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## 1. Introduction

The development of natural gas resources has become particularly important because of the increasing demand for clean energy around the world. Among the known natural gas reservoirs, those with a high-sulfur content account for a high proportion.<sup>1,2</sup> High-sulfur gas reservoirs (HSGR) refer to reservoirs with a relatively high content (>2%) of hydrogen sulfide. In the HSGR development, sulfur deposition often occurs to block the pore throats that are abundant in the formations, remarkably lowering gas productivity.<sup>3–5</sup> The occurrence of sulfur deposition comes from the solubility reduction of elemental sulfur in natural gas, which leads to the formation and precipitation of solid sulfur.<sup>3–7</sup> Understanding the solubility evolution of elemental sulfur in natural gas is the basis of controlling sulfur deposition in practice.

Unfortunately, little is known about the molecular mechanism of sulfur dissolution in natural gas. For example, elemental sulfur has many allotropes, such as  $S_N$  (N = 2, 3, ...,8), that may coexist under the formation conditions. Their contents vary with buried depth.  $S_2$  content increases with

# Molecular mechanism of elemental sulfur dissolution in H<sub>2</sub>S under stratal conditions†

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Resulting from the solubility reduction of elemental sulfur during the development of high sulfur gas formations, sulfur deposition often occurs to reduce the gas production and threaten the safety of gas wells. Understanding the dissolution mechanism of elemental sulfur in natural gas is essential to reduce the risk caused by sulfur deposition. Because of the harsh conditions in the high-sulfur formations, it remains challenging to *in situ* characterize the dissolution–precipitation processes, making deficient the knowledge of sulfur dissolution mechanism. The dissolution of sulfur allotropes (S<sub>N</sub>, N = 2, 4, 6 and 8) in H<sub>2</sub>S, the main solvent of sulfur in natural gas, is studied in this work by means of first-principles calculations and molecular dynamics simulations. While S<sub>6</sub> and S<sub>8</sub> undergo physical interaction with H<sub>2</sub>S and form stable polysulfides. Unravelling the mechanism would be helpful for understanding and controlling the sulfur deposition in high-sulfur gas development.

temperature, while S<sub>8</sub> content decreases with temperature.<sup>8</sup> It remains unclear what the solute is among these allotropes, while H<sub>2</sub>S has been well identified as the main solvent. Furthermore, there remains controversary whether the dissolution is a chemical or a physical process. It has been reported that elemental sulfur forms  $H_2S_n$  through association with  $H_2S$ under the temperature and pressure that are comparable to the formation conditions.<sup>8-11</sup> Yu et al.<sup>11</sup> characterized the H<sub>2</sub>S<sub>N</sub> species at 120-250 °C in the S-H<sub>2</sub>S-CH<sub>4</sub>-H<sub>2</sub>O systems with Raman spectroscopy. However, the number of S atoms in the polysulfides was not addressed in the experiments. Moreover, the *in situ* characterization of  $H_2S_N$  species in high-sulfur gas formation remains challenging. Polysulfides were not detected when the experimental temperature was below 373 K,9 but detected under 393-523 K.11 In a computational study, He et al.<sup>12</sup> reported that in the ground-state  $S_N$ -H<sub>2</sub>S complexes, the interaction between  $S_N (N = 2, 4, 6 \text{ and } 8)$  and  $H_2S$  is as weak as a typical physical interaction, but the effect of temperature was not considered. Intermolecular physical interaction was assumed in some recent molecular simulations13-16 in which the force fields describing only the non-covalent interactions were used. In practice, however, the dissolution process is treated as a chemical reaction from which the Chrastil model<sup>17</sup> is often used to estimate the solubility variations.18-23 It can be concluded that there is not sufficient evidence to classify the sulfur dissolution in natural gas as a chemical or a physical process.

