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# Similarity scores of vibrational spectra reveal the atomistic structure of pentapeptides in multiple basins†

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Vibrational spectroscopy combined with theoretical calculations is a powerful tool for analyzing the interaction and conformation of peptides at the atomistic level. Nonetheless, identifying the structure becomes increasingly difficult as the peptide size grows large. One example is acetyl-SIVSF-N-methylamide, a capped pentapeptide, whose atomistic structure has remained unknown since its first observation [T. Sekiguchi, M. Tamura, H. Oba, P. Çarçarbal, R. R. Lozada-Garcia, A. Zehnacker-Rentien, G. Grégoire, S. Ishiuchi and M. Fujii, *Angew. Chem., Int. Ed.*, 2018, **57**, 5626–5629]. Here, we propose a novel conformational search method, which exploits the structure-spectrum correlation using a similarity score that measures the agreement of theoretical and experimental spectra. Surprisingly, the two conformers have distinctly different energy and geometry. The second conformer is 25 kJ mol<sup>-1</sup> higher in energy than the other, lowest-energy conformer. The result implies that there are multiple pathways in the early stage of the folding process: one to the global minimum and the other to a different basin. Once such a structure is established, the second conformer is unlikely to overcome the barrier to produce the most stable structure due to a vastly different hydrogen bond network of the backbone. Our proposed method can characterize the lowest-energy conformer and kinetically trapped, high-energy conformers of complex biomolecules.

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## Introduction

Advanced technologies in gas-phase vibrational spectroscopy have made it feasible to elucidate the structure and interaction of complex molecules and clusters. Various systems have been studied to date; for example, ionic liquid,<sup>1–4</sup> protonated water clusters,<sup>5–10</sup> metal oxide clusters,<sup>11–15</sup> and so on. Conformer-selective vibrational spectra of polypeptides<sup>16–26</sup> have been measured with the usage of infrared (IR) and ultraviolet (UV)

double resonance spectroscopy and supersonic jet expansions. We have developed cryogenic ion traps<sup>27</sup> combined with an electrospray ion source,<sup>28,29</sup> which efficiently produce peptides and peptide–ligand complexes in the gas phase. The method has been applied to building blocks of the receptor domain of ion channels,<sup>30–32</sup>  $\beta_2$ -adrenoceptors,<sup>33,34</sup> and kinase<sup>35</sup> to elucidate the mechanism for molecular recognition.

As the molecule grows complex, theoretical analysis plays a crucial role in assigning spectral peaks and molecular structures.<sup>36</sup> One of the common approaches is to optimize the geometry of candidate structures and calculate their harmonic vibrational spectra using electronic structure calculations. However, the agreement between harmonic spectra and the experiment is insufficient due to the lack of anharmonicity. Notably, NH/OH groups, which form hydrogen bond (HB) networks, induce strong anharmonic couplings. Furthermore, polypeptides have many possible conformers due to their flexibility. In the previous work, we proposed a method that combines conformational sampling, clustering analysis, geometry optimization, and anharmonic vibrational analysis (Fig. 1a).<sup>37</sup> We used the replica-exchange molecular dynamics (REMD) method<sup>38–41</sup> and the second-order vibrational quasi-degenerate perturbation theory (VQDPT2),<sup>42,43</sup> for sampling

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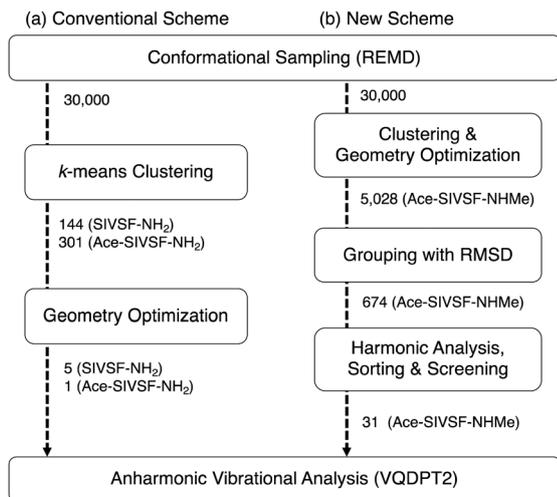


Fig. 1 Schematic illustration of (a) the conventional conformational search scheme used in the previous work (ref. 37) and (b) that of the present work. The numbers indicate the number of candidate structures in each process.

and vibrational calculations, respectively. The method has been applied to a pentapeptide, Ser-Ile-Val-Ser-Phe (SIVSF-NH<sub>2</sub>) (Fig. 2a), which is a partial sequence of the binding site of the  $\beta_2$ -adrenoceptor.<sup>26</sup> Our method reproduced the experimental IR spectrum in a range of 3100–3700 cm<sup>-1</sup> with a mean absolute deviation (MAD) of 11.2 cm<sup>-1</sup>, and determined the peptide structure.

