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Triple-chain boron clusters: lengthening *via* phosphorus doping and enhancing stability through {P} by {CH} substitution†

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This theoretical study presents novel insights into the doping of boron clusters with an increasing number of dopant atoms, ranging from 1 to 4, that preserve the integrity of the original boron framework. The triple-chain forms of clusters B_{10} and B_{16} remain unchanged upon sequential addition of P atoms, showcasing a perfect isolobal substitution of {P} with {CH}. Similarities in the number of delocalized electrons are observed between pure and doped boron clusters, alongside the subsequent substitution of {P} with {CH}. All triple-chain structures exhibit high thermodynamic stability, having low vertical attachment energies and high vertical ionization energies. The lowest-lying isomer of $B_{16}P_4$ has thus a triple-chain shape instead of a tetrahedral T_d form as previously reported. While AdNDP analysis confirms the number of globally delocalized electrons, it differs much from a previous interpretation. The magnetic ring current maps support the double aromaticity of triple-chain structures. Electron counting rules established for triple-chain structures are verified. The particle-in-a-rectangular-box model elucidates the relationship between the structure size and electron configuration and aids in understanding the transition from anti-aromatic to aromatic configurations. The self-locking phenomenon is crucial for adhering to the triple-chain model and satisfying electron configuration requirements.

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1. Introduction

The field of nanocluster science has continuously developed over the past few decades, and the growth mechanisms of the clusters of several elements have gradually emerged. Of the atomic clusters investigated, those formed by the boron atom exhibit the most diverse and non-conventional structural motifs and unpredictable geometry transformations following a small change in the size, net charge, and doping.¹ In a series of small pure clusters, going from B_3 to B_{19} , they are either

planar or quasi-planar ($2D$)^{2,3} with a fullerene-like intercalation of the size of B_{14} .⁴ The size of B_{20} is renowned for its double ring (DR) tubular structure;⁵ after which the B_n class returns to the quasi-planar B_{21} class.⁶ At larger sizes, there is still an alternating occurrence of the global minima between 2D and 3D structures.^{7–12} Due to such a geometric diversity of boron clusters, various models of electronic structures have been proposed to rationalize their thermodynamic stability, and in particular their aromatic nature which in part governs their stability. Boron clusters appear to challenge the classical models of chemical bonding, requiring the introduction of numerous new electron count models that also necessitate a redefinition of the aromaticity concept.^{13,14}

For small size clusters, the classical Hückel rule proves effective for most planar and quasi-planar structures.^{15,16} However, for circular structures such as the anion B_{19}^- ,^{17,18} or the dianion B_{20}^{2-} ,¹⁹ the Hückel model becomes inadequate; in fact, it failed to rationalize their aromatic character. Instead, the disk aromaticity model^{19–21} has proved to be more appropriate for the circular disk and even generalizable for a larger class of planar and bowl structures.

Instead of using the $2(N + 1)^2$ electron count of the Hirsch rule²² or the phenomenological shell model (PSM),²³ the hollow cylinder model^{24,25} provides us with a better under-

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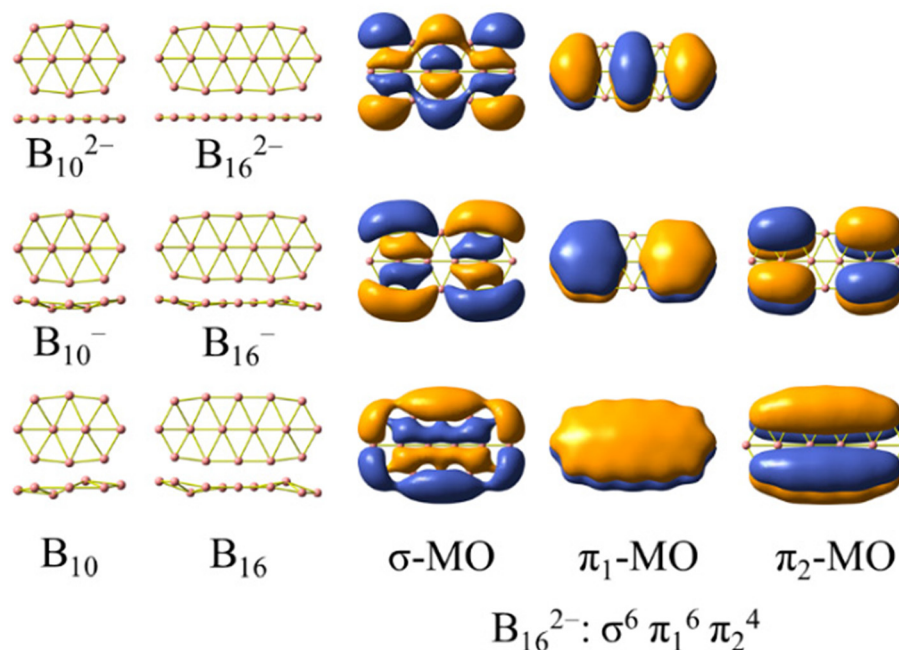
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Scheme 1 Global minima of boron clusters $B_{10}^{2-/-/0}$ and $B_{16}^{2-/-/0}$ and the electronic configuration of the planar dianion B_{16}^{2-} including six σ and ten π orbitals.

standing of the electronic configuration in tubular structures, especially when the tubes are formed from multiple atomic rings, making the electron picture more evident.²¹

The ribbon or double-chain motif^{26–29} has emerged as a distinctive form due to its two boron chains, but because of impurities, often in a negatively charged state, it can now be extended up to a length of 17.0 Å.²⁹ The ribbon model^{30,31} has subsequently been used to rationalize the aromaticity of ribbon-like structures without necessarily requiring cyclic electron delocalization¹³ in the structure. Surpassing mass spectrometry experiments for investigating boron ribbons in an anionic state,²⁷ the boron ribbon cluster $B_2C_4H_4$ was synthesized in a neutral state upon substitution of H atoms with appropriate ligands.³²

The structures formed from three boron chains³³ are less commonly found, and the electron counting rule of $[\sigma^{2(n+1)}\pi_1^{2(n+1)}\pi_2^{2n}]$ was established for rationalizing their aromaticity.³⁴ Scheme 1 presents two dianionic structures, B_{10}^{2-} and B_{16}^{2-} , which represent the triple-chain motif best. The electron configuration of B_{16}^{2-} satisfies the $[\sigma^{2(n+1)}\pi_1^{2(n+1)}\pi_2^{2n}]$ counting rule with $n = 2$. Scheme 1 also illustrates the global minima of the anionic and neutral $B_{10}^{-/0}$ and $B_{16}^{-/0}$,^{2,35–37} whose shapes involve a slight geometric deformation from a perfect planarity of the corresponding dianions B_{10}^{2-} and B_{16}^{2-} , respectively. In this context, a question of interest is whether it is possible to extend the size of boron triple-chain clusters by means of doping. Following multiple attempts to introduce various impurities to the latter, we find that the phosphorus element becomes both a neutralizing impurity and an extending agent. As a matter of fact, the incorporation of P atoms into the above dianionic species not only neutralizes the dianions but also extends the triple-chain form of the resulting $B_{10}P_4$ and

$B_{16}P_4$ systems. A similar picture for the evolution of the structural motif of the B_xP_y clusters remains valid in the isoivalent analogues in which each {P} atom is replaced by a {CH} unit (both entities having 5 valence electrons each). The substitution of {P} with {CH} ultimately leads to carborane structures that offer more practical opportunities for synthesis.

The account presented in the next sections aims to contribute to a demonstration of the validity of the $[\sigma^{2(n+1)}\pi_1^{2(n+1)}\pi_2^{2n}]$ electron counting rule for this class of triple-chain compounds. Our calculated results point out that the inherent electronic distribution, and thereby the corresponding aromatic character, favours the planar triple-chain form that emerges to be thermodynamically more stable than the more symmetrical tetrahedron or other three-dimensional isomers. This is particularly related to a recent theoretical study which reported that the tetrahedron is the lowest-lying isomer of the $B_{16}P_4$ cluster system.³⁸ In contrast, our results show that the most stable $B_{16}P_4$ isomer exhibits a perfect planar triple-chain geometry.

2. Computational methods

Isomers of each of the clusters considered in this theoretical study were located following full geometry optimizations of over 1000 different initial geometries. These initial geometries were generated using a stochastic search algorithm³⁹ and a genetic algorithm (GA)⁴⁰ that was implemented by our group.⁸ Geometries of the initial guess structures were optimized using density functional theory (DFT) with the PBE⁴¹ functional, which has recently been benchmarked and found to be suitable for examining the relative energies of clusters contain-



ing multiple B atoms,⁴² and the 6-31G(d)^{43,44} basis set without subsequent vibrational frequency calculations. The set of isomers with relative energies within 3 eV with respect to the most stable structure is referred to as the seed structure ensemble. Each isomer in the seed structure ensemble was used to generate a series of input for optimization *via* both the stochastic search algorithm³⁹ and the genetic algorithm (GA).⁴⁰ After optimizations, the new set of output generated was evaluated to determine whether they belong to the seed structure ensemble. This iterative process continued until no new seed structures were identified.

