldwin, J. W. Crowe, M. D. Shannon, C. P. Jaroniec and P. L. McGrier, *Chem. Mater.*, 2015, **27**, 6169.
- 9 R. Katoono, Y. Tanaka, K. Kusaka, K. Fujiwara and T. Suzuki, *J. Org. Chem.*, 2015, **80**, 7613.
- 10 R. Katoono, S. Kawai, K. Fujiwara and T. Suzuki, *Chem. Sci.*, 2015, **6**, 6592.
- 11 R. Katoono, T. Kudo and S. Kawai, *Org. Biomol. Chem.*, 2023, **21**, 2562.
- 12 R. Katoono, *Chem. Lett.*, 2023, **52**, 627.
- 13 R. Katoono, K. Sakamoto and T. Suzuki, *Chem. Commun.*, 2019, **55**, 5503.
- 14 R. Katoono, Y. Obara, K. Fujiwara and T. Suzuki, *Chem. Sci.*, 2018, **9**, 2222.
- 15 R. Katoono and K. Shimomura, *Chem. Commun.*, 2022, **58**, 13385.
- 16 A. T. Martin, S. M. Nichols, V. L. Murphyad and B. Kahr, *Chem. Commun.*, 2021, **57**, 8107.
- 17 F. Bohle, J. Seibert and S. Grimme, *J. Org. Chem.*, 2021, **86**, 15522.
- 18 J. R. McElhanon and D. V. McGrath, *J. Am. Chem. Soc.*, 1998, **120**, 1647.
- 19 H.-F. Chow and M.-K. Ng, *Tetrahedron: Asymmetry*, 1996, **7**, 2251.
- 20 H.-F. Chow and C. C. Mak, *J. Chem. Soc., Perkin Trans. 1*, 1997, 91.
- 21 S. Anderson, U. Neidlein, V. Gramlich and F. Diederich, *Angew Chem. Int. Ed. Engl.*, 1995, **34**, 1596.
- 22 Y. Morisaki, K. Inoshita and Y. Chujo, *Chem. - Eur. J.*, 2014, **20**, 8386.
- 23 Corresponding values of the chemical shift (H^c) in pr-1-pr-9 were within the range of 4.30–4.38 ppm and were close to that (4.41 ppm) in **12**.
- 24 Ö. Demir and İ. Doğan, *Chirality*, 2003, **15**, 242.
- 25 Y. Liu, S. A. Vignon, X. Zhang, K. N. Houk and J. F. Stoddart, *Chem. Commun.*, 2005, 3927.
- 26 S. Cantekin, D. W. R. Balkenende, M. M. J. Smulders, A. R. A. Palmans and E. W. Meijer, *Nat. Chem.*, 2011, **3**, 42.
- 27 V. Diemer, J. Maury, B. A. F. L. Bailly, S. J. Webb and J. Clayden, *Chem. Commun.*, 2017, **53**, 10768.
- 28 R. Katoono, K. Kusaka, K. Fujiwara and T. Suzuki, *Chem.-Asian J.*, 2014, **9**, 3182.
- 29 We considered the possible reason(s) for this consistency in the sign of the optical rotation according to odd or even numbers, aside from the arrangement of each element or the generation of a secondary chiral structure by the arrangement. In fused macrocycles with odd numbers of elements, it could be explained in either case where (i) all elements prefer the same sense throughout the entire molecule, and (ii) different senses of twisting coexist in a predominant conformation in which there is no chance for an induced preference to be canceled entirely. In fused macrocycles with even numbers of elements, it would not be surprising for a homochiral conformer to be dominant, as with the odd-number group. Alternatively, the consistency in the sign could not be ensured for a molecule to adopt an optically inactive conformation in which there was the same number of senses with *M*- and *P*-helicity (*Cf.* the 1H NMR spectrum of **11**, Fig. 3).
- 30 Complexation-induced changes in absorption in the longer-wavelength region seemed relatively small for **7** compared with other fused macrocycles **3**, **6**, **8**, and **9** (Fig. S25[†]), which was probably due to a slight difference in absorption among conformers of **7** (*Cf.* Fig. S5[†]).
- 31 Due to the low solubility of a complex with **13**, CD spectra of **10** and **11** in the presence of **13** could not be obtained.

