PAPER

Orthorhombic lead-free hybrid perovskite CH₃NH₃SnI₃ under strain: an *ab initio* study†

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We report a computational study where we explore the possibility of tuning the electronic properties of orthorhombic methylammonium tin iodide CH₃NH₃SnI₃ using strains. According to our findings, a moderate [001] strain, smaller than 2%, would open the band gap up to 1.25 eV and enhance the exciton binding energy, opening up new possibilities for the use of CH₃NH₃SnI₃ in technological applications. To better understand the impact of strain, we also examined its influence on bonding properties. The results reveal that the directional pnictogen and the hydrogen bonding are not altered by strains and that the tuning of the electronic properties is the result of changes induced in the orbital contributions to states near the Fermi level and the tilting of the SnI₆ octahedral units.

Introduction

In recent years, the advent of perovskite solar cells based on hybrid halide perovskites has revolutionized the field of photovoltaic (PV) solar cells.[1,2] In particular the synthesis[3–5] of lead-free methylammonium tin iodide CH₃NH₃SnI₃ opened new avenues for photovoltaic materials. To be efficiently used in PV applications, a semiconductor material should have a high light absorption ($\sim 10^5$ cm^{-1} for >1.4 eV).[6,7] A low carrier recombination loss and an efficient carrier collection efficiency are also requisites, together with a long optical path to promote photon recycling.[8] Recent experiments[5] showed that CH₃NH₃SnI₃ has a direct band gap of 1.2–1.3 eV. Thus, it would be beneficial to modify its band-gap energy to meet the ideal PV conditions. One possibility to modify the band-gap energy of hybrid perovskites is the application of external strain/stresses.[9–11] In our case, we will focus on the orthorhombic structure (space group *Pnma*) which is observed at low

temperatures below 200 K.[12] Regarding the influence of strain in this structure, there are two important characteristics of CH₃NH₃SnI₃. First, the methylammonium (MA) ion (CH₃NH₃)⁺ is an asymmetric and positively charged organic unit with a permanent dipole. Second, the low-temperature orthorhombic structure is formed by a framework of SnI₆ corner-sharing octahedral framework. The MA molecules are within cages formed by six SnI₆ octahedra. The interaction of the MA molecule with iodine atoms, forming and hydrogen bonding, induces a distortion of the SnI₆ octahedra. Strains will affect both the MA molecule and the interaction with SnI₆ units affecting therefore the physical properties of CH₃NH₃SnI₃.

Strain engineering is a very helpful technique for fine-tuning the electronic properties of materials by adjusting their band structure.[13] It has been shown[14] that hybrid perovskite crystals can be exposed to strains, which are usually created by deposition on substrates with a lattice mismatch with the hybrid perovskite.[14] It is known that the strains should be small to not cause a non-periodicity on the crystal lattice and to avoid crystal instabilities.[15] Thus, a careful balance is needed to achieve the desired outcomes when applying external stresses. Density-functional theory (DFT) calculations can be a very useful tool for deeply understanding the effects of strain in the properties of hybrid perovskites and for a rational design of composing multilayers including them.[16] In this work, we have used DFT simulations to predict the most important properties of CH₃NH₃SnI₃ and to explore how strains can be used for tailoring the band-gap energy of this compound. We will show that small controlled strains can modify the electronic in a way that could be beneficial for photoelectronic applications. In contrast with previous DFT studies,[17–20] we will report the first study, in which by including van der Waals interactions, an accurate description of the crystal structure is provided and the dynamical

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stability of orthorhombic $CH_3NH_3SnI_3$ is supported.[21] The band-gap energy and exciton binding energies[22,23] have been calculated under different strain conditions. We have found that a tensile [001] strain in the range of +2% is enough to open the band gap in ~1.25 eV. Additionally, since lattice instabilities may result from changes in the bonding pattern, particularly from the hydrogen bonds in the methylammonium ion, we have characterized the strength of hydrogen bonds and other interactions using the non-covalent interactions (NCI) index.[24] Previous to calculations under strain, we tested our method by performing calculations of mechanical, vibrational, and electronic properties of $CH_3NH_3SnI_3$ at normal conditions. These results will also be reported for completeness.

Computational details

We have performed DFT calculations using the Vienna *ab initio* simulation package (VASP).[26–28] The projector-augmented wave (PAW) scheme has been utilized.[28] A kinetic energy cut-off of 700 eV was used for the plane-wave basis (see Fig. S1 in ESI† for the convergence test). We have employed the DFT-D2 weighted exchange potential of Perdew–Burke–Ernzerhof (PBE),[29] which includes the van der Waals (vdW) dispersion as a correction to the ground state energy.[30,31] Furthermore, since PBE tends to underestimate band-gap energy, we have used the modified Becke and Johnson (mBJ)[32] and Heyd–Scuseria–Ernzerhof (HSE) hybrid density functional (HSE06)[33] to calculate the electronic density of state (DOS) and the band structure. Additionally, Phonopy[34] interfaced to VASP have been used to perform lattice-dynamics calculations.[35] The direct force constant approach has been employed.[36,37] We have used $(2 \times 2 \times 2)$ supercells to obtain the phonon dispersion curves. The phonon density of states (PDOS) has been obtained by integrating the phonon frequencies with a large number of k-points ($14 \times 14 \times 14$ grid). The exciton binding energy (E_b) was estimated by the mean of the two-band model of Wannier–Mott.[22,23] Additionally, because the effect of spin–orbit coupling (SOC) is significant for hybrid perovskite due to the presence of Sn atoms, we also checked the effect of SOC on the band gap value. This task was taken into account in the band structure calculations, using a second variational method.[38] The binding energy of the first exciton is given by $E_b = R\mu/m_0\varepsilon_\infty^2$, where R is the Rydberg unit of energy, ε_∞ is the macroscopic dielectric constant, $\mu = (m_e^* m_h^*)/(m_e^* + m_h^*)$ is the reduced mass of the electron and hole, and m_0 is the electron rest mass. m_e^* and m_h^* represent respectively the effective mass of the electron and hole.

We have used the Non-covalent Interactions Index (NCI) as a descriptor[39,40] to analyze the covalent and ionic bonding character. The NCI has been computed using the reduced density gradient of the electron density (ρ), where the density varies gradually. This characterization has been carried out within the parameters of QTAIM, which are specified by.[41]

$$\text{NCI} = s = \frac{1}{2(3\pi^2)^{1/3}} \frac{|\nabla\rho|}{\rho^{4/3}} \tag{1}$$

In the question, the parameter s is dimensionless, which is ensured by the 4/3 density exponent. Critical points of $s(r)$ isosurfaces define their characteristics.[39,40] The sign of the second eigenvalue of the Hessian (λ_2) multiplied by the electron density of rho determines the significance of the NCI isosurface. If the outcome is negative, the isosurface is colored blue and the interactions are considered attractive. If it is positive, the corresponding domains are colored red and the interactions are deemed as repulsive. Weak interactions, such as hydrogen bonds or van der Waals interactions, are activated when $(\lambda_2) \times \rho$ is close to zero, and the isosurfaces are shown in green.[42]

