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# The aromatic nature of auracycles and diauracycles based on calculated ring-current strengths†

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We have calculated the magnetically induced current density susceptibility for gold-containing organo-metallic molecular rings using the gauge-including magnetically induced currents (GIMIC) method. The aromatic nature has been determined by calculating the strength of the magnetically induced ring current susceptibility, which is often called ring current. To our knowledge, we show here for the first time that gold-containing organometallic rings may be aromatic or antiaromatic sustaining ring currents in the presence of an external magnetic field. The calculated aromatic character of the rings agrees with the aromatic nature one expects when using Hückel's aromaticity rules. The studied auracycles and diauracycles with  $4n$  electrons in the conjugated orbitals generally sustain a weak paratropic ring current, whereas those having  $4n + 2$  electrons in the conjugated orbitals sustain a diatropic ring current that is almost as strong as that of benzene. The number of electrons are obtained by assuming that each C, N and Au atom of the ring contribute one electron, and a H atom connected to a N atom in the ring increases the number of electrons by one. An electron-attracting ligand at Au removes one electron from the ring. Formation of a short Au–Au bonding diauracycles reduces the number of electrons in the ring by two.

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## 1 Introduction

The *metalloaromaticity* concept refers to organometallic molecules that exhibit chemical and physical properties similar to those of classical organic aromatic molecules such as benzene.<sup>1,2</sup> These properties include planar molecular rings with bond-length equalization, distinctive <sup>1</sup>H NMR chemical shifts of exo and endocyclic protons due to the magnetically induced ring current, and an enhanced thermodynamical stability relative to non-aromatic analogues. Examples of such metal-containing molecules include metallabenzenes, metallabenzenoids, metallabenzynes, (spiro)metalloles, metallapentalenes, and metallapentalynes, which are obtained by the formal replacement of a CH group (or C atom) of the parental molecule by an isolobal metallic fragment. In particular, gold-

containing molecular rings can also be constructed by replacing C–C≡C–C moieties of organic rings by C–Au–N.<sup>3</sup>

Aromaticity itself is an already fuzzy concept,<sup>4,5</sup> but it becomes even fuzzier for this kind of molecules.<sup>6</sup> The main reason is that there is no consensus on the number of occupied metal d orbitals participating in the  $\pi$  binding with the conjugated bonds of the organic fragment, leading to an unclear number of electrons in the conjugated orbitals. Möbius and Craig-Möbius aromaticity models,<sup>7–10</sup> for which  $4n$   $\pi$  electrons lead to aromaticity, are invoked for explaining disagreements between the classical Hückel's  $4n + 2$   $\pi$ -electron rule and the experimental properties of metalloaromatic molecules.

The first reported stable metallabenzene was osmabenzene [OsC<sub>5</sub>H<sub>4</sub>(SMe)(CO)(I)(PPh<sub>3</sub>)<sub>2</sub>], which was synthesized by Roper *et al.*<sup>11</sup> The synthesis was followed by other examples where the ring contains osmium, iridium, platinum, ruthenium, or rhodium.<sup>1,12–24</sup> Surprisingly, no *aurabenzene*, *i.e.* a metallabenzene containing gold, has yet been reported, despite the fact that platinum(II) and iridium(I) are isoelectronic with gold(III). Representative examples of aromatic platinum and iridium containing molecular rings are platinabenzenes,<sup>25,26</sup> iridafurans,<sup>27</sup> spiroaromatic platinacycles,<sup>28</sup> and the antiaromatic platinacorrole.<sup>29</sup> Many reviews have been written about metallabenzenes.<sup>1,13–16,19,30–33</sup>

There are few examples of gold complexes such as gold(III) auracyclopentadienes that may exhibit metalloaromaticity.

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† Electronic supplementary information (ESI) available: Cartesian coordinates of molecules 1–18, X–Au–X angles of molecules 1–18, selected molecular orbitals of molecules 1–5, 13, and 16, MIC strengths of molecules 1–4 at X2C-1C and X2C-2C levels of theory, 3D streamline plots of the MIC density pathways of molecules 1–18. See DOI: <https://doi.org/10.1039/d4dt00827h>



Usón *et al.* prepared the first auracyclopentadiene complex  $[\text{AuCl}(\text{C}_4\text{Ph}_4)(\text{tht})]$  (tht = tetrahydrothiophene) and its dimer  $[\text{Au}(\mu^2\text{-Cl})(\text{C}_4\text{Ph}_4)]_2$  by the transmetallation reaction of  $[\text{Sn}(\text{C}_4\text{Ph}_4)\text{Me}_2]$  and  $[\text{AuCl}_3(\text{tht})]$ .<sup>34</sup> These complexes further react with neutral and anionic ligands with release of the labile tht ligand or leading to chloride bridge cleavage, respectively.<sup>34,35</sup> Structural evidence was provided for  $[\text{AuCl}(\text{C}_4\text{Ph}_4)(\text{phen})]$  (phen = phenanthroline), which features a planar five-membered  $\text{AuC}_4$  ring shown in Fig. 1.<sup>35</sup> This  $\text{AuC}_4$  core has also been structurally characterized as an intermediate in the gold (iii)-catalyzed conversion of enyne-amines into cyclopentadienes,<sup>36</sup> and as a precursor of a ( $\eta^1$ -cyclobutadiene)gold(i) complex, which is obtained by reductive elimination.<sup>37</sup> Other types of gold-containing aromatic rings may remain to be discovered, as the aromatic nature of gold complexes has not yet been studied in depth.

Here, we examine the magnetically induced current (MIC) density susceptibility and the aromatic behaviour of model auracycles and diauracycles by performing calculations with the gauge-including magnetically induced currents (GIMIC) method. A globally aromatic (antiaromatic) molecule is able to sustain a strong net diatropic (paratropic) MIC density around the whole molecular ring, where a diatropic ring current means that the current-density flux is in the classical circulation direction and paratropic represents a current-density flux in the opposite direction. The employed computational methods are presented in section 2. The results obtained in the computational studies on auracycles and diauracycles are discussed in section 3. The study is summarized and conclusions are drawn in section 4.

