Dissociation of HNO₃ in water revisited: experiment and theory†

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Nitric acid dissociation in water is studied as a function of concentration, employing experimental techniques (^{1}H NMR spectroscopy and calorimetry), quantum chemical methods (B3LYP and PBE functionals for molecular clusters) and molecular dynamics simulations (the PBE-D3 functional for solutions under periodic boundary conditions). The extent of dissociation, *via* proton transfer to a neighboring water molecule, as a function of concentration is studied computationally for molecular nitric acid clusters $HNO_3(H_2O)_x$ ($x = 1$–8), as well as periodic liquids (HNO_3 mole fractions of 0.19 and 0.5, simulated at $T = 300$ K and 450 K). Despite the simple nature of these structural models, their computed and simulated average ^{1}H chemical shifts compare well with the experimental measurements in this study. Finally, the measured and calculated chemical shifts have shown reasonable relationships with the enthalpy change upon mixing of this binary complex.

Introduction

The investigation of microhydration is key to understanding the behavior of various anions in water solutions and aerosols. The nitrate ion holds a special place among the anions studied since it is one of the most abundant anions on Earth. The nitrate ion participates in a variety of processes ranging from atmospheric chemistry to nuclear waste processing:[1] nitric acid is reported to play a role in the formation of the Antarctic stratosphere ozone hole[2] and nitrate anion behavior in water solutions may affect further the processes of nuclear waste preparation. Furthermore, nitrate ion pollution in water due to the excessive use of fertilizers is both serious and widespread. The dissociation of strong acids in water is of great importance for a large class of chemical reactions in aqueous solutions.[2] Proton transfer (PT) reactions are widely known in chemistry and biochemistry. Among the most familiar of these reactions is the transfer of a proton from strong acids such as nitric acid (HNO_3) to a water molecule in an aqueous solution. Theoretical investigation of microhydration is an important task for

understanding the behavior of various anions in water solutions and aerosols. Molecular level insight into the dissociation of nitric acid in water has been obtained from DFT calculations and molecular dynamics simulations.[3] Xanteas and coworkers have studied the formation of $HNO_3(H_2O)_n$ complexes theoretically ($n = 0$, 4) and experimentally in the gas phase.[4] Calculations (MP2/aug-cc-pVDZ) have predicted the appearance of ion-pair configurations in the gas phase for $n = 4$ or higher.[4] Escribano *et al.* investigated (B3LYP/aug-cc-pVDZ) the complexes formed by nitric acid with one, two and three water molecules.[5] They have found that complexes are stabilized by hydrogen bonds: the acid being the donor with a first water molecule, and further H bonds are formed between successive water molecules. Scott *et al.* performed MP2/6-311++G(2d,p) and B3LYP/6-311++G(2d,p) calculations to determine the optimum energies and binding energies for $HNO_3 \cdot nH_2O$ systems ($n = 1,\ldots, 4$). The first stable ion-pair configuration is obtained for a complex with $n = 4$.[6] Leopold and coworkers used Fourier transform microwave spectroscopy to characterize the gas-phase complex HNO_3–$(H_2O)_3$ in a supersonic jet. The structure was confirmed by MP2/-6-311++G(2df,2pd) calculations and it involved a nearly planar 10-membered ring with the HNO_3 proton hydrogen-bonded to the first water.[7] Note also that in a 1:3 mole ratio mixture of HNO_3 and H_2O at 298 K,[8] the percentage of dissociation is 51%, while in a 1:20 HNO_3/H_2O mixture at 278 K, 98% of the acid is dissociated.[9] More recently, Leopold summarized the nature of hydrated protons, and a parallel discussion of structural aspects of acid–water complexes was presented.[10]

In this study, we revisit the work of Lewis *et al.*,[3] where the concentration dependence of the dissociation of nitric acid in

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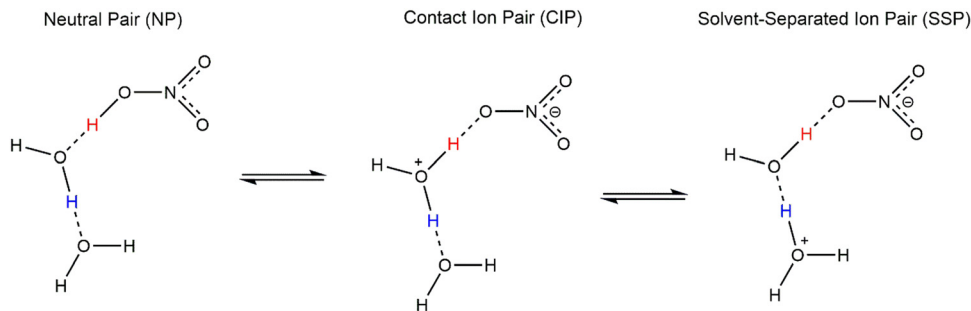
Fig. 1 Schematic of consecutive proton transfer NP → CIP → SSP for HNO$_3$ acid dissociation.[2]

water is investigated based on a combination of experiments and theoretical electronic–structure-based molecular dynamics (MD) simulations.

