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A spin and intensity multiplexed encryption metasurface

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Recently, metasurfaces have received widespread attention due to their superior performance in regulating the physical properties of light. In the field of optical encryption, the most common methods utilizing metasurfaces mainly include metasurface coloration, malus metasurfaces and metasurface holography. However, such methods are complex to achieve and prone to noise interference. Here, a spin and intensity multiplexed compact metasurface optical element is proposed and its feasibility for stable optical encryption is verified through simulations. Based on the photon spin Hall effect, a series of optical ciphertexts are generated with continuous changes in the spin state and intensity. As a concept demonstration, this spin and intensity multiplexed encryption metasurface will promote advanced applications of metasurfaces in many fields, such as optical communication and holography.

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Introduction

A metasurface is an artificial structure array composed of a large number of sub-wavelength unit structures arranged on two-dimensional planes, which arbitrarily can modulate various parameters of incident electromagnetic waves, including phase,^{1–3} wavelength,^{4–6} polarization,^{7–10} orbital angular momentum,^{11–13} etc. It is precisely because of these unique advantages that metasurfaces have become the perfect carrier for wavefront regulation.^{14–19} Generally speaking, in order to achieve specific functions, it is necessary to design the arrangement of meta-atoms. Due to the existence of spin-orbit interactions in anisotropic structures, the local additional geometric phase generated by meta-atoms can be induced by rotation. Because of the convenience of geometric phase modulation, this method has been widely applied in various fields, such as optical displays, optical communication, optical holography, optical micromanipulation, etc.^{20–28}

One of the most important application fields of metasurfaces is optical encryption.^{29–31} With the rapid development of optical and wireless communication, the security and stability of optical information transmissions

are receiving increasing attention. In current research, optical encryption using metasurfaces has been achieved with many methods, including metasurface coloration, malus metasurfaces, and metasurface holography.¹⁸ For these methods, the principles are different. For example, metasurface coloration usually achieves the encryption function through resonance and malus metasurfaces use the Malus law to regulate the orthogonal polarization state and achieve encryption. As for metasurface holography, this is mainly based on using holographic algorithms to obtain encryption. These three commonly used optical encryption methods can indeed hide information with high security. However, due to processing errors and mechanism limitations, there is inevitably crosstalk in complex optical encryption systems, which leads to errors in encryption and reading.

Here, we propose a spin and intensity multiplexed metasurface with an area of $11.4 \times 22.8 \mu\text{m}^2$ to achieve stable optical encryption communication of text information. The simulated change rate of the full width half maximum (FWHM) and diameter of the focal spot profiles were calculated as $\alpha_1 = 3.85 \text{ nm nm}^{-1}$ and $\alpha_2 = 13.25 \text{ nm nm}^{-1}$, respectively. By changing the intensity and spin state of the incident light, four different output states are obtained. Subsequently, through encoding the output states with binary digital signals, the optical ciphertext is achieved. Finally, by reverse decoding the optical ciphertext, optical encryption based on the design of metasurfaces is ultimately achieved. Compared with other types of optical encryption, this work proposes a simple method for encoding and transmitting

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information with changes of spin state and intensity. Therefore, this work proposes a scheme for the application of spin and intensity multiplexed metasurfaces in optical encryption and verifies it through simulation.

Results and discussion

In order to manipulate the light field phase with the modulation principle of the Pancharatnam–Berry phase (P–B phase), highly anisotropic structures need to be constructed. Among them, cubic structures are an ideal solid geometry due to their ease of manufacturing. In addition, the high refractive index and high transmittance of silicon (Si) in the infrared band also indicate that it is a great material for metasurfaces. As shown in Fig. 1(a), cubic Si nanopillars are designed as the meta-atom of the array, and the substrate material is silica (SiO_2). The length and width of the Si nanopillars are denoted by L and W , respectively, while the height is H , and the period of the meta-atoms is P . For incident light with the $|+\sigma\rangle$ spin state, the outgoing light will be a mixture of the $|+\sigma\rangle$ state and the $|-\sigma\rangle$ state, where the $|\pm\sigma\rangle$ spin states represent left and right circularly polarized light, respectively. Assuming that the rotation angle of the meta-atom is θ , the propagation phase will change correspondingly with the change of the propagation position of the light. According to the equivalent refractive index theory, the propagation phase generated at each position will not change because the size of the meta-atoms is the same. However, except for the propagation phase, the rotation angle θ of the meta-atoms will produce an additional geometric phase $\Phi_{\text{ge}} = e^{i2\theta}$ due to the anisotropy of the meta-atoms. The Jones matrix of the total outgoing electric field can be calculated as follows:³²