Nevertheless, the method faces a challenge when multiple conformers are observed in the experiment. In Fig. 1a, the clustering and the geometry optimization aim to find energetically stable structures. However, the observed conformers may not appear in the energetic order. For example, Gloaguen *et al.* studied a model dipeptide, *N*-acetyl-(Ala)<sub>2</sub>-O-benzyl, and observed

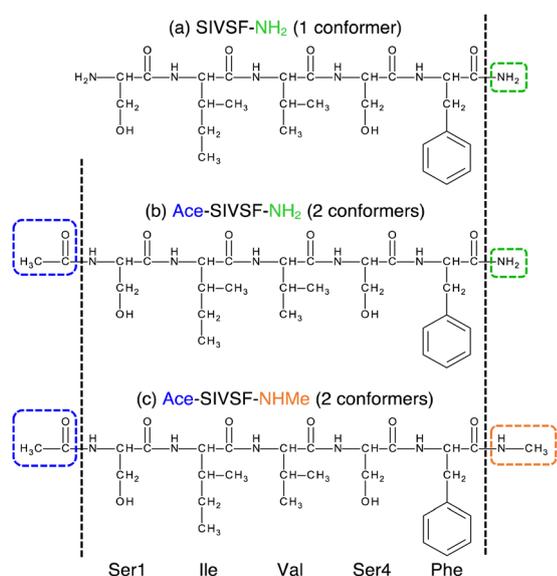


Fig. 2 Chemical formulae of (a) SIVSF-NH<sub>2</sub>, (b) Ace-SIVSF-NH<sub>2</sub>, and (c) Ace-SIVSF-NHMe.

IR spectra of two conformers.<sup>25</sup> With the aid of theoretical calculations, the two conformers have been assigned to the most stable folded structure and a fully extended backbone structure. Notably, the extended structure is higher in energy than the folded structure by *ca.* 16 kJ mol<sup>-1</sup>.

In this study, we investigate the structure of Ace-SIVSF-NH<sub>2</sub> and Ace-SIVSF-NHMe (Fig. 2b and c, respectively). Previously, we found two conformers of Ace-SIVSF-NHMe by the IR/UV double resonance spectroscopy.<sup>34</sup> However, the conformer structures have remained tentative. In addition, we carried out a similar measurement for Ace-SIVSF-NH<sub>2</sub> and found two conformers (Section S2, ESI<sup>†</sup>). Revealing the structures of these conformers poses a challenge.

Here, we develop a new conformational search method that exploits the correlation between structure and spectrum as a guiding principle (Fig. 1b). In this new method, candidate structures are categorized based on their structural differences, and the conformer is determined by comparing the theoretical and experimental spectrum. For this purpose, we have incorporated similarity scores (see Methods), which objectively measure the agreement between two spectra. These scores prove to be useful tools in selecting the calculated spectrum that most accurately matches with the experimental one, without any subjective bias. The structural search reveals that the two conformers of Ace-SIVSF-NH<sub>2</sub> come from the same basin, whereas those of Ace-SIVSF-NHMe have distinctly different geometry (Table 1).

## Results

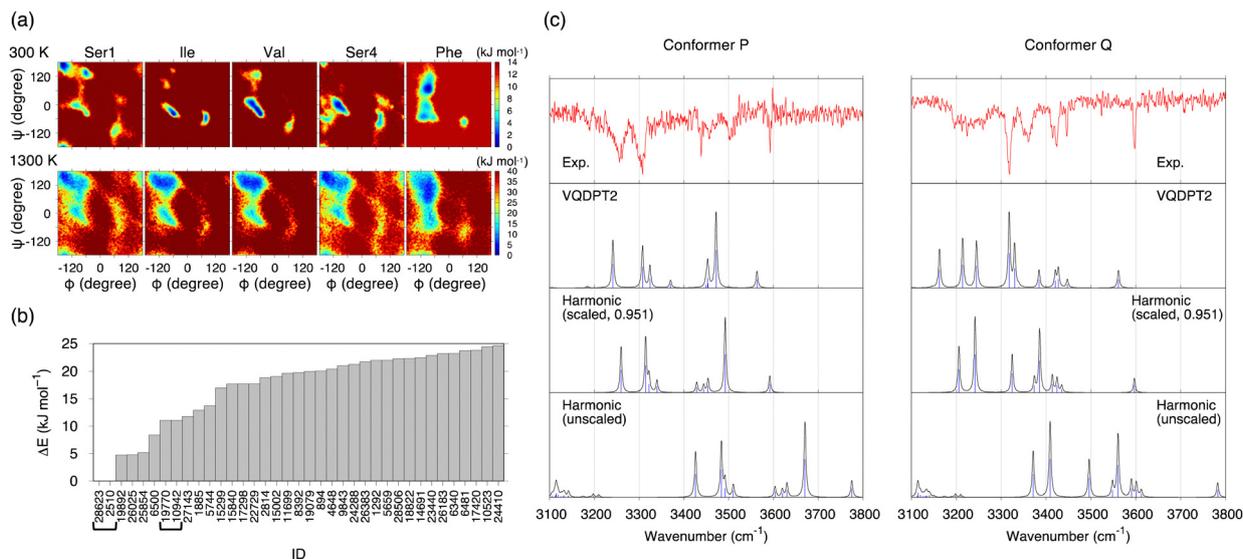
### Conformational search of Ace-SIVSF-NH<sub>2</sub>