Results and discussion
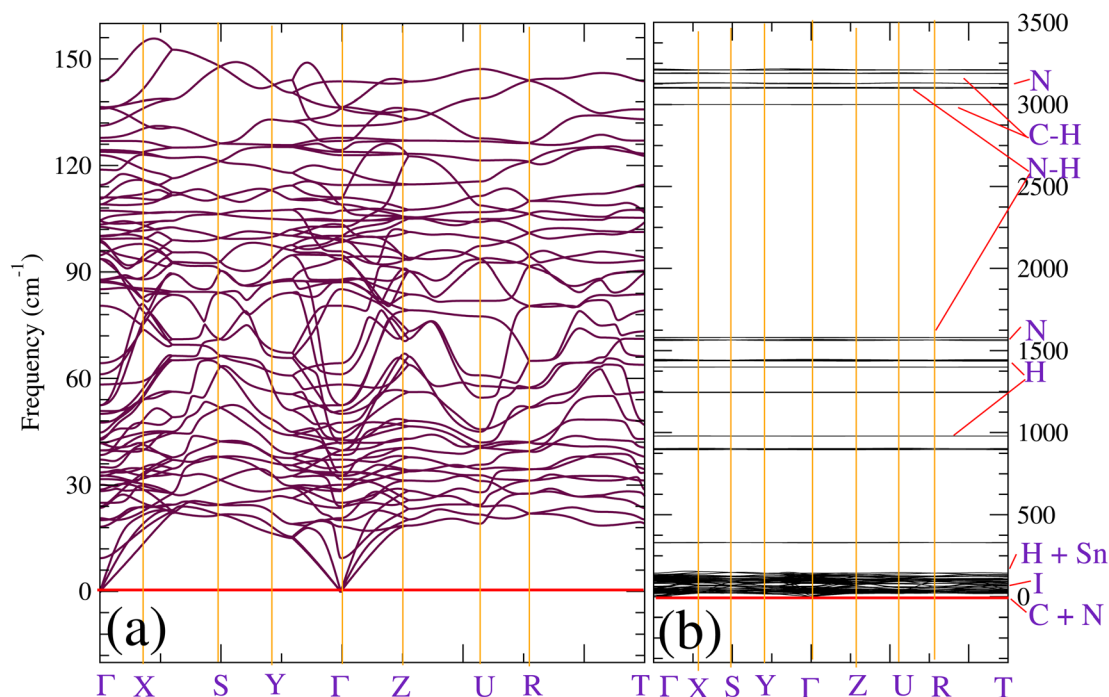
Stability and mechanical properties of orthorhombic $CH_3NH_3SnI_3$

We began our simulations with the geometry optimization of orthorhombic $CH_3NH_3SnI_3$, including the dispersion forces (An overview of this structure is given in Fig. S2 of the ESI†). These interactions become increasingly important in systems with large and polarized electron clouds, such as organic molecules. For this reason, some difference is found between our lattice parameters and those previously calculated without dispersion corrections[17–20] (see Table 1). On the other hand, our results are similar to recent results of ref. 17 conducted with the same approximation. The differences between both studies are related to the use of a smaller (400 eV cutoff energy in ref. 17. Our results show the best agreement with experiments[25] showing the importance of using a large energy cut-off and including dispersion forces in calculations. We are aware that the cation $(CH_3NH_3)^+$ tends to have rotational dynamics, however, this phenomenon is not relevant to our study. We used in simulations the position and configuration of the cation $(CH_3NH_3)^+$ that minimizes the total energy.

We also calculated the phonon dispersion including the D2 correction. So, in contrast to the study done in ref. 20, which found that orthorhombic $CH_3NH_3SnI_3$ the structure is dynamically unstable for pressure smaller than 0.7 GPa, our zero-pressure phonon dispersion does not show any imaginary mode; signature of its dynamical stability (see Fig. 1). This shows that incorporating the weak dispersive interactions is fundamental for describing the studied compound. Fig. 1 shows the entire phonon spectrum in (a) and a zoom of the low-frequency region in (b). The zoom facilitates the identification of low-frequency vibrations associated with the inorganic part of the compound. The high-frequency vibrations corresponding to the inorganic part of the compound can be clearly seen in Fig. 1(b). The phonon modes of orthorhombic $CH_3NH_3SnI_3$ obey to the following mechanical representation: $\Gamma = 19$ $A_g + 17$ $A_u + 14$ $B_{1g} + 22$ $B_{1u} + 19$ $B_{2g} + 17$ $B_{2u} + 14$ $B_{3g} + 22$ B_{3u}. Where there are 22 $B_{1u} + 17$ $B_{2u} + 22$ $B_{3u} = 61$ infrared modes 19 $A_g + 14$ $B_{1g} + 19$ $B_{2g} + 14$ $B_{3g} = 66$ Raman modes and 17 A_u Silent modes. The calculated mode as well as their assignment and activity are reported in Table 2. Vibrations of the inorganic molecule are identified in Fig. 1(b). All modes reported below 200 cm^{-1} arise from internal stretching, libration, and bending vibrations of the SnI_6 octahedron as well as to vibrations where the octahedra

Table 1 Calculated lattice parameters, bulk modulus (B_0 in GPa) and its derivative (B_0'), and elastic constants (C_{ij}). The table also contains the average mechanical properties of bulk polycrystals like the bulk modulus B (in GPa), shear modulus G (in GPa), Young modulus E (in GPa), vickers hardness HV (in GPa) obtained from the elastic constants using Voigt (V), Reuss (R), and Hill (H) approximations are also included. Results are compared with the literature

	a (Å)	b (Å)	c (Å)	B_0	B_0'	C_{11}	C_{12}	C_{13}	C_{22}	C_{23}	C_{33}	C_{44}	C_{55}	C_{66}
PBE + D2 (this work)	8.34	12.63	8.93	19.28	4.47	31.85	12.91	13.99	38.83	11.85	26.53	6.05	13.13	5.15
Experiment ref. 25	8.75	12.35	8.53	—	—	—	—	—	—	—	—	—	—	—
PBE + D2 [17]	8.37	12.72	9.05	—	—	—	—	—	—	—	—	—	—	—
Ref. 18	9.03	12.94	8.56	—	—	—	—	—	—	—	—	—	—	—
Ref. 19	8.49	12.72	9.19	21.89	—	35.83	13.54	17.13	44.88	14.12	28.73	5.85	15.72	5.03
Ref. 20	9.059	12.496	8.394	—		30.48	14.69	11.08	26.08	10.51	39.67	6.04	13.70	4.85

B_V	B_R	B_H	E_V	E_R	E_H	G_V	G_R	G_H	VH_V	VH_R	VH_H
19.413	19.046	19.229	22.849	20.227	21.546	8.762	7.644	8.203	1.731	1.375	1.550

Fig. 1 (Color online) Phonon dispersion of orthorhombic $CH_3NH_3SnI_3$. The plots (a) and (b) represent a zoom for frequencies from 0 to 200 cm^{-1} and the full phonon spectra, respectively. Atoms whose vibrations are associated with the different modes are indicated in (b).

and the organic molecule vibrate as rigid units. The high-frequency modes are mainly associated with internal vibrations of the methylammonium molecule involving vibrations of the C–H and N–H bonds. We have used the tools on the Bilbao Crystallographic Server to extract the activity of each mode. With these tools, using the point group symmetry as well as the selection rules for IR and Raman activities, the specific symmetry and activity of each vibrational mode is obtained. The results are displayed in Table 2.

We have also analyzed the mechanical properties of the studied compound. We have fitted the energy *versus* volume results with a third-order Birch–Murnaghan equation of state[44] to determine the bulk modulus (B_0) and its pressure derivative, and we have calculated elastic constants ($\mathbb{C}_{ij}$) and their related

elastic moduli. Results are shown in Table 1. The elastic moduli have been obtained under the Voigt (V), Reuss (R), and Hill (H) approximations[45] and the hardness has been calculated using the model proposed by Mazhnik and Oganov.[46] We have evaluated the Born stability criteria,[47] which allows us to determine the elastic stability of the crystal. For an orthorhombic system, they are:[43]

$$C_{11} > 0, \ C_{44} > 0; \ C_{55} > 0, \ C_{66} > 0;$$
$$C_{11}C_{12} > C_{22}^2;$$
$$C_{11}C_{22}C_{33} + 2C_{12}C_{13}C_{23} - C_{11}C_{23}^2 - C_{22}C_{13}^2 \tag{2}$$

The mechanical stability of the orthorhombic phase of $CH_3NH_3SnI_3$ is demonstrated here by the fulfillment of the

Table 2 Calculated frequencies of phonon modes as well as their symmetry assignment and activity

