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Self-supervised graph neural networks for polymer property prediction[†]

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The estimation of polymer properties is of crucial importance in many domains such as energy, healthcare, and packaging. Recently, graph neural networks (GNNs) have shown promising results for the prediction of polymer properties based on supervised learning. However, the training of GNNs in a supervised learning task demands a huge amount of polymer property data that is time-consuming and computationally/experimentally expensive to obtain. Self-supervised learning offers great potential to reduce this data demand through pre-training the GNNs on polymer structure data only. These pre-trained GNNs can then be fine-tuned on the supervised property prediction task using a much smaller labeled dataset. We propose to leverage self-supervised learning techniques in GNNs for the prediction of polymer properties. We employ a recent polymer graph representation that includes essential features of polymers, such as monomer combinations, stochastic chain architecture, and monomer stoichiometry, and process the polymer graphs through a tailored GNN architecture. We investigate three self-supervised learning setups: (i) node- and edge-level pre-training, (ii) graph-level pre-training, and (iii) ensembled node-, edge- & graph-level pre-training. We additionally explore three different transfer strategies of fully connected layers with the GNN architecture. Our results indicate that the ensemble node-, edge- & graph-level self-supervised learning with all layers transferred depicts the best performance across dataset size. In scarce data scenarios, it decreases the root mean square errors by 28.39% and 19.09% for the prediction of electron affinity and ionization potential compared to supervised learning without the pre-training task.

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Design, System, Application

Our manuscript on “Self-supervised graph neural networks for polymer property prediction” is a graph-based machine learning method to improve molecular property prediction in scarce data domains. We develop node-level, edge-level, and graph-level self-supervised learning strategies for weighted directed message passing graph neural networks. We show how our method improves the performance of a state-of-the-art property predictor when limited data is available. Thus, the method is useful for screening and design efforts in scarce data domains. The molecular systems are co-polymers based on combinations of almost 700 distinct monomer chemistries, varying monomer stoichiometries (1:1, 1:3, 3:1), and three distinct chain-architectures. The properties of interest are electron affinity and ionisation potential. The immediate application potential of the work is to improve photocatalyst design for the production of green hydrogen. Ultimately, our work can be further employed for any co-polymer property prediction task which can be modelled through GNNs.

1 Introduction

The rise of many novel technologies demands the development of innovative polymers, with applications such as polymer-based organic batteries,¹ polymer photocatalysts

that aid hydrogen generation,² or more sustainable plastics.³ However, navigating the vast chemical space to identify polymers with optimal properties poses a considerable challenge. Consequently, various computational methods have been proposed to assist preliminary screening tasks.

One widely recognized class of methods is quantitative structure–property relationships (QSPR),⁴ which link molecules' physical or chemical properties to their structural information through the use of predefined molecular descriptors and linear or nonlinear regression techniques. Nonetheless, QSPR models carry intrinsic limitations. For instance, significant domain expertise is required to select appropriate molecular descriptors and potentially sub-

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optimal choices impact their prediction capacity. Additionally, the feature selection process needs to be repeated for each target property. These limitations are addressed by end-to-end learning methods in machine learning (ML), bypassing the need for manual selection of descriptors and enabling the models to discern relevant features autonomously. Here, the algorithms learn a molecular fingerprint directly from the molecular representation without the need for descriptor selection. Graph neural networks (GNNs) have recently emerged as a key end-to-end learning technique for molecular property prediction tasks, as they leverage the graphical representation of molecules.⁵ Particularly, atoms are represented as nodes, and bonds are represented as edges. GNNs have shown to be very successful in a broad range of molecular prediction tasks, such as predicting combustion-related properties,⁶ predicting the growth of *Escherichia coli* for new antibiotic discovery,⁷ and protein function⁸ or protein–protein interaction tasks.⁹

Despite the success of GNNs in molecular machine learning, extending them to polymer property prediction remains challenging. The reasons for that are twofold. Firstly, polymer structures are difficult to model accurately. They exhibit an inherent hierarchical complexity and they are not one uniquely defined molecular structure but are composed of an ensemble of similar molecules.¹⁰ Secondly, unlike in the domains of small molecules and ordered materials, where numerous large (>100K) and open-source databases exist,^{11,12} there is an absence of accessible polymer property data.^{13–15} The recent work by Aldeghi *et al.*¹⁰ has represented polymers with selected higher-order structural information as a stochastic graph, making them applicable for GNNs. However, the second obstacle, the lack of sufficient polymer property data is still challenging. The measurements of polymer properties in the community rely highly on the instruments in the experiments. However, those instruments have few open interfaces and data models, hindering further developments of large property databases.^{16–18}

To address the scarcity of labeled data, several strategies have been proposed, including transfer learning^{19,20} and multi-task learning.^{21,22} For instance, Zhang *et al.*¹⁹ pre-trained a transformer model on a dataset of 1 billion small molecules and subsequently fine-tuned the model with a small amount of labeled polymer property data (ranging from 300 to 3000 samples). The resulting accuracies were comparable to those achieved by the TransPolymer²³ and polyBERT²⁴ models, without the expensive generation and pretraining on large-scale augmented polymer datasets. Furthermore, the objective of a multi-task training approach is to enhance the performance and generalization of a model by concurrently training it on multiple related tasks, thereby leveraging shared information and representations. Gurnani *et al.*²¹ introduced multi-task GNNs for predicting 34 polymer properties. Their results indicated that, for datasets with fewer than 300 samples, the proposed models generally outperform the benchmark models.

Self-supervised learning (SSL) is another method for learning from limited data and currently helps solve data scarcity challenges in many fields like computer vision^{25,26} and natural language processing.²⁷ SSL first designs a predictive learning task within the unlabelled data itself such that the model learns universal features and semantics, which subsequently contribute to the downstream supervised task with less labeled training data. A common SSL technique, for example, is to create a pseudo label from the unlabelled data structure. Unlike other training strategies that incorporate pseudo-labels into the input to enhance performance,²⁸ SSL pre-trains the model using pseudo-labels to extract initial semantic information from unlabeled data. This approach reduces the amount of labeled data needed for subsequent fine-tuning tasks. Taking computer vision as an example,²⁹ one can rotate an image and task the model with predicting the rotation angle. Thereby the model learns certain features from images and their orientation in space; semantics that are useful for the downstream task of interest. In the field of graph-based molecular property prediction, such tasks are commonly designed according to the structure of the molecular graph. For example, Zhang *et al.*³⁰ leveraged node and edge masking as an SSL technique to pre-train GNNs, which improves the performance of predicting properties of organic semiconductors. Zang *et al.*³¹ implemented a hierarchical molecular graph neural network (HMGNN) with multi-level SSL techniques to achieve superior molecular property prediction results on both classification and regression tasks. With various successful applications in small molecular property prediction^{30–32} and proteins,^{33,34} SSL is a promising technique for prediction tasks in the sparse data domain of polymer informatics. Several studies^{19,23,24,33} have leveraged large language models (LLMs) for polymer property prediction tasks in an SSL manner. For example, polyBERT is pre-trained using masked language modeling (MLM) on approximately 80 million polymer strings, generated from about 13 800 original polymers. During fine-tuning, the pre-trained transformer weights are frozen and employed to provide polymer embeddings, which serve as inputs to a multi-layer perceptron for multitask property prediction. While these studies achieve similar performance, they are limited by using the PSMILES language, which only specifies the repeating unit and neglects important structural information such as chain architecture, stoichiometry, and monomer bonding, crucial for determining polymer properties.

We propose self-supervised GNNs for polymer property prediction. In particular, we utilize the state-of-the-art polymer graph representation and tailored GNN model from Aldeghi *et al.*¹⁰ as foundation, and investigate three self-supervised learning setups: (i) pre-training with node- and edge-level pseudo tasks, (ii) pre-training with graph-level pseudo tasks, and (iii) ensembled node-, edge-, and graph-level pre training. Additionally, we investigate various



strategies for transferring the model architecture to augment the predictive accuracy, providing a novel perspective in the realm of polymer property prediction.