The pronounced distinctions between chemical and physical processes may lead to different strategies in controlling the sulfur deposition in natural gas development. For example, the

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sensitivity with respect to temperature is usually different between these two processes because of their different energy barriers. Then, different temperature control strategies should be used for these two processes. It is therefore of great significance to identify the molecular mechanism of sulfur dissolution in natural gas. In this work, we first conducted first-principles molecular dynamics (FPMD) calculations on the S<sub>N</sub>-H<sub>2</sub>S mixtures of N = 2, 4, 6 and 8, followed by quantum chemical calculations on their reaction paths and activation energies. Direct evidences are provided for the interaction between the solute and solvent molecules under a varying formation depth at which the temperature and pressure vary accordingly. Our study unravels the interaction mechanism of elementary sulfur with H<sub>2</sub>S at the atomistic level, laying a basis for the further studies of real systems with additional components of CH<sub>4</sub>,  $CO_2$ , etc.

## 2. Computational methods

 $S_N$  (N = 2, 4, 6 and 8) are selected as the solute molecules and H<sub>2</sub>S as the solvent in our FPMD simulations. The ground-state structures of these allotropes have been well characterized in previous studies.<sup>24-26</sup> Fig. 1 illustrates the molecular structures of sulfur oligomers. S4 is a linear molecule with its two end atoms on the same side of the middle two atoms.  $S_6$  and  $S_8$  are cyclic with  $C_{3v}$  and  $C_{4v}$  symmetry, respectively. Given the low solubility of elemental sulfur in H<sub>2</sub>S (about 0.001 in molar ratio), the computational models are constructed by putting randomly one hundred H<sub>2</sub>S molecules and one S<sub>N</sub> molecule into a cubic box with an initial density of  $0.8 \text{ g cm}^{-3}$ . Periodic boundary conditions are applied in the three directions. Fig. 2 illustrates the models in which S2-S8 are surrounded by H2S molecules. The side length of the cubic is about 1.95 nm, which is long enough to avoid from the interaction of two S<sub>N</sub> molecules in the adjacent boxes.

The Born–Oppenheimer molecular dynamics (BOMD) simulations<sup>27</sup> are carried out under the isothermal–isobaric (NPT) ensemble. The temperature is controlled by using the canonical sampling through velocity rescaling (CSVR) thermostat,<sup>28</sup> while the pressure is controlled using the Martyna–Tobias–Klein (MTK) barostat.<sup>29</sup> A number sets of temperature



Fig. 1 The ground-state structures of molecular  $S_2$  (a),  $S_4$  (b),  $S_6$  (c) and  $S_8$  (d).

and pressure are applied by considering the geological strata at Sichuan Basin in Southwest China, which is one of the main high-sulfur gas reservoirs in the world. Table 1 lists the pressure and temperature at different depths of the geological strata, which are used in our FPMD simulations. A total of 25 ps simulations are applied for all the systems. The simulations, unless otherwise mentioned, usually reach their equilibrations within 15 ps, while the remaining time is used for data collection and analysis. The time step is set to 1 fs. All atoms in the structures underwent unconstrained relaxation to their equilibrium positions without any fixation. Energy minimization was performed using the Orbital Transformation (OT) method, and the convergence criterion was set to 10<sup>-6</sup> atomic units (a.u.). The exchange-correlation functional of Perdew-Burke-Ernzerhof (PBE)<sup>30</sup> with a semi-empirical DFT-D3 correction<sup>31</sup> to the dispersion effect is used in the studied systems that are characterized by their weak intermolecular interaction. The double- c basis set (DZVP-MOLOPT)32 combined with Goedecker-Teter-Hutter (GTH) pseudopotentials33 are employed in the DFT calculations. The energy cutoff is set to 400 Ry in the self-consistent calculations. The FPMD calculations are performed using the CP2K package's Quickstep module.34,35

The radial distribution function (RDF), denoted as g(r), stands as a frequently employed tool in statistical mechanics for characterizing the microstructure of disordered systems. The g(r) signifies the probability of finding another particle ( $\beta$ ) at a radial distance r, with any particle ( $\alpha$ ) acting as the center. It can be mathematically expressed by<sup>16</sup>

$$g(r) = \frac{n(r)}{4\pi r^2 \rho_0 \delta_r} \tag{1}$$

where *r* represents the specified central atomic radius. n(r) denotes the number of particles of type  $\beta$  found within a shell of thickness  $\delta_{r}$ .  $\rho_0$  is the number density of particle of type  $\beta$  in the whole system. The RDF analysis, as implemented in the VMD software,<sup>38</sup> is applied to the coordinate files derived from FDMD simulations for the studied mixtures.

