


Cite this: *RSC Adv.*, 2024, 14, 10209

# Mechanisms of manipulating valley splitting in MoTe<sub>2</sub>/MnS<sub>2</sub> van der Waals heterostructure by electric field and strains†

Xiao Liang,<sup>a</sup> Yiqun Liu,<sup>a</sup> Tianjun Zhong,<sup>a</sup> Ting Yang,<sup>a</sup> Jie Li,<sup>a</sup> Li Luo,<sup>a</sup> Gao Dong,<sup>b</sup> Yanhong Chen,<sup>a</sup> Xuelian Luo,<sup>a</sup> Tingting Tang<sup>\*a</sup> and Lei Bi<sup>\*b</sup>

In this study, we discuss the tunability of valley splitting using first-principles calculations with a monolayer MoTe<sub>2</sub> and layered ferromagnetic MnS<sub>2</sub> heterostructure as an example. We observe that, due to the magnetic proximity effect (MPE) at the interface, a monolayer of MoTe<sub>2</sub> can exhibit a significant valley splitting of 55.2 meV. The production of the interlayer dipoles with spin-adapted configuration could be the origin of MPE at the interface. Furthermore, the valley splitting can be regulated continuously by the perpendicular electric field and biaxial strain. Interestingly, the valley splitting increases with the increasing induced magnetic moments in MoTe<sub>2</sub> by applying an electric field while the inverse laws are presented by applying biaxial strains, which indicates that the mechanisms of valley splitting manipulating in these two ways are quite different. The calculation results suggest that the electric field influences the electric dipole distributions at the interface, which determines the induced magnetic moments in monolayer MoTe<sub>2</sub>, and results in valley splitting variations. However, biaxial strains not only affect MPE at the interface but also the intrinsic spin splitting caused by spin–orbital coupling (SOC) effects of monolayer MoTe<sub>2</sub> itself and the latter is even the dominating mechanism of valley splitting variations.

Received 8th February 2024

Accepted 9th March 2024

DOI: 10.1039/d4ra01013b

rsc.li/rsc-advances

## 1. Introduction

Recent studies of two-dimensional transition-metal dichalcogenides (2D-TMDCs) have revealed many new phenomena such as the quantum spin/valley anomalous Hall effect,<sup>1–3</sup> valley-dependent optoelectronics,<sup>4</sup> spin/valley polarization of plasmons,<sup>5–7</sup> magneto-optical conductivity,<sup>8</sup> electrical transport of valley carriers,<sup>9–11</sup> and spin-polarized edge currents,<sup>12</sup> which have generated intense interest in these valley-polarized systems. As a result of strong intrinsic spin–orbit coupling (SOC) and inversion symmetry broken effect, 2D-TMDCs exhibit distinct valley-selective states with different angular momenta, named K and K' valleys, which brings a new degree of freedom to photoelectric devices.<sup>13–15</sup> Therefore, 2D-TMDCs have emerged as promising candidates for optical, nanoelectronics and optoelectronics applications, propelling the development of valleytronics.<sup>16–20</sup> Despite significant advances in 2D-TMDC based valleytronics devices, maneuvering a pair of valleys in

2D-TMDCs still poses a significant challenge because the pair is locked by the time-reversed symmetry (TRS) energy degradation, limiting the device's tunability of the valleys.<sup>21,22</sup>

To solve this problem, it is necessary to break TRS in 2D-TMDCs, and then dynamically and efficiently polarize the K and K' valleys, which requires exciting carriers to produce a transient non-equilibrium distribution in both valleys. One effective strategy to break this correlation and induce non-equilibrium carrier distributions in the valleys is through the utilization of ultrafast circularly polarized laser pumping, which leverages the optical Stark effect.<sup>13,23–25</sup> Nevertheless, optical pumping is also facing the challenge of precise control and is constrained by the inherently short carrier lifetimes. An alternative strategy involves applying a vertical magnetic field, leveraging the Zeeman effect to break the valley degeneracy.<sup>14,22</sup> However, achieving significant valley splitting typically demands the use of strong magnetic fields exceeding 10 tesla, which greatly enhances the power dissipation and is inconvenient to miniaturization and integration of nano-devices.

Recent research studies have proposed an approach to introduce non-range magnetic orders to 2D-TMDCs through magnetic proximity effects (MPE),<sup>15,26</sup> resulting from their adjacency to ferromagnetic materials such as EuO,<sup>26</sup> EuS,<sup>27–29</sup> MnO,<sup>21</sup> Fe<sub>2</sub>O<sub>3</sub>,<sup>30</sup> and YMnO<sub>3</sub>.<sup>31</sup> However, it is worth noting that the application of the bulk substrates inherently constrains the scalability of devices in the nanoscale regime. Traditional magnetic materials, due to the principle of lattice adaptation,

<sup>a</sup>Optoelectronic Sensor Devices and Systems Key Laboratory of Sichuan Provincial University, Chengdu University of Information Technology, Chengdu 610225, China. E-mail: liangxiao@cuit.edu.cn; skottt@163.com

<sup>b</sup>National Engineering Research Center of Electromagnetic Radiation Control Materials, University of Electronic Science and Technology of China, Chengdu 610054, China. E-mail: bilei@uestc.edu.cn

† Electronic supplementary information (ESI) available. See DOI: <https://doi.org/10.1039/d4ra01013b>



are difficult to prepare *in situ* heterojunctions. In addition to the aforementioned methods, a promising avenue for enhanced valley control involves the creation of vertical two-dimensional magnetic van der Waals (vdW) heterostructures employing layered two-dimensional materials. This particular approach offers the advantage of forming exceptionally clean interfaces, thereby mitigating impurity scattering effects. Furthermore, it minimizes the impact of lattice mismatch, a factor that can otherwise weaken the observed valley splitting.<sup>15</sup> The inherent flexibility of layer stacking processes offers a versatile means of creating van der Waals heterostructures by seamlessly combining integration of the layered ferromagnets with a variety of 2D materials, including graphene, Weyl semimetals such as  $\text{WTe}_2$ , and superconductors such as  $\text{NbSe}_2$ .<sup>32</sup> The bond-free vdW interactions in heterostructure provide a natural interfacial strain relaxation,<sup>33</sup> and vdW heterostructure may exhibit superior properties through strain.<sup>34</sup> Furthermore, the advantage of constructing heterostructures exclusively from 2D materials cannot be overstated, as it streamlines the integration process when fabricating valley electronic devices. Notably, recent theoretical predictions and experimental discoveries concerning 2D  $\text{WSe}_2/\text{CrI}_3$  heterostructures have unveiled their remarkable attributes, demonstrating significant valley splitting and the potential for optically controllable valley pseudo-spin.<sup>35</sup> In view of these advantages, the strategic engineering and the assembly of 2D layered magnetic/semiconductor heterostructures assume paramount importance in the exploration of spin valley splitting phenomena. A recent development of great significance lies in the theoretical prediction of  $\text{MnS}_2$  monolayers as ferromagnetic semiconductor materials exhibiting a high Curie temperature.<sup>36,37</sup> What makes this particularly compelling is the minimal lattice mismatch observed between  $\text{MoTe}_2$  and  $\text{MnS}_2$  monolayers, measuring a mere 3.52 Å for  $\text{MoTe}_2$  (ref. 38–40) and 3.47 Å for  $\text{MnS}_2$ .<sup>36</sup> This observation underpins the promise of the  $\text{MoTe}_2/\text{MnS}_2$  heterostructure, which has the potential to manifest valleytronics properties and holds great promise for a wide array of applications in valleytronics devices.

We employed density functional theory in this study to study the precise modulation of valley degrees of freedom within monolayer  $\text{MoTe}_2/\text{MnS}_2$  heterostructures. The TRS of the  $\text{MoTe}_2$  monolayer undergoes perturbation due to the MPE arising from the ferromagnetic (FM)  $\text{MnS}_2$  substrate. This interaction leads to a large degree of substantial static valley polarization within the heterostructure, accompanied by a discernible valley splitting of 55 meV. We meticulously explored the manipulation of both spin and valley properties by subjecting the system to an electric field oriented in the vertical direction and biaxial strain. Notably, our analysis reveals that in the K-valley and K'-valley, the Berry curvatures exhibit opposing signs. These findings underscore the exciting potential for the application of 2D magnetic vdW heterostructures in the realm of valley electronic devices.

