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Phase change material nanocapsules for latent function thermal fluids with tuneable thermal energy storage profiles†

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Phase change materials (PCMs) can capture and release thermal energy in the form of latent heat and PCMs as liquid dispersions are known as latent function thermal fluids. For these dispersions, the PCMs are encapsulated to warrant colloidal stability. Here, capsule formation of mini-emulsions of various methacrylates in the presence of trimethylolpropane trimethacrylate (TMA) as a crosslinker, and *n*-hexadecane (HD), *n*-octadecane (OCT), and *n*-docosane (DOC) as PCM was investigated. An ω -unsaturated poly(*n*-butyl methacrylate-*b*-[(methacrylic acid)-*co*-(methyl methacrylate)]) macromonomer was used as a reactive macromolecular emulsifier. The mini-emulsion polymerizations, capsule fabrication and performance were optimized. The resulting latent function thermal fluids and their dried equivalents were studied with differential scanning calorimetry (DSC). A challenge of these materials is matching the temperature range of the application to that of their phase change. The performance of a thermal fluid of DOC nanocapsules was tested against the base fluid water with promising results. As a tunability concept, crosslinked poly(methyl methacrylate) nanocapsules of *n*-octadecane (OCT) and *n*-docosane (DOC) were blended as a tuneable latent function thermal fluid.

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Introduction

The global climate and energy crises and the desire to reach net-zero emissions drive the importance of the capture, storage, and (re)use of energy. Phase change materials (PCMs) offer a viable option in helping to address these issues.^{1–4} PCMs rely on a phase transition, commonly a crystalline solid-to-liquid transition or *vice versa*. During the phase transition of such PCMs, external energy is captured (heating cycle) or released (cooling cycle) by the material in the form of latent heat.⁵ Materials with high latent heat suitable for temperature regulation are typically fatty acids, alkyl esters, *n*-alkanes and paraffin waxes, metals, and salt hydrates.⁶ PCMs for thermal management and storage are often stored as bulk materials in

stainless steel and polyolefin containers,⁴ or manufactured as metallic and organic composites.⁷

By segregating bulk PCMs into micron-sized or even nano-sized domains, heat transfer rates are increased, and the ease of product formulation and handling can improve.⁸ One way to do this is to fabricate core-shell capsules, the core being the PCM and the shell a mechanically robust layer. PCM capsules can be made by various methods including suspension polymerization,^{9–13} interfacial polymerization,^{14,15} *in situ* phase separation polymerization,^{16,17} solvent evaporation,^{18–20} coacervation,²¹ spray drying²² and by use of the dynamic swelling method.^{23,24}

Dried powders of encapsulated PCMs are frequently used as direct replacements for bulk materials. However, this limits their use to applications that are rigid or immobile.^{25,26} By dispersing the PCM capsules in a carrier fluid, the benefits of latent energy storage and release are now combined with the fluid's ability to flow. In addition, the specific heat capacity of the fluid itself and thermal conductivity can be optimised. This subclass of PCM materials is known as latent function thermal fluids or PCM slurries. Thermal fluids can be composed of surfactant-stabilised PCM emulsions.^{27,28} Encapsulation of the PCM in a (polymeric) shell improves stability and can potentially allow for dry powder storage and redispersion. Micro-encapsulated PCM slurries have been used in air conditioning,²⁹ solar heat collectors³⁰ and solar photo-

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† Electronic supplementary information (ESI) available: Series of recipes for *n*-hexadecane capsules made with various methacrylates, details of the reactive macromolecular emulsifier, transition onset temperatures and enthalpies for crystallisation and fusion for hexadecane (HD) containing capsules, scanning transmission microscopy data of crosslinked PMMA-OCT capsules, DSC data for *n*-hexadecane and polymer *n*-hexadecane blends, electron microscope images of poly(benzyl methacrylate)-hexadecane capsules synthesised using different amounts of trimethylolpropane trimethacrylate (TMA) crosslinking monomer, temperature specific heat capacity data. See DOI: <https://doi.org/10.1039/d4py00789a>



voltaic systems.³¹ However, the use of nano-capsule PCM fluids for these applications remains sparse. The surface area to volume ratio of encapsulated PCMs plays a crucial role in determining their thermal conductivity. For spherical capsules, the area-to-volume ratio equals $3/r$, where r is the radius of the sphere. By decreasing the size of the capsules to the nanoscale, the thermal performance of PCM fluids can be increased significantly. Moreover, miniaturizing the dimensions of the capsules brings rheological benefits when used as dispersions, with clustering and jamming of capsules less likely once colloidal stability has been optimized. Encapsulation is essential as the crystallization of dispersions of bare PCM mini-emulsion droplets at high overall volume fractions upon cooling can lead to fusion where a crystallized droplet penetrates an adjacent droplet, triggering crystal growth.

PCM nanocapsule-based fluids, therefore, have great potential. Petrovic and co-workers evaluated the performance of encapsulated *n*-octadecane aqueous dispersions for use in heat sinks.³² In microchannels of 0.3 mm in diameter, it was found that 2 and 3% v/v slurries outperformed pure water by demonstrating higher heat transfer coefficients and lower substrate temperatures. The best results were at low temperatures due to the temperature dependence of heat capacity. Rehman and co-workers used a computational model to evaluate the thermal and hydrodynamic performance of a microchannel with hydrofoil-shaped walls.³³ The PCM dispersion combined with the ribbed walls significantly outperformed pure water in smooth microchannels. However, for particles of 100 nm in diameter, the performance was reduced at solid contents higher than 10% w/w due to, as they claimed, increased turbulence. Doruk and co-workers investigated using aqueous *n*-nonadecane nanocapsule slurries in a heat exchanger.³⁴ The double pipe design had a central tube inside a larger pipe. The PCM slurry was pumped through the central tube, absorbing heat from the hot water in the outer pipe. The slurries with the lowest concentrations of PCM capsules (0.42 and 0.84% w/v) showed no improvement over water. However, a 10% increase in heat transfer coefficient was obtained when the concentration was increased to 10% w/w.

To produce PCM nanocapsules, mini-emulsion polymerization is an ideally-suited technique owing to (1) the long-term stability of the small droplets against coarsening, also known as Ostwald-ripening, and (2) the direct droplet nucleation mechanism. Nano-encapsulation by mini-emulsion encompasses multiple polymerization techniques (polycondensation,^{35,36} sol-gel,^{37,38} phase-inversion,³⁹ etc.) and core materials.^{40–44}

The fundamentals of the encapsulation process have been studied throughout the last few decades, elucidating the interplay of thermodynamic and kinetic forces to achieve complete encapsulation. Due to the classical use of *n*-hexadecane (HD) as an agent to resist emulsion droplet coarsening (Ostwald ripening),^{45,46} much of the mini-emulsion research employs HD or other long-chain *n*-alkanes as model compounds for encapsulation. One of the early studies on encapsulation of HD by mini-emulsion polymerisation was carried out by

Landfester and co-workers in 2001.⁴⁷ They studied the effect of monomer type, monomer : HD ratio and amount of surfactant on the morphology of the nanocapsules/particles. The authors demonstrated that the difference in hydrophilicity between the core HD material and polymer shell drove nanocapsule formation. Capsule morphology predictions were also made by Mahdavian and co-workers, who assessed the impact of shell polarity.⁴⁸ In mini-emulsions which contain HD as the core material, methyl methacrylate (MMA) was copolymerised with 2-ethylhexyl acrylate (EHA) or methacrylic acid (MA). The phase-separated morphologies were compared by electron microscopy and DSC against configurations predicted by Torza and Mason's thermodynamic theory, and overall, good agreement was found.⁴⁹

Thermodynamic factors influencing the formation of polystyrene-paraffin capsules were researched by Lou and Zhou.⁵⁰ The authors investigated the thermodynamic effect of increasing the SDS concentration and observed a shift from capsules to bowl-shaped particles. This aligns with the spreading coefficient, where lowering only the polymer-aqueous and HD-aqueous interfacial tensions shifts the predicted equilibrium morphology from capsules to partial encapsulation and eventually non-engulfment. Similar to the research by Mahdavian, the authors adjusted the shell polarity by copolymerising 1–3% w/w of MAA with styrene. Yet, adding a hydrophilic monomer disfavors capsule formation based on Torza and Mason's spreading coefficient equations. Given that they report capsule formation, it is more likely a kinetic factor in which the ionised MAA restricts polymerisation to the interface.

This kinetic factor was investigated by Klumperman and co-workers who demonstrated that capsule formation could be driven by the choice of initiator.⁵¹ Initiating the mini-emulsion polymerisation of *n*-butyl acrylate (BA) and HD with AIBN resulted in solid particles (total dissociation) as predicted thermodynamically. However, when water-soluble anionic initiators or oil-soluble redox initiators were used, capsules were synthesised. Using an anionic initiator, such as potassium persulfate, may influence capsule morphology thermodynamically by forming amphiphilic oligomers. However, this is not true for the cumyl hydroperoxide redox initiator, whose influence on particle morphology is purely kinetic. This result highlighted that capsule formation by mini-emulsion polymerisation can be directed by fixing the locus of polymerisation to the interface.

It is feasible that these findings inspired the development of interface-confined reversible-deactivation radical mini-emulsion polymerisation. In this sub-category, amphiphilic RAFT or ATRP agents reside at the droplets' surface and restrict polymerisation to the interface, controllably encapsulating the core material.^{52–58} It has been shown by Lou and Hawke that the choice of stabiliser block length is crucial to ensure a high percentage of capsules are synthesised.^{53,59} If the stabiliser is too water-soluble, desorption can occur, triggering secondary nucleation. With the ability to tailor the stabiliser's surface activity, Lou and Chen synthesised HD capsules with cross-



linked fluorinated shells.⁵⁶ This was only made possible using an amphiphilic poly(dodecafluoroheptyl acrylate-*co*-methacrylic acid) RAFT agent.

We decided to use ω -unsaturated methacrylate-based macromonomers as a reactive macromolecular stabilizer, as not only will these provide superior colloidal stability through grafting but also have the potential to graft more exotic core materials and polymer shells in the future.⁶⁰ Polymeric stabilisers also benefit from favouring the engulfment morphology thermodynamically. They are able to provide considerable colloidal stability without drastically lowering the interfacial tensions between the aqueous phase and the polymer or core. Inversely, low molecular weight anionic surfactants such as SDS favour non-engulfment at high concentrations.^{61–63}

The use of crosslinking monomers can have a substantial effect on capsule formation. Crosslinking reduces the mobility of chains, allowing for the access of non-equilibrium morphologies. Though it has been proven for styrene-divinyl benzene shells in particular, high amounts of the crosslinker lead to porous shells. The effect of divinyl benzene (DVB) on the morphology of alkane capsules was studied by Landfester and co-workers.⁶⁴ Using polymerizable surfactants in various amounts, they found that when using styrene to encapsulate HD, there was a 50% split of capsules and particles. Swapping styrene entirely for DVB produced a much higher percentage of capsules. Research by Li and co-workers synthesised isooctane capsules by balancing the styrene:DVB and core:shell ratios.⁶⁵ In accordance with the thermodynamic theory developed by Sundberg,⁶⁶ the most thermodynamically favourable morphology depends on the surface area of the phases, as well as the interfacial tensions. Capsules with styrene-DVB shells, containing 30% mol/mol DVB, were synthesised by increasing the mass fraction of isooctane to monomer. The authors also studied the effect of DVB concentration, claiming from TEM analysis that the capsule shells become porous when >70% mol/mol DVB was used. The speculation of shell porosity was confirmed by work from Yingwu and co-workers as they attempted to synthesize non-collapsible hollow capsules.⁵⁷ The authors measured the porosity of polystyrene hollow capsules crosslinked with 60% mol/mol DVB by nitrogen adsorption and desorption and found them exceedingly porous. The 110 nm diameter capsules, with a shell thickness of 11 nm, had a substantial pore volume of 2.74 mL g⁻¹ and an approximate pore diameter of 9 nm.

As an aqueous capsule dispersion, the presence of pores is less of an issue due to capillary forces, preventing leakage of the hydrophobic core into the aqueous phase. However, if the capsules were used as dried PCMs and stored as a powder, the release of the core material, especially if it is volatile, is likely to occur.