The optimized structures whose total energies were within ~3 eV from the most stable geometry (the final seed structure ensemble) were then reoptimized using the same PBE functional but with a larger 6-311+G(d)^{43,44} basis set, along with vibrational frequency calculations in order to ensure the true local minimum character. Zero-point vibrational energy corrections were obtained from the harmonic frequencies without scaling. To identify the global minimum of each system, the electronic energies of a set of ten lowest-lying isomers were subsequently computed using single-point coupled-cluster theory CCSD(T)/6-311+G(d) calculations making use of the PBE/6-311+G(d) optimized geometries. Unrestricted Hartree-Fock (UHF) formalism was used for open-shell systems. All electronic structure calculations were performed using the Gaussian 16 software suite.⁴⁵

The adaptive natural density partitioning (AdNDP) algorithm,⁴⁶ as implemented in the Multiwfn software,⁴⁷ was used to probe the number of globally delocalized electrons. The chemical bonding and aromatic character were assessed through the electron localization function (ELF) maps^{48,49} using the Dgrid 5.0 package.⁵⁰

Topological analysis of the electron localization function (ELF) map indicates that a structure with a high bifurcation value on the ELF isosurface displays aromatic characteristics, while that with a low bifurcation value does not exhibit aromaticity. A planar molecule often has aromaticity based on the behavior of its π and σ electrons. Santos *et al.* demonstrated that ELF $_{\pi}$ and ELF $_{\sigma}$ maps can help classify the aromaticity of these electron types.⁵¹ In certain specific cases, σ electrons can distinctly be categorized into localized σ electrons and delocalized σ electrons. At this point, the separation of ELF $_{\sigma}$ into ELF $_{\sigma l}$ (for localized σ electrons) and ELF $_{\sigma d}$ (for delocalized σ electrons) further clarifies the impact of each electron type on the properties and stability of the structure considered.^{30,52}

Maps of the magnetic current density induced by a perpendicular magnetic field to the planar structure were calculated and visualized using the SYSMOIC⁵³ program; current flows were utilized to indicate the diatropic (clockwise) or paratropic (counterclockwise) nature of the ring current.

3. Results and discussion

3.1. B_xP_y systems

As stated above, we use phosphorus atoms as dopants in two boron systems displayed in Scheme 1. Four phosphorus atoms

are thus successively added into the B₁₀ and B₁₆ skeletons. The lowest-lying isomers of the resulting B₁₀P_y and B₁₆P_y with $y = 1, 2, 3$ and 4 are presented in Fig. 1 and 2. The relative energy ordering of isomers at 0 K established by (U)CCSD(T) calculations and corrected for zero-point energies (ZPEs) are marked by the labels having increasing numbers of 1, 2, 3, etc...

Fig. 1 and 2 illustrate two prominent trends when phosphorus atoms are added into the boron triple-chain structures. Firstly, P atoms are preferentially attached to positions 1, 2, 3 and 4 of four B–B bonds at both ends of the structures, as marked in Scheme 2. The next preferred positions are the B–B bonds denoted as 5, 6, 7 and 8 on the outermost of the two outer B rows.

The second trend is a rapid flattening of the triple-chain structure following doping, where, upon the second P atom addition, the triple-chain form already becomes perfectly planar, and such a perfect planarity is maintained following doping with the 3rd and 4th P atoms. This is particularly intri-

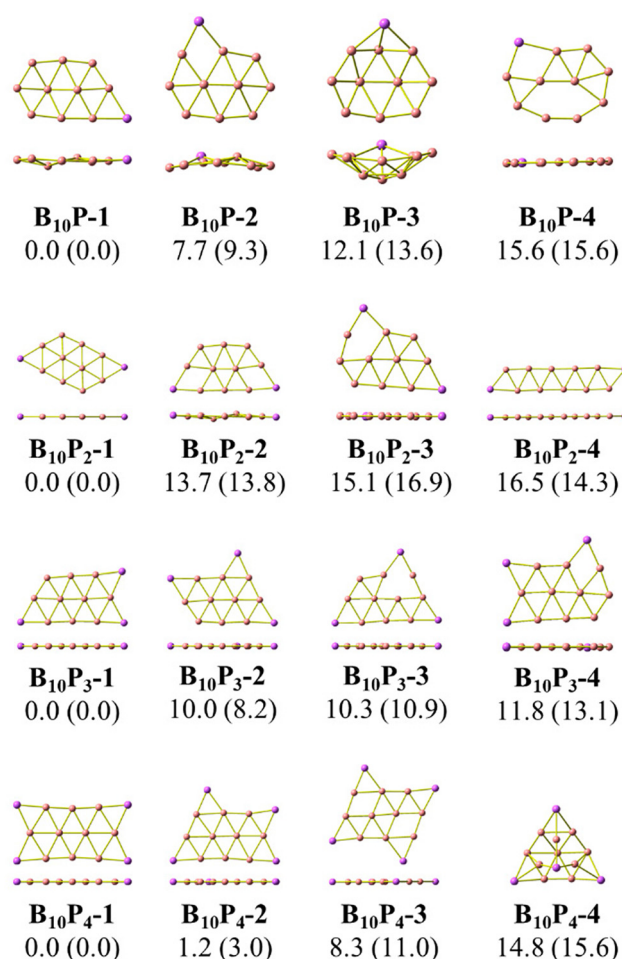


Fig. 1 Optimized geometries of the lowest-lying B₁₀P_y isomers with $y = 1, 2, 3$, and 4. Relative energies, given in kcal mol⁻¹, are obtained from (U)CCSD(T)/6-311+G(d) + ZPE computations; PBE/6-311+G(d) + ZPE values are given in parentheses.



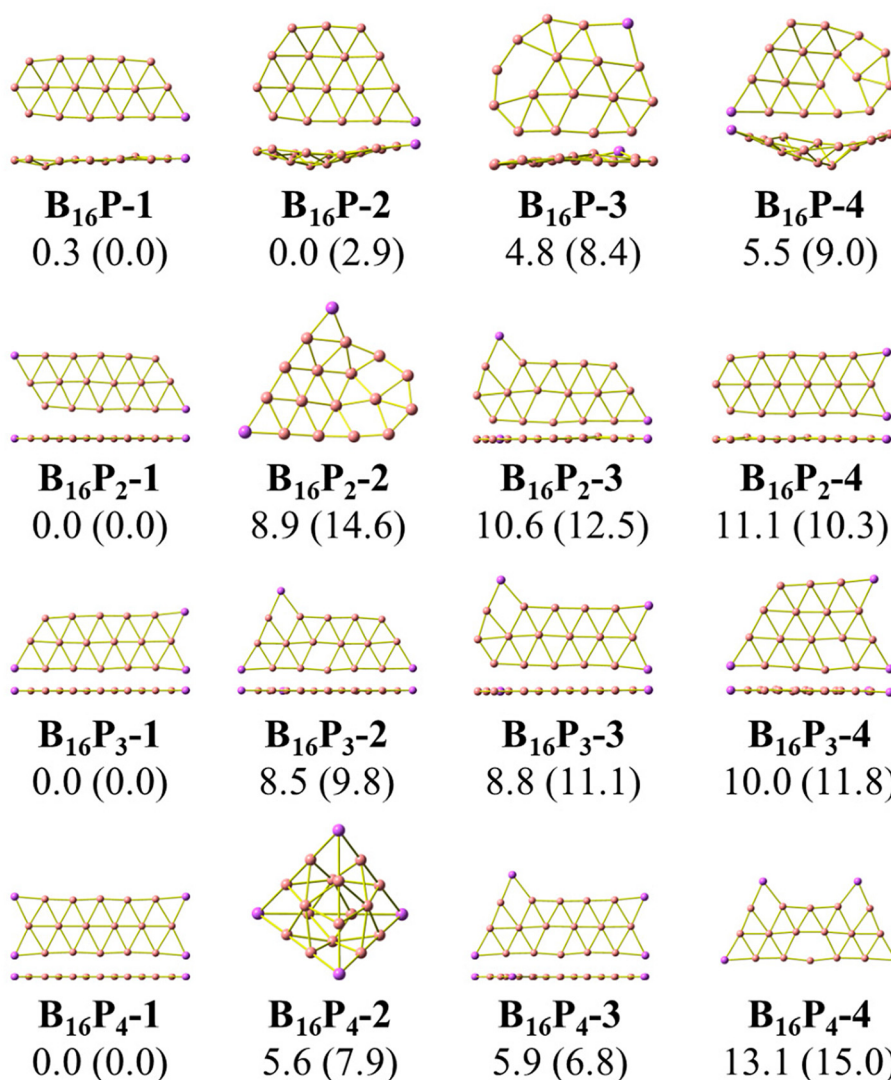
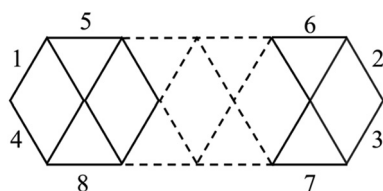


Fig. 2 Optimized geometries of the lowest-lying $B_{16}P_y$ isomers with $y = 1, 2, 3,$ and 4 . Relative energies, given in kcal mol^{-1} , are obtained from (U) CCSD(T)/6-311+G(d) + ZPE computations; PBE/6-311+G(d) + ZPE values are given in parentheses.



