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Fulminic Acid: A Quasibent Spectacle

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Abstract

Fulminic acid (HCNO) played a critical role in the early development of organic chemistry, and chemists have sought to discern the structure and characteristics of this molecule and its isomers for over 200 years. The mercurial nature of the extremely flat H–C–N bending potential of fulminic acid, with a nearly vanishing harmonic vibrational frequency at linearity, remains enigmatic and refractory to electronic structure theory, as dramatic variation with both orbital basis set and electron correlation method is witnessed. To solve this problem using rigorous electronic wavefunction methods, we have employed focal point analyses (FPA) to ascertain the *ab initio* limit of optimized linear and bent geometries, corresponding vibrational frequencies, and the HCN + O(³P) → HCNO reaction energy. Electron correlation treatments as extensive as CCSDT(Q), CCSDTQ(P), and even CCSDTQP(H) were employed, and complete basis set (CBS) extrapolations were performed using the cc-pCVXZ (*X* = 4-6) basis sets. Core electron correlation, scalar relativistic effects (MVD1), and diagonal Born-Oppenheimer corrections (DBOC) were all included and found to contribute significantly in determining whether vibrationless HCNO is linear or bent. At the all-electron (AE) CCSD(T)/CBS level, HCNO is a linear molecule with $\omega_5(\text{H-C-N bend}) = 120 \text{ cm}^{-1}$. However, composite AE-CCSDT(Q)/CBS computations give an imaginary frequency ($51i \text{ cm}^{-1}$) at the linear optimized geometry, leading to an equilibrium structure with an H–C–N angle of 173.9° . Finally, at the AE-CCSDTQ(P)/CBS level, HCNO is once again linear with $\omega_5 = 45 \text{ cm}^{-1}$, and inclusion of both MVD1 and DBOC effects yields $\omega_5 = 32 \text{ cm}^{-1}$. A host of other topics has also been investigated for fulminic acid, including the dependence of r_e and ω_i predictions on a variety of CBS extrapolation formulas, the question of multireference character, the N–O bond energy and enthalpy of formation, and issues that give rise to the quasibent appellation.



1. INTRODUCTION

Fulminic acid (HCNO) and its isomers isocyanic acid (HNCO), cyanic acid (HOCN), and isofulminic acid (HONC) have played pivotal roles in the history of chemistry,¹ and these compounds are still the target of much current research.²⁻⁵ Although fulminic acid is compositionally simple, this molecule has challenged generations of chemists and physicists seeking to uncover its structure and properties. Fulminic acid has been a test case for the development of spectroscopic methods of analysis owing to its intriguing rovibrational dynamics,^{6,7} and the species even has considerable astrochemical interest as a precursor to prebiotic molecules.⁸⁻¹²

In 1800 the English chemist Edward Howard first prepared salts of fulminic acid by reacting mercury oxide, nitric acid, and ethanol.^{1,13-15} The explosive properties of these salts led Howard to call them “fulminating,” appropriately drawing from the Latin *fulminare* meaning “to strike like lightning.”^{1,13,16} However, the primitive methods of quantitative analysis at the time were unable to elucidate the true identity of the compounds. Liebig was particularly fascinated by silver fulminate and in 1824 discovered that its percentage composition was identical to that of the silver cyanate prepared by Wöhler.^{1,15,17} As such, fulminic and cyanic acids gained widespread acclaim as examples of the newly discovered phenomenon of isomerism.¹⁷ Fulminate salts emerged as the predominant detonator for firing projectiles in the 19th century, and Alfred Nobel even introduced fulminate cartridges for the safe use of dynamite.^{1,14}

The quest to definitively establish the bonding in fulminic acid persisted for over a century.^{1,18-31} Fulminic acid was initially regarded as a two-carbon compound originating from ethanol, leading to many erroneous attempts at structural characterization.^{1,28-31} However, in 1894 Nef asserted that experimental evidence pointed to a one-carbon CNOH structure for fulminic acid, making it identical to carbyloxime.¹⁹⁻²¹ A formyl nitrile oxide structure (HCNO) was proposed²² as early as 1899 and favored by a theoretical analysis of free energies by Pauling in 1926,²³ but retention of the oxime formula persisted well into the 1950s.¹ Proof of the formyl nitrile oxide structure was finally obtained by Beck and coworkers in 1965-66 after the IR spectrum of pure gaseous fulminic acid revealed H–C–N–O connectivity.^{24,25}

Even after the connectivity was ascertained accurately, characterizing fulminic acid still proved elusive, as suspicions grew that the species was quasilinear. This classification is generally given to molecules with a nonlinear electronic minimum but a low barrier to linearity, allowing large-amplitude bending motion that engenders rovibrational spectra reminiscent of a linear



framework.^{7,32} Fitting the microwave spectrum recorded by M. Winnewisser and Bodenseh³³ to a linear structure gave rise to a disturbingly short $r_3(\text{C-H})$ distance; moreover, the lowest-frequency bending vibration ν_5 could not be located by Beck and Feldl²⁵ in the IR spectrum. The first experimental information for ν_5 was later obtained from analysis of the rotational transitions of seven HCNO excited vibrational states in 1969.³⁴

Although a wealth of low-resolution microwave, millimeter-wave, and infrared data had accumulated by 1974,³⁵⁻³⁷ the highly anharmonic, large-amplitude nature of the H-C-N bending vibration of fulminic acid was not clearly established until measurement and analysis in that year of the high-resolution far-infrared spectrum between 180 and 420 cm^{-1} with 0.1 cm^{-1} resolution.³⁸ One year later, Stone³⁹ performed a rigid-bender treatment of the ν_5 fundamental and overtone bands of HCNO and DCNO and extracted an associated one-dimensional model potential function with an equilibrium H-C-N angle of 161° and a barrier to linearity of 70 cm^{-1} . Shortly thereafter, the anomalous vibrational dependence of the observed rotational constants and l -doubling interactions were analyzed with a simple rovibrational Hamiltonian, placing the H-C-N angle near 170° and the barrier to linearity at only 2 cm^{-1} .⁴⁰ Substantial improvements in the previous analyses were made in 1979 by Bunker and coworkers,⁴¹ who used a semirigid bender Hamiltonian to fit the entire body of known HCNO and DCNO rovibrational energy separations.^{33-38,42-51} They concluded that vibrationless HCNO is linear within the uncertainty of the analysis but zero-point motion or vibrational excitation of the complementary stretching modes produces a nonlinear minimum on the effective potential curve for large-amplitude H-C-N bending.⁴¹ In 1983 Jensen⁵² extended the semirigid bender Hamiltonian to also account for the ν_4 C-N-O bending mode and confirmed the conclusions reached by Bunker et al.⁴¹ Technical details of this landmark research^{41,52} that deemed the molecule “quasibent” are discussed below when our new theoretical results are presented.

High-resolution rovibrational spectroscopy of the ground electronic state of HCNO and DCNO continued in earnest through the early 2000s. Additional infrared bands of HCNO in the 500-657 cm^{-1} region were characterized;⁵³ moreover, 46 l -sublevel vibrational satellites were assigned in the millimeter wave spectrum involving rotational transitions within excited vibrational manifolds having up to 4 quanta of bending.⁶ The vibrational band origins of HCNO were ascertained for nearly every state in the 700-7000 cm^{-1} region, revealing networks of anharmonic resonances.⁵⁴⁻⁵⁷ Far-infrared data for HCNO and DCNO were further refined to a precision of 0.0012 cm^{-1} (FWHM) in 2000.⁵⁴ Infrared, far-infrared, microwave, and millimeter



wave spectra were obtained and analyzed for five isotopologues of HCNO.⁵⁸⁻⁶⁵ Finally, in recent years the paradigmatic energy levels of fulminic acid involving the H–C–N bending mode have been analyzed via several novel approaches, including Lie algebraic methods,⁶⁶ as well as quantum monodromy⁶⁷ and quantum phase transitions^{68,69} within a champagne-bottle potential.

Even almost two centuries after its initial discovery, fulminic acid and its isomers captivated quantum chemists.^{32,70-84} Electronic structure computations gave muddled results for the equilibrium geometry of HCNO, as strong dependence on the orbital basis set and electron correlation method were observed. The struggles of early *ab initio* work with low levels of theory and small basis sets revealed the difficulty of the problem.^{70,71} In 1982, Farnell, Nobes, and Radom⁷² obtained a linear equilibrium structure for HCNO at the MP3/6-31G** level and computed harmonic vibrational frequencies as a function of the H–C–N angle; the zero-point vibrational energy of the complementary modes was shown to favor a bent structure, but this correction was not sufficient to overcome the Born-Oppenheimer potential function that favored linearity. In contrast, in 1989 a bent equilibrium structure was obtained at MP2/6-31G** with a nonnegligible barrier to linearity of 0.64 kcal mol⁻¹.⁷³ Similarly, in 1991 both the 6-31G** and 6-311G** basis sets produced bent structures at the MP2 and MP4 levels but linear structures at MP3 and CISD; MCSCF/DZP also gave a bent molecule, while MRCISD computations built on these MCSCF wave functions yielded either linear or bent structures depending on the choice of reference space.⁷⁴ The robust and newly popularized CCSD(T) theory was applied to HCNO for the first time in 1992 by Rendell, Lee, and Lindh,⁷⁵ predicting a linear structure upon use of a TZ2P basis set; however, four years later another study found that improving the method to CCSD(T)/cc-pVQZ produced a bent equilibrium geometry with a minuscule 7 cm⁻¹ barrier to linearity.⁷⁶ This led Albert and Quack⁸⁵ to comment in a 2007 report that prevailing quantum chemical research had failed to provide a full understanding of the observed rovibrational spectra of HCNO.

