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Hydrogen storage in M(BDC)(TED)_{0.5} metal–organic framework: physical insights and capacities†

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Finding renewable energy sources to replace fossil energy has been an essential demand in recent years. Hydrogen gas has been becoming a research hotspot for its clean and free-carbon energy. However, hydrogen storage technology is challenging for mobile and automotive applications. Metal–organic frameworks (MOFs) have emerged as one of the most advanced materials for hydrogen storage due to their exceptionally high surface area, ultra-large and tuneable pore size. Recently, computer simulations allowed the designing of new MOF structures with significant hydrogen storage capacity. However, no studies are available to elucidate the hydrogen storage in M(BDC)(TED)_{0.5}, where M = metal, BDC = 1,4-benzene dicarboxylate, and TED = triethylenediamine. In this report, we used van der Waals-dispersion corrected density functional theory and grand canonical Monte Carlo methods to explore the electronic structure properties, adsorption energies, and gravimetric and volumetric hydrogen loadings in M(BDC)(TED)_{0.5} (M = Mg, V, Co, Ni, and Cu). Our results showed that the most favourable adsorption site of H₂ in M(BDC)(TED)_{0.5} is the metal cluster–TED intersection region, in which Ni offers the strongest binding strength with the adsorption energy of -16.9 kJ mol⁻¹. Besides, the H₂@M(BDC)(TED)_{0.5} interaction is physisorption, which mainly stems from the contribution of the d orbitals of the metal atoms for M = Ni, V, Cu, and Co and the p orbitals of the O, C, N atoms for M = Mg interacting with the σ^* state of the adsorbed hydrogen molecule. Noticeably, the alkaline-earth metal Mg strongly enhanced the specific surface area and pore size of the M(BDC)(TED)_{0.5} MOF, leading to an enormous increase in hydrogen storage with the highest absolute (excess) gravimetric and volumetric uptakes of 1.05 (0.36) wt% and 7.47 (2.59) g L⁻¹ at 298 K and 7.42 (5.80) wt% and 52.77 (41.26) g L⁻¹ at 77 K, respectively. The results are comparable to the other MOFs found in the literature.

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1 Introduction

The energy demands for industrialization based on fossil fuels have been causing an enormous increase in global warming. Finding clean and renewable energy alternatives to fossil fuels is an urgent need for a sustainable environment and the development of the global economy.^{1,2} Hydrogen gas has attracted much attention due to its high energy density, non-

toxicity, and high abundance on Earth.^{3–5} Compared to other renewable energy sources, such as solar and wind turbines, hydrogen energy is unaffected by season, temperature, geology, *etc.*^{3,6} However, storing hydrogen gas is challenging because hydrogen gas is very mobile and occupies an extensive volume. Besides, its high energy density contains potentially explosive risks when applying pressure-tank storage, which also require heavy equipment incompatible with mobile solutions. Therefore, searching for advanced storage materials plays a crucial role in the success of hydrogen energy technology.^{7–9} Metal–organic frameworks (MOFs) are promising H₂ adsorbents with their exceptionally high specific surface area, ultra-large pore size, high porosity, good chemical stability, tuneable porous structure, and reproducible and facile synthesis.^{6,9–14} Although thousands of MOFs have been synthesized, only a few have been investigated for H₂ storage, specifically at room temperatures and low pressures.^{15,16} The 2025 main criteria set by the US Department of Energy (DOE) are 55 mg H₂ per g [MOF + H₂] system or 5.5 wt% (1.8 kW h kg⁻¹) for gravimetric storage and 40 g H₂ per L [MOF + H₂] (1.3 kW h L⁻¹) for volumetric storage

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under moderate temperatures (from $-40\text{ }^{\circ}\text{C}$ to $60\text{ }^{\circ}\text{C}$) and low pressures (below 100 bar).^{7,17} Besides, the ultimate DOE targets are 6.5 wt% and 50 g H₂ per L.

At cryogenic temperatures ($\sim 77\text{ K}$), MOFs have achieved reasonable hydrogen capacities to meet the DOE storage targets.⁹ So far, the experimental data have recorded very high H₂ adsorption capacity for MOF-210 with 17.6 wt% (total uptake) and 8.6 wt% (excess uptake) at 80 bar and 77 K,¹⁸ NU-100 with 9.95 wt% at 56 bar and 16.4 wt% at 70 bar for excess capacity,¹⁹ MOF-200 with 16.3 wt% (total uptake) and 7.4 wt% (excess uptake) at 100 bar,¹⁹ MOF-205 with 12.0 wt% and 7.0 wt% for total and excess uptakes at 80 bar,¹⁸ MOF-177 with 11.0 total wt% and 7.5 excess wt% at 70 bar,²⁰ Be₁₂(OH)₁₂(BTB)₄ with 9.2 total wt% (43 g H₂ per L) and 6.0 excess wt%,²¹ and 5.46 MOF-5 with 5.1 wt% at 65 bar.²² Nevertheless, due to weak interaction with H₂ at ambient temperatures, MOFs store rather low H₂ uptake, below 2.0 wt% or 20 mg g⁻¹.^{9,23,24} In our knowledge, at the room temperature (298 K), the highest H₂ storage was found for Be₁₂(OH)₁₂(BTB)₄ about 1.0 excess wt% and 2.3 total wt% at 95 bar and Mn₃[(Mn₄Cl)₃(BTT)₈(MeOH)₁₀]₂ with 1.5 wt% (12 g L⁻¹) at 90 bar.²¹ Besides, most MOFs have low isosteric heats of H₂ adsorption (Q_{st}), often from -4 to -13 kJ mol^{-1} .²⁵ As suggested, for efficient H₂ storage in fuel cells using adsorption material-based hydrogen storage technology at room temperatures, the ideal Q_{st} of H₂ for MOFs should be from -15 and -25 kJ mol^{-1} .¹⁵ Therefore, temperatures must decrease to cryogenic range to improve hydrogen capacities and provide a satisfactory drive range in automotive applications. On the other hand, practical strategies have been proposed to strengthen H₂ adsorption at room temperatures to enhance the H₂@MOFs interaction *via* substituting metal centres, organic ligands, and counter-ions.¹¹ These strategies showed that Q_{st} and the H₂ uptakes significantly improved at ambient temperatures and low pressures below 100 bar.⁹

Recently, M(BDC)(TED)_{0.5} with the paddle-wheel structure of the metal clusters has been of great interest due to its high porosity and thermal stability.^{26,27} Ni and Zn(BDC)(TED)_{0.5} are excellent SO₂ capture materials,²⁸ Ni(BDC)(TED)_{0.5} for CO₂ and SO₂ co-adsorption,²⁹ and also other toxic gases.¹⁵ It is also well-known for highly selective separation of CH₃OH/H₂O and CO₂/CH₄ mixtures in Zn(BDC)(TED)_{0.5} (ref. 30) and C₂H₆/C₂H₄ in M(BDC)(TED)_{0.5} (M = Co, Cu, Ni, Zn).³¹ A study showed good adsorption/desorption of argon, hydrogen, and hydrocarbons in Zn and Cu(BDC)(TED)_{0.5}.^{30,32} Combining experiment and simulation, Liu and co-workers showed Zn(BDC)(TED)_{0.5} had good hydrogen adsorption loadings at 77 K with the maximum excess uptake of *ca.* 4.2 wt% at 20 bar, and at 298 K, *ca.* 0.23 wt% (by UFF), 0.28 wt% (by Buch potential), and 0.21 wt% (by experiment).³³ We find that M(BDC)(TED)_{0.5} is very promising for hydrogen storage. However, no works are available to elucidate the influences of metal substitutions (M = Mg, V, Co, Ni, and Cu) in M(BDC)(TED)_{0.5} on hydrogen adsorption and storage. Therefore, this work is devoted to solving the research topic with the aid of vdW-DF density functional theory and grand canonical Monte Carlo simulations. In the past, computer simulations allowed the prediction and design of new MOF structures with significant gas storage capacity.^{12,13,34} Here, we used the density functional theory