Then, the reaction paths and energy barriers for the reactions of  $S_n$  with  $H_2S$  are studied by DFT calculations with B3LYP<sup>39,40</sup>/6-311++G(d,p)<sup>41</sup> and M06-2X<sup>42</sup>/6-311++G(2d,2p),<sup>41</sup> as implemented in the Gaussian 16 package.43 While B3LYP is known for its robust predictive power across a broad range of chemical systems, M06-2X provides enhanced accuracy particularly in systems involving complex non-covalent interactions. All the structures including reactants, intermediates, transitionstate structures, and products are optimized and further verified with vibrational frequency calculations at the same level. The frequency scaling factor is 0.987 (ref. 44) under B3LYP/6-311++G(d,p), and 0.970 (ref. 45) under M06-2X/6-311++G(2d,2p). In these calculations, the long-range dispersion effect is considered by including the semi-empirical correction of DFT-D3.31 Since the FPMD simulations indicate that two H<sub>2</sub>S molecules are involved in their reactions with S<sub>2</sub>, the reaction paths with both one and two H<sub>2</sub>S molecules are designed. The synchronous transit guided quasi-Newton (STQN) method<sup>46,47</sup> is used to search for the transition-state structure based on the optimized structures, which are further identified by their exact



Fig. 2 Initial simulation models of  $S_2$  (a),  $S_4$  (b),  $S_6$  (c) and  $S_8$  (d) in  $H_2S$  (red for  $S_N$  and others for  $H_2S$ ).

Table 1Temperature and pressure at the depths of geological strataat Sichuan Basin, Southwest China.36.37

| Depth (km) | Pressure (MPa) | Temperature (K) |  |  |
|------------|----------------|-----------------|--|--|
| 1          | 15             | 310             |  |  |
| 2          | 30             | 340             |  |  |
| 3          | 45             | 370             |  |  |
| 4          | 60             | 400             |  |  |
| 5          | 75             | 430             |  |  |
| 6          | 90             | 460             |  |  |
|            |                |                 |  |  |

one imaginary frequency in vibrational spectra. The intrinsic reaction coordinate  $(IRC)^{34,48}$  calculations are performed to verify that the transition-state structures are able to connect contiguously the stable reactants, intermediates and products. The Shermo package<sup>49</sup> is used to derive the thermodynamic correction terms for the computed structures. Single-point calculations at the CCSD(T)<sup>50</sup> level with the aug-cc-pVQZ basis set<sup>51</sup> are conducted for the optimized structures. The complete basis set (CBS) extrapolation<sup>52</sup> is used to refine the computed values by conducting additional single-point calculations with the aug-cc-pVTZ basis set. The parameters for the CBS extrapolation are taken from the work by Neese *et al.*<sup>53</sup> Finally, the single-point energy is incorporated into the calculated free energy correction to yield the Gibbs free energy ( $\Delta G$ ).<sup>54,55</sup>

### 3. Results and discussions

We first verify the validity of our computational strategy by comparing the computed density of pure  $H_2S$  with the

measurements.<sup>56</sup> Fig. 3 shows the predicted and measured densities of  $H_2S$  at a varying depth. The predicted values are the averaged densities obtained from the equilibrium configurations of  $H_2S$  relaxed in an NPT ensemble consisting of 100  $H_2S$  molecules. The predicted densities overestimate the corresponding measurements by about 12–18%. The systematic overestimation in the predicted densities indicates the used functional and dispersion correction are inadequate to describe well the intermolecular interaction in the  $H_2S$  systems. The small size of the studied model may also have a contribution to the overestimation. The gaps remain almost unchanged between the predicted and measured values in the studied temperature and pressure ranges. It should be mentioned that



Fig. 3 Comparison between the computed and measured density of pure  $H_2S$  at a varying stratigraphic depth. The corresponding temperatures and pressures are given in Table 1.