More recently in 2008, Mladenović and Lewerenz⁷⁷ computed both frozen-core and all-electron CCSD(T) results with the cc-pVXZ ($X = 2-6$) and cc-pCVXZ ($X = 2-5$) basis sets. The optimized H–C–N bending angle of fulminic acid varied nearly 30° with basis set, but the best results trended toward a true linear equilibrium structure. The CCSD(T) computations were extended in 2009 to the aug-cc-pCVXZ ($X = 2-5$) family of basis sets, which predicted a linear HCNO structure at the complete basis set (CBS) limit.³² Thus far, only one *ab initio* study from Cambridge in 1993 has performed full 6-dimensional variational computations for HCNO



rovibrational states.⁷⁸ Practical limitations dictated a rather low level of theory (MP2/DZP) for generating 561 energy points, which were fit to various model potentials constructed from expansions in simple internal coordinates comprising up to 55 terms.⁷⁸ Considerable difficulty was encountered in obtaining good analytical fits, and the ν_5 results proved to be unstable with respect to the choice of model potential.⁷⁸ While a full 6-dimensional treatment of the HCNO problem was a cutting-edge accomplishment in 1993, the underlying MP2/DZP surface exhibits a bent HCNO minimum with $\angle\text{H-C-N} = 148.1^\circ$ and a barrier to linearity of 332 cm^{-1} , features now known to be unrealistic.

To date, the quasibent/quasilinear nature of fulminic acid has not been probed by any high-order coupled cluster method beyond CCSD(T), and the impact of relativistic effects (MVD1) and diagonal Born-Oppenheimer corrections (DBOC) has not been assessed. Moreover, structures at the CBS limit are sparse, and corresponding harmonic vibrational frequencies are nonexistent in the current literature. We have discovered that previous work failed to converge to the *ab initio* limit and that even more rigorous quantum chemical methods are essential in finally solving the HCNO problem. Therefore, in the present study, high-level electron-correlation methods as extensive as CCSDT(Q), CCSDTQ(P), and even CCSDTQP(H) are employed in conjunction with complete basis set (CBS) extrapolations using the cc-pCVXZ ($X = 4-6$) basis sets to accurately pinpoint the equilibrium structure, harmonic vibrational frequencies, and relative energies of HCNO via focal point analyses (FPA). Scalar relativistic effects (MVD1) and diagonal Born-Oppenheimer corrections (DBOC) are also studied. The well-established linear HCN molecule was used as a benchmark to demonstrate the extreme accuracy of our computational techniques used on HCNO.

2. THEORETICAL METHODS

A systematic progression of electronic wavefunction methods was employed to target the *ab initio* limit of molecular geometries and harmonic vibrational frequencies for HCN and HCNO, as well as the $\text{HCN} + \text{O}(^3P) \rightarrow \text{HCNO}$ reaction energy. The progression of methods incorporated Hartree-Fock theory;^{86,87} second-order Møller-Plesset (MP2)⁸⁸ perturbation theory; and coupled cluster (CC)^{89,90} theory, including full single and double excitations (CCSD),⁹¹ perturbative treatment of connected triple excitations [CCSD(T)],⁹² full triple excitations (CCSDT),⁹³ perturbative treatment of quadruple excitations [CCSDT(Q)],⁹⁴ full quadruple excitations



(CCSDTQ),⁹⁵ perturbative treatment of pentuple excitations [CCSDTQ(P)],^{96,97} full pentuple excitations (CCSDTQP), and perturbative treatment of hextuple excitations [CCSDTQP(H)].⁹⁶⁻⁹⁸

The wavefunction computations were executed using the family of correlation-consistent polarized-valence orbital basis sets cc-pVXZ ($X = D, T, Q, 5, 6$) and the related core-valence basis sets cc-pCVXZ ($X = D, T, Q, 5, 6$) developed by Dunning and coworkers.⁹⁹⁻¹⁰¹ To make the CCSDTQ(P) and CCSDTQP(H) jobs tractable, the 6-31G* Pople basis set¹⁰² was used instead of cc-pVDZ; the legitimacy of this replacement was carefully established. The electronic energies for CCSD(T) and lower levels were computed with the CFOUR 2.0^{103,104} package, while those of CCSDT and higher levels through CCSDTQP(H) were obtained with the MRCC^{105,106} program, either as a standalone package or interfaced with CFOUR.

The primary CBS extrapolations of the cc-pCV(Q,5,6)Z Hartree-Fock total energies (E_{HF}) and the cc-pCV(5,6)Z all-electron MP2, CCSD, and CCSD(T) correlation energies (E_{corr}) were performed according to the following equations:^{107,108}

$$E_{\text{HF}}(X) = E_{\text{HF,CBS}} + be^{-cX} \quad (1)$$

$$E_{\text{corr}}(X) = E_{\text{corr,CBS}} + bX^{-3} \quad (2)$$

where X is the cardinal number of the correlation-consistent basis set series. Additional extrapolation formulas from the literature were also tested:¹⁰⁹⁻¹¹¹

$$E_{\text{HF}}(X) = E_{\text{HF,CBS}} + be^{-(X-1)} + ce^{-(X-1)^2} \quad (3)$$

$$E_{\text{HF}}(X) = E_{\text{HF,CBS}} + b(X+1)e^{-9\sqrt{X}} \quad (4)$$

$$E_{\text{corr}}(X) = E_{\text{corr,CBS}} + b\left(X + \frac{1}{2}\right)^{-4} \quad (5)$$

Moreover, the Schwenke¹¹² and SchwenkeAug¹¹² extrapolation schemes were investigated for both Hartree-Fock and correlation energies. Two final correlation energy extrapolations are introduced in this work that entail three-parameter fits to $X = 4, 5, 6$ data:

$$E_{\text{corr}}(X) = E_{\text{corr,CBS}} + bX^{-c} \quad (6)$$

$$E_{\text{corr}}(X) = E_{\text{corr,CBS}} + b(X-c)^{-3} \quad (7)$$



A composite focal point analysis (FPA) scheme^{113,114} was utilized to obtain CCSDT, CCSDT(Q), CCSDTQ, CCSDTQ(P), CCSDTQP, and CCSDTQP(H) energies targeting the CBS limit. The following correlation increments (δ) were employed:

$$\delta[\text{CCSDT}] = E_{\text{corr}}(\text{CCSDT/cc-pVTZ}) - E_{\text{corr}}(\text{CCSD(T)/cc-pVTZ}) \quad (8)$$

$$\delta[\text{CCSDT(Q)}] = E_{\text{corr}}(\text{CCSDT(Q)/cc-pVTZ}) - E_{\text{corr}}(\text{CCSDT/cc-pVTZ}) \quad (9)$$

$$\delta[\text{CCSDTQ}] = E_{\text{corr}}(\text{CCSDTQ/6-31G}^*) - E_{\text{corr}}(\text{CCSDT(Q)/6-31G}^*) \quad (10)$$

$$\delta[\text{CCSDTQ(P)}] = E_{\text{corr}}(\text{CCSDTQ(P)/6-31G}^*) - E_{\text{corr}}(\text{CCSDTQ/6-31G}^*) \quad (11)$$

$$\delta[\text{CCSDTQP(H)}] = E_{\text{corr}}(\text{CCSDTQP(H)/6-31G}^*) - E_{\text{corr}}(\text{CCSDTQ(P)/6-31G}^*) \quad (12)$$

One-electron mass-velocity and Darwin terms (MVD1)¹¹⁵⁻¹¹⁷ were evaluated perturbatively to obtain scalar relativistic corrections at the AE-CCSD(T)/cc-pCV5Z level of theory. Diagonal Born-Oppenheimer (DBOC) corrections¹¹⁸ were computed at the AE-CCSD/cc-pCVQZ level and compared to corresponding HF/cc-pCVQZ values. These auxiliary corrections (Δ) were added to yield final FPA energies as follows:

$$E_{\text{FPA}} = E_{\text{HF, CBS}} + E_{\text{corr, CBS}}[\text{CCSD(T)}] + \delta[\text{CCSDT}] + \delta[\text{CCSDT(Q)}] + \delta[\text{CCSDTQ}] \\ + \delta[\text{CCSDTQ(P)}] + \Delta(\text{MVD1}) + \Delta(\text{DBOC}) \quad (13)$$

The small but extremely costly $\delta[\text{CCSDTQP(H)}]$ increment was added only when the HCN + O(³P) → HCNO reaction energy was computed.

A custom *Mathematica*¹¹⁹ program was written for this research to evaluate composite FPA energies, optimize geometries, and calculate harmonic vibrational frequencies in internal coordinates, all by specifying lists of energy points to be computed with the electronic structure codes and then processing the data upon completion of the sundry jobs. Energy gradients and diagonal quadratic force constants were obtained numerically from customary 3-point single-displacement formulas, whereas off-diagonal quadratic force constants were determined from two additional double displacements [(+,+) and (-,-)]; the displacement sizes were 0.005 Å for bond distances and 0.02 rad for angles. A key to getting results at such high levels of theory was the implementation of highly efficient optimization algorithms. Steps in the optimization of linear structures were found by defining an analytic potential function within *Mathematica* for the force field expansion complete through fourth order and then minimizing this function via built-in



modules; for this purpose, the gradients and quadratic force constants evaluated at the given level of theory were augmented with AE-CCSD(T)/CBS cubic and quartic force constants¹²⁰ listed in the Supplementary Information (SI). Steps in the optimization of bent geometries were taken via the full Newton-Raphson method elaborated with controlled damping or dilation of the step vector. Finally, the *Mathematica* program was used for error analyses in which random fuzz of a chosen order of magnitude was added to the input energies followed by recalculation of the final results for geometric parameters and harmonic frequencies. Such simulations were executed 1000 times to ascertain standard deviations in the final results as a function of the imparted uncertainty in the energies. In our computations, the largest final step in the CC iterations was (2.9×10^{-10} , 9.8×10^{-11}) E_h for energies around (linear, bent) stationary points, while the underlying HF energies were more tightly converged. The key conclusion from our simulations is that such energy convergence yields accuracy better than (10^{-5} Å, 0.01° , 0.1 cm^{-1}) in the predicted (distance, angles, frequencies). The lone exception is the pair of C–N–O bending frequencies of bent HCNO at the AE-CCSDT(Q)/CBS level, whose accuracy is better than 1 cm^{-1} , despite the numerical difficulties associated with a very nearly linear heavy-atom framework.

