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Effect of Sb–Bi alloying on electron–hole recombination time of Cs₂AgBiBr₆ double perovskite†

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The double perovskite material Cs₂AgBiBr₆, characterized by high stability, low toxicity, and excellent optoelectronic properties, has emerged as a promising alternative to lead-based halide perovskites in photovoltaic applications. However, its photovoltaic conversion efficiency after integration into solar cell devices is less than 3%, significantly lower than that of traditional perovskite solar cells. While alloying methods have been widely applied in the design of photovoltaic materials, their specific role in modulating the lifetime of photo-generated charge carriers in double-perovskite solar cells remains inadequately explored. In this study, through nonadiabatic molecular dynamics (NAMD) simulations, the excited-state dynamics properties of Cs₂AgBiBr₆ and alloyed Cs₂AgSb_{0.375}Bi_{0.625}Br₆ samples were compared. The results revealed that the introduction of Sb ions into the double perovskite structure induces lattice deformation upon heating to 300 K, leading to distortion of Bi–Br bonds and enhanced valence band delocalization. Using the decoherence-induced surface hopping method, the capture and recombination processes of charge carriers between different states were simulated. It was suggested that hole lifetime serves as the primary limiting factor for carrier lifetime in Cs₂AgBiBr₆, and replacing 0.375 proportion of Bi with Sb can decelerate the hole capture rate, extending carrier lifetime by 3–4 times. This study demonstrates that alloying offers a viable approach to optimizing the optoelectronic performance of the Cs₂AgBiBr₆ perovskite, thereby advancing the application of double perovskite materials in the field of photovoltaics.

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1. Introduction

The perovskites with the chemical formula ABX₃ (A⁺ = Cs⁺, MA⁺, FA⁺; B²⁺ = Sn²⁺, Pb²⁺; X[−] = Cl[−], Br[−], I[−]) exhibit excellent electronic and optical properties, such as long carrier diffusion lengths,^{1,2} high light absorption coefficients,³ and low exciton binding energies,⁴ thus attracting extensive attention as materials for solar energy and optoelectronics. In 2012, the team led by Nam-Gyu Park first reported on perovskite solar cells with an efficiency approaching 10% for the first time,⁵ and the efficiency of perovskite solar cells has now soared to 26.1%.⁶ However, lead-containing perovskite solar cells suffer from environmental instability and toxicity,^{7,8} prompting many researchers to seek materials capable of replacing lead while retaining outstanding optoelectronic properties.^{9,10} In recent years, lead-free halide double perovskites of the form A₂B₁B₁₁X₆

have emerged as promising alternatives to lead halide perovskites in photovoltaic applications due to their high stability, low toxicity, and excellent optoelectronic properties.^{11–13} Among them, Cs₂AgBiBr₆ is one of the most representative materials.^{14,15} Through experiments, Robert *et al.* found that the Cs₂AgBiBr₆ system possesses a long carrier lifetime of 1.4 μs, demonstrating the theoretically excellent optoelectronic performance of Cs₂AgBiBr₆ perovskite solar cells.¹⁶ However, the photovoltaic conversion efficiency of double perovskite solar cells based on Cs₂AgBiBr₆ falls short of expectations, reaching only around 6%, far below the Shockley–Queisser limit of 16%.¹⁷ Ou *et al.* enhanced the stability of Cs₂AgBiBr₆ perovskites by introducing SnS quantum dots, which suppressed the recombination of holes and electrons.¹⁸ Hence, further exploration of the photophysical properties of Cs₂AgBiBr₆ and a deeper understanding of carrier extraction and electron capture processes are of significant importance.

The lifetime of photo-generated charge carriers is an inherent factor influencing the photovoltaic conversion efficiency of solar cell devices. When the absorbing layer material of a solar cell is excited by light, it generates two types of charge carriers, electrons and holes. Electrons are excited to the conduction

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band, while holes remain in the valence band. Subsequently, relaxation occurs, and the electrons in the conduction band and the holes in the valence band recombine. Part of the energy is released in the form of photons, known as radiative recombination, while the other part is released as phonons, known as non-radiative recombination. Non-radiative recombination in perovskites increases the energy loss of charges, resulting in significantly lower efficiency compared to the Shockley–Queisser limit, thereby limiting the photovoltaic conversion efficiency of perovskite solar cells.¹⁹ Therefore, by simulating the dynamics of charge carriers and elucidating the mechanism of non-radiative recombination of electrons and holes, it is possible to provide theoretical explanations for corresponding experimental phenomena and guide the exploration of new materials. Understanding the effects of different modulation methods on charge carrier recombination and relaxation is crucial for enhancing the efficiency of perovskite solar cells.

