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## Towards graphene-based asymmetric diodes: a density functional tight-binding study

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Self-consistent charge density functional tight-binding (DFTB) calculations have been performed to investigate the electrical properties and transport behavior of asymmetric graphene devices (AGDs). Three different nanodevices constructed of different necks of 8 nm, 6 nm and 4 nm, named Graphene-N8, Graphene-N6 and Graphene-N4, respectively, have been proposed. All devices have been tested under two conditions of zero gate voltage and an applied gate voltage of +20 V using a dielectric medium of 3.9 epsilon interposed between the graphene and the metallic gate. As expected, the results of AGD diodes exhibited strong asymmetric  $I(V)$  characteristic curves in good agreement with the available experimental data. Our predictions implied that Graphene-N4 would achieve great asymmetry ( $A$ ) of 1.40 at  $|V_{DS}| = 0.2$  V with maximum transmittance ( $T$ ) of 6.72 in the energy range 1.30 eV. More importantly, while the  $A$  of Graphene-N4 was slightly changed by applying the gate voltage, Graphene-N6/Graphene-N8 showed a significant effect with their  $A$  increased from 1.20/1.03 under no gate voltage (NGV) to 1.30/1.16 under gate voltage (WGV) conditions. Our results open up unprecedented numerical prospects for designing tailored geometric diodes.

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### Introduction

Since its discovery, graphene<sup>1</sup> has shown outstanding features for the design and implementation of various devices with excellent carrier mobility,<sup>2</sup> mechanical properties,<sup>3</sup> thermal conductivity,<sup>4</sup> and optoelectronic properties.<sup>5,6</sup> The unique structure and intriguing mechanical and electronic properties of graphene have made it the subject of ever-growing research interest all over the world. This material consists of a planar, monatomic carbon layer arranged in a regular hexagonal structure with intermediate  $sp^3$ - $sp^2$  orbital hybridization of all atoms required to exhibit aromatic behavior. The C-C bonds in graphene have an intermediate length between C-C  $sp^3$  and C-C  $sp^2$  bonds.<sup>7</sup> Graphene is a perfect two-dimensional crystal with conductivity mediated by electrons with zero effective mass. These features make graphene a promising material for a new generation of solid-state electronics,<sup>8</sup> especially for applications in radio frequency electronics,<sup>9</sup> optoelectronics,<sup>10</sup> and sensor systems.<sup>11,12</sup>

Recent developments in fabrication techniques increased the carrier mobility of graphene to  $\sim 200\,000$  cm<sup>2</sup> V<sup>-1</sup> s<sup>-1</sup> at

room temperature<sup>13</sup> with a long carrier mean free path length (MFPL) exceeding 28  $\mu\text{m}$ .<sup>2</sup> An MFPL of the order of the critical dimension of conventional lithography techniques enables the realization of asymmetric graphene devices (AGDs),<sup>14</sup> which in recent years have received a great deal of attention. These devices can present ballistic transport properties in different geometries, *e.g.*, in two-terminal geometric diodes<sup>15,16</sup> and in three- or four-terminal graphene ballistic rectifiers.<sup>17</sup> Unlike conventional diodes and transistors, AGDs do not require a sizable band gap to exhibit current-voltage asymmetry. They instead rely on ballistic charge transport across a geometrically defined, asymmetric junction with dimensions of the same order as, or less than the MFPL.<sup>18</sup> To exhibit ballistic transport, scattering must be limited to the edges of the graphene device.<sup>19</sup>

Due to the lack of a bandgap, low turn-on voltages make ballistic graphene diodes prime candidates in energy harvesting and microwave detection applications at low received signal levels.<sup>20,21</sup> The combination of a high-frequency rectifier and an antenna is referred to as a *rectenna* in the literature. Rectennas have been successfully employed for energy harvesting at low frequencies in the microwave range and have recently attracted considerable research interest for their application to higher frequencies in the mm-wave, terahertz,<sup>22-24</sup> and infrared<sup>25,26</sup> spectral regions. Unlike photovoltaic cells, whose frequency response is determined by the semiconductor's bandgap, a rectenna's frequency response can be defined by the antenna,

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allowing high rectification efficiencies and responsivities across a wide spectral region.<sup>17,27,28</sup>

The rectification of solar electromagnetic radiation was first proposed in 1972, recognizing however the technical limitations of the time in realizing a rectifier that could operate at optical frequencies, in which the concept had the potential to achieve a maximum power conversion efficiency of 93%.<sup>29</sup> The proposed structure consists of patterned monolayer graphene, and the critical region of the diode is the neck (N) of graphene (Fig. 1). Scattering at the device edges allows motion of charge carriers preferentially in *a* direction defined by its geometry: charge transport occurs from right to left electrodes, which correspond to drain and source, respectively, through the neck channel.