In characterising PCM capsules, dynamic scanning calorimetry (DSC) is commonly used to inspect and compare the thermal properties of the materials with a particular focus on latent heat. To do so, the enthalpies of fusion (ΔH_f) and crystallisation (ΔH_c) are measured during temperature ramps. Due to the additional mass of the shell material, the ΔH_f of the PCM capsules will generally be lower than the bulk material. The ratio-percentage of capsule enthalpy of fusion ($\Delta H_{f,cap}$)

compared to the bulk value ($\Delta H_{f,bulk}$) is often presented as eqn (1):

$$\text{Capsule } \Delta H_f \text{ ratio} = \frac{\Delta H_{f,caps}}{\Delta H_{f,bulk}} \times 100\% \quad (1)$$

This, however, is of little use without knowing the mass fraction of PCM core to the overall capsule mass shell material, w , as shown in eqn (2) where M_{core} and M_{shell} are the masses of the PCM core and shell monomer and p_M is monomer conversion:

$$\text{Core mass fraction } (\phi_{core}) = \frac{M_{core}}{M_{core} + M_{mon} p_M} \quad (2)$$

Its percentage value we can also refer to as 'PCM loading'. By combining eqn (1) and (2), a measure of the percentage latent heat of fusion of the PCM capsules with respect to the theoretical maximum based on PCM loading and referred to as the thermal storage efficiency (TSE) then becomes:⁸

$$\text{TSE} = \frac{\Delta H_{f,caps}}{\phi_{core} \times \Delta H_{f,bulk}} \times 100\% \quad (3)$$

However, as Okubo and co-workers have pointed out,⁶⁷ the equation is not always used correctly. Efficiency implies that if the value is lower than 100%, not all the PCM was encapsulated. Yet, even if all PCM were encapsulated, if a portion of it did not crystallise on cooling, a lower-than-expected $\Delta H_{f,cap}$ would be recorded. This partial crystallisation is likely, as studies by NMR and neutron scanning have revealed that molecules near the wall of a confined geometry behave differently than their corresponding bulk counterparts.^{68,69} Furthermore, Amanuel and co-workers have proposed a method to estimate the thickness of non-freezing organic solvents in silica nanopores.^{70,71} The use of eqn (1) to measure efficiency also assumes that the latent heat of the confined material is equal to its bulk value. This is a poor assumption, as ΔH_f has been shown to decrease with confinement diameter at very small radii.^{72,73} However, the relationship between ΔH_f and geometry radii is not yet fully understood, with a conflicting relationship determined by Dorner.⁷⁴

Table 1 shows a selection of literature data for PCM nanocapsules synthesised by mini-emulsion polymerization. Due to the variance of published latent heat equations, data was extracted from the publications and used to recalculate the TSE using eqn (3).

Regarding the top three entries in Table 1, Mahdavian and co-workers studied the nanoencapsulation of HD in PMMA shells.⁷⁵ They demonstrated that although increasing the core:shell ratio did lead to an increase in the enthalpy of fusion of the capsules, this was not reflected in the thermal storage efficiency (TSE). Another study by Mahdavian and co-workers investigated the influence of comonomer polarity and is reported in the second set of entries in Table 1.⁴⁸ Adding 15% w/w of hydrophobic or hydrophilic comonomers increased the efficiency marginally, however adding more caused a significant decrease. This drop is caused by the thermodynamically



Table 1 Comparison of the reported latent heat ($\Delta H_{f,caps}$) and thermal storage efficiency (TSE) recalculated using eqn (1) and published data

Shell material	PCM	$w^a/wt\%$	$\Delta H_{f,caps}/$ kJ kg^{-1}	TSE/%	Ref.
PMMA	HD	28.9	74.0	108.9	75
PMMA	HD	51.3	75.3	62.5	75
PMMA	HD	77.5	96.8	53.1	75
PMMA	HD	50.4	72.9	61.5	48
P(MMA + 15% EHA)	HD	51.3	79.9	66.3	48
P(MMA + 20% EHA)	HD	51.1	40.2	33.5	48
P(MMA + 30% EHA)	HD	50.9	18.4	15.4	48
P(MMA + 15% MAA)	HD	50.7	77.8	65.4	48
P(MMA + 20% MAA)	HD	51.2	48.2	40.0	48
PMMA	OCT	86.7	208.7	101.5	76
PEMA	OCT	88.9	198.5	94.2	76
P(MMA + 2% ODMA)	OCT	28 ^b	102.0	154.9	77
P(MMA + 20% ODMA)	OCT	30 ^b	85.0	119.2	77
P(MMA + 40% ODMA)	OCT	31 ^b	84.0	115.0	77

^a Calculated using monomer conversion. ^b Monomer conversion not available. Shell materials methyl methacrylate (MMA), 2-ethylhexyl acrylate (EHA), methacrylic acid (MAA), ethyl methacrylate (EMA) and octadecyl methacrylate (ODMA). Values $\Delta H_{f,HD}$ and $\Delta H_{f,OCT}$ were 235 and 237 kJ kg^{-1} .

favoured particle morphology shifting from encapsulated to partially encapsulated due to changes in interfacial tensions. Zhao and co-workers used a high core/shell weight ratio of 80/20 to encapsulate *n*-octadecane in poly(methyl methacrylate) and poly(ethyl methacrylate) shells.⁷⁶ The authors reported TSE levels close to unity. However, it is difficult to confirm the morphology from the SEM images provided. The final three entries of Table 1 by Tang and co-workers highlight the importance of reporting monomer conversion when calculating TSE values.⁷⁷ Clearly, there cannot be more PCM in the system than added, and the only answer is that there is less shell material than expected.

The concept of this paper is to design a tuneable latent function thermal fluid by mixing dispersions of polymer nanocapsules, each loaded with a bespoke *n*-alkane PCM. We will show that our prototype water-based thermal fluid with multiple latent heat transitions has potential. The capsules are made by mini-emulsion radical polymerization. The effects of crosslinker and shell materials on shell morphology and PCM performance are investigated. As mentioned earlier, ω -unsaturated methacrylate-based macromonomers will be used as a reactive macromolecular stabilizer.⁶⁰ The covalent attachment of the emulsifiers to the particles ensures robust colloidal stability in the end application and aids capsule formation during polymerization.

Experimental

Materials

The monomers benzyl methacrylate (BzMA, 96%), *n*-butyl methacrylate (*n*BMA, $\geq 99\%$), isobornyl methacrylate (IBMA,

technical grade), trimethylolpropane trimethacrylate (TMA, technical grade) and methyl methacrylate (MMA, 99%) were purchased from Sigma-Aldrich and filtered through basic activated alumina to remove radical inhibitors before use. Methacrylic acid (MAA, 99%, Sigma-Aldrich) was filtered through a column of neutral activated alumina. *n*-Hexadecane (HD, $\geq 99\%$) was purchased from Alfa Aesar. Ammonia solution (aqueous, 35% w/w) and sodium hydroxide (NaOH) were purchased from Fisher Scientific. Ammonium persulphate (APS, $\geq 98\%$), azobisisobutyronitrile (AIBN), *n*-docosane (DOC, 99%), *n*-octadecane (OCT, 99%), potassium persulfate ($\geq 99\%$) and sodium dodecyl sulfate (SDS, $\geq 98.5\%$) were purchased from Sigma-Aldrich. AIBN was recrystallized from methanol and stored at $-18\text{ }^\circ\text{C}$ prior to use. Bis[(difluoroboryl)diethylglyoximate]cobalt(II) (CoEtBF) was synthesized using an analogous procedure as described for CoBF in the literature.⁷⁸

Methods

Synthesis of poly(*n*-butyl methacrylate-*b*-[methyl methacrylate-*co*-methacrylic acid]) macromonomer. Block copolymer macromonomer (MM) aqueous dispersions synthesis was adapted from work by Krstina *et al.*,⁷⁹ Moad *et al.*,⁸⁰ and Suddaby *et al.*⁸¹ To a jacketed 1 L reactor, water (519.95 g), sodium dodecyl sulfate (1.2 g, 4.16 mmol) and 4,4'-azobis(4-cyanovaleric acid) (2.0 g, 7.12 mmol) were added and purged with nitrogen for 1 hour with stirring at 300 rpm. In two separate vials, the cobalt(II)-porphyrin catalyst, CoEtBF (4.639 mg, 1.04×10^{-5} mol) and a mixture of methyl methacrylate (52.64 g, 56.0 mL, 0.526 mol) and methacrylic acid (24.48 g, 24.0 mL, 0.2844 mol) were prepared. Both were purged with nitrogen for 1 hour. The monomer mixture was added to the vial containing CoEtBF and the mixture stirred vigorously until CoEtBF dissolved. The reactor was heated to $72\text{ }^\circ\text{C}$ and on reaching the target temperature, 16 mL of the CoEtBF monomer mixture was added as a single dose and 64 mL of the mixture was then added at a rate of $0.6667\text{ mL min}^{-1}$. After 1 hour the temperature was raised to $85\text{ }^\circ\text{C}$. After two hours total reaction time, the latex was removed from the reactor, cooled and quenched with bubbling of air. Solid content 12.5%, DLS: Z-average diameter = $217.6 \pm 1.5\text{ nm}$, PDI = 0.189 ± 0.01 . GPC (THF): $M_n = 2800$, $M_w = 5900$, $D = 2.03$. $^1\text{H NMR}$ (400 MHz, DMSO- d_6) δ : 12.39 (br, 1H), 6.11 (m, 1H), 5.58 (m, 1H), 3.54 (s, 3H), 3.35 (br, 3H), 2.45–2.26 (m, 2H), 2.15–1.29 (m, 2H, m, 1H), 1.20–0.38 (m, 3H). DP_n ($^1\text{H NMR}$) = 31.

120 g of the above synthesised P(MAA-*co*-MMA) macromonomer latex (12.5% w/w, MM 15 g, 5.21 mmol) was added to a jacketed 250 mL reactor. Deionised water (30.0 g) was added to reduce the solid content to 10% w/w. The reactor was purged with nitrogen for 30 minutes with stirring at 250 rpm. *n*-Butyl methacrylate (11.21 g, 12.54 mL, 78.83 mmol) and an aqueous potassium persulfate solution (70.2 mg, 0.26 mmol, in 12.54 mL) were purged with nitrogen for 30 minutes. On heating the reactor to $85\text{ }^\circ\text{C}$, the *n*-butyl methacrylate and potassium persulfate solution were both fed into the reactor at a rate of 6.27 mL h^{-1} . Feeding monomer ensures starved conditions, that is a high instantaneous conversion and thus low



monomer concentration in the particles, essential for control of propagation to form the BMA block. After 2 hours, the pumps were stopped and the reactor temperature maintained for a further 1 hour. The latex was then removed from the reactor, cooled and quenched with bubbling of air. Solid content 16.0%, DLS: Z-average diameter 218.8 ± 3.1 nm, PDI 0.123 ± 0.004 . GPC (THF): $M_n = 5700$, $M_w = 8000$, $D = 1.41$. ^1H NMR (400 MHz, 2 : 1 CDCl_3 : DMSO-d_6) δ : 6.01 (m, 1H), 5.41 (m, 1H), 3.84 (br, 2H), 3.50 (s, 3H), 2.44 (m, 2H), 2.08–1.24 (m, 6H, m 1H), 1.16–0.42 (m, 6H). DP_n (^1H NMR) = 43.

Typical formation of P(BMA-*b*-[MAA-*co*-MMA]) micelle dispersion. Ammonium hydroxide (35% w/w, 1.12 g, 65.6 mmol) was added to a latex of P(BMA-*b*-[MAA-*co*-MMA]) block copolymer particles (15% w/w, 100.0 g, 5.0 mmol) and was diluted to 10% w/w with water (80.0 g). The mixture heated at 85 °C for 30 minutes. After heating the mixture was cooled to room temperature in an ice bath and stored at 5 °C.