The widely used Born–Oppenheimer approximation (adiabatic approximation) in traditional first-principles calculations only considers the average effect of stationary atomic nuclei and cannot adequately explain the nonadiabatic processes of electronic transitions from the ground state to the excited state.²⁰ To address this issue, we adopted the *ab initio* nonadiabatic molecular dynamics calculation program (Hefei-NAMD) developed by the research group led by Jin Zhao, which combines time-dependent density functional theory (TD-DFT) with the fewest switches surface hopping (FSSH) method to simulate excited-state dynamics.^{21,22} Currently, a considerable amount of work has utilized nonadiabatic dynamics to explore the charge carrier recombination and relaxation mechanisms in halide perovskites,^{23–31} but its application in the field of double perovskites remains limited.

In 2022, She *et al.* demonstrated the presence of harmful defect centers in $\text{Cs}_2\text{AgBiBr}_6$, attributed to the existence of Br vacancies, which increased hole trapping, while in doping slowed down hole trapping, extending charge recombination time by fourfold.³² This study thoroughly illustrates the significant modulation effect of alloying methods on the electronic structure of perovskites, capable of altering bandgap properties and values, passivating defects, and reducing hole trapping rates. Additionally, the influence of alloying on carrier relaxation, extraction, and transport has attracted attention from some researchers.^{33–37} Perovskite materials offer abundant routes for alloying modification, providing possibilities for defect passivation of $\text{Cs}_2\text{AgBiBr}_6$ using alloying methods. E. M. Hutter's group prepared Sb-doped Bi double perovskite films through powder wet chemistry treatment experiments, obtaining charge mobility and bandgap width at doping ratios of 0.05, 0.1, and 0.4, with the material exhibiting optimal light absorption ability at a doping ratio of 0.4.³⁸ However, there is still no consensus on whether doping Bi with Sb in $\text{Cs}_2\text{AgBiBr}_6$ can improve the efficiency of solar cell devices.

Inspired by the aforementioned experimental work, we partially replaced Bi elements in $\text{Cs}_2\text{AgBiBr}_6$ with Sb elements at a ratio of 0.375, constructing the $\text{Cs}_2\text{AgBi}_x\text{Sb}_{1-x}\text{Br}_6$ ($x = 0.375$) system, and conducted nonadiabatic molecular dynamics (NAMD) simulations on the charge capture and relaxation

processes in both systems. The results indicate that the bandgap of the alloyed system decreases, with significant influence on the orbital electrons of the Ag–Br bonds contributing to the valence band maximum (VBM), resulting in a decrease in the corresponding wave function's inverse participation ratio (IPR), indicating enhanced localization of the VBM. During the relaxation process of electron–hole pairs, quantum decoherence increases and the nonadiabatic (NA) coupling decreases. Ultimately, under the combined effects of both factors, the carrier lifetime is effectively extended by 3–4 times. This work demonstrates that alloying can effectively reduce energy losses, prolong carrier lifetimes, and provide another effective strategy for reducing electron–hole non-radiative recombination, offering guidance for enhancing the optoelectronic performance of halide double perovskites.

2. Methodology

This study employed the method of time-dependent density functional theory (TDDFT) combined with nonadiabatic molecular dynamics (NAMD) simulations. The Vienna *ab initio* simulation package (VASP) was utilized for geometric optimization, electronic structure calculations, and adiabatic molecular dynamics simulations.^{39–42} The electron–ion interactions were described using the projector augmented wave (PAW) method,⁴³ and the Perdew–Burke–Ernzerhof (PBE) functional under the generalized gradient approximation (GGA) was employed to handle the exchange–correlation energy of electrons.⁴⁴ The energy gap and chemical bond analyses were conducted using the projected crystal orbital Hamilton populations (pCOHP) method.^{45–47} K-point sampling was performed at the Γ point for geometric optimization and molecular dynamics. In geometric optimization, relaxation was halted when the force on all atoms fell below $1 \times 10^{-5} \text{ eV } \text{\AA}^{-1}$, with a plane-wave cutoff energy set at 450 eV. The structure after geometric optimization was heated to 300 K using the Nose–Hoover thermostat and then subjected to molecular dynamics simulations in the micro-canonical ensemble (NVE) with a time step of 1 fs for 10 ps. Subsequently, the population evolution of electrons and holes within 1 ns was computed using the decoherence-induced surface hopping (DISH) method based on the time-dependent Kohn–Sham (TD-KS) theory,^{48–53} leveraging the Hefei-NAMD code released by Zhao *et al.* in 2019.²² Since the Hefei-NAMD program is well-established for investigating carrier transitions at the same k -point and $\text{Cs}_2\text{AgBiBr}_6$ is an indirect bandgap material, in this work, the “supercell construction” approach was employed to achieve band folding, approximating the treatment with the Hefei-NAMD program at the Γ point.