ω (cm^{-1})	Silent	ω (cm^{-1})	Raman	ω (cm^{-1})	Infrared
15.71	A_u	15.11	B_{1g}	7.80	B_{2u}
27.95	A_u	16.81	A_{1g}	20.91	B_{1u}
31.49	A_u	30.79	B_{2g}	23.18	B_{2u}
32.52	A_u	31.55	A_{1g}	24.52	B_{3u}
41.33	A_u	34.82	B_{2g}	29.55	B_{1u}
61.24	A_u	35.49	B_{3g}	31.19	B_{2u}
92.76	A_u	37.13	A_{1g}	33.92	B_{3u}
97.83	A_u	37.59	B_{2g}	39.03	B_{3u}
105.67	A_u	40.26	B_{1g}	42.29	B_{1u}
136.16	A_u	51.03	B_{3g}	42.56	B_{3u}
329.12	A_u	51.87	A_{1g}	44.63	B_{2u}
898.24	A_u	57.17	B_{2g}	48.17	B_{1u}
1245.68	A_u	78.45	B_{1g}	52.30	B_{2u}
1440.45	A_u	82.26	A_{1g}	53.70	B_{3u}
1570.10	A_u	85.83	B_{2g}	64.68	B_{1u}
3105.28	A_u	90.36	B_{3g}	82.46	B_{3u}
3211.72	A_u	93.53	B_{3g}	84.22	B_{1u}
		94.83	B_{1g}	85.69	B_{1u}
		96.27	A_{1g}	89.33	B_{2u}
		98.03	A_{1g}	92.33	B_{3u}
		100.20	B_{3g}	96.33	B_{1u}
		101.53	B_{2g}	98.93	B_{3u}
		102.04	B_{1g}	101.24	B_{2u}
		110.61	B_{2g}	102.77	B_{1u}
		116.35	B_{3g}	109.17	B_{3u}
		131.09	B_{1g}	122.35	B_{2u}
		133.29	B_{3g}	131.19	B_{2u}
		138.53	A_g	143.53	B_{3u}
		144.23	B_{2g}	150.97	B_{1u}
		145.97	B_{1g}	330.32	B_{2u}
		331.16	B_{3g}	899.28	B_{2u}
		332.43	B_{1g}	906.82	B_{3u}
		899.91	B_{3g}	907.02	B_{1u}
		903.05	B_{2g}	978.27	B_{1u}
		904.05	A_g	978.37	B_{3u}
		905.68	B_{1g}	1245.85	B_{2u}
		977.89	A_{1g}	1247.41	B_{3u}
		978.93	B_{2g}	1247.68	B_{1u}
		1245.08	B_{1g}	1394.88	B_{3u}
		1245.85	B_{3g}	1395.51	B_{1u}
		1247.71	A_g	1438.24	B_{2u}
		1247.85	B_{2g}	1438.54	B_{3u}
		1396.12	A_{1g}	1440.05	B_{1u}
		1397.12	B_{2g}	1440.08	B_{3u}
		1438.54	B_{3g}	1445.45	B_{1u}
		1438.54	A_{1g}	1561.89	B_{2u}
		1438.68	B_{1g}	1579.34	B_{3u}
		1438.91	B_{2g}	1581.14	B_{1u}
		1439.54	A_g	2996.77	B_{3u}
		1450.92	B_{2g}	2997.14	B_{1u}
		1563.06	B_{1g}	3099.21	B_{1u}
		1565.46	B_{3g}	3099.24	B_{3u}
		1580.34	B_{2g}	3104.88	B_{2u}
		1580.94	A_{1g}	3128.96	B_{3u}
		2997.47	B_{2g}	3133.00	B_{1u}
		2998.77	A_{1g}	3192.84	B_{1u}
		3099.27	B_{2g}	3195.91	B_{3u}
		3099.37	A_g	3213.22	B_{2u}
		3104.41	B_{1g}		
		3104.84	B_{3g}		
		3130.09	A_{1g}		
		3133.96	B_{2g}		

Table 2 (*Contd.*)

ω (cm^{-1})	Silent	ω (cm^{-1})	Raman	ω (cm^{-1})	Infrared
		3192.67	B_{2g}		
		3193.70	A_{1g}		
		3212.18	B_{3g}		
		3221.52	B_{1g}		

stability criteria. The elastic constants summarized in Table 1 agree with results reported in Refs 19 and 20. According to the bulk modulus B_0 obtained from the equation of states fit and from elastic constants B, we can state that the studied hybrid perovskite is highly compressible. The bulk modulus is comparable to that of MAPbBr$_3$ (ref. 9) metalorganic framework[48] and rare-gas solids.[49] This can be attributed to the presence of organic components, specifically large organic MA cations, which are highly compressible. Additionally, given the low Vickers hardness of the material (see Table 1), we can conclude that its resistance to deformation is weak. This means that in a structure of this type, strains should only be applied very moderately. Interestingly, the bulk and Young modulus are similar, which indicates that the resistance to volumetric compression is similar to the tensile or compressive stiffness. In contrast, the shear modulus is approximately one-third of the other two moduli, indicating a preference for shear deformations.

Bonding properties of orthorhombic CH₃NH₃SnI₃

We will now discuss the bonding pattern of CH$_3$NH$_3$SnI$_3$. We will start by performing a topological analysis of bounded atomic basins using the electron localization function (ELF).[50] This tool provides an alternative and complementary analysis to QTAIM in terms of electron-pair localization regions.[51–53] It was successfully utilized to shed light on the chemical interactions found in molecules, molecular complexes, and crystals. It provides a bond path topology, which is the graphical representation of atomic domains bonded to each other. In addition to ELF, we will also use other indexes like the charge density (ρ_b), the sign and magnitude of the charge density's Laplacian ($\nabla^2\rho_b$), and the bond critical points, which are reliable markers for identifying inter- and intra-molecular interactions. Indeed, $\nabla^2\rho_b > 0$ can serve as a sign of polar covalent bonds, while $\nabla^2\rho_b < 0$ or $\nabla^2\rho_b > 0$, refers to whether an interaction between atomic basins has an open-shell (region with charge concentration) or a closed-shell (region with charge depletion) character.[51] After partitioning the structure into topological ELF attractors, we have determined the different basins which are summarized in Table 3. As the PAW method used by VASP incorporates the influence of core electrons without explicitly including them in the wavefunction calculations, no core basins exist for our partition. Instead, the focus is on valence electrons, with the core-electron effects being incorporated through pseudopotentials or PAW potentials.[55,56] Therefore, only the electron pairs that form closed atomic electronic shells around the nuclei are of interest to the current ELF analysis. Examples of these are the

Table 3 Electron localization analysis of basins of bonding of $CH_3NH_3SnI_3$. V (Ω), q, η, $\nabla^2\rho_b$, and ρ stand respectively to Bassin volumes of disynaptic $V(X, Y)$ and monosynaptic $V(X)$ bonds, electronic charges of the bond, ellipticity, Laplacian and electronic density charge (ρ_b). All these quantities are calculated at the (3, −3) ELF basin.[5,43]

Bassin	V (Ω) (Bohr^3)	q (electrons)	ELF	η	$\nabla^2\rho_b$	ρ_b (atomic units)
$V(H,C)$	129.249	−3.001	0.999	0.014	−3.427	0.294
$V(H,N)$	45.823	−1.123	0.996	0.003	−3.042	0.273
$V(H)$	33.333	0.163	0.999	0.043	−3.482	0.295
$V(C)$	31.978	−0.952	0.999	0.364	−0.908	0.177
$V(N)$	18.319	−0.223	0.984	5.060	−0.143	0.056
$V(I)$	242.577	−4.974	0.906	1.471	−0.212	0.093
$V(Sn)$	145.264	−2.761	0.890	2.146	−0.213	0.093

protonic or hydrogen $V(H)$ lone-pair (valence) basins, as well as the synaptic ($V(C)$, $V(N)$, $V(Sn)$, and $V(I)$) basins, and the disynaptic ($V(H, N)$ and $V(H, C)$) basins.[55,57] The first outstanding feature of the current ELF analysis shows that the overall geometric stability of $CH_3NH_3SnI_3$ arises from an environment consisting of an interplay between hydrogen, carbon, and pnictogen-bonded interactions. The appearance of N-centered bonding ($V(N)$) is accompanied by hydrogen bonds ($V(H)$). The high value of ellipticity of our ELF attractors indicates that the electrons of the $V(C)$ basin are strongly localized,[55] whereas the negative sign of $\nabla^2\rho_b$ indicates the covalent nature of most bonds (see Fig. 2). On the other hand, low ellipticity found for $V(H, C)$ and $V(H, N)$ implies that the electrons of these basins are more isotropic or spherical in their electronic domains.[55] Additionally, as the density between I and N/C atoms is small, we can stipulate that the pnictogen bonds present between $[NH_3NH_3]^{2+}$ and $[I]^{2+}$ in their ion-pair form are weaker, but we note an important number of hydrogenated $V(H)$ basins. Lastly, we observe that there is a hint of ionic bonding character from the V(Sn) basin.[54]