The potential of mean forces (PMFs) obtained by REMD simulations are shown in Fig. 3a. The PMF is plotted as a function of backbone dihedral angles  $\phi$  and  $\psi$  for each residue. Notably, the PMF of all residues resembles each other at 1300 K, indicating that the simulation samples a sufficiently wide conformational space. A random walk is achieved in replica, temperature, and potential energy space (Fig. S9, ESI<sup>†</sup>). 30 000 snapshot structures obtained from the REMD trajectory at 300 K are referred to by an ID number from 1 to 30 000 with the prefix “f”.

The conformational search was carried out in the conventional scheme. First, *k*-means clustering analysis was used to find representative structures from the trajectory. The clustering analysis yielded 301 structures by setting the clustering radius to 1.6 Å. Then, these structures were geometry optimized by the density functional theory (DFT) at the level of B3LYP/6-

Table 1 List of conformer names found in the experiment and ID labels of calculated structures assigned to them

Peptide	Conformer name	ID
Ace-SIVSF-NH <sub>2</sub>	P	A'
	Q	f28623
Ace-SIVSF-NHMe	X	f19375
	Y	f389



**Fig. 3** Results of the conformational search of Ace-SIVSF-NH<sub>2</sub> obtained with the conventional scheme. (a) The PMFs of the five residues obtained by REMD at 300 and 1300 K. (b) Relative energies of conformers up to 25 kJ mol<sup>-1</sup> obtained by the geometry optimization at the B3LYP/6-31(++)G\*\* level of theory. The conformer IDs of the same structure are shown in bracket. (c) Comparison of the experimental IR spectra of conformer P and conformer Q with the calculated ones for conformer A' and f28623 obtained by the harmonic approximation with and without scaling the frequency and the VQDPT2 method.

31(++)G\*\*. [This level was used to be consistent with the previous work on SIVSF-NH<sub>2</sub>.<sup>37</sup> The quality of this calculation is assessed in the Discussion section.] Fig. 3b shows the relative energies of the optimized structures. The most stable structure, f28623, is a strong candidate for the experimentally observed conformer.

One of the two spectra of Ace-SIVSF-NH<sub>2</sub>, conformer P, is very similar to that of SIVSF-NH<sub>2</sub> (Fig. S7, ESI†). Therefore, we have manually constructed a conformer of Ace-SIVSF-NH<sub>2</sub> by modifying conformer A of SIVSF-NH<sub>2</sub> found in the previous study.<sup>37</sup> The N-terminal of SIVSF-NH<sub>2</sub> is replaced with an acetyl group, and the geometry is optimized at the B3LYP/6-31(++)G\*\* level. We call this structure conformer A'. Conformer A' is 4.72 kJ mol<sup>-1</sup> higher in energy than f28623. The molecular structures of conformer A' and f28623 are compared in Fig. S11 (ESI†).

Fig. 3c shows the IR spectra of conformer A' and f28623 calculated by the harmonic approximation and the VQDPT2 method together with the experimental spectra. The peak positions obtained from the harmonic approximation deviate from the experimental ones by more than 100 cm<sup>-1</sup>, suggesting strong anharmonic effects on the N-H and O-H stretching vibration. Scaled harmonic spectra, in which the frequencies are scaled so that the highest frequency peak matches the experiment, show a substantial improvement. However, the agreement with the experiment is insufficient, especially for conformer Q. In contrast, VQDPT2 not only corrects the position to the right place but also yields overtones and combination bands due to Fermi resonance. Consequently, VQDPT2 spectra agree quantitatively with the experimental spectra. The MAD of the peak position between conformer P and conformer A', and conformer Q and f28623 are obtained as

14.9 and 13.5 cm<sup>-1</sup>, respectively. The accuracy is comparable to the previous work on SIVSF-NH<sub>2</sub> (MAD = 11.2 cm<sup>-1</sup>), in which the calculation was done in the same procedure.<sup>37</sup> We therefore conclude that the experimentally observed conformer P and conformer Q are assigned to conformer A' and f28623, respectively.