## 2. Computational method

In this work, all first-principles calculations based on density functional theory (DFT) were performed using the Vienna Ab

into Simulation Package (VASP).<sup>41</sup> The electron-ion interaction is solved by the method of the projected enhanced wave. To characterize the electron exchange–correlation interaction, the generalized gradient approximation (GGA) in the Perdew–Burke–Ernzerhof (PBE) functional was employed.<sup>42</sup> The cut-off energy was set to 500 eV, and a vacuum layer of 20 Å along the z-direction was introduced to mitigate the effect of periodic boundary conditions. In order to correctly describe the strongly correlated electrons in the partially filled d subshells, the GGA +  $U_{\text{eff}}$  method was employed, with  $U_{\text{eff}}$  set to 3.9 eV for Mn,<sup>36,43,44</sup> which previous reports have conducted tests on,<sup>45,46</sup> and the results are in excellent accordance with the experimental data.<sup>47</sup> Various values of  $U_{\text{eff}}$  were also explored in our study to demonstrate the appropriateness of the chosen  $U_{\text{eff}}$  and the general results of our study were not affected by the qualitative tests.<sup>48</sup> For  $\text{MoTe}_2$ ,  $\text{MnS}_2$ , and  $\text{MoTe}_2/\text{MnS}_2$  heterostructures, the Brillouin zone integration was sampled using a  $12 \times 12 \times 1$  gamma-pack *k*-point meshes for both structure optimization and static electronic structure calculations, and adjusting the direction of the magnetic moment by adjusting the SAXIS parameter in INCAR for band structure calculations. For the calculation of the Berry curvature, the maximally localized Wannier functions (MLWFs)<sup>49</sup> from WANNIER90 (ref. 50) were used. The force convergence criterion was set to be less than  $0.01 \text{ eV Å}^{-1}$ , and the electron iteration convergence criterion was established at  $1 \times 10^{-5} \text{ eV}$ , ensuring complete relaxation of the structural parameters and atomic positions. Additionally, the SOC effect was taken into account in electronic structure calculations.

## 3. Results and discussion

The optimized structures of the  $\text{MnS}_2$  with the space group  $P3m1$ ,  $\text{MoTe}_2$  with the space group  $P6/mmc$  and  $\text{MoTe}_2/\text{MnS}_2$  heterostructures are illustrated in Fig. 1a–c. The lattice constants for the optimized monolayers of  $\text{MnS}_2$  and  $\text{MoTe}_2$  were determined to be 3.47 Å and 3.52 Å, respectively. These values are in agreement with those from the earlier research. Under the aforementioned lattice parameters, the monolayers of  $\text{MnS}_2$  and  $\text{MoTe}_2$  exhibit vertical stacking of their primitive cells, resulting in a lattice mismatch of approximately 1.44%, laying the groundwork for constructing the  $\text{MoTe}_2/\text{MnS}_2$  vdWHs comprising  $\text{MoTe}_2$  and  $\text{MnS}_2$ . In Fig. 1c, 'd' represents the layer spacing at the energy nadir of the heterostructure formation between  $\text{MoTe}_2$  and  $\text{MnS}_2$ .  $\text{MoTe}_2$  and  $\text{MnS}_2$  monolayers exhibit four distinct configurations arising from the translational and rotational operations, as shown in Fig. 1d, AA: Te1 and Te2 atoms are above the S1 atoms and the Mo atom is above the Mn atom, AA\*: Te1 and Te2 atoms are above the S2 atoms and the Mo atom is above the Mn atom, AB: Te1 and Te2 atoms are above the S2 atoms and the Mo atom is above the S1 atom, AB\*: Te1 and Te2 atoms are above the S2 atoms and the Mo atom is above the S1 atom.

To ascertain the most stable configuration, the binding energy  $E_b$  for the  $\text{MoTe}_2/\text{MnS}_2$  heterostructures can be computed using the following relationship



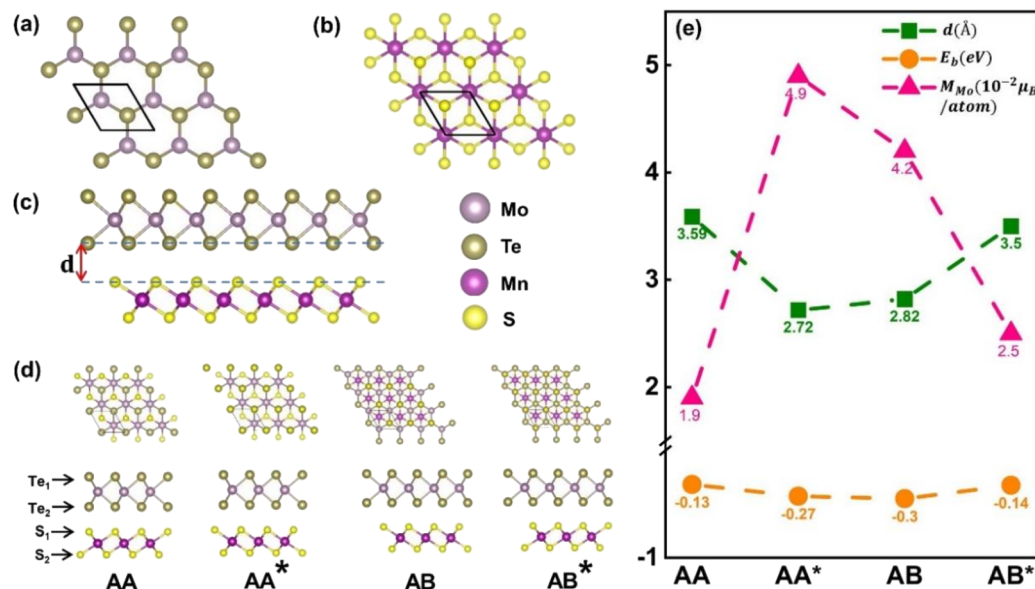


Fig. 1 The optimized structures of (a)  $MnS_2$  and (b)  $MoTe_2$  monolayers, (c) side view of the  $MnS_2/MoTe_2$  vdWHs, (d) top and side views of four stacked conformations. (e) Layer spacing of the four conformations, d, binding energy  $E_b$  and magnetic moments of Mo atoms.

$$E_b = E_{MoTe_2/MnS_2} - E_{MoTe_2} - E_{MnS_2}$$

where  $E_{MoTe_2/MnS_2}$ ,  $E_{MoTe_2}$ , and  $E_{MnS_2}$  are the total energy of  $MoTe_2/MnS_2$  heterostructure, and pristine monolayers of  $MoTe_2$  and  $MnS_2$ , respectively. The  $E_b$  for all four patterns are negative, indicating that these configurations are possible to exist. Notably, the  $E_b$  value for the AB pattern is the lowest. In our investigation, we conducted a systematic analysis of the interlayer distances and the Mo atomic magnetic moment, as depicted in Fig. 1e. Notably, we observed that the  $MoTe_2/MnS_2$  heterostructure in the AB configuration, with a layer spacing of 2.82, exhibits the lowest binding energy  $E_b$ , indicating its superior stability. Subsequently, we gave precedence to the AB configuration in our subsequent exploration of valley spin splitting. Moreover, in the same configuration, there exists a direct correlation between the layer spacing and the magnetic moment. Specifically, the magnetic moment of the Mo atoms intensifies as the monolayer  $MoTe_2$  approaches the substrate material within a certain range, while the magnetic moment of the Mo atoms diminishes as it moves farther away from the substrate material. Using the AB configuration as an example, we observe that the relationship between the layer spacing and valley splitting exhibits a similar trend to the variation of magnetic moments (see Fig. S1 in the ESI†).