Scheme 2 Identification of the preferred binding sites of P atoms into the B–B bonds of the B_{10+6n} triple-chain framework.

going as it basically differs from a typical observation on boron cluster doping which tends to favour 3D isomers. A recent study conducted by Jin *et al.*⁵⁴ reported that the doping of an aluminium atom into the B_{10} size leads to the most stable 3D isomer in which the Al atom is positioned on the surface of a triple-chain structure, while subsequent lower-

lying isomers of AlB_{10} do not feature any triple-chain framework. Similarly, stable isomers of AlB_{16} also do not have any triple-chain skeleton.⁵⁴ A previous study by Mai and co-workers⁵⁵ indicated that the silicon counterpart of $B_{10}P-3$ (Fig. 1) is the global minimum of the SiB_{10} cluster in which the Si atom is attached to one long edge of the triple-chain structure, while the triple-chain framework is not even present in higher-energy isomers. A subsequent study by Mai and co-workers⁵⁶ also demonstrated that SiB_{16} has a second lowest-lying isomer in which the Si atom lies in the plane of a triple-chain B_{16} , while the global minimum and other isomers lack a triple-chain skeleton.

With our current knowledge, no previous observation was reported on the doping effect of an element, excluding H, halogens and noble gases, into a small-sized boron cluster whose resulting doped structure retains the original pure boron framework by up to four dopant atoms. The 3D structure that



appeared in $B_{10}P_4$ is $B_{10}P_4-4$ which is 14.8 kcal mol⁻¹ higher in energy than the global minimum $B_{10}P_4-1$. In the case of $B_{16}P_4$, the 3D structure bearing the form of a T_d tetrahedron $B_{16}P_4-2$ is only 5.6 kcal mol⁻¹ higher than $B_{16}P_4-1$.

The T_d tetrahedron P_4 is well known for its superior thermodynamic stability,⁵⁷ which is believed to result from its electron shell satisfying the doubly spherically aromatic count of $2(N + 1)^2$ with 18σ and 2π electrons.⁵⁸ Thus, insertion of a B_{16} unit into the tetrahedral P_4 forming the $B_{16}P_4-2$ isomer is highly noteworthy. The existence of both $B_{16}P_4-1$ and $B_{16}P_4-2$ has been recently reported by Gao *et al.*³⁸ In their study, DFT computations using the PBE0 functional suggested that $B_{16}P_4-2$ (T_d) is more stable than $B_{16}P_4-1$, despite the results from TPSSh, or more importantly, CCSD(T) indicates a reversed energy ordering.

In the present study, we find agreement in the energy ordering between the PBE functional and CCSD(T) results, indicating that in the neutral state $B_{16}P_4-1$ is more stable than $B_{16}P_4-2$. Based on PBE functional calculations, $B_{16}P_4-1$ is more stable than $B_{16}P_4-2$ by 27 kcal mol⁻¹ in the anionic state. Consequently, it is more likely that the $B_{16}P_4-1$ can experimentally be detected.

Our present result disagrees with a previous report by Gao *et al.*,³⁸ which concluded that the T_d structure of $B_{16}P_4-2$ is the most stable isomer. These authors³⁸ also relied on the adaptive natural density partitioning (AdNDP) analysis to explain the stability of $B_{16}P_4-2$. In addition, the low-lying $B_{16}P_4-3$ and $B_{16}P_4-4$ isomers were missed in their study. To have another look at these conflicting results, we replicate the analysis made in ref. 38, the details of which are given in the ESI file.†

3.2. $B_xP_yC_zH_z$ systems

The concept of “isolobal analogy”, meaning “similar lobes”, developed by Hoffmann⁵⁹ proved to be helpful in designing novel molecules based on stable molecular structures, and numerous molecules have been discovered using this approach.^{60,61} Considering the fact that a {P} atom is not only isoivalent but also isolobal to a {CH} fragment, we now carry out a sequential substitution of {P} atoms by {CH} units, and the corresponding lowest-lying isomers are presented in Fig. 3 and 4. Furthermore, in the anionic state, the triple chain of $B_xP_yC_zH_z$ retains the global minima, as illustrated in Fig. S2 and S3 (ESI file†).

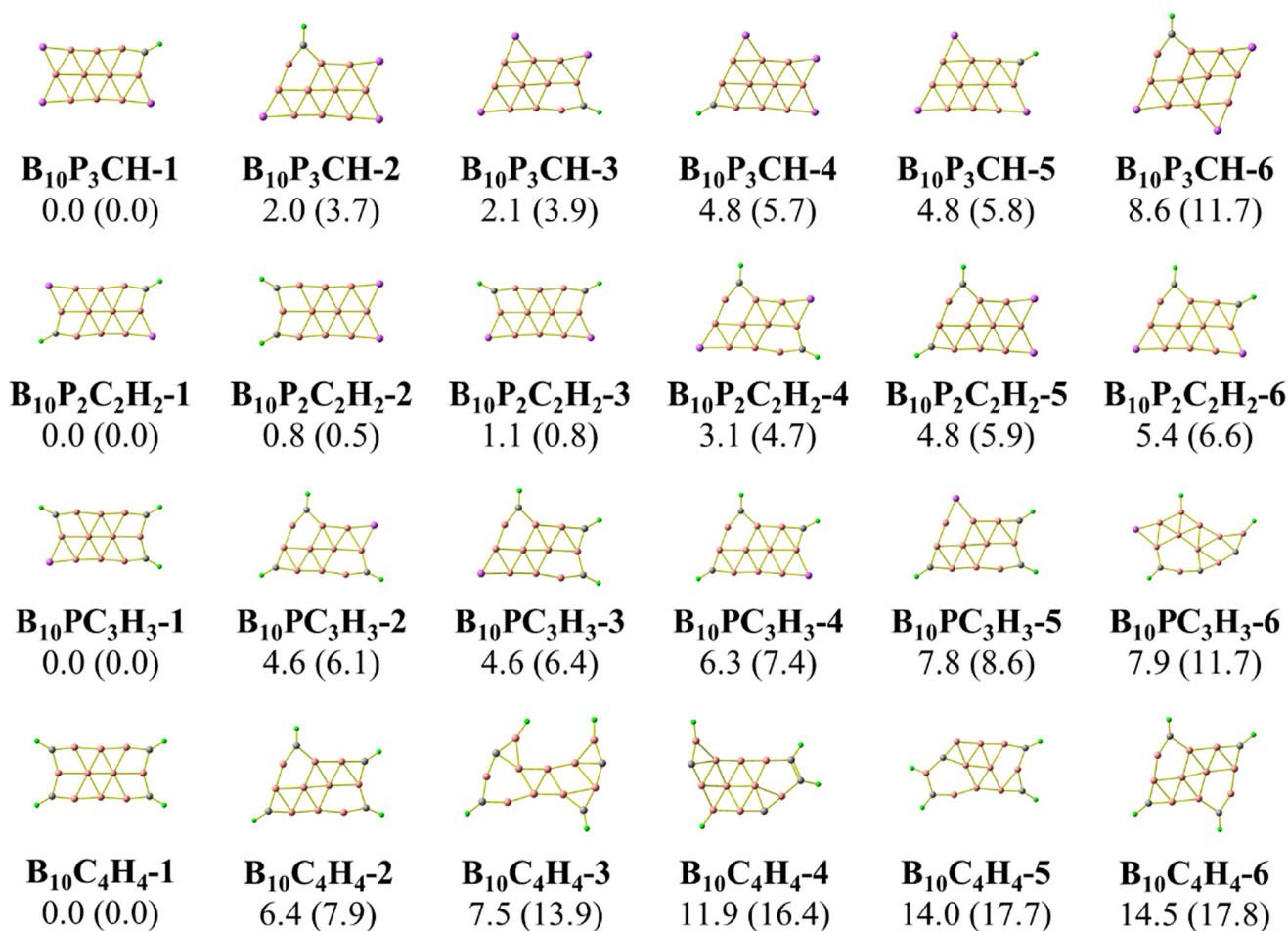


Fig. 3 Optimized geometries of the lowest-lying $B_{10}P_yC_zH_z$ isomers with $y = 3, 2, 1$ and 0 , and $z = 4 - y$. Relative energies given in kcal mol⁻¹ are obtained from CCSD(T)/6-311+G(d) + ZPE computations; PBE/6-311+G(d) + ZPE values are given in parentheses.



