



Cite this: *Nanoscale Adv.*, 2024, 6, 268

# Growing $sp^2$ materials on transition metals: calculated atomic adsorption energies of hydrogen, boron, carbon, nitrogen, and oxygen atoms, $C_2$ and BN dimers, $C_6$ and $(BN)_3$ hexamers, graphene and h-BN with and without atomic vacancies†

Ari Paavo Seitsonen \*<sup>a</sup> and Thomas Greber \*<sup>b</sup>

The growth of graphene and hexagonal boron nitride on hot transition metal surfaces involves the adsorption of precursor molecules, and their dissociation and assembly into two-dimensional honeycomb lattices. In a recent account it was found that h-BN may be distilled on a rhodium metal surface, which yields higher quality h-BN [Cun *et al.*, *ACS Nano*, 2020, 15, 1351]. In this context, we calculated in a systematic approach the adsorption energies and sites of hydrogen, boron, carbon, nitrogen, and oxygen atoms and from the site dependence the activation energy for diffusion. Existing computed values of the solvation energy into the bulk were compared to the present ones with our calculation scheme and found to be in good agreement. For the distinction of different systems we introduce the concepts of epiphilicity and epiphobicity. The adsorption energies and stabilities of the  $C_2$  and BN dimers, the  $C_6$  and  $(BN)_3$  ring-hexamers and the graphene and h-BN monolayers allow the prediction of the performance of different substrates in chemical vapor deposition (CVD) processes for the growth of graphene and h-BN. Finally, vacancy creation energies were calculated as a criterion for the stability of graphene and h-BN on metallic substrates.

Received 29th June 2023  
Accepted 31st October 2023

DOI: 10.1039/d3na00472d

rsc.li/nanoscale-advances

## 1. Background

The growth of two-dimensional (2D) materials on transition metals is a viable way for obtaining wafer-scale materials as they are needed in an industrial context.<sup>1,2</sup> Many production schemes rely on chemical vapor deposition (CVD) processes, where precursor molecules are exposed to a hot surface. In order to obtain a material with the highest quality the processes have to be controlled and understood at the atomic level. In detail, the process involves adsorption, diffusion, and new bond formation on a surface. The dissolution or solvation of atomic constituents into the 3D bulk opens perspectives for new strategies,<sup>3</sup> while also further complicating the processes. Because growth is a kinetic process, it may be guided by catalysts that shall produce the desired material. The transition metal substrates play the role of catalysts, *i.e.* they promote bond breaking and formation. It is a formidable task to understand and develop a strategy for the

rational design of the best catalyst. The strategy for getting the best material must involve experiment and theory. While experiments demonstrate the state of the art, a theory makes predictions and sets limits for ideal materials. For example, with a theory, it is possible to compare “perfect” layers, without defects on different metals and to judge their stability that is related to the lowest defect formation energy.<sup>4</sup>

Here we present calculated key numbers of boron, nitrogen and carbon on twelve different close packed transition metal surfaces. A main motivation was to add the values of boron to the literature, and to present a consistent dataset with H, C, N and O, which have been calculated for example for the case of Rh(111) before.<sup>5</sup> Furthermore, the binding energies of the  $C_2$  and BN dimers as the first agglomerates are shown, together with the adsorption energies of single layers of graphene and h-BN. The present account will also enable the cross-check of the list of existing experimental work of CVD graphene (gr)<sup>6,7</sup> or hexagonal boron nitride (h-BN).<sup>8</sup> It also makes predictions for substrates such as osmium that have not been addressed so far. In particular, it is useful for a better understanding of 2D distillation, a concept that has recently been presented for h-BN,<sup>9</sup> or for the quality assessment of h-BN by measuring the pyrolysis temperature on a given substrate.<sup>10</sup>

<sup>a</sup>Département de Chimie, École Normale Supérieure, F-75005 Paris, France. E-mail: ari.p.seitsonen@iki.fi

<sup>b</sup>Physik-Institut, Universität Zürich, CH-8057 Zürich, Switzerland. E-mail: greber@physik.uzh.ch; Fax: +41 44635 5704; Tel: +4144 635 5744

† Electronic supplementary information (ESI) available. See DOI: <https://doi.org/10.1039/d3na00472d>



## 2. Methods

We employ density functional theory<sup>11</sup> in our simulations of solvation and adsorption of atoms, small molecules and the monolayers of the relaxed system on the given (111) or (0001) close packed surfaces. In the case of Co we report here the values at the surface Co(0001); the corresponding values on the surface of the high-temperature phase Co(111) are given in the ESI.†

As atomic sites we distinguish octahedral (oct) and tetrahedral (tet) sites in the bulk, face centered cubic (fcc), hexagonally close packed (hcp), on top (top) and bridge (bri) sites. Below hcp hollow sites a substrate atom is found in the second substrate layer, and below fcc hollow sites no atom is found in the second substrate layer. On top sites are on top of the atoms in the first substrate layer. Bridge sites are located laterally between the fcc and the hcp sites. Fig. 1 demonstrates the labelling of the investigated atomic sites in the bulk and on the surface, and the nomenclature of the calculated structures of different agglomerates studied with an example of each type, from which other configurations may be inferred. In the case of the vacancies in the (1 × 1) layers the defect site AB indicates the registry of the type of atoms A and B, with the vacancy of type A and the site of species B with the lowest energy  $E_{\text{vac}}^{\text{A}}$  in the strained layer. The value of  $\Delta E_{\text{vac}}^{\text{A}}$  is the energy difference between the strained and the free standing layers which have the highest vacancy defect energies.

We applied a van der Waals functional<sup>12</sup> as the approximation of the exchange–correlation term in the Kohn–Sham equations.

We used a 4 × 4 × 4 super-cell of simple cubic shape, yielding 256 atoms (257 with the solvated atom) in the calculations of solvation into the bulk, and either (1 × 1) – commensurate monolayer –, (3 × 3) – adsorbed single atoms and dimers, and vacancies – or (5 × 5) – hexamers – laterally in

the calculations of the adsorption energies. Five layers of the substrate were used, with the two top most layers relaxed, in the slab geometry. The lateral size was set by the computer resources, as the computations were repeated on 12 different surfaces plus the Co(111), with several adsorption configurations on each of them.

Here we collect the definitions of the quantities that we used to analyse the energetics. We denote the total energies with the sub-script t, and all the other quantities are energy differences.

The solvation energy  $E_{\text{sol}}^{\text{A}}$  was calculated from

$$E_{\text{sol}}^{\text{A}} = \min_{\text{S}} E_{\text{t}}^{\text{A@bulk}} - (E_{\text{t}}^{\text{A}} + E_{\text{t}}^{\text{bulk}}), \quad (1)$$

where  $E_{\text{t}}^{\text{A@bulk}}$  is the total energy of one solute A dissolved in the bulk of the substance, and the minimum is taken over the energies on the different sites S of either the octahedral or the tetrahedral site. We note that our choice of using the total energy of the atom A in a vacuum,  $E_{\text{t}}^{\text{A}}$ , as the reference corresponds to the choice of this energy as the value of the chemical potential  $\mu$ , whereas in ref. 13 the energies were referred to as the reference states of the respective element, for example  $\mu = E_{\text{t}}(\text{N}_2)/2$ .  $E_{\text{t}}^{\text{bulk}}$  is the total energy of the bulk sample.