Typical synthesis of crosslinked poly(benzyl methacrylate) hexadecane capsules, varying type of methacrylate monomer, by mini-emulsion polymerisation. An aqueous dispersion of P(BMA-*b*-[MAA-*co*-MMA]) macromonomer micelles (10.8% w/w, 1.8553 g, 4.23×10^{-5} mol) was added to water (30.34 g) and the pH adjusted to 8.8 with NaOH solution.⁶⁰ To this dispersion, a mixture of methyl methacrylate (3.490 g, 34.86 mmol), trimethylolpropane trimethacrylate (1.310 g, 3.87 mmol, 10% mol/mol with respect to total monomer), hexadecane (3.2 g, 14.13 mmol) and azobisisobutyronitrile (0.010 g, 6.09×10^{-5} mol) was added and stirred for 30 minutes with a magnetic stirrer. The mixture was emulsified with a IKA ULTRA-TURRAX rotor-stator homogeniser for 120 seconds at 19 000 rpm. The coarse emulsion was then emulsified further using a Branson 250 Digital Sonifier for 15 minutes with pulses of 10 seconds at 60% strength, during which the mixture was cooled in a water bath regulated to 20 °C. The mini-emulsion was transferred to a round-bottom flask and purged with nitrogen gas for 30 min. The mini-emulsion was heated for 3 h at 70 °C under a positive pressure of nitrogen, with stirring at 350 rpm. Batch mini-emulsion polymerizations of methacrylate monomers under similar conditions take approximately 1 h. We ran for 3 hours as the presence of alkanes and crosslinks lowers the effective monomer concentration at the polymerization sites in each particles. 3 h was sufficiently long to reach near complete monomer conversion. Polymerization at 70 °C with AIBN means that throughout the reaction a steady flux of radicals is produced as $t_{1/2} = 6$ h.

Synthesis of crosslinked poly(methyl methacrylate) *n*-octadecane/*n*-docosane capsules by mini-emulsion polymerisation. A mixture of *n*-docosane or *n*-octadecane (3.2 g), methyl methacrylate (3.490 g, 34.86 mmol), trimethylolpropane trimethacrylate (1.310 g, 3.87 mmol, 10% mol/mol with respect to total monomer) was prepared and held at 50 °C (DOC) or 35 °C (OCT) to prevent crystallisation. Separately, an aqueous dispersion of P(BMA-*b*-[MAA-*co*-MMA]) macromonomer micelles (10.8% w/w, 1.8553 g, 4.23×10^{-5} mol) was added to water (30.34 g) and the pH adjusted to 8.8 with NaOH solution. An aqueous stock solution of ammonium persulphate (APS)

(0.01 g mL⁻¹, 43.8 mM) was also prepared. The macromonomer dispersion was heated to 50 °C (DOC) or 35 °C (OCT) and added dropwise into the hot wax/monomer mixture with stirring. The two-phase mixture was then emulsified with an IKA ULTRA-TURRAX rotor-stator homogeniser for 120 seconds at 19 000 rpm at 50 °C. The coarse emulsion was then emulsified further using a Branson 250 Digital Sonifier for 15 minutes with pulses of 10 seconds at 60% strength, during which the mixture temperature was regulated at 50 °C (DOC) or 35 °C (OCT). The mini-emulsion was transferred to a round-bottom flask. The RBF and APS solutions were purged with nitrogen gas for 30 min at room temperature. After purging, the mini-emulsion was heated at 70 °C for 10 minutes, whilst stirring at 350 rpm, after which 1 mL of the APS stock was added. The reaction was run for 3 h at 70 °C under a positive pressure of nitrogen, with stirring at 350 rpm.

Characterisation

Differential scanning calorimetry. The thermophysical properties of polymers and phase change materials were measured using a TA Instruments DSC 2500. To measure the glass transition temperatures, approximately 10 mg of the sample was weighed into a 40 μL aluminium pan fitted with a pierced lid. The analyses were conducted under an atmosphere of nitrogen gas with a cooling/heating rate of 10 °C min⁻¹. Polymer glass transition temperatures (T_g) were calculated at the midpoint of the transition following ASTM D3418-21 standards.⁸² To measure the phase change material transitions, approximately 10 mg of sample was weighed into a 40 μL aluminium hermetically sealed pan. The analyses were conducted under an atmosphere of nitrogen gas with a cooling/heating rate of 10 or 1 °C min⁻¹. Enthalpies of fusion and crystallisation were calculated using TA Instruments Trios software.

Dynamic light scattering. Particle size measurements were performed on a Malvern Zetasizer Ultra or Anton Paar Litesizer 500. The Zetasizer Ultra used a laser operating at 633 nm wavelength in the power range of 4–10 mW with a scattering angle of 173°. The Litesizer 500 used a laser operating at 658 nm wavelength, with power of 40 mW and a scattering angle of 175°. All measurements were conducted at 25 °C in filtered deionised water, three replicates were conducted for each sample. Time correlation functions were analysed with the cumulants method.

Size exclusion chromatography (THF). Polymer molecular weight analyses were conducted using an Agilent Infinity II MDS instrumentation with differential refractive index, viscometry, dual-angle light scatter, and multiple wavelength UV detectors. The system had 2 \times PLgel Mixed C columns (300 \times 7.5 mm) and a PLgel 5 μm guard column. THF with 0.01% butylated hydroxytoluene additive was used as the eluent. Samples were run at 1 mL min⁻¹ at 30 °C. PMMA and PS standards (Agilent EasyVials) were used for calibration. Analyte samples were filtered through a GVHP membrane with 0.22 μm pore size before injection. Experimental molar mass (M_n) and dispersity (D) values of synthesised polymers were determined by conventional calibration against PMMA stan-



dards using Agilent GPC software. The Mark–Houwink–Kuhn–Sakurada (MHKS) parameters pairs used for various polymers against PMMA calibration were as follows; for PBzMA, PMMA calibration $K = 12.8 \times 10^{-3} \text{ mL g}^{-1}$, $\alpha = 0.690$ and sample $K = 3.32 \times 10^{-3} \text{ mL g}^{-1}$, $\alpha = 0.701$; for P*n*BMA, PMMA calibration $K = 12.8 \times 10^{-3} \text{ mL g}^{-1}$, $\alpha = 0.690$ and sample $K = 16.2 \times 10^{-3} \text{ mL g}^{-1}$, $\alpha = 0.656$; for PIBMA PMMA calibration $K = 7.56 \times 10^{-3} \text{ mL g}^{-1}$, $\alpha = 0.731$ and sample $K = 3.80 \times 10^{-3} \text{ mL g}^{-1}$, $\alpha = 0.748$.^{83–85}

Light microscopy. Sample images were taken undiluted on an Olympus IX73 light microscope in dark-field mode. A magnification of 60 \times (Olympus LUCPlanFLN 60 \times Ph) was used. Images were captured on an Andor Zyla sCMOS camera and processed in ImageJ.

Scanning electron microscopy. Samples were imaged on a ZEISS Gemini SEM Field Emission Scanning Electron Microscope. They were imaged at an accelerating voltage of 0.2 kV and a working distance of 2.0 mm. Samples were prepared by drop casting dilute latexes, typically at 1–5% w/w onto silicon wafers and leaving them to dry by natural ventilation whilst protected from dust overnight.

Transmission electron microscopy. Samples were imaged on a ZEISS Gemini SEM Field Emission Scanning Electron Microscope using a detector positioned beneath the sample, in line with the electron beam. Samples were diluted to 5% w/w solid content. A 5 μL drop of the latex was placed onto a copper 200 mesh TEM grid with carbon film. The droplet was allowed to dry for 15 minutes at room temperature before the excess was blotted with filter paper. The grids were allowed to dry fully overnight through natural ventilation at room temperature.

Thermogravimetric analysis. Hexadecane evaporation rates were measured using a TGA/DSC 3+. Capsule latexes were added to pre-weighed 40 μL aluminium pans, and water evaporated at room temperature. The pans were sealed with a pierced aluminium lid and re-weighed before measurement. Measurements were conducted under an atmosphere of nitrogen gas.

Results & discussion

A series of ω -unsaturated amphiphilic macromonomers, poly(*n*-butyl methacrylate-*b*-[methacrylic acid-*co*-methyl methacrylate]) P(BMA-*b*-[MAA-*co*-MMA]), were synthesised by catalytic chain transfer emulsion polymerisation (CCTEP) and subsequent seeded sulfur-free RAFT emulsion polymerisation.⁶⁰

An initial series of mini-emulsion polymerisations was carried out at 20 wt% solids content, the dispersed phase being half (wt%) hexadecane and half monomer (benzyl methacrylate and trimethylolpropane trimethacrylate (TMA) as crosslinker) and using 2.5 wt% macromonomer stabiliser with respect to the dispersed phase. The reaction without the crosslinker formed, as expected, bowl-shaped particles. The introduction of crosslinker (10–30 wt% of total monomer) resulted in capsule formation. An amount of 20 wt% TMA (mole frac-

tion of 0.115) was seen as a good compromise between the mechanical strength of the capsules and the inner surface roughness of the capsule walls.

Choice of methacrylate shell monomer

An important question is the effect different shell materials have on the morphology and thermal properties of the PCM capsules. A wide range of methacrylate monomers are available. Methyl (MMA), benzyl (BzMA), *n*-butyl (*n*BMA) and isobornyl (IBMA) methacrylate were selected as they display a range of thermophysical properties and hydrophobicities (Table 2).

Mini-emulsions of HD, TMA (approximately 20% w/w to monomer) and each methacrylate monomer were prepared using a sonicator probe. The mass ratio of HD to monomer was fixed at 2 : 3 (see Table S1† for all experimental quantities). The mini-emulsions were stabilised by P(BMA-*b*-[MAA-*co*-MMA]) macromonomers (Table S2†), using 2.5 wt% with respect to the dispersed phase. An oil-soluble initiator, AIBN (1.25 g L⁻¹ in the dispersed phase), was used to discourage secondary nucleation and added to the HD monomer mixture before emulsification.

The size distributions of mini-emulsion droplets before polymerization and the corresponding latex particles were measured by DLS (Table 3 and Fig. 1).

Consistency in size distributions from droplets to particles indicated that stable mini-emulsions were formed in all cases and that particle formation and growth occurred predominantly by droplet nucleation. There is a sizeable difference of 9.5% and 8.8% between the average droplet and particle diameters of IBMA to the other three monomers. As IBMA has a much lower water solubility (Table 2), and therefore is more hydrophobic, the larger droplet and particles may be a result of P(BMA-*b*-[MAA-*co*-MMA]) stabiliser incompatibility. Although not explored in this work, the versatility of the macromonomer stabilisers allows the user to tune the hydrophobicity of the blocks to suit the intended application best.

To investigate the morphologies of the methacrylate series, the latexes were imaged by SEM and STEM, as shown in Fig. 2. For all samples in this paper, transmission electron micrographs were obtained using the ZEISS Gemini Field Emission Scanning Electron Microscope in TEM mode. This was chosen as the electron beam (15–20 kV) is much lower than conven-

Table 2 Monomer and polymer literature characteristic of methacrylate monomers

	Water solubility ^a /g L ⁻¹	$T_{g,\infty}$ ^b /°C
Methyl methacrylate	15.70	105
Benzyl methacrylate	0.19	54
<i>n</i> -Butyl methacrylate	0.20	20
Isobornyl methacrylate	5.44×10^{-3}	110

^a Literature data measured at 20 °C. MMA from Handbook of Aqueous Solubility Data⁸⁶ and others supplied by Evonik GPS Safety Summaries. ^b Glass transition temperatures obtained from the Polymer Handbook.⁸⁷



Table 3 Droplet and particle size characteristics for hexadecane capsules and particle surface area per macromonomer (a_{surf})

Reaction	Z-Avg. droplet diameter/nm	Droplet PDI	Z-Avg. capsule diameter/nm	Capsule PDI
PMMA_HD ^a	150.2 ± 2.3	14.27 ± 1.20%	158.1 ± 3.4	6.52 ± 5.96%
PBzMA_HD ^a	152.2 ± 2.5	14.52 ± 0.21%	155.4 ± 2.38	9.87 ± 5.70%
PnBMA_HD ^b	160.2 ± 0.1	0.130 ± 0.018	161.2 ± 1.4	0.055 ± 0.030
PIBMA_HD ^b	174.1 ± 1.0	0.080 ± 0.027	176.8 ± 0.8	0.098 ± 0.016

^a Droplet and capsule size were recorded on a Malvern Zetasizer Ultra at 25 °C and scattering angle of 173°. ^b Droplet and capsule size were recorded on an Anton Paar Litesizer Litesizer 500 25 °C and scattering angle of 175°. For the Z-average diameter and PDI results, three DLS scans were recorded and an average taken for each sample.