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the critical point is about 373 K and 9 MPa for  $H_2S$ ,<sup>57</sup> which is within the studied range. Nevertheless, our computations produce reliable density of pure  $H_2S$ , appropriate for the comparison of the reactivity of  $S_N$  allotropes with  $H_2S$ .

In their equilibrium configurations in the  $S_2$ -H<sub>2</sub>S mixtures, a new compound, H<sub>2</sub>S<sub>3</sub>, is characterized in all the simulations at different stratigraphic depths. Fig. 4 shows the snapshots of the  $S_2$ -H<sub>2</sub>S mixtures after reaching their equilibrium states. At 1 km (Fig. 4a), H<sub>2</sub>S<sub>3</sub> is a linear molecule totally different from the combination of H<sub>2</sub>S and S<sub>2</sub>. Instead, the bonds in the system are reorganized. The three S atoms are in the middle, ended by two H atoms. The conformers of H<sub>2</sub>S<sub>3</sub> are slightly different in the snapshots at different depths. However, it is evident that chemical reactions occur between H<sub>2</sub>S and S<sub>2</sub> in all the cases.

The formation of  $H_2S_3$  can be illustrated by tracking the interatomic bond lengths. By analyzing the molecular configuration variations in the slides, one finds that two  $H_2S$  molecules are involved in the chemical reactions. As presented in Fig. 5, the distances of three pairs, D1, D2 and D3, in  $H_2S_3$  are thus defined for the involved molecules. At low temperature at 1 km, the slow rates allow us to have some details about the reaction. After 2 ps fluctuations, D1 drops to about 2.15 Å, and keeps steadily in the left time, indicating that the S atom of one  $H_2S$  molecule approaches to the S atom in  $S_2$  and form a S–S bond. At about 15 ps, two S–H bonds are formed. One is formed by the other S atom in  $S_2$  with the H atom in the second  $H_2S$  molecule.

The other is formed by the H atom in the first  $H_2S$  molecule with the S atom in the second  $H_2S$  molecule. It is in fact a reaction catalyzed by the second  $H_2S$ , which donates one H atom to  $S_2$ and accept one H atom from the first  $H_2S$ .

Under higher temperatures at the deeper stratas, the reactions proceed in a similar path but a fast rate. For example, D1 is formed at about 5 ps at 3 km, while D2 and D3 at about 7 ps. At 5 and 6 km, the formation of the three bonds is completed within 1 ps. The averaged interatomic distances, D1, D2, and D3, in the equilibrium configurations are around 2.08, 1.37, and 1.36 Å, respectively. It is apparent that chemical bonds, one S–S and two S–H, are formed. The bond lengths are in agreement with previous studies<sup>58,59</sup> in which the corresponding bond lengths are 2.054, 1.344, and 1.336 Å, respectively. Remember that temperature effect was not included in the previous studies.

The molecules of  $S_4$ ,  $S_6$ , and  $S_8$  have different experiences during the simulations. At all the studied stratigraphic depths, these three molecules do not show an evident reaction with H<sub>2</sub>S. As presented in Fig. S1–S3 in the ESI,<sup>†</sup> the  $S_N$  molecule in the equilibrium configurations is surrounded by several H<sub>2</sub>S molecules, but none of which forms a bond with  $S_N$ . In other words, only non-bonded interaction exists in the systems of H<sub>2</sub>S and  $S_N$  (N = 4, 6 and 8). In the previous DFT calculations,<sup>12</sup> the interaction energy between H<sub>2</sub>S and  $S_N$  (N = 4, 6, and 8) is about 1–3 kcal mol<sup>-1</sup>, which indicates a typical physical interacting pattern between them. Under harsh conditions at the deepest



Fig. 4 Snapshots of the molecular configurations of  $S_N$  in  $H_2S$  at a varying stratigraphic depth (red and green balls are for S and H atoms in  $H_2S_3$ , others for atoms in  $H_2S$ ). 1 km (a), 2 km (b), 3 km (c), 4 km (d), 5 km (e) and 6 km (f).