The nitric acid dissociation process steps are shown in Fig. 1, where NP denotes a neutral pair, CIP refers to a contact ion pair, and SSP indicates a solvent-separated ion pair.

Lewis *et al.* studied aqueous nitric acid solutions with concentrations of up to 6 M.[3] We now investigate even more concentrated solutions (up to 50 mol%, 20 M), paying special attention to the use of NMR spectroscopy as a diagnostic tool. During these investigations, apparent relationships were revealed between the concentrations of the solutions and both their ^{1}H NMR chemical shifts and the measured heats of mixing. To gain a deeper understanding of the molecular origin of these observations, we performed quantum chemical calculations on small microsolvated HNO$_3$–water clusters with molar ratios covering the concentration range under scrutiny. Without proposing such simple clusters to be faithful representatives of the actual solutions, we now report remarkable similarities in the computed and observed trends for both.

Solvent–solute interactions and their impact on the NMR chemical shifts of the functional groups are well-known in NMR spectroscopy. Routine analyses can comfortably rely on empirical correlations and libraries. The dependence of these chemical shifts on the concentration of the solute can become an important component of the chemical shifts, especially for nuclei with a narrow chemical shift range such as ^{1}H. NMR spectroscopy can be used to extract quantitative information along with molecular structural information. Furthermore, carefully constructed multi-dimensional and/or multi-pulse sequences can reveal the nature and the rate of the local atomic, molecular and spin-exchange interactions. When these factors are combined, NMR spectroscopy becomes an attractive tool for operando methods.[11,12] When operando spectroscopy is applied under batch conditions, the solute concentrations are subject to change as a function of time. This change, if expected to occur over a large concentration range, can lead to altering the chemical shifts of other molecules. One of the motivations for this study is to lay the groundwork for demonstrating the effect of the solute concentration on the chemical shifts in ^{1}H NMR spectroscopy, when the nuclear spins are in rapid exchange in the chemical environment such that only a single resonance can be obtained in the NMR timeframe.

The second motivation is to look for the reasons through understanding the local structural environment with the help of estimating NMR shifts using first-principles methods. Furthermore, it is important to establish the connection between the NMR chemical shifts and the heats of solvation and heats of dissolution measured through calorimetry.[13,14]

Methodology

Experimental

^{1}H-NMR measurements were carried out using a Magritek Spinsolve 80 spectrometer. The data were visualized using the software of Magritek Spinsolve 80. For preparing the mixtures, pure water (H$_2$O), heavy water (D$_2$O) and high-purity nitric acid (HNO$_3$, 98%) were used. Mixtures were prepared just before the measurement at constant temperatures (25 °C and 40 °C). Since the mixing of nitric acid and water is significantly exothermic, the mixtures were kept at rest after mixing until they reached the initial temperature. The molar compositions of the mixtures were selected intentionally in order to match the composition of the water–nitric acid complexes with water to nitric acid ratios in the range of 1 to 8. The ^{1}H-NMR chemical shifts of the nitric acid–water mixtures were measured at constant temperatures (25 °C and 40 °C) as a function of composition. Measurements were performed utilizing the proton protocol, and chemical shifts were referenced to the proton chemical shift of tetramethylsilane (TMS). The ^{1}H frequency is 80 MHz in the magnetic field of the benchtop NMR spectrometer. Four scans were sufficient to obtain very good S/N ratios (S/N = signal/noise). A coffee-cup calorimeter was designed and used to determine the adiabatic heat of mixing. A thermally insulated chamber was loaded with the primary component (water or concentrated nitric acid), and its temperature stabilization was monitored with a thermometer with a 0.2 °C sensitivity. The secondary component, equilibrated at the same temperature, was introduced into the chamber. This chamber was carefully sealed and isolated to avoid the evaporative losses of mass and thermal energy. A thermometer was used to measure the generated thermal energy. The maximum temperature was recorded. The heat capacities of the individual components were used to determine excess heat upon mixing. The sensitivity of the mass measurements was within 1 mg, and temperature measurements

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were within 0.2 °C, resulting in an estimated error of ∼1 mJ of thermal energy.

Quantum mechanics (QM)

The equilibrium geometries and vibrational normal modes of hydrated nitric acid clusters and reference molecules were obtained using the PBE functional[15] in combination with Pople's 6-311+G(2d,p) basis set. Conformational analysis was performed in order to find the most stable conformer of each cluster (only results for the lowest conformer of each cluster are reported). The geometries were fully optimized, followed by the calculation of the harmonic vibrational frequencies at that level. The vibrational frequencies were used to characterize the minimum nature of the optimized structures and to evaluate thermodynamic corrections to enthalpies (at 1 atm and 323.15 K). Magnetic shielding $\sigma(i)$ was computed for the most stable structures at the PBE/6-311+G(2d,p) level as well as at the B3LYP/6-311+G(2d,p)//PBE/6-311+G(2d,p) level. To account for the bulk solvation effects, a continuum solvation model based on density (SMD)[16] was used for geometry optimization and NMR calculations. The molecular volumes of the nitric acid clusters were obtained using the PBE/6-311+G(2d,p) methodology.