$$E_{\text{out}} = \frac{T_l + T_s}{2} \begin{bmatrix} 1 \\ \mp i \end{bmatrix} + \frac{T_l - T_s}{2} e^{\pm i2\theta} \begin{bmatrix} 1 \\ \pm i \end{bmatrix} \quad (1)$$

where T_l and T_s represent the transmittance coefficients along the major and minor axes of the meta-atoms, respectively. Based on this principle, the phase of the light field can be modulated with the function of the rotation angle $\theta(r)$, which represents the phase at the position of each meta-atom. For the geometric phase, in order to obtain the best focusing effect, the polarization conversion ratio (PCR) and transmittance are simulated with different values of L and W , as shown in Fig. 1(b) and (c). The PCR can be calculated using the following equation: $\text{PCR} = T_{21}/(T_{21} + T_{11})$ and $T = I_{\text{out}}/I_{\text{in}}$, where T_{xy} represents the polarization conversion efficiency from state $|y\rangle$ to state $|x\rangle$. In order to get a higher diffraction efficiency, the PCR of the meta-atoms should be as large as possible. The height of the meta-atom is fixed at 500 nm. For incident light at the wavelength of 1310 nm, the maximum PCR of about 72.0% is calculated with meta-atoms of $L = 340$ nm and $W = 150$ nm. In this case, although it is not a complete half wave plate behavior, it can still be approximated as a half wave plate and can be used to rotate the polarization direction. It should be noted that the degree of approximation may vary with different PCR. The higher the conversion rate, the closer it is to the ideal half wave plate behavior. Therefore, the structure parameters corresponding to the maximum PCR value of 72% are chosen. With the same parameters, the transmittance of meta-atoms is about 52.8%. Different from them, T is used to represent the ratio of the intensity of the incident and outgoing light, which is shown as the following equation: $T = I_{\text{out}}/I_{\text{in}}$, where I_{out} represents the intensity of outgoing light and I_{in} represents that of incident light. In addition, the meta-atoms can also operate in the O-band of the optical communication range around 1310 nm due to the broadband property, as shown in Fig. 1(d). At the operating wavelength of 1310 nm, the Si nanopillar structure has a strong field confinement ability due to the high refractive index contrast between Si and SiO_2 . In order to ensure that adjacent meta-atoms can have independent regulatory effects on the phase of the electromagnetic field, the finite-difference time-domain (FDTD) method is used to calculate the field distribution around the meta-atoms, as shown in Fig. 1(e). As can be seen, the magnetic field is tightly bound within or near the cubic Si waveguide and the coupling between adjacent meta-atoms is weak, which indicates that there is little interference between the meta-atoms during the transmission of the light field.

For any electromagnetic wave, the Stokes parameters can be obtained by using at least four parameters, and the calculation process of the polarization state change can be further simplified. As shown in Fig. 2(a), a Poincaré sphere is often used to describe different states of polarization. In order to achieve the convergence function, we usually use the following hyperbolic phase cross-polarization focusing formula:³³

