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A fully dynamical description of time-resolved resonant inelastic X-ray scattering of pyrazine†

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Recent advancements in ultrashort and intense X-ray sources have enabled the utilisation of resonant inelastic X-ray scattering (RIXS) as a probing technique for monitoring photoinduced dynamics in molecular systems. To account for dynamic phenomena like non-adiabatic transitions across the relevant electronic state manifold, a time-dependent framework is crucial. Here, we introduce a fully time-dependent approach for calculating transient RIXS spectra using wavepacket dynamics simulations, alongside an explicit treatment of the X-ray probe pulse that surpasses Kramers–Heisenberg–Dirac constraints. Our analysis of pyrazine at the nitrogen K-edge underscores the importance of considering nuclear motion effects in all electronic states involved in the transient RIXS process. As a result, we propose a numerically exact approach to computationally support and predict cutting-edge time-resolved RIXS experiments.

1 Introduction

Resonant inelastic X-ray scattering (RIXS)^{1,2} is a Raman spectroscopy technique that exploits X-ray resonances to create an intermediate core-excited state, followed by a spontaneous photon emission that propels the quantum system to a lower excited state. The energy difference between incident and emitted X-ray photon provides an excitation spectrum that is not only element-specific but also specific to the particular chemical environment of an atom. Moreover, RIXS can populate final excited states that cannot be directly probed by conventional one-photon absorption spectroscopy due to restrictions imposed by dipole selection rules.^{3–6} A complicating factor in this process is the role of vibronic coupling between core-excited states, which can facilitate transitions that are otherwise forbidden due to symmetry restrictions. This is particularly relevant for molecules with equivalent atoms, as they possess delocalised core orbitals and, consequently, energetically degenerate core-excited states. Vibronic coupling may induce dynamical distortions and a loss of symmetry, resulting in a localisation of the core excitations.^{1,3,7} While environmental factors such as solvent interactions or temperature may also cause structural heterogeneity, already resulting in a localised configuration in the ground state, the motional effects arising from non-adiabatic

core-excited state dynamics can be distinctly determined by adjusting the excitation energy in RIXS measurements, thereby controlling the scattering time and the evolution of nuclear dynamics.^{8–10}

In the condensed phase, where solids and solvents prohibit measurement of UV absorption spectra beyond $\lesssim 9$ eV, RIXS allows accessing spectra up to energies in the extreme ultraviolet, *i.e.* inner-valence excitations.¹¹ As the spectral resolution is not constrained by the core-hole lifetime broadening of the initial core-excitation, transition bands in RIXS spectra can exhibit vibrational substructure, providing information on the underlying nuclear dynamics and corresponding potential energy surfaces.^{10,12–15} RIXS with hard X-rays usually targets core-excited final states because of the very low yield of valence-excited final states (resulting from so-called valence-to-core transitions of electrons that fill the core-hole). RIXS studies with soft X-rays generally target final states that are valence- or vibrationally excited (or of other nature such as magnons). The versatility of RIXS to valence-excited final states is demonstrated by its application in various studies, encompassing molecules,^{16–18} liquids,^{19–22} and solids.^{23–25}

Initially enabled by synchrotron radiation X-ray sources with increased spectral brightness,²⁶ RIXS experienced a further advancement with the emergence of X-ray free-electron lasers (XFELs).^{27–30} This development facilitated the extension of RIXS to time-resolved studies,^{31–33} exploiting nonlinear processes in optical pump/RIXS probe spectroscopy with applications in fields ranging from condensed matter physics³⁴ to molecular chemistry.¹⁸ Within the present work, we focus on chemical applications where recent successful inquiries into photodissociation dynamics,^{35–37} charge-transfer excitations,^{38–40} and excited-state proton transfer⁴¹ underscore the potential of time-resolved RIXS as a spectroscopic

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tool that provides element-specific Raman spectra of transient species on ultrafast timescales from vibrational frequencies to the vacuum ultraviolet in the condensed phase.

The complex nature of the underlying processes necessitates the utilisation of advanced computational techniques to decode mechanistic information from experimental data, aid in their analysis, and even forecast complicated spectral features. Consequently, a range of methods,⁴² both time-independent and time-dependent, have emerged to describe (steady-state) RIXS spectra for molecules where conventional time-independent approaches typically rely on the established Kramers–Heisenberg–Dirac formula employing an eigenstate representation of the system in the frequency domain.^{43,44} Conversely, time-dependent methods based on wavepacket propagation compute the scattering amplitude by the time-dependent overlap between initial and final vibronic states providing an equivalent time domain approach under steady-state conditions.^{45,46}

Previous *in silico* time-resolved RIXS studies of molecules considered pump-induced states as isolated quasi-static snapshots, for which steady-state RIXS spectra were simulated.^{36,37,40,47} This approach enabled identification of contributions from the considered chemical species to the overall RIXS spectrum in a simplified manner, neglecting real-time motion effects. However, when a molecule is impulsively excited, the created wavepacket will evolve in time depending on the shape of the corresponding potential energy surfaces. These dynamics and interplay between the resulting population transfers can significantly impact the nuclear motion and therefore the overall experimental signal measured. Hence, for a description that incorporates nuclear motion effects arising from both the pump-induced valence and intermediate core-excited state dynamics, as well as from dynamics of the final ground and valence-excited states, a time-dependent framework is required that is able to describe non-adiabatic phenomena.