3. Results and discussion

We employed first-principles calculations to investigate the band gap and photoelectric performance of the system after doping with different ratios of Sb. The specific calculation results and analysis process can be found in the ESI.† By comparing the results, we hypothesize that doping Bi in the original system with a ratio of 0.375 Sb will be more beneficial for



improving the photoelectric conversion efficiency of $\text{Cs}_2\text{AgBiBr}_6$. This study established a $2 \times 2 \times 2$ $\text{Cs}_2\text{AgBiBr}_6$ perovskite supercell comprising 320 atoms, with Ag and Bi atoms alternately arranged in three dimensions, as depicted in Fig. 1(a). For the doping sites, we chose high-symmetry points. The specific doping method involved interlayer substitution on the xz plane of the $\text{Cs}_2\text{AgBiBr}_6$ supercell, where $3/4$ of the Bi atoms were replaced by Sb, resulting in a $2 \times 2 \times 2$ $\text{Cs}_2\text{AgSb}_{0.375}\text{Bi}_{0.625}\text{Br}_6$ supercell, as depicted in Fig. 1(b). This doping method minimizes structural disruption, maintaining overall material stability. At the same time, high-symmetry sites also play a crucial role in the band structure and help reduce lattice scattering. Previous studies have shown that doping at high-symmetry points can effectively improve the performance of perovskite materials.^{38,54,55} After doping using this method, we performed geometric optimization and static calculations; the alloyed supercell is shown in Fig. 2. We found that structural changes were minimal, with negligible cell deformation, bond lengths even shortening, ionic binding energy decreasing, and crystallographic parameters remaining stable. The deformation caused by alloying was within 0.35%, and there was a trend of cell volume reduction. From a thermodynamic perspective, alloying can occur spontaneously in nature. Fig. S4 (ESI[†]) presents perspective views of the pristine $\text{Cs}_2\text{AgBiBr}_6$ system and the doped $\text{Cs}_2\text{AgSb}_{0.375}\text{Bi}_{0.625}\text{Br}_6$ system in various directions.

Fig. 3 illustrates the cell models of the (a) pristine $\text{Cs}_2\text{AgBiBr}_6$ and (b) Sb-doped $\text{Cs}_2\text{AgSb}_{0.375}\text{Bi}_{0.625}\text{Br}_6$ systems after geometric optimization at 0 K and 300 K. At low temperatures, the alloyed sample exhibited minimal deviation from the pristine sample after structural optimization. However, following a thermal bath at 300 K, significant differences arose in the octahedral structures of the two distinct cells. The pristine cell maintained a stable inorganic framework, with only slight adjustments in the geometric structure upon heating. In contrast, the Sb-doped system experienced substantial lattice distortion due to the introduction of smaller Sb ions compared to Bi ions. Fig. S5 (ESI[†]) shows the local octahedral structure configurations of the two cells at room temperature.

To quantitatively describe the effect of Sb element doping on the geometry of double perovskites, we calculated the average bond lengths of the original and doped systems at 0 K and 300 K, as shown in Table 1. At 0 K, the average Bi–Br and Ag–Br bond lengths in $\text{Cs}_2\text{AgBiBr}_6$ are 2.877 Å and 2.834 Å, respectively. At

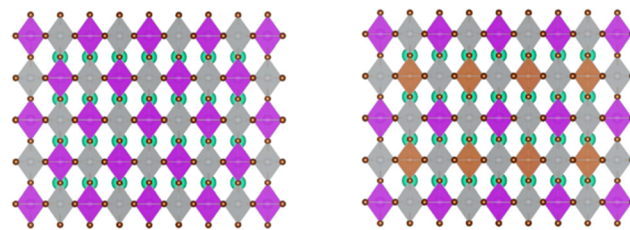


Fig. 2 $\text{Cs}_2\text{AgBi}_{0.375}\text{Sb}_{0.625}\text{Br}_6$ alloying solute Bi–Sb ratio diagram.

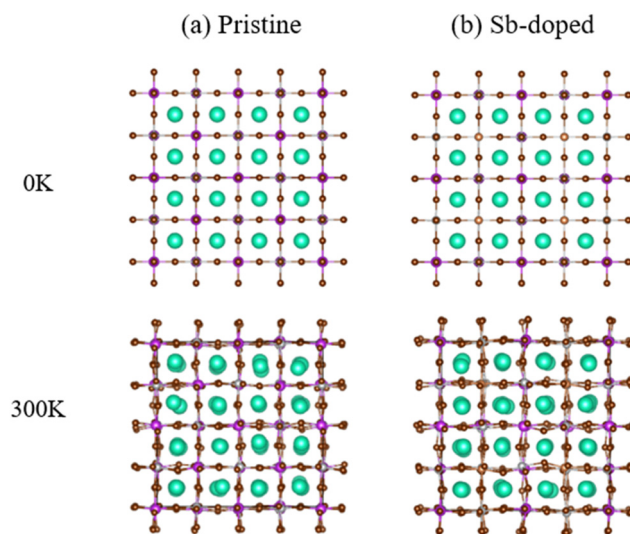


Fig. 3 Optimized geometric structures of (a) pristine $\text{Cs}_2\text{AgBiBr}_6$ and (b) Sb-doped $\text{Cs}_2\text{AgSb}_{0.375}\text{Bi}_{0.625}\text{Br}_6$ at 0 K and 300 K.