2 Methods

This section introduces the methodologies employed throughout our work. First, the graph representation of polymers is introduced in section 2.1 and the GNN architecture with tailored message-passing layers is illustrated in section 2.2 (adapted from Aldeghi *et al.*¹⁰). Then, three different strategies of self-supervised learning are explained: node- and edge-level, graph-level task, and node- and edge- and graph-level task consecutively. Moreover, we outline our weight transferal strategies. Finally, we introduce the details of the polymer datasets and the training procedure.

2.1 Polymer graphs

We make use of a polymer representation that combines the graph representation of monomers with stochastic edges according to linking probabilities. We denote the graph representation of a polymer p with nodes as atoms $v \in N$ and

edges as bonds $e_{vu} \in E$ connecting two nodes v and u . Specifically, there are two directed bonds between nodes v and u : bond e_{vu} and bond e_{uv} . Two directed edges allow for a wider variety of polymer structures. For example, as Fig. 1 shows, they can capture the impact of terminal ends when required such as oligomer with termini, and different possibilities of two atoms being adjacent to one another such as graft copolymers. Moreover, a feature vector and a stochastic weight are assigned to each node and each directed edge. We denote the feature vector and the stochastic weight of node v with $\mathbf{f}^v \in F^N$ and $w_v \in W^N$, respectively. \mathbf{f}^v contains specific information for atoms such as the atom type and w_v represents the stoichiometric ratio of the corresponding monomer. Similarly, for the directed edge from node v to node u , a feature vector $\mathbf{f}^{e_{vu}} \in F^E$ and a stochastic weight $w_{vu} \in W^E$ are attached. $\mathbf{f}^{e_{vu}}$ contains specific information for bonds such as the bond type. $w_{vu} \in (0, 1]$ is an associated weight value reflecting the probability of that bond occurring within the respective polymer topologies. Notably, within the monomer, the edge weight is set to 1. While for the directed edges connecting different monomers, the weights vary as shown in Fig. 1. Typical features are given in Table 1 for atoms and in Table 2 for bonds. The feature-

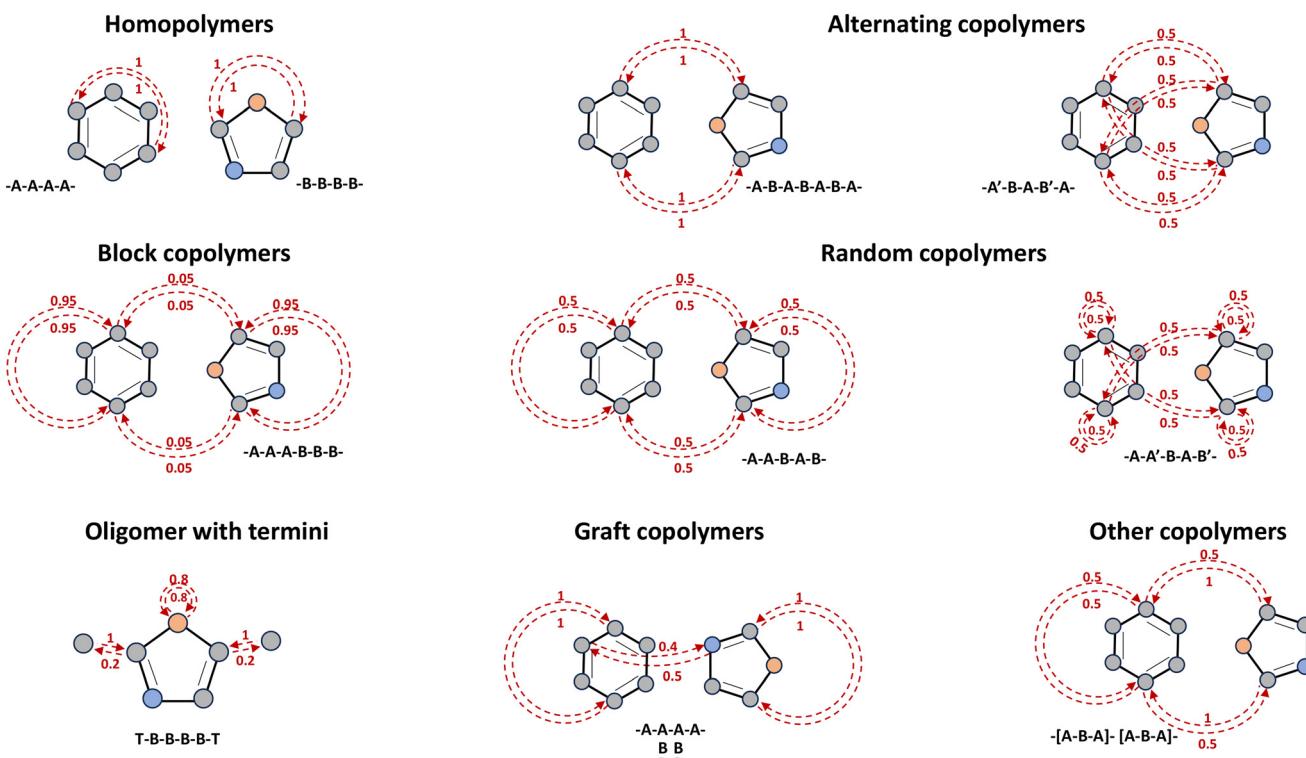


Fig. 1 Overview of polymer topologies (adapted from Aldeghi *et al.*¹⁰). The red dashed lines represent the direct edges which are assigned to corresponding weights between zero and one. The weights of incoming edges indicate the possibility that the originating node (atom) is adjacent to the target node (atom). For instance, in the case of graft copolymers, there is a 40% chance that the atoms on monomer A will be neighboring atoms on monomer B (two of five monomers A are connected to monomers B), whereas the atoms on monomer B have a 50% chance of being adjacent to atoms on monomer A (two out of four monomers B are connected to the monomers A). The text underneath of each topology represents an example of the corresponding polymer sequence, where A and B are different monomers. The polymer sequence depicts a tail-to-head orientation, e.g., -A-B- represents the tail of monomer A links to the head of monomer B, and -A'-B- indicates the head of monomer A connects to the head of monomer B.



Table 1 Atom features for initial node feature vector.¹⁰ Features are encoded as one-hot vectors except for atom mass

Feature	Description
Atom type	Type of atom
Chiral tag	Type of chirality
Degree	Number of bonded neighbors in the graph
Is aromatic	Whether the atom is part of an aromatic system
Hybridization	Type of hybridization such as sp, sp ²
Charge	Formal charge of the atom
#Hs	Number of bonded hydrogen atoms
Mass	Atom mass

Table 2 Bond features for all initial edge feature vector.¹⁰ Features are encoded as one-hot vectors

Feature	Description
Bond type	Single, double, triple, or aromatic
Conjugated	Whether the bond is conjugated
Is in a ring	Whether the bond is part of a ring
Stereo	None, any, E/Z, or cis/trans

enriched graph of a polymer p is then denoted by $G(p) = \{V, E, F^N, F^E, W^N, W^E\}$.

2.2 Graph neural networks

GNNs can learn desired target predictions from a featured graph representation. Fig. 2 shows an example of the GNN architecture that is used in this work for supervised learning-only training. GNNs consist of two phases: the message passing phase, which contains convolutional operations, and the readout phase, which forms the fingerprint and predicts the target task. In the following subsection, we will introduce these two phases separately.