In this work, we present a full quantum dynamical treatment of femtosecond (fs-) RIXS spectroscopy employing the multiconfiguration time-dependent Hartree (MCTDH) method which extends our previous work on steady-state RIXS simulations.⁴⁸ For this purpose, we utilise a vibronic coupling Hamiltonian encompassing all electronic states involved in the fs-RIXS process as well as an explicit description of the coherent X-ray probe pulse. We conduct calculations of transient RIXS spectra at the nitrogen K-edge of pyrazine. Pyrazine is chosen as an interesting likewise complex benchmark system due to its pronounced non-adiabatic behavior in both the valence and core excited state manifolds. Through explicit assignment of specific spectral features to nuclear motion, we highlight the significance of adopting a comprehensive time-domain approach to achieve an accurate description of time-resolved RIXS signals including all dynamical dimensions.

2 Methodology

2.1 Quantum dynamics

The time-dependent Schrödinger equation for the nuclear dynamics is solved employing the multi-layer (ML-) MCTDH^{49–51}

wavepacket propagation method. The total MCTDH^{52,53} wavefunction *ansatz* reads

$$\Psi(\mathbf{Q}, t) = \sum_{j_1 \dots j_f} A_{j_1 \dots j_f}(t) \prod_{i=1}^f \varphi_{j_i}(Q_i, t) \quad (1)$$

where $A_{j_1 \dots j_f}$ are expansion coefficients of the low-dimensional single particle functions (SPFs) φ_{j_i} . Using a linear combinations of time-independent primitive basis functions χ_{r_i} , the time-dependent SPFs are themselves represented by

$$\varphi_{j_i}(Q_i, t) = \sum_{r_i} c_{r_i j_i}(t) \chi_{r_i}(Q_i) \quad (2)$$

providing a discrete variable representation (DVR) grid. The equations of motion are finally derived by applying the Dirac–Frenkel variational principle.^{54,55}

Within ML-MCTDH, the SPFs are recursively expanded in the form of eqn (1) until the last layer of time-dependent SPFs is represented by the discrete time-independent grid. This variant of MCTDH provides an efficient tool to treat larger systems fully quantum mechanically.

2.2 Vibronic coupling Hamiltonian

Justified by the large energy gap, we completely decouple the valence- and core-excited states concerning non-adiabatic transitions. Moreover, the group approximation is employed separating both, the valence- and core-excited state manifold of pyrazine, into individual subsets of states, resulting in the subsequent matrix representation of the molecular Hamiltonian

$$\mathbf{H}_{\text{mol}} = \begin{pmatrix} \mathbf{H}_v & 0 \\ 0 & \mathbf{H}_c \end{pmatrix} \quad (3)$$

where $\mathbf{H}_v = \text{diag}(\mathbf{H}_{v_1}, \mathbf{H}_{v_2})$ and $\mathbf{H}_c = \text{diag}(\mathbf{H}_{c_1}, \mathbf{H}_{c_2})$ denote the sub-Hamiltonians acting on the valence- and core-excited state manifolds, respectively. In this model, \mathbf{H}_{v_1} contains all valence-excited states relevant for the pump-induced dynamics while \mathbf{H}_{v_2} augments the valence-excited state manifold with higher lying excited states only reached by the RIXS process. There are dipole allowed transitions from \mathbf{H}_{v_1} to both sub-Hamiltonians \mathbf{H}_{c_1} and \mathbf{H}_{c_2} where each consists of two nearly degenerate, vibronically coupled core-excited states. Other core-excited states have been neglected due to the short core-hole lifetime that suppresses internal conversion processes beyond the immediate Franck–Condon region.

In order to avoid singularities in the non-adiabatic coupling terms,^{56,57} we represent the molecular Hamiltonian \mathbf{H}_{mol} in a diabatic electronic basis such that each sub-Hamiltonian can be written as

$$\mathbf{H}_x = \hat{T}\mathbf{1} + \mathbf{W}_x, \quad x \in \{v_1, v_2, c_1, c_2\} \quad (4)$$

with the kinetic energy operator \hat{T} and the diabatic potential matrix \mathbf{W}_x . We further invoke a vibronic coupling model^{7,56,58} where the diabatic potentials are expanded as Taylor series around the Franck–Condon point

$$\mathbf{H}_x = \mathbf{H}^{(0)} + \mathbf{W}_x^{(0)} + \mathbf{W}_x^{(1)} + \mathbf{W}_x^{(2)} + \dots \quad (5)$$



where the zero-order Hamiltonian is the harmonic ground-state Hamiltonian

$$\mathbf{H}^{(0)} = \sum_i \frac{\omega_i}{2} \left(-\frac{\partial^2}{\partial Q_i^2} + Q_i^2 \right) \mathbf{1} \quad (6)$$

with ω_i representing the frequency of mode Q_i . The diabatic potential matrix up to first order is defined by

$$\mathbf{W}_x^{(\alpha\beta)}(\mathbf{Q}) = E^{(\alpha)} \delta_{\alpha\beta} + \sum_i \kappa_i^{(\alpha)} Q_i \delta_{\alpha\beta} + \sum_i \lambda_i^{(\alpha\beta)} Q_i (1 - \delta_{\alpha\beta}) \quad (7)$$

with the vertical excitation energies $E^{(\alpha)}$ to the α -th electronic state and the linear intra- and interstate coupling parameters

$$\kappa_i^{(\alpha)} = \frac{\partial \langle \Psi_\alpha | \mathbf{H}_{\text{el}} | \Psi_\alpha \rangle}{\partial Q_i} \Big|_{\mathbf{Q}=\mathbf{Q}_0} \quad (8)$$

$$\lambda_i^{(\alpha\beta)} = \frac{\partial \langle \Psi_\alpha | \mathbf{H}_{\text{el}} | \Psi_\beta \rangle}{\partial Q_i} \Big|_{\mathbf{Q}=\mathbf{Q}_0} \quad (9)$$

between state $|\alpha\rangle$ and $|\beta\rangle$. In order to include changes in the frequencies, we also include on-diagonal quadratic intrastate coupling constants $\gamma_i^{(\alpha)}$ for \mathbf{H}_{v_i} and \mathbf{H}_c representing the most relevant excited states in this investigation.