## 2 Computational details

The electronic structure calculations were carried out using TURBOMOLE versions 7.7.1 and 7.8- $\beta$ .<sup>38,39</sup> The starting structures were built from scratch and optimized at the density functional theory (DFT) level using the  $\omega$ B97X-D functional,<sup>40</sup> the def2-TZVP basis sets on all atoms<sup>41</sup> and the 60-electron def2-ecp effective core potential (ECP) for gold.<sup>42,43</sup> The mole-

cular structures were verified to be minima by calculating vibrational frequencies using the aoforce module of TURBOMOLE.<sup>44</sup> The molecular structures were reoptimized at the second-order Møller–Plesset (MP2) level of theory with def2-TZVP basis sets using the ricc2 module of TURBOMOLE.<sup>41,45,46</sup> The structures optimized at the MP2 level were used in the calculations of the magnetically induced current (MIC) densities using the gauge-including magnetically induced currents (GIMIC) method.<sup>47–49</sup> The current densities, which are also called ring-current strengths, were calculated at the DFT level using the BHandHLYP functional (LIBXC ID 436) and def2-TZVP basis sets.<sup>41,50,51</sup> In the MIC calculations, the core electrons of Au were replaced by the def2-ecp relativistic ECP.<sup>42</sup>

We also performed magnetic shielding calculations at the all-electron scalar-relativistic exact two-component (1C-X2C) level, and at the two-component (2C-X2C) level including spin-orbit effects.<sup>52,53</sup> Triple- $\zeta$  polarization basis sets developed for one- and two-component all-electron relativistic electronic structure calculations were used.<sup>54</sup>

The aromatic nature of the gold-containing rings was determined by integrating the current density passing through a plane, which is perpendicular to the ring and cuts half of it.<sup>47,48</sup> The ring-current strengths were also calculated by numerical line integration of Ampère-Maxwell's law.<sup>55</sup> The geometric center of the ring and the vortex center of the current density were assumed to coincide. At the X2C levels, the ring-current strengths were only calculated using Ampère-Maxwell's law because the picture change effect is considered in the magnetic shielding calculations but not in the current-density calculations. The obtained ring-current strength yields the aromatic nature that can be compared to the one estimated from the number of electrons in the conjugated bonds of the ring.

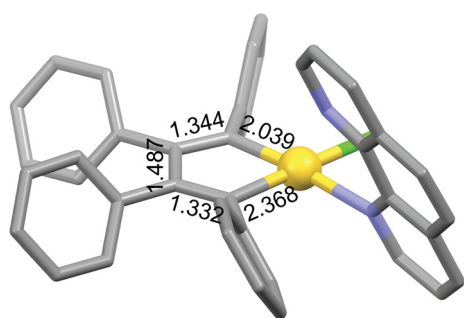
The MIC density pathways were plotted with ParaView version 5.11.0.<sup>56</sup> The strength of the MIC density is represented with a black-red-orange-yellow-white color scale.

## 3 Results and discussion

### 3.1 Auracycles

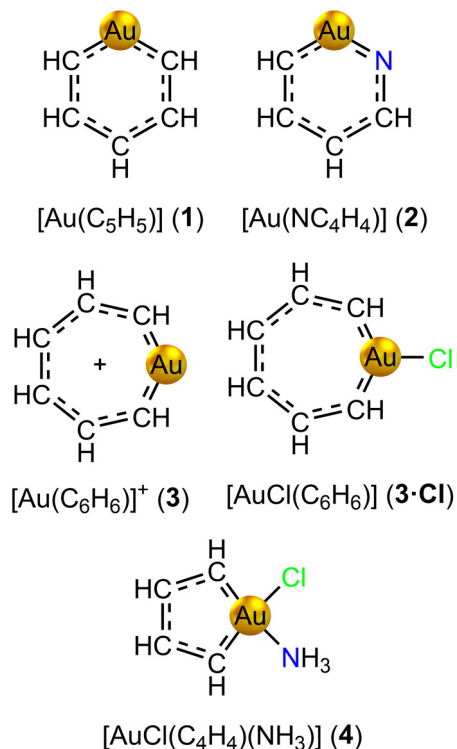
We have designed gold-containing analogues of regular Hückel aromatic benzene, pyridine and the cycloheptatrienyl cation by replacing a CH unit with a gold(i) atom (see Fig. 2). The negative charge of the carbon bridge is neutralized with the positive one of gold(i). The positive charge of  $[\text{Au}(\text{C}_6\text{H}_6)]^+$  is further neutralized with a chloride ligand attached to the metal. Our attempts to obtain an optimized structure for gold(i) auracyclopentadienide  $[\text{Au}(\text{C}_4\text{H}_4)]^-$  were unsuccessful due to convergence problems in the self-consistent field optimization of the orbitals. However, we designed the gold(III) analogue  $[\text{AuCl}(\text{C}_4\text{H}_4)(\text{NH}_3)]$  (4) as a model of the reported gold(III) auracyclopentadienes.

The number of electrons in the conjugated ring was estimated by assuming that each C, N and Au atom contribute one electron and an H atom connected to a N atom increases



**Fig. 1** The  $\text{AuC}_4$  core of  $[\text{AuCl}(\text{C}_4\text{Ph}_4)(\text{phen})]$  (Cambridge Structural Database refcode: BULPED).<sup>35</sup> Bond distances are given in Å. Hydrogen atoms are omitted for clarity. Color code: C, grey; Au, yellow; Cl, green; N, blue.





**Fig. 2** Molecular structures of aurabenzene (1), aurapyridine (2), auratropylium cation (3) and its chloride complex (3-Cl), and auracyclopentadiene (4) models.

the number of electrons in the ring by one. Substituting Cl or other electron attracting moieties to Au removes an electron from the ring.