So far, some experimental measurements and Monte Carlo simulations have been carried out to assess the physical properties of AGDs such as current (voltage)  $I(V)$  characteristics, responsivity, resistivity, and symmetry (*A*) as a method to evaluate the transport characteristics of diodes and consequently their rectification efficiency.<sup>30,31</sup> These findings suggest that the neck of graphene influences electron transport in the ballistic regime. In an experimental and theoretical study conducted by Zhu *et al.*,<sup>20</sup> a rectenna solar cell was fabricated from a geometric graphene diode to improve the rectifier efficiency with respect to the rectennas used in metal-insulator-metal (MIM) diodes which have been shown to be limited in their RC response time and poor impedance. While the results obtained from measured and Drude model simulations revealed asymmetric  $I(V)$  curves for the diode, the Monte Carlo simulation indicated that a smaller neck size yields lower current values with a greater *A*. In another work, Zhu *et al.*<sup>15</sup> demonstrated the rectification at an AGD at 28 THz with potential

rectification at optical frequencies. To investigate the effect of the geometry on  $I(V)$  properties, they fabricated another device with a symmetric graphene diode. The results demonstrated an asymmetric graphene diode with an *A* of 1.16 possessed better rectifier efficiency than a symmetric device with an *A* of 0.5. Nguyen<sup>32</sup> evaluated four AGD structures by mechanical changes in their geometry, including neck length and the direction of the current. In a study based on experimental observation and numerical simulations, they reported different *A* values for different types of ballistic device. This research proposed that a device with the typical shape of a ballistic rectifier provides a wide area for passing current in forward and backward directions, resulting in greater spreading of charges and higher *A*. In another study by Moddel *et al.*,<sup>25</sup> using a 1  $\mu\text{m}$  asymmetric thin graphene film diode, an *A* of 1.31 was obtained by applying a constant gate voltage ( $V_g = +18\text{ V}$ ).

From these foundations and the lack of knowledge about the atomistic behavior of geometric graphene diodes, we were persuaded to investigate the  $I(V)$  characteristics and corresponding *A* and transmittance (*T*) properties of AGDs. Herein, we propose three geometric graphene diodes investigated by density functional tight binding (DFTB) for the first time. DFTB, driven by its remarkable predictive power using the most accurate functionals, could operate as a pioneering tool in this field. DFTB is an approximation of density functional theory (DFT) with reduction of Kohn–Sham equations in the form of tight binding (TB). The original<sup>33,34</sup> formalism limits interactions to a non-self-consistent two-center Hamiltonian between confined atomic states. Later, a second-order expansion of the Kohn–Sham energy enabled charge self-consistent treatment of systems.<sup>35</sup>

Together with the high level of fabrication technology that has been reached experimentally, computer simulation at the nanoscale has become an indispensable tool for understanding the properties of devices that meet ever-increasing performance demands. Since the size of modern electronic and optoelectronic devices continues to be scaled down, quantum mechanics approaches based on atomistic simulations are inevitable to account for quantum mechanical phenomena that affect the transport and optical properties of nanoscale devices. In this regard, we modelled and simulated three graphene devices with a square area (length  $L =$  width  $W = 15\text{ nm}$ ) with different neck widths (Fig. 1). Graphene-N8, Graphene-N6, and Graphene-N4 correspond to devices with neck widths of 8 nm, 6 nm and 4 nm and angles of 63°, 58° and 52°, respectively, keeping all other parameters fixed. Finally, a dielectric medium and a gate region were added to atomistic systems to better reproduce experimental conditions. In our recent work,<sup>36</sup> we introduced a novel concept of the transport properties of geometric graphene diodes based on only one angle and an edge width (*E*) (instead of the neck), and the results showed a nonlinear electrical property with great transport characteristics. These studies allow us to investigate the responses of these diodes to an external electric field; the approach represents an important milestone in terms of atomistic simulations for optimizing graphene

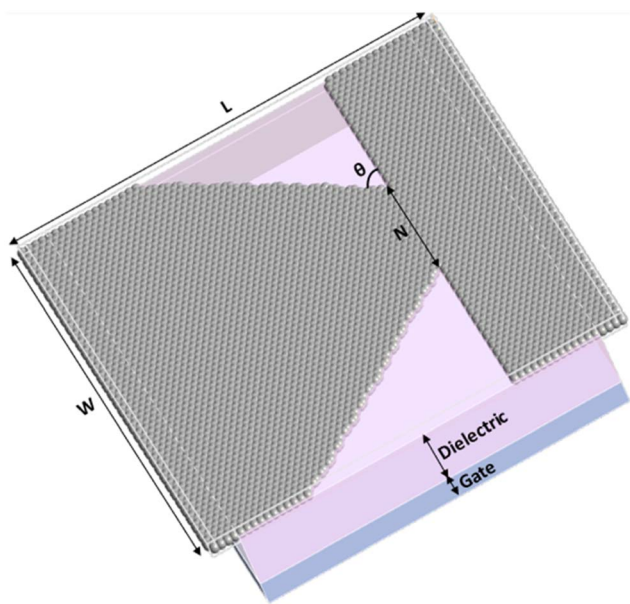


Fig. 1 Schematic representation of the graphene device with the presence of the ballistic graphene monolayer; the metallic gate and dielectric. The grey sticks are C atoms.



diodes for use in potential applications for energy harvesting devices.