For strongly anharmonic modes the harmonic expression of the diabatic potentials are replaced by state-specific quartic or Morse potentials with on-diagonal matrix elements

$$W^{(\alpha\alpha)}(Q_i) = E^{(\alpha)} + \frac{1}{2} \left(\omega_i + \gamma_i^{(\alpha)} + \varepsilon_i^{(\alpha)} Q_i^2 \right) Q_i^2 \quad (10)$$

$$W^{(\alpha\alpha)}(Q_i) = E^{(\alpha)} + D_0^{(\alpha)} \left\{ 1 - \exp \left(-a_i^{(\alpha)} (Q_i - Q_0) \right) \right\}^2 \quad (11)$$

respectively, where $\varepsilon_i^{(\alpha)}$ denotes the quartic expansion coefficient, $D_0^{(\alpha)}$ is the state-specific dissociation energy, $a_i^{(\alpha)}$ defines the curvature of the potential, and Q_0 is the equilibrium position.

2.3 Pump-probe spectra

We use a semiclassical approach, where the full laser-driven Hamiltonian \mathbf{H} reads

$$\mathbf{H}(t) = \mathbf{H}_{\text{mol}} + \mathbf{H}_{\text{int}}(t) \quad (12)$$

with the classical light-matter interaction operator \mathbf{H}_{int} acting as a perturbation to the molecular quantum Hamiltonian \mathbf{H}_{mol} . Within the dipole and Condon approximation and assuming a single polarisation direction, the coupling to the external field is given by

$$H_{\text{int}}^{(\alpha\beta)}(t) = -\mu_{\alpha\beta} \cdot \mathcal{E}(t) \quad (13)$$

where $\mu_{\alpha\beta}$ is the transition dipole moment. The total electric field

$$\mathcal{E}(t) = \mathcal{E}_{\text{pu}}(t; t_0 = 0) + \mathcal{E}_{\text{pr}}(t; \tau) \quad (14)$$

is composed of an ultrashort δ -like pump pulse \mathcal{E}_{pu} at time $t_0 = 0$ fs triggering the valence-excited state dynamics and a second pulse \mathcal{E}_{pr} probing the induced dynamics after a specific time delay $\Delta\tau$. In particular, the initial wavepacket in the

valence-excited states is generated by a vertical projection of the ground state wavefunction at 0 K onto the excited state manifold while the probe pulse is explicitly described using a time-dependent operator.

When calculating transient X-ray absorption spectra, we also assume a δ -like probe pulse striking the system at time $\tau > 0$. This induces transitions from the valence- to the core-excited state manifold with Hamiltonians \hat{H}_v and \hat{H}_c , respectively. The absorption cross section can then be obtained by the Fourier transform

$$I_{\text{XAS}}(\omega, \tau) \propto \omega \text{Re} \int_0^\infty dt \exp(i\omega t) C(t; \tau) \quad (15)$$

of the dipole-dipole correlation function

$$C(t; \tau) = \langle \Psi_v(\tau) | e^{i\hat{H}_v(t-\tau)} \hat{\mu}_{vc} e^{i\hat{H}_c(t-\tau)} \hat{\mu}_{cv} | \Psi_v(\tau) \rangle \quad (16)$$

$$= \langle \Psi_v(t) | \hat{\mu}_{vc} | \Psi_c(t) \rangle \quad (17)$$

where Ψ_v and Ψ_c denote wavepackets in the valence- and core-state manifolds, respectively, and $\hat{\mu}_{cv}$ is the transition dipole moment operator.⁵⁹

In absorption spectroscopy, δ -pulses are conceptualised as idealisations, allowing for simultaneous interrogation of the entire spectral range. On the contrary, the RIXS process depends on narrow-band excitations to precisely define the incoming photon energy. Employing RIXS as a probe for non-stationary systems thus requires an excitation pulse that strikes a balance: it must be long enough to mitigate uncertainties in the excitation process yet short enough to achieve adequate time resolution for probing the underlying dynamics. In this work, we use Gaussian-shaped X-ray probe pulses

$$\mathcal{E}_{\text{pr}}(t; \tau) = \mathcal{A}(t - \tau) \cos(\omega_I(t - \tau)) \quad (18)$$

$$= \frac{1}{\sqrt{2\pi\sigma^2}} \exp\left(-\frac{(t - \tau)^2}{2\sigma^2}\right) \cos(\omega_I(t - \tau)) \quad (19)$$

centered at time τ with carrier frequency ω_I and temporal full width at half maximum (fwhm) duration $F_t = 2\sqrt{\ln 2}\sigma$ of the intensity profile invoking the RIXS process. Assuming no temporal overlap of the pump and probe pulse, the transient RIXS signal can be calculated using the following expression for the RIXS spectrum induced by a coherent light source⁴⁸

$$I_{\text{RIXS}}(\omega_S; \omega_I, \tau) \propto \left(|\mathcal{U}|^2 * \int_{-\infty}^\infty dt \exp(-i\tilde{\omega}_S t) \langle \tilde{\mathcal{H}}(\cdot; \tau) | \tilde{\mathcal{H}}(\cdot, t; \tau) \rangle \right) (\tilde{\omega}_I) \quad (20)$$

where $\tilde{\omega}_S = \omega_S - \tilde{\omega}_I$ is the energy loss of the system with $\tilde{\omega}_I = \omega_I + E_i$ and scattering frequency ω_S . Further, $*$ denotes the convolution and \mathcal{U} is the Fourier transform

$$\begin{aligned} \mathcal{U}(\omega) &= \mathcal{F}^{-1}(\mathcal{A}(t - \tau)) \\ &= \exp(-i\omega\tau) \cdot \exp\left(-\frac{\sigma^2\omega^2}{2}\right) \end{aligned} \quad (21)$$

of the Gaussian-envelope function \mathcal{A} of the probe pulse defined in eqn (19). Furthermore, the evolving wavepacket