300 K, due to thermal effects, the average bond lengths of Bi–Br and Ag–Br extend to 2.904 Å and 2.873 Å. After Sb doping, the average bond lengths of Bi–Br and Ag–Br increase from 2.875 Å and 2.835 Å at 0 K to 2.903 Å and 2.873 Å at 300 K. Under thermal effects, the average Bi–Br and Ag–Br bond lengths in the original system increase by 0.027 Å and 0.039 Å, respectively, while in the doped system, they increase by 0.028 Å and 0.038 Å.

In addition to bond lengths, we also calculated the average Br–Bi–Br bond angles and Br–Ag–Br bond angles of the original and Sb-doped systems at 300 K, as shown in Table 2. The results show that both the Br–Bi–Br bond angle and Br–Ag–Br bond angle in $\text{Cs}_2\text{AgSb}_{0.375}\text{Bi}_{0.625}\text{Br}_6$ (144.04° , 143.28°) are smaller than those in $\text{Cs}_2\text{AgBiBr}_6$ (144.66° , 143.84°). Angles closer to the ideal 180° indicate weaker distortion of the shape. These results suggest that with the addition of Sb, bond lengths increase and

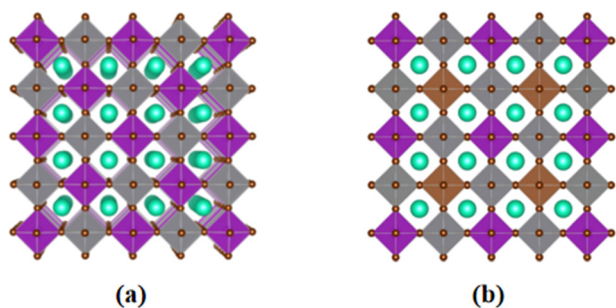


Fig. 1 Crystalline structures of (a) $\text{Cs}_2\text{AgBiBr}_6$ and (b) $\text{Cs}_2\text{AgSb}_{0.375}\text{Bi}_{0.625}\text{Br}_6$.

Table 1 The average length (Å) of Br–X (X = Bi, Ag, Sb) in pristine $\text{Cs}_2\text{AgBiBr}_6$ and doped $\text{Cs}_2\text{AgSb}_{0.375}\text{Bi}_{0.625}\text{Br}_6$

	Pristine		Doped		
	Bi–Br	Ag–Br	Bi–Br	Ag–Br	Sb–Br
0 K	2.877	2.834	2.875	2.835	2.822
300 K	2.904	2.873	2.903	2.873	2.855
Increase	0.027	0.039	0.028	0.038	0.033



Table 2 The average bond angles (deg.) of Br–X–Br (X = Bi, Ag, Sb) in pristine Cs₂AgBiBr₆ and doped Cs₂AgSb_{0.375}Bi_{0.625}Br₆

	Pristine		Doped		
	Br–Bi–Br	Br–Ag–Br	Br–Bi–Br	Br–Ag–Br	Br–Sb–Br
0 K	180	180	180	180	180
300 K	144.66	143.84	144.04	143.28	143.88
Increase	35.34	36.16	35.96	36.72	36.12

bond angles decrease. The incorporation of Sb increases geometric distortion, enhances atomic disorder, increases atomic motion, and promotes atomic fluctuations.

The migration and transport of carriers in double perovskites are closely related to the octahedral cage structure rather than the ions of a particular element. Therefore, the changes in the electronic structure brought about by Sb doping are not easily detected in traditional bandgap engineering. We used the Lobster software to calculate the pCOHP for analyzing bonding characteristics, as shown in Fig. 4. Fig. 4(a) illustrates that the conduction band minimum (CBM) of the pristine cell is mainly contributed by the Bi–Br bonds, while the VBM is primarily contributed by the Ag–Br bonds. Fig. 4(b) demonstrates that the contribution of the Sb–Br bonds after doping is significantly higher than that of the other two types of bonds. The results indicate that the VBM is elevated compared to the pristine cell Fermi level, with a shift of approximately 0.2 eV, reducing the bandgap from 1.27 eV to 0.97 eV, which is more favorable for light absorption.