## Computational methods

To better understand graphene-based devices, a preliminary study on the selection of a supercell was performed, in which graphene was investigated as a monolayer. We studied in detail the short-range phenomena that lead to the peculiar properties of graphene. In this context, a DFT approach on the basis of the Perdew–Burke–Ernzerhof (PBE) exchange correlation (xc) functional<sup>37,38</sup> was used. The band structure of graphene around the Fermi level is a perfect example of the TB model using just a single  $p_z$ -orbital ( $z \perp$  graphene) per carbon atom and nearest-neighbor interactions. Therefore, it can be easily reproduced by a linear combination of atomic orbitals (LCAO) with a single orbital per valence state for each carbon atom, corresponding to one  $s$  and three  $p$  orbitals. For this description, an LCAO basis set was adopted.<sup>39,40</sup> Norm-conserving Pseudo Dojo pseudopotentials<sup>41</sup> were used to describe the  $1s^2$  orbitals of C atoms. The energy cut-off was fixed at 900 eV and Brillouin-zone integration was performed over a  $50 \times 50 \times 1$   $k$ -point grid. These parameters were obtained with total energy convergence of  $1 \times 10^{-6}$  eV and force convergence of  $5 \times 10^{-5}$  eV per atom. QuantumATK (QATK) software<sup>42</sup> was utilized for all calculations.

Then, the semiempirical (SE) method<sup>43</sup> implemented by TB calculation was adopted for the simulation of geometric graphene diodes. The total energy of the TB method from a system of  $M$  electrons in a field of  $N$  nuclei was determined with the following equation,

$$E_0^{\text{TB}} = \sum_i^{\text{occ}} \langle \psi_i | \hat{H}_0 | \psi_i \rangle + E_{\text{rep}} \quad (1)$$

referring to occupied Kohn–Sham eigenstates  $\psi_i$ , with  $\hat{H}_0$  as the Hamiltonian operator, while the latter parameter  $E_{\text{rep}}$  strictly refers to the pairwise, repulsive, and short-range interactions. To solve the Kohn–Sham equations, single-particle wave functions  $\psi_i$  within the LCAO method are expanded into a suitable set of localized atomic orbitals  $\varphi_v$ ,

$$\psi_i(r) = \sum_v C_{vi} \varphi_v(r - R_\alpha), \quad (2)$$

where  $R_\alpha$  is the core distance of ion  $\alpha$ . Using this method, we employ confined atomic orbitals in a Slater-type representation. These are determined by solving a modified Schrödinger equation for a free neutral pseudoatom.<sup>44</sup>

The non-self-consistent field (nscf) part of the TB Hamiltonian was parametrized using a Slater–Koster model in which the distance-dependence of matrix elements is given by a numerical function.<sup>45</sup> The electronic transport properties were calculated using the non-equilibrium Green's function (NEGF) formalism.<sup>35,46–48</sup> Then, the coherent transport of electrons was assumed to occur between source and drain through the central region.

Once the self-consistent non-equilibrium density matrix had been determined, we evaluated the transport property and

current amount using the transmission coefficient  $T$  at electron energy  $E$  determined from the retarded Landauer formula,<sup>49</sup>

$$I(V_L, T_L, V_R, T_R) = \frac{e}{h} \sum \int T_\sigma(E) \left[ f\left(\frac{E - \mu_R}{k_B T_R}\right) - f\left(\frac{E - \mu_L}{k_B T_L}\right) \right] dE, \quad (3)$$

where  $f$  is the Fermi energy and  $T_L/T_R$  is the electron temperature of the left/right electrode, where the L and R electrodes are the source and drain, respectively.  $T_\sigma(E)$  is the transmission coefficient for spin component  $\sigma$ . Finally, the chemical potentials of the right/left electrode and  $V_{\text{bias}}$  can be defined by eqn (4)–(7),

$$\mu_R = E_F^R - eV_R \quad (4)$$

$$\mu_L = E_F^L - eV_L \quad (5)$$

$$\mu_R = \mu_L - eV_{\text{bias}} \quad (6)$$

$$V_{\text{bias}} = V_L - V_R \quad (7)$$

This approach suggests that a quantitative computationally inexpensive description of coherent transport in solid-state physics is readily achievable, enabling a new understanding of and control over charge transport properties of atomistic-scale interfaces at large bias voltages.