**Fig. 5** Variations in the interatomic distances among the three molecules involved in the reactions of  $S_2$  with  $H_2S$ . The involved atoms are traced from the last frame of the simulations. The interatomic distances, D1, D2 and D3, are marked in the insert (a) where S atoms are in green and hydrogen atoms in red. 1 km (a), 2 km (b), 3 km (c), 4 km (d), 5 km (e) and 6 km (f).

strata (460 K and 90 MPa), the three molecules retain their structures, as shown in Fig. S1–S3.†

Fig. 6 shows the RDF of the mixtures of  $S_N$  with  $H_2S$ . The interatomic distances between the S atom in  $S_N$  and H/S atom in  $H_2S$  are given. For  $S_4$ , the first peaks occur at 3.95 Å for the intermolecular S–S (Fig. 6d), and 3.75 Å for intermolecular S–H (Fig. 6a). It is apparent that no chemical bonds are formed between  $S_4$  and  $H_2S$  at all the studied stratigraphic depths. Similar analysis can be made for  $S_6$  and  $S_8$  (Fig. 6b, c, e and f), as well as a similar conclusion that  $S_6$  and  $S_8$  do not form chemical bonds with  $H_2S$  under the studied conditions. Moreover, the

peaks for the intermolecular S–S pairs are outstanding, while those for the S–H pairs are ignorable. This implies that the interaction is dominated by S–S pairs. It is the S atom in H<sub>2</sub>S that interacts with S<sub>N</sub>, which is similar to the case of S<sub>2</sub> with H<sub>2</sub>S. The attraction of S–S pairs has also been addressed in other studies.<sup>16</sup> The four atoms in S<sub>4</sub> may have different activity toward H<sub>2</sub>S. Fig. S4<sup>†</sup> compares the RDFs of the central and the terminal atoms with the S atom in H<sub>2</sub>S. The first peaks for these two types of atoms are similar both in position and height, and disordered H<sub>2</sub>S distributions are noted at long distances,



Fig. 6 RDFs of S atoms in  $S_N$  (N = 2, 4, 8) with atoms in  $H_2S$  at the stratigraphic depths of 1–6 km. S ( $S_4$ )–H ( $H_2S$ ) (a), S ( $S_6$ )–H ( $H_2S$ ) (b), S ( $S_8$ )–H ( $H_2S$ ) (c), S ( $S_4$ )–S ( $H_2S$ ) (d), S ( $S_6$ )–S ( $H_2S$ ) (e) and S ( $S_8$ )–S ( $H_2S$ ) (f).

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indicating that these two atoms do not exhibit much differences when they interact toward  $H_2S$ .

The dissolution of sulfur in  $H_2S$  thus has two paths, chemical and physical. In the physical path,  $S_N$  is surrounded by  $H_2S$ *via* weak non-bonded forces including Coulomb, van der Waals, dispersion, polarization, *etc.* The solubility contributed from physical interaction is determined by the strengths of these non-bonded forces. In the chemical path, the solubility is in fact contributed by the chemical reactions of  $S_N$  with  $H_2S$ . Understanding the reaction mechanism is thus helpful to control the solubility variations under the stratigraphic conditions. Although our AIMD simulations indicate that  $S_4$ ,  $S_6$ , and  $S_8$  do not react with  $H_2S$ . Considering the short simulation time, further investigations on their reaction paths and their activation barriers are necessary.