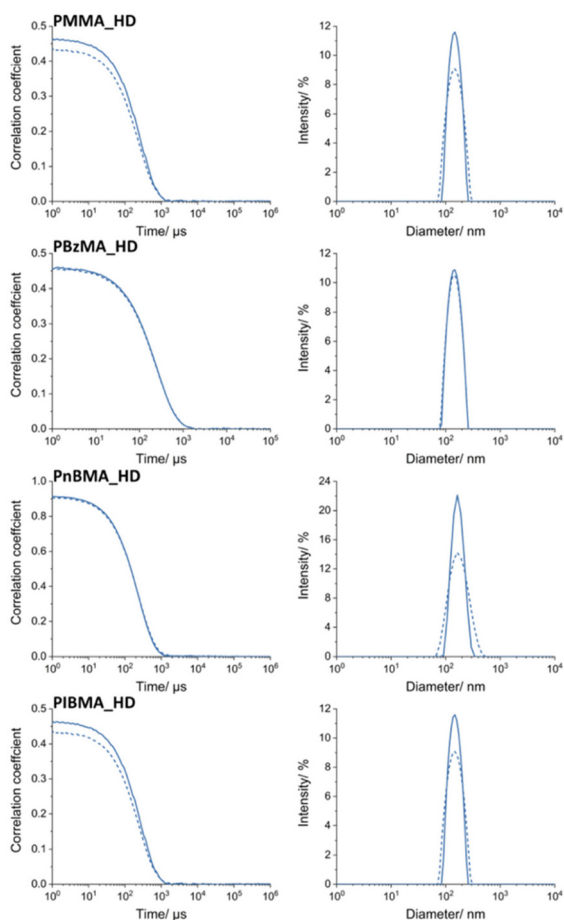


Fig. 1 Size analysis by DLS. Correlograms (left) and intensity weighted particle size distributions (right) for hexadecane crosslinked capsules made with four methacrylate monomers. Mini-emulsion droplets are dashed lines, post-polymerization capsules are represented by solid lines.

tional TEM (~200 kV), and this reduces the degradation of soft polymer samples.⁸⁸ However, even with this precaution, imaging the capsules proved difficult, especially at high magnification. When focusing on samples for more than a few seconds, the capsules visibly deformed, comparable to melting. This effect is illustrated for crosslinked PMMA octadecane capsules in the ESI (Fig. S1†).

The SEM images of reaction PBzMA_HD show a mixture of spheres and erupted spheres, whereas crumpled spheres are

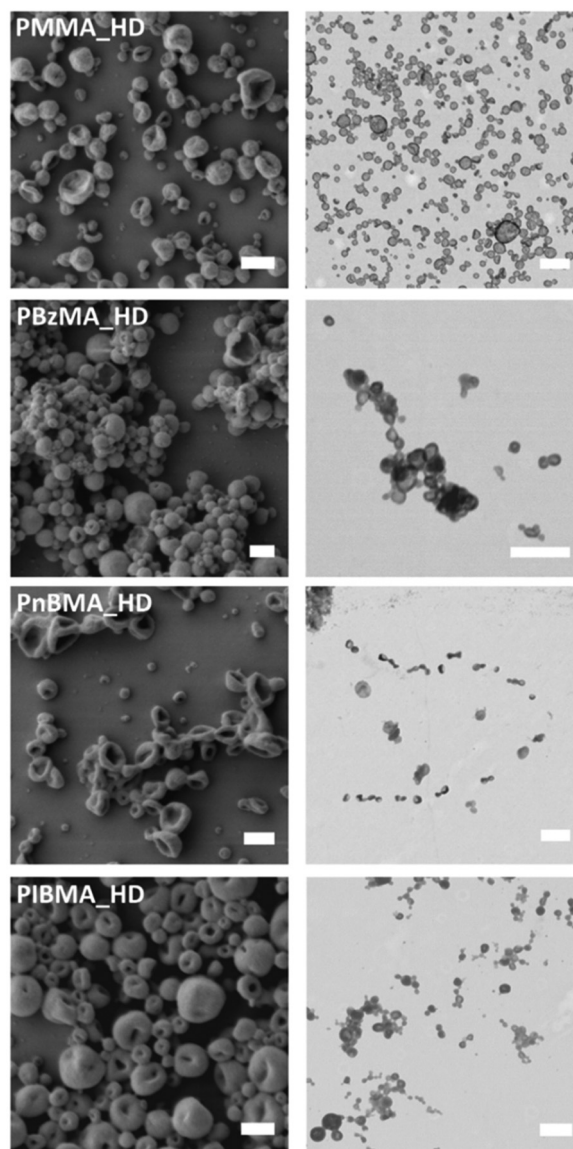


Fig. 2 Electron microscope images of hexadecane crosslinked capsules synthesised using different methacrylate monomers. Images from SEM (left) and STEM (right). SEM scale bars are 200 nm, TEM scale bars are 500 nm.

present in PMMA_HD, PnBMA_HD and PIBMA_HD reactions. All structures are a result of hexadecane evaporation and give an indication for capsule formation. The STEM images give



more substantial evidence for encapsulation, showing a contrast difference across the hollow capsules compared to the few solid particles present. These solid particles may be formed through limited particle nucleation by other means than the intended droplet nucleation, most likely homogeneous nucleation. Comparing the grey value profile across a capsule and particle (Fig. 3) highlights the different morphologies, the y-axis has been inverted to aid with visualisation. In Fig. 3, the grey value is a measure of how light/dark each pixel is, with absolute black being 0 and absolute white being 255. As the profile runs across the capsule and particle, the pixels become darker as the polymer wall scatters the electron beam. For the particle, there is a consistently dark pixel profile across the particle and pixels are darker, as indicated by a lower grey value. In contrast, as the centre of the hollow capsule is thinner, the grey value tends towards a lighter shade because more electrons reach the STEM detector.

With capsule formation confirmed by electron microscopy, the thermal properties of the capsules were studied using DSC. The latexes were dried at ambient conditions to remove water before analysis. For each dry powder sample, 3 cool and heating scans between -15 and 25 °C were conducted at a rate of 1 °C min^{-1} . A low rate of temperature change was chosen to resolve multiple crystalline phase transitions.

There is a reduction of the crystallisation and melting temperatures in all cases, caused by confinement of the HD. There are three matters to discuss for the crystallisation of HD in each sample: (i) the shape of the exotherms and multiple peaks, (ii) the large differences of supercooling (ΔT_c) and (iii) the small exothermic peak at 9.8 °C.

(i) Due to the molecular structure of linear *n*-alkanes, when cooled below the melting point, the molecules can undergo multiple transitions before reaching their most stable crystal structure.^{89–93} These metastable/transient phases are known as rotator phases, named so because the molecules stack in lamella crystals and have almost free rotation around their axis.^{94–96} There are five known rotator phases⁹⁷ and for even *n*-alkanes (C12 to C26) in bulk, the generally reported rotator phase is hexagonal and this stable phase is triclinic.^{98,99} HD transient and metastable rotator phases were studied by Sirota and Herhold who determined the thermodynamic stability of

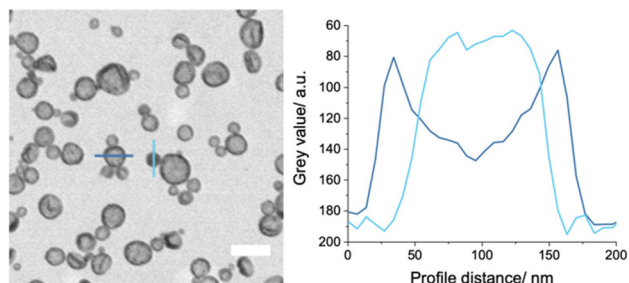


Fig. 3 (Left) STEM micrograph showing line profile across a PMMA capsule (dark blue) and PMMA particle (light blue). (Right) Grey value profile plotted against distance of a line traced across a PMMA capsule (dark blue) and PMMA particle (light blue).

the phases.¹⁰⁰ These solid–solid transitions are observed for bulk HD when cooled at 1 °C min^{-1} using the TA Instruments DSC 2500 (Fig. S2†). However, it has been shown that under confinement, *n*-alkanes exhibit changes in their crystal properties.¹⁰¹ Montengro and Landfester observed additional rotator phases transitions in nanodroplets and a size dependence of the stable crystal structure.¹⁰² From the spectra in Fig. 4 and 5, a mixture of many transitional phases is observed, but the elucidation of them all is beyond the scope of this work. Rotator phase transitions may also be responsible for the twin melting peaks for reaction PIBMA_HD, but more work using X-ray scattering is required to comment further.

(ii) As well as a significant difference in the shape of the crystallisation peaks, there are also considerable differences of supercooling (ΔT_c) depending on shell material. Reactions PMMA_HD and PBzMA_HD have a ΔT_c of 11.4 and 11.7 °C, whereas P*n*BMA_HD and PIBMA_HD crystallise at lower temperatures with a ΔT_c of 14.0 and 15.2 °C. The reasons for this are not fully understood at this moment in time. Nevertheless, it is possible to theorise potential reasons. Supercooling occurs due to the requirement of a nucleation event occurring in each capsule. As the capsules are <500 nm in diameter, the probability of having a foreign object (dust, *etc.*) to trigger heterogeneous crystal nucleation is extremely small, if not zero.¹⁰³ However, it may be possible that the capsule wall may act as a nucleation surface if it is significantly rough, in the same way scratching smooth glass triggers heterogeneous crystal nucleation. The inner surface of crosslinked PBzMA HD capsules was found to be considerably rough (Fig. S3†). The high inner shell roughness of PBzMA matches with the lower extent of ΔT_c . However, we do not know the inner surface topo-

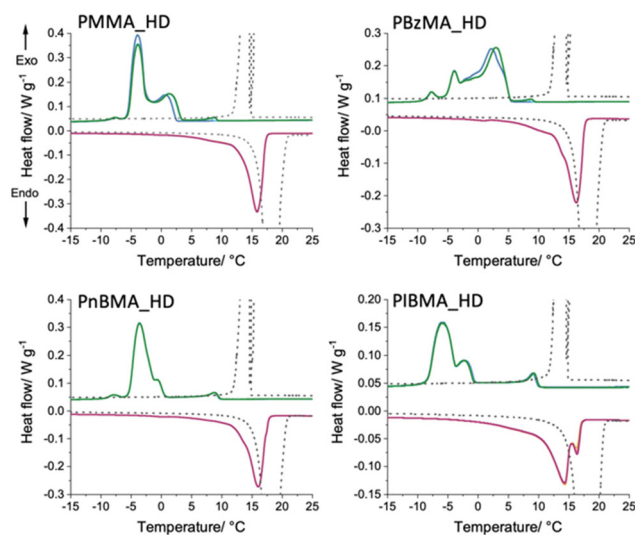


Fig. 4 Dynamic scanning calorimetry (DSC) curves for dried *n*-hexadecane crosslinked capsules synthesised with four different methacrylate monomers. Cooling curve for scans 1, 2 and 3 are coloured dark blue, light blue and green. Heating curves for scans 1, 2 and 3 are coloured yellow, pink and purple. Heat and cooling scans of bulk HD are shown as grey dashed line.



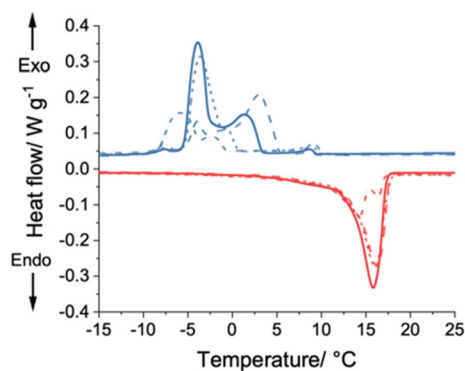


Fig. 5 Comparison of DSC curves for different methacrylate HD capsules. Measured using a TA Instruments DSC 2500, under nitrogen atmosphere, at 1 °C min^{-1} . The final scan of three temperature cycles is shown, cooling curves and heating curves are blue and red, respectively. Solid line (PMMA_HD), dashed line (PBzMA_HD), short-dashed line (PnBMA_HD), dashed-dotted line (PIBMA_HD).

graphy of PMMA_HD, PnBMA_HD and PIBMA_HD capsules. Yet, for PnBMA and PIBMA, given the closer likeness of the monomer side groups to HD, the more favourable solvent-polymer wetting during shell formation may lead to a smoother inner surface. This smooth surface would reduce the number of nucleation sites and further suppress the crystallisation point. Beside this, molecular dynamic studies on how different alkanes react to a specific polymer surface may provide insights.