In the message passing phase, graph convolution is utilized to extract the structural information from the polymer graph. Importantly, the weighted direct message passing neural network (wD-MPNN) is used as the graph convolutional layer. Fig. 3 shows the four steps in wD-MPNN to extract structural information from polymers. In the first step, taking node v as an example, the edge feature $\mathbf{f}^{e_{vu}}$ from node v to node u is updated into \mathbf{h}_{vu}^0 as eqn (1) shows.

$$\mathbf{h}_{vu}^0 = \tau(W_i(\mathbf{f}^v \parallel \mathbf{f}^{e_{vu}})) \quad (1)$$

where \parallel denotes concatenation, W_i is a learnable weight matrix, and τ is an activation function. In the next step, namely edge-centered message passing, the hidden edge feature \mathbf{h}_{vu}^0 is further updated by L graph convolutional layers. Specifically, within $l \in L$, the new hidden edge feature \mathbf{h}_{vu}^{l+1} is obtained by incoming edges to node v except the one from node u as eqn (2).

$$\mathbf{h}_{vu}^{l+1} = \tau\left(\mathbf{h}_{vu}^0 + W_h \sum_{k \in \{V(v)/u\}} w_{kv} \mathbf{h}_{kv}^l\right) \quad (2)$$

where W_i is a learnable weight matrix, and τ is an activation function. Furthermore, after L layers of edge-centered message passing, the updated node feature \mathbf{h}_v is acquired by taking the concatenation of the original node feature vector \mathbf{f}^v , with the weighted sum of the hidden edge feature vectors \mathbf{h}_{kv}^L incoming to node v and passing this through a single fully connected layer. eqn (3) shows all steps where W_0 is a learnable weight matrix, and τ is an activation function. Notably, the edge-centered message passing as introduced by Aldeghi *et al.*¹⁰ differentiates from node-centered message passing by previous works.^{35,36}

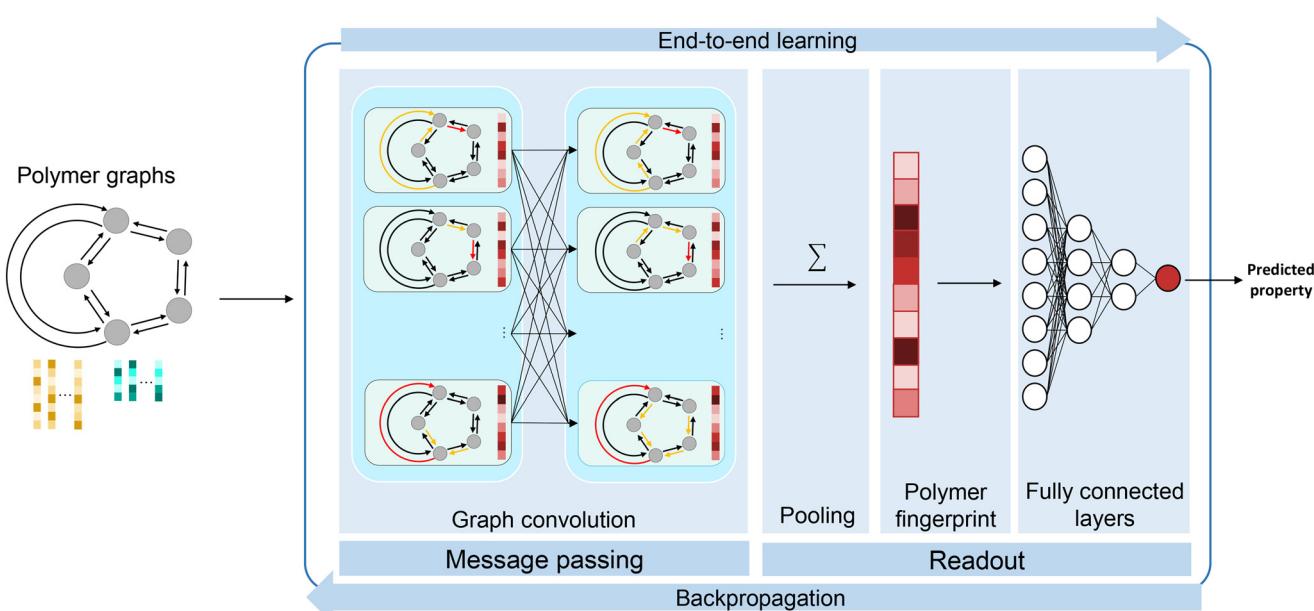


Fig. 2 Overview of a GNN architecture for polymer property predictions.



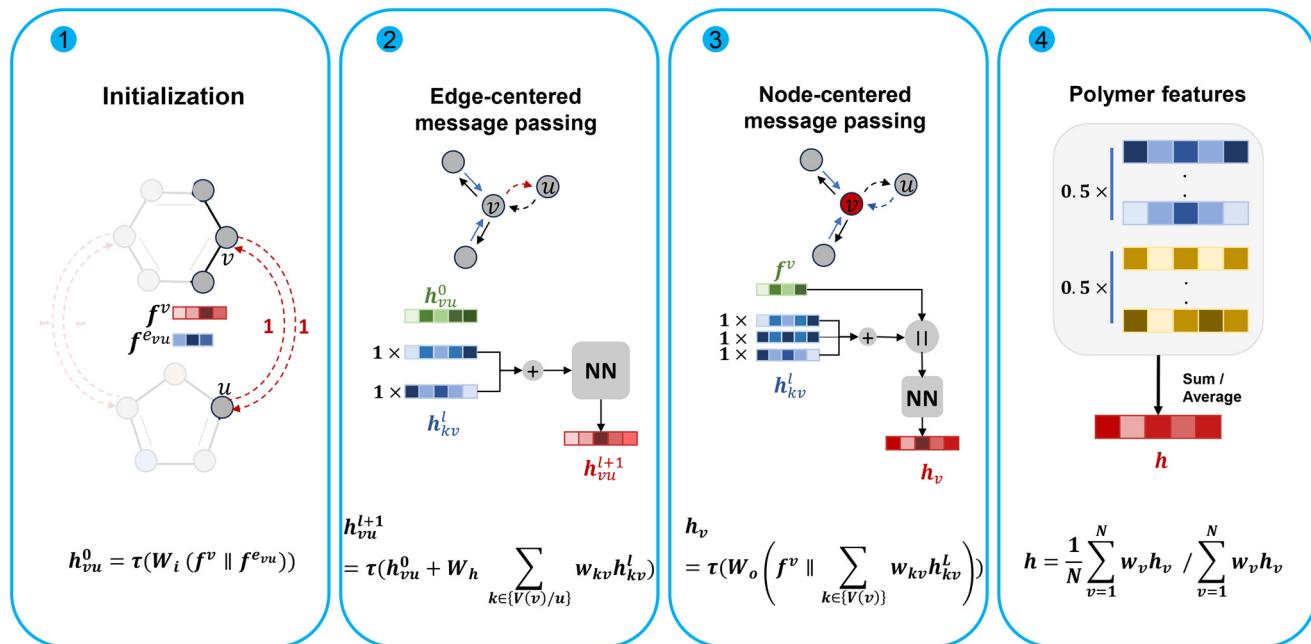


Fig. 3 Four steps visualization of wD-MPNN.¹⁰ First, the hidden edge features are initialized by concatenating originating atom features with edge features and then passing through a single fully connected layer. Second, hidden edge features are updated through L steps of edge-centered message passing. Within $l \in L$ steps, the neighboring hidden edge features are combined by the weighted sum, and then the results are added to the center hidden edge features h_{vu}^0 and passed through a fully connected layer. Third, the center atom features f^v are updated through the concatenation of the weighted sum of incoming hidden edge features and the original atom features. The results are then passed through a single fully connected layer. Finally, a polymer fingerprint is obtained by taking the weighted average or sum of the updated atom feature vectors.

$$\mathbf{h}_v = \tau \left(W_o \left(\mathbf{f}^v \parallel \sum_{k \in V(v)/u} w_{kv} \mathbf{h}_{kv}^L \right) \right) \quad (3)$$

In the *readout* phase, the learned information from the previous steps in the hidden nodes is aggregated into a polymer fingerprint by taking the weighted average/sum as eqn (4) shows, where N is the number of nodes in the graph, w_v are the associated stochastic weights of each node.

$$\mathbf{h} = \frac{1}{N} \left(\sum_{v=1}^N w_v \mathbf{h}_v \text{ or } = \sum_{v=1}^N w_v \mathbf{h}_v \right) \quad (4)$$

Finally, the polymer fingerprint \mathbf{h} is mapped into the property of interest. For GNNs, a multi-layer perception (MLP) is used to compute the property: $\hat{p} = \text{MLP}(\mathbf{h})$.