$|\tilde{\mathcal{R}}(\omega, t; \tau)\rangle = e^{-i\hat{H}_v t} |\tilde{\mathcal{R}}(\omega; \tau)\rangle$ is defined by the core-to-valence state projection $|\tilde{\mathcal{R}}(\omega; \tau)\rangle = \mu_{vc} |\mathcal{R}(\omega; \tau)\rangle$ of the Raman wavefunction

$$|\tilde{\mathcal{R}}(\omega; \tau)\rangle = \int_0^\infty dt e^{-i(\hat{H}_c - \frac{F_c}{2})t} \mu_{cv} e^{i(\hat{\omega}_1 - \omega)(t - \tau)} |\Psi_v(t)\rangle \quad (22)$$

collecting all dynamical information prior to the scattering event. In particular, the Raman wavefunction is a time-independent intermediate state that only parametrically depends on τ .

3 Computational details

The molecular Hamiltonian is divided into four energetically separated subsets of states. All parameters for the valence excited states, contained in \mathbf{H}_{v_1} and \mathbf{H}_{v_2} , and two lowest N-1s core-excited states in \mathbf{H}_{c_1} were adapted from previous studies.^{48,60} The values to parameterise \mathbf{H}_{c_2} were obtained by fitting the diabatic potential terms from *ab initio* quantum chemistry calculation using the fc-CVS-EOM-CCSD method⁶¹ with the Dunning correlation consistent basis set aug-cc-pVDZ⁶² matching the level of theory applied in ref. 48. All electronic structure calculations were carried out using the quantum chemistry software package Q-Chem.⁶³ The fitting procedure were performed using the VCHam tools, as part of the Heidelberg MCTDH package.⁶⁴

Quantum dynamics propagations were run using the ML-MCTDH method as implemented in the Heidelberg MCTDH package. The layer structure, DVR, number of grid points and SPF basis size were adapted from ref. 48 with an increased number of 24 electronic states. The output was written such that a sufficient time resolution and frequency span for subsequent Fourier transforms is guaranteed.

The most relevant parameters and computational details are listed in tabular form in the ESI.[†]

3.1 Model Hamiltonian

The vibronic coupling model Hamiltonian was obtained using all 24 mass- and frequency scaled normal modes of the ground state D_{2h} structure of pyrazine. While we utilise the (fc-CVS-) EOM-CCSD/aug-cc-pVDZ based linear vibronic coupling model for \mathbf{H}_{v_2} and \mathbf{H}_{c_1} from our recent study on steady-state RIXS of pyrazine,⁴⁸ we favour the vibronic model from Sala *et al.*⁶⁰ obtained from XMCQDPT2/aug-cc-pVDZ calculations to describe \mathbf{H}_{v_1} containing the ground and lowest four valence excited states where non-adiabatic transitions to the ground state are excluded within the model due to the large energy gap. This model was constructed to simulate the UV absorption spectrum of pyrazine and yielded an excellent agreement with experimental data demonstrating its suitability to accurately describe the valence-excited state behaviour after excitation to the $B_{2u}(\pi\pi^*)$ state. In order to maintain the energy gap between \mathbf{H}_{v_1} and \mathbf{H}_{v_2} as given in ref. 48 the vertical excitation energies in \mathbf{H}_{v_2} are consistently shifted by -0.6 eV. Moreover, we assume an intrinsic core-excited state lifetime of 8 fs⁶⁵ covered by an imaginary energy term in the core Hamiltonian \mathbf{H}_c . Fig. 1 shows cuts of potential

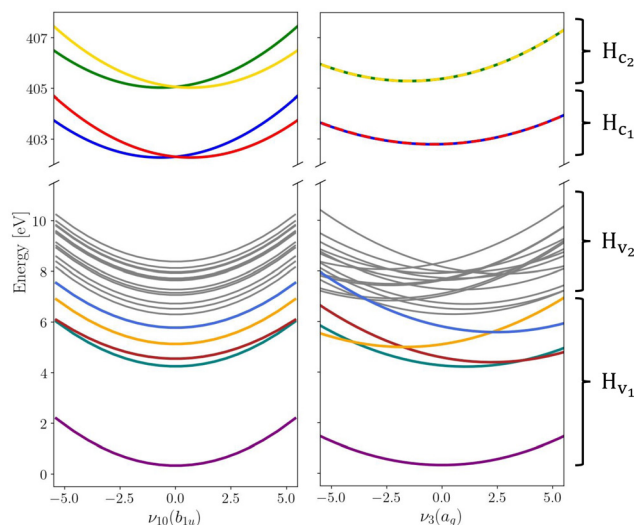


Fig. 1 Cuts through the diabatic potential energy surfaces along the asymmetrical $\nu_{10}(b_{1u})$ and totally symmetrical $\nu_3(a_g)$ vibrational normal modes. Electronic states that are coupled by the X-ray probe pulse are highlighted in colour while the other states that are thus playing a less significant role are held in grey for the sake of overview. Label and symmetry for each state can be found in the ESI.[†]

energy surfaces along one of the totally symmetric normal modes and along one of the core-excited state coupling modes.