The adsorption energy  $E_{\text{ads}}^{\text{A}}$  of an atom A on a surface was defined as

$$E_{\text{ads}}^{\text{A}} = \min_{\text{S}} E_{\text{t}}^{\text{A@surf}} - (E_{\text{t}}^{\text{A}} + E_{\text{t}}^{\text{surf}}), \quad (2)$$

where  $E_{\text{t}}^{\text{A@surf}}$  and  $E_{\text{t}}^{\text{surf}}$  are, respectively, the total energies of the surface with and without the adsorbate A. The minimum is taken as the lowest energy over the four high-symmetry adsorption sites fcc, hcp, top and bri(dge).

The diffusion barrier  $E_{\text{diff}}^{\text{A}}$  of adsorbate A was calculated from

$$E_{\text{diff}}^{\text{A}} = \min_{\text{3rd}} E_{\text{ads}}^{\text{A}} - \min_{\text{S}} E_{\text{ads}}^{\text{A}}, \quad (3)$$

where  $\min_{\text{3rd}} E_{\text{ads}}^{\text{A}}$  is the third lowest adsorption energy of the four calculated adsorption sites, as it can be shown that this corresponds to the lowest energy needed to diffuse A from its preferred adsorption site into the next cell on the hexagonal surfaces.

The adsorption energy of the dimer,  $E_{\text{ads}}^{\text{dim}}$ , was calculated from

$$E_{\text{ads}}^{\text{dim}} = \min_{\text{S}} E_{\text{t}}^{\text{dim@surf}} - (E_{\text{t}}^{\text{dim}} + E_{\text{t}}^{\text{surf}}), \quad (4)$$

where the minimum was taken over the adsorption of two atoms initially toward the two three-fold hollow sites fcc and hcp, as the  $E_{\text{ads}}^{\text{A}}$  is clearly the strongest there, so we can exclude the top site. Thus in the case of the dimer BN we have the two configurations  $B_{\text{hcp}}N_{\text{fcc}}$  and  $B_{\text{fcc}}N_{\text{hcp}}$  to select from, and only one in the case of the  $C_2$ .

The bond dissociation energy of the dimer on the surface,  $E_{\text{diss}}^{\text{AB}}$ , was determined from

$$E_{\text{diss}}^{\text{AB}} = (E_{\text{ads}}^{\text{A}} + E_{\text{ads}}^{\text{B}}) - (E_{\text{ads}}^{\text{dim}} - E_{\text{diss}}^{\text{dim}}), \quad (5)$$

with  $E_{\text{diss}}^{\text{dim}}$  being the dissociation energy of the dimer in the gas phase. We note that  $E_{\text{diss}}^{\text{dim}} > 0$ , and  $E_{\text{diss}}^{\text{dim}} + E_{\text{ass}}^{\text{dim}} = 0$ , where  $E_{\text{ass}}^{\text{dim}}$  is the dimer association energy.

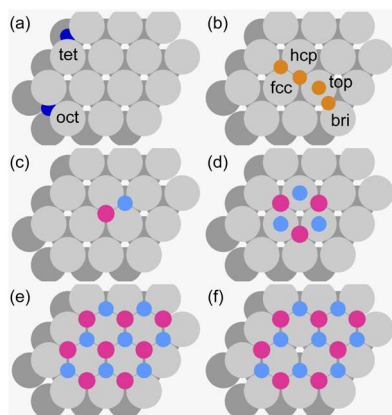


Fig. 1 Nomenclature of the atomic sites and sketches of the investigated structures. Two stacked hexagonally close packed layers are shown, the first layer in light and the second layer in dark grey. (a) Bulk octahedral (oct) and tetrahedral (tet) interstitial sites (dark blue) as they are encountered between two hexagonally close packed atomic layers. (b) Surface face centred cubic (fcc), hexagonally close packed (hcp), on top (top) and bridge (bri) sites (dark yellow). (c) Example of a dimer, at the registry (B, N) = (fcc, hcp) (B pink, N blue). (d) Example of a ring-hexamer, (B, N) = (hcp, top). (e) A (1 × 1) layer at the registry (B, N) = (fcc, hcp). (f) Example of a B vacancy defect (BN) = (fcc, hcp).



The adsorption energies of the ring-hexamers,  $E_{\text{ads}}^{\text{hex}}$ , were calculated similarly from

$$E_{\text{ads}}^{\text{hex}} = \min_S E_{\text{t}}^{\text{hex@surf}} - (E_{\text{t}}^{\text{hex}} + E_{\text{t}}^{\text{surf}}), \quad (6)$$

and the single bond dissociation energies of the ring-hexamers on the surface,  $E_{6\text{bo}}^{\text{hex}}$ , from

$$E_{6\text{bo}}^{\text{hex}} = ((3E_{\text{ads}}^{\text{A}} + 3E_{\text{ads}}^{\text{B}}) - (E_{\text{ads}}^{\text{hex}} + E_{\text{diss}}^{\text{hex}}))/6, \quad (7)$$

where the sites S range from fcc, hcp to top, yielding three different arrangements of the adsorption sites in the case of  $C_6$  and six in the case of  $(\text{BN})_3$ .

The adsorption energy of strained graphene or hexagonal boron nitride,  $E_{\text{ads}}^{2\text{D}^*}$ , was determined from

$$E_{\text{ads}}^{2\text{D}^*} = \min_S E_{\text{t}}^{2\text{D}^*@\text{surf}} - (E_{\text{t}}^{2\text{D}^*} + E_{\text{t}}^{\text{surf}}) \quad (8)$$

The super-script \* is used to denote that the system is under strain due to the use of the same lattice constant on the graphene and h-BN as the lateral lattice constant of the underlying substrate. We again allowed the sites S among the three-fold symmetric fcc, hcp and top, yielding three and six different site arrangements, respectively, in the case of graphene and h-BN.

The effective  $sp^2$  bond energy,  $E_{\text{sp}^2}^{2\text{D}^*}$ , was defined as

$$E_{\text{sp}^2}^{2\text{D}^*} = ((E_{\text{ads}}^{\text{A}} + E_{\text{ads}}^{\text{B}}) - (E_{\text{ads}}^{2\text{D}^*} + E_{\text{diss}}^{2\text{D}^*}))/3, \quad (9)$$

where the dissociation energy in the gas phase  $E_{\text{diss}}^{2\text{D}^*}$  was calculated at the value of the lateral lattice constant of the underlying substrate even if the substrate has been removed. As a comparison we give the value also in the case of the free-standing 2D layer, where the value corresponds to the negative of the cohesive energy of the monolayer.