Nitric acid clusters and selected water clusters [H_2O, $(H_2O)_3$, and $(H_2O)_4$ as models for pure water], as well as $(H_3O^+)(H_2O)_3$ as a model for a free hydrated proton were calculated. Due to the expected rapid exchange of all protons, all of the protons are taken into account for the average chemical shift calculations of nitric acid clusters.

The ^1H chemical shifts $\delta(i)$ of the clusters are calculated using eqn (1):

$$\delta(i) = \sigma(TMS) - \sigma(i), \qquad (1)$$

where $\sigma(TMS) = 31.46$ and 31.93 ppm at the PBE/6-311+G(2d,p) and B3LYP6-311+G(2d,p)/levels, respectively.

The enthalpy of mixing is calculated using eqn (2):

$$HNO_3 + (x/8)(H_2O)_8 \rightarrow HNO_3(H_2O)_x \quad (x = 1, 2, \ldots, 8).$$

The enthalpy of mixing $= H_{HNO_3(H_2O)_x} - H_{HNO_3} - H_{(x/8)(H_2O)_8}$
$$(2)$$

Molecular dynamics (MD)

Periodic DFT calculations were performed using version 22.11 of the plane wave CASTEP code,[17] which employs the GIPAW[18] algorithm to reconstruct the all-electron wave function in the presence of a magnetic field. The generalized gradient approximation (GGA) PBE[19] functional was employed with D3-BJ dispersion corrections.[20] Wave functions were expanded as plane waves with a kinetic energy smaller than the cutoff energy of 60 Ry (816 eV). Integrals over the first Brillouin zone were performed using a Monkhorst–Pack[21] grid with a k-point spacing of 0.1 Å^{-1}. Molecular dynamics trajectories were computed in the NVE and NVT ensemble using the Langevin thermostat,[22–24] a time step of 1 fs (0.5 for the $x = 0.50$ solution at 450 K), and further settings specified in the ESI.† Isotropic magnetic

Table 1 Experimental ^1H-NMR chemical shifts (in ppm) and heat of mixing (kcal mol^{-1})

| Formula | Mole fraction x_{HNO_3} | Chemical shift, δ, (ppm) | | | | Heat of mixing (kcal mol^{-1}) |
| | | H_2O–HNO_3 | | D_2O–HNO_3 | | |
		25 °C	40 °C	25 °C	40 °C	
H_2O	0.00	4.77	4.77	4.77^a	4.77^a	n/a
$HNO_3(H_2O)_8$	0.11	6.47	6.28	6.68	6.77	−4.20
$HNO_3(H_2O)_7$	0.13	6.65	6.53	6.83	6.89	−4.38
$HNO_3(H_2O)_6$	0.14	6.91	6.73	7.17	7.18	−4.16
$HNO_3(H_2O)_5$	0.17	7.16	6.99	7.44	7.41	−4.18
$HNO_3(H_2O)_4$	0.20	7.44	7.35	7.81	7.71	−4.03
$HNO_3(H_2O)_3$	0.25	7.81	7.82	8.20	8.26	−3.39
$HNO_3(H_2O)_2$	0.33	8.27	8.16	8.55	8.58	−3.02
$HNO_3(H_2O)$	0.50	8.84	8.85	8.99	8.95	−2.17
HNO_3	1.00	11.59	11.53	11.53	11.53	n/a

^{a} ^1H signal from H_2O impurities in D_2O.

shielding was computed for snapshots taken at regular intervals from the trajectories, using the same level and settings as the MD. ^1H shielding was averaged over all H atoms in each frame and over sufficient snapshots to ensure convergence (see ESI†) and converted to chemical shifts according to eqn (1) [where $\sigma(TMS)$ and $\sigma(i)$ denote the respective ensemble averages]. The value for TMS was obtained from an MD simulation of a single TMS molecule in an otherwise empty box with the same settings as above; the resulting averaged shielding values were $\sigma(TMS) = 30.84$ and 30.81 ppm at 350 K and 450 K, respectively.

Results and discussion

Experimental results

^1H-NMR chemical shifts. The ^1H chemical shift in liquid H_2O is typically observed at approximately 4.8 ppm around 300 K. The deshielding relative to the value of free H_2O in the gas phase ($\delta = 2.72$ ppm extrapolated to zero pressure)[25] is primarily due to hydrogen bonding.[26] The chemical shifts of water and heavy water were referenced at 4.77 ppm for the measurements. The data obtained from the ^1H-NMR chemical shift measurements are given in Table 1.

Effect of composition. As can be seen from Table 1, the signals of the nitric acid–water mixtures fall in between those of pure water and nitric acid, and the chemical shift increases with increasing acid concentration.