approach to explore physical insights into the H₂ adsorption sites and the interaction nature between H₂ and M(BDC)(TED)_{0.5}. We then used grand canonical Monte Carlo simulations to obtain hydrogen loadings *via* adsorption isotherms. To improve the H₂ adsorption ability of M(BDC)(TED)_{0.5}, the metal M(II) ions (alkaline earth and transition metals) are of concern, *i.e.*, magnesium (Mg), vanadium (V), cobalt (Co), nickel (Ni), and copper (Cu). These metals have been selected because, based on experimental and theoretical research, the first-row transition metals such as Ni, V, Co, and Cu are common connectors in MOFs.^{12,35-37} Also, Mg-based MOFs exhibited a good adsorption ability to H₂ and other small gases.^{7,36,38} Various factors can influence the hydrogen storage capacity of MOFs. However, this work focused only on the ideal structure of M(BDC)(TED)_{0.5} and ignored other factors, such as humidity, flexibility, defects, *etc.*, on the H₂ storage capacity and the H₂ interaction with M(BDC)(TED)_{0.5}.

2 Computational approaches

2.1 The density functional theory calculations

We used the van der Waals dispersion-corrected density functional theory (vdW-DF)³⁹ *via* the Vienna *ab initio* simulation package (VASP).^{40,41} The vdW-DF calculations were established with cut-off energy of 700 eV for expanding the plane wave basis set, the revised Perdew–Burke–Ernzerhof functional for the exchange–correlation energy,^{42,43} the projector-augmented-wave method for the electron–ion interaction,^{44,45} and Monkhorst and Pack *k*-points sampling of $5 \times 5 \times 5$ mesh grid for optimizing structure, calculating total energy, and investigating electronic properties.⁴⁶ The geometric structure of all designed H₂@M(BDC)(TED)_{0.5} systems was fully relaxed before computing the total energy. For analyzing the electronic properties of H₂@M(BDC)(TED)_{0.5} systems, we calculated the atomic point charges using the Bader partition technique,^{47,48} charge density difference (CDD), and the electronic density of states.⁴⁹ The adsorption energy ΔE of the hydrogen molecule in M(BDC)(TED)_{0.5} is defined as

$$\Delta E = E_{[\text{MOF}+\text{H}_2]} - E_{\text{MOF}} - E_{\text{H}_2} \quad (1)$$

where $E_{[\text{MOF}+\text{H}_2]}$, E_{MOF} , and E_{H_2} are the total energy of the H₂@M(BDC)(TED)_{0.5} system, the isolated M(BDC)(TED)_{0.5}, and the isolated hydrogen molecule, respectively.

The charge density difference (CDD) is calculated by

$$\Delta\rho = \rho_{[\text{M-MOF}+\text{H}_2]} - \rho_{\text{M-MOF}} - \rho_{\text{H}_2} \quad (2)$$

where $\rho_{[\text{M-MOF}+\text{H}_2]}$, $\rho_{\text{M-MOF}}$, and ρ_{H_2} are the charge density of the H₂@M(BDC)(TED)_{0.5} system, the adsorbed-state M(BDC)(TED)_{0.5}, and the adsorbed-state hydrogen molecule, respectively. Specifically, the structure of the last two systems was extracted from that of H₂@M(BDC)(TED)_{0.5}. The CDD plots by the VESTA software⁵⁰ were used to describe the polarization of the charge density of the H₂@M(BDC)(TED)_{0.5} system.

2.2 Grand canonical Monte Carlo simulations

The pair interactions between the i^{th} atom and the j^{th} atom of the H₂ molecule with M(BDC)(TED)_{0.5} were described by the van



der Waals interactions in the Lennard-Jones (LJ) 6–12 model (U_{ij}^{LJ}) with the cut-off radius of 20 Å and the electrostatic interactions or Coulomb interactions (U_{ij}^{CL}) with the cut-off radius of 13 Å as follows

$$U_{ij} = U_{ij}^{LJ} + U_{ij}^{CL} = 4\varepsilon_{ij} \left[\left(\frac{\sigma_{ij}}{r_{ij}} \right)^{12} - \left(\frac{\sigma_{ij}}{r_{ij}} \right)^6 \right] + k \frac{q_i q_j}{r_{ij}}, \quad (3)$$

here, r_{ij} is the distance between the i^{th} atom and the j^{th} atom, and k is the Coulomb's constant. The partial charge of the i^{th} atom is q_i , obtained using the DDEC6 package.^{51,52} The parameters for LJ interactions, ε_{ij} (potential-well depth) and σ_{ij} (potential-well diameter) for the pairs of unlike atoms, were computed by the Lorentz–Berthelot mixing rules.

$$\varepsilon_{ij} = \sqrt{\varepsilon_i \times \varepsilon_j} \text{ and } \sigma_{ij} = (\sigma_i + \sigma_j)/2. \quad (4)$$

herein, σ_i and ε_i for the atoms of M(BDC)(TED)_{0.5} and the H atom of the hydrogen molecule were taken from the generic force field parameters for MOFs (UFF) in the RASPA package.⁵³ In the present study, polarization is neglected, and the potentials were shifted to zero at the cut-off radius for the LJ model. For H₂, a single LJ interaction site model at the centre of mass H–H_{com}–H (TraPPE force field) with LJ parameters $\varepsilon_{\text{H}_2}/k_B = 36.70$ K and $\sigma_{\text{H}_2} = 2.96$ Å was used. The partial charges of each H nucleus and H_{com} are +0.486e and –0.936e, respectively.⁵⁴

In the GCMC simulations, the hydrogen molecule can move freely by inserting, deleting, translating, and rotating operations to reach an equilibrium state, whereas the MOF atoms were kept fixed. The hydrogen uptake capacities in wt% are calculated by

$$\text{wt}\% = \frac{\text{mass of H}_2}{\text{mass of (H}_2 + \text{MOF) system}} \times 100. \quad (5)$$

We calculated the absolute uptake (n_{abs}) and excess uptake (n_{exc}) of hydrogen gas for gravimetric and volumetric loadings at temperatures of 77 K and 298 K and pressures up to 100 bar using the RASPA package. The relationship between absolute and excess uptakes is

$$n_{\text{abs}} = n_{\text{exc}} + V_{\text{pore}} \rho'_{\text{H}_2}, \quad (6)$$

where, ρ'_{H_2} and V_{pore} are the molar density of the bulk H₂ in the gas phase and the pore volume of M(BDC)(TED)_{0.5}, respectively.

3 Results and discussion

3.1 Geometry optimization for M(BDC)(TED)_{0.5}

We designed the geometry structure of M(BDC)(TED)_{0.5} based on experimental data,^{28,29} where M = (Mg, V, Co, Ni, Cu), BDC = 1,4-benzene dicarboxylate, and TED = triethylenediamine, with the parameters for a primitive unit cell $\alpha = \beta = \gamma = 90^\circ$ and $a = b \neq c$, as shown in Fig. 1. The MOF has the secondary building units of metal–oxygen–carbon clusters in the paddle-wheel shape at the node of the network.^{28,31} The unit cell contains 54 atoms, including two metal (M), eight oxygen, two nitrogen, twenty-two carbon, and twenty hydrogen atoms. Two metal atoms combine with four surrounding O atoms to form the metal cluster, connecting to BDC linkers and TED groups.