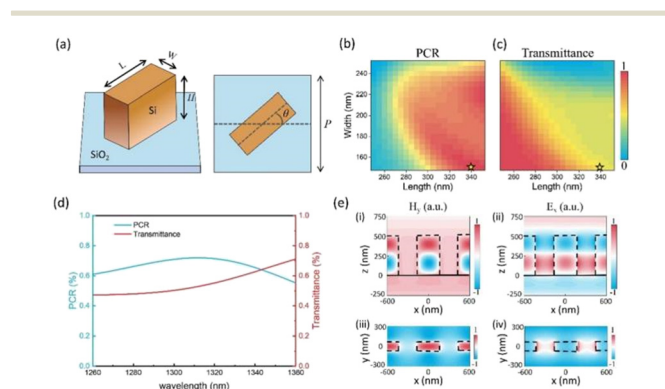


Fig. 1 (a) Schematic of the designed meta-atom consisting of a SiO_2 substrate and Si cubic nanopillars with $P = 600$ nm and $H = 500$ nm. (b) and (c) Simulated maximum PCR and transmittance of the meta-atoms with the variation of the length and width at the wavelength of 1310 nm. The PCR and transmittance are calculated at different L (from 250 nm to 350 nm) and W (from 150 nm to 250 nm). (d) Plot of PCR and transmittance as a function of wavelength. The blue and red lines represent the data of PCR and transmittance. (e) Simulated amplitude distribution of the electromagnetic field around the meta-atom: (i) and (iii) the amplitude distribution of the y-component magnetic field, and (ii) and (iv) the amplitude distribution of the x-component electric field.



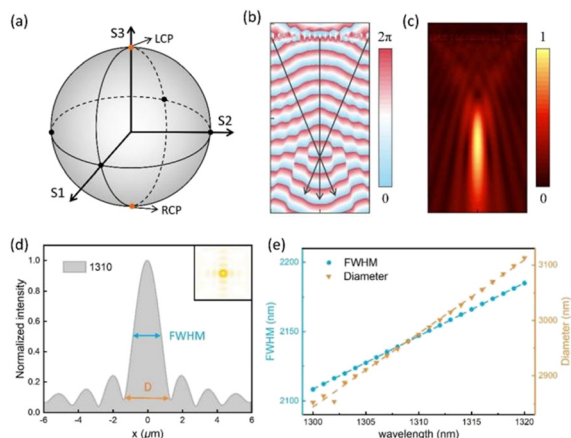


Fig. 2 (a) Stokes parameters of the incident and outgoing light (orange dots) plotted on the Poincaré sphere. (b) and (c) Simulated phase and intensity distribution of the metasurface in the x - z plane at the wavelength of 1310 nm. (d) Simulated normalized intensity line profile of the focal plane. Inset shows the focus intensity distribution. (e) Plot of simulated FWHM (blue) and diameter (orange) as a function of wavelength from 1300 to 1320 nm.

$$\varphi(x_i, y_i; f) = -\frac{2\pi}{\lambda} \left(\sqrt{x_i^2 + y_i^2 + f^2} - f \right) \quad (2)$$

Here, λ is the wavelength of the incident light, x_i and y_i are the coordinates of the location of the meta-atoms, and f is the focal length, which is designed to be 10 μm . Due to the existence of the geometric phase, the rotation angle of the meta-atoms can be arranged and designed in combination to achieve the function of cross-polarization focusing with formula (2). Then, using the left circularly polarized incident light as the source, the convergence function of transmitted light is realized. The electromagnetic field is simulated according to the finite integral technique (FIT) method, and the calculated phase and normalized intensity distributions are shown in Fig. 2(b) and (c), respectively. In the calculation process, an array of 19×19 meta-atoms are selected, where the total area size of the metasurface is $11.4 \times 11.4 \mu\text{m}^2$. As can be seen from Fig. 2(b), after the phase modulation effects of the metasurface, the wavefront has changed to an arc on the x - z plane. In other words, the direction of light propagation perpendicular to the wavefront will eventually focus on a point in space.

Compared with the traditional focusing lens, the designed metasurface has the unique advantage of a small focusing spot size, and not being easily distorted, which mainly comes from the metasurface characteristics of small size and high integration. To evaluate the focusing spot size of the metasurface, the intensity line profile of the focus plane is further simulated, as shown in Fig. 2(d). For incident light of 1310 nm, the focusing beam diameter of the designed metasurface is about 2.975 μm . Meanwhile, the simulated focus area only accounts for about 21.4% of the metasurface area. In order to