Effect of temperature. The chemical shifts of the resonance signals in the proton NMR spectrum of many acids and alcohols are slightly temperature dependent, arguably due to changes in vibrational averaging in the R–OH···O(H)R moieties with temperature. However, in the nitric acid–water case, there are no long-lived hydrogen bonds like that due to the strong acidity and ionization of the nitric acid, which is expected to afford hydronium ions and rapid diffusion of the protons through the well-known Grotthuss-type mechanism (see the MD results below). Also, the measured chemical shifts were very similar for each mixture composition with the same binary mixture. Therefore, it appears that the temperature increase

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Table 2 Calculated (PBE/6-311+G(2d,p), B3LYP/6-311+G(2d,p), SMD = H_2O) ^1H chemical shifts (ppm) of pure water clusters

Formula	δ_{calc} (ppm) PBE/ 6-311+G(2d,p)	δ_{calc} (ppm) B3LYP/ 6-311+G(2d,p)
H_2O	1.39	2.05
$(H_2O)_3$	4.81	5.44
$(H_2O)_4$	5.92	6.44
$(H_2O)_8$	4.92	5.48
$(H_3O^+)(H_2O)_3$	12.86	13.50

Table 3 Composition of the simulated nitric acid clusters (PBE/6-311+G(2d,p), SMD = H_2O)

	Formula	Mole fraction x_{HNO_3}	Volume (cm^3 mol^{-1})	Molarity (M)
1	$HNO_3(H_2O)$	0.50	50.0	20.0
2	$NO_3^-(H_2O)(H_3O)^+$	0.33	66.5	15.0
3	$NO_3^-(H_2O)_2(H_3O)^+$	0.25	80.0	12.5
4	$NO_3^-(H_2O)_3(H_3O)^+$	0.20	103.5	9.7
5	$NO_3^-(H_2O)_4(H_3O)^+$	0.17	125.7	8.0
6	$NO_3^-(H_2O)_5(H_3O)^+$	0.14	121.8	8.2
7	$NO_3^-(H_2O)_6(H_3O)^+$	0.13	148.2	6.7
8	$NO_3^-(H_2O)_7(H_3O)^+$	0.11	144.7	6.9

from 25 to 40 °C had no important effect on the measured chemical shift values among the nitric acid–water mixtures.

Heats of mixing. Nitric acid is ubiquitous in chemical processing industries, with end uses ranging from agriculture to explosives. The most important interaction that nitric acid experiences is with water, starting from the manufacturing process, where the solvation of nitrogen dioxide in water produces nitric acid and nitric oxide.

Aqueous solutions of nitric acid have a maximum boiling azeotrope at 69% HNO_3. Nitric acid undergoes exothermic dilution, which indicates that interactions lead to energy release at the molecular scale. A detailed understanding of the local molecular structure, leading to the energy release upon mixing, is important for both manufacturing and using nitric acid.

The composition-dependent heats of mixing values measured in this work (included in Table 1) compare well with the data reported in the literature.[27]

Both the measured ^1H NMR chemical shifts and the heats of mixing of the solutions show a monotonous trend with the concentrations. To gain more insights into the intermolecular interactions and structural motifs that could underpin these observations, we performed quantum chemical computations for the selected model systems, which are discussed below.

Quantum mechanical results. The first set of models are discrete nitric acid–water clusters, $HNO_3(H_2O)_n$, with the number of water molecules chosen to match the experimental concentrations (n = 1–8). Without implying the resulting static minima to be faithful representations of dynamic ensembles of the solutions, we were interested in the preferences for the structural motifs shown in Fig. 1 in such clusters and the effect on their computed ^1H chemical shifts and water binding energies. With these chemical shifts in mind, we first performed benchmark calculations for selected water clusters to identify a suitable DFT exchange–correlation functional for this property. Then, we used this level to optimize the nitric acid–water clusters. Finally, in an attempt to bridge the results for such static clusters and the real solutions, we performed first-principles molecular dynamics simulations of the two systems under periodic boundary conditions.

Water clusters: benchmark analysis for ^1H-NMR chemical shifts

The calculated average ^1H chemical shifts for the small water clusters are reported in Table 2, and the geometries are shown in Fig. S1 in the ESI.† $\delta(^1H)$ values are higher (more deshielded) at the B3LYP level than at the PBE level. For the trimeric and tetrameric clusters, which are arguably better models for the

bulk than a single molecule, the PBE results are in better agreement with the experimental results for the pure liquid (Table 1) than those at the B3LYP level. Therefore, there does not seem to be an advantage of using B3LYP (probably the more widely used functional for NMR computations) over PBE. In the following
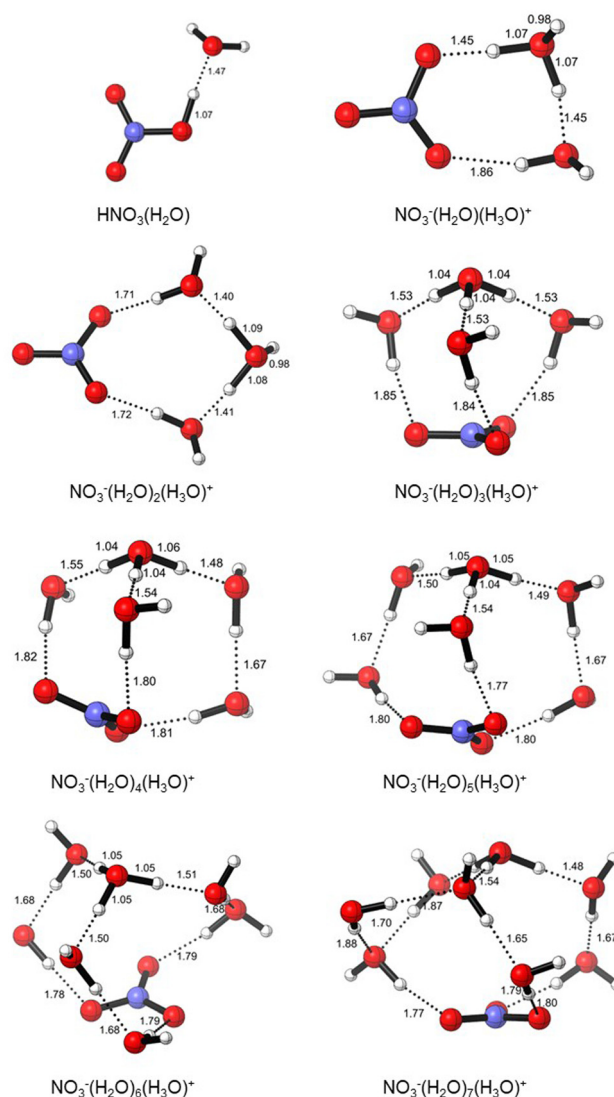