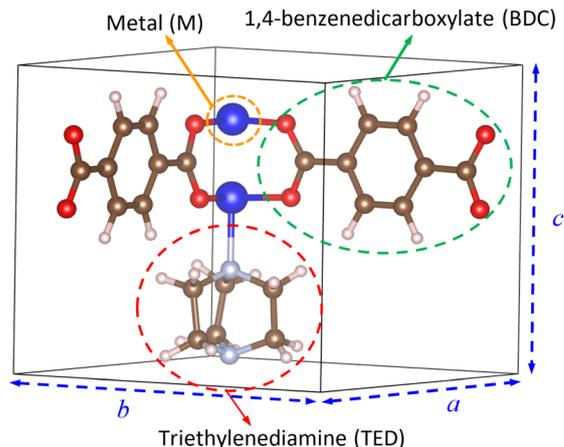


Fig. 1 The primitive unit cell of M(BDC)(TED)_{0.5}. Light pink (H), brown (C), light grey (N), red (O), and blue (M).

After designing the unit cell geometry, we fully optimized the atomic positions and the unit cell size of the M(BDC)(TED)_{0.5} using the vdW-DF calculations. The unit cell size of structures was optimized by fitting to the Murnaghan equation of state when presenting the DFT total energy as a function of the unit cell volume (V_{cell}) or the lattice constants (Fig. 2).^{55,56} From now on, we will use M-MOF to denote the short name of M(BDC)(TED)_{0.5}. The optimized parameters for the unit cell of the M-MOF structure are presented in Table 1. The average distance from two metal atoms to their nearest oxygen atoms is about 2.0 Å. The pore volume (V_{pore}) and specific surface area (SSA), obtained using the RASPA code,⁵³ are the parameters featuring the porosity of the M-MOF. Our obtained parameters for Ni-MOF are $a = b = 10.979$ Å, $c = 9.384$ Å, and $V_{\text{pore}} = 0.761$ cm³ g^{−1}, which are in good agreement with the experimental results $a = b = 11.15$ Å, $c = 9.53$ Å,⁵⁷ and $V_{\text{pore}} = 0.76$ cm³ g^{−1}.³¹ The optimized parameters for the remaining M-MOFs also agreed with the available experimental data.^{31,57} The SSA and V_{pore} of the primitive unit cell are in the order Mg-MOF > V-MOF > Ni-MOF > Co-MOF > Cu-MOF, which is reasonable compared to the experimental data,³¹ i.e., Ni-MOF > Co-MOF ≈ Cu-MOF for V_{pore} and Ni-MOF > Co-MOF > Cu-MOF for SSA.

3.2 Favourable H₂ adsorption sites

We added a hydrogen molecule to the optimized unit cell of M-MOF, then fully relaxed the geometric structure of the H₂@M-MOF system. Hydrogen molecules can adsorb on four possible regions: the metal cluster, BDC linker, TED group, and the intersection of the metal cluster and the TED group (the metal cluster–TED intersection). The favourable order of the adsorption sites was investigated *via* the adsorption energy (in kJ mol^{−1}) of the H₂ molecule, which was calculated *via* eqn (1). The more negative the adsorption energy ΔE , the more favourable the adsorption site for the H₂ molecule will be. The most favourable H₂ adsorption configuration, the one with the most negative adsorption energy for each region, is shown in Fig. 3. The detailed values for the H₂ adsorption energy and structural parameters are listed in Table 2. Here, d_1 and d_2 are



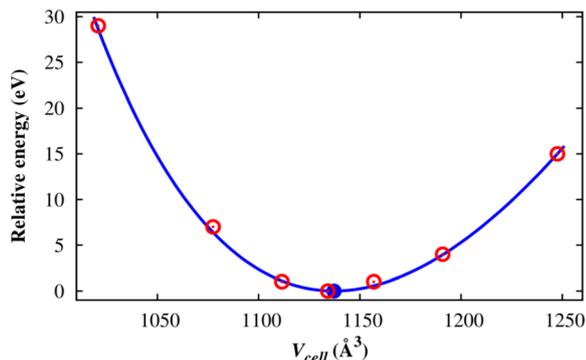


Fig. 2 The total energy (eV) of the M(BDC)(TED)_{0.5} unit cell as a function of the unit cell volume: calculated values (red points) and the Murnaghan fitting (solid line). The blue point denotes the minimum of the fitted curve.

the average distances from the nearest H atom of the H₂ molecule to six C atoms of the BDC linker and four O atoms of the metal cluster, respectively. The average distance from the nearest H atom of the H₂ molecule to the C atoms of the TED group is d_3 . The average distance from the nearest H atom to one metal atom (Mg, V, Co, Ni, or Cu) of the metal cluster and the N atom of the TED is d_4 . See Fig. 3 for the explanation of the distance from H₂ to the M-MOF.

Table 2 exhibits that the magnitude of the H₂ adsorption energy, ΔE , of M-MOF is in the following order of the adsorption sites: metal-TED intersection > TED group > metal cluster > BDC linker, except for M = Co, it is the intersection > metal cluster > TED group > BDC linker. On the other hand, the absolute value of ΔE is in decreasing order: Ni-MOF > Mg-MOF > V-MOF > Co-MOF > Cu-MOF for all adsorption sites of BDC linker, TED group, and metal-TED intersection, except for the metal node, the order between Mg-MOF and V-MOF is approximately the same. Notably, the H₂ adsorption strength of Ni-MOF and Cu-MOF is always the best and the worst among the considered metal substitutions, respectively. The most and second most negative H₂ adsorption energy of $-16.930 \text{ kJ mol}^{-1}$ on Ni-MOF and $-12.435 \text{ kJ mol}^{-1}$ on Mg-MOF is around the criterion (-15 kJ mol^{-1}) for the heat of adsorption. Therefore, Ni-MOF and Mg-MOF are expected to offer significant hydrogen adsorption capacity.⁵⁸ The obtained adsorption energies imply that the M(BDC)(TED)_{0.5} has a great potential for H₂ storage, where the intersection region between the metal cluster and the TED group is predicted to attract hydrogen gas the most. Note that our obtained adsorption energies include only the electronic effects of the interaction between the H₂ molecule and the M-MOFs, which are different compared to adsorption enthalpy values that include not only the electronic effects but also other factors such as coverage, temperature, and

Table 1 The optimized structural parameters for M(BDC)(TED)_{0.5} (M = Mg, V, Co, Ni, and Cu)

M-MOF	$d_{\text{M-O}}$ (Å)	Lattice constants (Å)		Unit cell volume, V_{cell} (Å ³)	Pore volume, V_{pore} (cm ³ g ⁻¹)	Specific surface area, SSA (g cm ⁻²)
		$a = b$	c			
Mg-MOF	2.040	10.989	9.393	1134.28	0.874	1931.34
V-MOF	2.022	10.969	9.375	1127.99	0.782	1727.54
Co-MOF	1.947	10.901	9.317	1107.16	0.741	1627.64
Ni-MOF	1.994	10.979	9.384	1131.13	0.761	1685.63
Cu-MOF	2.023	10.845	9.270	1090.28	0.709	1560.67
Co-MOF ³¹					0.619	1708
Ni-MOF ^{31,57}		11.15	9.53	1184	0.757	1905
Cu-MOF ³¹					0.627	1631

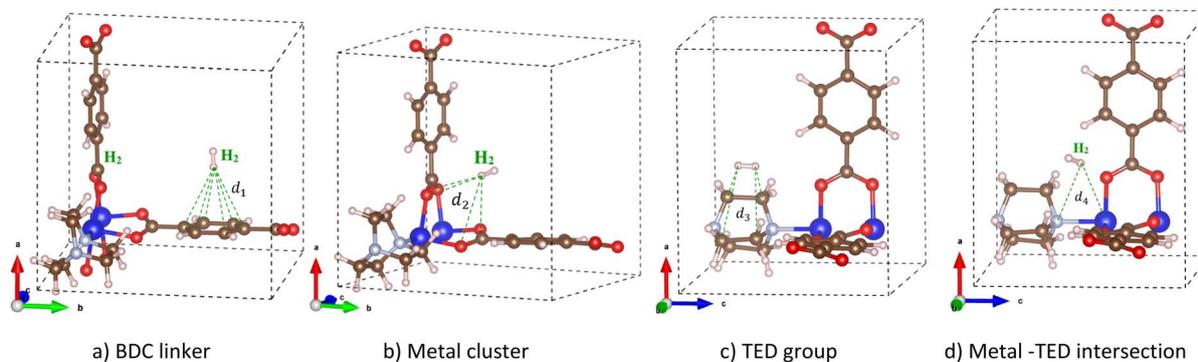


Fig. 3 The favourable adsorption sites of the H₂ molecule in M(BDC)(TED)_{0.5} and the denotation for the distances from the nearest H atom of the H₂ molecule to the neighbouring atoms of M(BDC)(TED)_{0.5} at the adsorption site: (a) BDC linker, (b) metal cluster, (c) TED group, and (d) the metal cluster-TED intersection.