Fig. 2a and b illustrate the band structures at the K-valley and K'-valley, respectively. The solid red and blue lines represent the band edges of spin-up and spin-down states in the  $MoTe_2$  band structure.  $\Delta_{soc}^{C/V}$  represents the spin splitting of  $MoTe_2$  without an applied magnetic field, which arises from the spin-orbit coupling in  $MoTe_2$  itself.  $\Delta_{spin}^{C/V,+/-}$  represents the spin splitting of  $MoTe_2$  under a magnetic field, where 'C' and 'V' denote the conduction band (CB) and valence band (VB), and '+' and '-' denote the K-valley and K'-valley, respectively.  $\Delta_{CB/VB}$  in the figure represents the valley splitting in the conduction band/

valence band. We define  $\Delta_{CB/VB} = E_{CB1/VB1'} - E_{CB1'/VB1}$ .  $\Delta'_{CB/VB} = E_{CB2'/VB2'} - E_{CB2'/VB2}$ ,  $\Delta_{opt}^+$  and  $\Delta_{opt}^-$  represent the absorption energy levels for left- and right-polarized light at the K-valley and K'-valley, respectively. We define the total K and K' valley Zeeman splitting as  $E_Z = \Delta_{opt}^+ - \Delta_{opt}^-$ .

The atom-projected band structures of  $MoTe_2$  and  $MoTe_2/MnS_2$  heterostructures are depicted in Fig. 2c and d, respectively. Notably, we observed that the K-valley and K'-valley of  $MoTe_2$  are strongly retained within the heterostructures. In the isolated  $MoTe_2$  structure, the electronic band structure exhibits varying degrees of spin splitting at the conduction band (CB) and valence band (VB) edges, primarily due to the influence of SOC. However, owing to the constraints imposed by TRS, the spin splitting in the K-valley and K'-valley remains symmetric, thereby precluding the occurrence of the valley Zeeman splitting. Upon forming a heterostructure with  $MnS_2$ , the MPE induces a limited magnetic moment in  $MoTe_2$ , thereby breaking the TRS inherent in the band structure. Consequently, the spin splitting in the K-valley and K'-valley ceases to be symmetric, giving rise to the emergence of valley Zeeman splitting. Remarkably, the valley Zeeman splitting magnitude in  $MoTe_2$  is 55.2 meV, which is greater than the reported values of valley splitting in  $MoTe_2/CrI_3$  (5.9 meV),<sup>51</sup>  $MoTe_2/NiCl_2$  (32.5 meV),<sup>45</sup> and  $MoTe_2/EuO$ .<sup>26</sup> Our computational findings bear substantial significance for prospective research endeavors. As exemplified in Fig. 2e, we scrutinized the atom-projected band structure of the  $MoTe_2/MnS_2$  heterostructure under in-plane magnetization. In this configuration,  $MoTe_2$  undergoes magnetization without exhibiting valley Zeeman splitting, suggesting that only the out-of-plane magnetization exerts an influence on valley splitting. The nuanced relationship between magnetization direction and valley splitting is further elucidated in Fig. 2f, accompanied by an inset illustrating the magnetization angle. During the rotation of the Mn atom's

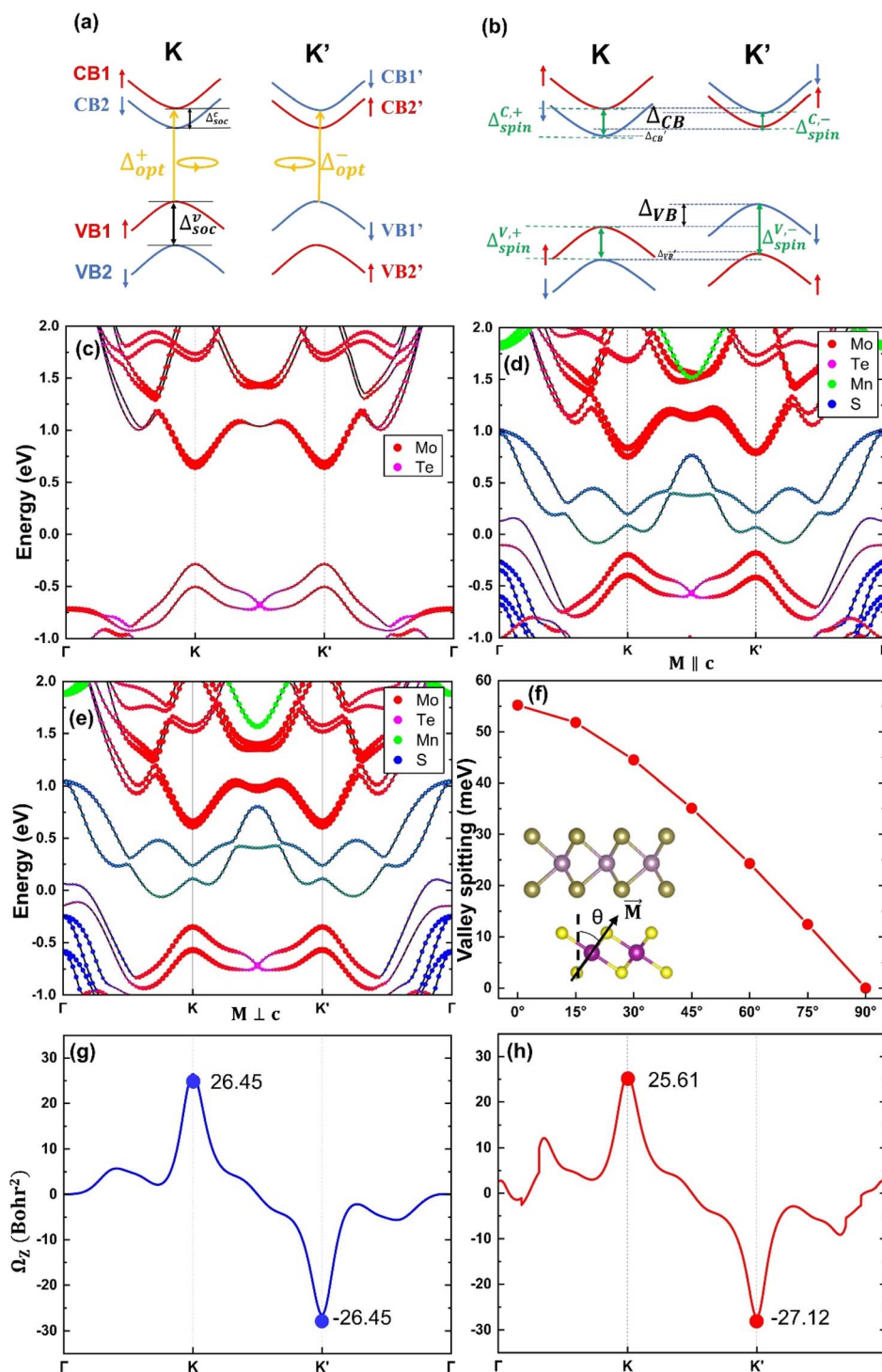


Fig. 2 (a) Schematic band structure of the K-valley and K'-valley without an applied magnetic field.  $\Delta_{\text{opt}}^+$  and  $\Delta_{\text{opt}}^-$  represent the absorption energy levels for left- and right-polarized light in the K-valley and K'-valley, respectively.  $E_{\text{SOC}}^c$  and  $E_{\text{SOC}}^v$  represent the spin splitting in the conduction band and valence band induced by SOC, respectively. The valley spin states of spin up and spin down are indicated by red up arrows and blue down arrows, respectively. (b) Schematic band structure of the KK' valleys under applied magnetic field.  $\Delta_{\text{CB}}$  and  $\Delta_{\text{VB}}$  represent the energy valley splitting of the conduction band and valence band, respectively.  $\Delta_{\text{spin}}^{c,+}$ ,  $\Delta_{\text{spin}}^{c,-}$  denote the spin splitting of the conduction band at the K and K' points, respectively, and  $\Delta_{\text{spin}}^{v,+}$ ,  $\Delta_{\text{spin}}^{v,-}$  represent the spin splitting of the valence band in the K-valley and K'-valley, respectively. (c) Band structure of the monolayer MoTe<sub>2</sub>. (d) Band structure of the MoTe<sub>2</sub>/MnS<sub>2</sub> heterostructure with the direction of magnetization parallel to the z-axis. (e) Band structure of the MoTe<sub>2</sub>/MnS<sub>2</sub> heterostructure with the direction of magnetization perpendicular to the z-axis. (f) Variation of the valley splitting with different magnetization angles. The illustration shows the angle of magnetization. (g) Berry curvature of monolayer MoTe<sub>2</sub>. (h) Berry curvature of the MoTe<sub>2</sub>/MnS<sub>2</sub> heterostructure.