3. RESULTS AND DISCUSSION

3.1. Electronic Structure of HCNO. To assess the possibility of multireference character in HCNO, the CCSD(T)/cc-pVTZ values shown in Table 1 for the traditional T_1 , $T_{2,\text{max}}$, D_1 , and D_2 diagnostics¹²¹⁻¹²³ were computed using Psi4¹²⁴ for linear HCNO and HCN at their respective AE-CCSDTQ(P)/CBS + MVD1 geometries and for bent HCNO at its AE-CCSDT(Q)/CBS structure. A T_1 diagnostic greater than 0.02 was proposed decades ago by Lee and Taylor¹²¹ as a criterion for closed-shell species exhibiting substantial multireference character. The linear and bent HCNO T_1 diagnostics are near 0.018, somewhat larger than the HCN value (0.012) but still comfortably below the stated multireference threshold. Moreover, the absolute maximum T_2 amplitudes ($T_{2,\text{max}}$) of both HCNO species are not large (0.075) and are actually less than their HCN counterpart (0.087). Original testing of the D_1 and D_2 diagnostics^{122,123} indicated that molecules with $D_1(\text{CCSD}) \leq 0.02$ and $D_2(\text{CCSD}) \leq 0.15$ display excellent agreement between CCSD and CCSD(T) bond distances and harmonic vibrational frequencies, whereas inadequacies of the CCSD method occur for molecules with $D_1(\text{CCSD}) > 0.050$ and $D_2(\text{CCSD}) > 0.18$. By these D_1 standards, HCN is intermediate in character, while both linear and bent HCNO



are problematic for CCSD. In contrast, the D_2 diagnostic indicates that all three species are borderline for the performance of CCSD. Nevertheless, the D_1 and D_2 criteria for CCSD are not precisely relevant to our current research on HCNO, for which the real question is whether high-order single-reference coupled-cluster treatments at or beyond CCSD(T) can yield accurate results, especially within the context of the FPA approach.

The development of new diagnostics for multireference electronic character and criticism of traditional metrics is an ongoing topic of research.¹²⁵⁻¹²⁹ Fortunately, in the current study we can obtain definitive electronic structure information using MOLPRO¹³⁰⁻¹³³ to perform full-valence CASSCF/cc-pVXZ ($X = D, T$) computations for HCNO and HCN with (16, 13) and (10, 9) active spaces, respectively. The resulting CI coefficients based on CASSCF natural orbitals were virtually independent of whether the cc-pVDZ or cc-pVTZ basis set was utilized or whether the geometries were optimized at the CASSCF level or set to our highest-quality structures. A representative sample of results is given in Table 1. For all three species, the HF reference has $C_0 > 0.94$, and the next most important contributions arise from a pair of $\pi^2 \rightarrow (\pi^*)^2$ excited determinants with CI coefficients near -0.12 . No other configuration has a coefficient greater than 0.08 in magnitude. Such CI coefficients are typical of molecules widely considered to be single-reference species. In brief, HCNO is indeed strongly dominated by a single configuration, and the nature of its electronic structure is very similar to that of HCN. Finally, the similarity of the coupled-cluster diagnostics and CASSCF CI coefficients indicates that a change to multireference behavior is not a factor in the large-amplitude H–C–N bending motion of fulminic acid.

Table 1. Comparative T_1 , $T_{2,\max}$, D_1 , and D_2 diagnostics [CCSD(T)/cc-pVTZ] and largest CASSCF CI coefficients (C_0 – C_3) for linear and bent HCNO and the HCN benchmark

	T_1	$T_{2,\max}$	D_1	D_2	C_0	C_1	C_2	C_3
HCN ^a	0.012	0.0867	0.029	0.178	0.958	−0.121	−0.121	0.078
Linear HCNO ^a	0.018	0.0745	0.053	0.179	0.943	−0.113	−0.113	0.080
Bent HCNO ^b	0.018	0.0746	0.053	0.179	0.942	−0.114	−0.113	0.080

^aAt the AE-CCSDTQ(P)/CBS + MVD1 optimized geometries.

^bAt the AE-CCSDT(Q)/CBS optimum geometry.

3.2. HCN Benchmark. To verify the extreme accuracy of the wavefunction methods applied here to HCNO, the computations summarized in Table 2 were first performed on HCN, which has been exhaustively studied by high-resolution spectroscopy. Systematic and strong convergence with respect to basis set is achieved to the level of 0.0001 Å and 0.1 cm^{−1} for bond



distances and harmonic frequencies. Similar convergence with respect to electron correlation treatment is also accomplished for these quantities to within 0.00006 Å and 1.0 cm⁻¹, as shown by the difference between AE-CCSDT(Q)/CBS and AE-CCSDTQ(P)/CBS results. Scalar relativistic effects shorten the bond distances slightly (≤ 0.0002 Å) and alter the frequencies by less than 0.5 cm⁻¹. Our best theoretical HCN results are near-identical matches to the best existing spectroscopic parameters. The empirical equilibrium bond distances (r_e) were extracted from ground-state rotational constants for eight different isotopologues, namely every combination of H, D, ¹²C, ¹³C, ¹⁴N, and ¹⁵N; the requisite B_0-B_e corrections were obtained from rigorous variational computations of the vibration-rotation energy levels and wavefunctions.¹³⁴ The empirical harmonic frequencies were derived from a least-squares fit of 50 vibrational band origins of HCN up to 10631 cm⁻¹ in energy; the best fit employing ω_1 , ω_2 , ω_3 , g_{22} , and 20 anharmonicity constants (x_{ij} , y_{ijk} , y_{ill} , and z_{3333}) was selected for comparison to our present *ab initio* HCN results.¹³⁵ The highest-level computations [AE-CCSDTQ(P)/CBS + MVD1] match the empirical r_e and ω_i values to 0.00017 Å and 1.6 cm⁻¹, respectively. Such astounding agreement is very gratifying and bodes well for a definitive solution of the HCNO problem.

Table 2. HCN bond distances (r_e , Å) and harmonic vibrational frequencies (ω_i , cm⁻¹)

Level of Theory	$r_e(\text{H-C})$	$r_e(\text{C-N})$	$\omega_1(\sigma)$	$\omega_2(\pi)$	$\omega_3(\sigma)$
HF/cc-pCVQZ	1.05698	1.12326	3607.8	877.1	2408.4
HF/cc-pCV5Z	1.05690	1.12319	3608.5	876.7	2407.9
HF/cc-pCV6Z	1.05689	1.12319	3608.6	876.5	2407.8
HF/CBS	1.05688	1.12319	3608.6	876.5	2407.8
AE-MP2/cc-pCV5Z	1.06264	1.15969	3475.2	727.5	2051.0
AE-MP2/cc-pCV6Z	1.06260	1.15942	3475.3	729.8	2051.9
AE-MP2/CBS	1.06255	1.15907	3475.4	733.3	2053.1
AE-CCSD/cc-pCV5Z	1.06311	1.14549	3474.9	756.6	2201.2
AE-CCSD/cc-pCV6Z	1.06303	1.14519	3475.5	758.4	2202.5
AE-CCSD/CBS	1.06292	1.14478	3476.2	761.1	2204.2
AE-CCSD(T)/cc-pCV5Z	1.06524	1.15300	3444.6	728.5	2134.8
AE-CCSD(T)/cc-pCV6Z	1.06516	1.15271	3445.0	730.3	2135.9
AE-CCSD(T)/CBS	1.06508	1.15232	3445.6	733.1	2137.4
AE-CCSDT/CBS	1.06495	1.15175	3447.0	734.8	2144.3
AE-CCSDT(Q)/CBS	1.06509	1.15333	3443.5	728.7	2126.7
AE-CCSDTQ/CBS	1.06504	1.15303	3444.5	729.3	2130.8
AE-CCSDTQ(P)/CBS	1.06505	1.15327	3444.0	728.6	2127.7
AE-CCSDTQ(P)/CBS + MVD1	1.06491	1.15307	3444.1	728.5	2127.3
Empirical ^{134,135}	1.06501(8)	1.15324(2)	3442.5(1)	726.9(2)	2127.2(4)



3.3. HCNO Structures and Vibrational Frequencies. Linear HCNO bond distances, harmonic vibrational frequencies, and bending quadratic force constants are reported in Table 3 for all levels of theory employed in this study. The HF bond distances are essentially converged to the CBS limit once the cc-pCV5Z basis set is employed. The HF/CBS distances are too short compared to those of AE-CCSDTQ(P)/CBS, the disparities being 0.007, 0.037, and 0.012 Å for $r_e(\text{H-C})$, $r_e(\text{C-N})$, and $r_e(\text{N-O})$, respectively. The $r_e(\text{C-N})$ error is larger than usual but mirrors that seen in Table 2 for HCN. For the MP2, CCSD, and CCSD(T) methods, the cc-pCV6Z distances differ from the corresponding CBS limits by only 0.0004 Å or less. In the [AE-MP2, AE-CCSD, AE-CCSD(T)] correlation series, $r_e(\text{H-C})$ and $r_e(\text{N-O})$ increase monotonically in modest steps, while $r_e(\text{C-N})$ exhibits highly oscillatory increments of (+0.048, -0.023, +0.011) Å at the CBS limit. At the AE-CCSD(T)/CBS level, [$r_e(\text{H-C})$, $r_e(\text{N-O})$] are within (0.0001, 0.0003) Å of the corresponding AE-CCSDTQ(P)/CBS limits. In contrast, $r_e(\text{C-N})$ continues to oscillate with variations of (-0.0010, +0.0024, -0.0004, +0.0001) Å as the [CCSDT, CCSDT(Q), CCSDTQ, CCSDTQ(P)] levels of theory are reached, similar to the HCN benchmark except with larger step sizes. Overall, the convergence of the linear HCNO bond distances with respect to both orbital basis set and electron correlation treatment is almost as good as that witnessed for the HCN benchmark, so that similar high accuracy is expected in the predictions. Nonetheless, it is apparent from Table 3 that post-CCSD(T) methods are essential to achieving this accuracy.