The formation energy of a vacancy of an atom of type A,  $E_{\text{vac}}^{\text{A}^*}$ , was calculated from

$$E_{\text{vac}}^{\text{A}^*} = (E_{\text{t,vac}}^{(2\text{D}^*-\text{A})@\text{surf}} + E_{\text{t}}^{\text{A}}) - E_{\text{t}}^{2\text{D}^*@\text{surf}} \quad (10)$$

The registry of the monolayer was taken as the lowest-energy one, because from test calculations we saw that this requires the lowest amount of energy to create the vacancy, and it is in any case the preferred configuration without the defect. In the case of graphene the C atom with the lower  $E_{\text{vac}}^{\text{C}}$  was chosen for the analysis.

The formation of a mono-vacancy in the free standing 2D layer was defined as

$$E_{\text{vac}}^{\text{A}^*}(\text{free}) = (E_{\text{t,vac}}^{(2\text{D}^*-\text{A})} + E_{\text{t}}^{\text{A}}) - E_{\text{t}}^{2\text{D}^*} \quad (11)$$

and the energy lowering for the vacancy creation on the substrates,  $\Delta E_{\text{vac}}^{\text{A}^*}$ , as

$$\Delta E_{\text{vac}}^{\text{A}^*} = E_{\text{vac}}^{\text{A}^*} - E_{\text{vac}}^{\text{A}^*}(\text{free}). \quad (12)$$

### 3. Results and discussion

Before presenting the results of the calculations the concepts epiphilicity and epiphobicity are outlined. They are important quantities in order to predict the behaviour of a given metal substrate for the growth of 2D materials.

#### 3.1. Epiphilic vs. epiphobic

For the prediction of the growth scenarios it is essential to know whether the reaction proceeds on the surface alone, or whether educts may dissolve or solvate into the bulk, and to judge the segregation behaviour. As we learn from effective medium theory,<sup>14,15</sup> the dissolution into the bulk must not be the lowest energy state, as there are systems in which the electron density is too high in the bulk, and where an atom finds the optimal electron density rather on a surface, between the bulk and the vacuum. This we call an epiphilic atom/substrate system. The epiphilic and its counterpart, the epiphobic scenario, are depicted in Fig. 2.

In the following we will recall the solvation energies of atoms, before the energies of atoms and their agglomerates on surfaces are described.

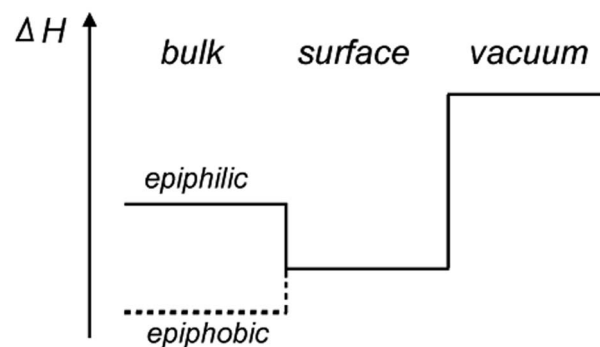


Fig. 2 Scheme of the enthalpies  $\Delta H$  involved in gas–solid reactions. In the epiphilic case the reactant has the lowest energy at the surface, while for the epiphobic case, the dissolution into the bulk is energetically favourable.

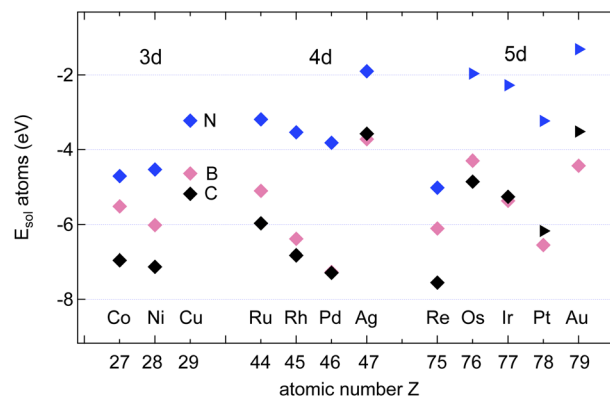


Fig. 3 Calculated solvation energies  $E_{\text{sol}}^{\text{A}}$ . A = B (pink), N (blue) and C (black) into the bulk of 12 different transition metals as a function of their atomic numbers. The symbols depict the octahedral  $\diamond$  or tetrahedral  $\triangleright$  sites. Data adapted from ref. 13.



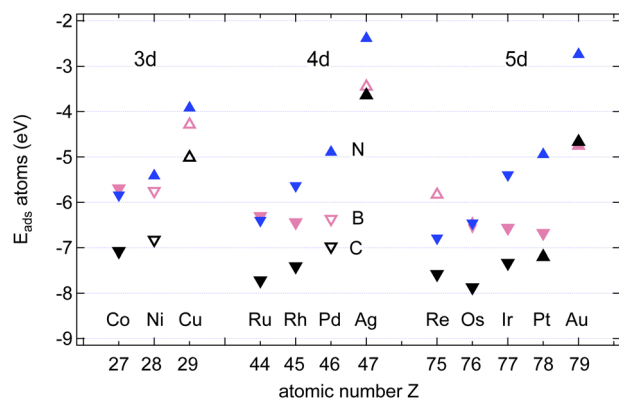


Fig. 4 The strongest adsorption energies  $E_{\text{ads}}^A$ ,  $A = \text{B}$  (pink),  $\text{C}$  (black) and  $\text{N}$  (blue), on transition metal surfaces. The symbols depict the preferred adsorption site:  $\Delta = \text{fcc}$ ;  $\nabla = \text{hcp}$ ;  $\diamond = \text{bridge}$ . Full symbols are used in epiphilic and open symbols in epiphobic cases.

### 3.2. Atom solvation

The calculated solvation energies  $E_{\text{sol}}^A$  of  $\text{B}$ ,  $\text{C}$  and  $\text{N}$  in three transition metals are in good agreement with the previously published results on dissolution energies into the bulk.<sup>13</sup> Fig. 3 shows the adopted dissolution energies with reference to the corresponding atoms in a vacuum.  $\text{N}$  has the lowest dissolution energy in all the investigated materials. Except for  $\text{Ir}$ ,  $\text{Pt}$  and  $\text{Au}$ ,  $\text{C}$  has the highest dissolution energy.  $\text{B}$  dissolution supersedes the one of  $\text{N}$  in all the investigated metals, and the dissolution energy in  $\text{Pd}$  is particularly large.

### 3.3. Atom adsorption

Fig. 4 shows the calculated adsorption energies of  $\text{B}$ ,  $\text{C}$  and  $\text{N}$  atoms on 12 investigated 3d, 4d and 5d transition metal surfaces; they are also listed in Table 1. It is seen that the  $E_{\text{ads}}^{\text{C}}$  supersedes that of  $\text{B}$  and  $\text{N}$ , where only in the case of  $\text{Au}(111)$  does  $\text{B}$  bind more strongly than  $\text{C}$ , namely by 100 meV, or 2%. This is an important hint that  $\text{C}$  contamination should be avoided if pure h-BN shall be grown at high temperatures.<sup>10</sup>

The adsorption of atoms is weakest on the coinage metals  $\text{Ag}$ ,  $\text{Cu}$ , and  $\text{Au}$  and it increases steadily with the number of holes in the d-bands in the case of  $\text{N}$ .