From the stoichiometric view,  $H_2S_3$  is the combination of one  $H_2S$  molecule and one  $S_2$  molecule, but the FPMD simulations indicate that two  $H_2S$  molecules sequentially interact with the  $S_2$ 

molecule in the reactions. Therefore, two paths are designed for the reactions, which are presented in Scheme 1. In Path I, S<sub>2</sub> first binds with H<sub>2</sub>S, forming an intermediate (IM1) in which only weak non-bonded interaction exists between them. A reorganization then occurs in IM1 to form a transition-state structure (TS1), followed by the formation of H<sub>2</sub>S<sub>3</sub> (P1). In Path II, its first step, the formation of IM1, is the same with Path I. In the next step, IM1 interacts with the second H<sub>2</sub>S. After the formation of a transition-state structure (TS2), H<sub>2</sub>S<sub>3</sub> (P1) is formed, accompanied by the release of one H<sub>2</sub>S molecule. Therefore, Path I contains two steps, while Path II has three steps.

All the structures shown in Scheme 1 are optimized and further identified with vibrational frequency calculations. Their structures are shown in Fig. 7 and their energy, and Gibbs free energy at 298 K and 0.1 MPa are given in Tables 2 and S1–S4.<sup>†</sup> Considering that the triplet state of S<sub>2</sub> is more stable by 16.98 kcal mol<sup>-1</sup> than its singlet, and the singlet state of H<sub>2</sub>S<sub>3</sub> is more stable by 47.29 kcal mol<sup>-1</sup> than its triplet, both the singlet



Scheme 1 Reaction paths of  $S_2$  with  $H_2S$  (the bonds to be broken are red, and those to be formed are in green).



**Fig. 7** Structure optimized at M06-2X/6-311++G(2d,2p) level.  $IM1^{T}$  (a),  $TS1^{S}$  (b),  $TS1^{T}$  (c),  $P1^{S}$  (d),  $P1^{T}$  (e),  $R2^{S}$  (f),  $R2^{T}$  (g),  $TS2^{S}$  (h),  $TS2^{T}$  (i),  $P2^{S}$  (j) and  $P2^{T}$  (k). S and T denote the singlet and triplet states, respectively.

**Table 2** Computed Gibbs free energy ( $\Delta G$ , in kcal mol<sup>-1</sup>) of reactants, intermediates, transition-state structures, and products (the Gibbs free energy of the triplet reactants in Paths I and II are taken as the references, and the values in parentheses are for the triplet states)

|                                  | R1     | IM1    | TS1     | P1      | R2     | TS2     | P2      |
|----------------------------------|--------|--------|---------|---------|--------|---------|---------|
| B3LYP/6-311++G(d,p)              | 23.33  | _      | 45.70   | -0.99   | 19.63  | 26.71   | -7.22   |
|                                  | (0.00) | (4.67) | (35.06) | (32.71) | (0.00) | (31.89) | (26.38) |
| CCSD(T)/aug-cc-pVQZ <sup>a</sup> | 17.63  |        | 55.39   | -6.90   | 18.01  | 25.49   | -13.40  |
|                                  | (0.00) | (4.89) | (40.89) | (36.48) | (0.00) | (41.58) | (41.58) |
| CCSD(T)/aug-cc-pVTZ <sup>a</sup> | 17.97  |        | 56.19   | -5.55   | 18.60  | 26.65   | -11.95  |
|                                  | (0.00) | (4.79) | (40.37) | (36.14) | (0.00) | (41.51) | (31.33) |
| M06-2X/6-311++G(2d,2p)           | 22.00  |        | 37.69   | -9.31   | 16.45  | 19.05   | -17.10  |
|                                  | (0.00) | (5.46) | (37.95) | (34.15) | (0.00) | (32.13) | (25.31) |
| CCSD(T)/aug-cc-pVQZ <sup>b</sup> | 17.89  |        | 37.07   | -8.48   | 15.93  | 20.14   | -16.40  |
|                                  | (0.00) | (5.41) | (40.36) | (36.29) | (0.00) | (36.54) | (27.60) |
| CCSD(T)/aug-cc-pVTZ <sup>b</sup> | 18.26  |        | 38.73   | -6.86   | 16.83  | 21.74   | -14.78  |
|                                  | (0.00) | (5.31) | (40.20) | (36.10) | (0.00) | (36.54) | (27.49) |
| $CCSD(T)/CBS^b$                  | 17.78  | _      | 36.59   | -8.92   | 15.67  | 19.63   | -16.87  |
|                                  | (0.00) | (5.45) | (40.39) | (36.38) | (0.00) | (36.48) | (27.62) |