All of the vibrational modes of linear HCNO exhibit (cc-pCV5Z, cc-pCV6Z, CBS) sets of HF harmonic frequencies in internal agreement to better than 1 cm^{-1} . In accord with expectation, the HF/CBS stretching frequencies (ω_1 , ω_2 , ω_3) are too large compared to those of AE-CCSDTQ(P)/CBS by (4.1, 9.7, 3.3)%; however, the HF/CBS overestimation of ω_4 (17.9%) is substantially greater than normal for this level of theory. For the AE-MP2, AE-CCSD, and AE-CCSD(T) methods, the cc-pCV6Z ω_1 - ω_4 values are within 1 cm^{-1} of the corresponding CBS limits, revealing tight basis set convergence. For AE-MP2/CBS the (ω_1 , ω_2 , ω_3 , ω_4) errors vis-à-vis AE-CCSDTQ(P)/CBS are (0.9, -0.6, 4.4, 1.8)%; because $\omega_3(\text{AE-MP2/CBS})$ is peculiarly greater than $\omega_3(\text{HF/CBS})$ by 14 cm^{-1} , its accuracy is diminished. For AE-CCSD/CBS the (ω_1 , ω_2 , ω_3 , ω_4) errors relative to the benchmark are (0.8, 3.1, 1.8, 5.1)%, so that ω_2 and ω_4 are actually less accurate than their AE-MP2/CBS counterparts. The rather erratic behavior of (ω_1 , ω_2 , ω_3 , ω_4) in the electron correlation series settles down at the AE-CCSD(T)/CBS level, which yields values that are slightly too large by (0.0, 0.5, 0.3, 0.9)%. Beyond this level, subtle variations accumulate



to net downward shifts. The (P) effect on $(\omega_1, \omega_2, \omega_3, \omega_4)$ is only $(0, -3, +3, 0)$ cm^{-1} , which indicates strong convergence with respect to electron correlation.

Table 3. Linear HCNO bond distances (r_e , Å), harmonic vibrational frequencies (ω_i , cm^{-1}), and bending quadratic force constants (F_{44} , F_{45} , F_{55} , aJ rad^{-2})

Level of Theory	$r_e(\text{H-C})$	$r_e(\text{C-N})$	$r_e(\text{N-O})$	$\omega_1(\sigma)$	$\omega_2(\sigma)$	$\omega_3(\sigma)$	$\omega_4(\pi)$	$\omega_5(\pi)$	F_{44}	F_{45}	F_{55}
HF/cc-pCVQZ	1.0526	1.1226	1.1894	3640	2499	1313	647	603	0.204	0.153	0.875
HF/cc-pCV5Z	1.0526	1.1223	1.1898	3639	2497	1310	646	604	0.205	0.152	0.871
HF/cc-pCV6Z	1.0526	1.1223	1.1899	3639	2497	1310	646	604	0.206	0.152	0.870
HF/CBS	1.0526	1.1223	1.1899	3639	2497	1310	646	604	0.206	0.152	0.869
AE-MP2/cc-pCV5Z	1.0564	1.1706	1.1910	3529	2264	1325	560	283i	-0.000 ₃	0.164	0.690
AE-MP2/cc-pCV6Z	1.0564	1.1703	1.1911	3528	2263	1324	559	273i	0.002	0.163	0.687
AE-MP2/CBS	1.0564	1.1700	1.1911	3527	2263	1324	558	260i	0.005	0.162	0.685
AE-CCSD/cc-pCV5Z	1.0575	1.1481	1.1978	3525	2346	1291	576	318	0.081	0.153	0.729
AE-CCSD/cc-pCV6Z	1.0574	1.1478	1.1977	3525	2346	1291	576	325	0.083	0.152	0.728
AE-CCSD/CBS	1.0574	1.1474	1.1976	3525	2347	1291	576	334	0.086	0.152	0.727
FC-CCSD(T)/cc-pCV5Z	1.0605	1.1609	1.2041	3492	2278	1266	551	82i	0.033	0.157	0.673
AE-CCSD(T)/cc-pCV5Z	1.0593	1.1587	1.2019	3498	2287	1272	554	54	0.037	0.154	0.680
FC-CCSD(T)/cc-pCV6Z	1.0605	1.1607	1.2042	3492	2278	1266	551	54i	0.035	0.157	0.673
AE-CCSD(T)/cc-pCV6Z	1.0593	1.1584	1.2019	3497	2286	1272	554	89	0.039	0.154	0.677
FC-CCSD(T)/CBS	1.0606	1.1604	1.2042	3491	2278	1266	550	65	0.038	0.156	0.670
AE-CCSD(T)/CBS	1.0592	1.1580	1.2019	3497	2287	1272	553	120	0.042	0.153	0.676
AE-CCSDT/CBS	1.0591	1.1570	1.2021	3499	2292	1270	553	146	0.045	0.152	0.676
AE-CCSDT(Q)/CBS	1.0592	1.1594	1.2034	3496	2275	1261	546	49i	0.034	0.152	0.660
AE-CCSDTQ/CBS	1.0592	1.1590	1.2029	3497	2279	1265	548	52	0.036	0.152	0.664
AE-CCSDTQ(P)/CBS	1.0591	1.1591	1.2022	3497	2276	1268	548	45	0.036	0.153	0.665
AE-CCSDTQ(P)/CBS + MVD1	1.0590	1.1588	1.2024	3497	2275	1266	548	19	0.035	0.153	0.664
AE-CCSDTQ(P)/CBS + MVD1 + DBOC/HF	1.0591	1.1588	1.2024	3497	2275	1267	548	41	0.036	0.153	0.664
AE-CCSDTQ(P)/CBS + MVD1 + DBOC/CCSD	1.0591	1.1588	1.2024	3497	2275	1267	548	32	0.036	0.153	0.664

The critical feature of Table 3 is the remarkable variation of the doubly-degenerate H-C-N bending frequency, $\omega_5(\pi)$, as depicted for the primary AE coupled cluster series at the CBS limit in Figure 1. The CBS extrapolations prove to be important in evaluating ω_5 with correlated methods, as seen most dramatically by comparing the AE-CCSD(T)/cc-pCV6Z value (89 cm^{-1}) with its CBS counterpart (120 cm^{-1}). At the HF/CBS level, HCNO is a linear molecule with a sizable $\omega_5 = 604 \text{ cm}^{-1}$. However, all AE-MP2 computations give an imaginary frequency at the linear optimized structure; in particular, $\omega_5 = 260i \text{ cm}^{-1}$ at the CBS limit. A rebound effect is provided by AE-CCSD, which gives $\omega_5 = (318, 325, 334) \text{ cm}^{-1}$ in the cc-pCV(5,6, ∞)Z



computations. Intriguingly, CCSD(T) with basis sets smaller than cc-pCV5Z can yield *imaginary* ω_5 values,^{76,77} but as the AE-CCSD(T)/CBS limit is approached, ω_5 steadily increases to 120 cm^{-1} . The post-CCSD(T) predictions for ω_5 continue to waver in a virtually unprecedented manner. Most notably, $\omega_5 = 49i \text{ cm}^{-1}$ results from CCSDT(Q) theory, so that HCNO constitutes a remarkable case in which the perturbative (Q) correlation correction actually changes the qualitative nature of the equilibrium structure. The bending quadratic force constants in Table 3 reveal a surprising aspect about the CCSDT(Q)/CBS imaginary ω_5 frequency, *viz.*, the diagonal constants F_{44} and F_{55} are both positive, showing that F_{45} coupling is essential to lowering the vibrational potential energy along the ω_5 mode. In other words, simultaneous *trans*-bending is required to achieve an imaginary frequency.

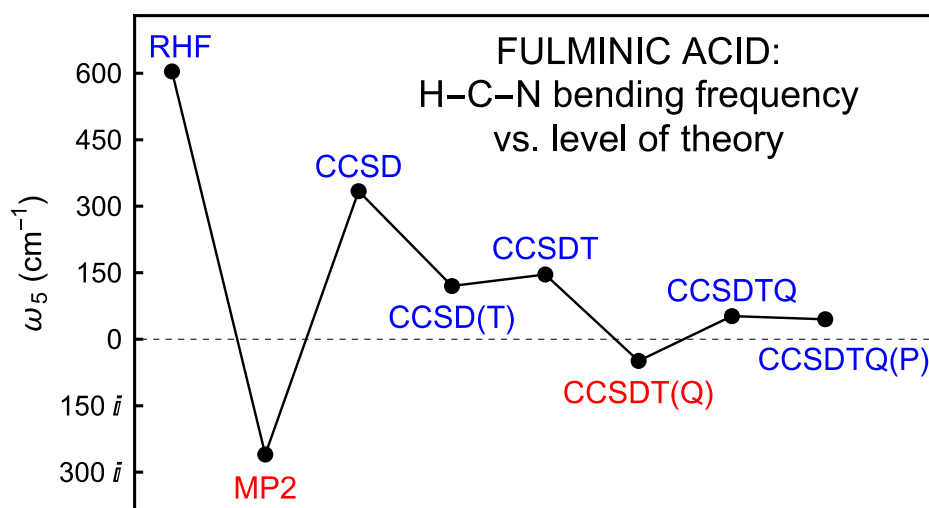


Figure 1. Variation of ω_5 (HCNO) in the all-electron coupled-cluster series at the CBS limit. The quantity actually plotted is $|\omega_5| \cdot \text{sgn}(\omega_5^2)$, but the ticks are labeled with the corresponding ω_5 values.