The details on the peak assignment and the Fermi resonance are provided in ESI† (Section S3.3).

### Conformational search of Ace-SIVSF-NHMe

REMD simulations were carried out for Ace-SIVSF-NHMe in the same way. Again, a random walk is achieved in replica, temperature, and potential energy space (Fig. S12, ESI†). 30 000 snapshot structures were obtained from trajectories at 300 K and used for the conformational search.

The conventional scheme was first employed to find the two conformers observed in the experiment (conformer X and conformer Y). Consequently, conformer X was assigned to the energetically most stable conformer, f19375, but conformer Y was not found among the five lowest energy structures (Section S4.2, ESI†). We then improved the search algorithm by incorporating hierarchical clustering analyses based on the principal component analysis (PCA) and Ward's method (Section S4.3, ESI†). Despite all these efforts, the structure of conformer Y remained unknown (Section S4.4, ESI†).

The failure of the conventional method and its variant has prompted us to develop a conceptually different approach, *i.e.*, a method that does not rely on the energetics but extensively exploits the structure-spectrum correlation. The new method outlined in Fig. 1b was carried out in the following steps: (1) the energetics (*i.e.*, the geometry optimization) were used for pre-screening, leaving more than 5000 candidate structures. (2)

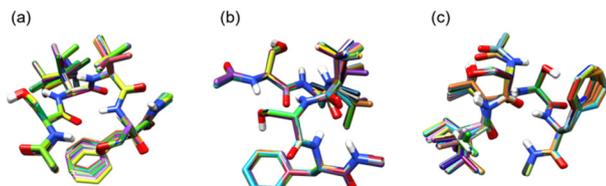


Fig. 4 Superimpositions of conformers of Ace-SIVSF-NHMe obtained by the grouping based on RMSD. (a) The first most populated group (428 conformers), (b) the second most populated group (187 conformers), and (c) the third most populated group (180 conformers).

Similar structures were classified into 674 groups based on an RMSD of backbone and important sidechain atoms. (3) The representative structure of each group was used for the harmonic vibrational analysis. Then, 56 low-energy structures were selected, and 25 structures were ruled out because the harmonic spectrum was qualitatively wrong. (4) VQDPT2 calculations were carried out for the remaining 31 structures. Finally, the conformers were assigned based on a similarity score, which measures the difference between the experimental and VQDPT2 spectra. Further details on calculation protocols, used programs, and computational costs are given in Section S1 (ESI†).

Fig. 4 shows superpositions of conformers of the three most populated groups obtained in step (2). The conformers are found to be well overlapped, demonstrating the usefulness of the proposed grouping procedure. Fig. 5 compares similarity scores,  $S_1$  and  $S_2$ , of the computed conformers. (The spectra are shown in Fig. S19, ESI†) In Fig. 5a and b, f19375 gives the smallest  $S_1(X)$  and the second smallest  $S_2(X)$  among the calculated conformers, reinforcing the assignment of conformer X to

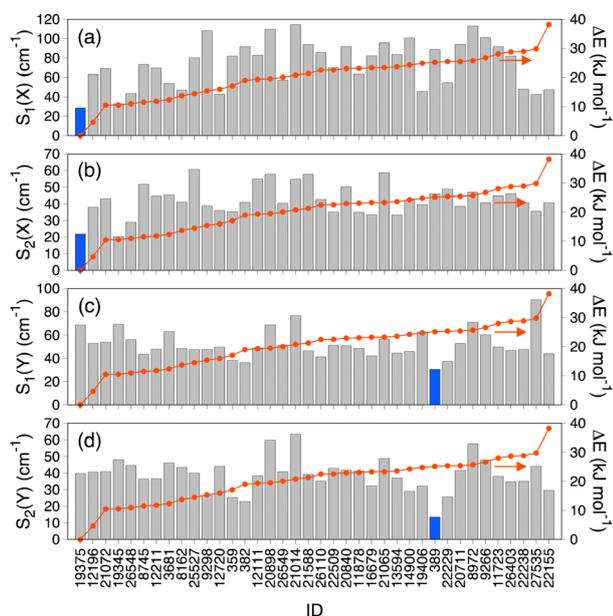


Fig. 5 The similarity scores  $S_1$  and  $S_2$  (left axis) with respect to conformer X [(a) and (b), respectively] and those with respect to conformer Y [(c) and (d), respectively], and the relative energy  $\Delta E$  (right axis) from the most stable conformer, f19375, obtained by the RI-MP2/def2-TZVP(-df) level. f19375 and f389 are indicated in blue.

f19375. In Fig. 5c and d, one of the conformers, f389, gives a distinctly small value of  $S_1(Y) = 30.6 \text{ cm}^{-1}$ . It is notable that f389 is less stable than f19375 by  $25.2 \text{ kJ mol}^{-1}$ . Fig. 6 compares the experimental spectrum with the theoretical spectra of five conformers in increasing order of  $S_1$ . The IR spectrum of conformer X and conformer Y agrees best with that of f19375 and f389, respectively, as indicated by the value of  $S_1$ . We therefore conclude that conformer X and conformer Y are assigned to f19375 and f389, respectively. The details on the peak assignment are provided in Section S4.6 (ESI†).