2.3 Self-supervised learning

Fig. 4 illustrates the general framework of SSL: the pre-training phase where pseudo-tasks are designed for larger, yet unlabelled, datasets and the fine-tuning phase where the actual target labels are used for training purposes. During the pre-training phase, the encoder (message-passing layers in our case) is trained by polymer graphs

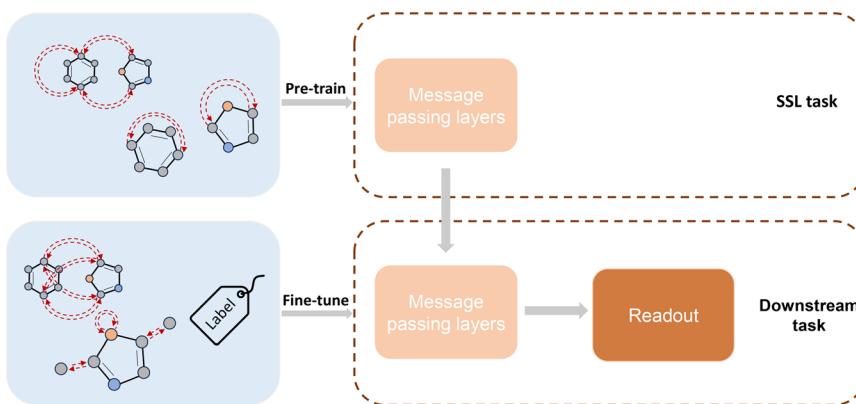


Fig. 4 General framework of SSL.³⁷ The message passing layers are first trained with SSL tasks. Then the trained message passing layers are transferred with/partially with a new readout training (e.g., new fully connected layers) to train with target labels for downstream tasks.

with pseudo labels. These pseudo labels are obtained from the featured polymer graph topology. The aim is to design tasks for which no labeled data, *i.e.*, physical properties, are needed to calculate these pseudo labels. Then, the pre-trained message-passing layers (including steps 1–4 in Fig. 3) are further fine-tuned with or partially with an additional new readout training (*e.g.*, new fully connected layers) by the downstream task with a small amount of labeled data in the second phase. Three SSL techniques are used in this work: (i) node- and edge-level, (ii) graph-level task, and (iii) node- and edge-level with consecutive graph-level tasks.

2.3.1 Node- and edge-level task. We deploy node and edge masking at this level which refers to the practice of intentionally hiding a subset of node or edge information from the model. The model is trained to predict the missing information (pseudo label) from the masked graphs. This approach allows the model to learn the intrinsic structural information associated with surrounding nodes and edges, potentially grasping elementary chemical principles such as valence, and possibly more advanced concepts like functional group configurations. Fig. 5 illustrates the workflow of node- and edge-level SSL and pseudo label prediction during training. Specifically, two node and two edge feature vectors are randomly selected and masked by nullifying their feature vectors. Then, we leverage wD-MPNN (including steps 1–3 in Fig. 3) to learn the structural information from the polymer graph, thereby obtaining learned node- and edge-level embeddings. Note that the prediction involves no pooling step as the pseudo labels are predicted from node- and edge-level information and not from graph-level information. Finally, taking the node- and edge-level embeddings as input, we use fully connected layers to predict the values of originally masked

nodes and edges. We utilized the root mean square error (RMSE) to evaluate the performance. Finally, the pre-trained encoder together with the new fully connected layers is fine-tuned with target labels for the downstream task. The extent of layer transferal will be discussed in section 2.3.4.

2.3.2 Graph-level task. The graph-level task aims at predicting a relevant pseudo label from graph-level information. As before with the node- and edge-level tasks the purpose is to pre-train the model with unlabelled data. The aim is that the graph-level pre-training can foster an understanding of overarching patterns, structural motifs, and inter-node relationships. Importantly, the aim is that through pre-training, the model can generalize better across various graph configurations and perform better in predicting target properties with less data. Fig. 6 shows the overview of the graph-level SSL task. We propose to use an ensemble polymer molecular weight that averages the molecular weight of the monomers (M_{mono}) with the corresponding stoichiometric ratio (w_{mono}) as eqn (5) shows.

$$M_{\text{ensemble}} = w_{\text{mono1}}M_{\text{mono1}} + w_{\text{mono2}}M_{\text{mono2}} \quad (5)$$

Specifically, we calculate the ensemble polymer weight for each data sample and then train the GNN with this new pseudo label as a predictive task. We utilize sum pooling layers to map the updated polymer graphs into a vector, *i.e.*, the polymer fingerprint, which is then further mapped into the prediction of the pseudo graph label through fully connected layers. After the pre-training phase, as in the node- and edge-level pre-training, the pre-trained encoder together with the new fully connected layers is fine-tuned with the target labels for the downstream prediction task. The extent of layer transferal will be discussed in section 2.3.4.

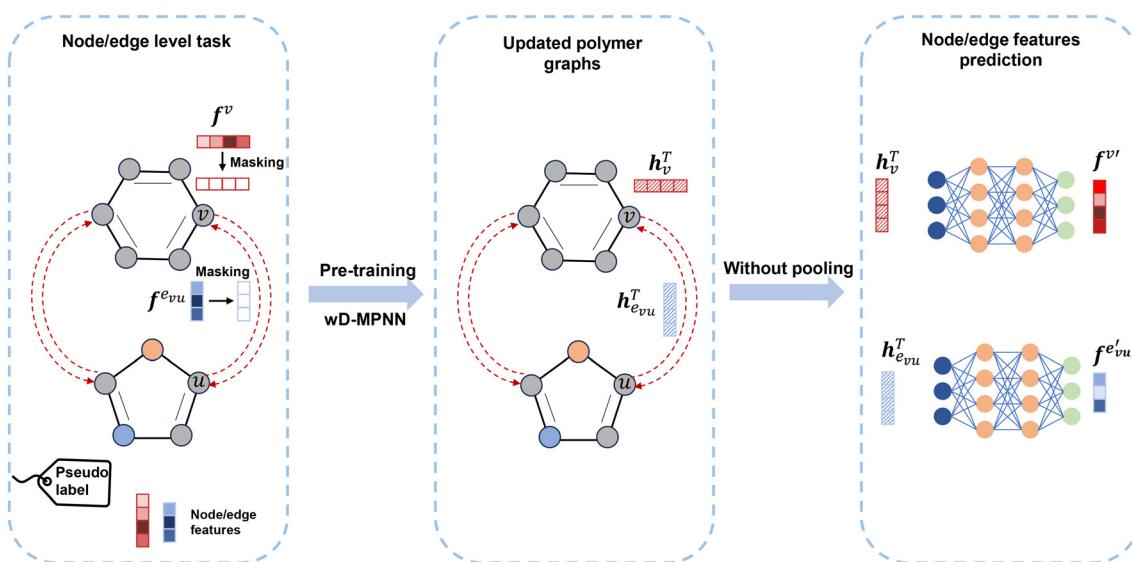


Fig. 5 Overview of node/edge masking task. Randomly selected node and edge feature vectors are masked, then new embeddings are learned through the message passing phase, and finally, the originally masked vectors are predicted from the learned embeddings.