The simulated  $I(V)$  dependencies refer to the specific transversal width of modelled devices using different boundary conditions (BCs). For simulation of the graphene monolayer, periodic BCs were used along  $x$  and  $z$  axes. Then, the  $y$  axis was increased to interrupt the periodicity to ensure the simulation of a unique monolayer. For diode simulations, the periodicity was interrupted along  $x$  and  $y$  directions since the real dimensions of the devices ( $15 \text{ nm} \times 15 \text{ nm}$ ) were simulated by changing the neck size. Then, a fixed potential was generated along the  $z$  axis using the Dirichlet condition. A Dirichlet BC means that the potential has been fixed to a certain potential ( $V_0$ ) at the boundary, for a facet  $S$  of the simulation cell,

$$V^H(r) = V_0, r \in S \quad (8)$$

To specify metallic and dielectric regions in combination with device systems, we need to find a solution for calculating the Hartree energy. This effect can be solved with the Poisson equation. For a metallic region denoted  $\Omega$ , the electrostatic potential is fixed to a constant potential value ( $V_0$ ) within this region, *i.e.*, the Poisson equation is solved with the constraint,

$$V^H(r) = V_0, r \in \Omega \quad (9)$$

For a dielectric region denoted  $\gamma$ , the right-hand side of the Poisson equation will be modified as follows:

$$\nabla^2 V^H(r) = -\frac{e^2}{4\pi\epsilon_0} n(r), r \notin \gamma \quad (10)$$

$$\nabla^2 V^H(r) = -\frac{e^2}{4\pi\epsilon_r\epsilon_0} n(r), r \notin \gamma, \quad (11)$$



where  $\epsilon_r$  is the relative dielectric constant, which can be specified as an external parameter in the calculations.

## Results and discussion

### 2D graphene characterization

To calculate the single monolayer properties of graphene and to compare our results with literature validating the reliability of the computational method, a  $4 \times 20$  nm system was modelled as a starting structure along  $x$  and  $z$  axes, respectively. Then, we increased the  $y$  axis to interrupt the periodicity to ensure the simulation of a unique monolayer (Fig. 2). Structural optimization revealed the precise displacements of atoms in the monolayer space. We confirmed that the final structure had the thickness of a C atom; moreover, bond angles and dihedral values found were always in line with a system based on planar hexagonal condensed rings. The bond length was always 1.42 Å, perfectly in agreement with the hybrid state of C–C bonds that favors the delocalization of the electrons among rings.

While the bond length is intermediate between a single and a double C–C bond, we found a perfectly conjugated system which allows the electron cloud to be delocalized over ring structures, giving graphene the already known outstanding property of electron mobility and conductivity.

Graphene possesses a zero-band gap and a linear dispersion relation due to massless electrons, and computations confirmed this behavior. In the calculation of the graphene band structure (Fig. 3(A)), seven bands have been reported with different colors in relation to the lowest and highest energy values. The effective mass was calculated considering each band, and values of 0.0008, 0.0009, 0.0011, 0.0021, 0.0016, 0.0009, 0.0039 and 0.0012 were obtained. Moreover, contacts between conduction bands and valences bands were detected in  $K$ -points in the Brillouin zone, where we can also observe the Dirac cones (see Fig. 3(A)). Following the Brillouin zone of graphene, six crossing points in the  $K$ -points can be detected, which means that we have six Dirac cones, and all of them appear in the six corners of the aromatic ring (Fig. 3(B)).<sup>50</sup>

In terms of energy, these bands intersect exactly at  $E_F$  (the Fermi level), which corresponds to the special  $K$ -point in the reciprocal space of the hexagonal lattice. In the density of states,

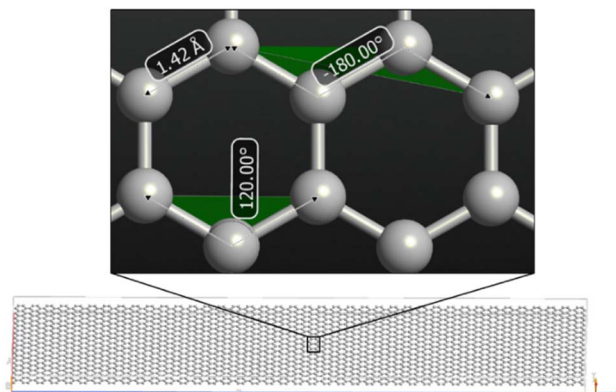


Fig. 2 Graphene monolayer with a focus on two rings.