As we could not extract all weak interactions by using the ELF partition, we also used the reduced density gradient (RDG, s)

approach to analyze the existing non-covalent interactions. Fig. 2 displays the 3D isosurface of the RDG. As we can see from Fig. 2, the plot does not show any red domains but rather green weak ones in the direction of N–H···I bonds. We also see significantly more delocalization of the electron density at the Sn and I critical bonding regions, which is reflected in the RDG isosurface, which is significantly more blue-green than green. This trend indicates that, even though the nature of these interactions comes from hydrogen atoms, they remain very weak, and more interactions are involved to describe the bonding pattern of the investigated compound. This finding does not match what was already proposed in Ref. 58 for tetragonal $CH_3NH_3PbI_3$, but is in good concordance with the conclusions given in the recent work of Ref. 59. At the same time, they indicate that this interaction is too small to affect the orthorhombic structure of $MASnI_3$.

Electronic properties of orthorhombic $CH_3NH_3SnI_3$

To get an accurate band gap value, we have used two approaches in addition to the PBE-GGA functional, namely the mBJ-GGA and HSE06 potentials. PBE-GGA yields a result of 0.7123 eV,

Fig. 2 (a) ELF plot (isosurface = 0.85), (b) 3D isosurface of the reduced density gradient of $CH_3NH_3SnI_3$ ($s = 0.3$). Strong attractive interactions are depicted as localized blue lentils, repulsive interactions as red isosurfaces, and van der Waals interactions as thin, delocalized green regions. In the iodine–cation bonding, the organic interactions are shown in red, and the non-covalent interactions are circled in blue. Here, the ELF topology gives a partition into localized electronic domains known as basins. They are used to rationalize the bonding schemes. The synaptic order of a valence ELF basin is determined by the number of core basins with which it shares a common boundary. Basins' spatial locations are very close to the valence shell electron pair repulsion domains.

while mBJ-GGA and HSE06 yield very similar results of 1.13 eV and 1.11 eV, respectively. Consequently, due to the high computational costs of the HSE06 calculation and the similarity of the results with mBJ-GGA; the analysis of electronic properties will be conducted using the latter method. Our calculated band gap values agree well with the 1.21–1.30 eV value reported in experiments[4] and the theoretical values obtained using mBJ (1.12 eV) in ref. 20. Due to the presence of heavy elements such as the Sn atom the relativistic effects could be important. Consequently, the effect of SOC was also estimated and found to be equal to 0.24 eV. We have shown the occurrence of splitting occurring at the low level of the conduction band. The SOC lifts the degeneracy of electronic states with the same energy but different spin orientations. This trend impacts electron transport and affects the band gap value (see Fig. S3 in the ESI† file). We present in Fig. 3 the band structure along the high symmetry points of the *Pnma* Brillouin zone. According to the band structure, $CH_3NH_3SnI_3$ has a direct band gap at the Γ point. The direct band gap is often considered advantageous for efficient light absorption and electron–hole pair generation as well as valuable for a range of photonic and electronic devices beyond solar cells.[60]

Concerning the topology of the band structure, we observed that the valence band appears to be significantly less dispersive than the conduction band. This characteristic suggests that the compound here studied might be a semiconductor of the *p* type.[61] In fact, the organic cations contribute delocalized π-electrons to the valence band, while the metal cations and halide anions contribute more localized orbitals. To check such a conclusion, we have additionally plotted the projected
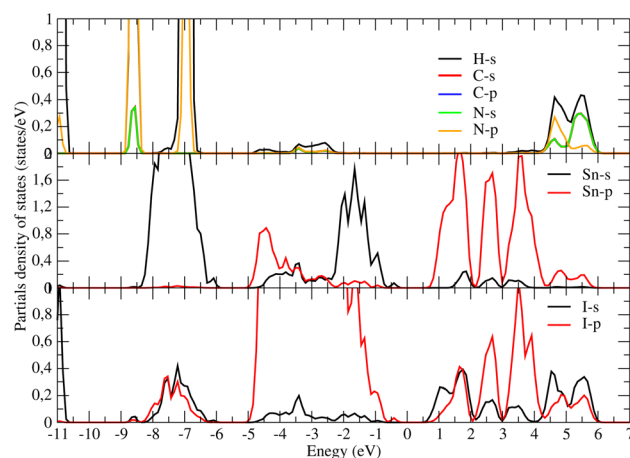

Fig. 4 Partial electronic density of states of un-strained $CH_3NH_3SnI_3$. The PDOS provides valuable insights into the contributions of specific atoms and orbitals to the electronic structure of the investigated structure.

electronic density of states (PDOS) to obtain insights into the electron orbital contribution of each atom. As shown in Fig. 4, the primary components of the conduction band minimum (CBM) are the 5p states of the Sn atoms, whereas the primary contribution of the Valence band maximum (VBM) is the 5p states of the I atoms with an overlap of the Sn 5s states. Additionally, our findings demonstrate that the organic $(CH_3NH_3)^+$ cation had a negligible impact on the formation of the CBM and VBM near the Fermi energy level. The topology of the electronic orbital analyzed below suggests that the band gap can be
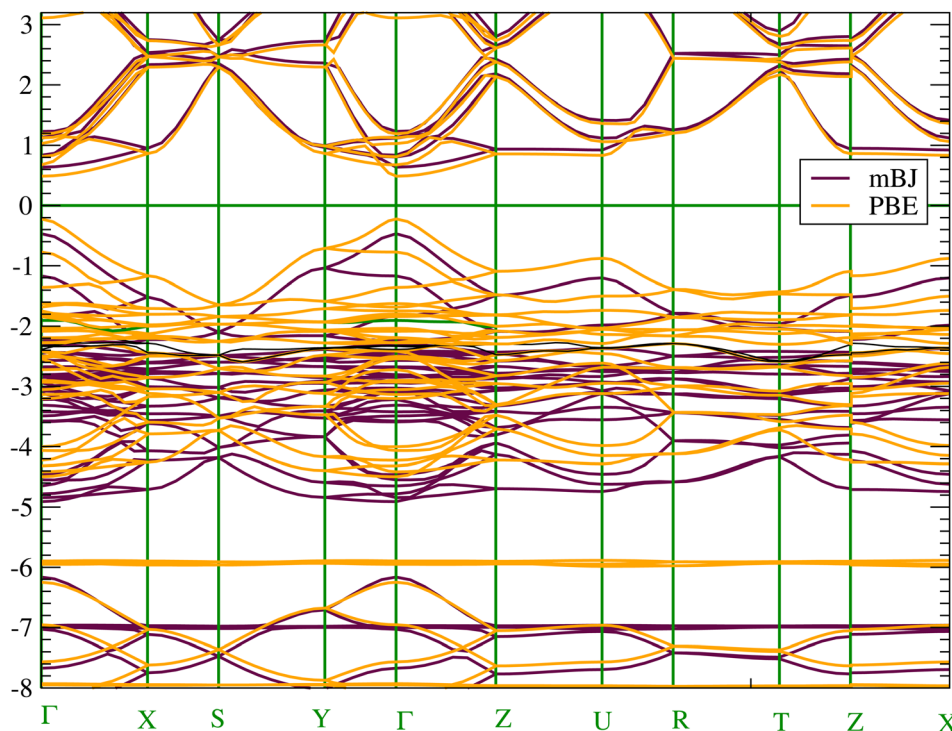

Fig. 3 (Color online) Electronic band structure of $CH_3NH_3SnI_3$ calculated with (a) at mBJ-GGA and (b) PBE-GGA.

engineered more efficiently by applying an external field to the SnI_6 units rather than by replacing the ionic cation $(CH_3NH_3)^+$ with a different one. This confirms the hypothesis made by Walsh.[62]

$CH_3NH_3SnI_3$ under [001] strain

We will discuss how the influence of strain on the bonding and electronic properties of orthorhombic $CH_3NH_3SnI_3$. We have considered strains along [100], [010], and [001] and found that only the last one does not destabilize the orthorhombic crystal structure. The strain applied along [001] direction is calculated as follows:

$$\varepsilon = \frac{c_0 - c}{c_0} \tag{3}$$

where c_0 and c are the lattice parameters that are strain-free and under strain, respectively. When the lattice length increases, the strain is referred to as tensile; when the length decreases, it is called compressive strain. Following the conclusions of previous studies, a narrow range of strains between −0.2% and +2% are applied to maintain the stability of the structure.