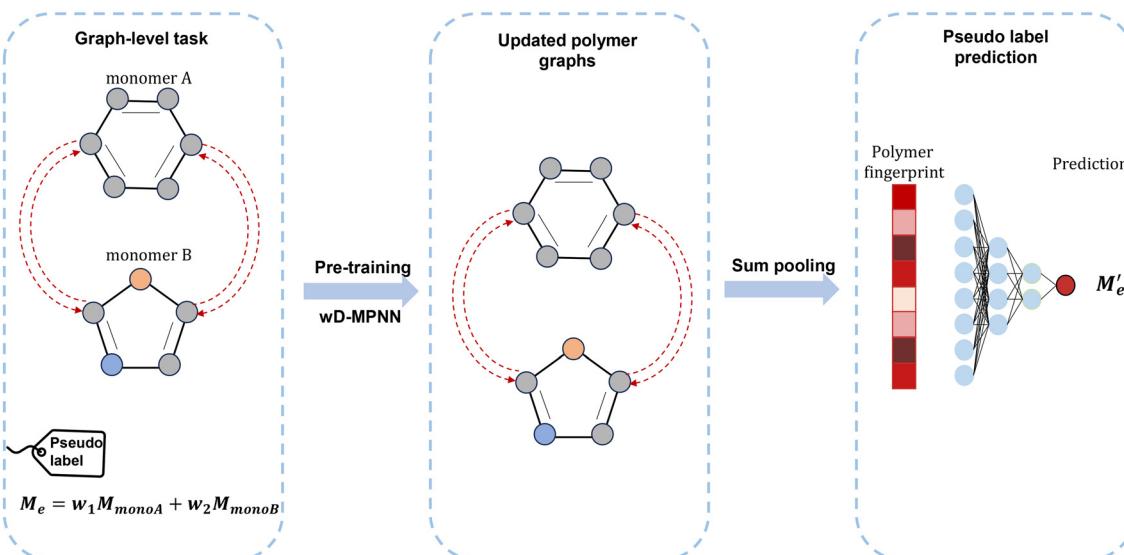


Fig. 6 Overview of the graph-level task. Per co-polymer graph, the ensemble polymer molecular weight is calculated as a label, and then the message passing and readout phases take place to predict the pseudo label.

2.3.3 Node-, edge- & graph-level task. Our third strategy combines all the node-, edge-, and graph-level tasks consecutively. The encoder is first trained with the node- and edge-level task. Then, the encoder is transferred to perform the graph-level task with new fully connected layers. Ultimately, we transfer the encoder to predict the property of interest with new fully connected layers as the prediction head.

2.3.4 Transfer of weights. Finally, we explore the impacts of transferring the fully connected layers of the readout phase from the pre-training phase to the fine-tuning stage for the graph-level task and the combined approach of node-, edge-, and graph-level tasks. In particular, we examined three distinct transfer strategies: exclusive transfer of message-passing layers (strategy a), transfer of both message-passing and two fully connected layers (strategy b), and message-passing and all fully connected layers (strategy c).

2.4 Polymer dataset

We develop our method on the polymer dataset presented by Aldeghi *et al.*,¹⁰ encompassing 42 966 polymers, composed of nine A monomers and 862 B monomers. These polymers are categorized based on three distinct chain architectures: alternating, random, and block, and are further characterized by three stoichiometric ratios, namely 1:1, 1:3, and 3:1. Furthermore, the dataset contains electron affinity (EA) and ionization potential (IP) as molecular properties, *i.e.*, target labels. Both properties were derived through density functional theory (DFT) simulations.

2.5 Training procedure

First, we trained two GNN models *via* a supervised learning paradigm, targeting both the EA and IP labels (in the following referred to as baseline training). Subsequently, we

perform three SSL techniques: (i) node- and edge-level, (ii) graph-level task, (iii) node-, edge-, and graph-level tasks. The polymer dataset is randomly shuffled and 40% of the dataset is used for SSL pre-training tasks. We then transferred the message-passing layers and subsequently conducted exploratory analyses across varying dataset sizes for fine-tuning, spanning 0.08%, 0.16%, 0.24%, 0.32%, 0.4%, 0.8%, 1.6%, 2.4%, 3.2%, 4%, 8%, 16%, 24%, 32%, and up to 40%, allowing us to explore the performance of SSL under varying label availability scenarios. The baseline models are only trained with the same fine-tuning datasets ranging from 0.08% to 40% in a supervised-only manner. Finally, the evaluation of the GNN models is conducted on the remaining 20% of the dataset. The Adam optimizer is used with a 10^{-3} learning rate and a batch size of 64 across 100 training epochs is used. The GNN architectures incorporate three edge-focused message passing layers with a hidden dimension calibrated at 300. Additionally, three fully connected layers are used to map the fingerprints to the prediction task.

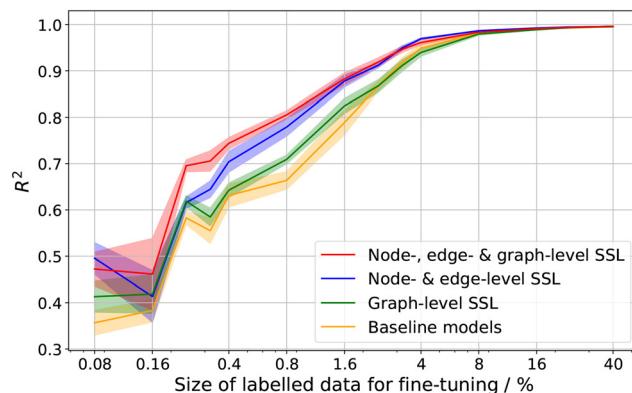
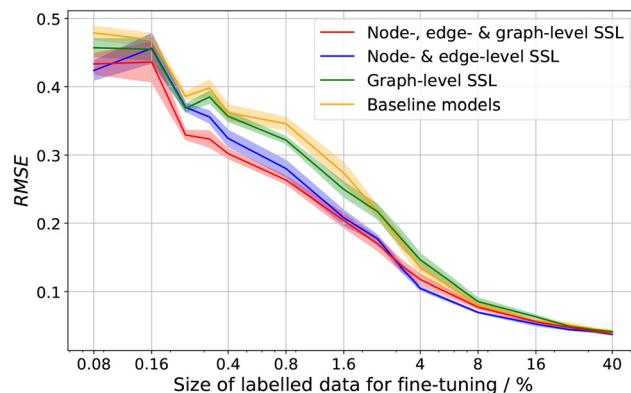
3 Results and discussion

In this section, we present the results from our three SSL techniques: (i) node- and edge-level, (ii) graph level task, and (iii) a sequential application of node- and edge-level followed by the graph-level task. We also outline the results with different layer transferal strategies.

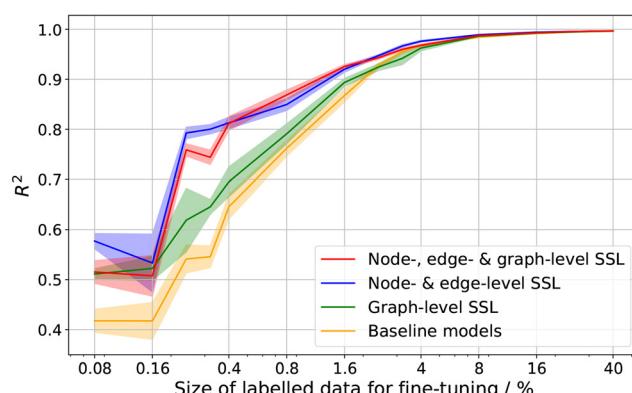
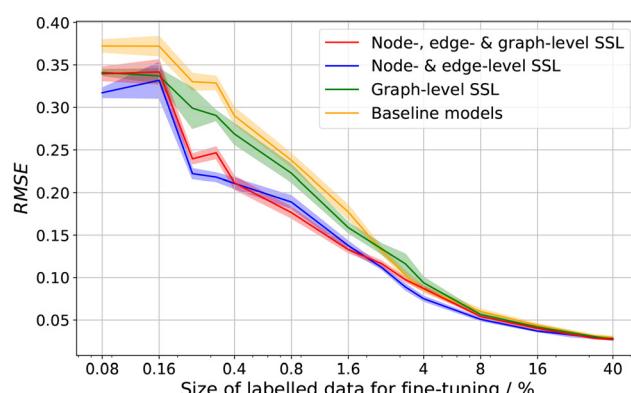
3.1 SSL results