direction of magnetization from the +Z direction ( $M\parallel c$ ) to the in-plane direction ( $M\perp c$ ), the valley splitting value remains positive, indicating that the valley splitting at the K-valley is higher than that at the K'-valley. Simultaneously, the value of valley Zeeman splitting gradually decreases from the maximum of 55.2 meV to 0. Therefore, the valley splitting can be adjusted by turning the direction of magnetization. Table 1 compares the spin splitting and valley splitting information for four different configurations. In the AA configuration, the valley Zeeman splitting is -11.9 meV, indicating that the valley splitting at the K' point is more than the valley splitting at the K point. The AA\* configuration exhibits the highest valley splitting, which may be attributed to the closest interlayer distance between MoTe<sub>2</sub> and MnS<sub>2</sub>, resulting in a significant magnetic proximity effect and the largest magnetic moment for Mo, leading to the large valley splitting.

To gain a better understanding of the large valley splitting induced by MPE, we build a low-energy effective Hamiltonian quantity according to the  $k\cdot p$  model.<sup>15</sup> The Hamiltonian quantity is denoted as:<sup>5,22</sup>

$$H = at(\tau k_x \hat{\sigma}_x + k_y \hat{\sigma}_y) + \frac{\Delta}{2} \hat{\sigma}_z - \lambda \tau \frac{\hat{\sigma}_z - 1}{2} \hat{s}_z + \frac{\hat{\sigma}_z - 1}{2} (\hat{s}_z + \tau \alpha) B$$

where  $a$ ,  $t$ ,  $\Delta$ ,  $2\lambda$ , and  $B$  are the lattice constant, effective hopping integral, band gap, SOC strength, orbital magnetic moment, and effective Zeeman magnetic field, respectively.<sup>52</sup>  $\hat{\sigma}$  are the Pauli matrices for the two base functions:  $|d_{z^2}\rangle$  and  $\frac{1}{\sqrt{2}}|d_{x^2-y^2} + i\tau d_{xy}\rangle$ . In this context,  $\tau = \pm 1$  represents the valley index, and  $\hat{s}_z = \pm 1$  represents the spin index. The Hamiltonian under consideration comprises four terms. The first three terms delineate the low-energy band dispersive characteristics of primitive monolayer MoTe<sub>2</sub>, while the fourth term encapsulates the exchange energy arising from the magnetic proximity effect. The valley splitting of the valence band denoted as  $\Delta_{VB}$ , can be deduced as  $2(1 + \alpha_V)B_V$  ( $\Delta'_{VB} = 2(1 - \alpha_V)B_V$ ), and the valley splitting of the conduction band, denoted as  $\Delta_{CB}$ , can be deduced as  $2(1 + \alpha_C)B_C$  ( $\Delta'_{CB} = 2(1 - \alpha_C)B_C$ ) by substituting the valley index  $\tau$  and spin index  $\hat{s}_z$  into the energy eigenvalue equation based on the Hamiltonian equation. By matching the intrinsic valley splitting to the first-principles calculations,  $\Delta_{VB} = 17.8$  meV and  $\Delta_{CB} = 37.3$  meV, the effective Zeeman field in the valence band,  $B_V$ , is obtained as 9.1 meV, and the effective Zeeman field in the conduction band,  $B_C$ , is obtained as 18.45 meV. In light of this, the valley Zeeman splitting arises from the interaction of the conduction and valence bands. Consequently,

we define the entire equivalent Zeeman field,  $B$ , is given by  $B = B_V + B_C$ , which corresponds to 27.55 meV. Switching a Bohr magneton to  $5.78 \times 10^{-5}$  eV T<sup>-1</sup>, the effective Zeeman fields,  $B_V$  and  $B_C$ , correspond to a perpendicular magnetic field of 476 T to the monolayer MoTe<sub>2</sub>.

Because of the intrinsic inversion symmetry breaking of MoTe<sub>2</sub>, along the out-of-plane, carriers at the K-valley and K'-valley obtained a nonzero Berry curvature. According to the derivation of the Kubo formula, the Berry curvature can be represented as the sum of contributions from the occupation states<sup>53,54</sup>

$$\Omega_z(k) = -\sum_n \sum_{n' \neq n} f_n \frac{2\text{Im}\langle \psi_{nk} | v_x | \psi_{n'k} \rangle \langle \psi_{n'k} | v_y | \psi_{nk} \rangle}{(E_n - E_{n'})^2}$$

where  $f_n$  is the Fermi-Dirac distribution function and  $v_{x(y)}$  is the velocity operator;  $|\psi_{nk}\rangle$  is the Bloch wave function with eigenvalue  $E_n$ . In Fig. 2g and h, we present the calculated Berry curvature along the high symmetry line for both monolayer MoTe<sub>2</sub> and the MoTe<sub>2</sub>/MnS<sub>2</sub> heterostructure. A compelling observation is the comparison of the Berry curvature values at K-valley and K'-valley in monolayer MoTe<sub>2</sub>, wherein we find that they possess identical magnitudes but exhibit opposite signs. Remarkably, upon the formation of the heterostructure, the preservation of the opposite signs in the Berry curvature suggests the retention of spin-valley properties. Furthermore, the absolute discrepancy in the Berry curvature values indicates the manifestation of TRS breaking in monolayer MoTe<sub>2</sub>, attributable to the presence of the magnetic substrate.

The control of the degree of valley polarization is crucial for fulfilling various device design requirements, given the significant valley properties of the MoTe<sub>2</sub>/MnS<sub>2</sub> heterostructure. By applying electric fields and in-plane biaxial strains to the MoTe<sub>2</sub>/MnS<sub>2</sub> heterostructure, there is a desire to achieve modulation of the degree of valley splitting. Applying an external electric field is an easily achievable method in the laboratory to control the electronic structure or valley properties.<sup>55</sup> We have calculated the band structure of MoTe<sub>2</sub>/MnS<sub>2</sub> under an externally applied electric field in the z-direction. A positive electric field represents the field pointing from MnS<sub>2</sub> towards MoTe<sub>2</sub>, while a negative electric field represents the electric field directed from MoTe<sub>2</sub> to MnS<sub>2</sub>. Fig. 3a shows the change in spin splitting of the valence and conduction bands. When a negative electric field is applied, with increasing electric field strength, we can observe an increase and gradual enlargement of  $\Delta_{\text{spin}}^{C,+}$ ,  $\Delta_{\text{spin}}^{C,-}$ , and  $\Delta_{\text{spin}}^{V,-}$  compared to the case

Table 1 Comparison between four configurations of MoTe<sub>2</sub>/MnS<sub>2</sub><sup>a</sup>

	$\Delta_{CB}$ (meV)	$\Delta_{VB}$ (meV)	$\Delta_{\text{spin}}^{C,+}$ (meV)	$\Delta_{\text{spin}}^{C,-}$ (meV)	$\Delta_{\text{spin}}^{V,+}$ (meV)	$\Delta_{\text{spin}}^{V,-}$ (meV)	$E_Z$ (meV)
AA	-12.0	0.1	23.5	47.2	221.5	212.6	-11.9
AA*	-44	152.2	0.4	72.2	77.3	31.0	115.8
AB	37.3	17.8	84.2	10.5	200.2	238.0	55.2
AB*	19.8	14.4	54.8	15.8	204.7	236.1	34.2

<sup>a</sup>  $\Delta_{CB/VB}$  representing the valley splitting in the conduction band/valence band.  $\Delta_{\text{spin}}^{C/V,+/-}$  representing the spin splitting.  $E_Z$  represents valley Zeeman splitting.