Table 2 The H₂ adsorption energies (ΔE) and the average distance (d) from the nearest H atom of the H₂ molecule to the atoms of M(BDC)(TED)_{0.5} at different adsorption sites

M-MOF		BDC linker	Metal cluster	TED group	Metal cluster–TED intersection
Ni-MOF	ΔE (kJ mol ⁻¹)	-12.428	-13.730	-15.457	-16.930
	d (Å)	3.209 (d_1)	3.466 (d_2)	3.444 (d_3)	4.156 (d_4)
Mg-MOF	ΔE (kJ mol ⁻¹)	-8.700	-10.008	-10.990	-12.435
	d (Å)	3.326 (d_1)	3.534 (d_2)	3.470 (d_3)	4.177 (d_4)
V-MOF	ΔE (kJ mol ⁻¹)	-7.744	-10.015	-10.634	-11.713
	d (Å)	3.256 (d_1)	3.314 (d_2)	3.479 (d_3)	4.060 (d_4)
Co-MOF	ΔE (kJ mol ⁻¹)	-6.448	-9.436	-9.190	-10.264
	d (Å)	3.084 (d_1)	3.294 (d_2)	3.483 (d_3)	3.770 (d_4)
Cu-MOF	ΔE (kJ mol ⁻¹)	-5.999	-8.591	-8.634	-9.828
	d (Å)	3.300 (d_1)	3.536 (d_2)	3.417 (d_3)	4.140 (d_4)

pressure.⁵⁹ Furthermore, the adsorption of a single H₂ molecule in the unit cell of the M-MOFs gave rise to the highest adsorption energy (Table 2). Simultaneous adsorption of many H₂ molecules in the unit cell will lower the average adsorption energy per H₂ molecule compared to the single site model. However, we can approximately estimate the average adsorption energies from various single site contributions (BDC linker, metal cluster, TED group, and metal cluster–TED intersection), *i.e.*, in the magnitude order: Ni-MOF (-14.64 kJ mol⁻¹) > Mg-MOF (-10.53 kJ mol⁻¹) > V-MOF (-10.03 kJ mol⁻¹) > Co-MOF (-8.83 kJ mol⁻¹) > Cu-MOF (-8.26 kJ mol⁻¹).

The average distance from the nearest H atom of the H₂ molecule to M-MOF (Table 2) shows that, on the BDC linker, the H₂ molecule is almost perpendicular to the BDC plane (the end-on configuration of H₂, see Fig. 3a) with the average distance from the nearest H atom of H₂ to the C atoms $d_1 = 3.0$ – 3.3 Å. On the metal cluster, the most stable adsorption site for H₂ is in the central region of the metal cluster (see Fig. 3b) with an average distance to four O atoms $d_2 = 3.3$ – 3.5 Å for different M-MOFs. On the TED group (Fig. 3c), H₂ is nearly parallel to the C–C bonds of TED (the side-on configuration) with the average distance $d_3 = 3.4$ – 3.5 Å from the nearest H atoms to the nearest C atoms. In the intersection region between the metal cluster and the TED group, H₂ is more favourable in the middle of the intersection with the H–H bond towards the metal cluster (see Fig. 3d). The average distance from the nearest H atom of H₂ to the nearest N atom and the nearest metal atom is in the range of $d_4 = 3.8$ – 4.2 Å. The actual distance from the nearest H atom to M-MOF is that from this H atom to the nearest O atom, which is 2.70 Å.

3.3 Electronic structure properties of H₂@M(BDC)(TED)_{0.5} systems

The total charge of the adsorbed hydrogen molecule calculated by the Bader partition method,^{47,48} in Table 3, shows that the H₂ molecule can gain the charge from M-MOF and lose the charge to M-MOF with the positive and negative values, respectively. However, the charge gain and loss are ignorable because their magnitude is the same as the error (0.005e⁻) of charge calculation. Therefore, the interaction between the H₂ molecule and

Table 3 The point charge (in e⁻) of the adsorbed H₂ molecule in the H₂@M(BDC)(TED)_{0.5} system at different adsorption sites

M-MOF	BDC linker	Metal cluster	TED group	Metal–TED intersection
Ni-MOF	0.0070	0.0048	-0.0003	0.0053
Mg-MOF	0.0054	0.0034	-0.0011	0.0053
V-MOF	0.0048	0.0027	-0.0004	0.0008
Co-MOF	0.0061	0.0043	-0.0001	0.0031
Cu-MOF	0.0052	0.0109	-0.0005	0.0059

the M-MOF is dominated by the charge attraction instead of the charge exchange. Therefore, the interaction between them is physisorption. This result supports the obtained adsorption energies, as shown in Table 2.

Besides, we can reveal the physical insights with more details into the interaction between the H₂ molecule and M-MOF *via* analysing the electronic density of states of the H₂@M(BDC)(TED)_{0.5} (M = Mg, V, Co, Ni, and Cu) systems. To answer the question of what state of the H₂ molecule participates in the interaction, we plotted the total DOS of the H₂ molecule before and after its adsorption on the substrate surface (Fig. 4). We found that the isolated H₂ molecule has two

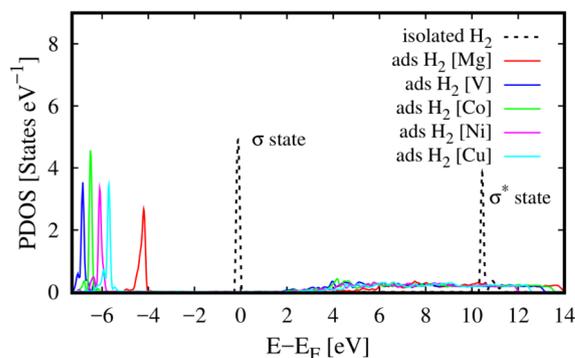


Fig. 4 The total DOS of the adsorbed hydrogen molecule (ads H₂) in M(BDC)(TED)_{0.5} (M = Mg, V, Co, Ni, and Cu) in the most favourable adsorption configuration (the metal cluster–TED intersection site) and that of the isolated H₂.



peaks, *i.e.*, the occupied σ and unoccupied σ^* states locating at the negative and positive energies, respectively. The first peak is at the Fermi level, while the second one is about 10 eV away from the Fermi level. When adsorbing in the M-MOF, the σ^* state becomes broadened and simultaneously reduced the

height; however, it is still in the range of positive energies. Whilst, the peak of the σ state is shifted to a more negative energy level with a slight modification in the shape of the peak. This shift is not due to the charge exchange with the M-MOF because the Bader charge exchange is ignorable, but it is due