Fig. 2 Structures of $HNO_3(H_2O)_n$ (n = 1) and $NO_3^-(H_2O)_m(H_3O)^+$ (m = 2–7) clusters (PBE/6-311+G(2d,p), SMD = H_2O).

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Table 4 Calculated and experimental average chemical shifts (ppm) of $HNO_3(H_2O)_n$ (n = 1), $NO_3^-(H_2O)_m(H_3O)^+$ (m = 2–7) clusters (PBE/6-311+G(2d,p), SMD = H_2O)

	Formula	Calculated chemical shifts δ (ppm)	Experimentally measured chemical shifts δ (ppm)	$\Delta\delta$ (ppm)
1	$HNO_3(H_2O)$	8.32	8.7	0.38
2	$NO_3^-(H_2O)(H_3O)^+$	8.74	8.13	−0.61
3	$NO_3^-(H_2O)_2(H_3O)^+$	8.12	7.72	−0.40
4	$NO_3^-(H_2O)_3(H_3O)^+$	7.74	7.45	−0.29
5	$NO_3^-(H_2O)_4(H_3O)^+$	7.18	7.12	−0.06
6	$NO_3^-(H_2O)_5(H_3O)^+$	7.07	6.83	−0.24
7	$NO_3^-(H_2O)_6(H_3O)^+$	6.75	6.64	−0.11
8	$NO_3^-(H_2O)_7(H_3O)^+$	6.62	6.45	−0.17

sections, we will discuss the results obtained with the latter functional.

Nitric acid–water clusters

The initial structures of the microsolvated clusters $HNO_3(H_2O)_n$ (n = 1, 2) and $NO_3^-(H_2O)_m(H_3O)^+$ (m = 2–3) were taken from the work of Gutberlet and coworkers, which is based on the aggregation-induced dissociation of $HCl(H_2O)_4$.[28] In this context, we used DFT calculations in order to understand the behavior of nitric acid in water as its mole fraction varies from 0.11 to 0.50. The compositions of modelled nitric acid clusters are given in Table 3, and their electronic and zero-point energies are given in Table S1 (ESI†). We found that microsolvation with a single water molecule maintains a neutral pair ($HNO_3(H_2O)$), which ionizes upon the addition of a second water molecule, resulting in a contact ion pair (cf. Fig. 1). Additional water molecules afford solvent-separated ion pairs ($NO_3^-(H_2O)_m(H_3O)^+$ (m = 2–7)), and the modelled clusters are shown in Fig. 2.[2] Spontaneous ionization of strong acids by a small number of solvent molecules is well known, and there is a loose correlation between acid pK_a and the number of water molecules required for this ionization.[29] The observation that only two water molecules are needed to ionize HNO_3 is in line with its very low pK_a. Note that these calculations were performed on a polarizable continuum to model bulk solvation in aqueous solutions. For comparison with literature data, which usually does not consider such bulk solvation, we also modeled the same clusters in the gaseous phase and noticed that the ion pair starts to form at n = 4 (see Fig. S2, ESI†). This finding is similar to one of Xanteas and coworkers (MP2/aug-cc-pVDZ), who predicted the appearance of ion-pair configurations in the gas phase for n = 4 or higher.[4] Similarly, Scott et al. obtained the first stable ion-pair configuration for a complex with n = 4 (MP2/6-311++G(2d,p) and B3LYP/6-311++G(2d,p)).[6] This good agreement provides further validation of our chosen level, PBE/6-311+G(2d,p).

When the polarity of the medium is taken into account, in the $HNO_3(H_2O)$ cluster corresponding to x = 0.50, the acidic proton is on NO_3^-. As more water is added, the proton moves towards H_2O, and H_3O^+ starts to form. In $HNO_3(H_2O)_2$, H_3O^+ is equidistant to NO_3^-; in $HNO_3(H_2O)_3$, NO_3^- is completely separated (1.71 Å) from the protonated water cluster. As the

solution becomes more dilute, the proton sticks to H_2O and the hydronium ion (H_3O^+) is surrounded by other H_2O molecules, which in turn stabilizes the NO_3^- anion.