The optimized molecular structure of aurabenzene  $[\text{Au}(\text{C}_5\text{H}_5)]$  (1) belongs to the  $C_2$  point group. It deviates from the regular structure of benzene due to the C–Au–C angle of  $103.1^\circ$  imposed both by the larger size of Au with respect to the replaced CH group, and by the tendency of Au to linear dicoordination in the formal +1 oxidation state. While the  $\text{AuC}_5$  core is planar, the hydrogen atoms are bent out of the plane. A similar bent structure is found for *ortho*-aurapyridine  $[\text{Au}(\text{NC}_4\text{H}_4)]$  (2), where the substitution of an *ortho*-CH group with a N atom breaks the symmetry to the  $C_1$  point group. The auratropylium cation  $[\text{Au}(\text{C}_6\text{H}_6)]^+$  (3) features a boat-shaped structure with the gold atom pointing out of the mean plane, and belonging to the  $C_s$  point group. Conversely, the structure of the auratropylium chloride complex  $[\text{AuCl}(\text{C}_6\text{H}_6)]$  (3-Cl) is perfectly planar belonging to the  $C_{2v}$  point group. Molecule  $[\text{AuCl}(\text{C}_4\text{H}_4)(\text{NH}_3)]$  (4) is also planar, belonging to the  $C_s$  point group. The analysis of the frontier molecular orbitals collected in Fig. S1† reveals that Au 5d orbitals do not participate much in the  $\pi$ -conjugation of molecules 1–4.

The ring-current strengths of auracycles 1–4 calculated at the DFT/BHandHLYP/def2-TZVP level of theory are collected in Table 1, together with those of benzene, pyridine, and the cycloheptatrienyl cation, for comparative purposes. Calculation of the MIC density shows that 1 sustains a strong

net diatropic ring current of  $10.51 \text{ nA T}^{-1}$ , which is almost as strong as the one for benzene of  $12.44 \text{ nA T}^{-1}$ .<sup>47</sup> Visualization of the MIC density pathways of 1 as 3D streamlines (see the ESI†) shows that the Au atom acts as a vortex centre connecting the diatropic ring current on both sides of the molecule, probably because the ring is not completely planar. A paratropic ring current flows along the inner rim of the molecular ring as also in benzene. The ring-current strength of 2 is  $7.41 \text{ nA T}^{-1}$ , revealing that it is less aromatic than 1 and pyridine. The MIC density pathways of 2 are similar to those of 1, with an additional coiling of the MIC around the C–N bond. The auratropylium models 3 and 3-Cl corresponding to  $(\text{C}_7\text{H}_7)^+$  are weakly aromatic sustaining a ring current of 3.82 and  $4.21 \text{ nA T}^{-1}$ , respectively. 3 and 3-Cl have a diatropic MIC density pathway around the Au atom that extends to the adjacent C atoms. They have a diatropic ring current along the outer edge and a paratropic ring current inside the ring. Molecule 4 is weakly antiaromatic sustaining a net paratropic ring current of  $-4.41 \text{ nA T}^{-1}$  inside the ring and a diatropic atomic current around the Au atom.

We have also calculated the ring-current strength of molecules 1–4 at all-electron relativistic levels of theory, which are reported in the ESI.† The ring-current strength of 1 is  $14.32 \text{ nA T}^{-1}$  at the fully relativistic 2C-X2C level. Spin-orbit effects increase the ring-current strength by  $3.81 \text{ nA T}^{-1}$  or 36% as compared to the one calculated at the quasi-relativistic level using ECPs. The ring-current strength calculated at the scalar X2C level is  $10.43 \text{ nA T}^{-1}$ , which agrees well with the strength calculated using the ECP.

The appearance of a strong ring current in the presence of a magnetic field is only one of the several ways in which aromaticity manifests itself. Thus, the proposed aromatic behaviour of auracycles 1–4 has been further studied by calculating the associated thermodynamic stabilization using the isomerization stabilization energy (ISE) method.<sup>57</sup> The ISE is calculated as the total energy difference between a methyl derivative of the aromatic molecule and its non-aromatic exocyclic methylene isomer. This method has been successfully applied to assess the aromaticity of several related metallabenzenes for which experimental evidence is available.<sup>20</sup> The considered tautomerization processes and the corresponding ISE values calculated at the MP2/def2-TZVP level of theory are shown in

**Table 1** The net, diatropic, and paratropic ring-current strengths (in  $\text{nA T}^{-1}$ ) of auracycles 1–4 and selected aromatic molecules, calculated at the DFT/BHandHLYP/def2-TZVP level of theory

Molecule	Net	Diatropic	Paratropic
$[\text{Au}(\text{C}_5\text{H}_5)]$ (1)	10.51	15.63	−5.11
$[\text{Au}(\text{NC}_4\text{H}_4)]$ (2)	7.41	13.06	−5.65
$[\text{Au}(\text{C}_6\text{H}_6)]^+$ (3)	3.82	11.92	−8.10
$[\text{AuCl}(\text{C}_6\text{H}_6)]$ (3-Cl)	4.21	12.08	−7.87
$[\text{AuCl}(\text{C}_4\text{H}_4)(\text{NH}_3)]$ (4)	−4.41	6.20	−10.61
$\text{C}_6\text{H}_6$	12.44	17.40	−4.96
$\text{C}_5\text{H}_5\text{N}$	12.01	17.08	−5.07
$(\text{C}_7\text{H}_7)^+$	12.43	17.70	−5.27



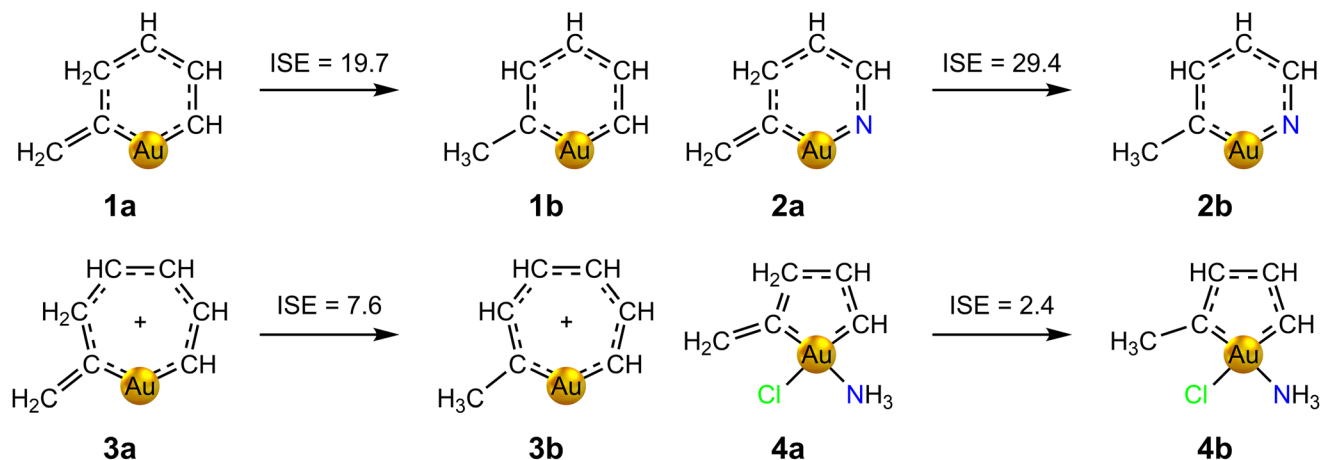


Fig. 3 Isomerization stabilization energies (in kcal mol<sup>-1</sup>) of auracycles 1–4, calculated at the MP2/def2-TZVP level of theory.