## Discussion

We have carried out REMD simulations, conformational searches, and VQDPT2 calculations to determine the atomistic structure of two conformers of capped SIVSF peptides, Ace-SIVSF-NH<sub>2</sub> and Ace-SIVSF-NHMe, observed in the gas-phase IR spectroscopy. Although the conventional scheme found one of the conformers (the lowest-energy structure), it failed to reveal the second conformer. Here, we have developed a new scheme that exploits the structure-spectrum correlation: (1) the candidate conformers are grouped based on structural features, and (2) the conformer is assigned utilizing similarity scores of the calculated VQDPT2 spectrum compared to the experimental one. Using the proposed approach, we have determined the structure of all conformers of capped SIVSF peptides observed in the experiment.

Fig. 7 shows the structure of SIVSF revealed in the present and previous works, together with a diagram of HB networks. Hereafter, we denote the OH, NH, and CO groups of residue R as OH<sub>R</sub>, NH<sub>R</sub>, and CO<sub>R</sub>, respectively. Two conformers of Ace-SIVSF-NH<sub>2</sub> are different only in the HB of OH<sub>Ser1</sub>. OH<sub>Ser1</sub> is hydrogen bonded to CO<sub>Val</sub> in conformer A', whereas it is bonded to CO<sub>Ace</sub> in f28623. Other HBs are common: NH<sub>Cter</sub>-CO<sub>Ser4</sub> ( $\gamma$ -turn), NH<sub>Phe</sub>-CO<sub>Ile</sub> ( $\beta$ -turn), NH<sub>Val</sub>-CO<sub>Ser1</sub> ( $\gamma$ -turn), NH<sub>Ile</sub>-CO<sub>Phe</sub>, and NH<sub>Cter</sub>-OH<sub>Ser1</sub>. In addition, the OH- $\pi$  interaction between OH<sub>Ser4</sub> and the phenyl ring of Phe (OH<sub>Ser4</sub>-Ph<sub>Phe</sub>) is also found in both conformers. Conformer A' is  $4.72 \text{ kJ mol}^{-1}$  less stable in energy than f28623 and is found to be the second lowest energy conformer among all the calculated ones. The structural similarity and the slight energy difference indicate that these conformers belong to the same basin. The result is in line with the previous report by Chin *et al.*,<sup>44–47</sup> where three conformers of Ace-Phe-NH<sub>2</sub> and two conformers of Ace-Phe-Val-NH<sub>2</sub> observed simultaneously have been found from the same basin of the conformational landscape within *ca.*  $4 \text{ kJ mol}^{-1}$  of the relative energy.

On the other hand, the second conformer of Ace-SIVSF-NHMe (f389) is  $25.2 \text{ kJ mol}^{-1}$  higher in energy than the most stable one (f19375). Notably, the energy difference is significantly larger than that of Ace-SIVSF-NH<sub>2</sub>. The diagram of HB networks in Fig. 7 demonstrates that f19375 and f389 are quite different in geometry. f19375 has eight HBs in total, whereas f389 has only five. The larger number of HBs stabilizes the structure of f19375. The difference in structure and energy suggests that f19375 belongs to a different basin from f389.