In the following, we will use the results obtained in the continuum (including the SMD-optimized structures) for consistency with the experimental conditions of bulk solutions. The calculated δ values are collected in Table 4. They follow the trend in the observed shifts remarkably well, and the resulting discrepancies $\Delta\delta$ ($\delta_{expt} - \delta_{calcd}$) are in the range between −0.61 and 0.38 ($-0.61 < \Delta\delta < 0.38$) ppm. Graphical comparisons between experimental ^{1}H NMR chemical shifts and the estimated values from DFT, as a function of mole fractions, are shown in Fig. S5 (ESI†). Arguably, as the number of water molecules in the clusters increases, the computed trend is to some extent due to the increased weight of the (intact) water sites in the total average.

Heat of mixing (experimental and calculated)

We also calculated (PBE/6-311+G(2d,p), 323.15 K, SMD = H_2O) the enthalpies of mixing through the enthalpies of formation of our microsolvated clusters from a single HNO_3 and a water octamer by using eqn (2) (Table S2, ESI†). These estimations were closer to the measured values at high nitric acid concentrations. At higher water concentrations, the discrepancy between the measured and estimated values increased. A perfect agreement between the experiment and the results for such a microsolvated model cluster was not expected. However, the general trend, i.e. the exothermicity increases with the water content, is well captured qualitatively. Part of this discrepancy can also be attributed to the peculiarities that continue to be discovered about the structure of water, especially at the interfaces.[30–33]

The correlation between the enthalpy of mixing (kcal mol^{-1}) and the average chemical shift (ppm) for the $(HNO_3)_n(H_2O)$ clusters is fair (Fig. S3, R^2 = 0.91, ESI†), while the same correlation with the experimental data is also within acceptable limits (Fig. S4, R^2 = 0.90, ESI†). With limited data at hand, the relationship between enthalpies of mixing and chemical shifts cannot be generalized at this stage. The NMR chemical shifts reflect the local structures at equilibrium. It is important to conduct further studies to determine whether there is a fundamental basis for the correlation between NMR chemical shift data and the corresponding heats of mixing values.

Simulation of bulk solutions under periodic boundary conditions

To complement the molecular cluster investigation, we performed simulations for bulk solutions under periodic boundary conditions (Fig. S6–S13, ESI†). We explored three different systems, each containing varying amounts of nitric acid. These systems included a pure water solution (x = 0.00), a nitric acid solution with a molecular fraction of x = 0.19, and a nitric acid solution with a molecular fraction of x = 0.50 (see Fig. 3). We specifically chose these solutions to cover the entire range of experimental results, from x = 0.00 to x = 0.50. To limit the computational effort, we started with a small box containing 32

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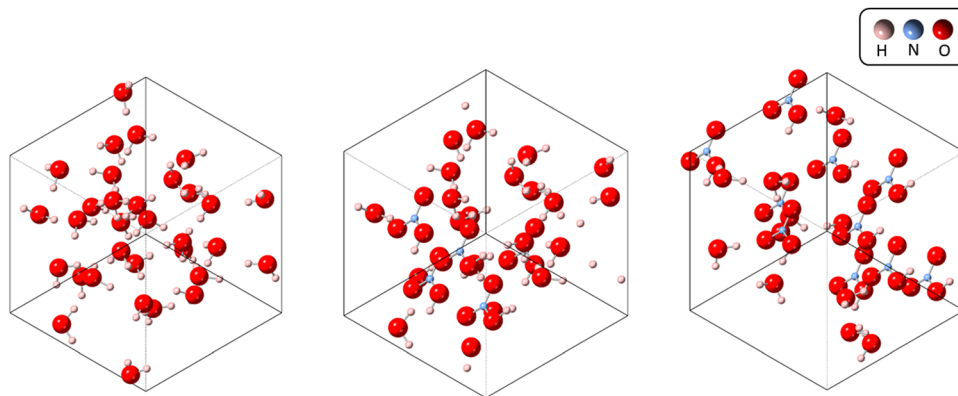
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Fig. 3 Unit cells for different solutions. From right to left: pure water, molecular fraction of 0.19, 50/50 solution of nitric acid.

water molecules (akin to that used in early CPMD studies of the properties of liquid water)[34,35] and replaced an appropriate number of water molecules with HNO_3 molecules to maintain the proper density within the same box dimensions. Because PBE (like the BLYP functional used more commonly) tends to overstructure the pure liquid[36] and since this overstructuring is improved by the inclusion of dispersion corrections,[37] we used the PBE-D3 variant in all simulations.

We started by simulating pure water and nitric acid solutions at 300 K, which corresponds to one of the experimental temperatures. However, these simulations did not properly describe the liquid-like behaviour of our system. This was validated through the radial distribution functions (RDFs) and the root mean square deviations of atomic positions (RMSDs) (see Fig. 4, and a more detailed description is provided in the ESI†). In our simulations, it appears that the solutions freeze after the first 1.5 ps, which is a physically incorrect representation of a solution.