(iii) A crystallisation peak at approximately 9.8 °C eventually appears for all capsule samples. For PMMA_HD and PBzMA_HD the peak does not appear in the first cooling scan and its appearance coincides with a shift in the main T_c to higher temperatures. The peak is present in all scans for reactions PnBMA_HD and PIBMA_HD. The event is kinetically driven as the melting transition for the four samples are identical. Fette and co-workers report a similar shift in aqueous capsule dispersions but, in their work, the entire peak shifts to the bulk temperature.¹⁰⁴ The authors proposed two hypotheses, the first explained the shift due to the exclusion of dissolved impurities in the HD over repeated cycles. These soluble impurities lowered T_c and are not to be confused with impurities that enable heterogeneous nucleation. Alternatively, over repeated cycles the shell walls become deformed producing a solid-phase nucleation site for crystallisation. The first theory does not fit as the impurity would also affect the melting transition. The shell deformation theory is also not in line with Fig. 4 as the peak at 9.8 °C remains stable after the first cycle in all samples. Nevertheless, the lower extent of supercooling does indicate a change in environment for the HD. It is possible that appearance of the peak may be caused by diffusion of HD out of the shell. For PnBMA_HD and PIBMA_HD the rate of diffusion through the shell was found to be fast (Fig. 6) and will be discussed later. It is likely the HD already moves through the shell upon drying and this matches with the observed peak during the first cycle. For PMMA_HD

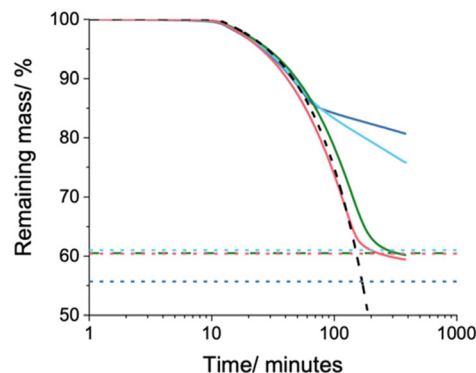


Fig. 6 Semi-log plot of percentage mass loss for crosslinked capsules containing hexadecane heated at 150 °C for 6 hours. Crosslinked capsule polymer used was poly(methyl methacrylate) (dark blue), poly(benzyl methacrylate) (light blue), poly(*n*-butyl methacrylate) (green) and poly(isobornyl methacrylate) (pink). Theoretical percentage masses after complete evaporation of HD are shown as dashed lines. Evaporation of bulk HD is shown as a black dashed line.

and PBzMA_HD, the rate of HD diffusion through the shell is restricted, but repeated crystallisation and melting appear to encourage a certain fraction to change the environment. In addition, the small peak appearing at 9.8 °C may be the result of a surface freezing phenomenon.¹⁰⁵

Regarding the melting points, there also appears to be the same split between the PMMA_HD, PBzMA_HD and PnBMA_HD, PIBMA_HD. The melting point depression (ΔT_m) of PMMA_HD and PBzMA_HD is 4.4 and 4.7 °C whereas ΔT_m of PnBMA_HD and PIBMA_HD are 5.2 and 6.6 °C . However, this trend appears to go against the thermodynamic theory of the Gibbs-Thomson equation (eqn (2)).⁷³ The Gibbs-Thomson equation describes the extent of melting point depression for a given capsule/pore size.^{73,106} The equation relates the energetic cost required to melt in a confined geometry due to the increase in Laplace pressure ($\Delta P = 2\gamma_{ij}/r$).

$$\Delta T_m = T_{m,b} - T_{m,\text{con}} = \frac{A \cdot \gamma_{ij} \cdot T_{m,b}}{r \cdot \Delta H_f \cdot \rho_c} \quad (4)$$

where $T_{m,b}$ and $T_{m,\text{con}}$ are the melting transition temperatures of the bulk phase and confined phase, γ_{ij} is the interfacial tension between the solid and the capsule wall, A is a geometry factor (2 for spherical pores, 4 for cylindrical), r is the radius of the confined phase, ΔH_f is the molar enthalpy of fusion and ρ_c is the crystal density. The interfacial tension of PMMA/HD was measured to be 18.1 mN m^{-1} by Mahdavian and the PBzMA/HD was determined to be 5.97 mN m^{-1} in Booth and co-workers.⁶⁰ It is highly probable that the HD will have a lower interfacial tension with PnBMA and PIBMA due to the hydrophobic groups of the polymers. However, a lower interfacial tension would result in a lower ΔT_m , opposite to the observed results in Table S3.†

Regardless, given the likeness of the side group of IBMA to HD, the solvent may interact strongly with the shell, resulting in non-freezing layers,⁷¹ which would alter the crystal-shell



interfacial tensions and complicate the thermodynamic prediction. Furthermore, the PIBMA shell material has a significant effect on the shape of the IBMA_HD endotherm. The theme of PIBMA as an outlier also carries over when comparing the measured enthalpy changes of the dried capsules in Table 4. Regarding the calculated percentage thermal storage efficiency (TSE, eqn (1)), reaction PIBMA_HD has a significantly lower value than the other three samples.

The interaction of HD with the shell may result in non-freezing layers which result in a deficit between the theoretical and measure ΔH_f .⁷¹

Given the hydrophobic nature of PnBMA alkane side chain and the bicyclic side group of PIBMA, a significant decrease in TSE would be expected as they are more compatible with HD.⁴⁸ Although the trend in Table 4 does not follow the theory exactly, there is a large decrease for IBMA_HD.

To further investigate the interaction of HD with the shell, the release profile of HD at elevated temperatures was measured by thermogravimetric analysis (TGA). It should be restated that TMA crosslinker was added to direct capsule formation. However, others report that crosslinking PS capsules with DVB results in highly porous shells.⁵⁷ For the TGA experiment, 50 μL of latex (20% w/w solids) was transferred into a 40 μL aluminium DSC/TGA pan. The surface tension of the liquid allowed for the pan to be overfilled. The samples were dried overnight at room temperature and the water evaporated leaving a ring of dried capsules in the bottom of each pan. Considering the boiling point of HD is 287 °C any loss overnight would be negligible. The dried samples were prepared this way to ensure comparable data, as the surface area of the material may influence evaporation rate.¹⁰⁷ The pans were sealed with pierced, crimped lids and the mass loss was recorded at 150 °C for 6 hours (Fig. 6).

For reference, a pan of pure HD was measured and is shown as the black dashed line. The coloured dashed lines represent the theoretical maximum mass loss for each sample based on the HD mass ratio. From Fig. 6 there is a clear split in evaporation rate between the capsules. For PnBMA and PIBMA, the rate of HD evaporation is unaffected, and it freely diffuses through the shell. For PMMA and PBzMA capsules, there is a two-stage release profile. HD evaporates at the bulk rate until at 15% mass loss, then the rate slows dramatically to

$-0.90\% \text{ h}^{-1}$ for PBzMA and $-0.40\% \text{ h}^{-1}$ for PMMA. Okubo and co-workers demonstrated from PS/DVB capsules swollen with toluene, the mass loss of residual solvent in the shell was dependent on crosslink density and shell thickness.¹⁰⁸ However, as the capsules in the four-monomer series had the same molar ratio of TMA crosslinker and ratio of HD to monomer, crosslinking and shell thickness cannot explain the observed difference in release rate. Alternatively, Taden and co-workers found a direct correlation between the capsule diffusion barrier and the interaction of the core and shell materials.¹⁰⁹ This argument appears much more likely, especially given the lower thermal storage efficiency of PIBMA_HD (Table 4), which was hypothesised to be due to more favourable HD-shell interaction.

Although the four polymers are immiscible in HD, and precipitate during capsule formation, the HD may act as a plasticizer. Plasticizers are a class of low-molecular-weight organic molecules that increase the flexibility, decrease tensile strength and lower the glass transition of polymers.¹¹⁰ The effect of HD on the glass transition of the four methacrylate polymers was probed by DSC. For this study, linear polymers were synthesised by solution polymerization. The glass transitions of the linear methacrylate polymers were measured dry and after soaking in HD for 48 hours (Table 5 and Fig. S4†).

Comparing the dry cooling cycle T_g values to literature (Table 5) PMMA, PBzMA and PnBMA are all close to reported data. Remarkably the value for PIBMA is 75 °C higher than the reported temperature in the polymer handbook. Although there is also a discrepancy in the literature, a higher value of 150 °C was reported by Zhang and Wang for PIBM, M_w 2.1 $\times 10^5 \text{ g mol}^{-1}$.⁸⁵

For PMMA and PBzMA, which both were soaked in hexadecane, the T_g of PMMA decreased by 14.0 and 16.2 °C measured during the heating and cooling scan, whereas PBzMA experienced a smaller decrease of 11.0 and 8.7 °C, during cooling and heating respectively. From the structures of these two polymers, it would be logical to assume they have a low compatibility with the aliphatic hydrocarbon HD. Plasticizers have the greatest effect when their structural properties are a close match to the polymers that they are interacting with.¹¹⁰

For PnBMA it would be expected that the plasticization effect is much greater. When cooled to -150 °C a sharp increase in specific heat was observed that shifted to lower temperatures with each scan (Fig. S4†). In the first scan (purple), a small step at -87.9 °C; in the second scan, a step change with a midpoint of -93.5 °C (light blue); and a shift to -101.9 °C in the third scan (dark blue). Unfortunately, the T_g of HD soaked PnBMA remains inconclusive due to the shape of the transition on cooling and lack of transition on heating. It should be noted that the mass of polymer analysed was substantial and should display a clear transition under normal conditions. 19.11 mg of sample was weighed and the calculated ΔH_f of HD was 20% of the bulk value, estimating ≈ 15 mg of polymer is present.

For HD soaked PIBMA, the sample was initially analysed between 20 and 230 °C (not shown). The glass transition for

Table 4 Monomer conversion and thermal properties of crosslinked methacrylate monomer series hexadecane capsules

Reaction	Monomer conversion/%	Theory	Measured	
		PCM loading ^a / % w/w	Capsule ΔH_f ratio ^b /%	TSE ^c / %
PMMA_HD	88.0	44.3	33.1	74.9
PBzMA_HD	100.0	39.0	29.5	75.7
PnBMA_HD	98.8	39.5	28.1	71.1
PIBMA_HD	98.6	39.6	18.2	45.9

^a Calculated using eqn (2), monomer conversion measured by gravimetry. ^b Calculated using eqn (1). ^c Calculated using eqn (3).



Table 5 Molecular weight characteristics and glass transition temperatures for methacrylate polymers. Polymers were measure dry or after soaking in hexadecane for 48 hours

	$M_n/\times 10^4 \text{ g mol}^{-1}$	$M_w/\times 10^4 \text{ g mol}^{-1}$	D	$T_g \text{ cooling}/^\circ\text{C}$		$T_g \text{ heating}/^\circ\text{C}$	
				Dry	HD soaked	Dry	HD soaked
PMMA	2.8	5.2	1.85	106.0	92.2	110.6	94.4
PBzMA	6.6	14.8	2.24	62.3	51.2	64.1	55.4
P <i>n</i> BMA	3.3	6.9	2.11	24.2	n.d	31.3	n.d
PIBMA	3.5	7.8	2.21	184.8	n.d	195.3	n.d

Glass transitions were measure using a TA Instruments DSC 2500 at a heating/cooling rate of $10 \text{ }^\circ\text{C min}^{-1}$ under an atmosphere of nitrogen. Data was taken from the final of three temperature cycles. Midpoint glass transition temperatures were measured following ASTM D3418-21 standards.⁸²

the dried polymer was determined in the cooling and heating scans to be 184.8 and 195.3 $^\circ\text{C}$, respectively. However, for the HD-soaked polymer, no transition was observed between 20–230 $^\circ\text{C}$. In response to this, the polymer was analysed down to $-150 \text{ }^\circ\text{C}$. Similar to HD soaked P*n*BMA, no discernible glass transition was observed in either cooling or heating scans. A weak transition in the heating scan that resembles the shape of glass transition is observed at $-40.0 \text{ }^\circ\text{C}$, however this contradicts the somewhat glassy physical appearance of the soaked polymer. Again, approximately 10 mg of polymer was analysed based on the measured enthalpy HD. Furthermore, for both P*n*BMA and PIBMA, if the transition was to occur below the crystallisation point of HD, the crystal lattice may also to interfere with the dynamic polymer glass formation process.¹¹¹

Once again there is a split in the observed properties of PMMA and PBzMA and of P*n*BMA and PIBMA when interacting with HD. Although the exact nature of the interaction could not be determined, to synthesise *n*-alkane PCM nanocapsules for use in thermal fluids, PMMA and PBzMA show the most potential, with PMMA having a slight edge looking at HD TGA release.