Fig. 7, Tables 3 and 4 illustrate the model performance metrics R^2 and RMSE regarding electron affinity and ionization potential. The corresponding values and 95% confidence interval values are also detailed in the ESI.† In the small labeled data regimes (*e.g.*, <0.4%), node and edge-level SSL, as well as node-, edge- & graph-level SSL, demonstrate



(a) R^2 results for EA

(b) RMSE results for EA

(c) R^2 results for IP

(d) RMSE results for IP

Fig. 7 R^2 and RMSE results for EA and IP for supervised learning only, node- and edge-level, graph-level task, and node-, edge- & graph-level, respectively. Each line is the mean from 10 individual runs and the shaded area is the 95% confidence interval.

similar performance across all evaluated models for both EA and IP according to the R^2 and RMSE. For instance, for node-, edge- & graph-level SSL, an increase of 32.21% and 23.21% in R^2 is observed for both EA and IP, respectively, compared

with baseline models in the smallest fine-tuning dataset (0.08%). Similarly, for node- and edge-level SSL, R^2 is improved by 38.66% and 38.04%, respectively, followed by graph-level SSL in the smallest fine-tuning dataset. Therefore,

Table 3 R^2 of predicting the EA and IP labels using different sizes of datasets for the fine-tuning part and the corresponding standard deviation can be found in ESI.† Specifically, we use baseline for representing baseline models, NE for representing node- & edge-level SSL, G for representing graph-level SSL, and NEG for representing node-, edge-, & graph-level SSL

Dataset size	R^2 of EA				R^2 of IP			
	Baseline	NE	G	NEG	Baseline	NE	G	NEG
0.08%	0.357	0.495	0.413	0.472	0.418	0.577	0.511	0.515
0.16%	0.383	0.413	0.418	0.461	0.417	0.533	0.522	0.508
0.24%	0.583	0.616	0.619	0.695	0.541	0.793	0.619	0.759
0.32%	0.555	0.644	0.585	0.706	0.546	0.800	0.645	0.744
0.4%	0.631	0.704	0.643	0.744	0.646	0.813	0.695	0.812
0.8%	0.664	0.779	0.709	0.805	0.762	0.850	0.791	0.869
1.6%	0.789	0.878	0.824	0.883	0.868	0.920	0.894	0.926
2.4%	0.867	0.912	0.867	0.919	0.927	0.947	0.924	0.943
3.2%	0.918	0.949	0.912	0.946	0.955	0.967	0.942	0.960
4%	0.949	0.969	0.939	0.961	0.968	0.976	0.963	0.968
8%	0.982	0.987	0.979	0.983	0.985	0.989	0.987	0.988
16%	0.991	0.992	0.989	0.991	0.992	0.994	0.993	0.993
24%	0.993	0.995	0.993	0.994	0.994	0.995	0.995	0.995
32%	0.994	0.995	0.995	0.995	0.994	0.996	0.995	0.996
40%	0.995	0.996	0.995	0.996	0.996	0.997	0.996	0.997



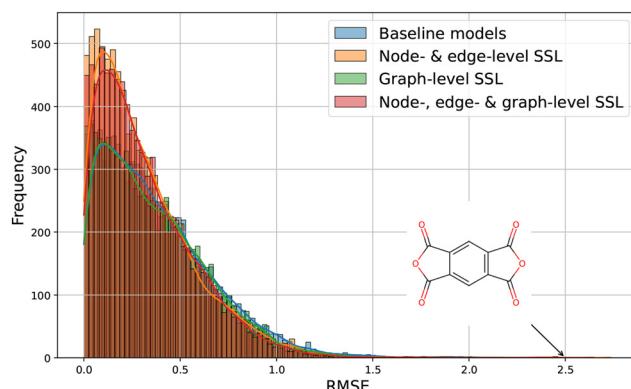
Table 4 RMSE of predicting the EA and IP labels using different sizes of datasets for the fine-tuning part and the corresponding standard deviation can be found in ESI.† Specifically, we use baseline for representing baseline models, NE for representing node- & edge-level SSL, G for representing graph-level SSL, and NEG for representing node-, edge-, & graph-level SSL

Dataset size	RMSE of EA				RMSE of IP			
	Baseline	NE	G	NEG	Baseline	NE	G	NEG
0.08%	0.479	0.424	0.457	0.433	0.372	0.317	0.341	0.340
0.16%	0.469	0.456	0.455	0.436	0.372	0.332	0.337	0.342
0.24%	0.386	0.370	0.369	0.329	0.330	0.222	0.299	0.239
0.32%	0.398	0.356	0.385	0.323	0.329	0.218	0.290	0.247
0.4%	0.362	0.324	0.357	0.302	0.290	0.211	0.269	0.211
0.8%	0.346	0.280	0.322	0.263	0.238	0.189	0.223	0.177
1.6%	0.273	0.208	0.250	0.204	0.177	0.138	0.159	0.133
2.4%	0.217	0.177	0.217	0.169	0.132	0.112	0.134	0.116
3.2%	0.170	0.134	0.177	0.138	0.103	0.089	0.116	0.098
4%	0.134	0.105	0.146	0.117	0.086	0.075	0.094	0.087
8%	0.080	0.069	0.085	0.077	0.060	0.051	0.057	0.054
16%	0.057	0.052	0.063	0.056	0.044	0.037	0.042	0.040
24%	0.051	0.044	0.049	0.047	0.036	0.033	0.035	0.033
32%	0.045	0.042	0.044	0.042	0.031	0.029	0.031	0.029
40%	0.042	0.037	0.041	0.038	0.030	0.028	0.027	0.027

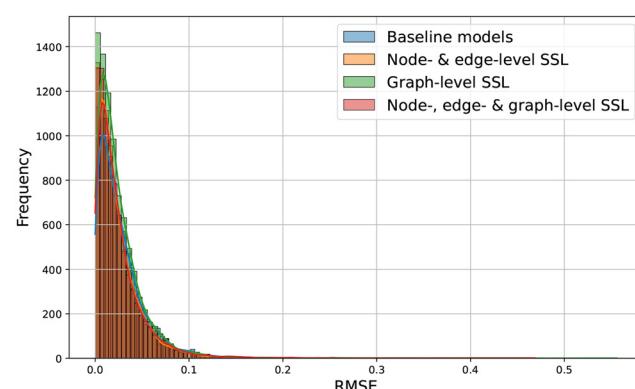
in the small labeled data regimes, SSL significantly enhances the prediction performance.

In the data regimes from 0.4% to 4%, node- and edge-level SSL, as well as node-, edge- & graph-level SSL, still boost the performance for both R^2 and RMSE compared with

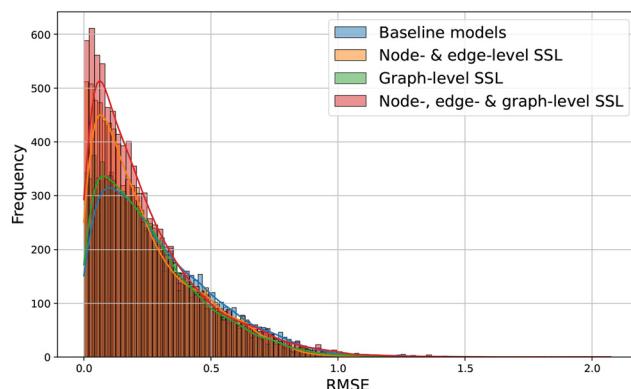
baseline models. However, graph-level SSL exhibits less significant improvements and even negative contributions compared with baseline models. A potential reason is that the chosen pseudo label (ensemble molecular weight) has a discrepancy with target labels EA and IP.