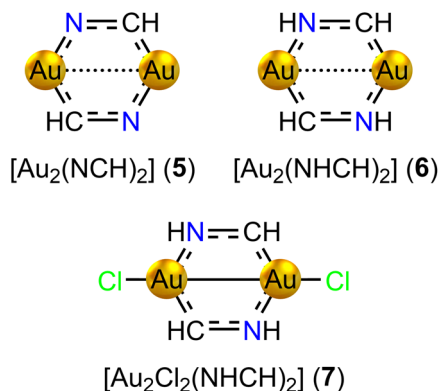


Fig. 4 The molecular structures of the six-membered diauracycle models 5–7.

Fig. 3. The obtained ISE values confirm the aromatic character suggested by the calculated ring-current strengths, and decrease in the series  $2 > 1 > 3 > 4$ . The trend agrees well with that obtained in the calculations of the ring-current strengths, although the correlation is not perfect. In particular, the ISE of molecule 2 of 29.4 kcal mol<sup>-1</sup> is *ca.* 10 kcal mol<sup>-1</sup> larger than the one of molecule 1, whereas 1 exhibits the strongest ring current in the series. This could be explained by the presence of the N atom.

### 3.2 Diauracycles

We have designed three series of model diauracycles of increasing size from six (5–7, Fig. 4) to eight (8–14, Fig. 5) to ten (15–17, Fig. 6) members, and studied their aromatic behaviour. The contribution of each atom to the total number of

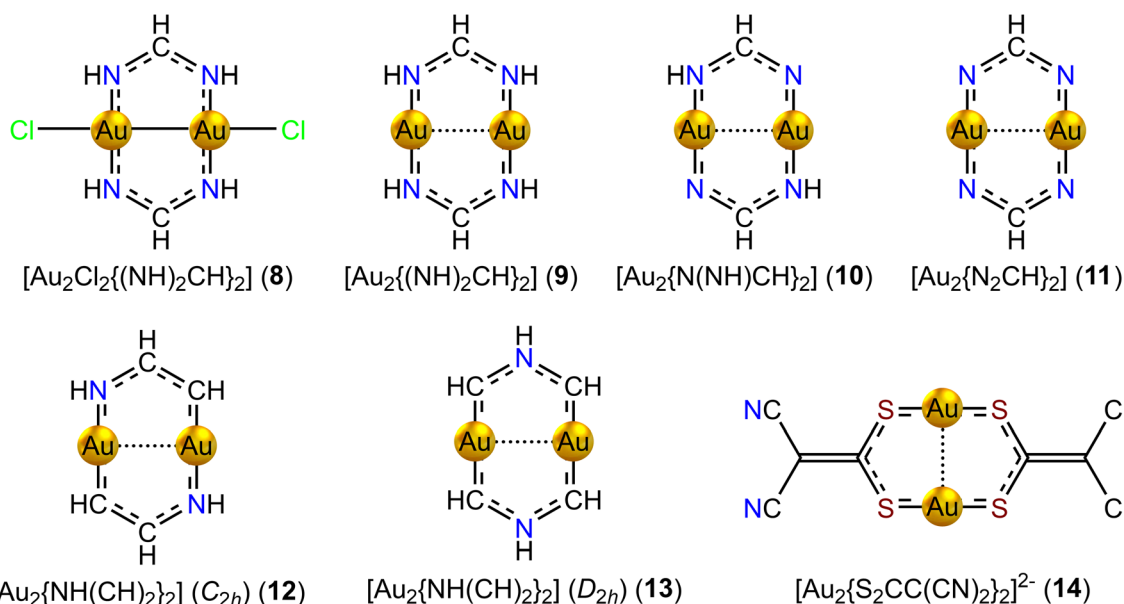


Fig. 5 The molecular structures of the eight-membered diauracycle models 8–14.



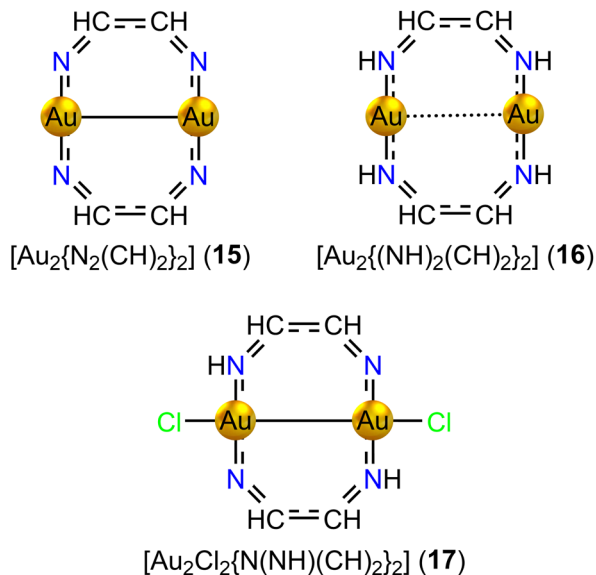


Fig. 6 The molecular structures of the ten-membered diauracyclic models 14–17.

electrons has been elucidated by analyzing the effect on the calculated MIC strength of binding Cl and H atoms to Au and N, respectively. Adding Cl is expected to oxidize gold(I) ( $[\text{Au}^{\text{I}}]: [\text{Xe}] 4f^{14} 5d^{10}$ ) to gold(II) ( $[\text{Au}^{\text{II}}]: [\text{Xe}] 4f^{14} 5d^9$ ), whereas binding H to N increases the number of electrons in the bond conjugation by one. The oxidized Au atoms can form a short Au–Au bond that also removes two electrons from the ring. The expected aromatic nature according to Hückel's aromaticity rules can then be determined.