For the growth of  $\text{BN}$  we find, except on  $\text{Co}$ ,  $\text{Ru}$ , and  $\text{Re}$ , that  $\text{B}$  binds stronger than  $\text{N}$ . In contrast to  $\text{N}$ , the binding of  $\text{B}$  does not increase steadily with the number of the d-holes but it is the strongest on  $\text{Pt}$ . The almost degenerate adsorption energies for  $\text{B}$  and  $\text{N}$  on  $\text{Co}$ ,  $\text{Ru}$  and  $\text{Os}$  are of interest if the stoichiometry of the precursor molecules shall be maintained during the growth process. The dissolution into the bulk has, however, to be considered, even if  $\text{Ru}$ , and  $\text{Os}$  are epiphilic for both  $\text{B}$  and  $\text{N}$ . For the growth of h-BN without the presence of  $\text{C}$  we expect on most substrates  $\text{B}$  enrichment. On  $\text{Cu}(111)$  at a temperature of 1200 K an equilibrium off stoichiometry factor  $\gamma_{\text{EOSF}} = \exp[-(E_{\text{ads}}^{\text{N}} - E_{\text{ads}}^{\text{B}})/(k_{\text{B}}T)]$  of 46 is found, which predicts a significant  $\text{B}$  enrichment. While  $\text{N}$  is epiphilic on all the substrates, with  $E_{\text{ads}}^{\text{N}}/E_{\text{sol}}^{\text{N}}$  between 1.2 ( $\text{Ni}$ ) and 3.3 ( $\text{Os}$ ),  $\text{B}$  may be both, either epiphilic or epiphobic, with  $E_{\text{ads}}^{\text{B}}/E_{\text{sol}}^{\text{B}}$  between 3.3 ( $\text{Os}$ ) and 0.88 ( $\text{Pd}$ ).

Table 1 Atomic adsorption energies  $E_{\text{ads}}^A$  and diffusion barriers  $E_{\text{diff}}^A$ ,  $A = \text{H}$ ,  $\text{B}$ ,  $\text{C}$ ,  $\text{N}$  and  $\text{O}$ , on twelve hexagonally close packed transition metal surfaces at the preferred adsorption sites among fcc, hcp, top and bridge. The lowest solvation energies  $E_{\text{sol}}^A$ ,  $A = \text{B}$ ,  $\text{C}$  and  $\text{N}$ , in the octahedral or tetrahedral sites were inferred from ref. 13. All energies are given in eV

Adsorbate	Substrate	$E_{\text{sol}}^A$	Site	$E_{\text{ads}}^A$	Site	$E_{\text{diff}}^A$	
H	Co			-2.99	fcc	0.16	
	Ni			-2.98	fcc	0.14	
	Cu			-2.69	fcc, hcp	0.13	
	Ru			-3.04	fcc	0.14	
	Rh			-2.98	fcc	0.11	
	Pd			-2.99	fcc	0.13	
	Ag			-2.28	fcc, hcp	0.11	
	Re			-3.10	fcc	0.19	
	Os			-2.92	fcc	0.09	
	Ir			-2.94	top	0.11	
	Pt			-2.93	top	0.06	
	Au			-2.32	fcc	0.05	
	B	Co	-5.51	oct	-5.69	hcp	0.16
		Ni	-6.02	oct	-5.75	hcp	0.23
Cu		-4.63	oct	-4.29	fcc	0.03	
Ru		-5.10	oct	-6.30	hcp	0.50	
Rh		-6.39	oct	-6.44	hcp	0.45	
Pd		-7.27	oct	-6.36	hcp	0.39	
Ag		-3.72	oct	-3.45	fcc	0.12	
Re		-6.11	oct	-5.83	fcc	0.20	
Os		-4.30	oct	-6.50	hcp	0.65	
Ir		-5.37	oct	-6.56	hcp	0.55	
Pt		-6.55	oct	-6.68	hcp	0.43	
Au		-4.42	oct	-4.75	fcc	0.27	
C		Co	-6.96	oct	-7.07	hcp	0.35
		Ni	-7.13	oct	-6.83	hcp	0.38
	Cu	-5.18	oct	-5.01	fcc	0.10	
	Ru	-5.97	oct	-7.72	hcp	0.77	
	Rh	-6.82	oct	-7.41	hcp	0.64	
	Pd	-7.29	oct	-6.97	hcp	0.43	
	Ag	-3.58	oct	-3.64	fcc	0.23	
	Re	-7.55	oct	-7.58	hcp	0.45	
	Os	-4.85	oct	-7.87	hcp	0.91	
	Ir	-5.26	oct	-7.33	hcp	0.71	
	Pt	-6.17	tet	-7.20	fcc	0.34	
	Au	-3.51	tet	-4.67	fcc	0.26	
	N	Co	-4.70	oct	-5.84	hcp	0.52
		Ni	-4.53	oct	-5.41	fcc	0.50
Cu		-3.22	oct	-3.92	fcc	0.28	
Ru		-3.19	oct	-6.40	hcp	0.89	
Rh		-3.54	oct	-5.63	hcp	0.67	
Pd		-3.82	oct	-4.89	fcc	0.43	
Ag		-1.90	oct	-2.39	fcc	0.28	
Re		-5.02	oct	-6.79	hcp	0.74	
Os		-1.96	tet	-6.45	hcp	1.05	
Ir		-2.27	tet	-5.39	hcp	0.68	
Pt		-3.23	tet	-4.95	fcc	0.32	
Au		-1.31	tet	-2.74	fcc	0.28	
O		Co			-5.84	hcp	0.38
		Ni			-5.49	fcc	0.50
	Cu			-4.87	fcc	0.33	
	Ru			-6.15	hcp	0.69	
	Rh			-5.25	fcc	0.50	
	Pd			-4.51	fcc	0.43	
	Ag			-3.72	fcc	0.29	
	Re			-6.86	hcp	0.86	
	Os			-6.02	hcp	0.77	
	Ir			-4.93	fcc	0.45	



Table 1 (Contd.)

Adsorbate	Substrate	$E_{\text{sol}}^{\text{A}}$	Site	$E_{\text{ads}}^{\text{A}}$	Site	$E_{\text{diff}}^{\text{A}}$
	Pt			-4.39	fcc	0.39
	Au			-3.31	fcc	0.26

In the growth of homoatomic graphene, with a CC basis, the substrate with the largest relative epiphilicity  $E_{\text{ads}}^{\text{C}}/E_{\text{sol}}^{\text{C}}$  of 1.6 is Au, and that with the highest epiphobicity  $E_{\text{ads}}^{\text{C}}/E_{\text{sol}}^{\text{C}}$  of 0.96 is Pd.