Although frozen, we still computed the chemical shifts for all three solutions. To this end, we extracted 20 snapshots from the MD trajectory and computed the NMR shielding(the computational details for the calculation of the magnetic properties can be found in the ESI†). Magnetic shielding for a single tetramethylsilane (TMS) system computed at the same level of theory provides a reference for chemical shielding. The resulting ^{1}H chemical shifts are collected in Table 5.

Overall, the agreement with the experiment is fair, and affords an average error of ~ 1.2 ppm. It should be noted that

the experimental trend of larger deshielding with increasing acid content is well reproduced and that the error (overestimation of the chemical shift) is rather systematic. Thus, if the reference used is not TMS, but the pure water system the agreement is significantly improved (see Table S6 in the ESI†). This is interesting, as it may suggest that the key interactions arising from the addition of nitric acid in the solution are well captured. Moreover, this sheds light on said interactions, which must be short-ranged as the solution behaves like a solid and the molecules only move about their local position without diffusion through the liquid. Therefore, long-distance interactions arising from the molecules freely moving in solution, which are not accounted for in these simulations, do not seem to be the key factors influencing the chemical shift.

One of the main issues that needs to be addressed is that the simulation does not behave as a solution, but as a solid. In fact, even though the chemical shift can be predicted to a high degree of accuracy when pure water is used as a reference, this is not entirely satisfactory as it only proves that the change introduced by nitric acid is reproduced, but not the behaviour of the solution as a whole. To address this issue, we followed the work of Xantheas and performed MD simulations at a higher temperature (450 K). The oxygen–oxygen RDF at this temperature shows a totally different behaviour, corresponding to a less-structured solution. As reported in ref. 38, a higher temperature allows for a correct description of the second coordination sphere (see the maximum at $r \approx 4.2$ Å on the
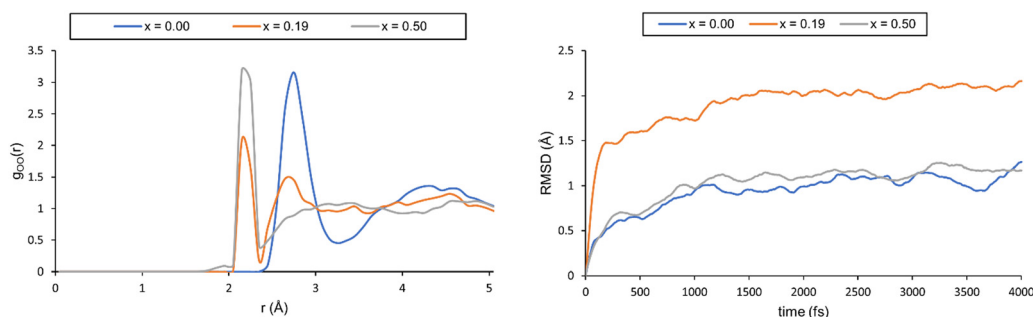

Fig. 4 Left: The oxygen–oxygen RDF for different systems computed at 300 K. Right: Plot of the RMSD for the three solutions.

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Table 5 Predicted and experimental ^{1}H chemical shifts (in ppm relative to TMS) for the three nitric acid solutions with mole fraction x. The last column shows the difference between the predicted and experimental chemical shifts

x	δ (CASTEP, 300 K)	δ (Exp., 300 K)	$\Delta\delta$
0.00	6.1	4.8	1.3
0.19	8.2	7.4	0.8
0.50	10.4	8.8	1.6

Table 6 Predicted and experimental ^{1}H chemical shifts (in ppm relative to TMS) for the three nitric acid solutions with molecular fractions of 0.00, 0.19 and 0.50. The last column reports the difference between the two

x	δ (CASTEP, 450 K)	δ (Exp., 300 K)	$\Delta\delta$
0.00	4.8	4.8	0.0
0.19	7.4	7.4	0.0
0.50	8.9	8.8	0.1

left-hand side of Fig. 5), whereas the probability associated with the first coordination sphere is underestimated (see the maximum at $r \approx 2.9$ Å). It should be noted that the shallow well depth between both peaks observed experimentally (indicative of a dynamic exchange between molecules in the first and second solvation spheres) is well reproduced at the higher simulation temperature, whereas the simulation at 300 K has a much deeper well. The RMSD at 450 K also shows a behaviour in line with that of a solution and not with that of a solid. In fact, its value keeps on increasing and does not plateau even after 10 ps (see the right-hand side of Fig. 5).

Overall, from the RDF and RMSD analyses, we can conclude that the simulation at 450 K behaves as a proper solution. We have, therefore, repeated the simulations of the two nitric acid solutions at this high temperature. While these systems tend to be more mobile at higher T than at 300 K, they do not attain truly diffusive states (which would probably require much longer simulation times); see the RMSDs in the ESI† (see Fig. S14). Nevertheless, in terms of NMR properties, the increased mobility has a strong beneficial effect. The experimental data (at 300 K) are reproduced almost quantitatively (see $\Delta\delta$ values in Table 6 and Fig. S15, ESI†).