Encapsulation of *n*-octadecane and *n*-docosane for use as thermal fluid

To produce an aqueous PCM slurry, HD is no longer suitable due to the reduced crystallisation temperature ($<0 \text{ }^\circ\text{C}$) when encapsulated. In response to this, two higher molecular weight *n*-alkanes, *n*-octadecane (OCT, C18) and *n*-docosane (DOC, C22), with bulk crystallisation temperatures of 25.8 and 42.0 $^\circ\text{C}$, were selected. We assume that the knowledge gained using HD as a model compound is transferable to OCT and DOC. Regarding capsule formation by phase separation, any minor changes to the $\gamma_{\text{Pol}/\text{PCM}}$ and $\gamma_{\text{Aqu}/\text{PCM}}$ values will be overcome by the kinetic force of restricted polymer mobility due to cross-linking.

To encapsulate OCT and DOC, MMA was chosen as methacrylate shell monomer. Firstly, the size distributions of the mini-emulsion droplets and polymerised capsules were measured by DLS and presented alongside correlograms in Fig. 7. The spectra of the PMMA_OCT reaction droplets and capsules appears as expected for a typical mini-emulsion polymerization. The droplet and particle distribution are near

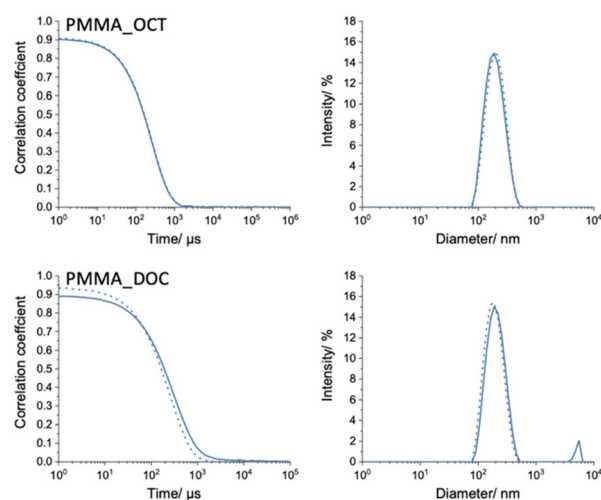


Fig. 7 Particle size analysis by DLS of crosslinked poly(methyl methacrylate) *n*-octadecane and *n*-docosane capsules. Correlograms (left) and normalized intensity weighted particle size distributions (right). Miniemulsion droplets are dashed lines, capsules are represented by solid lines.

identical with droplet Z-average diameter $186.5 \pm 0.9 \text{ nm}$ and PDI 0.109 ± 0.018 and capsule Z-average diameter $181.1 \pm 1.3 \text{ nm}$ and PDI 0.141 ± 0.031 . By contrast, there appears to be some irregularities in the correlogram and fitted distribution for the PMMA_DOC reaction. The correlation decay for capsules (solid line) is broader than droplets (dashed line) and when the data is fit using the cumulants method, a second distribution appears. For reaction PMMA_DOC, the droplet had a Z-average diameter of $175.0 \pm 0.7 \text{ nm}$ and PDI of 0.127 ± 0.021 . After polymerization, DLS recorded mean diameters of $213.3 \pm 1.8 \text{ nm}$ and $4891 \pm 291 \text{ nm}$ for the two populations. The percentage of larger objects by DLS intensity was 6.4%, by volume 15.8% and the peak disappeared in the number distribution. Additionally, the size distributions of PMMA_OCT and PMMA_DOC appear much broader than those recorded for the methacrylate monomer series (Fig. 1). To investigate this further the polymerised capsule latexes were imaged by SEM and STEM techniques (Fig. 8). As indicated by the DLS distribution, for PMMA_OCT, a very larger span of sizes can be seen



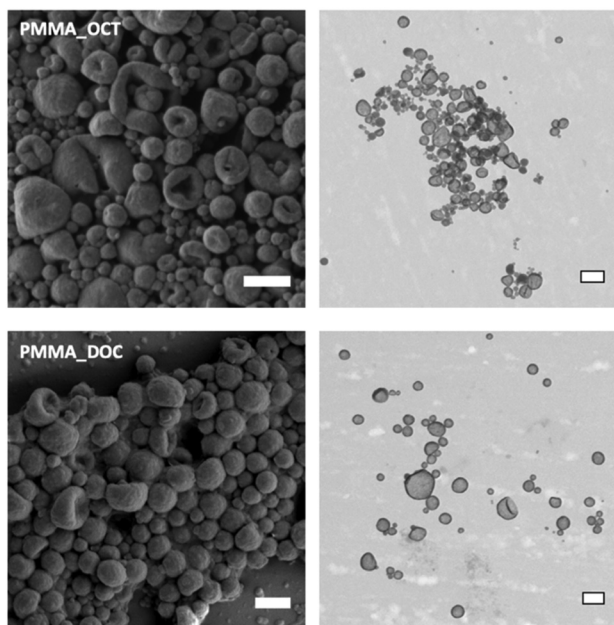


Fig. 8 Electron microscope images of crosslinked poly(methyl methacrylate) *n*-octadecane or *n*-docosane capsules. Scanning electron microscope (left) and scanning transmission electron microscope (right).

in the SEM image, suggesting the smallest particles have formed *via* secondary nucleation. This assumption is confirmed in the STEM image as the smallest particles are much darker, as explained previously (Fig. 3). A drawback of selecting MMA as the shell monomer is the higher water solubility (Table 2), which increases the probability of secondary nucleation. For the capsules, a difference in grey value across their profile is observed as *n*-octadecane is sublimed under EM vacuum, leaving hollow capsules.

For PMMA_DOC, the spread of sizes for the main population is like PMMA_OCT with some solid particles also found. Even with a melting point of 42 °C the docosane is sublimed under the extremely low pressures of the EM. This causes capsules to buckle, and a contrast difference is observed across the hollow capsules, identical to HD capsules (Fig. 3). However, unlike any of the capsule recipes discussed so far, the existence of micron-sized hollow structures was noted, a comparison of PMMA_OCT and PMMA_DOC imaged by light microscope in dark field mode is shown in Fig. 9.

The left image shows an image of PMMA_OCT latex, but the nanoparticles are unresolved. This is because the resolution of a light microscope is limited to half the wavelength of visible light and the particles by DLS are <500 nm in diameter. Several brighter particles are shown in the right image of PMMA_DOC, these represent the larger distribution seen in DLS after polymerization (*Z*-average 4891 ± 291 nm). To investigate this further the larger particles of PMMA_DOC were imaged by SEM and TEM, as shown in Fig. 10.

The large hollow objects appear to be decorated by smaller capsules and their structure draws similarities to Pickering stabilised emulsions.¹¹² As well as stabilising dispersed liquid,

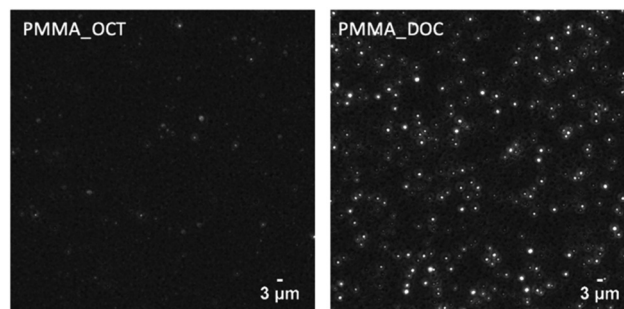


Fig. 9 Images of PMMA_OCT and PMMA_DOC latexes taken using a light microscope in dark field mode.

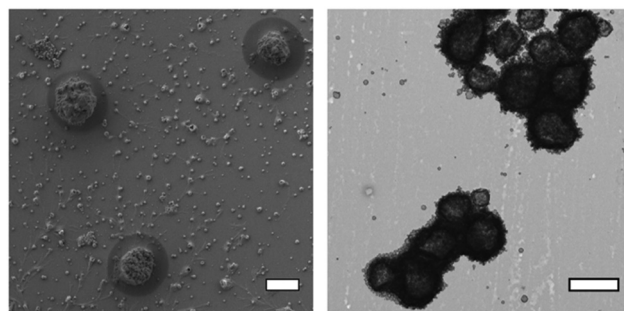


Fig. 10 Low magnification electron microscope images of poly(methyl methacrylate) *n*-docosane micro-sized objects. Scanning electron microscope (left) and scanning transmission electron microscope (right). Scale bars are both 2 μm.

Pickering stabiliser have also been shown to stabilise air droplets in the formation of stable foams.¹¹³ As DOC sublimes under EM conditions, it is inconclusive whether the large capsules are filled with DOC or air at ambient conditions. To probe this, the capsules as a latex were imaged on a heated light microscope stage above their melting point (Fig. 11). The latex was sandwiched between a microscope slide and a cover slip.

The left image shows a collection of large objects in the PMMA_DOC latex, the objects with a halo effect are out of focus due to diffusion in the *z*-plane. The collection of large objects is fixed in place due to the pressure of the glass cover slide. On heating above the melting point of bulk DOC, the expulsion of liquid can be seen in the right image. The evidence proves the capsules contain DOC, but that they also have a shell; although some liquid DOC is present at 50 °C, the majority of large capsules retained their core.

Their formation is not fully understood but it can be explained by investigating the reaction preparation steps. The mini-emulsion was prepared and emulsified 10 °C above DOC melting point. However, the mini-emulsion was not actively heated during 30 min of purging with nitrogen gas. On cooling, the monomer DOC mixture would have become supersaturated allowing for DOC to crystallise. When not encapsulated, this can lead to mini-emulsion destabilisation and



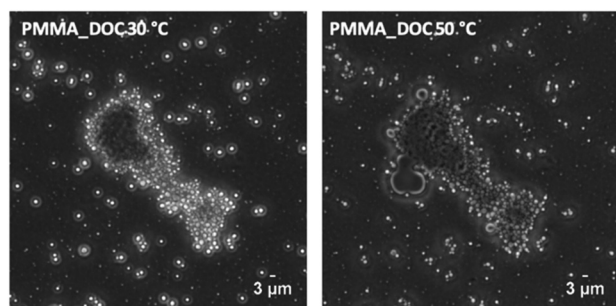


Fig. 11 Light microscope images of PMMA_DOC latex at 30 °C and 50 °C, DOC bulk M_p is 41.9 °C.

fusion of droplets leading to further crystal growth. Upon polymerization above the melting point, the now large droplets of DOC can heterocoagulate with mini-emulsion-derived DOC capsules, leading to the observed Pickering effect. To overcome this, the mini-emulsion should be heated above the DOC M_p at all times and not be allowed to cool.

Nevertheless, a substantial fraction of DOC was encapsulated into nanocapsules, as shown by DLS (Fig. 7) and therefore their thermal properties were measured. To investigate the phase change temperatures and latent heats of OCT and DOC capsules, the 20% w/w latexes were dried at ambient conditions to remove water and analysed using DSC. The dried powders were heated and cooled at a rate of 1 °C min⁻¹.