The amazing saga of ω_5 for fulminic acid is not complete even at the CCSDT(Q) level! A full accounting of connected quadruple excitations leads back to a linear minimum structure with $\omega_5 = 52 \text{ cm}^{-1}$ for CCSDTQ theory. Thereafter, the (P) effect on ω_5 is only -7 cm^{-1} , suggesting that the AE-CCSDTQ(P)/CBS frequency of 45 cm^{-1} is very near complete convergence, pending inclusion of auxiliary MVD1 and DBOC terms. As observed for HCN, the MVD1 relativistic effects shorten the HCNO bond distances by 0.0001-0.0003 Å; the corresponding changes for $(\omega_1, \omega_2, \omega_3, \omega_4)$ are merely (0, -1, -2, 0) cm^{-1} . However, MVD1 provides a driving force toward nonlinearity that reduces ω_5 to a minuscule 19 cm^{-1} at the AE-CCSDTQ(P)/CBS + MVD1 level.



Therefore, our ultimate conclusion for the Born-Oppenheimer potential energy surface is that HCNO exists as a linear minimum structure with an H–C–N bending frequency barely above zero. Because ω_5 is so small, room is thus left for first-order, mass-dependent, non-Born-Oppenheimer terms to influence the equilibrium structure. As shown in Table 3, such terms have a negligible effect on the bond distances and ω_1 – ω_4 , yet ω_5 is increased to stanch the MVD1 reductions. To ensure reliability, DBOC computations were run with the cc-pCVQZ basis set and both the HF and AE-CCSD methods, the latter providing $\omega_5 = 32 \text{ cm}^{-1}$. One can genuinely say that both the MVD1 and DBOC effects, which are normally just auxiliary corrections, play a decisive role in determining the final equilibrium structure of HCNO, and if the DBOC were to augment rather than compensate for the MVD1 shift on ω_5 , then vibrationless fulminic acid would be bent rather than linear.

While core electron correlation was fully incorporated and embedded in our FPA analyses of linear HCNO, insight is gained by singling out this effect, which is commonly treated as an auxiliary correction. For this purpose, frozen-core (FC) CCSD(T)/cc-pCV(5,6, ∞)Z computations were performed for the r_e and ω_i parameters of linear HCNO (Table 3). The differences between FC and AE results are quite insensitive to basis set and reveal that $1s$ correlation changes [$r_e(\text{H–C})$, $r_e(\text{C–N})$, $r_e(\text{N–O})$] by about (–0.001, –0.002, –0.002) Å, in accord with earlier findings on diatomic molecules.¹³⁶ The concomitant overall shifts in the (ω_1 , ω_2 , ω_3) stretching frequencies are (+6, +9, +6) cm^{-1} , as expected from Badger’s Rule.¹³⁷ For diatomic molecules such overall shifts can be deceptive, because the direct effect of core correlation is actually curvature reduction of $V(r)$, which is compensated by the indirect effect of r_e contraction. We find that linear HCNO exhibits the same phenomenon. In particular, evaluating the FC-CCSD(T)/cc-pCV6Z force constants at the AE-CCSD(T)/cc-pCV6Z equilibrium geometry yields (ω_1 , ω_2 , ω_3) = (3504, 2296, 1277) cm^{-1} , exposing the direct $1s$ correlation effect as (–7, –9, –5) cm^{-1} . In turn, the indirect effect of bond-length contraction on the stretching frequencies is (+13, +18, +11) cm^{-1} . The sum of these competing effects produces the aforementioned overall phenomenological shifts arising from $1s$ correlation. In the (cc-pCV5Z, cc-pCV6Z, CBS) cases, the FC \rightarrow AE CCSD(T) shifts are very striking for ω_5 : ($82i \rightarrow 54$, $54i \rightarrow 89$, $65 \rightarrow 120$) cm^{-1} . Clearly, core correlation is a pivotal factor favoring the linear structure.

Trans-bent HCNO minima are obtained at the AE-MP2/cc-pCV(5,6, ∞)Z and AE-CCSDT(Q)/CBS levels of theory by following the imaginary-frequency ω_5 mode of the respective linear structures (Table 3). The optimized geometries, barriers to linearity (E_B), and



harmonic frequencies of these bent HCNO minima are provided in Table 4. The AE-MP2 results for r_e , θ_{CNO} , ω_1 - ω_4 , and ω_6 of bent HCNO display basis-set convergence that is only slightly less rapid than found for linear HCNO. Such is not the case for the $(\theta_{\text{HCN}}, E_B, \omega_5)$ values of AE-MP2, for which the CBS limit is removed from cc-pCV6Z by $(+0.6^\circ, -11.3 \text{ cm}^{-1}, -15 \text{ cm}^{-1})$. Upon bending, AE-MP2/CBS yields $[r_e(\text{H-C}), r_e(\text{C-N})]$ elongations of $(0.002, 0.008) \text{ \AA}$ and associated (ω_1, ω_2) reductions of $(36, 11) \text{ cm}^{-1}$; simultaneously, $r_e(\text{N-O})$ contracts by approximately 0.002 \AA while ω_3 is unchanged. The AE-MP2/CBS θ_{HCN} and θ_{CNO} angles deviate from linearity by 23.5° and 5.5° , respectively, but these distortions only engender $E_B = 73 \text{ cm}^{-1}$. A similar comparison between bent and linear AE-CCSDT(Q)/CBS structures shows strikingly smaller differences. The $r_e(\text{H-C})$ and $r_e(\text{C-N})$ bond distances elongate by merely 0.0002 \AA and 0.0006 \AA , respectively, whereas $r_e(\text{N-O})$ contracts by 0.0002 \AA ; frequency differences upon bending are no more than 2 cm^{-1} . The CCSDT(Q) $(\theta_{\text{HCN}}, \theta_{\text{CNO}})$ angles are bent from linearity by merely $(6.1^\circ, 1.4^\circ)$, and the resulting $E_B = 0.1 \text{ cm}^{-1}$ is shockingly small.

Table 4. *Trans*-bent HCNO optimized bond distances (r_e , \AA) and bond angles (θ), barriers to linearity (E_B , cm^{-1}), and harmonic vibrational frequencies (ω_i , cm^{-1})

Level of Theory	$r_e(\text{H-C})$	$r_e(\text{C-N})$	$r_e(\text{N-O})$	θ_{HCN}	θ_{CNO}	E_B	$\omega_1(a')$	$\omega_2(a')$	$\omega_3(a')$	$\omega_4(a')$	$\omega_5(a')$	$\omega_6(a'')$
AE-MP2/cc-pCV5Z	1.0591	1.1783	1.1885	155.4°	174.2°	92.4	3491	2253	1325	555	404	569
AE-MP2/cc-pCV6Z	1.0591	1.1778	1.1887	155.9°	174.3°	83.9	3491	2253	1324	554	393	568
AE-MP2/CBS	1.0590	1.1771	1.1888	156.5°	174.5°	72.6	3491	2252	1324	554	378	567
AE-CCSDT(Q)/CBS	1.0594	1.1600	1.2032	173.9°	178.6°	0.1	3494	2273	1261	546	70	545

The energy profile for the H-C-N bending is so flat that zero-point vibrational energy (ZPVE) of the complementary modes comes into play. In the AE-MP2/CBS case, this ZPVE shift increases the effective barrier to linearity from 73 to 94 cm^{-1} , assuming the geometries are fixed at the r_e structure. Because the AE-CCSDT(Q)/CBS bending distortions are much smaller, the corresponding ZPVE shift is only $+2.5 \text{ cm}^{-1}$. However, this phenomenon overwhelms the tiny 0.1 cm^{-1} vibrationless barrier and enhances the barrier to linearity. A central question to be answered in future studies on fulminic acid is whether an accounting of complementary-mode ZPVE at a very high level of theory sufficiently amends the positive curvature of the AE-CCSDTQ(P)/CBS + MVD1 H-C-N bending curve to produce a nonlinear minimum for the *effective* vibrational potential.



Our best level of theory [AE-CCSDTQ(P)/CBS + MVD1] within the Born-Oppenheimer regime predicts that fulminic acid has a linear equilibrium structure with $[r_e(\text{H-C}), r_e(\text{C-N}), r_e(\text{N-O})] = (1.0590, 1.1588, 1.2024) \text{ \AA}$ and $(\omega_1, \omega_2, \omega_3, \omega_4) = (3497, 2275, 1266, 548) \text{ cm}^{-1}$. Previously, the best theoretical r_e structures for HCNO came from the AE-CCSD(T) work of Mladenovic and coworkers.^{32,77} Their cc-pCV5Z results exactly match ours, while their CBS extrapolation produced $[r_e(\text{H-C}), r_e(\text{C-N}), r_e(\text{N-O})]$ distances differing from our corresponding values by $(+0.0001, +0.0004, +0.0002) \text{ \AA}$. Variations in the CBS extrapolation methods are responsible for these differences. In ref 32, AE-CCSD(T)/aug-cc-pCV(3,4,5)Z total energies were fit to the three-parameter exponential form of eq 1. In contrast, our methodology applied eq 1 only to HF/cc-pCV(4,5,6)Z energies and appended the correlation energy derived from extrapolation of AE-CCSD(T)/cc-pCV(5,6)Z points via eq 2.