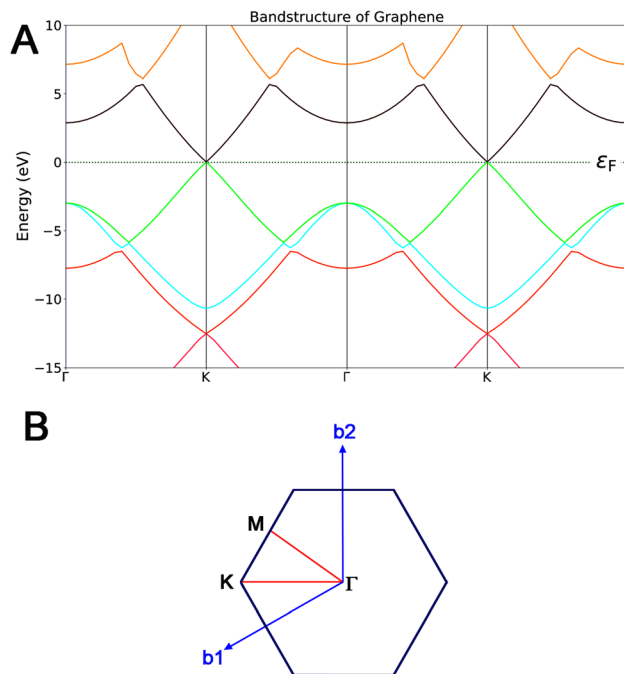


Fig. 3 Bandgap structures (A) and Brillouin zone of graphene (B).

the Dirac-cone-like energy bands result in a V-shaped structure with vanishing carrier density at  $E_F$ ; thus, monolayer graphene is a kind of zero-gap semimetal.<sup>51</sup>

### $I(V)$ characteristics of graphene diodes

Next, after the validation step, diodes with dimensions of 15 nm<sup>2</sup> along  $x$  and  $z$  axes were modelled, then three different necks were generated.  $I(V)$  property calculations were carried out for these geometrical graphene devices consisting of Graphene-N8, Graphene-N6, and Graphene-N4 at zero gate voltage. The computed results in Fig. 4(A) reveal the non-linear  $I(V)$  shapes of all cases in excellent consistency with the experimental measurements of Zhu *et al.*<sup>20</sup> According to the data presented in Fig. 4(A) and Table 1, by decreasing the neck width of the graphene devices from 8 nm to 4 nm, the current values were reduced at positive and negative voltages. Moreover, the amount of current at voltage 0.5 V reduces from 42  $\mu$ A for Graphene-N8 to 33  $\mu$ A for Graphene-N6 and 27  $\mu$ A for Graphene-N4. Similarly, the current values at voltage  $-0.5$  V dropped from 41  $\mu$ A for Graphene-N8 to 29  $\mu$ A for Graphene-N6 and 22  $\mu$ A for Graphene-N4. These values obtained from our quantum simulations for Graphene-N6 are in excellent agreement with experimental outcomes<sup>20</sup> (see Table 1) with 35  $\mu$ A and 30  $\mu$ A at  $-0.5$  V and 0.5 V, respectively. Conversely, our results follow the same trend as the Monte Carlo simulation in ref. 52 for large-scale geometric graphene diodes with neck widths of 50 nm, 200 nm and 600 nm.

In the next step, we performed quantum simulations for the effect of applying a gate voltage ( $V_g$ ) of 20 V to the three graphene devices in the presence of the dielectric ( $\epsilon$ ) in the zone between graphene diodes and the metallic gate (Fig. 1), to