The strength of non-adiabatic (NA) electron–phonon coupling is related to the overlap between the highest occupied molecular orbital (HOMO) and the lowest unoccupied molecular orbital (LUMO) wave functions. The matrix element between them is expressed as $-i\hbar\langle\varphi_i|\nabla_{\mathbf{R}}H|\varphi_j\rangle$, where φ_i and φ_j are the wave functions corresponding to the two orbitals. The formula for NAC is as follows:

$$d_{ij} = -i\hbar\langle\varphi_i|\nabla_{\mathbf{R}}|\varphi_j\rangle \cdot \dot{\mathbf{R}} = -i\hbar\frac{\langle\varphi_i|\nabla_{\mathbf{R}}H|\varphi_j\rangle}{E_j - E_i} \cdot \frac{d\mathbf{R}}{dt}$$

$$= -i\hbar\left\langle\varphi_i\left|\frac{\partial}{\partial t}\right|\varphi_j\right\rangle$$

Here, E_i and E_j are the energies of the two orbitals and $E_j - E_i$ is the corresponding energy gap. H is the Kohn–Sham Hamiltonian and $d\mathbf{R}/dt$ represents the nuclear velocity.⁵⁶ It can be seen that smaller overlap between HOMO and LUMO, a larger energy gap, and smaller nuclear velocity result in smaller NAC, which has a positive effect on the extension of carrier lifetime.

Fig. 5 illustrates the charge density of the HOMO and LUMO for both samples. In the pristine Cs₂AgBiBr₆ cell, the charge density of the HOMO primarily resides on the Br atoms, while the charge density of the LUMO is mainly concentrated on the Bi atoms, followed by the Br atoms. After Sb doping in the Cs₂AgSb_{0.375}Bi_{0.625}Br₆ lattice, the charge distribution on the LUMO orbitals tends to localize on the Sb and Br atoms, while the charge density on the Br atoms in the HOMO orbitals gradually delocalizes. The overlap of charge density distributions between LUMO and HOMO was reduced after alloying,

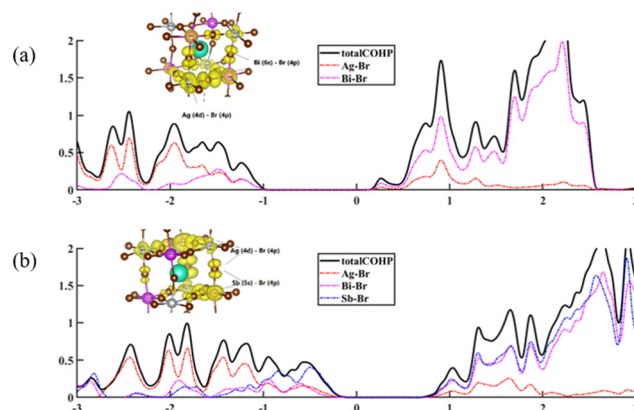


Fig. 4 Crystal orbital Hamilton populations (COHP) of (a) Cs₂AgBiBr₆ and (b) Cs₂AgSb_{0.375}Bi_{0.625}Br₆.

thereby decreasing the nonadiabatic coupling (NAC). The nuclear velocity is mainly related to temperature and atomic mass, both of which do not change significantly. The reduced overlap between the wave functions of LUMO and HOMO contributes to the reduction of NAC, whereas the increased band gap after alloying has a suppressing effect on reducing NAC. Between these two factors, the former plays a dominant role. Ultimately, the NAC of the system decreases after alloying. The calculated non-adiabatic coupling values are shown in Table 3. Fig. S6 (ESI†) provides three-dimensional charge isodensity surface imaging.

To identify the phonon modes involved in charge trapping and recombination dynamics, we performed a Fourier transform (FT) of the non-normalized autocorrelation function (un-ACF) of CBM–VBM band gap fluctuations to obtain the spectral density.⁵⁷ As shown in Fig. 6, low-frequency phonon modes play a major role in both the original and doped systems, as they generate non-adiabatic coupling and drive non-radiative

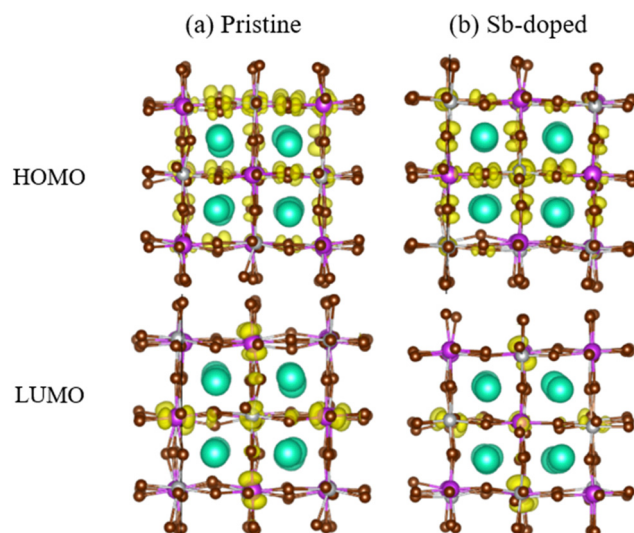


Fig. 5 Charge densities of the HOMO and LUMO in the (a) pristine Cs₂AgBiBr₆ and (b) Sb-doped Cs₂AgSb_{0.375}Bi_{0.625}Br₆.