### 3.4. Surface diffusion of the atoms

The data in Table S2 in the ESI† provide the site-dependence of the adsorption energies and thus allow the determination of an activation energy or energy barrier for diffusion. Four different sites in the unit cell were calculated. When the adsorbate is most stable on a hollow adsorption site, the bridge site is assumed to be the saddle point upon diffusion, and the energy barrier of diffusion  $E_{\text{diff}}^{\text{A}}$  is defined as the energy difference between the adsorbate on the bridge site and the preferred hollow site. When the preferred adsorption site is the bridge site, the diffusion barrier is defined as the energy difference between the less bound hollow site and the bridge site. These instances correspond to taking the energy difference between the energy at the third-lowest of the four sites and at the strongest adsorption site (Fig. 5).

Except for the coinage metals on most of the investigated surfaces the adsorption site with the highest binding energy is the hcp site, where in the second substrate layer an atom is located.

The results may be rationalised with the Evans–Polanyi relation stating that  $E_{\text{diff}}^{\text{A}}$  is smaller and proportional to  $E_{\text{ads}}^{\text{A}}$ .<sup>16</sup> The proportionality factors are in the order of 10%, though they depend on the adsorbate: From the data in Table 1 follows  $E_{\text{diff}}/E_{\text{ads}}$  of about 6, 7 and 11% for B, C and N, respectively, on the 12 substrates. In the specific example of B or N on Ni(111) we find  $E_{\text{diff}}^{\text{B/Ni}} = E_{\text{ads}}^{\text{bri}} - E_{\text{ads}}^{\text{hcp}} = 0.21$  eV or 4% of the adsorption energy  $E_{\text{ads}}$  and  $E_{\text{diff}}^{\text{N/Ni}} = E_{\text{ads}}^{\text{bri}} - E_{\text{ads}}^{\text{fcc}} = 0.50$  eV, or 9%, respectively. This predicts that B diffuses faster than N. The lower absolute and relative B diffusion barriers appear as a general trend on all the investigated surfaces. On Cu, with  $E_{\text{diff}}^{\text{B}} = 26$  meV, the diffusion of

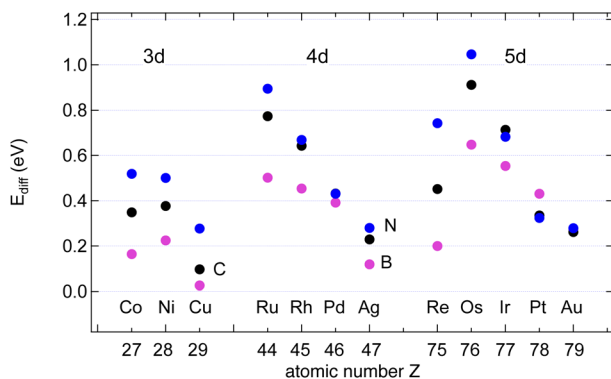


Fig. 5 Diffusion barriers  $E_{\text{diff}}^{\text{A}}$ , A = B (pink), C (black) and N (blue), on the studied surfaces.

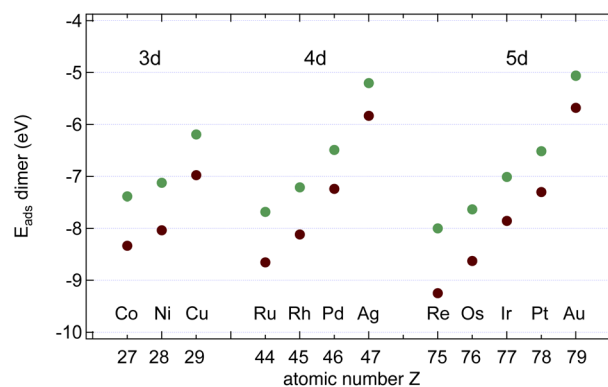


Fig. 6 Dimer adsorption energies  $E_{\text{ads}}^{\text{dim}}$ , dim = CC (brown) or BN (green), with respect to the dimers in the gas phase.

B appears to be particularly fast. Notably, this diffusion barrier of B is lower than that of H on all investigated surfaces. In general also C diffuses slower than B, but faster than N.

### 3.5. C<sub>2</sub> and BN dimers

In the next step, we calculated C<sub>2</sub> and BN dimers on the surfaces, and the results are shown in Fig. 6 and Table 2. On all the investigated substrates BN preferentially binds with the B closer to the metal than N, and C<sub>2</sub> binds stronger than the BN dimer.

As can be seen from a comparison between the data in Tables 1 and 2 BN dimers binds stronger to the substrate than a N atom, and only on Pd and Pt B binds a little bit stronger than BN. For C<sub>2</sub> there is no exception to the rule that the dimer binds stronger than one monomer.

The data suggest that all investigated surfaces greatly reduce the C<sub>2</sub> and the BN dissociation energy from that in a vacuum (6.00 and 4.62 eV respectively). On Ru, Rh, Pd, Os, Ir and Pt  $E_{\text{diss}}^{\text{CC}}$  is even negative, *i.e.* on these surfaces the dissociated state is more stable than the dimer state. The sign of the C<sub>2</sub> dissociation energies on Cu<sup>17</sup> and Ir<sup>18</sup> has been reported in the

Table 2 C<sub>2</sub> and BN dimer adsorption and dissociation energies and the lowest adsorption sites on the studied surfaces. The preferred adsorption site is B<sub>hcp</sub>N<sub>fcc</sub> except on Re(0001), where the site is B<sub>fcc</sub>N<sub>hcp</sub>. Energies are in (eV per dimer)

Substrate	$E_{\text{ads}}^{\text{CC}}$	$E_{\text{diss}}^{\text{CC}}$	Site	$E_{\text{ads}}^{\text{BN}}$	$E_{\text{diss}}^{\text{BN}}$	Site
Gas phase	—	6.00	—	—	4.62	—
Co	-8.34	0.19	fcc, hcp	-7.39	0.48	hcp, fcc
Ni	-8.03	0.38	fcc, hcp	-7.12	0.64	hcp, fcc
Cu	-6.98	2.96	fcc, hcp	-6.19	2.61	hcp, fcc
Ru	-8.66	-0.77	fcc, hcp	-7.68	-0.40	hcp, fcc
Rh	-8.12	-0.70	fcc, hcp	-7.21	-0.24	hcp, fcc
Pd	-7.24	-0.71	fcc, hcp	-6.49	-0.15	hcp, fcc
Ag	-5.83	4.56	fcc, hcp	-5.20	3.98	hcp, fcc
Re	-9.25	0.10	fcc, hcp	-8.27	0.28	fcc, hcp
Os	-8.63	-1.11	fcc, hcp	-7.63	-0.70	hcp, fcc
Ir	-7.85	-0.81	fcc, hcp	-7.01	-0.32	hcp, fcc
Pt	-7.30	-1.09	fcc, hcp	-6.51	-0.49	hcp, fcc
Au	-5.67	2.34	fcc, hcp	-5.06	2.18	hcp, fcc



literature and agrees with the present study. On Rh, Pd, Ir and Pt  $E_{\text{diss}}^{\text{BN}}$  is negative, *i.e.* on these surfaces the dissociated state is more stable than the dimer state. Positive dissociation energies as *e.g.* for Cu signify an energy gain upon B–N association. This has implications if it comes to the seed formation for graphene and h-BN formation.