**3.2.1 Six-membered diauracycles.** The molecular structure of  $[\text{Au}_2(\text{NCH})_2]$  (5) is a six-membered ring belonging to the  $C_{2h}$  point group. The transannular Au–Au distance is 293.3 pm at the MP2/def2-TZVP level. It has 6 electrons in the conjugated orbitals around the aromatic ring that sustain a net diatropic ring current of  $12.43 \text{ nA T}^{-1}$  along the outer edge of the molecular ring. It also has atomic vortices around the Au atoms extending from the Au atoms on both sides to half the Au–Au distance, where it returns. A weak diatropic MIC density pathway of  $1.80 \text{ nA T}^{-1}$  passes between the Au atoms.

Adding two H atoms to the N atoms of  $[\text{Au}_2(\text{NCH})_2]$  yields  $[\text{Au}_2(\text{NHCH})_2]$  (6,  $C_{2h}$ ) with 8 electrons in the bond conjugation of the six-membered ring. The Au–Au distance is 264.0 pm. The strength of the ring-current inside the ring is  $-2.96 \text{ nA T}^{-1}$ . The ring is weakly antiaromatic as expected from Hückel's aromaticity rule. It has diatropic atomic currents around the Au atoms. The Au–Au bond of 6 sustains a diatropic ring current of  $3.98 \text{ nA T}^{-1}$ , which is more than twice the strength of the Au–Au bond current of 5 with a longer Au–Au distance.

Adding two Cl atoms to the Au atoms of 6 yields  $[\text{Au}_2\text{Cl}_2(\text{NHCH})_2]$  (7,  $C_{2h}$ ). 7 has a short Au–Au distance of 244.8 pm. A very strong diatropic bond current of  $9.73 \text{ nA T}^{-1}$  circulates around the short Au–Au bond. The short Au–Au distance and population analysis indeed suggest that gold is in

Table 2 The net, diatropic, and paratropic ring-current strengths (in  $\text{nA T}^{-1}$ ) of the six-membered diauracycles 5–7, calculated at the DFT/BHandHLYP/def2-TZVP level of theory

Molecule	Net	Diatropic	Paratropic
$[\text{Au}_2(\text{NCH})_2]$ (5)	12.43	18.13	−5.70
$[\text{Au}_2(\text{NHCH})_2]$ (6)	−2.96	8.67	−11.63
$[\text{Au}_2\text{Cl}_2(\text{NHCH})_2]$ (7)	−1.18	9.40	−10.58

the +2 oxidation state. Since the Cl atoms remove two electrons from the ring and a Au–Au bond is formed, the ring fulfills Hückel's  $4n$  rule for antiaromaticity. However, the ring of 7 is nonaromatic sustaining a net global ring current of  $-1.18 \text{ nA T}^{-1}$ . The ring-current strengths of the six-membered diauracycles 5–7 calculated at the DFT/BHandHLYP/def2-TZVP level of theory are given in Table 2.

**3.2.2 Eight-membered diauracycles.** The synthesized eight-membered diauracycles  $[\text{Au}_2\text{Cl}_2(2,6\text{-Me}_2\text{PhN}_2\text{CH})_2]$  and  $[\text{Au}_2(2,6\text{-Me}_2\text{PhN}_2\text{CH})_2]$  have a Au–Au distance of 256.71(19) pm and 271.2(2) pm, respectively.<sup>58</sup> Two electrons are transferred from the ring to the Cl atoms. The Au–Au distance is shorter with the Cl atoms or with another molecular moiety that attracts electrons. When  $\text{C}_6\text{H}_5\text{COO}^-$  is added to the Au atoms of  $[\text{Au}_2(2,6\text{-Me}_2\text{PhN}_2\text{CH})_2]$ , the Au–Au distance is 2.489 (10) Å, which is one of the shortest Au–Au distances.<sup>58</sup> The corresponding model compounds are  $[\text{Au}_2\text{Cl}_2\{(\text{NH})_2\text{CH}\}_2]$  (8,  $D_{2h}$ ) and  $[\text{Au}_2\{(\text{NH})_2\text{CH}\}_2]$  (9,  $D_{2h}$ ). 8 is weakly antiaromatic with a ring current of  $-3.02 \text{ nA T}^{-1}$ . The Au–Au distance is 250.2 pm because Cl oxidizes  $\text{Au}^{\text{I}}$  to  $\text{Au}^{\text{II}}$  forming a Au–Au bond. A strong diatropic ring current of  $10.40 \text{ nA T}^{-1}$  circulates around the short Au–Au bond and extends to the whole molecule except for the carbon moiety. It is weakly antiaromatic since the organic part of the ring contributes 10 electrons to the conjugated bonds. The chloride ligands remove two electrons from the ring and two electrons of the oxidized gold atoms form the Au–Au bond yielding 8 electrons in the conjugated ring.

The corresponding model compound without the Cl atoms 9 has 12 electrons in the conjugated bonds. 9 is weakly antiaromatic sustaining a paratropic ring current of  $-1.88 \text{ nA T}^{-1}$ . The Au–Au distance of 273.6 pm is much longer than for 8. 9 also sustains a weak diatropic bond current of  $2.69 \text{ nA T}^{-1}$  in the vortex of the Au–Au bond. The calculated Au–Au distances of the model compounds 8 and 9 agree qualitatively with the experimental Au–Au distances for  $[\text{Au}_2\text{Cl}_2(2,6\text{-Me}_2\text{PhN}_2\text{CH})_2]$  and  $[\text{Au}_2(2,6\text{-Me}_2\text{PhN}_2\text{CH})_2]$ .

Removing two of the four H atoms of the NH moieties from 9 yields  $[\text{Au}_2\text{N}(\text{NH})\text{CH}_2]$  (10,  $C_i$ ). The s electrons of the Au atoms contribute to the 10 electrons in the conjugated bonds. The Au–Au distance is 279.5 pm. The eight-membered ring is weakly aromatic sustaining a ring current of  $5.78 \text{ nA T}^{-1}$ . There is a weak diatropic ring current of  $1.97 \text{ nA T}^{-1}$  between the two Au atoms.