Our AE-CCSDTQ(P)/CBS + MVD1 prediction of $\omega_5 = 19 \text{ cm}^{-1}$ for linear HCNO warrants assessment with respect to the experimental literature. Using high-resolution rovibrational spectroscopy, Winnewisser and coworkers^{33-38,42-46} assigned thousands of absorptions for the ground vibrational states of HCNO and DCNO, as well as the ν_1 and ν_2 fundamental levels of HCNO. The $\nu_3(\text{HCNO})$ band origin indisputably lies at 224.1 cm^{-1} ,^{38,47} but this frequency is pushed up considerably by the quartic anharmonicity of large-amplitude H-C-N bending. The analysis of experimental data by Bunker et al.⁴¹ adopted a sudden/adiabatic model in which the low-frequency H-C-N bending was separated from the complementary vibrational modes. For each vibrational state of the complementary modes, a semirigid bender Hamiltonian was used to fit the observed rotational levels for $J \leq 5$ to a two-parameter effective potential function for H-C-N bending comprised of a quadratic and quartic term. For the ground vibrational states of HCNO and DCNO, the resulting curves displayed minima with deviations from linearity of 15.83° and 12.90° and corresponding barriers to linearity of 11.5 and 5.4 cm^{-1} , respectively. Vibrational excitation of the ν_1 and ν_2 stretching modes increased the effective barriers to linearity to 40.6 and 35.3 cm^{-1} , respectively. The analysis found that for the H-C-N bending potential of the complementary-mode ground vibrational state, the zero-point energy lies at 146.9 cm^{-1} , well above the 11.5 cm^{-1} barrier to linearity. Thus, the large-amplitude H-C-N motion occurs over the top of a small bump on the potential curve at linearity.

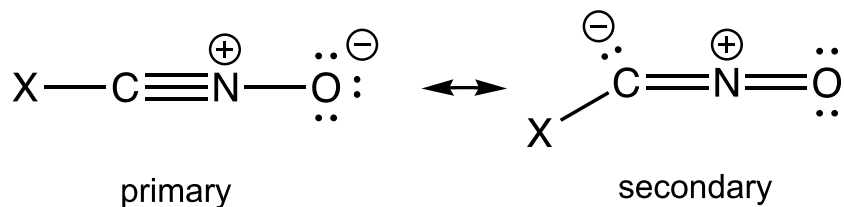
Bunker and coworkers⁴¹ finally employed an extrapolation scheme to work backwards from the vibrationally adiabatic H-C-N bending curves for the various states of the complementary vibrational modes; thus, a vibrationless (Born-Oppenheimer) potential function



for the pure H–C–N bending mode was inferred. This function displayed a remarkably small barrier to linearity of 0.2 cm⁻¹. A key conclusion was then made: “To within the uncertainties inherent in the fitting procedure, and the uncertainty introduced by the choice of model for the shape of the potential, ... the molecule is linear at equilibrium.” Of course, the same uncertainties prevent one from excluding the possibility that the molecule might instead have a very small barrier to linearity on the Born-Oppenheimer surface. Nevertheless, the ultimate conclusion of ref 41 is in full accord with our best theoretical predictions.

Our AE-CCSDTQ(P)/CBS + MVD1 results show that the H–C bond of fulminic acid has one of the shortest lengths (1.0590 Å) and highest harmonic frequencies (3497 cm⁻¹) known for organic compounds.^{5,138} For comparison, experimental values for the [*r*_e(H–C), ω₁] pair are (1.0606 Å, 3495 cm⁻¹) for acetylene,¹³⁹ (1.0591 Å, 3501 cm⁻¹) for monofluoroacetylene,^{140,141} and (1.0650 Å, 3443 cm⁻¹) for HCN.^{134,135} We find the C–N bond in fulminic acid to be 0.0058 Å longer than in HCN, but the associated stretching frequency is 148 cm⁻¹ higher due to coupling with the N–O stretch. The N–O bond distance obtained here for HCNO is 0.017 Å longer than that of the isoelectronic N₂O species, and this substantial change is accompanied by a harmonic frequency decrease of 32 cm⁻¹ for the N–O stretching mode.^{142,143}

The characteristics of HCNO can be placed into context by comparison with the properties of other small nitrile oxide compounds XCNO (X = F, Cl, Br, CN, CH₃, CF₃) that have been investigated by gas-phase, high-resolution rovibrational spectroscopy¹⁴⁴⁻¹⁵⁵ and by varying levels of electronic structure theory.¹⁵²⁻¹⁶⁴ Generally, the XCNO equilibrium structures are strongly dependent on both the orbital basis set and the electron correlation method, as observed in the HCNO case. The propensity for X–C–N bending in these compounds can be understood in terms of a competition between two Lewis structures:



Electron-withdrawing substituents tilt the balance toward the secondary structure and favor bending, whereas electron-donating or π-accepting substituents elevate the importance of the primary structure and maintain linearity. Thus, for the halogen fulminates, the X–C–N angle decreases and the barrier to linearity (*E*_B) increases with increasing electronegativity (X = Br, Cl,



F). At CCSD(T)/CBS, fluorofulminate has $\angle(\text{F}-\text{C}-\text{N}) = 135.1^\circ$ and a relatively high $E_B = 1870 \text{ cm}^{-1}$, so that FCNO is not quasilinear, but rather the first example of a truly bent nitrile oxide.^{156,157} Employing CCSD(T) with a mixed cc-pV5Z/cc-pVQZ basis set for X/(C,N,O) demonstrated that ClCNO¹⁵⁸ and BrCNO¹⁶⁰ are more weakly bent with $[\angle(\text{X}-\text{C}-\text{N}), E_B] = (152.2^\circ, 156 \text{ cm}^{-1})$ and $(153.1^\circ, 119 \text{ cm}^{-1})$, respectively. This conclusion is supported by the effective barriers to linearity (167, 131) cm^{-1} derived from spectroscopy¹⁴⁴ for (ClCNO, BrCNO). In contrast, acetonitrile N-oxide (X = CH₃, electron donating) and cyanofulminate (X = NC, π -accepting) have linear structures at the CCSD(T)/cc-pVQZ and CCSD(T)-F12/aug-cc-pVTZ-F12 levels of theory, respectively.^{161,164} Interestingly, a gas-phase mid-infrared and *ab initio* study of CF₃CNO was conducted by Havasi and coworkers¹⁵⁴ to ascertain the effect of the strongly withdrawing CF₃ group on the molecular framework. Their FC-CCSD(T)/cc-pVTZ computations gave a substantially bent structure with $[\angle(\text{C}-\text{C}-\text{N}), E_B] = (148.9^\circ, 174 \text{ cm}^{-1})$, while their experiments suggested but did not prove that the molecule has a near-linear backbone. In summary, the series for bending disposition in XCNO compounds is $\text{F} \gg \text{CF}_3 > \text{Cl} > \text{Br} > \text{H} > \text{CH}_3 > \text{CN}$, and the parent fulminic acid lies almost precisely on the cusp for breaking linearity of the equilibrium structure.

3.4. Assessing CBS Extrapolation Schemes. The sensitivity of the H–C–N bending potential of the fulminic acid to orbital basis set calls for an assessment of CBS extrapolation methods. In Table 5, AE-CCSDTQ(P)/CBS optimized bond distances and harmonic frequencies of linear HCNO are presented for nine different combinations of the E_{HF} and E_{corr} extrapolation schemes specified above in Section 2. While substantial research exists on energetic results from various CBS approaches in quantum chemistry, very little information is known on the sensitivity of r_e and ω_i predictions to the choice of CBS methodology. Our focus here is not on estimating CBS values using modest basis sets, rather we investigate possibilities for making the final step from rigorous cc-pCV(4,5,6)Z computations to the CBS limit. It is gratifying that the $[r_e(\text{H}-\text{C}), r_e(\text{C}-\text{N}), r_e(\text{N}-\text{O})]$ values in Table 5 lie within narrow intervals of width (0.00014, 0.00023, 0.00005) Å while the $(\omega_1, \omega_2, \omega_3, \omega_4)$ frequencies vary by no more than (0.1, 0.6, 1.6, 0.3) cm^{-1} . Not surprisingly, the ω_5 frequencies exhibit larger variations as the extrapolation method is changed. The Schwartz-4 result (22.5 cm^{-1}) of eq 5 is clearly an outlier, and the Schwenke schemes may suffer by a few cm^{-1} because they are not calibrated on the cc-pCVXZ basis set series. The remaining 6 results for ω_5 all reside within the range [44.0, 45.6] cm^{-1} . The essential observation



from Table 5 is that the primary approach employed here [eq 1 (4,5,6), eq 2 (5,6)] is buttressed by numerous reasonable alternatives. This conclusion is further supported by analyzing the c parameters resulting from the fits of $X = (4,5,6)$ data to eqs 6 and 7. Remarkably, the MP2 correlation energies in the vicinity of the AE-CCSDTQ(P)/CBS equilibrium geometry are characterized by an X exponent of 2.9953(5) in eq 6 or an X shift of 0.0056(6) in eq 7. On the other hand, the corresponding (exponent, shift) pair is [3.4760(4), $-0.5162(4)$] for CCSD and [3.5014(4), $-0.5406(4)$] for CCSD(T). Therefore, the coupled-cluster correlation energies for linear HCNO may be slightly better described by either an $X^{-3.5}$ or $(X + \frac{1}{2})^{-3}$ decay, but the assumption of X^{-3} dependence via eq 2 yields virtually indistinguishable results for r_e and ω_i .