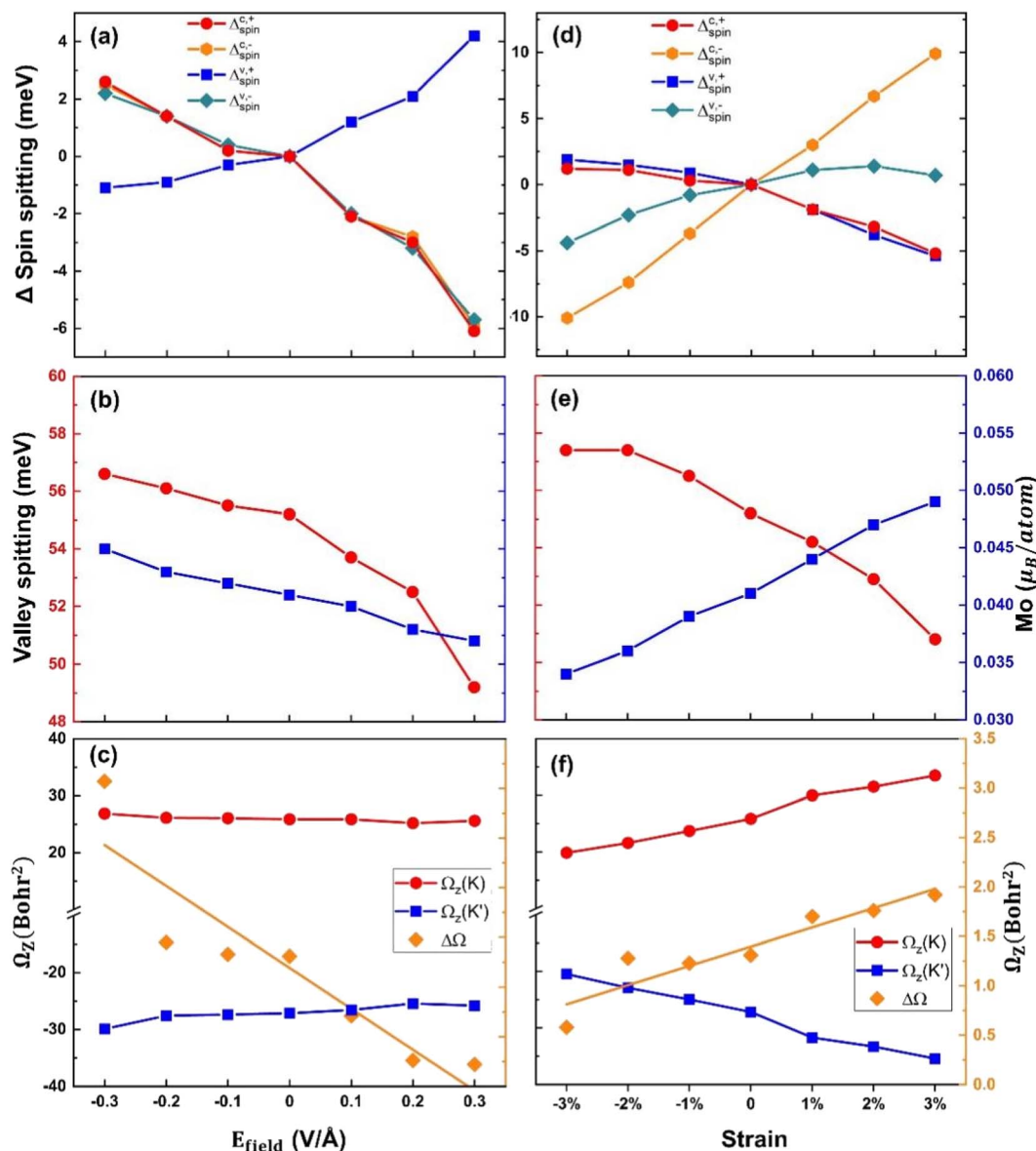


Fig. 3 (a and d) Spin splitting in the conduction and valence bands at the K and K' points. (b and e) Valley splitting in MoTe<sub>2</sub>/MnS<sub>2</sub> and the induced magnetic moment of Mo; the red and blue curves represent the valley splitting and magnetic moment, respectively. (c and f) Berry curvature and the difference in Berry curvature at the K and K' points.

without an electric field, while  $\Delta_{\text{spin}}^{V,+}$  gradually decreases. On the other hand, when a positive electric field is imposed, with the increasing electric field strength, we can observe a decrease and gradual reduction of  $\Delta_{\text{spin}}^{C,+}$ ,  $\Delta_{\text{spin}}^{C,-}$ , and  $\Delta_{\text{spin}}^{V,-}$  compared to the case without an electric field, while  $\Delta_{\text{spin}}^{V,+}$  gradually increases. Fig. 3b presents the relationship between valley splitting  $E_z$  and the Mo atomic magnetic moment as a function of the applied electric field. When the negative electric field is imposed, the magnetic moment of Mo atoms and the magnitude of valley splitting  $E_z$  both increase with the increasing electric field. At an intensity of  $-0.3 \text{ V } \text{\AA}^{-1}$ , the valley splitting reaches 56.6 meV. Conversely, when a positive electric field is applied, the magnetic moment of Mo atoms and the magnitude of valley splitting  $E_z$  are decreasing, with the valley splitting decreasing to 49.2 meV at

an intensity of  $+0.3 \text{ V } \text{\AA}^{-1}$ . These findings establish a positive correlation between the magnitude of valley splitting and the magnetic moment of Mo atoms. In Fig. 3c, we present a study of the influence of the electric field on the Berry curvature.  $\Omega_z(K)$  and  $\Omega_z(K')$  represent the Berry curvature at the K-valley and K'-valley, respectively, while  $\Delta\Omega$  represents the difference in Berry curvature between these two points. The electric field has little impact on  $\Omega_z(K)$ , but as the electric field increases, the value of  $\Omega_z(K')$  decreases, leading to a decrease in the difference in Berry curvature  $\Delta\Omega$ . This trend suggests a potential connection between the behavior of Berry curvature and the magnetic moment of Mo atoms.

In-plane strain is also a useful method for controlling the electronic characteristics of heterostructures and can be



performed through substrate tensile or bending.<sup>56–58</sup> Biaxial strain can be defined using the following equation:  $\varepsilon = (a - a_0)/a_0$ , which refers to the relative difference in the lattice constants before and after applying biaxial strain.  $a_0$  is the lattice constant without the applied strain.  $a$  is the lattice constant after applying strain. Fig. 3d shows the variation in spin splitting under biaxial stress. We define tensile strain as a positive value and compressive strain as a negative value. With an increase in compressive strain, the spin-splitting  $\Delta_{\text{spin}}^{\text{C},+}$  and  $\Delta_{\text{spin}}^{\text{V},+}$  slightly increase compared to the unstrained case, while  $\Delta_{\text{spin}}^{\text{C},-}$  and  $\Delta_{\text{spin}}^{\text{V},-}$  gradually decrease. When applying tensile strain, we can observe a decrease in  $\Delta_{\text{spin}}^{\text{C},+}$  and  $\Delta_{\text{spin}}^{\text{V},+}$  compared to the unstrained case, and they decrease further with an increase in strain. Conversely,  $\Delta_{\text{spin}}^{\text{C},-}$  and  $\Delta_{\text{spin}}^{\text{V},-}$  gradually increase with increasing tensile strain. As can be seen from the figure, the spin splitting in the  $K'$ -valley of the conduction band is changed to be sensitive. Fig. 3e illustrates the relationship between valley-splitting  $E_z$  and the Mo atomic magnetic moment under strain. With increasing compressive strain, the magnetic moment of Mo decreases, while the valley splitting  $E_z$  increases. At  $-3\%$  compressive strain, the valley splitting is 57.4 meV. Conversely, as tensile strain increases, the magnetic moment of Mo increases, while the valley splitting  $E_z$  decreases. At  $3\%$  tensile strain, the valley splitting is 50.8 meV. Notably, the size of the valley splitting does not exhibit a positive correlation with the Mo atomic magnetic moment; rather, a larger magnetic moment leads to a smaller valley splitting. This finding contrasts with the conclusions drawn from studies involving electric field manipulation. In Fig. 3f, the values of the Berry curvature  $\Omega_z(K)$  and  $\Omega_z(K')$  display a decreasing trend with increasing compressive strain, while increasing with escalating tensile strain. Additionally, the difference in the Berry curvature  $\Delta\Omega$  shows an increasing trend from compressive  $3\%$  to tensile  $3\%$ . Based on the observations from Fig. 3c and f, we can infer that the difference in Berry curvature is closely associated with the magnitude of the magnetic moment.