Removing all four H atoms from the NH moieties of 9 leads to  $[\text{Au}_2(\text{N}_2\text{CH})_2]$  (11,  $C_{2h}$ ), whose ground state is an aromatic



triplet state sustaining a ring current of  $11.12 \text{ nA T}^{-1}$ . The Au–Au distance is 263.3 pm and a bond current of  $3.65 \text{ nA T}^{-1}$  circles around the vortex of the Au–Au bond. The ring has formally 8 electrons in the conjugated bonds fulfilling Hückel's  $4n$  aromaticity rule for triplet states. Structure optimization at the RI-MP2/def2-TZVP level failed for this molecule.

Replacing two of the NH moieties of **9** by CH yields  $[\{\text{Au}_2\text{NH}(\text{CH})_2\}_2]$  (**12**,  $C_{2h}$ ), with 10 electrons in the conjugated bonds. **12** has a Au–Au distance of 250.0 pm suggesting that the oxidation state is  $\text{Au}^{\text{II}}$ , which also agrees with the population analysis. The formation of the Au–Au bond reduces the total number of conjugated electrons to 8, leading to antiaromaticity. **12** is nonaromatic sustaining a very weak paratropic ring current of  $-1.69 \text{ nA T}^{-1}$ , whereas a strong diatropic bond current of  $9.88 \text{ nA T}^{-1}$  circulates around the vortex of the short Au–Au bond.

The NH moiety can also be placed in the middle between the two CH groups. The symmetric  $[\{\text{Au}_2\text{NH}(\text{CH})_2\}_2]$  (**13**,  $D_{2h}$ ) has a long Au–Au distance of 276.5 pm. **13** has 10 electrons in the conjugated bonds and is aromatic sustaining a diatropic ring current whose strength is  $12.32 \text{ nA T}^{-1}$ . A weak diatropic bond current of  $2.50 \text{ nA T}^{-1}$  circulates around the vortex of the long Au–Au bond. Thus, the electronic structures of the symmetric **13** and non-symmetric **12**  $[\{\text{Au}_2\text{NH}(\text{CH})_2\}_2]$  isomers are different. The charge of the Au atoms of **13** is  $0.46e$  as compared to  $0.85e$  for **12**.

Other kinds of diauracycles like  $[\{\text{Au}_2\text{S}_2\text{CC}(\text{CN})_2\}_2]^{2-}$  (**14**,  $D_2$ ) have also been synthesized.<sup>59</sup> **14** has a Au–Au distance of 275.8 pm. Since the ring has several C–S and S–Au single bonds, it is expected to sustain a weak ring current, if any. The calculated ring-current strength of **14** is  $-1.97 \text{ nA T}^{-1}$  and the Au–Au bond sustains a diatropic bond current of  $2.65 \text{ nA T}^{-1}$ . The ring-current strengths of the eight-membered diauracycles **8–14** calculated at the DFT/BHandHLYP/def2-TZVP level of theory are given in Table 3.

**3.2.3 Ten-membered diauracycles.** Even though  $[\text{Au}_2\{\text{N}_2(\text{CH})_2\}_2]$  (**15**,  $D_{2h}$ ) is a ten-membered ring having formally 10 electrons in the conjugated bonds, MIC density calculations show that **15** is antiaromatic sustaining a paratropic ring current of  $-22.01 \text{ nA T}^{-1}$ . **15** sustains a strong diatropic bond current of  $10.71 \text{ nA T}^{-1}$  in the short Au–Au bond of 245.4 pm. Population analysis and the short Au–Au distance suggest that two electrons from Au form the Au–Au bond. Thus, the

**Table 3** The net, diatropic, and paratropic ring-current strengths (in  $\text{nA T}^{-1}$ ) of the eight-membered diauracycles **8–14**, calculated at the DFT/BHandHLYP/def2-TZVP level of theory

Molecule	Net	Diatropic	Paratropic
$[\text{Au}_2\text{Cl}_2\{(\text{NH})_2\text{CH}\}_2]$ ( <b>8</b> )	-3.02	7.17	-10.19
$[\text{Au}_2\{(\text{NH})_2\text{CH}\}_2]$ ( <b>9</b> )	-1.88	8.30	-10.18
$[\{\text{Au}_2\text{N}(\text{NH})\text{CH}\}_2]$ ( <b>10</b> )	5.78	12.14	-6.36
$[\text{Au}_2(\text{N}_2\text{CH})_2]$ ( <b>11</b> )	11.12	17.06	-5.94
$[\{\text{Au}_2\text{NH}(\text{CH})_2\}_2]$ ( <b>12</b> )	-1.69	7.58	-9.27
$[\{\text{Au}_2\text{NH}(\text{CH})_2\}_2]$ ( <b>13</b> )	12.32	17.65	-5.33
$[\{\text{Au}_2\text{S}_2\text{CC}(\text{CN})_2\}_2]^{2-}$ ( <b>14</b> )	-1.97	8.40	-10.37

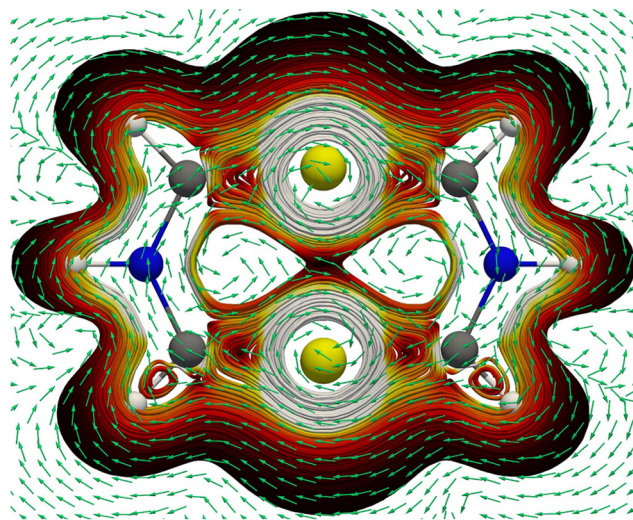
ring has 8 electrons in the conjugated bonds, which explains its antiaromaticity. **15** is to our knowledge the first strongly antiaromatic gold-containing molecular ring.