Populations in the ground and the three lowest valence-excited states give rise to strongly dipole-allowed transitions to three N-1s core-excited states⁶⁶ where the lower two, X_1 and X_2 , build \mathbf{H}_{c_1} . The third core excited state, X_3 , is furthermore vibronically coupled to a nearly degenerate fourth state, X_4 , necessitating its inclusion in the Hamiltonian \mathbf{H}_{c_2} . The energies and linear coupling parameters obtained in this work for \mathbf{H}_{c_2} are listed in Table 1. Transition dipole moments to valence- and core-excited states were computed at the Franck–Condon point employing the EOM-CCSD and fc-CVS-EOMCCSD method, respectively. The norm of the corresponding transition dipole moments are given in Table 2. A complete list of parameters of the full molecular Hamiltonian can be found in ref. 60 and 48 or in the form of an operator file in the ESI,[†] to this study.

4 Results

4.1 Time-resolved X-ray absorption spectra

To ascertain appropriate excitation energies for investigating the UV-induced dynamics of pyrazine with RIXS at the nitrogen K-edge, we compute time-resolved spectra in the X-ray absorption near-edge structure (XANES) region. For this purpose, we assume δ -pulses for both the pump and probe steps and calculate the spectra according to eqn (15). The diabatic valence-excited state population dynamics subsequent to the pump pulse along with a three-dimensional collection of differential absorption spectra are shown in Fig. 2. At time $t = 0$ fs, the system is primarily excited to S_3 with minor contributions to S_1 according to their transition dipole moments given in Table 2. S_3 rapidly depopulates to both the bright S_1 and the dark S_2 state



Table 1 Vertical excitation energies $E^{(a)}$ as well as linear intra- and interstate coupling constants $\kappa_i^{(a)}$ and $\lambda_i^{(a\beta)}$, respectively, for the core-excited states contained in \mathbf{H}_{c_2} . All values are in eV

	Symmetry				E
X_3	B_{1g}				405.05
X_4	A_u				405.06
	κ_3	κ_{11}	κ_{15}	κ_{20}	
X_3	0.1231	−0.0787	−0.1236	−0.2731	
X_4	0.1230	−0.0787	−0.1240	−0.2754	
	λ_{10}	λ_{14}	λ_{18}	λ_{22}	
(X_3, X_4)	0.0998	0.1087	0.0213	0.0224	

Table 2 Norm of transition dipole moments $\mu_{\alpha\beta}$ between two states $|\alpha\rangle$ and $|\beta\rangle$. The transition dipole moments to valence- and core-excited states are obtained from EOM-CCSD and fc-CVS-EOM-CCSD calculations, respectively

State transition	$\mu_{\alpha\beta}$
$S_3 \leftarrow S_0$	0.25
$S_1 \leftarrow S_0$	0.82
$X_2 \leftarrow S_0$	0.10
$X_1 \leftarrow S_1$	0.06
$X_3 \leftarrow S_2$	0.06
$X_3 \leftarrow S_3$	0.03
$X_2 \leftarrow S_4$	0.04
$X_1 \leftarrow S_6$	0.02
$X_4 \leftarrow S_7$	0.04
$X_3 \leftarrow S_{12}$	0.05
$X_1 \leftarrow S_{16}$	0.04
$X_1 \leftarrow S_{18}$	0.04

followed by oscillatory population dynamics between S_1 and S_2 . This diabatic population behaviour can be traced back to low-lying conical intersections between all state pairs, S_1/S_2 , S_1/S_3 and S_2/S_3 .⁶⁰

The population dynamics are well reflected in the transient absorption spectra, where the strong negative bleach signal located around 402.5 eV corresponds to $X_2 \leftarrow S_0$ transitions while the positive excitation bands at approximately 399.0 eV and 401.8 eV stem from excited state absorption. Within the first few femtoseconds, S_3 is mainly populated leading to an absorption band around 400.5 eV. Due to vibrational relaxation in S_3 as well as X-ray excitation to potentially higher vibronic states in X_3 , the $X_3 \leftarrow S_3$ transitions are then shifted to higher frequencies by about 1.3 eV where they energetically overlap with the $X_3 \leftarrow S_2$ transition band. The absorption band at 399.0 eV only stems from $X_1 \leftarrow S_1$ transitions. The non-adiabatic oscillatory population dynamics between S_1 and S_2 are accurately mapped in the intensity variations of the two main excited state absorption bands in good agreement with previous simulations.⁶⁶ However, it is worth noting that we formerly used a reduced pyrazine model that comprised only the 9 most dominant vibrational normal modes. In this study, a full 24-dimensional model is used leading to more delocalised wavepackets on the valence excited state manifold that manifest in broader and somewhat asymmetrical