To gain a deeper understanding of the valley splitting characteristics in the  $\text{MoTe}_2/\text{MnS}_2$  heterostructure, we conducted an extensive investigation focusing on the underlying mechanisms influencing the Mo atom's magnetic moment. Specifically, we examined the electron transfer between the top layer material ( $\text{MoTe}_2$ ) and the substrate material ( $\text{MnS}_2$ ) under various conditions. We defined the accumulation of electrons as positive and the depletion of electrons as negative. At equilibrium, in the protocell of a heterojunction,  $\text{MoTe}_2$  loses electrons and  $\text{MnS}_2$  gains electrons. In Fig. 4a, the transfer of electrons from the  $\text{MoTe}_2$  layer to the  $\text{MnS}_2$  layer decreases as the electric field increases. According to what is shown in Fig. 3b, the Mo atomic magnetic moment also decreases linearly with the gradual increase of the electric field. In Fig. 4d, the transfer of electrons from the  $\text{MoTe}_2$  layer to the  $\text{MnS}_2$  layer increased as the strain increased. The Mo atomic magnetic moment also linearly increases with the gradual increase in strain according to what is shown in Fig. 3e. The magnitude of the Mo atomic magnetic moment shows a similar trend with the amount of  $\text{MoTe}_2$  electrons transferred. Every electron lost in the  $\text{MoTe}_2$  monolayer gives rise to a revised magnetic moment, which makes the

magnetic moment of Mo atoms increase. We can deduce from this analysis that the influence of the electric field as well as strain on the MPE is due to changing the number of electrons transferred between  $\text{MoTe}_2$  and  $\text{MnS}_2$ . Fig. 4b presents the planar differential charge density under different electric fields, with the top right inset depicting the three-dimensional differential charge density at  $-0.3 \text{ V \AA}^{-1}$  electric field and the bottom left inset representing the three-dimensional differential charge density at the  $+0.3 \text{ V \AA}^{-1}$  electric field. In the inset, the regions colored in yellow indicate electron accumulation, whereas the blue regions represent electron loss. Notably, the transferred electrons originating from  $\text{MoTe}_2$  do not directly enter  $\text{MnS}_2$  but instead induce the formation of an electric dipole moment between the two layers, as shown in the illustrations in Fig. 4a and d. Similarly, Fig. 4e demonstrates the planar differential charge density at different strains, with the top right inset representing the three-dimensional differential charge density at  $-0.3 \text{ V \AA}^{-1}$  electric field and the bottom left inset representing the three-dimensional differential charge density at  $+0.3 \text{ V \AA}^{-1}$  electric field. Importantly, our findings, as shown in Fig. 4b and e, align well with the observations presented in Fig. 4a and d.

In order to figure out the conclusions that the applied electric field and the strain appear differently we performed the following analysis. It is well known that the valley Zeeman splitting phenomenon is a result of the combined interaction of SOC and magnetic fields. Fig. 4c shows the variation rates of the effective Zeeman field  $B$ , conduction band Zeeman field  $B_{\text{C}}$ , valence band Zeeman field  $B_{\text{V}}$  of  $\text{MoTe}_2/\text{MnS}_2$  heterostructures and conduction band spin splitting  $\Delta_{\text{soc}}^{\text{C}}$ , valence band spin splitting  $\Delta_{\text{soc}}^{\text{V}}$  of monolayer  $\text{MoTe}_2$ , under applied electric fields. Upon applying the electric field, the valence band Zeeman field  $B_{\text{V}}$  exhibits a decreasing trend from  $-0.3 \text{ V \AA}^{-1}$  to  $+0.3 \text{ V \AA}^{-1}$ , while the conduction band Zeeman field  $B_{\text{C}}$  remains unchanged. The influence of the applied electric field on the spin splitting of the monolayer  $\text{MoTe}_2$  was found to be minimal. As mentioned above, as depicted in Fig. 3b, the magnetic moment of Mo also exhibited a decreasing trend with the electric field. This indicates that the change of magnetic moment primarily affects the  $B_{\text{V}}$ , which leads to a decrease in the Zeeman field  $B$  and a corresponding decrease in the valley splitting.

In Fig. 4f, we examine the effects of different strain conditions on the variation rates of the effective Zeeman field  $B$ , conduction band Zeeman field  $B_{\text{C}}$ , valence band Zeeman field  $B_{\text{V}}$  of  $\text{MoTe}_2/\text{MnS}_2$  heterostructures and conduction band spin splitting  $\Delta_{\text{soc}}^{\text{C}}$ , and valence band spin splitting  $\Delta_{\text{soc}}^{\text{V}}$  of monolayer  $\text{MoTe}_2$ . We observe that the change in  $B_{\text{V}}$  follows an increasing trend from  $-3\%$  to  $3\%$ , akin to the variation in the magnetic moment of Mo depicted in Fig. 3e. The changes of  $B_{\text{C}}$  and  $\Delta_{\text{soc}}^{\text{C}}$  show the same downward trend, which indicates that the strain leads to the decrease of spin splitting of monolayer  $\text{MoTe}_2$ , so also it leads to the decrease of conduction band splitting after the formation of heterostructure;  $\Delta_{\text{soc}}^{\text{V}}$  remains relatively constant. This suggests that  $B_{\text{V}}$  is primarily influenced by the magnetic moment, while strain affects the extent of SOC in the conduction band. Considering the opposing