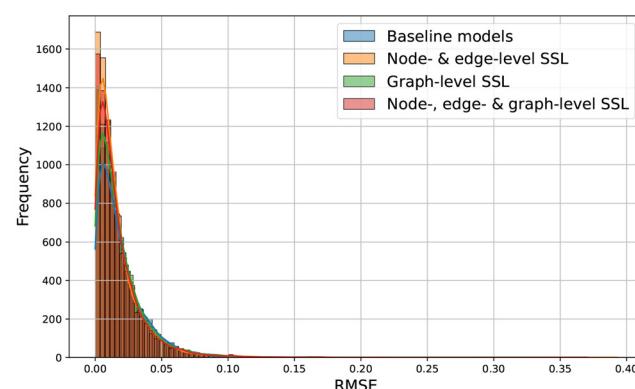
(a) 0.08% fine-tuning dataset for EA



(b) 24% fine-tuning dataset for EA



(c) 0.08% fine-tuning dataset for IP



(d) 24% fine-tuning dataset for IP

Fig. 8 Error distribution for EA and IP with fine-tuning dataset 0.08% and 24%, respectively.



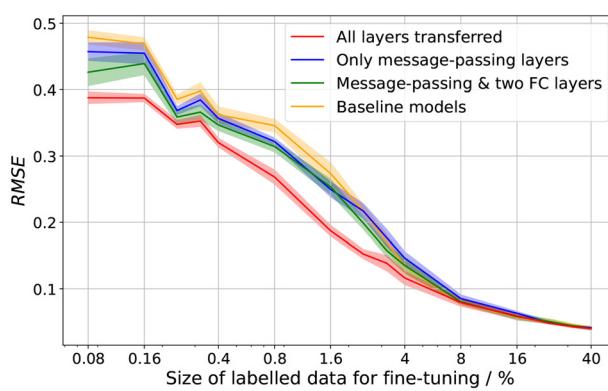
As for larger labeled data regimes (e.g., >4%), the differences between the models become smaller (potentially neglectable) regarding both performance metrics and property labels. A plausible explanation is that with larger fine-tuning dataset availability, the graph semantics can be learned directly through the target label in the supervised fine-tuning phase, which improves the final prediction together with the pre-training SSL phase.

We further analyzed the error distribution of all four models for predicting EA and IP (see Fig. 8). First, it is evident that all error distributions follow a long-tail pattern, indicating that while the majority of predictions are accurate (low RMSE), there are a few significant outliers. In the smallest labeled data regime (0.08%), both for EA and IP, graph-level pre-training contributes minimally to performance improvement, as indicated by error distributions close to those of the baseline models. In contrast, the node-, edge-level, and combined node-, edge-, and graph-level SSL models demonstrate superior performance, with error distributions peaking over 500 with slightly lower RMSE and being narrower for both EA and IP. Notably, for EA, all models struggle to predict polymers containing pyromellitic dianhydride (PMDA) as Fig. 8 shows. This difficulty likely arises

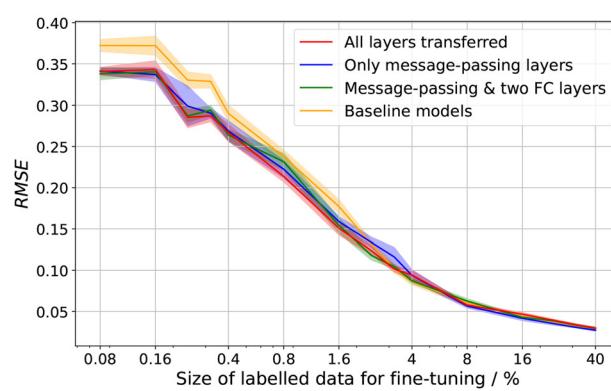
from PMDA's strong electron-withdrawing properties due to the presence of anhydride groups, complicating EA predictions. Additionally, only 63 out of 42 966 samples contain PMDA, and this data scarcity contributes to poor generalization. Conversely, for IP, there is no common failure pattern in the predictions for specific polymers. In the larger labeled data regime (24%), significant improvements are observed for both EA and IP, with RMSE distributions becoming narrower. For both properties, SSL models continue to outperform baseline models, demonstrated by higher peaks with slightly lower RMSE and narrower error distributions. Overall, node- and edge-level SSL, as well as node-, edge- & graph-level SSL, exhibit consistently better performance than the baseline supervised-learning results even in the biggest labeled data regime. For example, the R^2 still increases by 0.1% and 0.1% for both EA and IP for node-, edge- & graph-level SSL.

3.2 Transferring fully connected layers

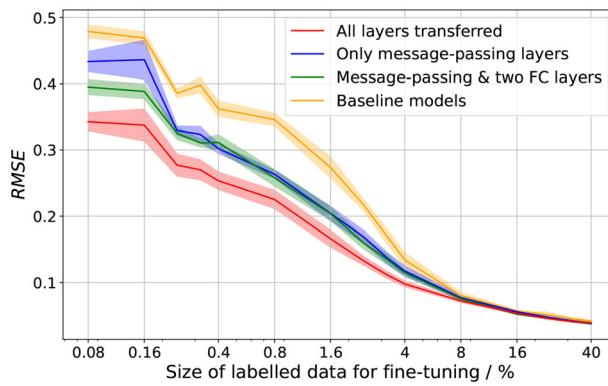
In this section, we present and discuss the impact of the layer transfer strategy within SSL for both graph-level SSL and node-, edge- & graph-level, respectively. Fig. 9,



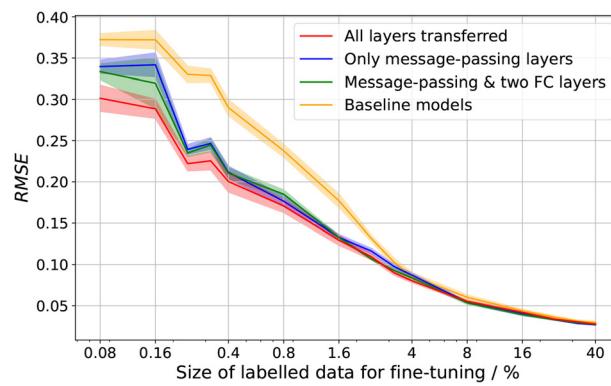
(a) Graph-level SSL of $RMSE$ results for EA



(b) Graph-level SSL of $RMSE$ results for IP



(c) Node-, edge- & graph-level SSL of $RMSE$ results for EA



(d) Node-, edge- & graph-level SSL of $RMSE$ results for IP

Fig. 9 Graph-level and node-, edge- & graph-level SSL of RMSE results for both EA and IP. The results are from supervised-only, transferring only message-passing layers (strategy a) indicated in green in all four subplots, transferring message-passing & two fully connected layers (strategy b) indicated in blue in all four subplots, and transferring all layers (strategy c) indicated in red in all four subplots. Each line is the mean from 10 individual runs and the shaded area is the 95% confidence interval.