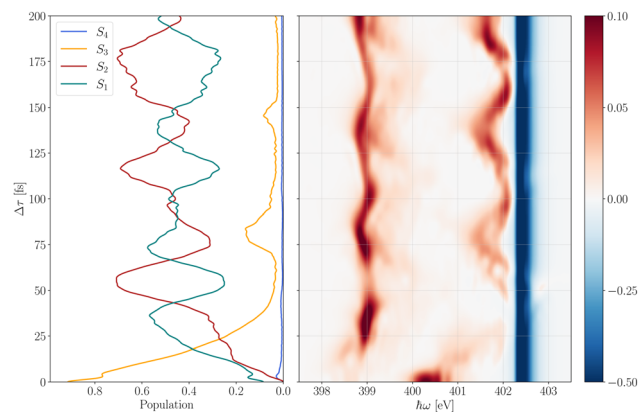


Fig. 2 Valence-excited state population after instantaneous, vertical excitation to the bright S_3 and S_1 states at the Franck-Condon point (left) and a three-dimensional map showing all computed differential X-ray absorption spectra for time delays between 0 and 200 fs (right). A figure showing fs-XANES spectra for all individual transitions can be found in the ESI.†

line shapes of the excitation bands. This behaviour is particularly pronounced in the strongly fluctuating absorption band around 401.8 eV which also overlaps with the bleach signal at some time delays. In contrast, our previous calculations showed this absorption band to be well separated from the bleach signal for the entire propagation time.

Based on the time-dependent differential absorption map in Fig. 2, we choose excitation energies of 399.0 eV and 401.5 eV for the following fs-RIXS simulations, probing the dynamics on S_1 and S_3/S_{22} , respectively. The latter X-ray excitation energy was chosen slightly below the center of the fluctuating absorption band to exclude contributions from ground-state bleaching. Moreover, the ESI,† also contains fs-RIXS calculations for an excitation energy of 402.5 eV to show the behaviour in the overlap region of the bleach signal and the close-lying excited state absorption.

4.2 Femtosecond resonant inelastic X-ray scattering

The dynamics triggered by the optical pump pulse primarily involve three valence excited states and are mainly driven by the interstate coupling parameters between the state pairs S_1/S_3 and S_1/S_2 with oscillation periods of 19 fs and 21 fs, respectively.⁶⁰ We therefore choose a Gaussian X-ray probe pulse with a temporal FWHM duration of $F_t \approx 8$ fs enabling to follow this ultrafast dynamics without losing relevant information due to spectral broadening caused by a broadband excitation pulses.⁴⁸

The transient RIXS spectra are computed using eqn (20) with carrier frequencies of 399.0 eV and 401.5 eV and at time-delays $\Delta\tau$ ranging from 5 to 200 fs. A three-dimensional collection of all spectra along with a single fs-RIXS spectrum for $\Delta\tau = 100$ fs is shown in Fig. 3. Moreover, a two dimensional representation of the time evolution of the fs-RIXS spectrum in 10 fs steps for both excitation energies can be found in the ESI.†

As discussed in the previous section, RIXS probing at 399.0 eV only promotes $X_1 \leftarrow S_1$ transitions entailing four dipole allowed scattering transitions back to valence excited states S_1 , S_6 , S_{16} and S_{18} (see Table 2) with transition bands located at



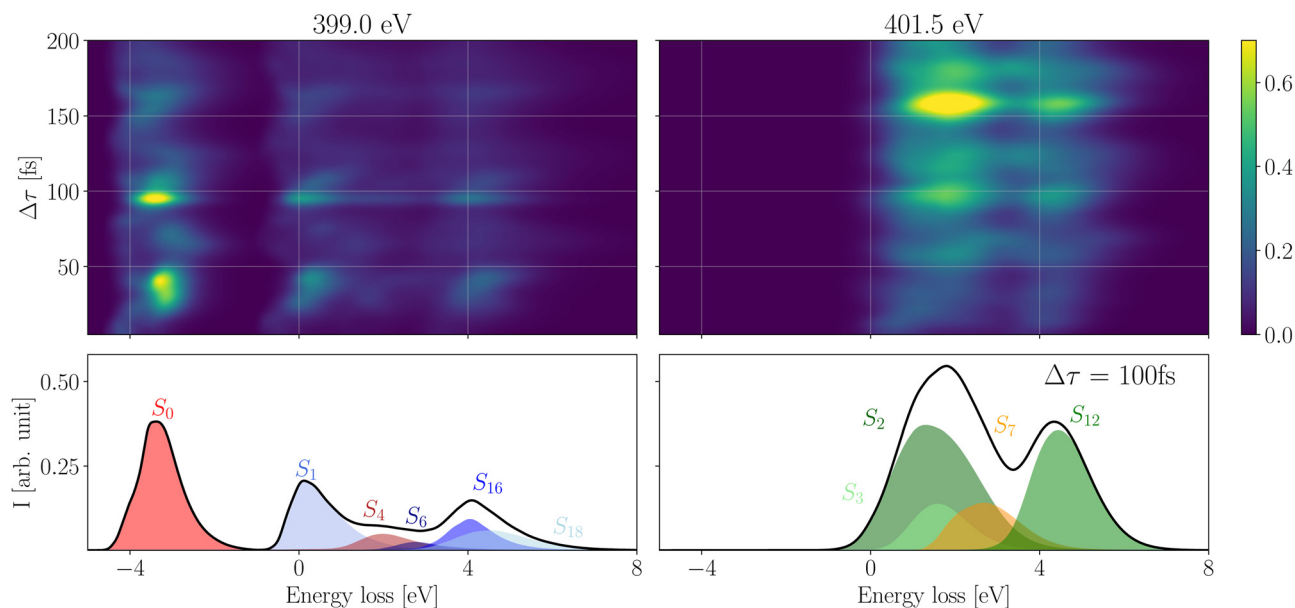


Fig. 3 Top: Three-dimensional collection of calculated fs-RIXS spectra for time delays $\Delta\tau$ between 5 fs and 200 fs with a step size of 5 fs using excitation energies of 399.0 eV (left) and 401.5 eV (right). Bottom: fs-RIXS spectrum at time delay $\Delta\tau = 100$ fs. Transitions stemming from X_1 , X_2 , X_3 and X_4 are highlighted in blue, red, green and yellow, respectively. The final electronic state of each transition is annotated in the plot.