To determine the distortion of the SnI_6 octahedron, we estimated the distortion index (ID) using Bauer's definition.[63] In untrained orthorhombic $CH_3NH_3SnI_3$ ID is equal to 0.24%. A negative strain of $\varepsilon = 0.2\%$ changes the distortion index to 0.3% and the maximum one of tensile $\varepsilon = +2\%$ changes it to ID = 2%.[13] So, the range of applied strain that we used does not exceed 2.2%. This moderate distortion may be regarded as within an acceptable range, maintaining the stability of the octahedral networks so that the *Pnma* symmetry is preserved.[13] These slight distortions do not substantially modify bond lengths and angles of SnI_6 but are rather enough to affect the overlap of atomic orbitals, which changes the electronic band structure as well as the value of the band gap.[64]

The evolution of band gap as a function of applied strain is shown in Fig. 5. These results are calculated using the PBE-GGA

Fig. 5 The evolution of band gap and binding energy as a function of strain. In this plot, the Wannier–Mott Model is used to calculate the exciton binding energy E_b. The exciton energy ($E_{exciton}$) can be approximated by: $E_{exciton} = E_g - E_b$.

approximation to minimize computational time. This approximation gives an underestimated value for the band gap but describes correctly the changes induced by strain.[65,66] The band gap changes from 0.7 to ∼2 eV. Also, due to the importance of excitons in PV applications, the binding energy of excitons (E_b) was calculated. The un-strained structure has a value of $E_b = 66$ meV, which is similar to the value calculated in ref. 17 ($E_b = 60$ meV) for $MASnI_3$, for $CsPbCl_3$ (ref. 67) ($E_b = 65$ meV) and the value measured for $MAPbI_3$ ($E_b = 55$ meV).[68] Fig. 5 shows the evolution of E_b *vs.* strain. We should keep in mind that the band gap of the material is 1.3 eV, so this value needs to be pushed down to achieve maximum power conversion efficiency (PCE). Our results show that with a moderate tensile strain, the band gap value of $CH_3NH_3SnI_3$ can be considerably tuned to values where it can be used for PV devices, with high power conversion efficiencies.[69] We have also found that for a tensile strain of +2%, the exciton binding energy is enhanced reaching a value of 144 meV. Tailoring the band structure and excitonic levels offers an efficient way to optimize exciton dissociation and improve the overall performance of photovoltaic devices. The strained structure with $\varepsilon = +2\%$, thus, can enhance the absorption of photons and the generation of photo-carriers, opening the way to enhancing PV efficiency.

To further understand how strains affect $CH_3NH_3SnI_3$, we have performed an NCI analysis on the strained structure with $\varepsilon = +2\%$. For the sake of comparison, the results of both un-strained and strained structures are shown in Fig. 6a and b. In this case, we used the 2D map at the PBE level $sign(\lambda)_2 \times \rho$ *vs.* RDG plots. As we already mentioned in the description given in the computational detail section, the interactions are classified according to their position on the $(sign(\lambda_2) \times \rho(r))$ scale, where $(sign(\lambda_2))$ is the sign of the second eigenvalue of the Hessian matrix of ρ.[70] Such a sign is used in conjunction with ρ to distinguish between attractive and repulsive interactions. According to the color code described above, we can notice the existence of three RDG regions, the first one corresponds to the region (1) for $-0.03(a.u) < sign(\lambda_2) \times \rho(r) < -0.02$ (a.u.), the second region (2) to -0.01 (a.u.) $< sign(\lambda_2) \times \rho(r) < +0.01$ (a.u) and the last one corresponds to the region (3) around $sign(\lambda_2) \times \rho(r) = +0.03$ (a.u.). Region (1) corresponds to both I···I non-covalent interactions and Sn–I ionic bonds. They are the inherent geometrical features of the organic and inorganic systems and are dispersive. We can observe that applying tensile strain does not affect region I, indicating that the structure's bonding pattern, which maintains the strained structure's stability, has not changed. The intermolecular interactions of this region are compatible with the isosurface of the bi-colored disk shown in Fig. 2. Region (2) corresponds to the N–H···I bonds with values of 3.11 and 3.15 Å for respectively, un-strained and +2% strained structures. The green color and the region around $sign(\lambda_2) \times \rho(r) = 0$ indicates that there are hydrogen bonds, which are described as somewhat depleted between the I and H atoms.[71] A similar value of $sign(\lambda_2) \times \rho(r) = -0.01$ (a.u.) was noticed while this bond was analyzed in the O-$CD_3ND_3PbI_3$ compounds.[71] We can see that applying tensile strain enhances region (2), but it appears to be concentrated around the non-covalent region, suggesting that the tilting
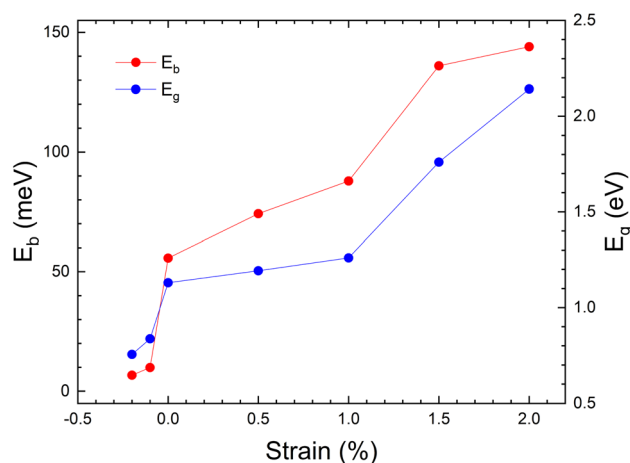
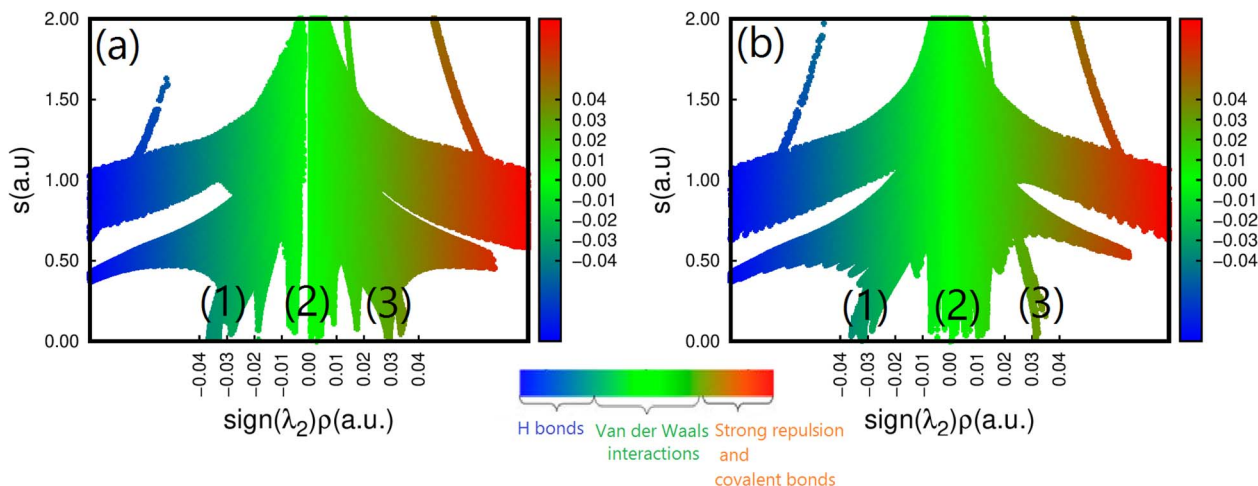**Fig. 6** Reduced density gradient $S(r)$ vs. sign$(\lambda_2)\rho(r)$ for the (a) un-strained and (b) strained structure ($\varepsilon = +2\%$) of $CH_3NH_3SnI_3$.