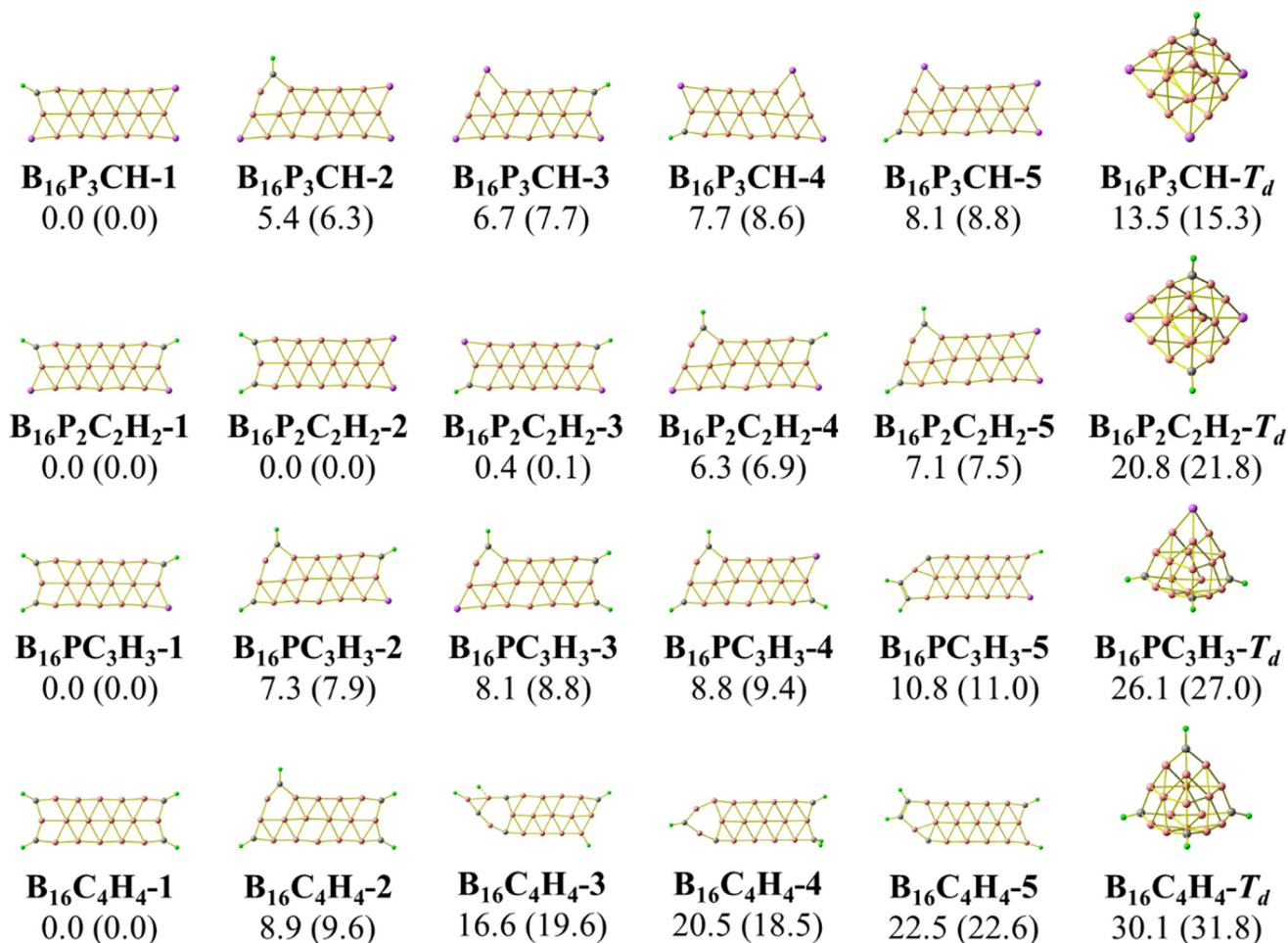


Fig. 4 Optimized geometries of the lowest-lying $B_{16}P_yC_zH_z$ isomers with $y = 3, 2, 1$ and 0 , and $z = 4 - y$. Relative energies, given in kcal mol^{-1} , are obtained from PBE/6-311+G(d) + ZPE computations.

Calculated results indicate the emergence of several stable isomers with a close relative energy (RE) as a consequence of the multiple permutations of positions between {P} and {CH}. The 1-4-isomer is the isomer with {P} or {CH} bonds at the 1, 2, 3 and 4 positions as shown in Scheme 2, and the 5-(2-4)-isomer is that with {P} or {CH} bonds at the 2, 3, 4 and 5 positions. Even more interestingly, we observe a gradual increase in the RE of the most stable isomer (1-4-isomer) as compared to the 5-(2-4)-isomer. This RE increases from 3.0 to 7.9 kcal mol^{-1} going from $B_{10}P_4$ to $B_{10}C_4H_4$. From $B_{16}P_4$ to $B_{16}C_4H_4$, the RE increases from 6.8 to 9.6 kcal mol^{-1} , and eventually the triple-chain $B_{16}C_4H_4-1$ exhibits a higher likelihood for experimental synthesis with a minimal occurrence of other isomers. The recent synthesis of the ribbon-like carborane $B_4C_2R_4$ ³² constitutes a stimulation for a promising generation of these triple-chain carboranes $B_xC_4H_4$, which in turn could facilitate the synthesis of $B_xP_yC_zH_z$ structures in a reversed manner.

The isomers derived from the T_d structure of $B_{16}P_xC_yH_y$ presented in Fig. 4 emphasize a rapid increase in the REs

between both triple-chain and T_d forms when {P} is sequentially substituted by {CH}. This is analogous to the transition from the 3D to the 2D form observed in the tetrahedral P_4 when {P} is successively replaced by {CH} forming C_4H_4 .^{62,63}

3.3. Stability trend

The vertical attachment energy (VAE) and the vertical ionization energy (VIE) are defined as:

$$\text{VAE} = E(\mathbf{X}^0) - E(\mathbf{X}^-) \quad (1)$$

$$\text{VIE} = E(\mathbf{X}^0) - E(\mathbf{X}^+) \quad (2)$$

where $E(\mathbf{X}^{-/0/+})$ is the energy of cluster \mathbf{X} in anionic, neutral and cationic states, respectively, at the optimized neutral geometry. The chemical hardness⁶⁴ (η), electronegativity⁶⁵ (χ) and electrophilicity⁶⁶ (ω) are then calculated using formulas (3), (4) and (5):

$$\eta = \frac{\text{VIE} - \text{VAE}}{2} \quad (3)$$



$$\chi = \frac{\text{VIE} + \text{VAE}}{2} \quad (4)$$

$$\omega = \frac{\mu^2}{2\eta} \quad (5)$$

where the chemical potential (μ) is the opposite of electronegativity ($\mu = -\chi$).

The frontier orbital HOMO–LUMO gaps (HLGs) of $\text{B}_x\text{P}_y\text{C}_z\text{H}_z$ are presented in Fig. 5, whereas the VAE, VIE, η , χ and ω values are plotted in the graphs shown in Fig. 6, and given in Tables S1 and S2 of the ESI file.†

The HLG and η values point toward increasing structural stability as their values increase, whereas ω indicates that stability increases as its values fall. A high VIE suggests that the structure tightly holds its electrons, whereas a low VAE indicates a stabilized neutral state. Therefore, a high VIE and low VAE values show the stability of a structure in its neutral state. Overall, while the HLG, VAE and η values of $\text{B}_{16}\text{P}_y\text{C}_z\text{H}_z$ are lower than those of $\text{B}_{10}\text{P}_y\text{C}_z\text{H}_z$, VIE and ω of $\text{B}_{16}\text{P}_y\text{C}_z\text{H}_z$ are higher than that of $\text{B}_{10}\text{P}_y\text{C}_z\text{H}_z$; $\text{B}_{10}\text{P}_y\text{C}_z\text{H}_z$ thus have greater stabilization as compared to $\text{B}_{16}\text{P}_y\text{C}_z\text{H}_z$.

Initially, when P is doped into B_x , the values of HLG, VAE, VIE, η and ω vary according to parity; closed-shell systems are more kinetically stable than their open-shell counterparts. Considering only the closed-shell systems, their stability decreases upon P addition: B_x is more stabilized than B_xP_2 , and B_xP_2 is more stable than B_xP_4 . Subsequently, the replacement of {P} with {CH} leads to the opposite effect: the more {P} is replaced by {CH}, the more stable the structure becomes.

The electronegativity (χ) of a molecule refers to its ability to attract electrons towards itself. The electronegativity of structures considered here exhibits less variability as compared to the aforementioned parameters with the lowest value being 5.0 eV for $\text{B}_{16}\text{C}_4\text{H}_4$ and the highest value being 5.7 eV for B_{10} .

3.4. Chemical bonding

The AdNDP method is often employed with the aim of verifying the nature of the MOs in the species considered. The set of σ bonds of the B_{16}^{2-} dianion, which was assigned from AdNDP analysis carried out by Sergeeva *et al.*,³⁷ suggests that B_{16}^{2-} has eight σ delocalized electrons leading to its σ antiaromatic character, according to the classical ($4n$) electron count.

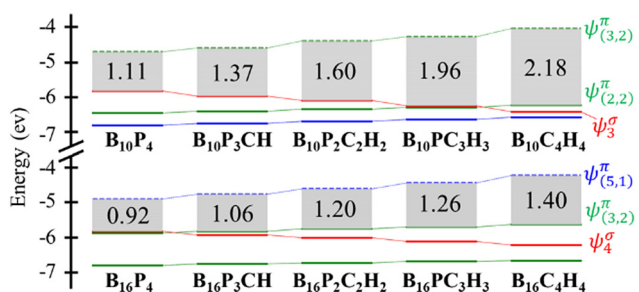


Fig. 5 Energy diagram of triple-chain $\text{B}_x\text{P}_y\text{C}_z\text{H}_z$. HOMO–LUMO gaps (eV) are given in grey areas.