Table 3 Pure-dephasing time and average NAC of pristine $\text{Cs}_2\text{AgBiBr}_6$ and Sb-doped $\text{Cs}_2\text{AgSb}_{0.375}\text{Bi}_{0.625}\text{Br}_6$

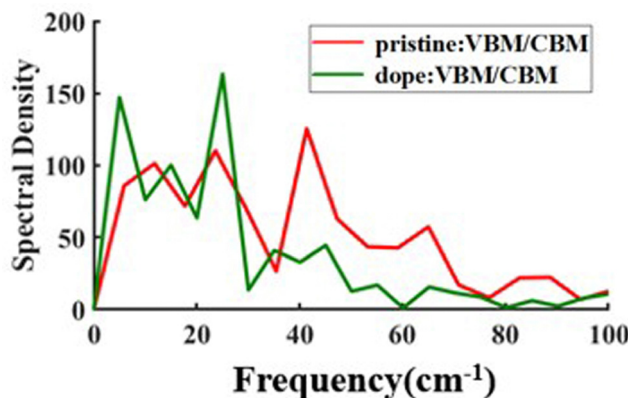
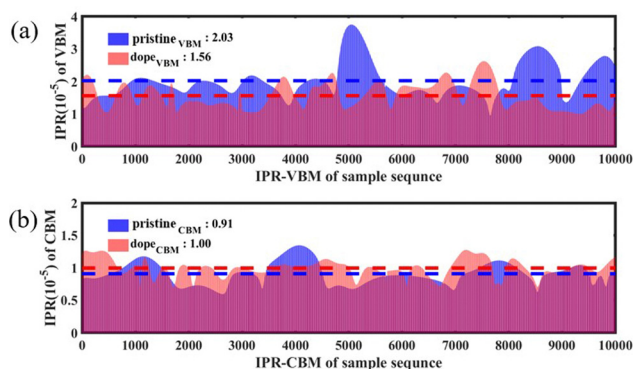
	Pristine	Doped
	Initial-ground	Initial-ground
Dephasing (fs)	30.4	22.7
NAC (10^{-6} eV)	105.8	13.7

electron-hole recombination. Phonon modes below 40 cm^{-1} dominate the electron-hole recombination process. When the spectral signals of both the original and doped systems are distributed in regions below 40 cm^{-1} , the doped system exhibits higher-frequency vibration modes overall compared to the original system. This is due to the introduction of Sb elements, forming Sb-Br bonds, which fluctuate most intensely, further enhancing the motion of the double perovskite lattice. This influences the selection rules of electron-vibration coupling, activating new high-frequency vibration modes. The introduction of new high-frequency phonon modes accelerates the decoherence process, facilitating the prolongation of the charge recombination process.

To further characterize the impact of alloying on the charge distribution of key electronic states, we calculated the inverse participation ratio (IPR) of the VBM and CBM over a 10 ps MD trajectory at 300 K. The IPR is an important parameter for calculating the orbital space probability amplitude,

$$\text{IPR} = N \times \frac{\sum k_i^4}{(\sum k_i^2)^2}$$

$0 < \text{IPR} \leq 1$, where N represents the sum of the total grid points in the plane wave basis in the Kohn-Sham equation and k_i represents the charge density contributed by electronic state i .^{58,59} By computing the IPR sequences, the localization degree of the wave function in a certain state can be obtained. A larger IPR value indicates a more localized wave function. $\text{IPR} = 1$ indicates a fully localized state. Fig. 7(a) and (b) respectively show the comparison of the IPR at the VBM and CBM for the pristine $\text{Cs}_2\text{AgBiBr}_6$ sample and the alloyed sample

**Fig. 6** The spectral density of the original and doped systems obtained by the Fourier transform of the energy gap fluctuation autocorrelation function.**Fig. 7** Comparison of the IPR sequences at the (a) VBM and (b) CBM between the pristine sample and the doped sample.

$\text{Cs}_2\text{AgSb}_{0.375}\text{Bi}_{0.625}\text{Br}_6$. In these figures, blue represents the pristine sample, pink represents the sample after alloying, and purple indicates the overlapping parts. From Fig. 7(b), it can be observed that the change in IPR at the CBM can be almost negligible. However, in Fig. 7(a), the average IPR of the VBM after alloying increased by approximately 1.3 times compared to the pristine sample, indicating a high degree of localization of the VBM wave function. The high localization of electronic states facilitates effective separation of electrons and holes, thereby weakening NAC.