Table 5 RMSE of predicting the EA and IP labels using different sizes of datasets for transferring different fully connected layers in graph-level SSL and the corresponding standard deviation can be found in ESI.† Specifically, we use baseline for representing baseline models, G for representing graph-level SSL without transferring fully connected layers, G2 for representing graph-level SSL without transferring two fully connected layers, and G3 for representing graph-level SSL without transferring all fully connected layers

Dataset size	RMSE of EA				RMSE of IP			
	Baseline	G	G2	G3	Baseline	G	G2	G3
0.08%	0.479	0.457	0.426	0.388	0.372	0.341	0.338	0.341
0.16%	0.469	0.455	0.439	0.388	0.372	0.337	0.340	0.343
0.24%	0.386	0.369	0.359	0.348	0.330	0.299	0.287	0.285
0.32%	0.398	0.385	0.366	0.353	0.329	0.290	0.294	0.287
0.4%	0.362	0.357	0.347	0.320	0.290	0.269	0.264	0.267
0.8%	0.346	0.322	0.314	0.268	0.238	0.223	0.231	0.214
1.6%	0.273	0.250	0.253	0.187	0.177	0.159	0.154	0.151
2.4%	0.217	0.217	0.198	0.152	0.132	0.134	0.118	0.124
3.2%	0.170	0.177	0.158	0.139	0.103	0.116	0.104	0.102
4%	0.134	0.146	0.135	0.116	0.086	0.094	0.087	0.094
8%	0.080	0.085	0.080	0.079	0.060	0.057	0.063	0.058
16%	0.057	0.063	0.058	0.059	0.044	0.042	0.043	0.047
24%	0.051	0.049	0.051	0.048	0.036	0.035	0.039	0.039
32%	0.045	0.049	0.044	0.043	0.031	0.031	0.033	0.033
40%	0.042	0.041	0.040	0.040	0.030	0.027	0.030	0.030

Tables 5 and 6 show the RMSE results with our three different transfer strategies for both EA and IP. Here we only show the RMSE results as the R^2 renounces in the same trend. In the labeled data regimes $<4\%$, we observe a pronounced difference when transferring all layers (strategy c) for the prediction of the label EA in contrast to the baseline model and the two other strategies where fewer layers are transferred. This holds both for graph-level SSL and node-, edge- & graph-level SSL. For example, the RMSE significantly decreases by 15.10% and 20.79% compared to strategy a, where only message-passing layers are transferred, for both graph-level SSL and node-, edge- & graph-level SSL, respectively. Strategy a and b also outperform the baseline models in all low data availability scenarios, yet less significantly than strategy c. On the other

hand, when predicting the IP, the three strategies for graph-level SSL have a similar performance in terms of RMSE and show a less significant improvement over the baseline model. For node-, edge-, and graph-level SSL, all three strategies still exhibit a similar performance but improve the prediction significantly compared to the baseline model. For example, the RMSE of strategy c decreases by 19.09% compared to the baseline model in the smallest data scenario (0.08%). This indicates that during the node- & edge-level SSL pre-training, the learned semantics are additionally embedded in the message passing layers, which significantly contributes to predicting the target labels in the downstream tasks.

In the labeled data regime (e.g., $>4\%$), the impact of transferring fully connected layers becomes less significant:

Table 6 RMSE of predicting the EA and IP labels using different sizes of datasets for transferring different fully connected layers in node-, edge- & graph-level SSL and the corresponding standard deviation can be found in ESI.† Specifically, we use baseline for representing baseline models, NEG for representing node-, edge- & graph-level SSL without transferring fully connected layers, NEG2 for representing node-, edge- & graph-level SSL without transferring two fully connected layers, and NEG3 for representing node-, edge- & graph-level SSL without transferring all fully connected layers

Dataset size	RMSE of EA				RMSE of IP			
	Baseline	NEG	NEG2	NEG3	Baseline	NEG	NEG2	NEG3
0.08%	0.479	0.433	0.395	0.343	0.372	0.340	0.333	0.301
0.16%	0.469	0.436	0.389	0.338	0.372	0.342	0.320	0.289
0.24%	0.386	0.329	0.325	0.277	0.330	0.239	0.235	0.222
0.32%	0.398	0.323	0.311	0.270	0.329	0.247	0.245	0.226
0.4%	0.362	0.302	0.311	0.253	0.290	0.211	0.211	0.200
0.8%	0.346	0.263	0.258	0.225	0.238	0.177	0.185	0.171
1.6%	0.273	0.204	0.204	0.166	0.177	0.133	0.133	0.129
2.4%	0.217	0.169	0.160	0.133	0.132	0.108	0.107	0.110
3.2%	0.170	0.138	0.136	0.112	0.103	0.093	0.093	0.090
4%	0.134	0.117	0.115	0.098	0.086	0.087	0.084	0.080
8%	0.080	0.077	0.076	0.072	0.060	0.054	0.053	0.055
16%	0.057	0.056	0.052	0.054	0.044	0.039	0.039	0.042
24%	0.051	0.047	0.046	0.045	0.036	0.033	0.033	0.034
32%	0.045	0.042	0.041	0.041	0.031	0.029	0.029	0.030
40%	0.042	0.038	0.038	0.039	0.030	0.028	0.028	0.028



the importance of SSL decreases as shown by the performance curves approaching each other. For node-, edge- & graph-level SSL, strategy c is still consistently better than the baseline models for both EA and IP. However, for IP, we do observe a slightly negative contribution (4%) from strategy c compared to the baseline model for graph-level SSL. A plausible explanation is that graph-level SSL indeed has a negative contribution in the larger labeled data regime as we observed before. The chosen pseudo label from the pre-training phase is not sufficiently informative for the target label IP, and the learned semantics stored in the fully connected layer introduce extra bias during the pre-training and thereby hinder further learning in fine-tuning.

To sum it up, the extent of transferred weights impacts the overall performance of SSL in the two case studies investigated in our work. In small fine-tuning dataset scenarios (e.g., <0.4%), all transferal strategies perform better than the baseline models in both prediction tasks and both SSL scenarios. For both EA and IP, strategy c where most layers were transferred demonstrates the best performance, which decreases the RMSE by 28.39% and 19.09% respectively, compared to the baseline models for node-, edge- & graph-level SSL. In larger fine-tuning dataset scenarios, the differences become less pronounced as the impact of SSL decreases. Here, scenario c, where most layers are transferred, also showed to perform slightly worse than the baseline model for IP. Thus, we showed that next to the design of the molecular-topology based pseudo-tasks, additional design decisions on the extent of layer transfer are important for designing best performing SSL pipelines.

4 Conclusions

We propose a first SSL framework using GNNs for polymer property prediction to address the challenge of improved learning from small polymer datasets. We employ a state-of-the-art polymer graph representation and a wD-MPNN architecture to process polymer graphs. Our contribution investigates three different SSL techniques: (i) node- and edge-level SSL, (ii) graph-level SSL (iii) node-, edge- & graph-level SSL. Furthermore, we explore the impacts of different weight transfer strategies for the fully connected layers. The results show that SSL indeed boosts R^2 32.21% and 23.21% for EA and IP respectively, especially when labeled data is extremely limited (0.08%) for the fine-tuning phase (our two smallest data size scenarios). Additionally, SSL can still contribute to augmenting the R^2 by 0.1% and 0.1% for EA and IP, even in the largest labeled data regime. Moreover, we highlighted the impact of layer transferal during SSL, where transferring all fully connected layers was advantageous in small data scenarios. Overall, the ensemble node-, edge- & graph-level SSL with all transferred layers depicts the best performance. It

decreases the RMSE by 28.39% and 19.09% for EA and IP, respectively. Our results contribute to well-reasoned and improved SSL pipelines in the field of polymer property prediction. Our current study introduces a single graph pseudo label and one node/edge masking strategy. Future research could explore the extension to multiple graph pseudo labels and diverse node/edge masking strategies. Additionally, subsequent work may consider integrating various datasets to evaluate the robustness of the proposed SSL framework. Moreover, a promising future investigation is the integration of SSL with quantitative structure-activity relationship (QSAR) or QSPR modeling for predicting polymer properties. For instance, one approach could involve masking a specific property within the descriptors and predicting the masked property during the pre-training phase. This pre-trained model could then be fine-tuned using the target property dataset.

Data availability

This study was carried out using publicly available data (dataset with electron affinity and ionization potential values for 42 966 copolymers) from polymer-chemprop-data at <https://github.com/coleygroup/polymer-chemprop-data>. The data supporting this article have been included as part of the ESI.†

Conflicts of interest

There are no conflicts to declare.

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