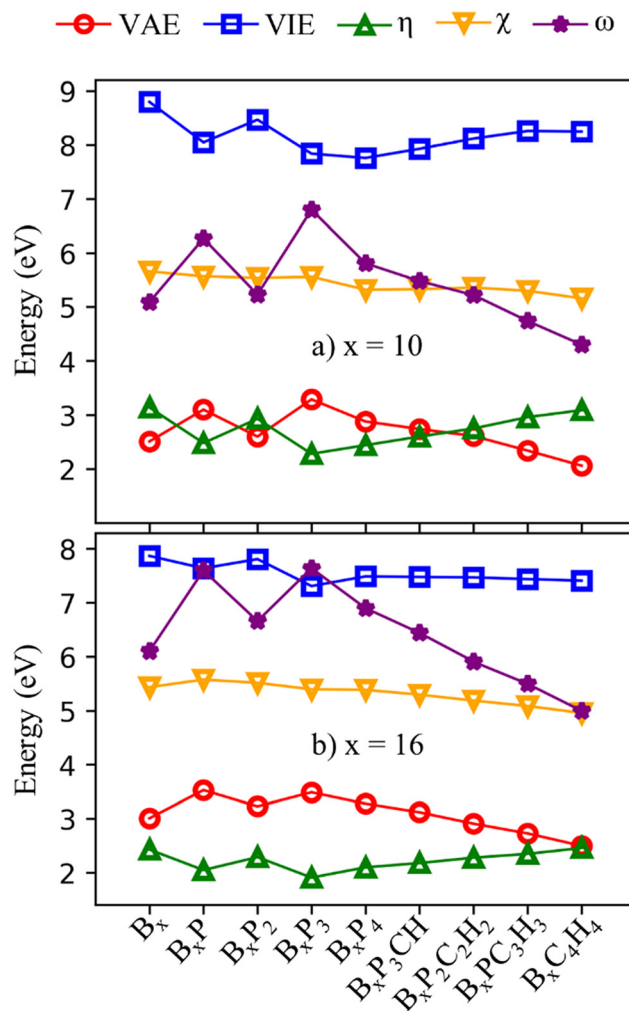


Fig. 6 VAE, VIE, η , χ and ω values of $\text{B}_x\text{P}_y\text{C}_z\text{H}_z$ clusters in (a) $x = 10$ and (b) $x = 16$.

Our subsequent study,³⁴ which was a thorough analysis of the σ -out-of-plane contributions to the molecular magnetizability, revealed that B_{16}^{2-} rather exhibits σ aromaticity with the sum of magnetic components $\sum \chi_{zz}(\Omega)^{\text{intra}} = -40$ cgs ppm. Our present AdNDP analysis is summarized in Fig. 7 whereas the corresponding MOs are shown in Scheme 1. The ring current maps for σ electrons of B_{16}^{2-} displayed in Fig. S8 (ESI file†) also confirm the σ aromatic character of this dianion.

In view of such a significant discrepancy, we conducted the AdNDP analysis again, and our recent results are presented in Fig. 7a, corresponding to the σ bonding framework of B_{16}^{2-} . The set of eighteen σ bonds from (1) to (6) are well reproduced, similar to those reported by Sergeeva *et al.*,³⁷ despite a slight discrepancy in the occupation numbers (ONs) that are rather not significant due to the utilization of different theoretical methods. It is noteworthy that after collecting eighteen σ bonds (*cf.* (1–6) in Fig. 7a) and five π bonds (Fig. 7c), a significant amount of residual valence electrons remains sufficient to be considered as a bond. Indeed, a σ 16c–2e bond (7) is obtained from this set of residual valence electrons with an



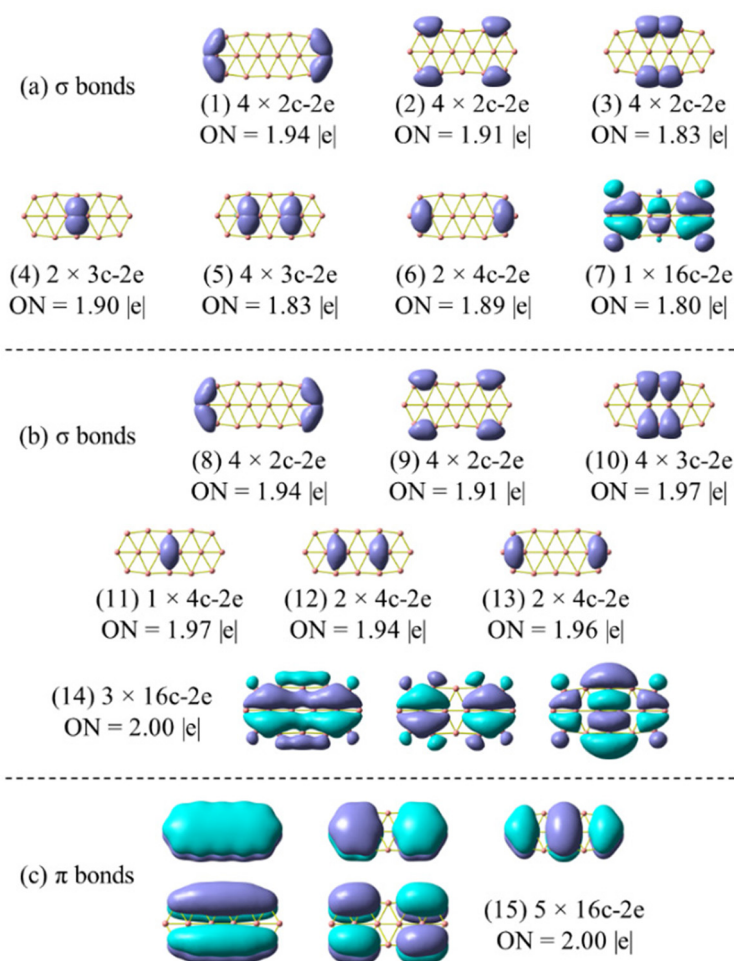


Fig. 7 Chemical bonding pattern of the B_{16}^{2-} dianion based on AdNDP analysis. Occupation numbers (ONs) are indicated. (a) is the set of σ bonds obtained by replicating Sergeeva's results (ref. 37) excluding bond (7); (b) is the set of σ bonds obtained by the method employed in this study, and (c) represents a set of π bonds, applicable to both (a) and (b).

ON value of 1.80 |e|, demonstrating its delocalized nature. This points out that the analysis reported in ref. 37 is not appropriate, thereby prompting us to repeat it by setting the occupation threshold to 1.9 |e| to first identify the bonds with ON values being larger than 1.9 |e|.

The σ bond framework as depicted in Fig. 7b reveals that the four $2c-2e$ σ bonds (3) turn out to be four $3c-3e$ σ bonds (10) with ON values now exceeding 1.9 electrons, the six σ $3c-2e$ bonds (4-5) turn out to be only three σ $4c-2e$ σ $3c-2e$ bonds (12-13), and finally, the set of remaining residual valence electrons comprises three globally delocalized σ bonds with shapes analogous to those of the σ delocalized MOs indicated in Scheme 1 (or Fig. S4a in the ESI file†).

The π bond framework also contains five globally delocalized π bonds whose shapes are akin to the π MOs as indicated in Scheme 1. Overall, the B_{16}^{2-} dianion truly comprises 3 globally delocalized σ MOs and 5 π MOs as illustrated in Scheme 1. The remaining σ electrons include localized ($2c-2e$) electrons and restricted delocalized ($nc-2e$) electrons with $n = 3$ or 4. Such a chemical bonding pattern, which is similar to those of

the B_{22}^{2-} , $B_{10}P_4$, $B_{10}C_4H_4$, $B_{16}P_4$ and $B_{16}C_4H_4$ systems, is presented in Fig. S5, S6 and S7 (ESI file†), and demonstrates the assignment of the MOs pictured in Fig. 8 and Fig. S4 (ESI file†) as globally delocalized MOs are entirely justified.

The electron counting rule of $[\sigma^{2(n+1)}\pi_1^{2(n+1)}\pi_2^{2n}]$ which has been proposed in our previous studies,³⁴ appears to be suitable for rationalizing the aromatic character of the triple-chain B_{10}^{2-} and B_{16}^{2-} , and the antiaromaticity of the perfectly planar triple-chain B_{22}^{2-} .

It should be reiterated again that this electron counting rule stems from consideration of the π electrons of the triple-chain structure as freely moving within a rectangular potential well with infinitely high potential at the boundaries. The corresponding Schrödinger equation for a particle moving in a rectangular box is a well-known basic concept found in many textbooks of quantum chemistry. Its eigenvalues are presented in eqn (6) that express the energy levels:

$$E_{(p,q)} = \frac{\hbar^2}{8m} \left(\frac{p^2}{a^2} + \frac{q^2}{b^2} \right) \quad (6)$$