Finally, we simulated the capture and recombination processes of carriers between different states using the DISH method, obtaining the decay process of the excited-state carriers. We fitted the relaxation curve with an exponential function to obtain a smooth curve, where equilibrium was reached at infinity, and 98% of the equilibrium distribution was considered the end of relaxation. The results are shown in Fig. 8, with the unfitted images displayed in Fig. S7 (ESI†). Fig. 8(a) and (b) depict the evolution curves of electrons and holes in different states for the pristine sample, while Fig. 8(c) and (d) show the evolution curves of electrons and holes for the doped sample. According to the previous analysis in this paper, the lifetime of holes is the main factor determining the carrier lifetime of the system we are studying. When exposed to light, electrons and holes separate, and the holes absorb the photon's energy and are excited to the valence band. Due to the randomness of energy level transitions, holes may occupy different energy levels in the valence band. Studying only one of these states does not provide a comprehensive understanding, and the probability of transitions to energy levels deeper than the deep state is relatively low. Therefore, to ensure more accurate, rigorous, and comprehensive results, we studied three representative states in the valence band. Electrons transition from the initial state to the ground state, while holes transition from the initial state to the other three states (initial state, shallow state and deep state). Comparing Fig. 8(a) and (b), it can be observed that the lifetimes of electrons and holes differ by an order of magnitude. When surplus electrons accumulate net charges at the two poles of the battery material, forming a saturated drift field, the excess electrons annihilate through non-radiative recombination involving mutual repulsion. According to previous studies, holes, as



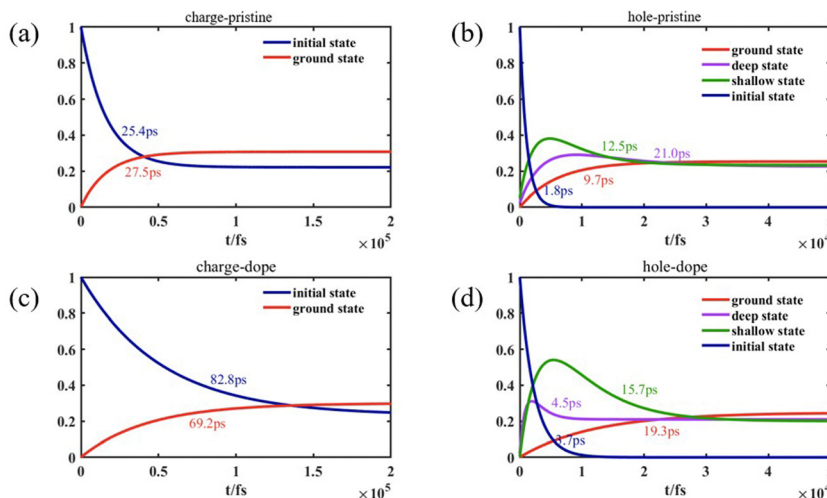


Fig. 8 Time-dependent orbital population evolution curves of (a) electrons and (b) holes in the pristine sample, and (c) electrons and (d) holes in the doped sample.

minority carriers in the $\text{Cs}_2\text{AgBiBr}_6$ system, play a major role in determining carrier lifetime.^{60,61} Therefore, in the samples constructed in this study, we primarily consider the evolution of hole populations. We investigated three representative states in the valence band: the initial state, shallow state, and deep state. As for the electrons, which do not play a major role, their lifetime is mainly related to recombination with holes in the ground state. However, carriers may dwell in shallow and deep energy states, but these states are merely transitional during the relaxation process. In most cases, electron–hole recombination occurs in the ground state, so we mainly compare the recombination time of carriers in the ground state. As shown in Fig. 8(b) and (d), the relaxation process in the pristine sample ends before 10 ps, while in the doped sample, the capture time of non-radiative transitions for holes is extended, and the multi-level states only reach equilibrium at 20 ps. Thus, Sb doping significantly slows down the electron–hole recombination, extending the carrier lifetime by 3–4 times.

The decoherence method can observe the quantum state evolution of microscopic systems, providing physical evidence for particle jumps between potential energy surfaces; the decoherence time corresponding to state α is τ_α .

$$\frac{1}{\tau_\alpha}(t) = \sum_{i \neq \alpha}^N |c_i(t)|^2 r_{\alpha i} \quad (1)$$

where c_i is the population in the adiabatic representation and $r_{\alpha i}$ is the decoherence rate during the collapse process of state α , and in adiabatic kinetic sampling, the decoherence processes of nuclear trajectories and adiabatic states can be described by interference terms due to state superposition.

$$J_{ij}(t) \approx \langle J_{ij}(R(t)) \rangle_T = \exp(i\omega_{ij}t) \exp\left[-\frac{i}{\hbar} \int_0^t \Delta E_{ij}(\tau) d\tau\right] \quad (2)$$

The time-dependent term J_{ij} is the wavepacket overlap of the two-state system, and the environmentally induced

decoherence process can be estimated. Zheng Qijing *et al.* approximated the canonical averaging of the above equation to second-order cumulant terms.

$$D(t) = \exp\left(\frac{1}{\hbar^2} \int_0^{t_1} dt_1 \int_0^{t_2} dt_2 [E(t_2)E(0)]\right) \quad (3)$$