effect is not caused by the hydrogen or the carbon- and pnictogen bond changes. Finally, region (3) stands for the methylammonium ion $(CH_3NH_3)^+$ which has a pronounced covalent bonding. It is seen that the application of strain does not weaken these bonds. However, the effect of the out-of-plane strains on the ionic Sn–I bond should not be overlooked, as they partly contribute to determining the overall structure of $CH_3NH_3SnI_3$.

Conclusions

We have reported a theoretical study of $CH_3NH_3SnI_3$ including both *ab initio* calculations and an analysis based on the topology of the electron localization function and the reduced form of the density. We present here a first attempt to analyze the bonding of un-strained and strained hybrid $CH_3NH_3SnI_3$. We found that including ver der Waals interations improved the description of the crystal structure of the studied compound, First, we have analyzed the un-strained crystal structure. We have found that the structure of $CH_3NH_3SnI_3$ is dynamically and mechanically stable in the orthorhombic *Pnma* phase structure. This conclusion is supported by the phonon dispersion and elastic constants that fulfill the Born criteria. The study also contains a discussion of the main features of chemical bonding and routes to tuning the properties of $CH_3NH_3SnI_3$ without altering its stability. Specifically, we have found that the H atoms form hydrogen bonding interactions with the bridging halogens, while the N atoms form directional pnictogen bonding interactions with the halogen sites of the SnI_6 octahedra of the inorganic counterpart.

We have also shown that the band-gap energy of orthorhombic $CH_3NH_3SnI_3$ can be tuned using strains. A 2% strain induces a change in the band gap of 1.25 eV and, at the same time, increases the exciton binding energy, which enhances the possibility of going beyond the use of this material for near-infrared light emitter applications. The examination of the chemical interactions that govern the bonding pattern reveals that these strains only slightly modify the global ionic and

covalent bonding, leaving the hydrogen and strong bonds unaffected. We consider that the reported results contribute to open new avenues for the use of $CH_3NH_3SnI_3$ in technological applications. Strains of the order of 2% can be achieved by depositing thin films of $CH_3NH_3SnI_3$ on wide band-gap substrates like indium tin oxide. The selection of different substrates with the appropriate mismatch strain with $CH_3NH_3SnI_3$ stipulated by our calculations will allow the use of $CH_3NH_3SnI_3$ in applications with band gaps ranging from 0.7 to 2.2 eV.

Data availability

The data that support the findings of this study are available on request from the corresponding author.

Author contributions

A. D. investigation, writing – original draft, R. B. writing – review & editing, Supervision. T. O.: conceptualization, validation, formal analysis, investigation, data curation, writing – original draft, writing – review & editing. A. M.: formal analysis, resources, investigation, writing – review & editing. A. M.-S: resources, validation, formal analysis, writing – review & editing. D. E.: validation, formal analysis, writing – review & editing.

Conflicts of interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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References

1 I. Fernandez-Guillen, C. A. Aranda, P. F. Betancur, M. Vallés-Pelarda, C. Momblona, T. S. Ripolles, R. Abargues and P. P. Boix, Perovskite Thin Single Crystal for a High Performance and Long Endurance Memristor, *Adv. Electron. Mater.*, 2024, 2300475, DOI: **10.1002/aelm.202300475**.

2 P. Serafini, P. P. Boix, E. M. Barea, T. Edvinson, S. Sánchez and I. Mora-Seró, Photonic Processing of MAPbI₃ Films by Flash Annealing and Rapid Growth for High-Performance Perovskite Solar Cells, *Sol. RRL*, 2023, 7, 2201102, DOI: **10.1002/solr.202200641**.

3 C. C. Stoumpos, C. D. Malliakas and M. G. Kanatzidis, Semiconducting Tin and Lead Iodide Perovskites with Organic Cations: Phase Transitions, High Mobilities, and Near-Infrared Photoluminescent Properties, *Inorg. Chem.*, 2013, 52, 9019–9038, DOI: **10.1021/ic401215x**.

4 F. Hao, C. Stoumpos, D. H. Cao, R. P. H. Chang and M. G. Kanatzidis, Lead-free solid-state organic-inorganic halide perovskite solar cells, *Nat. Photonics*, 2014, 8, 489–494, DOI: **10.1038/nphoton.2014.82**.

5 I. Mohanty, S. Mangal, S. Jana and U. P. Singh, Synthesis and characterization of Methylammonium tin iodide (CH₃NH₃SnI₃) absorber layer for photovoltaic applications, *Mater. Today: Proc.*, 2023, DOI: **10.1016/j.matpr.2023.05.677**.

6 A. Ennaoui, S. Fiechter, Ch. Pettenkofer, N. Alonso-Vante, K. Büker, M. Bronold, Ch. Höpfner and H. Tributsch, Iron disulfide for solar energy conversion, *Sol. Energy Mater.*, 1993, 29, 289–370, DOI: **10.1016/0927-0248(93)90095-K**.

7 R. Murphy and D. R. Strongin, Surface reactivity of pyrite and related sulfides, *Surf. Sci. Rep.*, 2009, 64, 1–45, DOI: **10.1016/j.surfrep.2008.09.002**.

8 A. Zunger, S. Wagner and P. M. Petroff, New materials and structures for photovoltaics, *J. Electron. Mater.*, 1993, 22, 3–16, DOI: **10.1007/BF02665719**.

9 A. Liang, J. Gonzalez-Platas, R. Turnbull, C. Popescu, I. Fernandez-Guillen, R. Abargues, P. P. Boix, L.-T. Shi and D. Errandonea, Reassigning the Pressure-Induced Phase Transitions of Methylammonium Lead Bromide Perovskite, *J. Am. Chem. Soc.*, 2022, 144(43), 20099–20108, DOI: **10.1021/jacs.2c09457**.

10 A. Liang, R. Turnbull, C. Popescu, I. Fernandez-Guillen, R. Abargues, P. P. Boix and D. Errandonea, Pressure-Induced Phase Transition versus Amorphization in Hybrid Methylammonium Lead Bromide Perovskite, *J. Phys. Chem. C*, 2023, 127(26), 12821–12826, DOI: **10.1021/acs.jpcc.3c03263**.

11 X. Lu, W. Yang, Q. Jia and H. Xu, Pressure-induced dramatic changes in organic-inorganic halide perovskites, *Chem. Sci.*, 2017, 8, 6764, DOI: **10.1039/C7SC01845B**.

12 Y. Q. Huang, J. Su, Q. F. Li, D. Wang, L. H. Xu and Y. Bai, Structure, optical and electrical properties of CH₃NH₃SnI₃ single crystal, *Physica B*, 2019, 563, 107–112, DOI: **10.1016/j.physb.2019.03.035**.

13 H.-S. Kim and N.-G. Park, Importance of tailoring lattice strain in halide perovskite crystals, *NPG Asia Mater.*, 2020, 12, 78, DOI: **10.1038/s41427-020-00265-w**.

14 U. W. Pohl, *Epitaxy of Semiconductors: Introduction to Physical Principles*, Springer, 2013.

15 O. V. Oyelade, O. K. Oyewole, D. O. Oyewole, S. A. Adeniji, R. Ichwani, D. M. Sanni and W. O. Soboyejo, Pressure-Assisted Fabrication of Perovskite Solar Cells, *Sci. Rep.*, 2020, 10, 7183, DOI: **10.1038/s41598-020-64090-5**.