and triplet states of these structures are taken into account in the structure optimization and vibrational frequency calculations. For IM1, only the triplet structure is identified, while its singlet structure is unstable.

Although structures optimized with B3LYP/6-311++G(d,p)and M06-2X/6-311++G(2d,2p) are topologically similar, they exhibit different stability at the CCSD(T) level at the CBS limit. As shown in Table 2, the  $\Delta G$  values on the B3LYP-optimized structures are higher than those on the corresponding M06-2X-optimized structures. Therefore, the  $\Delta G$  values obtained at the CCSD(T) level on the M06-2X structures are used for the subsequent analysis. Starting from IM1 in Path I, the H<sub>2</sub>S molecule rotates about the intermolecular S…S linker until one of its H atoms bonds with the other S atom in S<sub>2</sub> to form TS1. TS1 has a four-membered ring in which the S-S double bond of S<sub>2</sub> is weakened, and becomes a single bond. Meanwhile, its two S atoms form one S-S bond and one S-H bond with H<sub>2</sub>S, and one of the original S-H bonds is broken. P1 is then formed. Fig. 8 presents the energy landscape of Path I. The triplet structures are more stable for R1 and IM1, but less stable for TS1 and P1 than the corresponding singlet structures. A spin multiplicity transition from the triplet to the singlet states occurs in the formation of TS1. The identified energy barrier is

thus between the triplet IM1 and the singlet TS1, 31.66 kcal  $mol^{-1}$ , for Path I.

In Path II, starting from IM1, the second H<sub>2</sub>S forms a sixmembered ring with IM1 (TS2) with its S atom linking to the H atom of the first H<sub>2</sub>S, and one of its H atoms linking to the S atom of S2. An isodesmic reaction in which the type and number of the bonds formed in the product is identical to those broken in the reactant then occurs by losing two S-H bonds and simultaneously forming two S-H bonds. In the product, the formed H<sub>2</sub>S is leaving from the H<sub>2</sub>S<sub>3</sub>. Similar to Path I, the singlet structures are more stable than the triplet structures for TS2 and P2. The energy barrier of Path II is thus between the triplet R2 and the singlet TS2, 20.14 kcal  $mol^{-1}$ . It is evident that Path II has a lower barrier than Path I, which is attributed to the stable six-membered ring structure and the isodesmic reorganization in TS. The isodesmic reactions usually proceed under facile conditions because the required energy for the bond breaking is mostly compensated by the released energy in the bond formation.<sup>60-62</sup> It is thus the reactions of  $S_2$  with  $H_2S$ proceed by involving one S2 and two H2S molecules. In both paths, the products have lower energy than the corresponding reactants, indicating that the products are stable and the reactions are exothermic. The revealed kinetics verifies the



Fig. 8 Comparison of the energy barriers of the reactions of (a) one  $H_2S$  with one  $S_2$  and (b) two  $H_2S$  with one  $S_2$ .



Fig. 9 Intermediates (IM3 (a), IM4 (d) and IM5 (g)), transition-state structures (TS3 (b), TS4 (e) and TS5 (h)), products (P3 (c), P4 (f) and P5 (i)) for the reactions of  $S_4$ ,  $S_6$  and  $S_8$  with  $H_2S$ , which are optimized at the M06-2X/6-311++G(2d,2p) level.