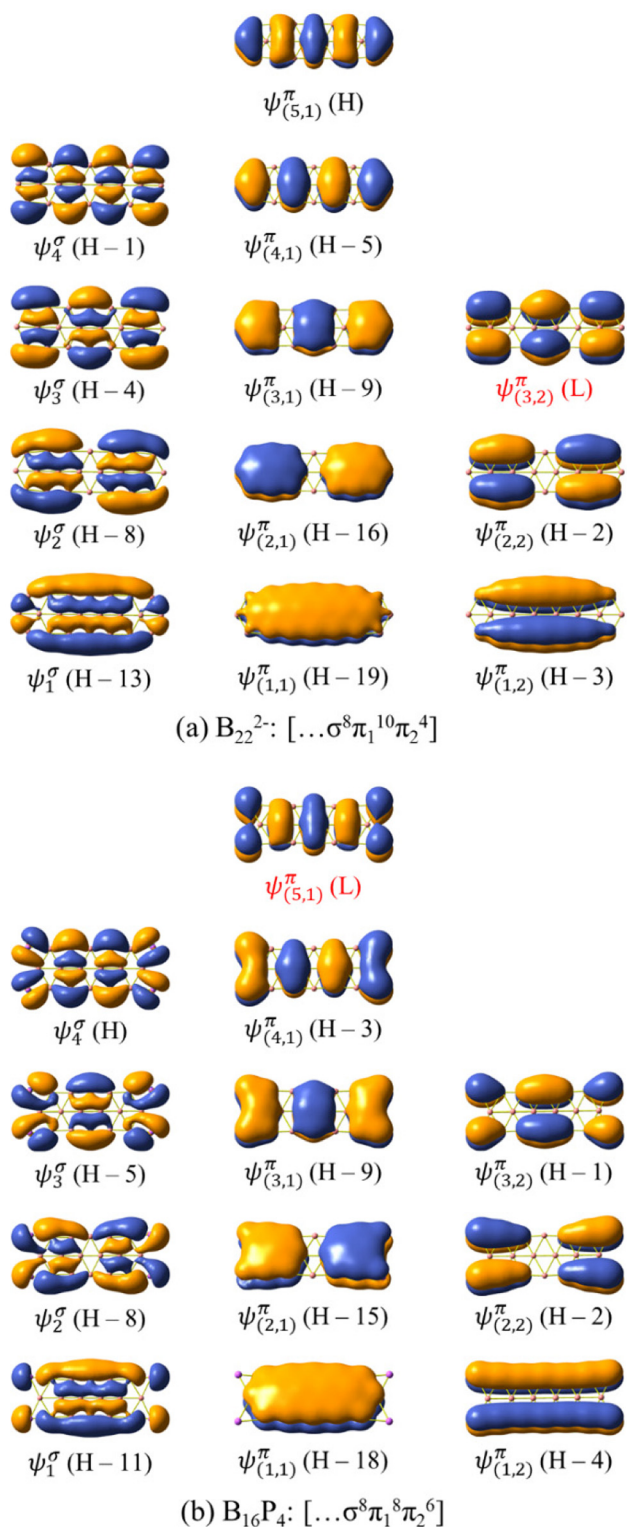


Fig. 8 The σ delocalized and π MOs of (a) B_{22}^{2-} and (b) $B_{16}P_4$. H and L stand for the HOMO and LUMO, respectively.

in which a and b are the length and the width of the rectangular box, respectively, and $p = 1, 2, 3, \dots$ and $q = 1, 2, 3, \dots$ are the length and width quantum numbers, respectively. While the wavefunction $\psi_{(p,1)}^\pi$ with $q = 1$ belongs to the π_1

group, the wave function $\psi_{(p,2)}^\pi$ with $q = 2$ belongs to the π_2 group.

The σ and π MOs of both B_{16}^{2-} and B_{22}^{2-} as well as those of the doped $B_{10}P_4$ and $B_{16}P_4$ are shown in Fig. 8 and Fig. S4 (ESI file†). Here, the electron configuration $[\sigma^6\pi_1^6\pi_2^4]$ of $B_{10}P_4$ coincides with that of B_{16}^{2-} and indicates that $B_{10}P_4$ achieves triple-chain aromaticity.

The B_{22}^{2-} dianion exhibits triple-chain antiaromatic characteristics due to the electron configuration of $[\sigma^8\pi_1^{10}\pi_2^4]$. Interestingly, there is a permutation between the two wavefunctions $\psi_{(5,1)}^\pi$ and $\psi_{(3,2)}^\pi$, where $\psi_{(5,1)}^\pi$ is the HOMO in B_{22}^{2-} and becomes the LUMO in $B_{16}P_4$, and $\psi_{(3,2)}^\pi$ is the LUMO in B_{22}^{2-} and becomes the HOMO-1 in $B_{16}P_4$. This leads to fulfilment of the electron counting rule of $[\sigma^8\pi_1^8\pi_2^6]$ for $B_{16}P_4$. According to this triple-chain model, both $B_{10}P_4$ and $B_{16}P_4$ behave as triple-chain aromatic species.

Each of the B_{22}^{2-} and $B_{16}P_4$ species exhibits 14 π electrons and thus appears to be aromatic according to the classical $(4n + 2)$ rule with $n = 3$. As pointed out in our previous study³⁴ and as also demonstrated by the π ring current maps illustrated in Fig. 9, while B_{22}^{2-} turns out to be a π antiaromatic species, $B_{16}P_4$ is a π aromatic one. Thus, the classical $(4n + 2)$ electron counting rule does not account for the aromaticity of a triple-chain structure, whereas the $[\pi_1^{2(n+1)}\pi_2^{2n}]$ electron count represents the more suitable rule related to the triple-chain aromaticity, albeit its representation is somewhat more complex.

The $(4n + 2)$ rule tends to lead us to associate these electrons with one non-degenerate level and n doubly degenerate levels of energy. However, many related structures are characterized with an electron count satisfying the $(4n + 2)$ rule but they do not have any degenerate energy level, such as the oligoacenes. Several recently discovered structures exhibit aromatic properties and are explained by having electron spectra similar to that of naphthalene ($C_{10}H_8$)^{37,67} or anthracene ($C_{14}H_{10}$).⁶⁸ Such a comparison is only partially correct, because while the π electron configuration of boron clusters can be compared to those of hydrocarbons on the basis of the similarity between the π -MO shapes and the number of π electrons, the boron clusters have in addition a set of σ delocalized electrons that do not exist in hydrocarbons. Accordingly, it appears better to avoid an explanation for the aromaticity of boron clusters using the classical $(4n + 2)$ electron counting rule. Indeed, the electron configurations of oligoacenes including naphthalene, anthracene and tetracene that are presented in Fig. S11 (ESI file†) demonstrate well that they follow the $[\pi_1^{2(n+1)}\pi_2^{2n}]$ rule. In summary, the stability of boron clusters often needs to be understood considering both sets of π and σ characteristics, whereas hydrocarbons only involve their π electrons.

Two additional issues need some further attention, namely, why triple-chain structures need to satisfy the $[\pi_1^{2(n+1)}\pi_2^{2n}]$ rule, and how a cluster structure can satisfy this rule. Answers for both issues have been presented in our previous study,³⁴ but here, taking the doping effect into account, we would again demonstrate that the above rationalization is entirely valid.



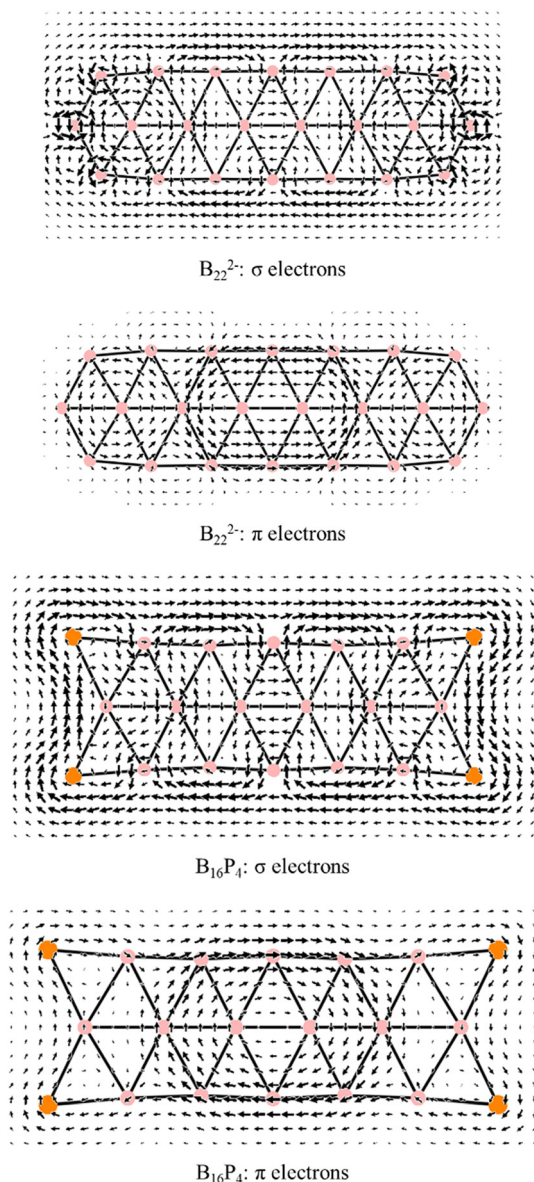


Fig. 9 The σ and π ring current maps of B_{22}^{2-} and $B_{16}P_4$ triple-chain structures.

The initial answer can be found through the relationship between the electron localization function (ELF) maps and bond lengths of structures as depicted in Fig. 10 and S10 (ESI file[†]). Both $ELF_{\sigma d}$ and ELF_{π} maps represent the ELF's originating from both sets of globally σ and π delocalized electrons. In these figures, the structures are highlighted with purple and yellow rhombuses. Purple rhombuses correspond to locations where multiple interactions of $ELF_{\sigma d}$ and ELF_{π} basins are present, resulting in shorter edge lengths and diagonals as compared to the edges and diagonals of the yellow rhombuses.