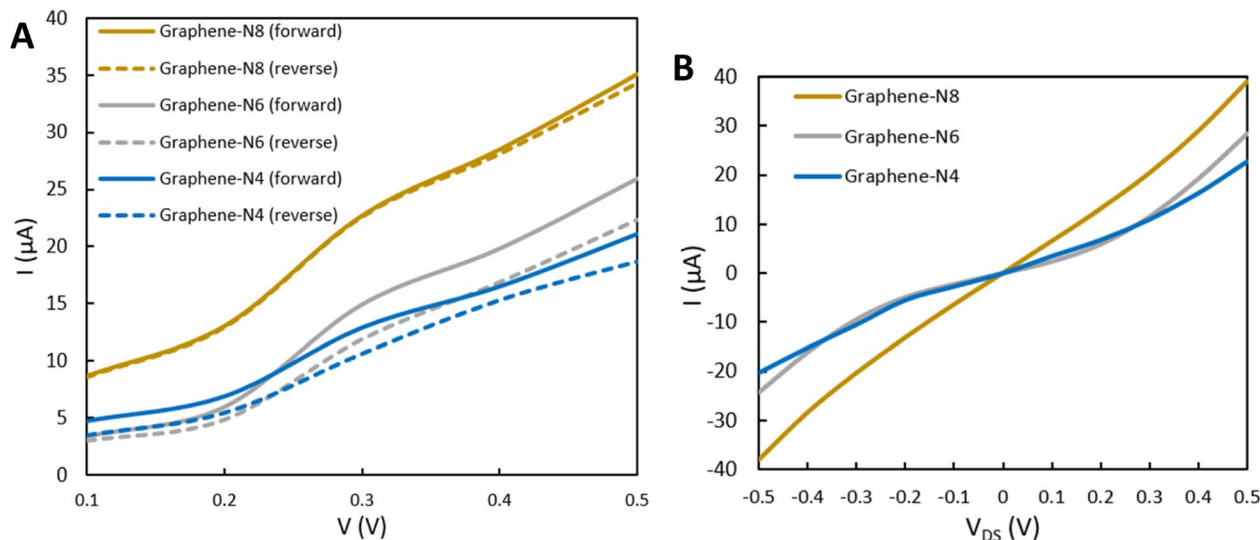


Fig. 4  $I(V)$  characteristics of Graphene-N8, Graphene-N6, and Graphene-N4 diodes without applying a gate voltage (A) and with applying a gate voltage at  $V_g = 20$  V and  $\epsilon = 3.9$  (B).  $V_{DS}$  refers to the voltage from drain to source and N is the neck of the graphene.

Table 1  $I(V)$  characteristics of Graphene-N8, Graphene-N6, and Graphene-N4 in comparison with experimental measurements at voltages of  $\pm 0.5$  V and  $\pm 1$  V

1 V	-0.5 V	Device	0.5 V	-1 V
100 $\mu\text{A}$	41 $\mu\text{A}$	Graphene-N8	42 $\mu\text{A}$	99 $\mu\text{A}$
86 $\mu\text{A}$	29 $\mu\text{A}$	Graphene-N6	33 $\mu\text{A}$	84 $\mu\text{A}$
72 $\mu\text{A}$	22 $\mu\text{A}$	Graphene-N4	27 $\mu\text{A}$	60 $\mu\text{A}$
—	30 $\mu\text{A}$	Exp. <sup>20</sup>	35 $\mu\text{A}$	—

observe how an electric field passing from different  $\epsilon$  can affect the  $I(V)$  characteristic and transport behavior of the graphene diodes. Consistent with experiments,<sup>20,25,53</sup> Fig. 4(B) reveals asymmetric  $I(V)$  properties calculated for Graphene-N8, Graphene-N6, and Graphene-N4 devices with majority charge carriers of electrons and holes at  $V_g = 20$  V and  $\epsilon = 3.9$ . Inspection of Table 2 reveals that at higher voltages, Graphene-N8 with high current values of 177  $\mu\text{A}$  and 174  $\mu\text{A}$  slightly overestimates the experimental values of 155  $\mu\text{A}$  and 115  $\mu\text{A}$  at 1.5 V and -1.5 V, respectively, whereas Graphene-N6 gave us a very close current value of 153  $\mu\text{A}$  at voltage 1.5 V with good consistency between experiment and theory. Further, the  $I(V)$

Table 2 Current  $I(A)$  characteristics of Graphene-N8, Graphene-N6, and Graphene-N4 in comparison to experimental measurements and Monte Carlo simulations at lower voltages of  $\pm 0.5$  V and higher voltages of  $\pm 1.5$  V by applying  $V_g = 20$  V and  $\epsilon = 3.9$

-1.5 V	-0.5 V	Device	0.5 V	1.5 V
174 $\mu\text{A}$	38 $\mu\text{A}$	Graphene-N8	39 $\mu\text{A}$	177 $\mu\text{A}$
149 $\mu\text{A}$	24 $\mu\text{A}$	Graphene-N6	28 $\mu\text{A}$	153 $\mu\text{A}$
111 $\mu\text{A}$	20 $\mu\text{A}$	Graphene-N4	23 $\mu\text{A}$	126 $\mu\text{A}$
115 $\mu\text{A}$	33 $\mu\text{A}$	Exp. <sup>20</sup>	40 $\mu\text{A}$	155 $\mu\text{A}$
107 $\mu\text{A}$	40 $\mu\text{A}$	Monte Carlo Simulation <sup>52</sup>	50 $\mu\text{A}$	155 $\mu\text{A}$

characteristics of Graphene-N4 with 111  $\mu\text{A}$  at -1.5 V is in very good agreement with the experimental and theoretical values of 115  $\mu\text{A}$  and 107  $\mu\text{A}$ , respectively. The results reveal that at lower voltages a graphene device with neck width 8 nm showed greater similarity to experiments for the current values, whereas by increasing the bias those devices with shorter necks (Graphene-N6 and Graphene-N4) showed better agreement with measurements in forward and reverse directions of voltage, respectively.