Adding four H atoms to the N atoms of **15** yielding  $[\text{Au}_2\{(\text{NH})_2(\text{CH})_2\}_2]$  (**16**,  $D_{2h}$ ) increases the Au–Au distance to 284.8 pm, which suggests that the s electrons of Au contribute to the conjugated bonds of the ring. **16** with 14 electrons in the ring is strongly aromatic. It sustains a strong global diatropic ring current and two weaker paratropic ring currents inside the  $\text{Au}_2\text{N}_2\text{C}_2$  rings that touch each other in the center of the Au–Au interaction forming a sandglass-shaped ring current. The strength of the ring current along the organic fragment is  $13.83 \text{ nA T}^{-1}$  and the net ring current passing between the gold atoms is  $3.33 \text{ nA T}^{-1}$ .

Removing H atoms from two of the N atoms of **16** and adding Cl atoms to the Au atoms yield  $[\{\text{Au}_2\text{Cl}_2\text{N}(\text{NH})(\text{CH})_2\}_2]$  (**17**,  $C_2$ ). The molecular structure of **17** has a short Au–Au distance of 250.1 pm. Population analysis and the short Au–Au distance suggest that the s electrons are transferred to Cl and the Au atoms are in oxidation state  $\text{Au}^{\text{II}}$  forming a Au–Au bond. Thus, only 8 electrons contribute to the conjugated bonds. However, **17** is nonaromatic instead of antiaromatic sustaining a weak ring current of  $-0.44 \text{ nA T}^{-1}$ . A strong diatropic

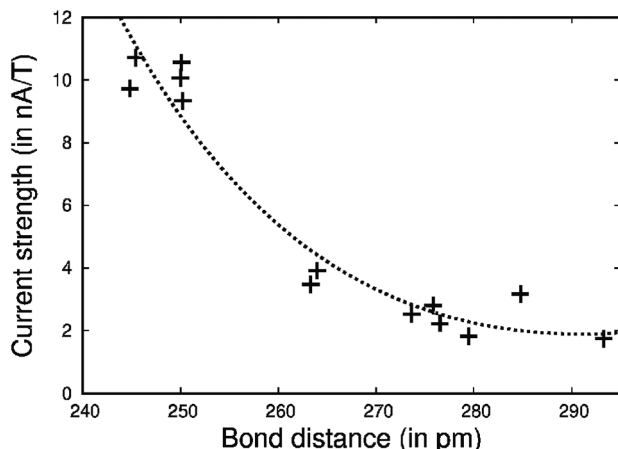
**Table 4** The net, diatropic, and paratropic ring-current strengths (in  $\text{nA T}^{-1}$ ) of the ten-membered diauracycles **15–17**, calculated at the DFT/BHandHLYP/def2-TZVP level of theory

Molecule	Net	Diatropic	Paratropic
$[\text{Au}_2\{(\text{N}_2(\text{CH})_2\}_2]$ ( <b>15</b> )	-22.01	23.89	-1.88
$[\text{Au}_2\{(\text{NH}_2)(\text{CH}_2)_2\}_2]$ ( <b>16</b> )	13.83	17.78	-3.95
$[\text{Au}_2\text{Cl}_2\{(\text{NH}_2)(\text{CH}_2)_2\}_2]$ ( <b>17</b> )	-0.44	4.61	-5.05



**Fig. 7** The 3D streamline plot of the MIC density pathways of the aromatic  $[\text{Au}_2\{(\text{CH})_2\text{NH}\}_2]$  (**13**). The flux direction of the MIC density is indicated by the green arrows that point in the clockwise (anticyclotronic) direction when the MIC density is diatropic (paratropic). Color code: C, grey; H, white; Au, yellow; N, blue.





**Fig. 8** The strength of the current-density vortex ( $I(x)$  in  $\text{nA T}^{-1}$ ) of the Au–Au bond as a function of the Au–Au distance ( $x$  in pm). The ring-current strengths were calculated at the DFT/ $\omega$ B97X-D level using the Ampère-Maxwell approach. The  $a$ ,  $b$  and  $c$  parameters of  $I(x) = a + b(240 - x) + c/(180 - x)$  are optimized to fit  $I(x)$  to the numerical values in the ESI.†

pic bond current of  $10.56 \text{ nA T}^{-1}$  circulates around the vortex of the short Au–Au bond. The ring-current strengths of the eight-membered diauracycles 15–17 calculated at the DFT/BHandHLYP/def2-TZVP level of theory are given in Table 4.

**3.2.4 MIC density pathways.** The MIC density pathways are similar for the thirteen studied diauracycles (see the ESI†). Fig. 7 shows the MIC density pathways of 13 as an example. There is a global diatropic ring current along the outer edge of the molecule. The Au atoms feature a local diatropic bond current with the vortex center between the Au atoms. The shape and strength of the vortex depend on the oxidation state of the Au atoms, *i.e.* whether they have a Cl ligand or not, and on the global aromatic character of the diauracycle. The strong atomic currents of the Au atoms split the paratropic ring current on the inside of the diauracycle into two smaller current-density vortices in the molecular rings formed by the organic fragment and the Au–Au axis. The center of the Au–Au interaction/bond is a stagnation point with no current density passing it. The current strength of the bond vortex depends strongly on the distance between the gold atoms as seen in Fig. 8. The bond-vortex strengths of the studied diauracycles are given in the ESI.†

## 4 Conclusions

The magnetically induced current (MIC) density susceptibility has been calculated for gold-containing organometallic molecular rings of different size by using the gauge-including magnetically induced currents (GIMIC) method. The aromatic nature of the rings has been investigated by calculating the strength of the magnetically induced ring current. The obtained aromatic nature was compared to the one judged from the number of electrons in the conjugated bonds accord-

ing to Hückel's aromaticity rules. The number of electrons in the conjugated bonds have been obtained by assuming that each conjugated C, N and Au atom contribute one electron. A H atom connected to a N atom in the ring increases the number of electrons in the bond conjugation by one. Substituting a chloride ligand or another electron attracting moiety to Au removes one electron from the ring. The formation of a short Au–Au bond in diauracycles also consumes two electrons from the ring.