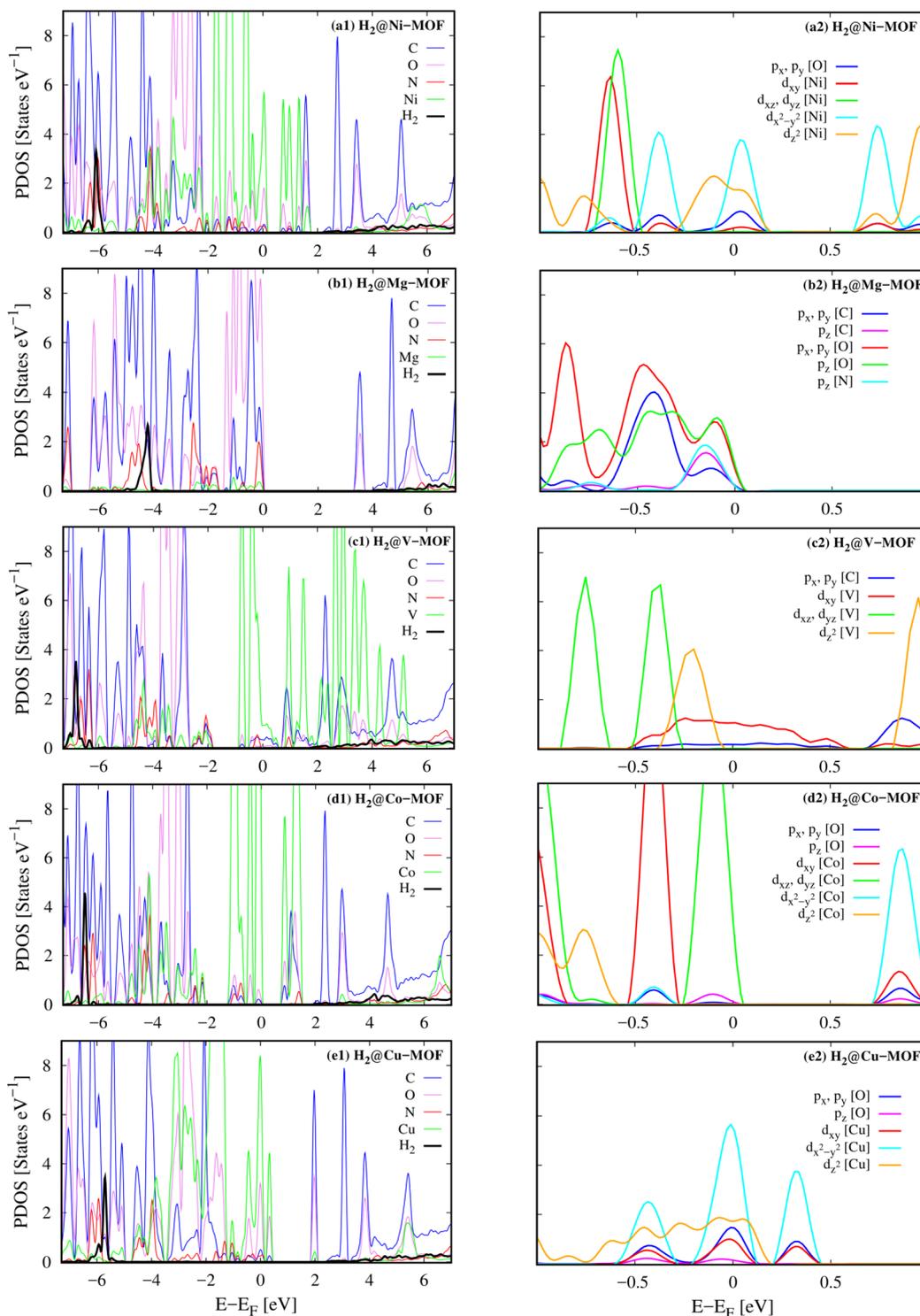


Fig. 5 Left column: the atom-projected DOS of the $H_2@M(BDC)(TED)_{0.5}$ systems (a1–e1). Right column: the orbital-projected DOS around the Fermi level of the adsorbed-state $M(BDC)(TED)_{0.5}$ systems (a2–e2) for the metal cluster–TED intersection adsorption site of H_2 . The identical orbitals are presented with the same colour.



to the Coulomb attractive interaction between the H₂ molecule and the M-MOF (as analysed above). We know that an adsorbate and an adsorbent can combine into a system because the occupied states of the adsorbate can attract the unoccupied states of the adsorbent and *vice versa*. Therefore, we have to analyse the DOS of the adsorbed-state M-MOF and the adsorbed H₂ molecule to understand the contributions of each component of the M-MOF to the interaction with the H₂ molecule. As shown in Fig. 5a1–e1 for the metal cluster–TED intersection adsorption site, the atom-projected DOS around the Fermi level is dominated by the states of the N and O atoms for the cases M = Ni, Co, and Cu (Fig. 5a1, d1 and e1), by those of the V and C atoms for M = V (Fig. 5c1), and by the O, C, and N atoms for M = Mg (Fig. 5b1). We found that the metal component (the green line) is dominated around the Fermi level for the considered M-MOFs except for M = Mg. The occupied states of the M-MOFs just below the Fermi level attract and broaden the unoccupied σ^* state of the H₂ molecule, while the unoccupied states of the M-MOFs, just above the Fermi level for M = Ni, V, Co, and Cu, and at 3.5 eV for M = Mg, attract the occupied σ state of the H₂ molecule. However, this attractive interaction is not strong enough to bring the peaks of the H₂ molecule to cross the Fermi level. Therefore, no significant charge exchange was found between the adsorbate (H₂) and adsorbent (M-MOF), resulting in the physisorption between H₂ and M(BDC)(TED)_{0.5}. We have to emphasise that similar characteristics of the DOS were also found for the other adsorption sites (BDC linker, metal cluster, and TED group) of the H₂@M-MOF systems. Therefore, we have just focused on the DOS analysis for the metal cluster–TED intersection region. This selection becomes representative because it is the most favourable adsorption site for the H₂ molecule, and it is not only close to the metal cluster but also the TED group and the BDC linker.

The close-up view around the Fermi level of the orbital-projected DOS, Fig. 5a2–e2, explained the contribution of the different orbitals of the adsorbed-state M-MOFs. We found that the main contributors at the Fermi level are the $d_{x^2-y^2}$ and d_{z^2} orbitals of the metal atoms for M = Ni and Cu (Fig. 5a1 and e2), the d_{xy} orbital for M = V (Fig. 5c2), and the d_{xz} and d_{yz} orbitals for M = Co (Fig. 5d2). The other portions also come from the O p_x , p_y orbitals (Fig. 5a, b2 and e2) and the C p_x , p_y orbitals (Fig. 5c2). Besides, the O p_z orbital also made a significant contribution at the Fermi level for the Mg-MOF (Fig. 5b2).

Fig. 6 shows the charge density difference for the H₂@Ni(BDC)(TED)_{0.5} system at various adsorption sites. Charge accumulation and donation (in the e^- unit) are presented in purple and green colours, respectively. We found that the H₂ molecule exhibits the antibonding (σ^*) state, showing by two different colours for two H atoms with the node in the middle region of the H–H bond length, for all cases disregarding the end-on configuration (Fig. 6a, b and d) or the side-on configuration (Fig. 6d) of the H₂ molecule. One H atom accumulates and the other H atom donates the negative charge. However, the accumulation and donation of the H atoms should not come from the charge exchange with the M-MOF (as mentioned above), but it should stem from the charge rearrangement between two H atoms. This rearrangement creates the charge dipole that, in turn, induces the rearrangement in the charge clouds of the M-MOF to collaborate with the dipole of the H₂ molecule. Interestingly, the σ^* state of the H₂ molecule in the side-on configuration on the TED region is arranged strangely, with the symmetry axis not perpendicular to but made an angle with the H–H bond.