### Asymmetry (A)

It is worth mentioning that efficient rectification requires a large forward-to-backward current ratio. This ratio is referred to as the “A ratio” of the diode and some other figures of merit (such as the responsivity) also depend on the A of the  $I(V)$  behaviour. More importantly, to confirm the effect of the geometry of graphene on the  $I(V)$  curves, as an important difference in the characteristics of geometrically asymmetric graphene diodes with respect to symmetric ones, we quantified the  $I(V)$  A ratio for different diodes.<sup>54</sup> To analyze the A property of the  $I(V)$  characteristics for different diodes, we considered the ratio of the current absolute value at positive (+V) and negative (-V) voltages using the formula asymmetry ratio =  $|I(+V)/I(-V)|$ . If  $A > 1$ , electron transport is dominant, whereas in the case when  $A < 1$ , hole transport is dominant. The data obtained from A are presented in Fig. 5, calculated from the  $I(V)$  characteristics of different AGDs under no gate voltage (NGV) and with gate voltage (WGV) conditions. As the results show in the NGV, Graphene-N4 with a smaller neck size achieved the greatest A of 1.39 at voltage  $|0.1$  V|, while Graphene-N6 and Graphene-N8 have their maximum A of 1.20 and 1.03 at higher voltages of  $|0.22$  V| and  $|0.4$  V|, respectively. As shown in Fig. 5, A in lower voltages indicates higher values while by raising the voltage we observed lower amounts of A and some graph convergence.



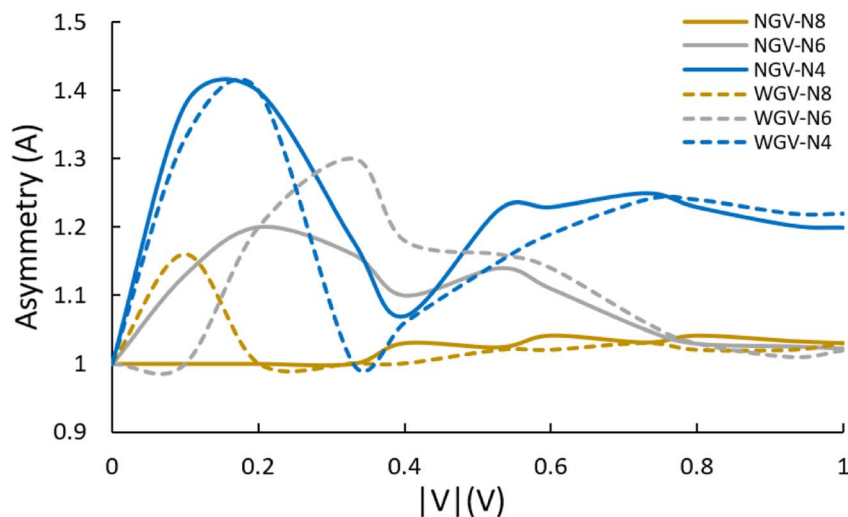


Fig. 5 Calculated asymmetry ( $A$ ) values of graphene devices with different necks of Graphene-N8, Graphene-N6, Graphene-N4 with no gate voltage (NGV (solid lines)) and with gate voltage (WGV (dashed lines)) of 20 V.

By applying a gate voltage (WGV) of +20 V, the  $A$  of Graphene-N4 showed a slight increase to 1.40 (Fig. 5, blue dashed line) that was calculated for  $|V| = 0.2$  V. However, the corresponding  $A$  for Graphene-N6 and Graphene-N8 were raised to 1.30 and 1.16 at  $|V| = 0.3$  V and  $|V| = 0.1$  V with respect to the NGV system. The results of the AR trend in this study are very consistent with the Monte Carlo simulations in Zhu *et al.*<sup>20</sup> and experimental measurements of Passi *et al.*<sup>20,55</sup> in which the smallest neck device yields a higher  $A$ .

### Transmission spectra ( $T$ )

Modeling of  $T$  spectra was performed to compare the ballistic efficiencies of geometric graphene devices as a function of optical properties, quantitatively and qualitatively. For a 2D graphene structure, the  $T$  spectrum in principle represents just a sum over available modes in the band structure at each energy. As can be seen in Fig. 6, we estimated  $T$  spectra for

different geometrical graphene devices at bias energies ranging from  $-2$  to  $+2$  eV using a Dirac self-energy calculator, while we fixed the difference in chemical potential between the right and left electrodes at 5 eV. The simulation results from Fig. 6 and Table 3 show that the maximum value of  $T$  increases with a decrease in the neck of graphene in various devices, among which Graphene-N4 shows at higher value of  $T = 6.72$  in the energy range 1.30. This simulation indicates that the overall trend of  $T$  is in agreement with the  $A$  properties of graphene devices, as confirmed by some previous studies.<sup>32,56</sup> It is worth noting that the harvesting efficiency of antennas has been discussed by several authors in recent years. While Midrio *et al.*<sup>57</sup> referred to receiving efficiency in antennas, some previously published papers focused on transmission and reflection efficiencies. Recently, in a study by Ma *et al.*<sup>58</sup> the optical efficiency of nano-antenna systems for solar energy harvesting was considered. The maximum upper bounds were found to be in the order of 60–70%. Moreover, Zhao *et al.*,<sup>59</sup> investigated the