When the ring has  $4n + 2$  electrons in the conjugated orbitals it is aromatic sustaining a strong diatropic ring current, whereas auracycles and diauracycles with  $4n$  electrons generally sustain a weak paratropic ring current. The studied molecules with  $4n$  electrons in the conjugated ring are with one exception weakly antiaromatic or non-aromatic. The calculations show that gold-containing organometallic rings follow Hückel's aromaticity rules and can indeed be aromatic or antiaromatic depending on the number of electrons in the conjugated bonds. More generally, one can state that the studied molecules with odd number of occupied conjugated orbitals are aromatic or weakly aromatic, whereas the studied molecules with even number of occupied conjugated orbitals are antiaromatic or nonaromatic. The generalized rule holds for both open-shell and closed-shell molecules.<sup>60</sup> Note that antiaromaticity is actually a stabilization with respect to nonaromaticity, otherwise it would not exist. The ring-current strengths, the number of electrons in the conjugated ring, and the aromatic nature of the studied molecules are summarized in Table 5.

Even though the number of  $\pi$  electrons determines the global aromatic character, geometrical features such as the pla-

**Table 5** The ring-current strength ( $I$  in  $\text{nA T}^{-1}$ ), the number of electrons in the conjugated bonds, and the aromatic nature of the studied molecules. SA is strongly aromatic ( $I \in [18, \infty) \text{ nA T}^{-1}$ ), A is aromatic ( $I \in [6, 18) \text{ nA T}^{-1}$ ), WA is weakly aromatic ( $I \in [3, 6) \text{ nA T}^{-1}$ ), NA is nonaromatic ( $I \in [-3, 3) \text{ nA T}^{-1}$ ), WAA is weakly antiaromatic ( $I \in [-6, -3) \text{ nA T}^{-1}$ ), AA is antiaromatic ( $I \in [-18, -6) \text{ nA T}^{-1}$ ), and SAA is strongly antiaromatic ( $I \in [-\infty, -18) \text{ nA T}^{-1}$ )

Molecule	# Electrons	$I$	Arom.
[Au(C <sub>5</sub> H <sub>5</sub> )] (1)	6	10.51	A
[Au(NC <sub>4</sub> H <sub>4</sub> )] (2)	6	7.41	A
[AuCl(C <sub>6</sub> H <sub>6</sub> )] (3)	6	4.21	WA
[AuCl(C <sub>4</sub> H <sub>4</sub> )(NH <sub>3</sub> )] (4)	4	-4.41	WAA
[Au <sub>2</sub> (NCH) <sub>2</sub> ] (5)	6	12.43	A
[Au <sub>2</sub> (NHCH) <sub>2</sub> ] (6)	8	-2.96	NA
[Au <sub>2</sub> Cl <sub>2</sub> (NHCH) <sub>2</sub> ] (7)	4	-1.18	NA
[Au <sub>2</sub> Cl <sub>2</sub> {(NH) <sub>2</sub> CH <sub>2</sub> }] (8)	8	-3.02	WAA
[Au <sub>2</sub> {(NH) <sub>2</sub> CH <sub>2</sub> }] (9)	12	-1.88	NA
[{Au <sub>2</sub> N(NH)CH <sub>2</sub> }] (10)	10	5.78	WA
[Au <sub>2</sub> (N <sub>2</sub> CH) <sub>2</sub> ] (11) <sup>a</sup>	8	11.12	A
[{Au <sub>2</sub> NH(CH) <sub>2</sub> }] (12)	8	-1.69	NA
[{Au <sub>2</sub> NH(CH) <sub>2</sub> }] (13)	10	12.32	A
[{Au <sub>2</sub> S <sub>2</sub> CC(CN) <sub>2</sub> }] <sup>2-</sup> (14)	16	-1.97	NA
[Au <sub>2</sub> {N <sub>2</sub> (CH) <sub>2</sub> }] (15)	8	-22.01	SAA
[Au <sub>2</sub> {(NH) <sub>2</sub> (CH) <sub>2</sub> }] (16)	14	13.83	A
[{Au <sub>2</sub> Cl <sub>2</sub> N(NH)(CH) <sub>2</sub> }] (17)	8	-0.44	NA
[AuCl(C <sub>4</sub> Ph <sub>4</sub> )(py)] (18)	4	-3.33	WAA

<sup>a</sup> Triplet state.



narity and strain of the ring also affect the strength of the ring current. The deviation of the calculated X–Au–X angles from the ideal ones of 180° for linear gold(i) and 90° for square-planar gold(III) is an adequate estimate of the ring strain. The X–Au–X angles and ring-current strengths of the studied molecules are collected in Table S3† for comparative purposes. For instance, the coordination of chloride (3-Cl) to [Au(C<sub>6</sub>H<sub>6</sub>)]<sup>+</sup> (3) results in a planar ring and releases the ring strain by slightly opening the C–Au–C angle, which consequently increases the ring-current strength and preserves the aromatic character.

Calculation of the ring-current strength of the AuC<sub>4</sub> core of [AuCl(C<sub>4</sub>Ph<sub>4</sub>)(phen)] (Fig. 1) is complicated because of the presence of the phenyl substituents and of the phenanthroline ligand capping the gold(III) atom. Thus, phenanthroline was replaced with pyridine leading to [AuCl(C<sub>4</sub>Ph<sub>4</sub>)(py)] (18), for which experimental evidence also exists.<sup>35</sup> The strength of the ring current that was obtained by applying Ampère-Maxwell's law is –3.33 nA T<sup>–1</sup> suggesting that it is weakly antiaromatic, which is also suggested by the 4n electrons in the conjugated ring.

To our knowledge, we show here for the first time that gold-containing organometallic rings may be aromatic or antiaromatic sustaining ring currents in the presence of an external magnetic field. Electron attracting ligands such as chloride oxidize Au<sup>I</sup> to Au<sup>II</sup> that can form a short Au–Au bond to another gold atom in the ring. There is a current density vortex between the gold atoms, whose strength increases with decreasing Au–Au distance.

## Author contributions

DB and DS have performed calculations and written the text.

## Conflicts of interest

There are no conflicts to declare.

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