3.4 Gravimetric and volumetric hydrogen storage capacities of M(BDC)(TED)_{0.5} MOFs

Before calculating the hydrogen storage capacities, we have to obtain the point charge for the atoms of the M-MOF in terms of the DDEC6 framework, where the point charge of hidden atoms is also calculated with better accuracy compared to the Bader partition method. The unit cell size and the geometric structure of M(BDC)(TED)_{0.5} were first optimized by the vdW-DF density functional theory calculations and the charge density of the obtained structure was exported. The atomic point charge was then computed with the DDEC6 package, which is listed in Table 4 for Ni(BDC)(TED)_{0.5}. The atomic indices are shown in Fig. 7. For the substitutions of the other metals, calculating their partial charges is also performed using the same methodology and steps.

By GCMC simulations for the system repeating by $3 \times 3 \times 3$ times of the DFT unit cell, this work studies the H₂ uptake capacity for excess adsorption (n_{exc}) and absolute adsorption (n_{abs}) per the unit mass and volume at cryogenic (77 K) and room (298 K) temperatures, where n_{abs} is calculated *via* n_{exc} using the expression (6).⁶⁰ Before officially computing the H₂ uptake capacities of M(BDC)(TED)_{0.5}, we are going to validate

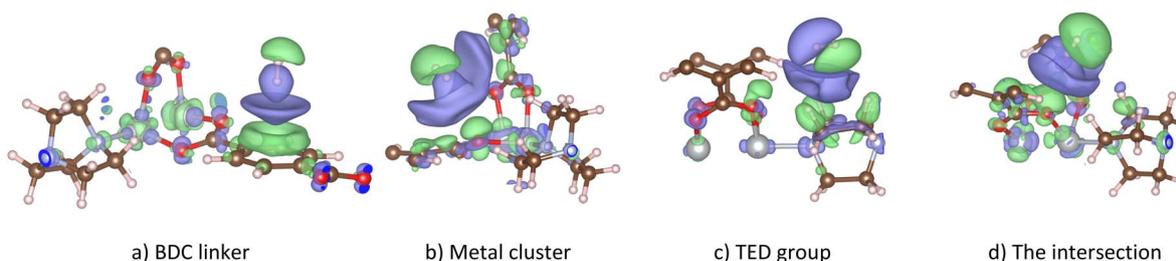


Fig. 6 The charge density difference of H₂@Ni(BDC)(TED)_{0.5} at the favourable adsorption sites (iso-surface level at $8 \times 10^{-5} e^- \text{ Bohr}^{-3}$): BDC linker (a), metal cluster (b), TED group (c), and the intersection (d). Purple and green present negative charge gain and loss, respectively. Similar characteristics of the charge density difference were also found for the other metal substitutions.



Table 4 The DDEC6 partial charges of the H, C, O, N, and Ni atoms of pristine Ni(BDC)(TED)_{0.5} with the atom labels presented in Fig. 7

Atoms	q (e)	Atoms	q (e)						
H	0.093277	H	0.074371	C2	-0.06467	C2	-0.06565	O	-0.53948
H	0.093177	H	0.074219	C2	-0.07018	C3	0.638866	O	-0.51495
H	0.094422	H	0.064973	C2	-0.06689	C4	-0.081851	O	-0.53399
H	0.092604	H	0.06552	C2	-0.0655	C3	0.634135	O	-0.52034
H	0.092547	H	0.074004	C3	0.637809	C4	-0.075996	O	-0.53516
H	0.093763	H	0.067559	C4	-0.08061	C1	-0.026607	O	-0.52142
H	0.094164	H	0.071051	C3	0.634733	C1	-0.029119	O	-0.53036
H	0.092883	H	0.076798	C4	-0.07643	C1	-0.019935	O	-0.52943
H	0.067228	H	0.06806	C2	-0.06137	C1	-0.024998	Ni	0.667318
H	0.074921	C1	-0.02552	C2	-0.06856	N	-0.115297	Ni	0.653275
H	0.068644	C1	-0.02485	C2	-0.06969	N	-0.121477		

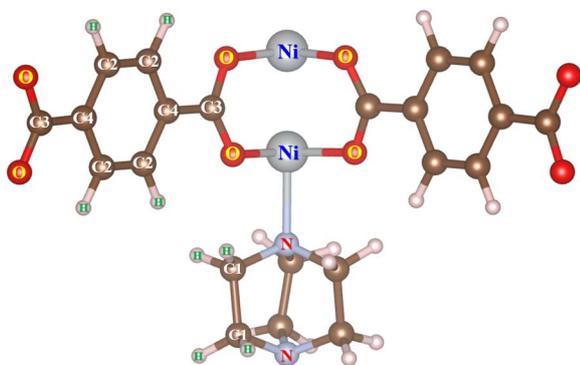
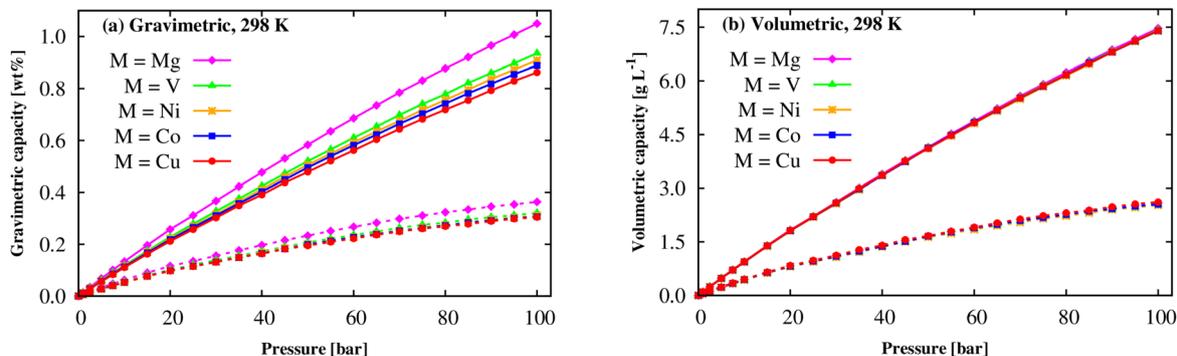


Fig. 7 The atomic indices for the M-MOF atoms.

our model within a rigid M-MOF structure and the selected LJ force field parameters (Subsection 2.2). Although we do not intend to study Zn(BDC)(TED)_{0.5}, the experimental isotherms of this M-MOF are available and shown in the full range of 0–50 bar pressures and at temperatures of 298 K and 77 K. As shown in Fig. S1 and Table S1 of ESI,[†] our obtained results, with the same model as Subsection 2.2, are in good agreement, particularly for 298 K, with the experiment with an error of well below 20% for the gravimetric excess loadings. Using flexible and new parameterized force fields perhaps solves the discrepancies. However, such force fields are not available in the present work.