approximately 0.0 eV, 3.0 eV, 4.0 eV and 4.5 eV, respectively. These values correspond to the vertical energy gap of the electronics states to S_1 . Moreover, the RIXS spectrum exhibits a strong anti-Stokes signal at -3.8 eV and a weaker transition band at 2.0 eV belonging to transitions to S_0 and S_4 , respectively, which are dipole forbidden from the initially excited X_1 state. However, due to the delocalised nature of the N-1s core orbitals over the equivalent nitrogen atoms, pyrazine naturally possesses nearly degenerate core-excited states, X_1 and X_2 , that are vibronically coupled through asymmetrical normal modes of symmetry b_{1u} .⁴⁸ This coupling leads to ultrafast symmetry breaking of the system within the core-hole lifetime accompanied by a localisation of the core orbitals that finally permits the dipole allowed $S_0 \leftarrow X_2$ and $S_4 \leftarrow X_2$ transitions. Furthermore, besides the rather weak and spectrally overlapping signals at higher energy loss, the clearly distinguishable $S_0 \leftarrow X_2$ and $S_1 \leftarrow X_1$ transition bands can be seen over the entire time range as demonstrated in the upper left panel of Fig. 3. Consequently, after photo-excitation to S_3 the system leaves the immediate Franck-Condon region but remains in a configurations where the two nitrogen atoms are equivalent holding the system close to the conical intersection seam formed along the four normal modes with symmetry b_{1u} . These modes are responsible for disturbing the equivalence of the nitrogen atoms. This result particularly confirms the assumption that none of these vibrational normal modes plays a prominent role in the UV induced dynamics of pyrazine. They can thus be neglected in linear UV absorption simulations.⁶⁰ Lastly, we note that the overall signal strengths vary in accordance with the population dynamics of S_1 shown in Fig. 2.

X-ray excitations at 401.5 eV addresses $X_3 \leftarrow S_2$ as well as $X_3 \leftarrow S_3$ transitions where the latter only significantly

contribute within the first 20–30 fs due to the rapid depopulation of S_3 . The related fs-RIXS spectra show two dominant spectral bands where the lower band actually originates from three energetically overlapping transitions. As before, there are two nearly degenerate core-excited states, X_3 and X_4 , that are vibronically coupled along the b_{1u} normal modes with coupling strengths listed in Table 1. Due to their large overlap, ultrafast nuclear motion cannot be separately attributed to individual transitions within this spectral region. Contrary to probe excitations at 399.0 eV, the transient RIXS spectra at 401.5 eV do not contain anti-Stokes signals. Thus, the absence of transitions to the ground state indicate the symmetry of the core-excited state at 401.5 eV. Moreover, an increase of the overall signal strength can be observed for time delays $\Delta\tau$ beyond 100 fs. On the one hand, this trend can be explained by the considerable lower transition dipole moment $\mu_{X_3 \leftarrow S_3}$ compared to $\mu_{X_3 \leftarrow S_2}$ yielding less likely transitions at very early times, and, on the other hand by the strong modulation of the absorption band (see Fig. 2) resulting in a large detuning effect for time delays between 20 fs and 80 fs.

Fig. 4 presents differential XANES spectra and RIXS maps as a function of excitation energy ω_i of the X-ray probe pulse and energy loss ω_s to the molecule at specific time delays. Both the transient absorption and the RIXS spectra exhibits positive features stemming from valence-excited state transitions and negative bleach signals related to ground-state transitions of the non-excited system. The bleach signal remains the same for all time delays as there is no radiationless relaxation mechanism from excited states back to the ground state on the femtosecond timescale. Moreover, X-ray transitions involving the ground state S_0 are considerably more likely compared to valence-excited state transitions (see Table 2) resulting in a very



dominant bleach signal at approximately 402.5 eV. Overall the shape of the excited-state transition bands is rather broad and asymmetrical for both probing techniques which must be therefore traced back to the evolution of the nuclear wavepacket of the pumped system. Additionally, the fs-RIXS maps also contain dynamical features from the intermediate core-excited states as well as from the final ground and valence-excited states.

For both time delays shown in Fig. 4 the RIXS bleach signal consists of five transition bands (stemming from six core-to-valence state transitions). The higher four bands are energetically separated from the lowest transition band by about 3.9 eV, 5.3 eV, 6.5 eV and 7.5 eV. As the lowest transition band of the bleach signal is located just above 0 eV it can be uniquely assigned to the electronic ground state. Moreover, for 20 fs time delay the energy-level separation pattern of the bleach signal repeats in the excited-state signals at 399.0 eV shifted by -3.9 eV. This suggests that the corresponding initial ground and valence-excited states address the same core-excited state pair leading in turn to similar emission bands. However, the progressive valence-excited state dynamics after 55 fs smear out the recurrences, thereby making a direct assignment without additional analysis support difficult.

The spectral proximity of the RIXS band around 401.5 eV masks parts of the time-dependent signal. Particularly at 55 fs the dominant time-independent bleach signal overlaps with the stronger part of the excited-state signal. Within the first 20 fs after valence excitation the two signals do not overlap appreciably before population transfer to S_2 sweeps the resonance – and hence, the RIXS signal – to higher energy. As already discussed

above, the missing energy-gain features at 401.5 eV clearly indicate X-ray transitions to another pair of core-excited states.