From the DSC curves of dried OCT PMMA capsules (Table 6 and Fig. 12), suppression of crystallisation and melting onset, as well as rotator phase transitions are observed. The main crystallisation peak for PMMA_OCT has a ΔT_c of 5.7 °C, this reduces to 4.4 °C after the first cooling/heating cycle as an addition peak appears, similar to the DSC spectra of PMMA_HD and PBzMA_HD (Fig. 5). The extent of supercooling is much less for PMMA_OCT than for HD PMMA capsules. The reason for this is not fully understood but given the similarities of the ΔT_m , it would appear the cause is a kinetic

Table 6 Transition onset temperature and enthalpy for crystallisation and fusion for *n*-octadecane (OCT) and *n*-dodecane (DOC) in cross-linked poly(methyl methacrylate) capsules. Measured using a TA instruments DSC 2500 under nitrogen atmosphere at 1 °C min⁻¹. The final heating and cooling scans of three cycles were analysed

Sample	Crystallisation			Melting		
	$T_{c,i}/$ °C	$T_{c,ii}/$ °C	$\Delta H_c/$ J g ⁻¹	$T_{m,i}/$ °C	$T_{m,ii}/$ °C	$\Delta H_f/$ J g ⁻¹
OCT (bulk)	25.4	—	208.9	26.0	—	209.7
PMMA_OCT	21.0 ^a	19.7	68.4	19.9	23.3	67.5
DOC (bulk)	42.8	—	234.1	41.9	43.3	232.5
PMMA_DOC	39.1	—	111.4	31.5	40.4	110.3

$T_{c,i}$ and $T_{c,ii}$ are onset temperatures of crystallisation, ΔH_c enthalpy of crystallisation, $T_{m,i}$ and $T_{m,ii}$ are onset temperatures of melting, ΔH_f enthalpy of fusion. ^aCrystallisation phase transition peak is not present in the first cooling scan.

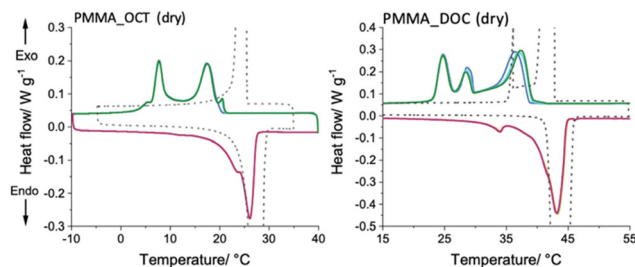


Fig. 12 Dynamic scanning calorimetry spectra of dried PMMA cross-linked capsules containing *n*-octadecane (left) and *n*-docosane (right). Phase transitions were measured using a TA Instruments DSC 2500, under nitrogen atmosphere, at a rate of 1 °C min⁻¹. Cooling scans 1, 2 and 3 shown as dark blue, light blue and green. Heating scans 1, 2 and 3 shown as yellow, pink and purple. Bulk *n*-octadecane and *n*-docosane are shown as dashed lines.

factor and not thermodynamic. A second large peak (onset of 9.3 °C) with an extended tail is also present. It is likely that this is a transition from rotator phase to the stable crystal phase as observed by in the bulk spectra (see later Fig. 15) and by Montenegro and Landfester for OCT in confinement.¹⁰²

Unlike PMMA_HD, the melting transition of PMMA_OCT shows a clear step change due to the solid–solid rotator phase melting transition with two onset temperatures 19.9 and 23.3 °C, both onsets are lower than the bulk temperature, ΔT_m 6.1 and 2.7 °C, due to nanocapsule confinement.^{114–116} The extent of melting point suppression for reaction PMMA_OCT is comparable to the 4.4 °C ΔT_m for the PMMA_HD nanocapsules. This result is in line with thermodynamic theory as the capsules are of similar size and will have similar core–shell interfacial tensions.

Inspecting the crystallisation behaviour of PMMA_DOC, three transitions occur during the broad transition with onset temperatures of 39.1, 29.5 and 26.1 °C. The large tailing peak at 39.1 °C may represent the micron-sized objects observed in DLS and EM imaging as the magnitude of ΔT_c is decreased on increasing capsule radius. On the other hand, the peak may represent a rotator phase transition. Further analysis using crystallographic techniques is required to confirm these theories. For PMMA_DOC the melting transition reflects the melting behaviour of the bulk material as both display secondary peaks during the transition due to the presence metastable crystal structures. The determination ΔT_m is complicated by the rotator transitions as they are likely to alter under confinement.¹⁰¹ Furthermore, the main melting transition of PMMA_DOC has three different gradients. In contrast to the sharp transition of bulk DOC, the process of melting in nanoconfinement is much more complex.

As with the previous capsules, the enthalpy of fusion was measured by DSC and compared to the theoretical value, this comparison is presented as the thermal storage efficiency (eqn (3) and Table 7). The TSE of PMMA_OCT is comparable to PMMA_HD (74.9%, Table 4) and this lower-than-expected value can be explained by favourable PCM–shell interaction causing non-freezing OCT. Assuming all the OCT is encapsu-



Table 7 Thermal properties of crosslinked poly(methyl methacrylate) *n*-octadecane (OCT) and *n*-docosane (DOC) dried capsules

Reaction	Monomer conversion/%	Theory	Measured	TSE ^c / %
		PCM loading ^a / % w/w	Capsule ΔH_f ratio ^b /%	
PMMA_OCT	77.9	44.9	32.2	71.6
PMMA_DOC	71.7	46.9	47.4	101.1

^a Calculated using eqn (2), monomer conversion measured by gravimetry. ^b Calculated using eqn (1). ^c Calculated using eqn (3).

lated, a TSE of 71.6% accounts for 14.5% by mass of the OCT that does not freeze. A further experiment to test this would be to vary the core : shell ratio. If this theory was correct, reducing the amount of shell material would reduce the amount of non-freezing OCT and a higher TSE would be obtained. Interestingly, in line with the theory, Zhao and co-workers encapsulated OCT with PMMA (no crosslinker) using a PCM loading of 86.7% and achieved a TSE of 101.5.

Although the core loading percentage of PMMA_OCT and PMMA_DOC is similar, PMMA_DOC has a much higher TSE. This cannot be explained by shell ratio but may be caused by shell interaction. Longer alkanes are less compatible with PMMA and it possible that the low interaction encourages all of the DOC to freeze when cooled. TSE of 100% for PMMA capsules of a commercial paraffin wax were also reported by Okubo and co-workers.⁶⁷

As the PCM nanocapsule are to be used as a latent function thermal fluid, their thermal properties as a 20% w/w solids latex were also analysed by DSC. Approximately 35 μ L of the latexes were transferred into hermetically sealed pans and the phase transition were measured as low as 0 $^{\circ}$ C and as high as 55 $^{\circ}$ C at a rate of 1 $^{\circ}$ C min⁻¹ (Fig. 13). As before the phase transitions were characterised and are presented in Table 8.

Interestingly, the crystallisation transitions are significantly altered when the nanocapsules are analysed as an aqueous dispersion. For LATEX_OCT (Fig. 13, left) the crystallisation phase

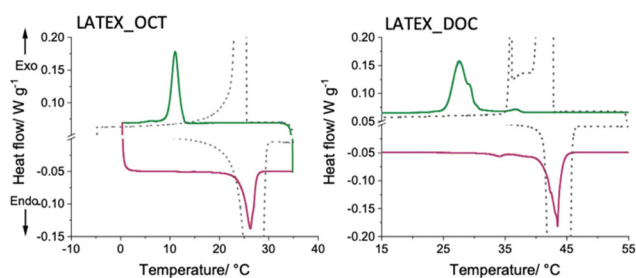


Fig. 13 Dynamic scanning calorimetry spectra of 20% w/w latexes of PMMA crosslinked capsules containing *n*-octadecane (left) and *n*-docosane (right). Phase transitions were measured using a TA Instruments DSC 2500, under nitrogen atmosphere, at a rate of 1 $^{\circ}$ C min⁻¹. Cooling scans 1, 2 and 3 shown as dark blue, light blue and green. Heating scans 1, 2 and 3 shown as yellow, pink and purple. Bulk *n*-octadecane and *n*-docosane are shown as dashed lines.

Table 8 Nanocapsule latex phase transition onset temperatures and enthalpy for crystallisation and fusion for *n*-octadecane (OCT) and *n*-dodecane (DOC). Measured using a TA instruments DSC 2500 under nitrogen atmosphere at 1 $^{\circ}$ C min⁻¹. The final heating and cooling scans of three cycles were analysed

Sample	Crystallisation			Melting		
	$T_{c,i}$ / $^{\circ}$ C	$T_{c,ii}$ / $^{\circ}$ C	ΔH_c / $J g^{-1}$	$T_{m,i}$ / $^{\circ}$ C	$T_{m,ii}$ / $^{\circ}$ C	ΔH_f / $J g^{-1}$
OCT (bulk)	25.4	—	208.9	26.0	—	209.7
LATEX_OCT	12.4	—	13.0	24.4	—	12.5
DOC (bulk)	42.8	—	234.1	41.9	43.3	232.5
LATEX_DOC	37.8	30.2	18.6	32.3	41.3	17.4

$T_{c,i}$ and $T_{c,ii}$ are onset temperatures of crystallisation, ΔH_c enthalpy of crystallisation, $T_{m,i}$ and $T_{m,ii}$ is onset temperatures of melting, ΔH_f enthalpy of fusion.

transition is simplified, with a single tailing peak with a crystallisation suppression ΔT_c of 13.0 $^{\circ}$ C. This is a much greater suppression than recorded for dried capsules in which the main peak was supercooled by 5.7 $^{\circ}$ C. Regarding the DSC spectra of LATEX_DOC, there is a main crystallisation peak with a small shoulder as well as a smaller peak closer to the bulk transition temperature. Interestingly, the smaller peak, with onset 37.8 $^{\circ}$ C matches the onset of large exotherm in PMMA_DOC at 39.1 $^{\circ}$ C, whereas the main peak for the latex at 30.2 $^{\circ}$ C is close to the dried second peak of 29.5 $^{\circ}$ C. There is a striking difference in intensity of OCT crystallisation around 38 $^{\circ}$ C when dried or dispersed and the similarities of the values cannot be ignored.

The significant difference in supercooling between the dried capsules and the aqueous dispersion of capsule may be caused by shell diffusion. To begin each DSC experiment, the PCM nanocapsule sample is heated above its melting point, then the three cooling–heating cycles begin. If during this initial heating stage, leakage of OCT and DOC occurred, crystallisation of this material would happen at much higher temperatures, this is more possible when dried as the capsules are in close contact in a packed film. As an aqueous dispersion the nanocapsules are continuously separated and only experience momentary collisions undergoing Brownian motion. This enhanced separation prevents crosstalk between capsules and leads to greater compartmentalisation and supercooling.

For the melting transitions, the endotherm for LATEX_OCT is also simplified; compared to the dried capsules (Fig. 12), the rotator transition at 19.9 $^{\circ}$ C is no longer observed. For the degree of suppression in main melting transitions, there is a slight difference with ΔT_m for LATEX_OCT calculated as 1.6 $^{\circ}$ C and PMMA_OCT as 2.7 $^{\circ}$ C. The melting transition of LATEX_DOC is a similar complexity to the dried sample with a small rotator phase transition occurring at 32.3 $^{\circ}$ C (31.5 $^{\circ}$ C for PMMA_DOC) and at least four changes in gradient during the main transition. Multiple gradients complicate the melting point depression calculation, but it is estimated to be 0.8–2 $^{\circ}$ C (onset between 41.3–42.5 $^{\circ}$ C) depending on the region of ana-



lysis. The difference of melting transitions may be influenced by the enhanced thermal regulation of water.

Proof of concept for a binary thermal fluid with multiple tuneable transitions

To demonstrate the feasibility of the OCT and DOC capsules as latent thermal fluid, an experiment was designed to evaluate the thermal performance of PCM capsule slurry against the base fluid. The designed experiment is similar to a method published by Yang for determining the thermal properties of bulk PCMs.¹¹⁶ A flat-based glass vial was partially filled with either PMMA_DOC latex or water. A temperature probe was submerged and the vial sealed with a PTFE temperature probe guide. The vial was placed on a thermoelectric module and heated at a constant heat flux for 800 seconds.

PMMA_DOC was chosen for the feasibility study due to the high TSE. To test the performance of the thermal fluid the sample was concentrated to 31.3% w/w under reduced pressure, this was carried out to increase the latent heat response of the fluid. However, high capsule solid contents should be avoided due to the loss of performance from the lower ratio of water and its high heat capacity (Table 9).

The temperature change over time was recorded in triplicate for the 31% w/w PMMA_DOC fluid and water and is plotted in Fig. 14. It should be noted that this is a study of first principles and further development of the experimental procedure is required. Due to the simplified experimental design, three repeats of each sample were carried out. Comparison of the 30% w/w PMMA_DOC latex and water base fluid heating rates implies the greater performance of the PCM dispersion. The high variance in the rates is most likely due to the heat loss through the glass vial sidewalls. An expected step change in temperature gradient during DOC melting, as proposed for PCMs by Yang, is not observed.¹¹⁷ This is due to the fast temperature ramp during the experiment which will lengthen the melting transition. Nevertheless, the initial results are encouraging for the application of the thermal fluid.