further verify the sensitivity of the metasurface to the change of incident light wavelength, the diameter and FWHM of the focus spot are simulated at different wavelengths from 1300 to 1320 nm. The relevant results are shown in Fig. 2(e). It can be seen from this figure that the FWHM of the light spot shows a great near-linear change relationship within the range of wavelength change. Therefore, through linear fitting of the data, the calculated linearity coefficients are $\alpha_1 = 3.85 \text{ nm nm}^{-1}$ and $\alpha_2 = 13.25 \text{ nm nm}^{-1}$, where α_1 and α_2 represent the change rate of the focus spot FWHM and diameter, respectively. This means that even tiny wavelength changes and subtle fluctuations of the incident light can be distinguished by measuring the FWHM and diameter change. With this method, the change of FWHM and diameter can be used to determine if the wavelength is 1310 nm. In optical communication systems, wavelength stability is crucial. For optical signals with the operating wavelength at 1310 nm, even subtle fluctuations in wavelength can have a serious impact on the overall transmission performance. Firstly, wavelength deviation from the optimal range of 1310 nm will lead to increased fiber optic transmission loss, thereby reducing the signal power and shortening the communication distance. At the same time, the dispersion effect will also intensify, causing signal distortion and inter-symbol interference, limiting the transmission rate and bandwidth of the system. In addition, various optoelectronic devices in communication systems, such as light sources, optical fibers, optical amplifiers, *etc.*, are optimized and designed for the 1310 nm wavelength. If the wavelength shifts, the performance and compatibility of these devices will decrease, increasing the difficulty of system integration. Therefore, a tiny change of wavelength can lead to a series of problems and decreased performance of optical devices. This not only reduces the performance and reliability of the entire communication system, but also increases the difficulty of maintenance and repair. Therefore, maintaining high stability of the 1310 nm wavelength is one of the most important goals of optical communication systems. Through the methods mentioned in this work, we can ensure that the wavelength is 1310 nm, achieving the function of spectral purification.

In order to detect the $|\pm\rangle$ spin states simultaneously, we construct an array of 2×1 metasurfaces. The related phase gradients are shown as follows:

$$\varphi(x_i, y_i; f) = \begin{cases} -\frac{2\pi}{\lambda} \left(\sqrt{x_i^2 + y_i^2 + f^2} - f \right), & x_i < 0 \\ \frac{2\pi}{\lambda} \left(\sqrt{x_i^2 + y_i^2 + f^2} - f \right), & x_i > 0 \end{cases} \quad (3)$$

Here, $x_i = 0$ is the boundary of two different functional regions. These two regions have similar functions of convergence but opposite effects, as is shown below:



$$\begin{aligned} |+\sigma\rangle &\rightarrow e^{i2\theta} |-\sigma\rangle \\ |-\sigma\rangle &\rightarrow e^{-i2\theta} |+\sigma\rangle \end{aligned} \quad (4)$$

Due to the photonic spin Hall effect, these two sub-metasurfaces can achieve the function of converging photons with opposite spin angular momentum. If each sub-metasurface is regarded as a pixel, multiple pixels consisting of sub-metasurface arrays can realize the detection of the intensity and spin state of incident light. Based on this principle, optical encryption can be achieved with a metasurface array.

Fig. 3(a) and (b) show the phase distributions of the sub-metasurfaces of the array, which are calculated by formula (3). With the combination of two sub-metasurfaces, the metasurface array containing two pixels can be constructed. Fig. 3(c) shows the calculated phase profile of the line along the symmetric center line $y = 0$. When the intensity and spin state of the incident light change, the intensity and lateral position of the focus spot on the fixed object surface will also change. By changing the incident light state $|I_{\text{in}}, \pm\sigma\rangle$, four different states of optical output are obtained by simulation. Simulated intensity profiles of the focal plane and intensity curves of the focal spot are shown in Fig. 3(d). In the process of optical communication, information is usually converted into binary digit (bits) for transmission. Due to the involvement of two physical parameters in optical encryption, an optical ciphertext consists of two bits of information. The optical ciphertext represents different states of incident light, where the first bit of information represents intensity and the second bit of information represents spin state. For example, the optical ciphertext “00” means that the incident light has low intensity of the $|+\sigma\rangle$ spin state. As a result, the conversion between the bit signal and the optical ciphertext is attainable, which serves as the fundamental principle for optical encoding and decoding.

Furthermore, to achieve the encryption of a series of bits and continuous optical encryption, the designed metasurface

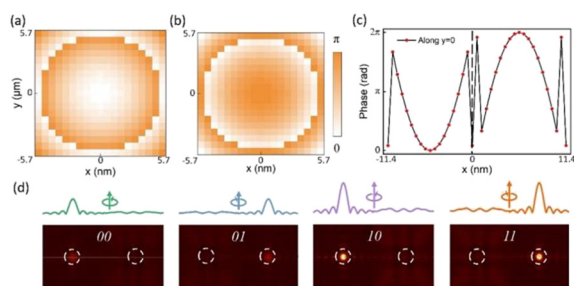


Fig. 3 (a) and (b) Calculated rotation angle distribution of the designed 2×1 metasurface arrays with opposite functions. (c) The rotation angle profile of the line along $y = 0$. (d) Four different simulated optical outputs and corresponding standard ciphers, where the white dashed circular box represents the two focal areas. The upper image shows the intensity curves of the focal spot and the corresponding intensity and spin state of incident light. The lower image shows the intensity profiles of the focal plane.