The first observation is that in $ELF_{\sigma d}$ (cf. Fig. S9, ESI file[†]), which is similar to what has been observed in ribbon-like,³⁰ double ring,⁵² or triple ring²⁴ structures, the basins of attrac-

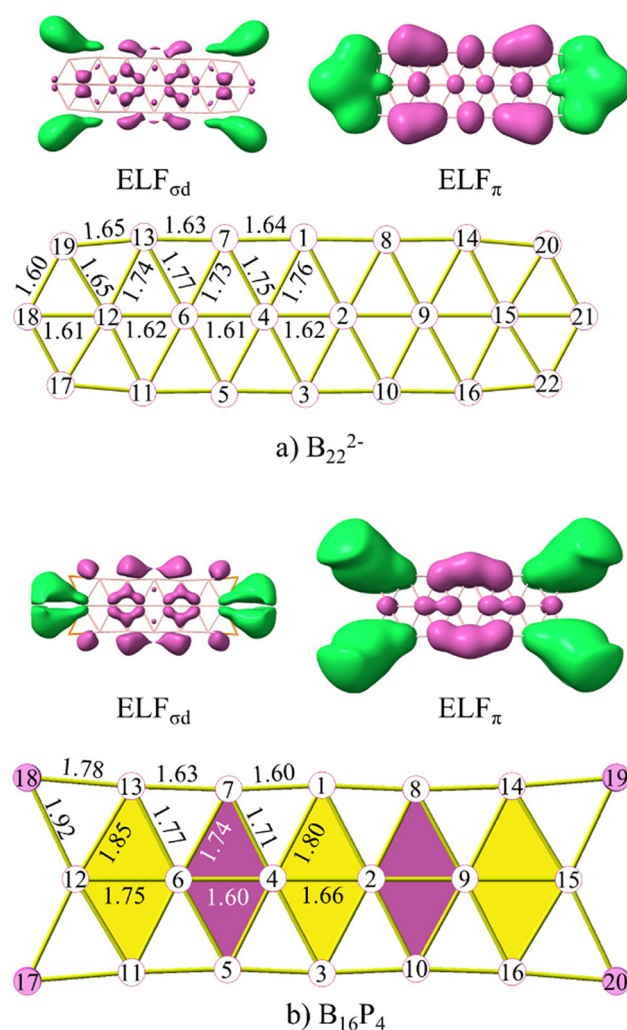


Fig. 10 The $ELF_{\sigma d}$, ELF_{π} and the structures of (a) B_{22}^{2-} and (b) $B_{16}P_4$. Bond lengths are given in angstrom.

tion are only observed for bonds within the same row (sr-bond), not connecting rows (cr-bond), except for the bonds at the ends of each structure. Therefore, the common resulting characteristic is that the lengths of sr-bonds are shorter than those of cr-bonds. The ELF_{π} basins also indicate that they enhance more the bonding of sr-bonds than that of the cr-bonds. Within the same row, the bonds where ELF_{π} basins are present tend to have shorter distances than those of the same type without ELF_{π} basins.

The B2–B4 bond length (cf. Fig. S10 ESI file[†] for atom labels) corresponds to the shortest B–B bond that amounts to 1.54, 1.61 and 1.60 Å in B_{16}^{2-} , $B_{10}P_4$ and $B_{10}C_4H_4$, respectively. The B4–B6 (B2–B9) bonds are the smallest diagonals within the yellow rhombus adjacent to the central purple rhombus. The deviation between B4–B6 and B2–B4 in B_{16}^{2-} , $B_{10}P_4$ and $B_{10}C_4H_4$ amounts to 0.09, 0.17 and 0.24 Å, respectively. This significant difference is analogous to the presence of the ELF_{π} basin in the B2–B4 bond while such a basin is absent in the B4–B6 bond. In B_{16}^{2-} , the B6–B16 bond distance is 1.6 Å, and



it is also shorter than the neighbouring B4–B6 bond for the same reason. Thus, $\text{ELF}_{\sigma\text{d}}$, in turn, tends to show an enhancement of the cr-bonds.

An interesting observation from these results is that the rhombuses with small diagonals that are enhanced continue to be reinforced by $\text{ELF}_{\sigma\text{d}}$, while the rhombuses with small diagonals that are not enhanced are not reinforced by $\text{ELF}_{\sigma\text{d}}$. We present herewith the clearest observation of this trend. The B6–B7 bond in B_{16}^{2-} is still influenced by $\text{ELF}_{\sigma\text{d}}$, resulting in a bond length of 1.80 Å. However, in B_{10}P_4 it is no longer affected by $\text{ELF}_{\sigma\text{d}}$, and this bond length is then increased to 1.85 Å. In $\text{B}_{10}\text{C}_4\text{H}_4$ the latter distance further increases to 1.91 Å. The B6–B7 bond in B_{10}P_4 corresponds to the B12–B13 bond in B_{16}P_4 and $\text{B}_{10}\text{C}_4\text{H}_4$ whose respective bond lengths amount to 1.85 and 1.90 Å.

There is an alternating arrangement of domains, coloured as purple and yellow rhombuses, in the triple-chain structure when it achieves aromaticity (cf. Fig. 10). Indeed, such alternation does not exist in B_{22}^{2-} and therefore the B_{22}^{2-} dianion is considered as a π antiaromatic species.

Although both B_{16}P_4 and B_{22}^{2-} have the same number of σ and π electrons, only B_{16}P_4 is aromatic. The enhanced and non-enhanced rhombuses observed in B_{16}P_4 indicate that the triple-chain aromaticity requires its electrons to be distributed in such a way that there is an alternating arrangement of rhombuses in the structure, as described above. This alternation also appears in triple-chain hydrocarbons as previously presented for the ribbon clusters.³⁴

The alternation between enhanced and non-enhanced regions in triple-chain structures³⁴ or ribbon structures³⁰ challenges the common notion of bond length equalization⁶⁹ for an aromatic structure (such as in the case of benzene). This challenge is further reinforced when the B_{22}^{2-} structure, which exhibits even more bond length equalization, is now identified as a π antiaromatic species.

In the $\text{ELF}_{\sigma\text{d}}$ and ELF_{π} maps (cf. Fig. 10), large anomalous basins have appeared that are highlighted in green. Due to the insignificant difference between the bonds affected by these basins in B_{16}^{2-} as compared to the adjacent bonds, the role of these basins was not mentioned in our previous study.³⁴ Because of the strong influence of impurities, the roles of these basins become more apparent. The significantly shorter bond length of P12–B7 (C12–B7) as compared to P12–B6 (C12–B6) in B_{10}P_4 ($\text{B}_{10}\text{C}_4\text{H}_4$) or P18–B13 (C18–B13) compared to P18–B12 (C18–B12) in B_{16}P_4 ($\text{B}_{16}\text{C}_4\text{H}_4$) suggests a self-locking phenomenon akin to the ribbon model.³⁰ Indeed, these B–P (or B–C) bonds that are anomalously short with respect to their normal lengths, and are located at the four corners of the rectangular structure, indicate that the aromatic motif in an triple-chain model self-adjusts to the particle in a rectangular box (PIARB) model, which has infinite potential at the boundary, making it the most suitable electron configuration possible.

Although they have the same number of π electrons, the correspondence between the antiaromatic B_{22}^{2-} to the aromatic B_{16}P_4 clearly demonstrates the significance of the triple-

chain model. In B_{22}^{2-} , the $\psi_{(5,1)}^{\pi}$ level is occupied and the $\psi_{(3,2)}^{\pi}$ level is unoccupied, whereas in B_{16}P_4 the $\psi_{(3,2)}^{\pi}$ level is occupied and the $\psi_{(4,1)}^{\pi}$ level is unoccupied (cf. Fig. 8). That means, if the $\psi_{(p2,2)}^{\pi}$ level is the molecular orbital with $p2$ being the highest quantum number for the π_2 group, then the energy level of $\psi_{(p2+2,2)}^{\pi}$ must be higher than that of $\psi_{(p2,2)}^{\pi}$, and the structure must have enough π electrons for the $\psi_{(p2+1,1)}^{\pi}$ level to be fully occupied. If we set $p1 = p2 + 2$ and according to eqn (6), the above condition implies:

$$\frac{p1^2}{a^2} + \frac{1}{b^2} > \frac{p2^2}{a^2} + \frac{4}{b^2}$$

or

$$\frac{a}{b} < \sqrt{\frac{p1^2 - p2^2}{3}} = \text{SR} \quad (7)$$

with the SR being the standard a/b ratio for which a/b must be smaller, in such a way that the energy of $\psi_{(p2+2,1)}^{\pi}$ is higher than that of $\psi_{(p2,2)}^{\pi}$.

In a recent study, a small and simple Python code snippet was written to determine the dimensions a and b of the rectangle in which the π electrons move freely,⁴² in which the root mean square error (RMSE) index was calculated for determining the accuracy of the model (eqn (8)):

$$\text{RMSE} = \sqrt{\frac{\sum_{i=1}^m (E_i^{\text{DFT}} - E_i^{\text{PIARB}})^2}{m}} \quad (8)$$

with m being the number of occupied molecular orbitals; E_i^{DFT} and E_i^{PIARB} represent the energies of the MOs calculated from the DFT method and from the PIARB, respectively.

Applying this code, the results for the structures C_{10}H_8 , B_{16}^{2-} , B_{10}P_4 and $\text{B}_{10}\text{C}_4\text{H}_4$ for 10 π electron systems and $\text{C}_{14}\text{H}_{10}$, B_{22}^{2-} , B_{16}P_4 and $\text{B}_{16}\text{C}_4\text{H}_4$ for 14 π electron systems are provided in Table 1. With the $\text{RMSE} < 0.01$ for all systems considered in Table 1, the π electrons appear to follow the PIARB model.