The compartmentalisation of OCT and DOC PCMs into nanocapsules enables the creation of a thermal fluid with multiple transitions. The current proposed system is 1 : 1 binary mixture but the possible combinations of different encapsulated PCMs and capsule mass fractions are vast. A branch of research exists that focuses on the study PCM mixtures known as eutectic PCMs.¹¹⁸ A eutectic system is a mixture of substances at a specific ratio that has a single melting point, the

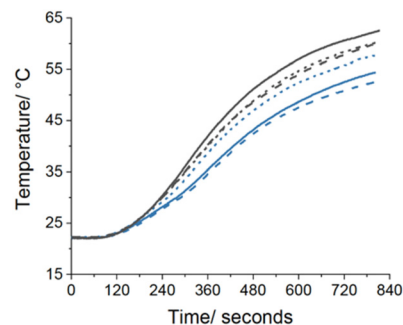


Fig. 14 Plot of fluid temperature during heating from a thermoelectric module at a constant heat flux. Water shown in black, DOC latex at 30% w/w solids shown in blue. Solid, dashed and dotted lines are repeat measurements.

melting temperature at the eutectic point is lower than the individual components.¹¹⁹ The eutectic PCM is generally chosen to alter the thermophysical properties of the system to match a specific application.^{120,121}

For the design of a binary thermal fluid, the encapsulation of waxes and prevention of core mixing is essential. To demonstrate the importance of PCM segregation, the phase transitions of bulk OCT and DOC, analysed separately and as a 1 : 1 mixture, are compared to a 1 : 1 dispersion of PMMA_OCT and PMMA_DOC capsules. Three cycles between -20 and 60 °C for the bulk *n*-alkanes were conducted, cycles between 0 and 60 °C were carried out for the latex mixture due to the presence of water. All scans were conducted at a rate of 1 °C min^{-1} . The phase changes of the *n*-alkanes when cooled and heated as a 1 : 1 mixture (Fig. 16) are changed dramatically compared to their separate bulk spectra (Fig. 15). There is a sharp onset of crystallisation for the mixture at 33.0 °C but the

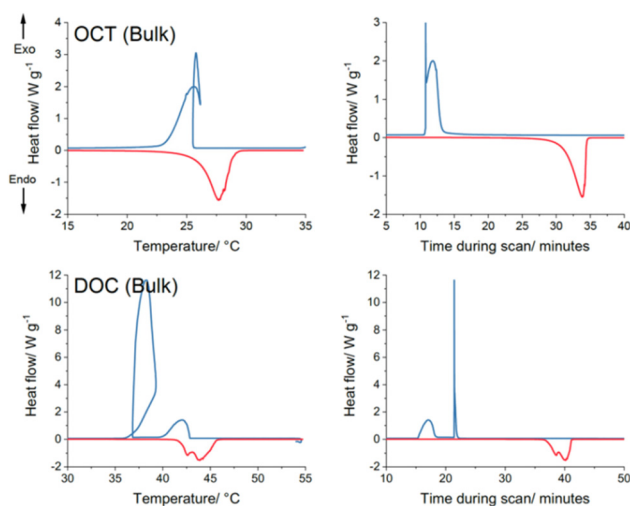


Fig. 15 DSC scans of *n*-octadecane and *n*-docosane. X-axes of temperature and time are shown to visual transition points. Cooling and heating scans shown in blue and red, respectively. Cooling and heating rate was 1 °C min^{-1} under an atmosphere of nitrogen.

Table 9 Energy required to heat water and PMMA_DOC aqueous thermal fluids at increasing solid contents from 20 to 60 °C

	Capsule solid content/% w/w			
	Pure water	20	30	50
Energy required/kJ	168.4	164.4	162.4	158.4

The temperature-dependent specific heat capacity and transition enthalpy data found in the ESI (Table S4†).



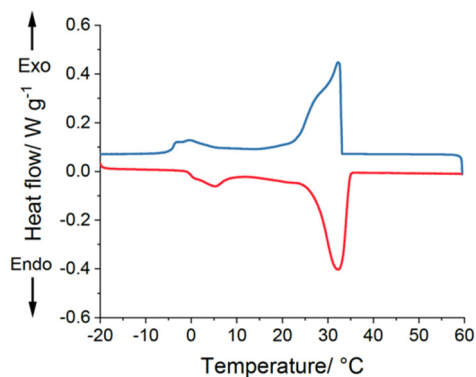


Fig. 16 Dynamic scanning calorimetry spectra of 1:1 pure wax mixture of *n*-octadecane and *n*-dodecane. Phase transitions were measured using a TA Instruments DSC 2500, under nitrogen atmosphere, at a rate of 1 °C min^{-1} . Cooling and heating shown as blue and red, respectively.

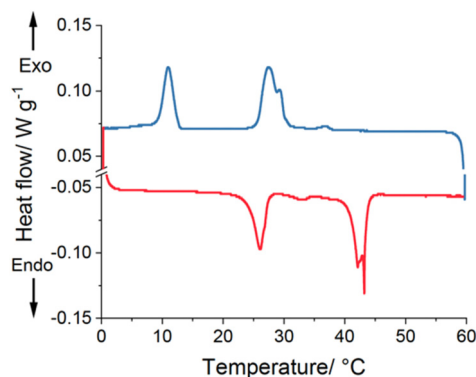


Fig. 17 Dynamic scanning calorimetry spectra of 1:1 capsule mixture of *n*-octadecane and *n*-dodecane waxes. Phase transitions were measured using a TA Instruments DSC 2500, under nitrogen atmosphere, at a rate of 1 °C min^{-1} . Cooling and heating shown as blue and red, respectively.

heat flow continuous to change until 0 °C indicating during this period a stable crystal structure was not reached. A similar reflection of this is observed in the melting transition of the bulk mixture.

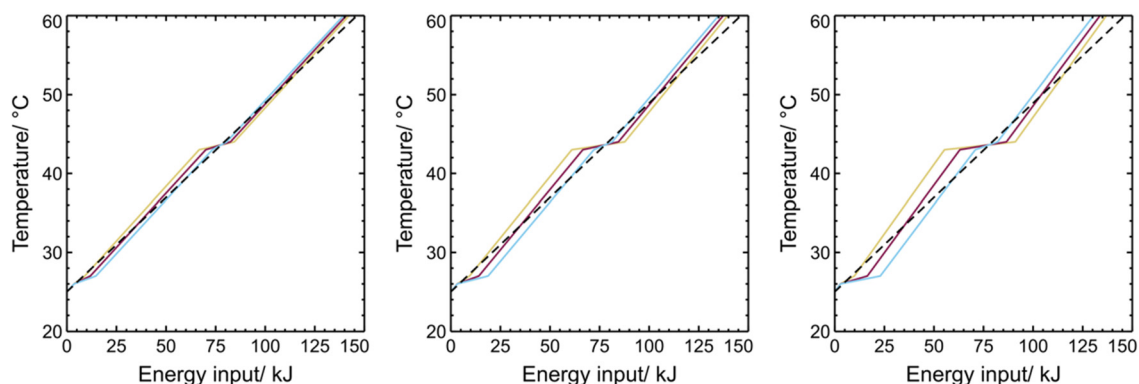


Fig. 19 Thermal energy profile for linear combinations of PMMA_OCT and PMMA_DOC capsule dispersions at varying capsule wt%. 30 wt% (left), 50 wt% (centre) and 70 wt% (right). DOC : OCT ratio in each case is represented as 20 : 80 (blue), 50 : 50 (pink), 80 : 20 (yellow).

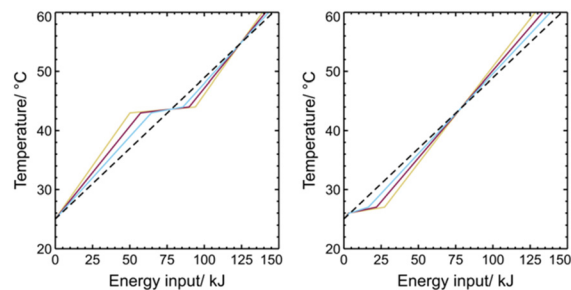


Fig. 18 Thermal energy profile for PMMA_OCT (left) and PMMA_DOC (right) capsule dispersions at varying capsule wt%: 30 wt% (blue), 50 wt% (pink), 70 wt% (yellow).

The benefits of encapsulation are clear when analysing the 1:1 mixture of OCT and DOC nanocapsules (Fig. 17). Blending the capsule dispersions produces a combinatorial spectrum of the two PCMs from Fig. 13. The identical phase transition onset temperatures in the latex blend compared to individual latexes demonstrates that no cross-talk occurs and the different PCMs remain compartmentalised throughout.

To this end, through the combination of both OCT and DOC capsules in varying proportions, it is possible to afford tunability to the thermal energy storage properties of a latent thermal fluid. That is, we can choose whether to have one or two latent heats present and we can vary the magnitude of each by simply varying the relative proportions of each capsule dispersion added to the system. Theoretical calculations were carried out to model the thermal energy storage profile of each of the DOC and OCT dispersions individually and of blends of the two capsule dispersions thereof. The total thermal energy stored by a material can be viewed as the summation of the sensible/specific heat (related to increasing the temperature of the material) and the latent heat (related to a material phase change) and is given by eqn (5) and (6).

$$Q = \sum(\text{sensible} + \text{latent}) \quad (5)$$

$$Q = mc_p\Delta T + \Delta H_{\text{transition}} \quad (6)$$



This is made more complex by the temperature-dependent nature of the specific heat capacity of a material and can be expressed as:

$$Q = m \int_{T_1}^{T_2} c_p(T) dT + \Delta H_{\text{transition}} \quad (7)$$

Given that a phase transition may occur anywhere during a given temperature range the total thermal energy stored can be split into the sensible heat before and after the phase transition and the enthalpy of the given transition:

$$Q = m \int_{T_1}^{T \leq T_{\text{transition}}} c_p dT + \Delta H_{\text{transition}} + m \int_{T_{\text{transition}} \leq T}^{T_2} c_p dT \quad (8)$$

Using eqn (8) and the temperature-dependent specific heat capacity and transition enthalpy data found in the ESI (Table S4†) the thermal storage profiles for heating from 25 to 60 °C can be calculated (Fig. 18 and 19). The latent heats utilised in these calculations were taken as those for the confined wax obtained *via* DSC (see Table 6).

Conclusions

A latent functional thermal fluid with multiple, separate, endothermic and exothermic transitions has been developed. This was accomplished by nanoencapsulation of OCT and DOC PCMs in a crosslinked PMMA shell *via* mini-emulsion polymerization. SEM and STEM were used to show the encapsulation of both PCMs was successful. However, a population of micron-sized DOC capsules were also observed which were a result of DOC crystallisation in monomer droplets before polymerization. It was found the extent of supercooling was much greater for the fluid dispersion than for dried capsules. This was theorised to be caused by capsule leakage in the dried state, which was restricted when dispersed. This observation also strengthens the argument for the usefulness of the PCM fluid. A deep understanding of the encapsulation process and shell-core compatibility was gained in this study, and this helped to drive the development of a binary thermal fluid. The proof-of-concept study was successful. The performance of the DOC nanocapsule dispersion was evaluated as a cooling fluid against water by itself and demonstrated promising results. Furthermore, we showed that, indeed, dispersions of PCM capsules containing *n*-octadecane and *n*-dodecane could be blended into a bespoke thermal fluid dispersion. Calculations show that such mixtures bring benefits to performance and, therefore, that the concept of tuneability has been realised. From the overall results, it becomes clear that nanocapsule PCM dispersions can behave superior to water in energy storage and release, in certain temperature windows. The challenges are not only to optimize this efficiency but also to look at the effects on the thermal conductivity and durability of the system.

Author contributions

Joshua R. Booth: conceptualization, formal analysis, investigation, methodology, project administration, resources validation, visualization, writing – original draft. Joshua D. Davies: formal analysis, investigation, visualization, writing – original draft. Stefan A. F. Bon: conceptualization, supervision, project administration, methodology, formal analysis, resources, funding acquisition, writing – review and editing.

Data availability

The data supporting this article have been included as part of the ESI.†

Conflicts of interest

There are no conflicts to declare.

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