Table 5. Linear HCNO FPA bond distances (r_e , Å) and harmonic vibrational frequencies (ω_i , cm^{-1}) at the AE-CCSDTQ(P)/CBS level as a function of the CBS extrapolation method^a

E_{HF}	E_{corr} [CCSD(T)]	$r_e(\text{H-C})$	$r_e(\text{C-N})$	$r_e(\text{N-O})$	$\omega_1(\sigma)$	$\omega_2(\sigma)$	$\omega_3(\sigma)$	$\omega_4(\pi)$	$\omega_5(\pi)$
eq 1 (4,5,6)	eq 2 (5,6)	1.05913	1.15910	1.20229	3496.9	2275.9	1268.1	548.3	45.3
eq 4 (5,6)	eq 2 (5,6)	1.05913	1.15910	1.20229	3496.9	2275.9	1268.1	548.3	45.6
eq 1 (4,5,6)	eq 2 (4,5,6)	1.05907	1.15901	1.20231	3496.9	2275.6	1267.4	548.4	44.4
eq 3 (4,5,6)	eq 2 (5,6)	1.05913	1.15909	1.20231	3496.9	2275.9	1268.0	548.1	45.9
eq 1 (4,5,6)	eq 6 (4,5,6)	1.05921	1.15924	1.20226	3496.9	2276.5	1269.0	548.1	44.0
eq 1 (4,5,6)	eq 7 (4,5,6)	1.05919	1.15920	1.20227	3496.9	2276.3	1268.7	548.2	44.7
eq 1 (4,5,6)	eq 5 (5,6)	1.05913	1.15919	1.20230	3496.9	2275.9	1268.1	548.4	22.5
Schw (5,6)	Schw (5,6)	1.05913	1.15913	1.20229	3496.9	2276.0	1268.1	548.4	37.3
augSchw (5,6)	augSchw (5,6)	1.05913	1.15913	1.20229	3496.9	2275.9	1268.1	548.4	39.4

^aThe applied CBS extrapolation equations from the text are listed in the first two columns along with the X values of the fitted points for the Hartree-Fock (E_{HF}) and CCSD(T) correlation energy (E_{corr}). The Schwenke extrapolation schemes¹¹² (Schw, augSchw) do not have explicit extrapolation formulas

3.5. Reaction energy for HCNO formation. The electronic wavefunction methods employed here for the quasilinear/quasibent problem of fulminic acid were put to a stern test by application to the $\text{HCN} + \text{O}(^3P) \rightarrow \text{HCNO}$ reaction energy. The two-dimensional FPA grid for extrapolation to both the orbital basis set (CBS) and electron correlation (FCI) limits comprises Table 6. The HF/CBS reaction energy is $+15.2 \text{ kcal mol}^{-1}$, while the MP2/CBS correction to this starting point is a prodigious $-78.4 \text{ kcal mol}^{-1}$. Thus, the reaction is substantially endoergic with HF and strongly exoergic with MP2, demonstrating the demands placed on the coupled-cluster series to reach a converged answer. Toward this end the [CCSD, CCSD(T)] increments are $(+20.1, -8.3) \text{ kcal mol}^{-1}$ at the CBS limit, after which $\Delta E_e[\text{CCSD(T)/CBS}] = -51.4 \text{ kcal mol}^{-1}$ is obtained. In brief, a phenomenal oscillatory series is witnessed that is unfettered until the triple excitations are accounted for by coupled-cluster theory. The convergence of the energetic predictions with respect



to orbital basis set displays the characteristic properties of the FPA method.¹⁶⁵⁻¹⁷³ In particular, HF reaches the CBS limit very rapidly, $\delta[\text{MP2}]$ displays a protracted decay that varies $0.7 \text{ kcal mol}^{-1}$ even after cc-pCV6Z, and the higher-order correlation increments are increasingly insensitive to basis set as the electronic excitation level builds up.

Table 6. Vibrationless reaction energy (ΔE_e , kcal mol⁻¹) of $\text{HCN} + \text{O}(^3P) \rightarrow \text{HCNO}^a$

	$\Delta E_e(\text{HF})$	$\delta[\text{MP2}]$	$\delta[\mathcal{C}]$	$\delta[\mathcal{C}(\text{T})]$	$\delta[\mathcal{C}(\text{T})]$	$\delta[\mathcal{C}(\text{T}(\text{Q}))]$	$\delta[\mathcal{C}(\text{TQ})]$	$\delta[\mathcal{C}(\text{TQ}(\text{P}))]$	$\delta[\mathcal{C}(\text{TQP})]$	$\delta[\mathcal{C}(\text{TQP}(\text{H}))]$	NET
6-31G* (FC)	18.29	-66.05	16.69	-5.62	0.20	-0.95	0.21	0.12	-0.15	0.01	-37.23
cc-pVDZ (FC)	19.77	-65.98	16.12	-5.92	0.22	-0.96	0.24	0.14	[-0.15]	[0.01]	[-36.50]
cc-pVTZ (FC)	15.96	-72.43	18.82	-7.54	0.50	-0.95	[0.24]	[0.14]	[-0.15]	[0.01]	[-45.40]
cc-pCVQZ (FC)	15.34	-75.39	19.48	-7.91	[0.50]	[-0.95]	[0.24]	[0.14]	[-0.15]	[0.01]	[-48.70]
cc-pCVQZ (AE)	15.34	-75.96	19.53	-8.07	[0.50]	[-0.95]	[0.24]	[0.14]	[-0.15]	[0.01]	[-49.38]
cc-pCV5Z (AE)	15.18	-77.16	19.82	-8.18	[0.50]	[-0.95]	[0.24]	[0.14]	[-0.15]	[0.01]	[-50.55]
cc-pCV6Z (AE)	15.16	-77.69	19.95	-8.22	[0.50]	[-0.95]	[0.24]	[0.14]	[-0.15]	[0.01]	[-51.01]
CBS	[15.16]	[-78.40]	[20.13]	[-8.29]	[0.50]	[-0.95]	[0.24]	[0.14]	[-0.15]	[0.01]	[-51.62]

AE-CCSDTQ(P)/CBS + MVD1 reference geometries

$$D_e(\text{HCN-O}) = -[\Delta E_e(\text{FPA}) + \Delta(\text{MVD1}) + \Delta(\text{DBOC}) + \Delta(\text{SOC})] \Rightarrow$$

$$D_e(\text{HCN-O}) = -(-51.62 + 0.35 - 0.03 + 0.22) = \mathbf{51.08 \text{ kcal mol}^{-1}}$$

$$D_0(\text{HCN-O}) = D_e(\text{HCN-O}) + \Delta(\text{ZPVE}) = 51.08 - 2.00 = \mathbf{49.08 \text{ kcal mol}^{-1}}$$

^a \mathcal{C} is shorthand for CCSD. The symbol δ denotes increments in ΔE_e with respect to the preceding level of theory in the electron correlation series HF \rightarrow MP2 \rightarrow CCSD \rightarrow CCSD(T) \rightarrow CCSDT \rightarrow CCSDT(Q) \rightarrow CCSDTQ \rightarrow CCSDTQ(P) \rightarrow CCSDTQP \rightarrow CCSDTQP(H). Brackets signify results from primary CBS extrapolations (eqs 1 and 2) or additivity assumptions. The sum across each row yields the NET column entry, which approximates the CCSDTQP(H) (or FCI) result with the corresponding basis set. UHF orbitals were employed for $\text{O}(^3P)$, given that the spin contamination of the UHF reference wavefunction is negligible. (FC, AE) specifies whether a given row pertains to (frozen-core, all-electron) computations.

Our FPA of the reaction energy embeds the $1s$ effects in the AE-[MP2, CCSD, CCSD(T)] computations with the cc-pCV(Q,5,6)Z basis sets, superseding any auxiliary correction for core correlation. To proceed toward a definitive reaction energy, AE results have been carefully seamed together in Table 6 with frozen-core treatments up to CCSDTQP(H). The inclusion of rows for both FC- and AE-CCSD(T)/cc-pCVQZ effectuates a smooth fusion and yields a new type of construction for FPA layouts. For example, the difference of the NET entries for these two rows gives $-0.68 \text{ kcal mol}^{-1}$ as the $1s$ correlation effect on ΔE_e , similar in size to the corresponding bond-energy shift for the NO diatomic.¹³⁶ The oscillatory pattern for the correlation increments persists with $(\delta[\text{CCSDT}], \delta[\text{CCSDT}(\text{Q})], \delta[\text{CCSDTQ}]) = (+0.50, -0.95, +0.24) \text{ kcal mol}^{-1}$, after which the net effect is essentially zero. The 6-31G* and cc-pVDZ increments past the CCSD(T) level are virtually identical, justifying use of the smaller basis set in the extension toward the FCI



limit. The final FC-CCSDTQP(H)/6-31G* job on HCNO required 10 weeks of continuous CPU time on a high-performance cluster, yielding an FPA table of unprecedented reach. The coup de grâce is the final increment revealing that hexuple excitations change the reaction energy by only 0.01 kcal mol⁻¹.

The dual extrapolation in Table 6 yields $\Delta E_e(\text{FPA}) = -51.6$ kcal mol⁻¹, which is appended with $\Delta(\text{MVD1}) = 0.35$ kcal mol⁻¹ [AE-CCSD(T)/cc-pCV5Z], $\Delta(\text{DBOC}) = -0.03$ kcal mol⁻¹ [AE-CCSD/cc-pCVQZ], and $\Delta(\text{SOC}) = 0.22$ kcal mol⁻¹. The last auxiliary term is a spin-orbit correction for the O atom, derived as usual by taking a weighted average of the relative energies (0, 158.265, 226.977) cm⁻¹ pinpointed spectroscopically for the (³P₂, ³P₁, ³P₀) multiplets.¹⁷⁴ The final result for ΔE_e translates into the vibrationless dissociation energy $D_e(\text{HCN-O}) = 51.1$ kcal mol⁻¹.

Constructing the ZPVE correction for the HCN-O dissociation energy is complicated by the anharmonicity of the large-amplitude H-C-N bending mode (ν_5) of fulminic acid. Fortunately, an optimum effective one-dimensional potential for the ν_5 mode is available from semirigid bender fits of high-resolution spectroscopic data, and the vibrational states supported by this potential have been determined by matrix diagonalization of the corresponding effective Hamiltonian.⁴¹ As discussed above in Section 3.2, a ZPVE of 146.9 cm⁻¹ is found for ν_5 on the adiabatic curve given by the ground state of the complementary vibrational modes.⁴¹ Combining this ν_5 value with the ZPVEs given by our AE-CCSDTQ(P)/CBS + MVD1 harmonic frequencies (Tables 2 and 3) for the other vibrational modes of HCNO and HCN, we arrive at $\Delta(\text{ZPVE}) = -2.00$ kcal mol⁻¹. Hence, we ascertain $D_0(\text{HCN-O}) = 49.08$ kcal mol⁻¹, with a rough uncertainty estimate of ± 0.15 kcal mol⁻¹. This bond energy for fulminic acid is over 10 kcal mol⁻¹ larger than the value $D_0(\text{N}_2\text{-O}) = 38.44$ kcal mol⁻¹ given by current thermochemical tabulations¹⁷⁵ for the isoelectronic nitrous oxide molecule.