The data in Tables 1 and 2 further suggest that the desorption of C is not expected to proceed preferentially *via* the  $C_2$  association and desorption channel. On all the investigated substrates the  $C_2$  adsorption energies are larger than the C adsorption energy, and  $E_{\text{diss}}^{\text{CC}}$  is smaller than the desorption energy, which indicates that depletion *via*  $C_2$  desorption is unlikely. For B and N, as well, desorption is not expected to proceed preferentially *via* the dimer channel. On all investigated substrates, the BN adsorption energies are larger than B or N adsorption energy, and  $E_{\text{diss}}^{\text{BN}}$  is smaller than the desorption energy, which indicates that depletion *via* BN desorption is unlikely.

### 3.6. $C_6$ and $(\text{BN})_3$ ring-hexamers

While dimers have no isomers, the hexamers display a variety of possible molecular configurations. In the case of  $(\text{BN})_3$  on Cu(111) four different isomers have been investigated, where the linear isomer displayed the lowest energy, lower than that of the hexamer forming a ring.<sup>19</sup> In the present article we restrict ourselves to the ring-hexamers, which have the same rotational symmetry as the substrates and the 2D materials gr and h-BN.

In Table 3 the adsorption energies of the  $C_6$  and  $(\text{BN})_3$  ring-hexamers and the corresponding C–C and B–N bond energies are summarised. The atomisation energies of the molecules  $C_6$  and  $(\text{BN})_3$  in the gas phase are 34.30 and 32.20 eV, respectively, which result in single bond-dissociation energies of 5.72 and 5.37 eV. Compared to the dimers the adsorption energies decrease. Also the single bond energies  $E_{\text{6bo}}^{\text{hex}}$  of the ring-hexamers are smaller than the C–C and the B–N bond energies  $E_{\text{diss}}^{\text{AB}}$  in the dimers. As for the dimers, there are substrates where the dissociated state is favoured. On these substrates like

**Table 3** The adsorption  $E_{\text{ads}}$  and single bond-dissociation energies  $E_{\text{6bo}}$  and lowest energy adsorption sites of the  $C_6$  and  $(\text{BN})_3$  ring-hexamers on the studied surfaces. Energies are in (eV per hexamer) and (eV per bond)

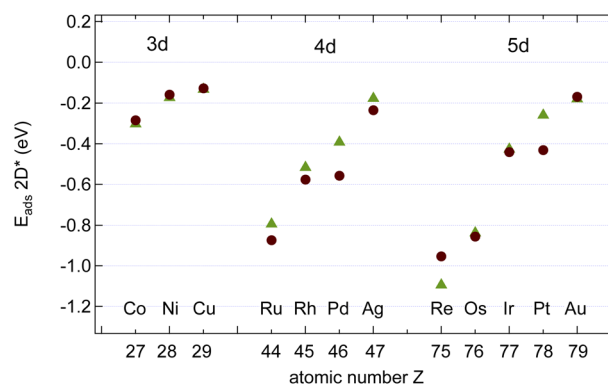
Substrate	$E_{\text{ads}}^{C_6}$	$E_{\text{6bo}}^{\text{CC}}$	Site	$E_{\text{ads}}^{(\text{BN})_3}$	$E_{\text{6bo}}^{\text{BN}}$	Site
Gas phase	—	5.72	—	—	5.37	—
Co	−7.91	−0.04	fcc, hcp	−4.28	0.32	hcp, fcc
Ni	−7.07	0.07	fcc, hcp	−3.81	0.42	hcp, fcc
Cu	−4.15	1.40	fcc, hcp	−1.87	1.58	fcc, hcp
Ru	−7.74	−0.71	fcc, hcp	−4.70	−0.20	hcp, top
Rh	−6.05	−0.68	fcc, hcp	−4.29	0.05	hcp, top
Pd	−5.41	−0.36	hcp, top	−3.57	0.33	hcp, top
Ag	−2.28	2.46	hcp, top	−0.78	2.58	fcc, top
Re	−8.82	−0.39	fcc, hcp	−4.66	−0.16	fcc, hcp
Os	−6.54	−1.06	fcc, top	−5.07	−0.26	hcp, top
Ir	−5.75	−0.65	fcc, top	−4.52	0.14	hcp, top
Pt	−5.66	−0.54	hcp, top	−3.98	0.22	hcp, top
Au	−2.76	1.51	hcp, top	−0.94	1.78	top, hcp

Ru, it may be concluded that ring-hexamers on terraces are not stable nuclei for the growth of the 2D layers.

### 3.7. $(1 \times 1)$ commensurate graphene and h-BN

As can be seen from Tables 2 and 3 the dimers and ring-hexamers are not stable on all the investigated metal surfaces. Yet graphene and h-BN single layers may be grown also on such metals like Ru,<sup>20,21</sup> on which the dimers and the ring-hexamers are not stable. This suggests that the growth seeds in cases of a negative hexamer dissociation energy are larger than six atoms. In the case of graphene on Ir(111) the graphene seed size was worked out theoretically to be about 16 C atoms before the energy per C atom becomes lower than that of the single atom adsorbed on Ir and it was shown that atomic steps reduce the seed barrier, though not the seed size.<sup>18</sup> On substrates with a large lattice mismatch to graphene and h-BN as it is the case for the 4d and 5d metals the issue of the commensurability and the size of the unit cell emerges. For example, h-BN on Ru forms a 14 on 13 coincidence lattice, which reduces the tensile stress in the h-BN, as found by surface X-ray diffraction.<sup>22</sup> The situation of the graphene systems is more involved, as for example a 25 on 23 superstructure has been observed<sup>23</sup> and simulated with calculations.<sup>24</sup>

In the present account we did not perform calculations in the large supercells, but on  $(1 \times 1)$  unit cells with the lattice constant of the substrate. Accordingly, the calculated  $(1 \times 1)$  adsorption energies neglect the dislocation of the graphene or h-BN layer in a super cell. In Fig. 7 the calculated adsorption energies of strained graphene and h-BN are shown. All metals favour adsorption. There is a clear trend in the adsorption energies with the number of valence band d-holes in the substrate atoms, as has been reported on h-BN by Laskowski *et al.*<sup>25</sup> The increase of the effect in going from the 3d to the 5d transition metals is also seen in the trends of the adsorption energies of the N and C atom (Fig. 4). Re displays the largest  $sp^2$  effective adsorption energies, where the h-BN adsorption energy is particularly strong. When we calculated the adsorption energies with respect to the relaxed graphene and h-BN in the



**Fig. 7** Calculated energies  $E_{\text{ads}}^{\text{AB}}$  of graphene (brown circles) and h-BN (green triangles) on the studied surfaces. The energy reference is graphene or h-BN strained to the lattice constant of the corresponding transition metal. Except for Re (B, N = C, C = hcp, top) and Au (B, N = C, C = top, fcc) all registries are (B, N = C, C = fcc, top).