For gravimetric loadings at 298 K, Fig. 8a shows that the n_{abs} and n_{exc} quantities monotonically increase as the pressures increase up to 100 bar. Mg can significantly enhance the isotherms over the other metals, and the absolute amount increases relatively faster than the excess quantity. In a close-up view, for each pressure, the gravimetric adsorption capacity is in the order: Cu-MOF < Co-MOF < Ni-MOF < V-MOF < Mg-MOF. Here, the Mg(BDC)(TED)_{0.5} achieves the highest H₂ uptake capacity among the studied M-MOFs with $n_{\text{exc}} = 0.36$ wt% and $n_{\text{abs}} = 1.05$ wt%, see Table 5. However, the gravimetric excess and absolute capacities are slightly different for the other metals at room temperature and pressure of 100 bar. The results exhibited that gravimetric H₂ uptakes of M(BDC)(TED)_{0.5} are an acceptable agreement with the experiments for Co(BDC)(DABCO)_{0.5},^{61,62} Cu(BDC)(DABCO)_{0.5} (ref. 62) (DABCO = TED), and comparable to those of well-known MOFs such as MIL-101 (Cr),⁶³ but lower than those of the best MOFs so far, *i.e.*, MOF-74 (Mg),⁶⁴ Be₁₂(OH)₁₂(BTB)₄,²¹ and MOF-5,⁶⁵ and slightly higher than MIL-88A (M).¹³ Note that the best MOFs only achieved 1–2 wt% absolute H₂ uptake at ambient conditions.^{11–13,23,24} A monotonic behaviour (Fig. 8b) is also found for the volumetric excess and absolute uptakes for all the cases of metals. Also, the metal substitution negligibly impacts volumetric H₂ storage capacity at ambient conditions. The maximum values for the volumetric excess and absolute loadings are about 2.55 and 7.40 g L⁻¹ (*i.e.*, 29.0 and 83.5 cm³ (STP)

Fig. 8 The H₂ adsorption isotherms of the M(BDC)(TED)_{0.5} MOF at 298 K: gravimetric loading (a) and volumetric loading (b). The solid and dashed lines present the absolute (n_{abs}) and excess (n_{exc}) loadings, respectively.

cm^{-3} , STP = standard temperature and pressure) at 298 K and the pressure of 100 bar. These values are the same as those of MIL-88A (M);¹³ however, the maximum absolute capacity of M-MOF is lower than the best MOF, $\text{Be}_{12}(\text{OH})_{12}(\text{BTB})_4$.²¹ We can also decrease the temperature to cryogenic condition to significantly increase the hydrogen uptake capacities.^{11,60}

At the cryogenic temperature of 77 K, Fig. 9 shows that a similar behaviour was found for the gravimetric and volumetric uptake capacities, where the absolute and excess curves increase quickly at low pressures, and then the excess uptakes approach the maximum values at the pressure of 20 bar for $M = \text{Mg}, \text{V}, \text{Co}, \text{Cu}$ and of 25 bar for $M = \text{Ni}$, while the absolute values continue increasing until 100 bar. The maximum values are shown in Table 6. We found that $\text{Mg}(\text{BDC})(\text{TED})_{0.5}$ also obtains the best gravimetric and volumetric H_2 adsorption capacities at 77 K, $n_{\text{exc}} = 5.80 \text{ wt}\%$ and $n_{\text{abs}} = 7.42 \text{ wt}\%$ followed by $\text{V-MOF} > \text{Ni-MOF} > \text{Co-MOF} > \text{Cu-MOF}$ for gravimetric uptake, 41.26 g L^{-1} and 52.77 g L^{-1} and slightly higher than the other M-MOFs. Although the gravimetric H_2 storage capacity of the M-MOFs is still lower than that of the best MOFs such as MOF-177, MOF-210, and NU-100, comparable to that of MOF-5 and $\text{Be}_{12}(\text{OH})_{12}(\text{BTB})_4$, but significantly higher than that of MOF-74, MIL-53 (M), $\text{Zn}(\text{BDC})(\text{TED})_{0.5}$, and MIL-88A (M) (Table 6).

Remarkably, our result for Co-MOF shows a reasonable agreement with the experimental data, 4.87 vs. 4.11 wt%.⁶² To date, much attention has been paid to gravimetric capacities and less volumetric capacities to reach DOE's target. Our results indicated that M-MOFs exhibit comparable volumetric uptakes to MIL-88A (M) and significantly higher than those 43 g L^{-1} at 100 bar of $\text{Be}_{12}(\text{OH})_{12}(\text{BTB})_4$.²¹ We also found that the adsorbed H_2 amounts at 77 K are much higher than those at 298 K, also meeting the DOE targets. Therefore, the $\text{M}(\text{BDC})(\text{TED})_{0.5}$ MOFs are promising for hydrogen storage at low temperatures.

As shown in the above parts, we observed that the Ni and Mg substitutions displayed the best and the second-best enhancements of the H_2 adsorption energy at the adsorption sites. However, their order is opposite for the gravimetric and volumetric storage capacities. The order of their adsorption energies can be explained *via* the differences in their electronic structure properties, as discussed in the upper section. We now have to study the effects of structural characteristics such as specific surface area (SSA) and pore volume (V_{pore}) of M-MOFs to see whether there are any influences of these factors on the H_2 adsorption capacity, particularly for the gravimetric uptake because of more significant variations found for the metal substitutions. The data are visualized in Fig. 10, which shows

Table 5 The maximum H_2 adsorption capacity of $\text{M}(\text{BDC})(\text{TED})_{0.5}$ compared to the previous MOFs at 298 K

MOFs	Pressure (bar)	Excess (absolute) uptakes	
		Gravimetric in wt%	Volumetric in g L^{-1}
Mg-MOF	100	0.36 (1.05)	2.59 (7.47)
V-MOF	100	0.32 (0.94)	2.55 (7.42)
Ni-MOF	100	0.31 (0.91)	2.53 (7.39)
Co-MOF	100	0.31 (0.90)	2.55 (7.39)
Cu-MOF	100	0.30 (0.86)	2.62 (7.40)
$\text{Co}(\text{BDC})(\text{DABCO})_{0.5}$	100	0.32 (293 K) ⁶²	
$\text{Cu}(\text{BDC})(\text{DABCO})_{0.5}$	100	0.42 (293 K) ⁶²	
MIL-101 (Cr)	80	0.43 (ref. 63)	
MOF-74 (Mg)	100	0.80 (ref. 64)	
$\text{Be}_{12}(\text{OH})_{12}(\text{BTB})_4$	95	1.0 (2.3) ²¹	(11) ²¹
MOF-5	48	1.65 (ref. 65)	
MIL-88A (M) ($M = \text{Co}, \text{Fe}, \text{Ni}, \text{Mn}, \text{Cr}, \text{V}, \text{Ti}, \text{Sc}$) (simulation)	100	0.22–0.29 (0.63–0.72) ¹²	2.44–2.83 (6.94–7.08) ¹²