In essence, time-resolved RIXS emerges as a dependable tool to unravel the ultrafast photophysical actions of pyrazine, augmenting the capabilities of other ultrafast X-ray spectroscopic methods such as fs-XANES spectroscopy. Although fs-XANES adeptly probes the dynamics induced by UV radiation, time-resolved RIXS delves deeper into dynamic facets, unveiling symmetry distortions resulting from non-adiabatic transitions within core-excited states. Furthermore, it furnishes insights into higher-lying valence excited states, which remain inaccessible in transient absorption spectroscopy due to symmetry constraints or weak transition dipole moments.

5 Conclusion

While steady-state soft X-ray RIXS has already proven appropriate in probing the chemical and physical properties of molecular systems, time-resolved RIXS experiments have been less common due to the even more demanding spectral brightness requirements. However, advances in XFEL technology, accompanied by new instrumentation such as the hRIXS instrument at European XFEL and the ChemRIXS instrument at LCLS-II,⁶⁷ hold promise of making time-resolved RIXS a routinely employed technique in the coming years. Moreover, our approach can be expanded to describe stimulated processes which will benefit from advances in seeding technology with a further leap in spectral brightness of XFEL sources. To effectively extract the rich information contained within the experimental data,

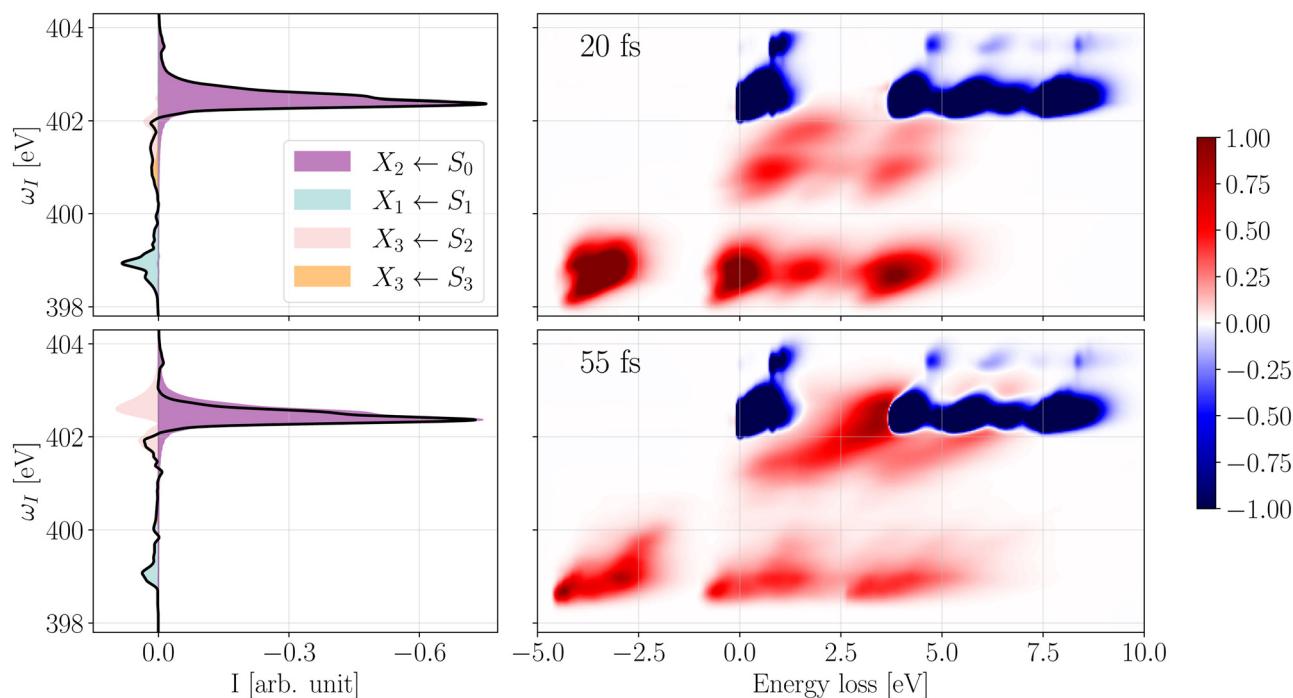


Fig. 4 fs-XANES (left) and corresponding fs-RIXS spectra (right) for time delays $\Delta\tau = 20$ fs (top) and $\Delta\tau = 55$ fs (bottom). fs-RIXS spectra are computed for excitation energies ω_i ranging from 397.0 eV to 404.9 eV with 0.1 eV stepsizes.



theoretical progress in truly describing dynamics are imperative to support these expanded experimental capabilities.

In this study, we presented a fully time-dependent quantum mechanical approach to simulating time-resolved RIXS experiments. Leveraging the capabilities of the MCTDH method, we establish a robust framework to accurately describe the intricate photophysics of pyrazine, encompassing all relevant dynamical dimensions. The interplay between population transfers within the valence-excited state manifold and the symmetry-breaking nuclear motions after X-ray interrogation can only be faithfully captured through nuclear quantum dynamics simulations that incorporate non-adiabatic phenomena. Our study further discloses challenges in building reduced-dimensionality models in larger molecules and elucidates the necessity of incorporating symmetry-breaking degrees of freedom. In particular, our time-dependent approach enables simulations beyond steady-state conditions contributing to the growing field of nonlinear spectroscopy at pulsed X-ray sources of high spectral brightness.

Data availability

The data supporting this article have been included as part of the ESI.†

Conflicts of interest

There are no conflicts to declare.

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