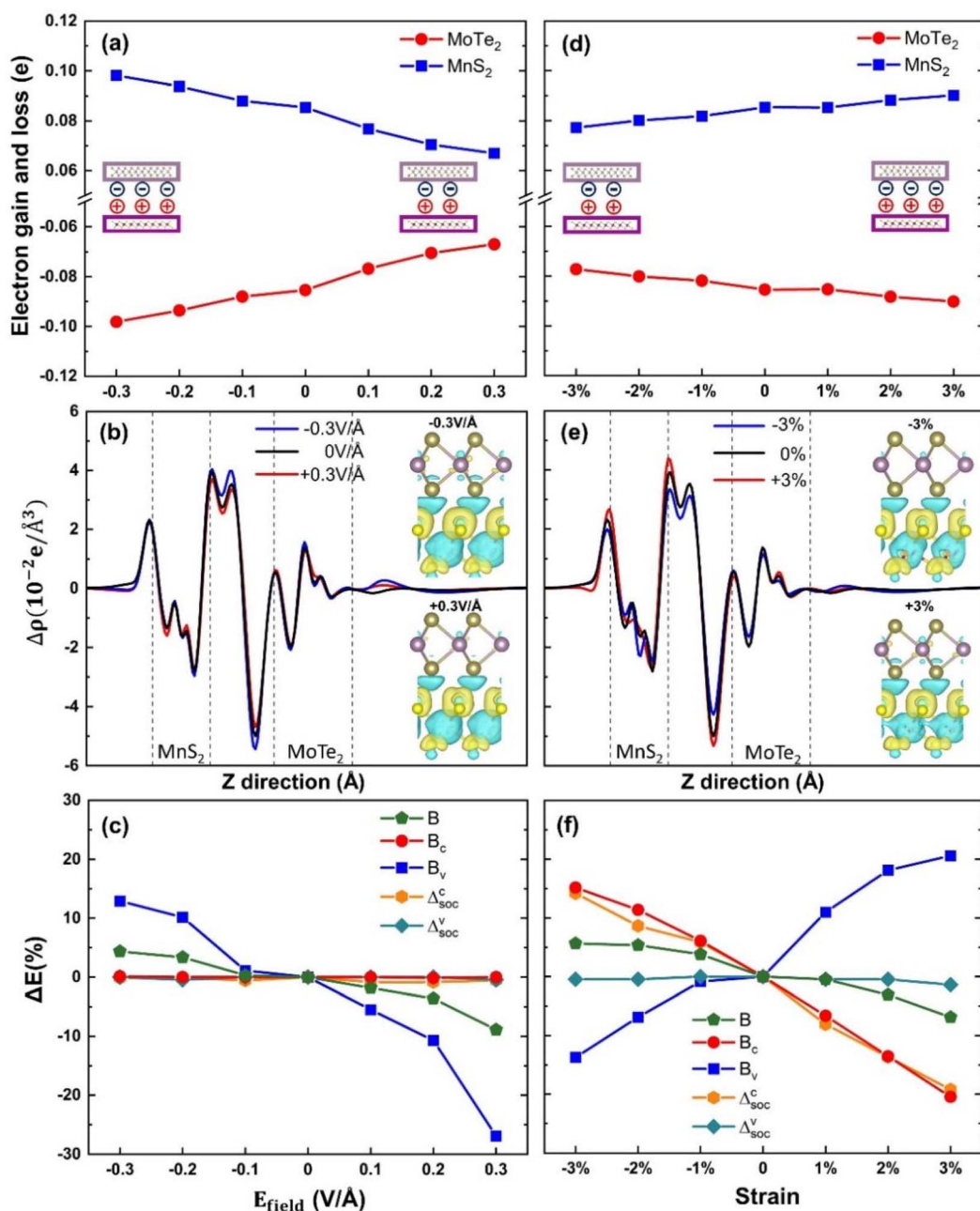


Fig. 4 (a and d) The quantity of electrons gained and lost between MoTe<sub>2</sub> and MnS<sub>2</sub>. (b and e) Planar differential charge density under different electric fields and strains; the top-right insets represent the differential charge density under the electric field of  $-0.3 \text{ V \AA}^{-1}$  and the strain of  $-3\%$ ; the bottom-right insets represent the differential charge density under the electric field of  $+0.3 \text{ V \AA}^{-1}$  and the strain of  $+3\%$ . (c and f) The effective Zeeman field  $B$ , conduction band Zeeman field  $B_C$ , valence band Zeeman field  $B_V$  of the MoTe<sub>2</sub>/MnS<sub>2</sub> heterostructure, and the conduction band spin splitting  $E_{\text{SOC}}^C$  and valence band spin splitting  $E_{\text{SOC}}^V$  induced by the SOC of monolayer MoTe<sub>2</sub>.

trends of  $B_C$  and  $B_V$ , the overall variation of the Zeeman field  $B$  demonstrates a decrease, indicating that the change in  $B_C$  is more significant than in  $B_V$ . Hence, we propose that the mechanisms underlying the influence of electric fields and strain on valley splitting are distinct. The modulation of valley splitting by the electric field is due to a direct influence on the MPE between the interfaces leading to a change in the Mo atomic magnetic moment, causing a change in the Zeeman

splitting field in the valence band. Similarly, we define strains as the strain field, which affects not only the MPE between the interfaces leading to a change in the Zeeman splitting field in the valence band, but also the spin splitting caused by the SOC of MoTe<sub>2</sub> itself, leading to a change in the Zeeman splitting field in the conduction band, and thus the magnitude of the valley splitting is modulated by the combined influence of the two factors.





## 4. Conclusions

In this study, we employed first-principles calculations to show the large valley splitting induced in monolayer MoTe<sub>2</sub> when interfaced with ferromagnetic monolayer MnS<sub>2</sub>. The results revealed a substantial intrinsic valley splitting in the MoTe<sub>2</sub>/MnS<sub>2</sub> heterostructure, reaching up to 55.3 meV, which corresponds to the magnitude of splitting induced by the external magnetic field of 476 T. Moreover, we demonstrate the tunable valley splitting through the application of electric fields and biaxial strains. Under electric field conditions, the valley splitting can be finely adjusted within the range of 49.2 to 56.6 meV, while the biaxial strains allow modulation from 50.8 to 57.4 meV. Therefore, the MoTe<sub>2</sub>/MnS<sub>2</sub> heterostructure is a potential candidate material for valley electronics with strong valley splitting properties, presenting significant potential for applications in valley electronic devices. Furthermore, the Berry curvature is also influenced by different electric fields or strains. Additionally, we observed the influence of electric fields and strains on Berry curvature, with the difference in Berry curvature decreasing under varying electric fields ( $-0.3 \text{ V } \text{\AA}^{-1}$  to  $+0.3 \text{ V } \text{\AA}^{-1}$ ) and increasing under biaxial strains ( $-3\%$  to  $3\%$ ). According to our study, we also found that the two modes of action, applied electric field and strain, have different mechanisms for regulating the valley splitting of MoTe<sub>2</sub>. The electric field affects the MPE leading to a change in the distribution of electric dipoles at the interface, which in turn affects the induced magnetic moments of the Mo atoms leading to a change in the valley splitting. Biaxial strain affects not only the MPE at the interface, but also the intrinsic spin splitting due to the SOC of the monolayer MoTe<sub>2</sub> itself, and these two factors jointly influence the change of valley splitting, even the latter being the main influence mechanism.

## Conflicts of interest

There are no conflicts to declare.

## Acknowledgements

We are grateful for the support of the National Natural Science Foundation of China (NSFC, Grant No. 51902033, 62175021), the China Postdoctoral Science Foundation (Grant No. M2020683282), the Sichuan Provincial Science and Technology Department (Grant No. 99203070) the Scientific Research Foundation of Chengdu University of Information Technology (Grant No. KYTZ202006, KYQN202312), and the College student Innovation Project (Grant No. 202210621239).

## References

- 1 M. Ezawa, *Phys. Rev. Lett.*, 2012, **109**, 5.
- 2 M. Tahir, A. Manchon, K. Sabeeh and U. Schwingenschlogl, *Appl. Phys. Lett.*, 2013, **102**, 4.
- 3 C. J. Tabert and E. J. Nicol, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 2013, **87**, 7.
- 4 W. Yao, D. Xiao and Q. Niu, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 2008, **77**, 7.
- 5 B. Van Duppen, P. Vasilopoulos and F. M. Peeters, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 2014, **90**, 10.
- 6 C. J. Tabert and E. J. Nicol, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 2014, **89**, 9.
- 7 M. Mirzaei, T. Vazifeshenas, T. Salavati-fard, M. Farmanbar and B. Tanatar, *Phys. Rev. B*, 2018, **98**, 9.
- 8 D. Oliveira, L. Villegas-Lelovsky, M. A. G. Soler and F. Y. Qu, *Phys. Rev. B*, 2018, **97**, 12.
- 9 Y. Ye, J. Xiao, H. L. Wang, Z. L. Ye, H. Y. Zhu, M. Zhao, Y. Wang, J. H. Zhao, X. B. Yin and X. Zhang, *Nat. Nanotechnol.*, 2016, **11**, 597–602.
- 10 M. Q. Sui, G. R. Chen, L. G. Ma, W. Y. Shan, D. Tian, K. Watanabe, T. Taniguchi, X. F. Jin, W. Yao, D. Xiao and Y. B. Zhang, *Nat. Phys.*, 2015, **11**, 1027–1031.
- 11 M. Kim, J. H. Choi, S. H. Lee, K. Watanabe, T. Taniguchi, S. H. Jhi and H. J. Lee, *Nat. Phys.*, 2016, **12**, 1022–1026.
- 12 N. Cortes, O. Avalos-Ovando, L. Rosales, P. A. Orellana and S. E. Ulloa, *Phys. Rev. Lett.*, 2019, **122**, 6.
- 13 K. F. Mak, K. L. He, J. Shan and T. F. Heinz, *Nat. Nanotechnol.*, 2012, **7**, 494–498.
- 14 A. Srivastava, M. Sidler, A. V. Allain, D. S. Lembke, A. Kis and A. Imamoglu, *Nat. Phys.*, 2015, **11**, 141–147.
- 15 Q. Y. Zhang, S. Y. A. Yang, W. B. Mi, Y. C. Cheng and U. Schwingenschlogl, *Adv. Mater.*, 2016, **28**, 959–966.
- 16 Y. C. Cheng, Q. Y. Zhang and U. Schwingenschlogl, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 2014, **89**, 15.
- 17 W. Hu and J. L. Yang, *Comput. Mater. Sci.*, 2016, **112**, 518–526.
- 18 R. Mas-Balleste, C. Gomez-Navarro, J. Gomez-Herrero and F. Zamora, *Nanoscale*, 2011, **3**, 20–30.
- 19 S. A. Vitale, D. Nezich, J. O. Varghese, P. Kim, N. Gedik, P. Jarillo-Herrero, D. Xiao and M. Rothschild, *Small*, 2018, **14**, 15.
- 20 D. Xiao, G. B. Liu, W. X. Feng, X. D. Xu and W. Yao, *Phys. Rev. Lett.*, 2012, **108**, 5.
- 21 L. Xu, M. Yang, L. Shen, J. Zhou, T. Zhu and Y. P. Feng, *Phys. Rev. B*, 2018, **97**, 6.
- 22 G. Aivazian, Z. R. Gong, A. M. Jones, R. L. Chu, J. Yan, D. G. Mandrus, C. W. Zhang, D. Cobden, W. Yao and X. Xu, *Nat. Phys.*, 2015, **11**, 148–152.
- 23 H. L. Zeng, J. F. Dai, W. Yao, D. Xiao and X. D. Cui, *Nat. Nanotechnol.*, 2012, **7**, 490–493.
- 24 J. Kim, X. P. Hong, C. H. Jin, S. F. Shi, C. Y. S. Chang, M. H. Chiu, L. J. Li and F. Wang, *Science*, 2014, **346**, 1205–1208.
- 25 E. J. Sie, J. McIver, Y. H. Lee, L. Fu, J. Kong and N. Gedik, *Nat. Mater.*, 2015, **14**, 290–294.
- 26 J. S. Qi, X. Li, Q. Niu and J. Feng, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 2015, **92**, 5.
- 27 C. Zhao, T. Norden, P. Y. Zhang, P. Q. Zhao, Y. C. Cheng, F. Sun, J. P. Parry, P. Taheri, J. Q. Wang, Y. H. Yang, T. Scrase, K. F. Kang, S. Yang, G. X. Miao, R. Sabirianov, G. Kioseoglou, W. Huang, A. Petrou and H. Zeng, *Nat. Nanotechnol.*, 2017, **12**, 757–762.