The $D_0(\text{HCN-O})$ result obtained in this research by high-level computations provides an important alternative route for the determination of $\Delta_f H_0^\circ$ for fulminic acid. Utilizing the precisely known¹⁷⁵ values $\Delta_f H_0^\circ(\text{HCN}) = 30.994 \pm 0.021$ kcal mol⁻¹ and $\Delta_f H_0^\circ(\text{O}) = 58.9971 \pm 0.0005$ kcal mol⁻¹, our $D_0(\text{HCN-O})$ yields $\Delta_f H_0^\circ(\text{HCNO}) = 40.92$ kcal mol⁻¹. The current ATcT value for this enthalpy of formation (40.81 ± 0.11 kcal mol⁻¹) appears to come essentially from $\Delta_f H_0^\circ(\text{HNCO}) = -27.71 \pm 0.07$ kcal mol⁻¹ and the isocyanic acid \rightarrow fulminic acid isomerization energy of 68.5 ± 0.2 kcal mol⁻¹ surmised in a 2004 computational study.⁸⁰ This ATcT quantity is in accord with our alternative derivation of $\Delta_f H_0^\circ(\text{HCNO})$, and the level of agreement is certainly within the collective



error bars of the two numbers. Nevertheless, our $\Delta_f H_0^\circ(\text{HCNO})$ result provides valuable new information for the ATcT refinement algorithm.

4. SUMMARY

This comprehensive quantum chemical investigation of fulminic acid has performed numerous analyses and reached an abundance of conclusions, as summarized in the following bullet points:

- (1) Previous theoretical work on fulminic acid through the CCSD(T) level is not sufficiently converged to the *ab initio* limit to definitively solve longstanding, vexing problems posed by this paradigmatic molecule of historical prominence.
- (2) For HCN, our best *ab initio* [AE-CCSDTQ(P)/CBS + MVD1] equilibrium bond distances and harmonic vibrational frequencies match the empirically derived values to within 0.00017 Å and 1.6 cm⁻¹, respectively, constituting a genuine triumph of modern theoretical and experimental chemical physics.
- (3) In our final analysis, fulminic acid (HCNO) manifests a linear minimum on the Born-Oppenheimer potential energy surface with $[r_e(\text{H-C}), r_e(\text{C-N}), r_e(\text{N-O})] = (1.0590, 1.1588, 1.2024)$ Å and $(\omega_1, \omega_2, \omega_3, \omega_4) = (3497, 2275, 1266, 548)$ cm⁻¹, as provided by the same level of theory [AE-CCSDTQ(P)/CBS + MVD1] that yields essentially exact results for the HCN benchmark.
- (4) The extensive series of AE correlation methods applied here with CBS extrapolation to the H-C-N bending frequency of linear HCNO generates phenomenal fluctuations: $\omega_5(\pi) = (604, 260i, 334, 120, 146, 49i, 52, 45)$ cm⁻¹ for [HF, MP2, CCSD, CCSD(T), CCSDT, CCSDT(Q), CCSDTQ, CCSDTQ(P)]. With incorporation of MVD1 relativistic effects, $\omega_5 = 19$ cm⁻¹ is obtained as the final Born-Oppenheimer frequency. Accordingly, without ZPVE modulation from complementary vibrations, the ω_5 mode of linear HCNO is an almost perfect quartic oscillator with a nearly vanishing quadratic component.
- (5) Core electron correlation, the diagonal Born-Oppenheimer correction (DBOC), and scalar relativistic effects (MVD1) all play a pivotal role in determining whether vibrationless HCNO is linear or bent; the cooperation of the first two driving forces against MVD1 preserves the linear structure. The influence of 1s correlation on the H-C-N bending frequency is particularly dramatic, as FC-CCSD(T)/CBS yields $\omega_5 = 65$ cm⁻¹, but AE-CCSD(T)/CBS gives $\omega_5 = 120$ cm⁻¹.



- (6) The AE-MP2/CBS method incorrectly favors a bent optimum structure of HCNO that lies 73 cm^{-1} below the linear form; the associated $(\theta_{\text{HCN}}, \theta_{\text{CNO}})$ angles deviate from linearity by $(23.5^\circ, 5.5^\circ)$.
- (7) Remarkably, the (Q) electron correlation contribution wrongly changes the structure of HCNO from linear to bent; nevertheless, the AE-CCSDT(Q)/CBS barrier to linearity is a microscopic 0.1 cm^{-1} , and the $(\theta_{\text{HCN}}, \theta_{\text{CNO}})$ angles are bent by only $(6.1^\circ, 1.4^\circ)$ from linearity.
- (8) Although both AE-MP2/CBS and AE-CCSDT(Q)/CBS give an imaginary ω_5 frequency for linear HCNO, the diagonal force constants $F_{44}(\text{H-C-N bend})$ and $F_{55}(\text{C-N-O bend})$ are both positive; accordingly, favorable F_{45} coupling via simultaneous *trans*-bending is necessary to drive the molecule downhill in energy.
- (9) With correlated methods the CBS limit for ω_5 is reached slowly, making basis-set extrapolations paramount to accurate conclusions. Notably, the AE-CCSD(T)/cc-pCV6Z frequency of linear HCNO is raised by 31 cm^{-1} upon extrapolation, and at the FC-CCSD(T) level the cc-pCV6Z imaginary ω_5 ($54i \text{ cm}^{-1}$) actually becomes real (65 cm^{-1}) at the CBS limit.
- (10) The energy profile for H-C-N bending in fulminic acid is so flat that complementary-mode ZPVE becomes an important factor; the H-C and C-N bonds elongate upon bending, reducing the ZPVE in these modes, but contraction of the N-O bond may partially compensate for this effect.
- (11) Novel work has been completed for linear HCNO investigating the dependence of AE-CCSDTQ(P)/CBS r_e and ω_i values on a litany of CBS extrapolation schemes and substantiating our final predictions. Nonlinear fits to new extrapolation formulas reveal that the all-electron correlation energy within the cc-pCVXZ basis set series exhibits almost perfect X^{-3} decay for MP2 but either an $X^{-3.5}$ or $(X + 1/2)^{-3}$ dependence for CCSD and CCSD(T).
- (12) The D_1 and D_2 wavefunction diagnostics indicate that HCNO has borderline multireference electronic character, but full-valence CASSCF wavefunctions contradict this notion and show that this issue is not the cause of sensitivity to level of theory.
- (13) Core electron correlation contracts the bond distances in HCNO by $0.001\text{-}0.002 \text{ \AA}$, an order of magnitude more than MVD1. Incorporating $1s$ correlation causes an overall increase in harmonic stretching frequencies by $6\text{-}9 \text{ cm}^{-1}$; however, these frequency shifts are deceptive because the direct effect without geometry relaxation is to *decrease* $\omega_1\text{-}\omega_3$ by $5\text{-}9 \text{ cm}^{-1}$.



- (14) Fulminic acid has one of the shortest $r_e(\text{H-C})$ distances and highest C–H stretching frequencies known for organic compounds, perhaps rivaled only by monofluoroacetylene.
- (15) The facility of bending in XCNO compounds follows the order $\text{CN} < \text{CH}_3 < \text{H} < \text{Br} < \text{Cl} < \text{CF}_3 \ll \text{F}$, with the parent fulminic acid appearing just before the critical point for breaking the symmetry of the linear equilibrium structure.
- (16) The dissociation energy $D_e(\text{HCN-O})$ has been investigated by the first FPA computations to reach the CCSDTQP(H) level (at least for a tetra-atomic or larger system); new ground is thus broken in showing that the final correlation increment in the coupled cluster series for a challenging bond cleavage can be reduced to $0.01 \text{ kcal mol}^{-1}$.
- (17) The final N–O bond energy of fulminic acid from cutting-edge FPA computations is $D_0(\text{HCN-O}) = 49.1 \text{ kcal mol}^{-1}$, which is 28% larger than that of nitrous oxide; the $1s$ correlation effect on $D_0(\text{HCN-O})$ is a sizable $0.7 \text{ kcal mol}^{-1}$.
- (18) Our final theoretical analysis supports the spectroscopic characterization that fulminic acid is by strict criteria a quasibent rather than a quasilinear molecule, because its true Born-Oppenheimer equilibrium structure is linear but the effective one-dimensional potential for large-amplitude H–C–N bending has a small protuberance at linearity.

The rovibrational quantum structure of fulminic acid remains a worthwhile and inviting target for future theoretical investigations. The current study reveals the severe demands for generating an accurate potential energy surface of full dimensionality for variational computations. A less formidable intermediate goal is to use high levels of theory to map out the most favorable course for H–C–N bending from linearity and rigorously determine the energy profile and complementary-mode ZPVE along this route. Such an endeavor would aim to cement the quasibent status of fulminic acid by showing that the empirical one-dimensional effective H–C–N bending potentials surmised from voluminous spectroscopic data are consonant with purely *ab initio* quantum chemical computations at the highest possible levels.



ASSOCIATED CONTENT

Supplementary Information contains the quartic force field of linear HCNO [AE-CCSD(T)/CBS] and the total energies for the FPA computation of $D_e(\text{HCN-O})$.

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Notes

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Data Availability Statement

The data supporting this article have been included as a part of the Supplementary Information.



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Data Availability Statement

The data supporting this article have been included as a part of the Supplementary Information.