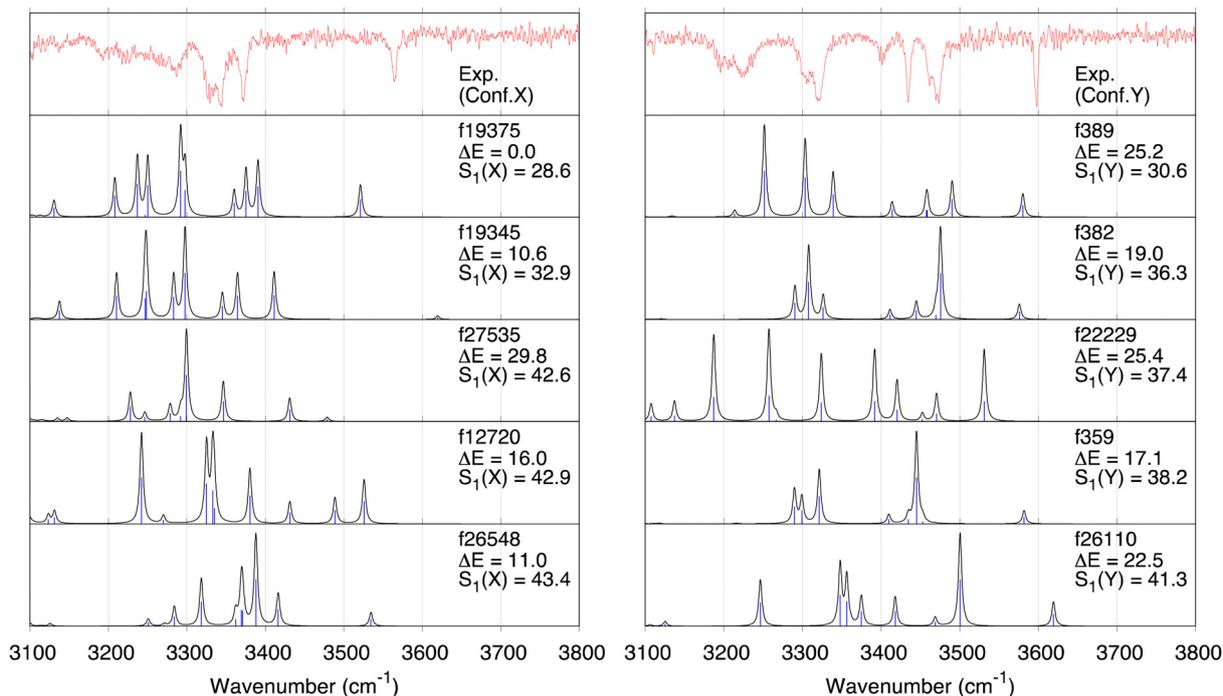


Fig. 6 Theoretical IR spectra of the conformers of Ace-SIVSF-NHMe compared with the experimental spectra of conformer X and conformer Y.  $\Delta E$  (in kJ mol<sup>-1</sup>) is the relative energy from the most stable conformer (f19375) obtained at the RI-MP2/def2-TZVP(-df) level. The similarity scores  $S_1$  (in cm<sup>-1</sup>) with respect to conformer X and conformer Y are written as  $S_1(X)$  and  $S_1(Y)$ , respectively.

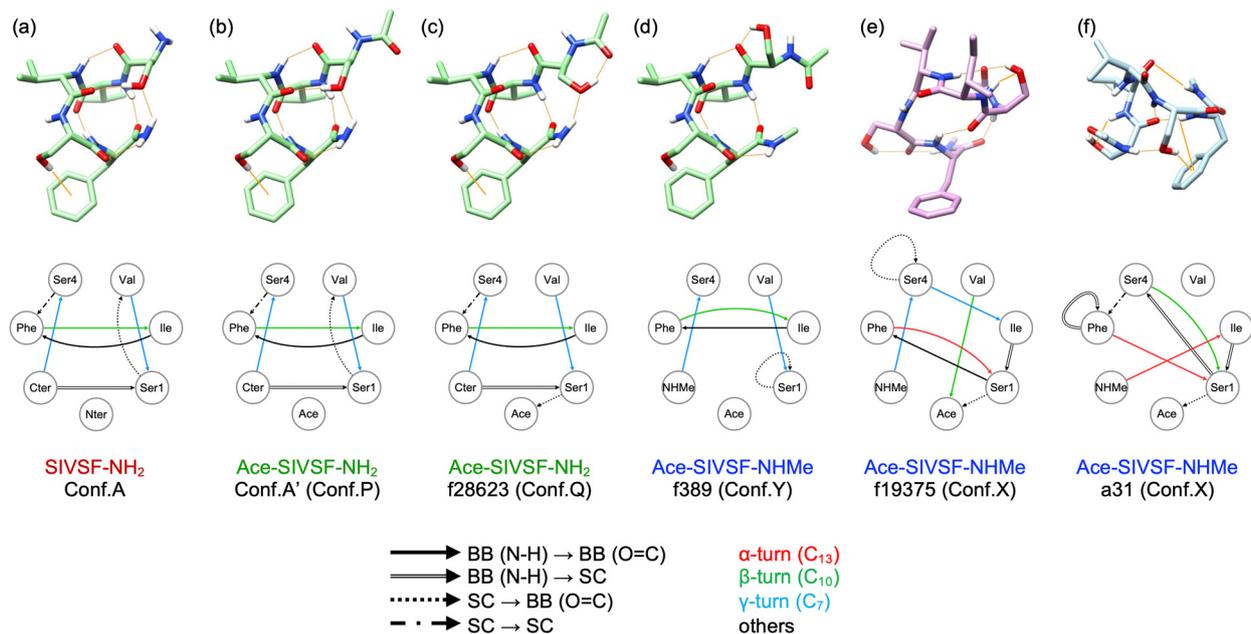


Fig. 7 Molecular structures and diagrams of HB networks of SIVSF. (a) Conformer A of SIVSF-NH<sub>2</sub>. (b) and (c) conformer A' and f28623 of Ace-SIVSF-NH<sub>2</sub>. (d) and (e) f389 and f19375 of Ace-SIVSF-NHMe. (f) a31 of Ace-SIVSF-NHMe obtained in ref. 34. Hydrogen atoms except for OH and NH are omitted for clarity. Hydrogen bonds are shown in orange lines.