- 28 X. Liang, L. J. Deng, F. Huang, T. T. Tang, C. T. Wang, Y. P. Zhu, J. Qin, Y. Zhang, B. Peng and L. Bi, *Nanoscale*, 2017, **9**, 9502–9509.
- 29 T. Norden, C. Zhao, P. Y. Zhang, R. Sabirianov, A. Petrou and H. Zeng, *Nat. Commun.*, 2019, **10**, 10.
- 30 Y. Song, Q. Zhang, W. B. Mi and X. C. Wang, *Phys. Chem. Chem. Phys.*, 2016, **18**, 15039–15045.
- 31 Y. Song, X. C. Wang and W. B. Mi, *Adv. Electron. Mater.*, 2017, **3**, 7.
- 32 D. Zhong, K. L. Seyler, X. Y. Linpeng, R. Cheng, N. Sivadas, B. Huang, E. Schmidgall, T. Taniguchi, K. Watanabe, M. A. McGuire, W. Yao, D. Xiao, K. M. C. Fu and X. D. Xu, *Sci. Adv.*, 2017, **3**, 6.
- 33 F. K. Deng, J. H. Wei, Y. D. Xu, Z. Q. Lin, X. Lu, Y. J. Wan, R. Sun, C. P. Wong and Y. G. Hu, *Nano-Micro Lett.*, 2023, **15**, 106.
- 34 W. F. Cai, J. Y. Wang, Y. M. He, S. Liu, Q. H. Xiong, Z. Liu and Q. Zhang, *Nano-Micro Lett.*, 2021, **13**, 74.
- 35 K. L. Seyler, D. Zhong, B. Huang, X. Y. Linpeng, N. P. Wilson, T. Taniguchi, K. Watanabe, W. Yao, D. Xiao, M. A. McGuire, K. M. C. Fu and X. D. Xu, *Nano Lett.*, 2018, **18**, 3823–3828.
- 36 M. Kan, S. Adhikari and Q. Sun, *Phys. Chem. Chem. Phys.*, 2014, **16**, 4990–4994.
- 37 D. J. O'Hara, T. C. Zhu, A. H. Trout, A. S. Ahmed, Y. K. Luo, C. H. Lee, M. R. Brenner, S. Rajan, J. A. Gupta, D. W. McComb and R. K. Kawakami, *Nano Lett.*, 2018, **18**, 3125–3131.
- 38 X. L. Xu, Y. Pan, S. Liu, B. Han, P. F. Gu, S. H. Li, W. J. Xu, Y. X. Peng, Z. Han, J. Chen, P. Gao and Y. Ye, *Science*, 2021, **372**, 195–200.
- 39 I. G. Lezama, A. Ubaldini, M. Longobardi, E. Giannini, C. Renner, A. B. Kuzmenko and A. F. Morpurgo, *2D Mater.*, 2014, **1**, 021002.
- 40 C. Ruppert, O. B. Aslan and T. F. Heinz, *Nano Lett.*, 2014, **14**, 6231–6236.
- 41 G. Kresse and J. Furthmuller, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 1996, **54**, 11169–11186.
- 42 J. P. Perdew, K. Burke and M. Ernzerhof, *Phys. Rev. Lett.*, 1996, **77**, 3865–3868.
- 43 D. Chen, C. L. Wang, J. J. Li and F. F. Liu, *J. Magn. Magn. Mater.*, 2022, **563**, 169966.
- 44 J. T. Guan, C. X. Huang, K. M. Deng and E. J. Kan, *J. Phys. Chem. C*, 2019, **123**, 10114–10119.
- 45 L. Wang, T. Maxisch and G. Ceder, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 2006, **73**, 6.
- 46 C. Ling and F. Mizuno, *Chem. Mat.*, 2012, **24**, 3943–3951.
- 47 M. Kan, J. Zhou, Q. Sun, Y. Kawazoe and P. Jena, *J. Phys. Chem. Lett.*, 2013, **4**, 3382–3386.
- 48 S. L. Dudarev, G. A. Botton, S. Y. Savrasov, C. J. Humphreys and A. P. Sutton, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 1998, **57**, 1505–1509.
- 49 N. Marzari, A. A. Mostofi, J. R. Yates, I. Souza and D. Vanderbilt, *Rev. Mod. Phys.*, 2012, **84**, 57.
- 50 A. A. Mostofi, J. R. Yates, Y. S. Lee, I. Souza, D. Vanderbilt and N. Marzari, *Comput. Phys. Commun.*, 2008, **178**, 685–699.
- 51 H. S. Zhang, W. J. Yang, Y. H. Ning and X. H. Xu, *Phys. Rev. B*, 2020, **101**, 9.
- 52 C. M. Ke, Y. P. Wu, W. H. Yang, Z. M. Wu, C. M. Zhang, X. Li and J. Y. Kang, *Phys. Rev. B*, 2019, **100**, 6.
- 53 D. J. Thouless, M. Kohmoto, M. P. Nightingale and M. den Nijs, *Phys. Rev. Lett.*, 1982, **49**, 405–408.
- 54 Y. Yao, L. Kleinman, A. H. MacDonald, J. Sinova, T. Jungwirth, D.-S. Wang, E. Wang and Q. Niu, *Phys. Rev. Lett.*, 2004, **92**, 037204.
- 55 Z. Y. Zhang, M. S. Si, Y. H. Wang, X. P. Gao, D. Sung, S. Hong and J. He, *J. Chem. Phys.*, 2014, **140**, 174707.
- 56 C. X. Wang, B. Fu and Y. K. An, *Phys. E*, 2022, **136**, 9.
- 57 M. Abdollahi and M. B. Tagani, *J. Phys.: Condens. Matter*, 2022, **34**, 12.
- 58 G. Yang, J. Li, Z. Liu, C. C. Li and X. J. Mao, *Phys. Chem. Chem. Phys.*, 2019, **21**, 15151–15156.