16 Z. Liu, B. Wang and C. Cazorla, Mechanical and electronic properties of CeO₂ under uniaxial tensile loading: A DFT study, *Materialia*, 2021, 15, 101050, DOI: **10.1016/j.mtla.2021.101050**.

17 N. T. Han, V. K. Dien and M.-F. Lin, Electronic and Optical Properties of CH₃NH₃SnI₃ and CH(NH2)2SnI3 Perovskite Solar Cell, *Phys. Status Solidi RRL*, 2023, 17, 2300020, DOI: **10.1002/pssr.202300020**.

18 N. Suhaili, M. F. M. Taib, M. K. Yaakob, O. H. Hassan and M. Z. A. Yahya, Properties of Lead-Free Hybrid Organic-Inorganic Halide Perovskite CH₃NH₃BX₃ Using Density Functional Theory, *Mater. Today: Proc.*, 2017, 4, 5154–5160, DOI: **10.1016/j.matpr.2017.05.021**.

19 V. K. Sharma, V. Kanchana, M. K. Gupta and R. Mittal, Ultra-low thermal conductivity of orthorhombic CH₃NH₃SnI₃: A first-principles investigation, *J. Solid State Chem.*, 2020, 290, 121541, DOI: **10.1016/j.jssc.2020.121541**.

20 I. O. Abdallah-Ali, D. P. Joubert and M. S. H. Suleiman, First-principles study of structural, mechanical, dynamical stability, electronic and optical properties of orthorhombic CH3NH3SnI3 under pressure, *Eur. Phys. J. B*, 2019, 92, 202, DOI: **10.1140/epjb/e2019-100101-1**.

21 M. Fox and G. F. Bertsch, Optical Properties of Solids, *Am. J. Phys.*, 2002, 70, 1269–1270, DOI: **10.1119/1.1691372**.

22 F. Bassani, G. P. Parravicini, R. A. Ballinger and J. L. Birman, Electronic States and Optical Transitions in Solids, *Phys. Today*, 1976, 29, 58, DOI: **10.1063/1.3023374**.

23 M. Fox and G. F. Bertsch, Optical properties of solids, *Am. J. Phys.*, 2002, 70, 1269, DOI: **10.1119/1.1691372**.

24 A. Otero-de-la-Roza, E. R. Johnson and J. Contreras-Garcıa, Revealing non-covalent interactions in solids: NCI plots revisited, *Phys. Chem. Chem. Phys.*, 2012, 14, 12165–12172, DOI: **10.1039/C2CP41395G**.

25 Y. Takahashi, R. Obara, Z. Z. Lin, Y. Takahashi, T. Naito, T. Inabe, S. Ishibashi and K. Terakura, *Dalton Trans.*, 2011, **40**, 5563, DOI: **10.1039/D3DT03772J**.

26 G. Kresse and J. Furthmüller, Efficiency of ab-initio total energy calculations for metals and semiconductors using a plane-wave basis set, *Comput. Mater. Sci.*, 1996, **6**, 15–50, DOI: **10.1103/PhysRevB.47.558**.

27 G. Kresse and J. Hafner, Ab initio molecular dynamics for liquid metals, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 1993, **47**, 558–561, DOI: **10.1103/PhysRevB.47.558**.

28 G. Kresse and D. Joubert, From ultrasoft pseudopotentials to the projector augmented-wave method, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 1999, **59**, 1758–1775, DOI: **10.1103/PhysRevB.59.1758**.

29 J. P. Perdew, K. Burke and M. Ernzerhof, Generalized Gradient Approximation Made Simple, *Phys. Rev. Lett.*, 1996, **77**(18), 3865–3868, DOI: **10.1103/physrevlett.77.3865**.

30 S. Grimme, J. Antony, S. Ehrlich and H. Krieg, A consistent and accurate *ab initio* parametrization of density functional dispersion correction ($DFT - D$) for the 94 elements $H - Pu$, *J. Chem. Phys.*, 2010, **132**(15), 154104, DOI: **10.1063/1.3382344**.

31 S. Grimme, S. Ehrlich and L. Goerigk, Effect of the damping function in dispersion corrected density functional theory, *J. Comput. Chem.*, 2011, **32**(7), 1456–1465, DOI: **10.1002/jcc.21759**.

32 F. Tran and P. Blaha, Accurate band gaps of semiconductors and insulators with a semilocal exchange-correlation potential, *Phys. Rev. Lett.*, 2009, **102**, 226401, DOI: **10.1103/PhysRevLett.102.226401**.

33 J. Heyd, G. E. Scuseria and M. Ernzerhof, Hybrid functionals based on a screened Coulomb potential, *J. Chem. Phys.*, 2003, **118**, 8207–8215, DOI: **10.1063/1.1564060**.

34 A. Togo and I. Tanaka, *Scr. Mater.*, 2015, **108**, 1–5, DOI: **10.1016/j.scriptamat.2015.07.021**.

35 P. Liu, B. Kim, X.-Q. Chen, D. D. Sarma, G. Kresse and C. Franchini, Relativistic GW+BSE study of the optical properties of Ruddlesden-Popper iridates, *Phys. Rev. Mater.*, 2018, **2**, 075003, DOI: **10.1103/PhysRevMaterials.2.075003**.

36 X. Gonze and C. Lee, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 1997, **55**, 10355, DOI: **10.1103/PhysRevB.55.10355**.

37 P. Giannozzi, S. de Gironcoli, P. Pavone and S. Baroni, *Phys. Rev. B*, 1991, **43**, 7231, DOI: **10.1103/PhysRevB.43.7231**.

38 S. Steiner, S. Khmelevskyi, M. Marsman and G. Kresse, Calculation of the magnetic anisotropy with projected-augmented-wave methodology and the case study of disordered $Fe_{1-x}Co_x$ alloys, *Phys, Rev. B*, 2018, **93**, 224425, DOI: **10.1103/PhysRevB.93.224425**.

39 R. A Boto, J.-P. Piquemal and J. Contreras-García, Revealing strong interactions with the reduced density gradient: a benchmark for covalent, ionic, and charge-shift bonds, *Theoretical Chemistry Accounts: Theory, Computation, and Modeling*, 2017, **136**, 139. **https://hal.archives-ouvertes.fr/hal-01636270**.

40 E. R. Johnson, S. Keinan, P. Mori-Sánchez, J. Contreras-García, A. J. Cohen and W. Yang, *J. Am. Chem. Soc.*, 2010, **132**, 6498–6506, DOI: **10.1021/ja100936w**.

41 H. Z. Guedda, T. Ouahrani, A. Morales-García, R. Franco, M. A. Salvadó, P. Pertierra and J. M. Recio, Computer simulations of 3C-SiC under hydrostatic and non-hydrostatic stresses, *Phys. Chem. Chem. Phys.*, 2016, **18**, 8132–8139, DOI: **10.1039/C6CP00081A**.

42 T. Ouahrani, R. Khenata, B. Lasri, A. H Reshak, A. Bouhemadou and S. Bin-Omran, First and second harmonic generation of the XAl_2Se_4 (X= Zn, Cd, Hg) defect chalcopyrite compounds, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 2012, **407**, 3760–3766, DOI: **10.1016/j.physb.2012.05.057**.

43 T. Ouahrani, F.-Z. Medjdoub, S. Gueddida, Á. Lobato-Fernandez, R. Franco, N.-E. Benkhettou, M. Badawi, A. Liang, J. Gonzalez and D. Errandonea, Understanding the Pressure Effect on the Elastic, Electronic, Vibrational, and Bonding Properties of the $CeScO_3$ Perovskite, *J. Phys. Chem. C*, 2021, **125**(1), 107–119, DOI: **10.1021/acs.jpcc.0c08641**.

44 F. Birch, Finite Elastic Strain of Cubic Crystals, *Phys. Rev.*, 1947, **71**, 809–824.

45 D. H. Chung and W. R. Buessem, *J. Appl. Phys.*, 1967, **38**, 2535–2540.

46 E. Mazhnik and A. R. Oganov, A model of hardness and fracture toughness of solids, *J. Appl. Phys.*, 2019, **126**, 125109.