Interestingly, f389 has a similar HB network to conformers of Ace-SIVSF-NH<sub>2</sub>, which forms HBs between NH<sub>NHMe</sub>-CO<sub>Ser4</sub> ( $\gamma$ -turn), NH<sub>Phe</sub>-CO<sub>Ile</sub> ( $\beta$ -turn), NH<sub>Val</sub>-CO<sub>Ser1</sub> ( $\gamma$ -turn), NH<sub>Ile</sub>-CO<sub>Phe</sub>, and OH<sub>Ser4</sub>-Ph<sub>Phe</sub>. Note that OH<sub>Ser4</sub>-Ph<sub>Phe</sub> is absent in

f389 because one geometrical parameter is slightly out of the range of Malone's criteria for D-H... $\pi$  interactions (Fig. S21, ESI<sup>†</sup>).<sup>48</sup> Thus, the three conformers, f28623, conformer A', and f389, are different only in the orientation of OH<sub>Ser1</sub>. The

structures of these conformers are overlapped in Fig. S22 (ESI<sup>†</sup>). This is because OH<sub>Ser1</sub> avoids the steric hindrance with the methyl group of the C-terminal cap. Consequently, f389 lacks in the HB between NH<sub>NHMe</sub>-OH<sub>Ser1</sub>.

The distinct geometry between f19375 and f389 is fascinating, suggesting multiple pathways in the early stage of the folding process. One is a pathway to the global minimum, but the other path leads to a different basin. From the observation that f389 has a similar structure to SIVSF-NH<sub>2</sub> and Ace-SIVSF-NH<sub>2</sub>, we speculate that the sequence, SIVSF, has an intrinsic folding propensity of the backbone, *i.e.*, NH<sub>Cter</sub>-CO<sub>Ser4</sub> ( $\gamma$ -turn), NH<sub>Phe</sub>-CO<sub>Ile</sub> ( $\beta$ -turn), NH<sub>Val</sub>-CO<sub>Ser1</sub> ( $\gamma$ -turn), and NH<sub>Ile</sub>-CO<sub>Phe</sub>. The pathway leads to forming the most stable conformer in SIVSF-NH<sub>2</sub> and Ace-SIVSF-NH<sub>2</sub> but not in Ace-SIVSF-NHMe due to an instability caused by the *N*-methyl cap. Nonetheless, once such a structure is formed, it is difficult to overcome the barrier to produce the most stable structure, *i.e.*, f19375, because the HB network of the backbone is vastly different. Consequently, two conformers are produced in Ace-SIVSF-NHMe.

One of the characteristic structures of f19375 is the  $\alpha$ -turn, which has been rarely reported in spectroscopic studies of neutral peptides.<sup>25</sup> Abo-Riziq *et al.*<sup>17</sup> reported that the  $\alpha$ -turn is formed in a pentapeptide FDASV, although the conformer is not the most stable one. They assigned the band at 3322 cm<sup>-1</sup> to  $\nu$ (NH) of the  $\alpha$ -turn. As for charged peptides, Stearns *et al.*<sup>29</sup> reported that alanine-rich polypeptide Ace-Phe-(Ala)<sub>10</sub>-Lys-H<sup>+</sup> has  $\alpha$ -helical structures and that the frequency of  $\nu$ (NH) in  $\alpha$ -helix is in a range of 3320–3350 cm<sup>-1</sup>. In the present study,  $\nu$ (NH<sub>Phe</sub>) is assigned to a band observed at 3371.7 cm<sup>-1</sup> (Fig. S20 and Table S5, ESI<sup>†</sup>), consistent with the reported value.