This excellent agreement may, to some extent, be fortuitous, given the essentially frozen nature of the solutions in the simulations. With a large proportion of nitrate and hydronium ions, however, diffusion in these concentrated nitric acid solutions may share some characteristics with those in ionic liquids. This is frequently described as a random walk-hopping process between ion cages.[39] If the lifetime of such ion cages exceeds the duration of individual hopping events, dynamic averaging of NMR properties over a representative, instantaneous set of such ion cages may indeed capture key features, with further (minor) modulations expected through

changes of these properties during hopping. As mentioned, proper modelling of this aspect would require larger boxes and, particularly, much longer simulation times.

In the dynamic (albeit ''frozen'') ensembles of nitric acid solutions, NPs, CIPs and SSPs are encountered to various extents. Fig. 6 shows representative snapshots from the simulations of the two systems (at higher T), where at lower concentrations, SSPs are prevalent (shown as isolated nitrate ions, labeled A), with a smaller population of CIPs and NPs (shown as intact HNO$_3$ moieties, labelled B and C, respectively); see Fig. 6a. At higher concentrations, these populations are reversed as shown in Fig. 6b. There is no indication of the presence of discrete HNO$_3$ dimers (akin to the doubly bridged motif well known for carboxylic acids) in these simulations.

These structural features can be quantified by analysing the relevant RDFs (see ESI† for details). Unfortunately, no energetic quantities could be extracted from these relatively short MD simulations, which could be related to the heats of mixing. Again, much longer simulations (including those for pure HNO$_3$) are required for this purpose.

Conclusions

In this study, insights into the dissociation of nitric acid in water at the molecular level were deduced from ^{1}H NMR, DFT calculations and molecular dynamics simulations. The dependence of ^{1}H NMR chemical shifts on the concentration of the solute has been experimentally measured, and molecular (static) clusters bearing the formula HNO$_3$(H$_2$O)$_x$ (x = 1, 2, ..., 8) and corresponding to the experimental concentrations have been modeled successfully with PBE/6-311+G(2d,p) in conjunction with the SMD solvation model employing the parameters of H$_2$O. Except for the monohydrated complex (x = 1), all
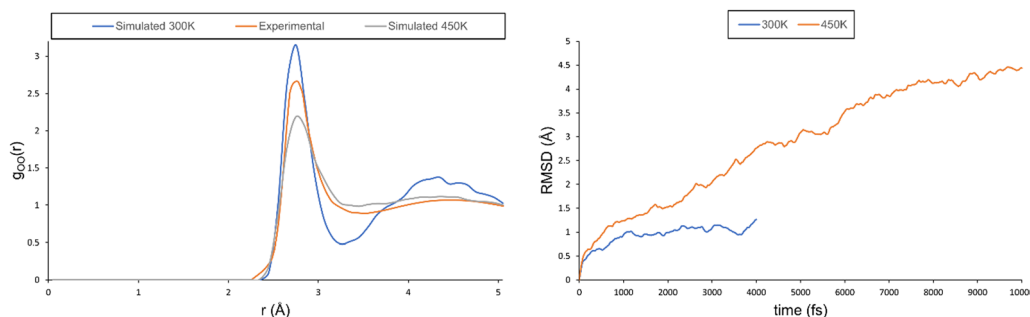

Fig. 5 Left: Predicted and experimental oxygen–oxygen RDF for the pure water system (x = 0.00). Right: RMSD plot for the pure water system at 300 and 450 K.
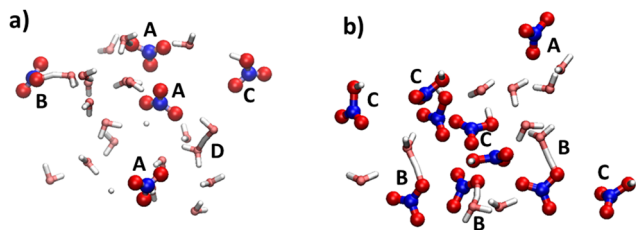
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Fig. 6 Snapshots from nitric acid simulations with (a) $x = 0.19$ and (b) $x = 0.50$ (at $T = 450$ K); structural features are labelled (see text). Note the instantaneous occurrence of an $H_5O_3^+$ ion in (a) (labelled D).

microsolvated clusters have been optimized in a dielectric continuum to contact or solvent-separate ion pairs with discrete NO_3^- and H_3O^+ ions. In addition to a pure water reference, MD simulations have been performed for two nitric acid solutions with mole fractions of 0.19 and 0.50 (PBE-D3 functional, $T = 300$ K and 450 K). Despite using fairly small periodic boxes and short simulation times, the ^1H chemical shifts averaged over the trajectories at a higher temperature ($T = 450$ K) reproduce the observed change in chemical shift in this concentration range very well. As expected, and in line with the molecular cluster models, a much higher degree of dissociation is found at a lower concentration (mole fraction: 0.19) than at a higher one (mole fraction: 0.5), where the majority of nitric acid is present in the form of intact HNO_3 molecules.

This study has also provided insights into the relationship between the experimentally measured heats of mixing and the chemical shifts of the solutions, as well as between the calculated enthalpies of reaction and the average chemical shifts. Additional data are necessary for a conclusive interpretation of these findings.

Author contributions

The three first authors and the three corresponding authors contributed equally.

Conflicts of interest

There are no conflicts to declare.

Acknowledgements

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