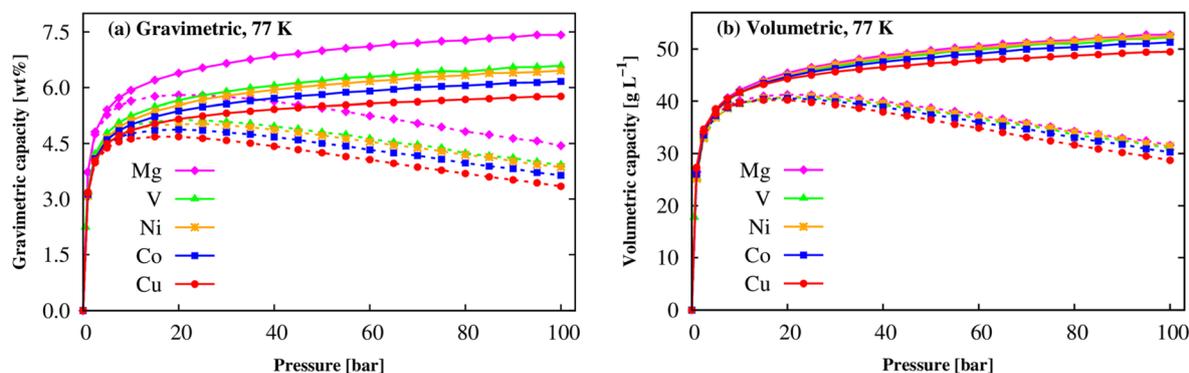
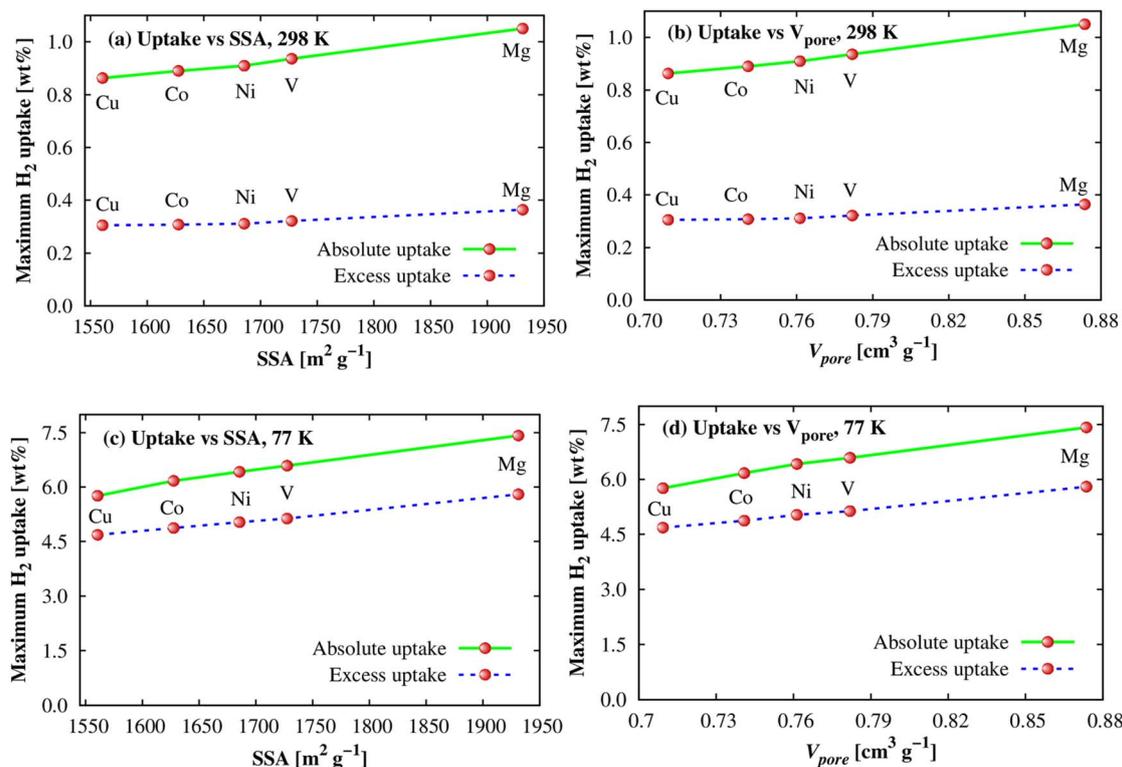


Fig. 9 The H_2 adsorption isotherms of the $\text{M}(\text{BDC})(\text{TED})_{0.5}$ MOFs at 77 K: gravimetric uptake (a) and volumetric uptake (b). The solid and dashed lines present the absolute and excess uptakes, respectively.



Table 6 The maximum H₂ adsorption capacity of M(BDC)(TED)_{0.5}, compared to the previous MOFs at 77 K

MOFs	Pressure for excess (absolute) uptakes, bar	Excess (absolute) uptakes	
		Gravimetric, wt%	Volumetric, g L ⁻¹
Mg-MOF	20 (100)	5.80 (7.42)	41.26 (52.77)
V-MOF	20 (100)	5.13 (6.59)	40.71 (52.23)
Ni-MOF	25 (100)	5.03 (6.42)	40.91 (52.52)
Co-MOF	20 (100)	4.87 (6.17)	40.55 (51.29)
Cu-MOF	20 (100)	4.11 (ref. 62)	40.20 (49.47)
MOF-74	30	4.68 (5.76)	
MIL-53 (M) (M = Al, Cr)	16	2.8 (ref. 70)	
Zn(BDC)(TED) _{0.5}	20	3.8 (Al), 3.1 (Cr) ⁷¹	
		~4.06 (UFF), ~4.38 (Buch potential), ³³ ~4.28 (experiment) ³³	
MIL-88A (M) (M = Co, Fe, Ni, Mn, Cr, V, Ti, Sc) (simulation)	10–15 (100)	4.00–4.63 (4.60–5.30) ¹²	43.78–45.51 (50.57–51.99) ¹¹
MOF-5	65	5.1 (ref. 22)	
Be ₁₂ (OH) ₁₂ (BTB) ₄	20 (100)	6.0 (9.2) ²¹	(43) ²¹
MOF-177	70	7.5 (11) ²⁰	
MOF-210	80	8.6 (17.6) ¹⁸	
NU-100	56 (70)	9.95 (16.4) ¹⁹	

Fig. 10 The dependence of the H₂ gravimetric uptakes on SSA and pore volume of M-MOFs at 298 K (a and b) and 77 K (c and d).

a correlation between the maximum gravimetric uptake *versus* SSA and V_{pore} at 298 K (Fig. 10a and b) and 77 K (Fig. 10c and d). It shows that the correlations are almost linear. Compared to 298 K, the linear dependences of the adsorption amount at 77 K on SSA and V_{pore} are also more obvious. This behaviour was also found for several MOFs in the literature,^{12,66,67} higher than Chahine's rule that was widely accepted in many previous works

that every 500 m² g⁻¹ of SSA obtains *ca.* 1.0 wt% saturated H₂ loading at 77 K and the pressure \geq 20 bar.^{67–69}

4 Conclusions

We investigated the hydrogen storage in M(BDC)(TED)_{0.5} metal-organic framework (M = Mg, V, Co, Ni, and Cu) by the



combination of the vdW-DF density functional theory calculations and the grand canonical Monte Carlo simulations. We obtained the most favourable adsorption sites and configurations for the hydrogen molecule in $M(\text{BDC})(\text{TED})_{0.5}$. The favourable order for the H_2 adsorption sites is the metal cluster–TED intersection > TED group > metal cluster > BDC linker for $M = \text{Mg}, \text{V}, \text{Ni}$, and Cu , but the metal cluster–TED intersection > metal cluster > TED group > BDC linker for $M = \text{Co}$. The constructive order for enhancing the H_2 adsorption strength is $\text{Ni} > \text{Mg} > \text{V} > \text{Co} > \text{Cu}$. The H_2 molecule uses its σ^* antibonding state, while $M(\text{BDC})(\text{TED})_{0.5}$ mainly uses the d orbital of the metal atoms for $M = \text{Ni}, \text{V}, \text{Cu}$, and Co and the p orbital of the O, C, N atoms for $M = \text{Mg}$, to participate in the interaction between the H_2 molecule and $M(\text{BDC})(\text{TED})_{0.5}$. This interaction is physisorption with the local rearrangement of charge dipoles without charge exchange crossing the adsorbate and the adsorbent. Considering the effects of temperature and pressure, we obtained the gravimetric and volumetric H_2 uptake capacities and found that the adsorption ability of $M(\text{BDC})(\text{TED})_{0.5}$ with $M = \text{Mg}$ is the best one among the considered metal substitutions. The Mg atoms bring not only the differences in the characteristics of DOS but also the largest specific surface area and pore volume to facilitate hydrogen storage.

Data availability

The data supporting this article have been included as part of the ESI.†

Author contributions

Conceptualization (DNS, NTXH), formal analysis (DNS, NTXH, NTYN), investigation (NTXH, DNS), resources (DNS, NTXH, VTN, VC), supervision (DNS, VC), validation (NTXH, DNS, VTN), visualization (NTXH, NTYN), writing of original draft (DNS, NTXH), reviewing and editing (DNS, NTXH, VC).

Conflicts of interest

There are no conflicts of interest to declare.

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