**Table 4** Strained graphene and h-BN adsorption,  $E_{\text{ads}}^{2\text{D}^{\dagger}}$ , and effective  $\text{sp}^2$  bond energies  $E_{\text{sp}^2}^{2\text{D}^{\dagger}}$  on the studied surfaces. Energies are given in (eV per  $(1 \times 1)$  unit cell) and (eV per bond)

Substrate	$E_{\text{ads}}^{\text{gr}}$	$E_{\text{sp}^2}^{\text{gr}}$	Site CC	$E_{\text{ads}}^{\text{h-BN}}$	$E_{\text{sp}^2}^{\text{h-BN}}$	Site BN
Free standing	—	5.17	—	—	4.63	—
Co	-0.28	0.55	top, fcc	-0.30	0.88	fcc, top
Ni	-0.16	0.67	top, fcc	-0.17	0.96	fcc, top
Cu	-0.13	1.87	top, fcc	-0.13	1.94	fcc, top
Ru	-0.87	0.32	top, fcc	-0.79	0.66	fcc, top
Rh	-0.58	0.42	top, fcc	-0.52	0.78	fcc, top
Pd	-0.56	0.71	top, fcc	-0.39	1.00	fcc, top
Ag	-0.23	2.82	top, fcc	-0.17	2.74	fcc, top
Re	-0.95	0.44	top, hcp	-1.09	0.79	hcp, top
Os	-0.86	0.21	top, fcc	-0.84	0.59	fcc, top
Ir	-0.44	0.43	top, fcc	-0.43	0.78	fcc, top
Pt	-0.43	0.52	top, fcc	-0.26	0.84	fcc, top
Au	-0.17	2.12	top, fcc	-0.18	2.19	top, fcc

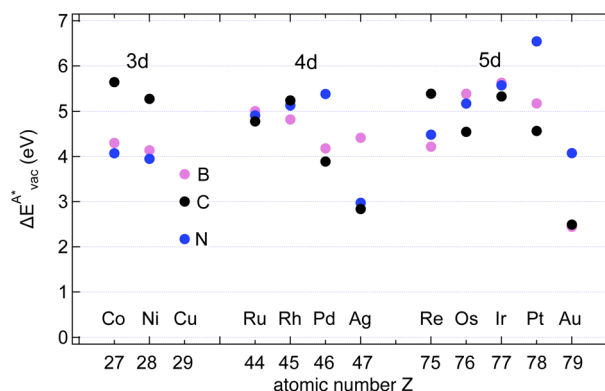
gas phase some systems with a large lattice mismatch were not stable as commensurate  $(1 \times 1)$  systems because the elastic strain energy of  $(1 \times 1)$  commensurate layers is substantial.

Table 4 shows the adsorption energies and the effective  $\text{sp}^2$  bond energies of graphene and h-BN in  $(1 \times 1)$  structures on the investigated transition metals. All effective bond energies are positive, which confirms the stability of the 2D layers.

In the ESI†, graphs are shown in Fig. S1† that summarise the solvation and the different adsorption energies of the graphene and boron nitride systems on the investigated substrates.

### 3.8. Vacancy defect energies

If the ultimate thermal stability of graphene or h-BN shall be predicted, the formation energy of single atomic vacancies is a key quantity.<sup>4</sup> In Table 5 the calculated vacancy defect energies for strained graphene and h-BN on the twelve different metal substrates are given. From the  $E_{\text{vac}}^{\text{AB}^{\dagger}}$  the Cu substrate has the highest stability of graphene and h-BN. Another general observation is that in the case of h-BN nitrogen has a lower



**Fig. 8** Vacancy defects. The  $\Delta E_{\text{vac}}^{\text{A}}$  is the lowering of the vacancy defect creation energy in the strained adsorbed layer, compared to the strained free-standing layer. For graphene (black dots) the defect with the higher  $\Delta E_{\text{vac}}^{\text{C}}$  is displayed. The particularly low  $\Delta E_{\text{vac}}^{\text{B}}$  on Au is due to the fact that the gold atom beneath the vacancy lifts out of the substrate and accordingly increases the energy of the system with the vacancy on the substrate.

vacancy formation energy than boron. This is important information if single photon emitters based on h-BN shall be grown.<sup>26</sup> In the ESI, Table S8† further contains the energetics referred to as the chemical potential of the atoms in the single layer instead of free atoms as used here; those values can be used for example to calculate the equilibrium concentration of vacancies.

The results in Fig. 8 display the lowering of the vacancy defect creation energies with respect to the strained free standing layers  $\Delta E_{\text{vac}}^{\text{A}}$  in the strained adsorbed layers. In the case of gr/Ir(111) defect formation energies in a  $(10 \times 10)$  on  $(9 \times 9)$  supercell have been calculated and found to depend on the registry of the C atoms with respect to the Ir atoms.<sup>27</sup> From these energies we derive values of  $\Delta E_{\text{vac}}$  between 1.7 and 3.0 eV. They compare to 5.32 eV from the present calculation of the strained graphene. In the case of h-BN/Rh(111) defect formation energies in the whole  $(13 \times 13)$  on  $(12 \times 12)$  supercell have been calculated in order to explain the so called “can-opener” effect.<sup>28</sup>

**Table 5** Vacancy defect energies in graphene and h-BN on the studied surfaces. The values for the strained free standing  $\text{sp}^2$  layers are given in the ESI. Energies are given in eV

Substrate	$E_{\text{vac}}^{\text{C}^{\dagger}}$	$\Delta E_{\text{vac}}^{\text{C}^{\dagger}}$	Site $\bar{\text{C}}\bar{\text{C}}$	$E_{\text{vac}}^{\text{B}^{\dagger}}$	$\Delta E_{\text{vac}}^{\text{B}^{\dagger}}$	Site $\bar{\text{B}}\bar{\text{N}}$	$E_{\text{vac}}^{\text{N}^{\dagger}}$	$\Delta E_{\text{vac}}^{\text{N}^{\dagger}}$	Site $\bar{\text{B}}\bar{\text{N}}$
Free standing, unstrained	15.61	0	—	16.13	0	—	13.07	0	—
Co	10.01	5.64	top, fcc	11.83	4.31	fcc, top	8.49	4.14	fcc, top
Ni	10.37	5.27	top, fcc	11.82	4.31	fcc, top	8.59	3.95	fcc, top
Cu	12.48	3.01	top, fcc	12.43	3.61	fcc, top	11.14	2.17	fcc, top
Ru	8.74	4.78	top, fcc	9.33	5.00	fcc, top	8.24	4.91	fcc, top
Rh	8.53	5.24	top, fcc	9.74	4.82	fcc, top	8.14	5.13	fcc, top
Pd	8.59	3.89	top, fcc	9.20	4.18	fcc, top	7.21	5.38	fcc, top
Ag	6.17	2.84	top, fcc	6.29	4.41	fcc, top	7.81	2.96	fcc, top
Re	7.18	5.39	top, hcp	9.24	4.22	hcp, top	8.15	4.48	hcp, top
Os	8.36	4.55	top, fcc	8.38	5.38	fcc, top	7.66	5.17	fcc, top
Ir	7.85	5.32	top, fcc	8.38	5.63	fcc, top	7.40	5.57	fcc, top
Pt	7.37	4.57	top, fcc	7.75	5.17	fcc, top	5.73	6.55	fcc, top
Au	5.94	2.49	top, fcc	7.88	2.44	top, fcc	6.44	4.08	top, fcc



From this we derive values of  $\Delta E_{\text{vac}}^A$  between 2.57 and 5.96 eV for B and between 1.56 and 4.43 eV for N. They compare to 4.82 and 5.15 eV in the present calculation for B and N, respectively, of strained h-BN vs. strained h-BN/Rh(111). The present vacancy formation energies may therefore be considered as upper bounds, as in a larger unit cell lower vacancy defect formation energies may be expected.