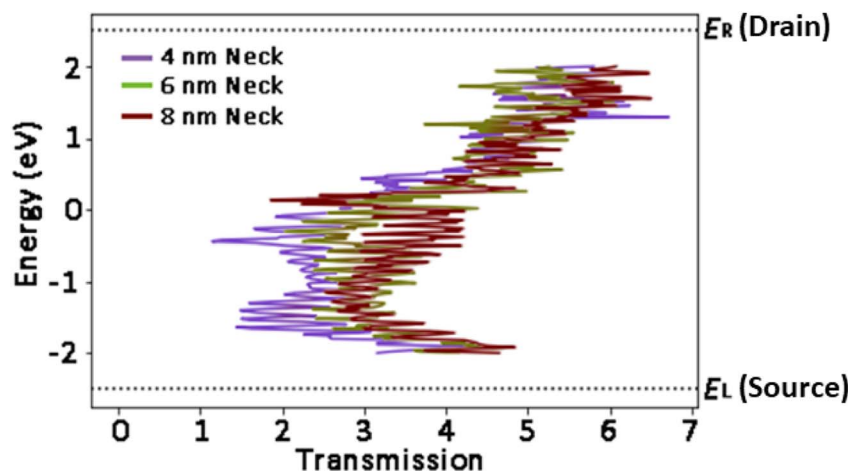


Fig. 6 Simulated transmission spectra of Graphene-N8, Graphene-N6, and Graphene-N4 devices.



**Table 3** Maximum transmittance values in corresponding energy ranges of graphene diodes

Device	Energy (eV)	Max transmittance
Graphene-N8	1.56	6.44
Graphene-N6	1.52	6.16
Graphene-N4	1.30	6.72

collection of solar energy by a broad-band antenna to overcome the low efficiency of a solar rectenna based on conventional nano-antennas. The antenna impedance, radiation, polarization and effective area are all considered in efficiency calculations using the finite integral technique. The wavelength range investigated is 300–3000 nm, which corresponds to more than 98% of solar radiation energy. Recently Mencarelli *et al.*,<sup>60</sup> using Monte Carlo simulations, studied the charge transmittivity of geometric diodes based on graphene patterned with spatial asymmetry for a voltage difference of 1.76 V. With fixed external voltage, charge direction is not relevant for transmittivity, owing to reciprocity. However, when a voltage with the opposite sign is considered, the transmittivity changes due to superposition between voltage and asymmetric geometry, so that  $I(V)$  asymmetry follows. Clearly, different methodologies from atomistic DFTB to Monte Carlo and experiments cannot calculate the same  $T$  property for geometrical graphene diodes; however, each of them can satisfy effective implementation of the concept of a geometric diode for harvesting applications.

## Conclusions

In this study, geometric graphene diodes were investigated from the atomic perspective using the first principles DFTB-NEGF method. To this end, three different AGDs consisting of Graphene-N8, Graphene-N6, and Graphene-N4, in the shape of ballistic diodes were modelled with different neck widths. The atomic behavior of the graphene devices was explored through  $I(V)$  characteristics,  $A$  properties and  $T$  spectra. Whereas all simulated AGDs exhibited asymmetric  $I(V)$  characteristics in excellent agreement with experimental measurements and Monte Carlo simulation, Graphene-N8 delivers the highest current values at lower and higher voltages under no gate voltage (NGV) and with gate voltage (WGV) conditions. By applying a gate voltage of +20 V, Graphene-N6 and Graphene-N4 showed better agreement with the experimental data for forward and reverse directions of voltage, respectively. The best  $A$  was found for Graphene-N4 with a value of 1.40 at a corresponding voltage of  $|V| = 0.2$  with maximum  $T = 6.72$  in an energy range of 1.30 eV. This computational study for optimizing geometrical graphene devices offers a new insight into the development of energy harvesting devices. Furthermore, the accuracy demonstrated by the atomistic approach allowed us to highlight in detail phenomena that could be difficult to interpret with a purely experimental approach, thus suggesting points of focus for the production of promising graphene rectifiers, enabling the realization of optical rectennas.

## Author contributions

Conceptualization, E. M., E. L. and P. S.; methodology, E. M. and E. L.; validation, E. M., E. L., P. S., L. P. and D. M.; investigation, E. M.; data curation, E. M.; writing—original draft preparation, E. M.; writing—review and editing, E. M., E. L., E. P., P. S., L. P., A. H., and D. M.; visualization, E. M.; supervision, P. S.; project administration, E. M., E. L., E. P., P. S., A. H., L. P. and D. M. All authors have read and agreed to the published version of the manuscript.

## Conflicts of interest

There are no conflicts to declare.

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