47 *Dynamical Theory and Experiment*, ed. M. Born and K. Huang, Springer, Berlin, 1982, vol. 1. DOI: **10.1007/bf02645493**.

48 J. Navarro-Sánchez, I. Mullor-Ruíz, C. Popescu, D. Santamaría-Pérez, A. Segura, D. Errandonea, J. González-Platas and C. Martí-Gastaldo, Peptide metal-organic frameworks under pressure: flexible linkers for cooperative compression, *Dalton Trans.*, 2018, **47**, 10654–10659, DOI: **10.1039/C8DT01765D**.

49 D. Errandonea, R. Boehler, S. Japel, M. Mezouar and L. R. Benedetti, Structural transformation of compressed solid Ar: An x-ray diffraction study to 114 GPa, *Phys. Rev. B*, 2006, **73**, 092106, DOI: **10.1103/PhysRevB.73.092106**.

50 A. D. Becke and K. E. Edgecombe, A simple measure of electron localization in atomic and molecular systems, *J. Chem. Phys.*, 1990, **92**, 5397–5404, DOI: **10.1063/1.458517**.

51 R. F. Bader, *Atoms in Molecules: A Quantum Theory*, Oxford University Press, Oxford, UK, 1990.

52 P. L. A. Popelier, *Atoms in Molecules: An Introduction*, Pearson Education, Harlow, UK, 2000.

53 S. Belarouci, T. Ouahrani, N. Benabdallah, A. Morales-García and I. Belabbas, Two-dimensional silicon carbide structure under uniaxial strains, electronic and bonding analysis Comp, *Mater. Sci.*, 2018, **151**, 288–295, DOI: **10.1016/j.commatsci.2018.05.020**.

54 T. Ouahrani, I. Merad-Boudia, H. Baltache, R. Khenata and Z. Bentalha, Effect of pressure on the global and local properties of cubic perovskite crystals, *Phys. Scr.*, 2011, **84**, 025704, DOI: **10.1088/0031-8949/84/02/025704**.

55 R. J. Gillespie and R. S. Nyholm, Inorganic stereochemistry, Quarterly Reviews, *Chem. Soc. Rev.*, 1957, **11**, 339–380, DOI: **10.1039/QR9571100339**.

56 T. Ouahrani, R. Franco, J. M. Menéndez, M. Marqués and J. M. Recio, Microscopic partition of pressure and elastic constants in CdTe polymorphs, *J. Alloys Compd.*, 2014, **592**(15), 150–156, DOI: **10.1016/j.jallcom.2013.12.153**.

57 A. Savin, O. Jepsen, J. Flad, L. K. Anderson, H. Preuss and H. G. von Schnering, Electron localization in solid-state structures of the elements: the diamond structure, *Angew Chem. Int. Ed. Engl.*, 1992, **32**, 187–188, DOI: **10.1002/anie.199201871**.

58 F. El-Mellouhi, A. Marzouk, E. T. Bentria, S. N. Rashkeev, S. Kais and F. H. Alharbi, Hydrogen Bonding and Stability of Hybrid Organic– Inorganic Perovskites, *ChemSusChem*, 2016, **9**, 1–9, DOI: **10.1002/cssc.201600864**.

59 A. Varadwaj, P. R. Varadwaj and H. M. Marques, The Pnictogen Bond, Together with Other Non-Covalent Interactions, in the Rational Design of One-, Two- and Three-Dimensional Organic-Inorganic Hybrid Metal Halide Perovskite Semiconducting Materials, and Beyond, *Int. J. Mol. Sci.*, 2022, **23**, 8816, DOI: **10.3390/ijms23158816**.

60 E. Mosconi, A. Amat, M. D. K. Nazeeruddin, M. Grätzel and F. De Angelis, First-principles modeling of mixed halide organometal perovskites for photovoltaic applications, *J. Phys. Chem. C*, 2013, **117**, 13902–13913, DOI: **10.1021/jp4048659**.

61 R. Shukla, A. Arya and A. K. Tyag, Interconversion of perovskite and fluorite structures in Ce-Sc-O system, *Inorg. Chem.*, 2010, **49**, 1152–1157, DOI: **10.1021/ic9020096**.

62 A. Walsh, Principles of Chemical Bonding and Band Gap Engineering in Hybrid Organic-Inorganic Halide Perovskites, *J. Phys. Chem. C*, 2015, **119**, 5755–5760, DOI: **10.1021/jp512420b**.

63 W. H. Baur, The geometry of polyhedral distortions. Predictive relationships for the phosphate group, *Acta Crystallogr., Sect. B: Struct. Sci.*, 1974, **30**, 1195, DOI: **10.1107/S0567740874004560**.

64 T. Ouahrani, R. M. Boufatah, M. Benaissa, Á. Á. Morales-García, M. Badawi and D. Errandonea, Effect of intrinsic point defects on the catalytic and electronic properties of Cu_2WS_4 single layer: Ab initio calculations, *Phys. Rev.*

Mater., 2023, **7**, 025403, DOI: **10.1103/PhysRevMaterials.7.025403**.

65 S. López-Moreno, J. Sánchez-Martín, E. Bandiello, M. Bettinelli, C. L. Bull, C. Ridley and D. Errandonea, The effect of pressure on the band-gap energy in $FePO_4$ and $FeVO_4$, *J. Phys. Chem. Solids*, 2023, **183**, 111604, DOI: **10.1016/j.jpcs.2023.111604**.

66 D. Errandonea, F. Rodriguez, R. Vilaplana, D. Vie, S. Garg, B. Nayak, N. Garg, J. Singh, V. Kanchana and G. Vaitheeswaran, Band-Gap Energy and Electronic d–d Transitions of $NiWO_4$ Studied under High-Pressure Conditions, *J. Phys. Chem. C*, 2023, **127**(31), 15630–15640, DOI: **10.1021/acs.jpcc.3c03512**.

67 M. Baranowski, P. Plochocka, R. Su, L. Legrand, T. Barisien, F. Bernardot, Q. Xiong, C. Testelin and M. Chamarro, Exciton binding energy and effective mass of $CsPbCl_3$: a magneto-optical study, *Photonics Res.*, 2020, **8**, A50–A55, DOI: **10.1364/PRJ.401872**.

68 K. Galkowski, A. Mitioglu, A. Miyata, P. Plochocka, O. Portugall, G. E. Eperon, J. Tse-Wei Wang, T. Stergiopoulos, S. D. Stranks, H. J. Snaith and R. J. Nicholas, Determination of the exciton binding energy and effective masses for methylammonium and formamidinium lead tri-halide perovskite semiconductors, *Energy Environ. Sci.*, 2016, **9**, 962–970, DOI: **10.1039/C5EE03435C**.

69 K. Galkowski, A. Surrente, M. Baranowski, B. Zhao, Z. Yang, A. Sadhanala, S. Mackowski, S. D Stranks and P. Plochocka, Excitonic Properties of Low Bandgap Lead-Tin Halide Perovskites, *ACS Energy Lett.*, 2019, **4**(3), 615–621, DOI: **10.1021/acsenergylett.8b02243**.

70 S. Bouguima, T. Ouahrani, A. Bouheddadj, M. Le Roux, D. Errandonea and M. Badawi, Understanding the optical and bonding properties of hybrid metal-halide ($C_5H_{16}NP$) PbX_4 (X= Cl, Br, I) perovskite: A density-functional theory study, *Inorg. Chem. Commun.*, 2021, **130**, 108721, DOI: **10.1016/j.inoche.2021.108721**.

71 P. R. Varadwaj, A. Varadwaj, H. M. Marques and K. Yamashita, Significance of hydrogen bonding and other noncovalent interactions in determining octahedral tilting in the $CH_3NH_3PbI_3$ hybrid organic-inorganic halide perovskite solar cell semiconductor, *Sci. Rep.*, 2019, **9**, 50, DOI: **10.1038/s41598-018-36218-1**.