## 4. Conclusions

The present article reports comprehensive sets of calculated energies of atomic systems as they are encountered in the growth of graphene and hexagonal boron nitride on twelve different transition metals. Solvation, adsorption and diffusion energies for single atoms are presented. This database forms a guideline for the expected processes. For the growth of 2D materials the surface adsorption energies of dimers and ring-hexamers and their stability as seeds were calculated. The stability of the  $sp^2$  layers was estimated from the vacancy creation energies.

From the trends above, criteria for the rational design of high quality and stability graphene and h-BN on transition metals have become available.

## Author contributions

The manuscript was written through the contributions of both authors. T. G. initiated the project and wrote the first version of the manuscript. APS performed the calculations, cross checked and inserted the results in the tables.

## Conflicts of interest

There are no conflicts to declare.

## Acknowledgements

We acknowledge financial support from the Swiss National Science Foundation (SNF project no. 200020\_201086) and by the European Commission under the Graphene Flagship (contract no. CNECT-ICT-604391). We further acknowledge access to Piz Daint and Eiger@Alps at the Swiss National Supercomputing Centre (CSCS), Switzerland under the share of the Universität Zürich with the project ID uzh11.

## Notes and references

- 1 L. Zhang, J. Dong and F. Ding, *Chem. Rev.*, 2021, **121**, 6321–6372.
- 2 T. Zhao, J. Guo, T. Li, Z. Wang, M. Peng, F. Zhong, Y. Chen, Y. Yu, T. Xu, R. Xie, P. Gao, X. Wang and W. Hu, *Chem. Soc. Rev.*, 2023, **52**, 1650–1671.
- 3 K. Y. Ma, L. Zhang, S. Jin, Y. Wang, S. I. Yoon, H. Hwang, J. Oh, D. S. Jeong, M. Wang, S. Chatterjee, G. Kim, A.-R. Jang, J. Yang, S. Ryu, H. Y. Jeong, R. S. Ruoff, M. Chhowalla, F. Ding and H. S. Shin, *Nature*, 2022, **606**, 88–93.
- 4 F. Banhart, J. Kotakoski and A. V. Krasheninnikov, *ACS Nano*, 2011, **5**, 26–41.
- 5 M. Mavrikakis, J. Rempel, J. Greeley, L. B. Hansen and J. K. Nørskov, *J. Chem. Phys.*, 2002, **117**, 6737–6744.
- 6 J. Winterlin and M. Bocquet, *Surf. Sci.*, 2009, **603**, 1841–1852.
- 7 M. Saeed, Y. Alshammari, S. Majeed and E. Al-Nasrallah, *Molecules*, 2020, **25**, 3856.
- 8 W. Auwärter, *Surf. Sci. Rep.*, 2019, **74**, 1–95.
- 9 H. Cun, Z. Miao, A. Hemmi, Y. Al-Hamdani, M. Iannuzzi, J. Osterwalder, M. S. Altman and T. Greber, *ACS Nano*, 2021, **15**, 1351–1357.
- 10 A. Hemmi, A. Seitonen, T. Greber and H. Cun, *Small*, 2022, **22**, 2205184.
- 11 P. Hohenberg and W. Kohn, *Phys. Rev.*, 1964, **136**, B864.
- 12 I. Hamada, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 2014, **89**, 121103.
- 13 X. Hu, T. Bjorkman, H. Lipsanen, L. Sun and A. Krasheninnikov, *J. Phys. Chem. Lett.*, 2015, **6**, 3263–3268.
- 14 J. K. Nørskov and N. D. Lang, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 1980, **21**, 2131–2136.
- 15 M. J. Puska, R. M. Nieminen and M. Manninen, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 1981, **24**, 3037–3047.
- 16 M. G. Evans and M. Polanyi, *Trans. Faraday Soc.*, 1938, **34**, 11–24.
- 17 S. Riikonen, A. V. Krasheninnikov, L. Halonen and R. M. Nieminen, *J. Phys. Chem. C*, 2012, **116**, 5802–5809.
- 18 C. Herbig, E. H. Åhlgren, W. Jolie, C. Busse, J. Kotakoski, A. V. Krasheninnikov and T. Michely, *ACS Nano*, 2014, **8**, 12208–12218.
- 19 Z.-Q. Liu, J. Dong and F. Ding, *Nanoscale*, 2019, **11**, 13366–13376.
- 20 Y. Pan, D.-X. Shi and H.-J. Gao, *Chin. Phys.*, 2007, **16**, 3151–3153.
- 21 A. Goriachko, Y. He, M. Knapp, H. Over, M. Corso, T. Brugger, S. Berner, J. Osterwalder and T. Greber, *Langmuir*, 2007, **23**, 2928–2931.
- 22 D. Martoccia, T. Brugger, M. Björck, C. Schlepütz, S. Pauli, T. Greber, B. Patterson and P. Willmott, *Surf. Sci.*, 2010, **604**, L16–L19.
- 23 D. Martoccia, P. R. Willmott, T. Brugger, M. Björck, S. Günther, C. M. Schlepütz, A. Cervellino, S. A. Pauli, B. D. Patterson, S. Marchini, J. Winterlin, W. Moritz and T. Greber, *Phys. Rev. Lett.*, 2008, **101**, 126102.
- 24 M. Iannuzzi, I. Kalichava, H. Ma, S. J. Leake, H. Zhou, G. Li, Y. Zhang, O. Bunk, H. Gao, J. Hutter, P. R. Willmott and T. Greber, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 2013, **88**, 125433.
- 25 R. Laskowski, P. Blaha and K. Schwarz, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 2008, **78**, 045409.
- 26 T. T. Tran, K. Bray, M. J. Ford, M. Toth and I. Aharonovich, *Nat. Nanotechnol.*, 2016, **11**, 37.
- 27 S. Standop, O. Lehtinen, C. Herbig, G. Lewes-Malandrakis, F. Craes, J. Kotakoski, T. Michely, A. V. Krasheninnikov and C. Busse, *Nano Lett.*, 2013, **13**, 1948–1955.
- 28 H. Y. Cun, M. Iannuzzi, A. Hemmi, J. Osterwalder and T. Greber, *ACS Nano*, 2014, **8**, 7423–7431.