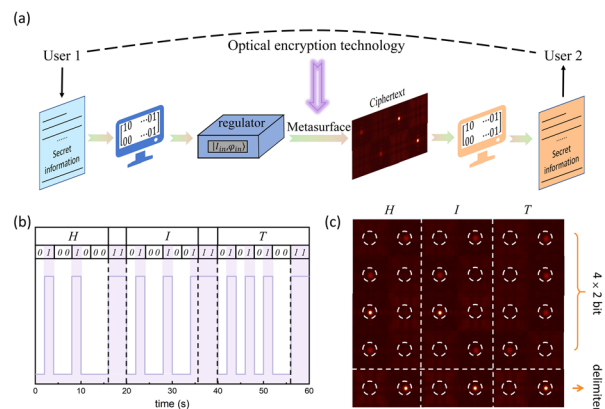


Fig. 4 (a) Schematic diagram of the optical encryption system based on the designed metasurface optical element. (b) The input and output signals of converting ACSII code “HIT” in the optical encryption system. There is a delimiter “11” between the letters. (c) Simulated optical ciphertext of secret information “HIT”.

serves as a converter between bits and optical ciphertext, as shown in Fig. 4(a). Here, user 1 wants to transmit high confidentiality secret information to user 2, taking “HIT” text content as an example. First of all, the “HIT” needs to be converted into bit signals with a combination of 0 and 1. As a process demonstration, American Standard Code for Information Interchange (ASCII) is used for the conversion of “HIT”, and the bit signal result is shown in Fig. 4(b). Between each letter, a “11” is inserted as a delimiter to identify the position of letter separation. Next, the bit signals are input into the regulator. With the continuous change of incident light, a series of optical ciphertexts can ultimately be obtained from CCD, as shown in Fig. 4(c). For every letter, the ciphertext in each column changes over time from top to bottom. In this process, each letter contains 5 optical ciphertexts due to a delimiter being included. To decode and translate the secret message, it is necessary for user 2 to compare the optical ciphertext with the standard ciphers. With the help of specially designed software, the “HIT” text encryption information can be decoded and transmitted accurately. Therefore, by using the method proposed above, optical encryption can be achieved with the designed metasurface array.

Method

The numerical simulation

The silicon metasurface is numerically simulated with the FIT and FDTD method. The Si nanopillars are placed on a SiO_2 substrate with refractive indices of 3.50 and 1.45 at 1310 nm. The height of the nanopillars is fixed at 500 nm, the period at 600 nm and the lengths and widths are L and W , respectively. The polarization conversion ratio (PCR) and intensity transmittance are obtained (shown in Fig. 1) by parameter sweeping of the in-plane dimensions (L and W).



Conclusions

In summary, a spin and intensity multiplexed metasurface has been proposed and the feasibility of the designed metasurface for stable optical encryption has been verified by simulation. A metasurface with an area of $11.4 \times 22.8 \mu\text{m}^2$ has been designed with the hyperbolic phase distribution formula of cross-polarization focusing, which operates at the wavelength of 1310 nm. By simulating the distribution of the electromagnetic field in the image space of the metasurface, the FWHM and diameter change rate of the focal plane intensity profile are calculated as $\alpha_1 = 3.85 \text{ nm nm}^{-1}$ and $\alpha_2 = 13.25 \text{ nm nm}^{-1}$, which verifies the frequency stability in optical communication. In addition, the designed 2×1 metasurface array element can produce four different optical outputs by changing the intensity and spin state of the incident light. By encoding the generated four states of optical output with binary digital signals, the concept of the proposed optical encryption has been finally realized. This work proves the advantages of metasurfaces in optical encryption, and further promotes the application of metasurface optical elements in many fields, such as optical information multiplexing, optical encryption, optical data storage, etc.

Conflicts of interest

There are no conflicts to declare.

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