The heteromolecular compounds with an RMSE being twice as large as that of the pure boron triple-chain clusters indicate the presence of the phenomenological shell model (PSM)²³ on the electron spectrum, but it remains non-significant. As the triple-chain size increases, the number of π elec-

Table 1 Length a and width b of C_{10}H_8 , B_{16}^{2-} , B_{10}P_4 , $\text{B}_{10}\text{C}_4\text{H}_4$, $\text{C}_{14}\text{H}_{10}$, B_{22}^{2-} , B_{16}P_4 and $\text{B}_{16}\text{C}_4\text{H}_4$ and their distance ratio a/b , standard ratio SR, and the RMSE value of each structure

Species	a (Å)	b (Å)	a/b	SR	RMSE
C_{10}H_8	9.21	6.52	1.41	2.00	0.0052
B_{16}^{2-}	10.61	5.75	1.85	2.00	0.0022
B_{10}P_4	10.27	6.90	1.49	2.00	0.0065
$\text{B}_{10}\text{C}_4\text{H}_4$	10.34	6.97	1.48	2.00	0.0052
$\text{C}_{14}\text{H}_{10}$	11.98	6.57	1.82	2.31	0.0057
B_{22}^{2-}	13.84	5.78	2.39	2.31	0.0021
B_{16}P_4	13.55	6.54	2.07	2.31	0.0056
$\text{B}_{16}\text{C}_4\text{H}_4$	13.56	6.55	2.07	2.31	0.0044



trons also increases, proportional to the a/b ratio and SR. However, the ratio a/b is found to increase more rapidly than the SR, leading a/b to approach the SR or even exceed the SR as in B_{22}^{2-} . Substitution of a $\{B_6^{2-}\}$ unit with a $\{P_4\}$ atom does not only decrease the length a but also increases the width b of the triple-chain form, thereby reducing the a/b ratio. In other words, there is no significant change in the variation of a and b following substitution of $\{P\}$ with $\{CH\}$.

As the triple-chain size increases, the levels $\psi_{(p2,2)}^x$ and $\psi_{(p2+2,1)}^x$ in the oligoacenes approach each other more closely, meaning that the frontier orbital (HOMO–LUMO) energy gap (HLG) decreases, thereby increasing the multi-reference nature of the molecule and reducing its kinetic stability.^{70–72} The perfect planarity of $B_{22}X_4$ with $X = \{P\}$ or $\{CH\}$ is also due to an electron configuration satisfying the $[\sigma^{2(n+1)}\pi_1^{2(n+1)}\pi_2^{2n}]$ rule, but the HLG amounts to only 0.13 and 0.31 eV for $B_{22}P_4$ and $B_{22}C_4H_4$, respectively, leading to the appearance of imaginary frequencies for high symmetry structures. Therefore, these clusters are not further discussed in the present work. Furthermore, in boron-based clusters, σ electrons can also serve as the HOMO as seen in $B_{16}P_4$ or the LUMO as in the B_{15}^- anion,⁴² thus making the prediction of the size of the HLG as well as their aromatic character and stability even more challenging.

For a broader perspective on the effect of substitution of $\{P\}$ with $\{CH\}$, the energy diagrams of the structures studied are presented in Fig. 5. At a rapid glance, substitution of $\{P\}$ with $\{CH\}$ leads to an increase in HLG, corresponding to enhanced kinetic stability as indicated above. The increase in HLG stems from two opposing processes resulting from the substitution, namely the downward shift of σ MOs and the upward shift of π MOs. This phenomenon is observed more distinctly in $B_{10}P_yC_zH_z$ as compared to $B_{16}P_yC_zH_z$. In $B_{10}P_yC_zH_z$, this displacement leads to a rearrangement of the HOMO and HOMO–1 cross positions in $B_{10}PC_3H_3$. Therefore, under strict consideration, only $B_{10}P_4$, $B_{10}P_3CH$ and $B_{10}P_2C_2H_2$ are deemed to be isolobal, while the entire set of $B_{10}P_yC_zH_z$ structures are better considered as isovalent.

In $B_{16}P_yC_zH_z$, the ψ_4^x level becomes HOMO–1 in $B_{16}PC_3H_3$ and continues to shift downwards with increasing substitution of $\{P\}$ with $\{CH\}$. Therefore, all $B_{16}P_yC_zH_z$ isomers are considered as isolobal, except for $B_{16}P_4$. Both the HOMO and LUMO of $B_{16}P_yC_zH_z$, except for $B_{16}P_4$, are π MOs, and their energy levels increase. Consequently, the increase in HLG for $B_{16}P_yC_zH_z$ is much slower as compared to that of $B_{10}P_yC_zH_z$. The increase in HLG for $B_{16}P_yC_zH_z$ is also facilitated by a faster increase in the energy levels of LUMO (antibonding) as compared to HOMO (bonding).

With their π aromaticity, the triple-chain $B_xP_yC_zH_z$ that are analogues of the aromatic oligoacenes and further enhanced by intrinsic σ aromaticity, along with a wide range of HLG spectra spanning from 1.1 to 2.2 eV, offer a diverse selection for experimental studies, with tailored applications according to specific purpose on triple-chain boron clusters. To emphasize further that boron triple-chain structures are not entirely analogous to acenes, the UV-Vis spectra of boron triple-chain

compounds and oligoacenes displayed in Fig. S12 and S13,† with identical π electron configurations are presented in Fig. S10 (ESI file†). These electronic spectra demonstrate that triple-chain boron compounds exhibit the ability to absorb light across a broad range in the visible region, whereas oligoacenes mainly absorb light within a much narrower range and exhibit a pronounced blue-shift in the ultraviolet region.

4. Concluding remarks

The results obtained in the present theoretical study offer us a case of doped boron clusters in which the original boron framework remains largely unchanged as the number of phosphorus dopant atoms goes from 1 to 4. Indeed, both B_{10} and B_{16} host systems maintain their triple-chain form following sequential addition of P atoms. Furthermore, our calculated results indicate a perfect isovalent/isolobal substitution of $\{P\}$ with $\{CH\}$. The similarity in the number of delocalized electrons formed between the triple-chain form of the pure boron B_n^{2-} and the doped $B_{n-6}P_4$ clusters and in those formed by the substitution of $\{P\}$ with $\{CH\}$ thereafter are intriguing. A remarkable effect of P substitution is neutralization of both dianionic hosts. In each series, the triple-row form remains by far the global minimum, ensuring a high likelihood of its experimental detection.

This study does not diminish the significance of AdNDP in the analysis of chemical bonding in molecules. However, the subjective nature of AdNDP can lead to user-dependent results. Relying solely on AdNDP analysis can result in a significant misunderstanding of the chemical bonding involved. Therefore, it is essential to employ additional methods to verify the AdNDP findings.

The number of globally delocalized σ and π electrons present in these clusters and the magnetic ring current maps contribute to the verification that $B_xP_yC_zH_z$ triple-chain structures exhibit double aromaticity.

While the electron counting rule for the double-chain and ribbon species is $[\sigma^{2(n+1)}\pi^{2n}]$, the electron counting rule of $[\sigma^{2(n+1)}\pi_1^{2(n+1)}\pi_2^{2n}]$ is established in the present study for the triple-chain form. The latter is first introduced for the dianions B_{10}^{2-} and B_{16}^{2-} , and following doping, it is confirmed to be accurate for $B_{10}P_4$ and $B_{16}P_4$ through a similarity in electron configuration between the dianions and the doped derivatives. It can also be verified going from the configuration of $[\sigma^8\pi_1^{10}\pi_2^4]$ in B_{22}^{2-} to that of $[\sigma^8\pi_1^8\pi_2^6]$ in $B_{16}P_4$.

The model of a particle moving in a rectangular box proved to be effective in elucidating the relationship between the size of a structure and its electron configuration, thereby explaining the transition from an antiaromatic configuration of B_{22}^{2-} to an aromatic configuration of $B_{16}P_4$. The model of a particle moving in a rectangular box also helps us rationalize the decrease in the frontier orbital energy gap (HLG) of oligoacenes as their size increases.

The electron localization function (ELF) maps and their relationship with different types of bond lengths highlight the



self-locking phenomenon as a crucial point for a cluster structure to adhere to the triple-chain model and the $[\sigma^{2(n+1)}\pi_1^{2(n+1)}\pi_2^{2n}]$ electron configuration to satisfy the regions of enhanced rhombuses and alternately non-enhanced rhombus areas.

All structures considered have vertical attachment energies (VAEs) smaller than 4 eV and vertical ionization energies (VIEs) larger than 7 eV. The substitution of a {P} atom with a {CH} unit indeed enhances the thermodynamic stability of the boron triple-chain form, which helps facilitate its laboratory synthesis and open avenues for a new class of materials with versatile electronic properties. The calculated UV-Vis spectrum also suggests its potential application as a semi-conductor.

Data availability

AdNDP analysis for the T_d tetrahedron $B_{16}P_4-3$ isomer and triple-chain structures; the σ delocalized and π -MOs of triple-chain structures and π -MOs of some oligoacenes; the σ and π ring current maps of triple-chain structures; ELF $_{\sigma}$, ELF $_{\sigma d}$, and ELF $_{\pi}$ of triple-chain structures; the predicted electronic absorption spectrum of triple-chain and some oligoacenes; and tables of the HOMO–LUMO gap (HLG), VIE, VAE, hardness (η), electronegativity (χ) and electrophilicity (ω) of triple-chain structures.

The quantum chemical program Gaussian 16 has been used. The reference to this program is given in the list of references. The datasets supporting this article are uploaded as part of the ESI file† that also includes the Cartesian coordinates of the optimized geometries and information on their electronic structures.

Conflicts of interest

The authors declare no conflicts of interest.

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