Fig. 10 Gibbs free energies of the reactants, intermediates, transition-state structures, and products for the reactions of  $S_4$  (a),  $S_6$  (b) and  $S_8$  (c) with  $H_2S$ , which are calculated at the CCSD(T)/aug-cc-pVTZ level.

formation of  $H_2S_3$  and the reaction mechanism observed in the FPMD simulations.

For N = 4, 6 and 8, the reactions start from the attack of S atom in H<sub>2</sub>S toward the terminal atom in S<sub>4</sub>, and one atom in S<sub>6</sub> and S<sub>8</sub>, forming the intermediates (IM3, IM4 and IM5 in Fig. 9). Then, one of H atoms in H<sub>2</sub>S attacks the other terminal S atom in S<sub>4</sub>, forming the transition-state structure (TS3) with a six-membered ring. H<sub>2</sub>S<sub>5</sub> is then formed by breaking the H–S bond in H<sub>2</sub>S. For S<sub>6</sub> and S<sub>8</sub>, the transition-state structures (TS4 and TS5) have a fourmembered ring consisting of two S atoms in S<sub>N</sub> and one S and one H atom in H<sub>2</sub>S. The formation of polysulfides, H<sub>2</sub>S<sub>7</sub> and H<sub>2</sub>S<sub>9</sub>, is facilitated by the breaking of S–S bond in S<sub>N</sub>.

Fig. 10 illustrates the Gibbs free energies of the identified reactants, intermediates, transition-state structures and products shown in Fig. 9, and their optimized structures and thermodynamic parameters in Tables S12–S20 of ESI.<sup>†</sup> For the reaction of S<sub>4</sub> with H<sub>2</sub>S, the energy barrier is 25.84 kcal mol<sup>-1</sup>,

only 6.21 kcal mol<sup>-1</sup> higher than that of  $S_2$ , indicating that  $S_4$  is also reactive toward  $H_2S$ . The low barrier is attributed to the reactivity of the terminal S atoms in  $S_4$ , as well as the stable sixmembered ring in the transition-state structure. For  $S_6$  and  $S_8$ , the corresponding barriers are 54.02 and 62.54 kcal mol<sup>-1</sup>, respectively. The high barriers are mainly attributed to the bond-breaking of S–S bond, and the strain in the fourmembered rings in the transition-state structures. Therefore,  $S_6$  and  $S_8$  unlikely react with  $H_2S$  under typical geological conditions. The dissolution of  $S_N$  allotropes in  $H_2S$  has different mechanism, physical for  $S_6$  and  $S_8$ , and chemical for  $S_2$  and  $S_4$ .

## 4. Conclusions

DFT calculations and MD simulations are carried out to study the dissolution mechanism of elemental sulfur in its main solvent,  $H_2S$ , in high-sulfur gas formations. The interacting models of sulfur allotropes  $S_N$  (N = 2, 4, 6 and 8) with  $H_2S$  molecules are created and simulated with FPMD under the temperature and pressure ranges corresponding the stratal depth of 1–6 km. While FPMD simulations indicate that only  $S_2$  is active toward  $H_2S$ , quantum chemical calculations on the reaction paths reveal that both the reactions of  $S_2$  and  $S_4$  with  $H_2S$  have low activation energies, contrast to the high barriers in the reactions of  $S_6$  and  $S_8$ . These  $S_N$  allotropes have different activities toward  $H_2S$ , indicating a chemical dissolution for  $S_2$  and  $S_4$  in  $H_2S$  under typical geological conditions, and a physical dissolution for  $S_6$  and  $S_8$ . Our computations reveal the molecular mechanism of sulfur dissolution in  $H_2S$ , which lays the groundwork for future study of the solubility evolution of elemental sulfur in natural gas.

## Author contributions

Sheng Yuan: conceptualization, data curation, writing original draft. Ying Wan: investigation, methodology, conceptualization. Li Wang: resources. Nong Li: validation, data curation. Mingli Yang: supervision, validation, Shengping Yu: sata curation. Li Zhang: formal analysis, methodology, conceptualization.

## Conflicts of interest

The authors declare no conflicts of interest.

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