When the response function is obtained by accumulating trajectories according to the above cumulative terms, the characteristic time obtained from fitting a Gaussian function can be considered the decoherence time of the two-state system.

$$d_{ij} \cdot \dot{R} = -i\hbar \left\langle \phi_j \left| \frac{\partial}{\partial t} \right| \phi_k \right\rangle \quad (4)$$

Meanwhile, the nuclear potential energy acts as the system bath in the quasi-continuous time-dependent evolution, and the NAC vector generated by the two states is part of the time-dependent Hamiltonian evolution.^{52,62,63}

Table 3 provides the decoherence times and NAC coefficients for the electron evolution between the initial and ground states in the pristine $\text{Cs}_2\text{AgBiBr}_6$ system and the Sb-doped system $\text{Cs}_2\text{AgSb}_{0.375}\text{Bi}_{0.625}\text{Br}_6$. It can be observed that after doping, the decoherence time decreases, and the decoherence rate increases by approximately 1.34 times. Additionally, Sb doping reduces the NAC coefficient by an order of magnitude. While electrons do not predominantly influence the recombination time, alloying still significantly modulates the electron orbitals, which is beneficial for extending the carrier lifetime.

In the dominant thermal hole evolution process, alloying modulation leads to a significant enhancement in the ability to capture carriers by shallow defects. The decoherence time and NAC coefficients for the evolution of holes from the shallow state to the deep state and ground state in the pristine $\text{Cs}_2\text{AgBiBr}_6$ system and the Sb-doped $\text{Cs}_2\text{AgSb}_{0.375}\text{Bi}_{0.625}\text{Br}_6$ system are shown in Table 4. The relaxation process from the shallow state to the deep state primarily dominates the decoherence



Table 4 Pure-dephasing time and average NAC of pristine $\text{Cs}_2\text{AgBiBr}_6$ and Sb-doped $\text{Cs}_2\text{AgSb}_{0.375}\text{Bi}_{0.625}\text{Br}_6$

	Pristine		Doped	
	Shallow–deep	Shallow–ground	Shallow–deep	Shallow–ground
Dephasing (fs)	77.2	29.4	32.6	19.4
NAC (10^{-6} eV)	2847.5	7.12	1152.4	144.0

time, and after alloying, the decoherence acceleration of hot holes under this pair of energy states is twice that of the pristine sample, greatly hindering the recombination process. In general, a smaller band gap, stronger nonadiabatic coupling, and slower decoherence will lead to faster carrier recombination. After Sb doping, the NAC during the transition from the shallow state to the deep state significantly decreases, indicating an extension of the carrier lifetime. However, there is an opposite trend in NAC when transitioning from the shallow state to the ground state. The final electron–hole recombination time is related to both NAC and decoherence time. We can consider that the reduced decoherence time successfully outweighs the increased NAC. Alloying is an important means of coherence modulation, which can accelerate the decoherence process and delay carrier recombination, and thus extend carrier lifetime.

4. Conclusion

In this study, to elucidate the regulatory mechanism of alloying on the carrier lifetime of the $\text{Cs}_2\text{AgBiBr}_6$ double perovskite, we established the pristine $\text{Cs}_2\text{AgBiBr}_6$ system and an alloying system, $\text{Cs}_2\text{AgSb}_{0.375}\text{Bi}_{0.625}\text{Br}_6$, by replacing Bi with Sb at a ratio of 0.375. Nonadiabatic molecular dynamics simulations combined with time-dependent density functional theory were employed to systematically investigate the excited-state dynamics of these systems. The results indicate that introducing Sb ions with a smaller radius than Bi ions significantly alters the lattice structure of the double perovskite, changes the intrinsic frequencies of atomic vibrations, and reduces the wave function overlap, thereby lowering the NAC of relevant states. The bandgap of the alloyed sample decreased from 1.27 eV to 0.97 eV, with significant effects on bromine bonds and modification of the conduction band contributed by Bi–Br bonds. Particularly, Sb doping slowed down the hole capture rate and decelerated the non-radiative recombination process of carriers by 3–4 times. The thermalization processes of electrons and holes were presented separately, with electron decoherence increasing by approximately 1.34 times and NAC decreasing. Hole lifetime, which is the bottleneck affecting carrier lifetime, was significantly increased by the alloying method, ultimately effectively extending the carrier lifetime. In summary, this study demonstrates the regulatory effect of alloying on the $\text{Cs}_2\text{AgBiBr}_6$ system, provides compelling evidence for extending carrier lifetime in the $\text{Cs}_2\text{AgSb}_{0.375}\text{Bi}_{0.625}\text{Br}_6$ sample, and offers suggestions for mitigating harmful defects in $\text{Cs}_2\text{AgBiBr}_6$ double perovskite solar cells.

Data availability

All data included in this study are available upon request by contact with the corresponding author.

Conflicts of interest

There are no conflicts to declare.

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