Another interesting HB is OH<sub>Ser1</sub>-CO<sub>Ace</sub>, found in f19375 of Ace-SIVSF-NHMe and f28623 of Ace-SIVSF-NH<sub>2</sub>.  $\nu$ (OH<sub>Ser1</sub>) is assigned to a weak band at 3223.7 cm<sup>-1</sup> in conformer X and to a sharp band at 3317.8 cm<sup>-1</sup> in conformer Q. The result suggests that these HBs are extremely strong, yielding a large red-shift relative to  $\nu$ (OH) of the free OH group ( $\sim$ 3600 cm<sup>-1</sup>). Note that OH<sub>Ser1</sub>-CO<sub>Ace</sub> forms a seven-membered ring analogous to the  $\gamma$ -turn. The  $\gamma$ -turn is well known to be a strong HB exhibiting a significant red shift of the amide A band, *i.e.*,  $\nu$ (NH).<sup>44</sup> On the other hand, the HB of the OH group and the backbone CO group is scarcely documented.<sup>25</sup> Abo-Riziq *et al.*<sup>17</sup> reported that the HB of serine OH<sub>*i*</sub> and CO<sub>*i-1*</sub> (*i* is the residue number) exhibited a red-shift of 210 cm<sup>-1</sup> in FDASV. The OH group of the C-terminal COOH should be able to form a seven-membered-ring HB with the backbone CO.<sup>25</sup> However, to our knowledge, the peak of such  $\nu$ (OH) has never been characterized. In Gly-Trp-COOH, the COOH group was suggested to be hydrogen bonded with the backbone CO, but the peak of  $\nu$ (OH) was not detected in the IR spectrum. The authors concluded that the peak was hidden in a broad band due to a strong HB.<sup>49</sup> The present study provides a clear-cut assignment of the OH stretching frequency of the OH group involved in seven-membered-ring HBs.

In the previous work,<sup>34</sup> conformer X and conformer Y were tentatively assigned to a31 and a3033 (we refer to the conformer ID in ref. 34 with prefix “a”) obtained by the geometry

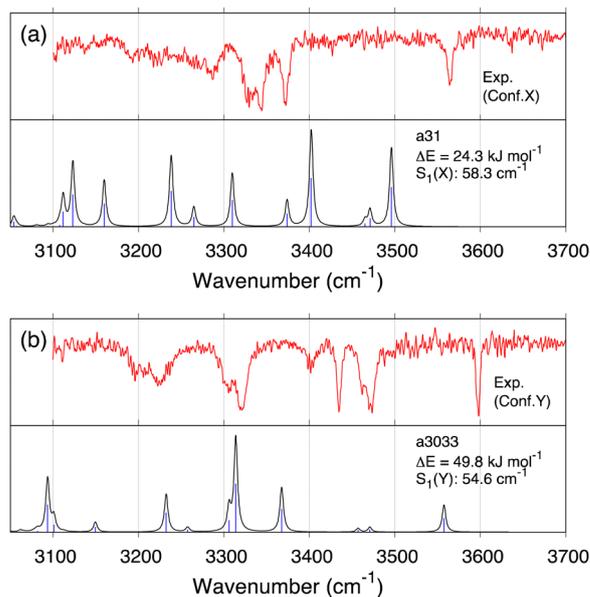


Fig. 8 VQDPT2 spectra of (a) a31 and (b) a3033 of Ace-SIVSF-NHMe compared with the experimental spectra.  $\Delta E$  (in kJ mol<sup>-1</sup>) is the relative energy from the most stable conformer (f19375) obtained at the RI-MP2/def2-TZVP(-df) level. The similarity scores  $S_1$  (in cm<sup>-1</sup>) with respect to conformer X and conformer Y are given as  $S_1(X)$  and  $S_1(Y)$ , respectively.

optimization and the harmonic vibrational calculation at the level of RI-B97-D3/TZVPP.<sup>50–54</sup> To compare with the present result, we re-optimized the geometry and computed the VQDPT2 spectrum of a31 and a3033 at the B3LYP/6-31(++)G\*\* level.

Fig. 8 shows the calculated IR spectra, similarity scores, and the relative energy of a31 and a3033. (The peak assignment is given in Fig. S23 and Tables S7, S8, ESI<sup>†</sup>) The calculated spectra agree poorly with the experimental ones, yielding  $S_1(X) = 58.3$  and  $S_1(Y) = 54.6$  cm<sup>-1</sup>. Furthermore, these conformers are unfavorable in terms of the energy as well. Therefore, the present calculation does not support the assignment of the previous work. We emphasize that the scaled harmonic spectra of a31 obtained by the RI-B97-D3/TZVPP method showed reasonable agreement with the experiment (see the ESI<sup>†</sup> of ref. 34), which was misleading. Nevertheless, both f19375 and a31 have  $\alpha$ -turn between NH<sub>Phe</sub>-CO<sub>Ser1</sub> (Fig. 7), which was the main finding about the atomistic structure of conformer X in the previous study.<sup>34</sup>

We now assess the quality of the DFT calculation used in this work, *i.e.*, B3LYP/6-31(++)G\*\*. The relative energies of the conformers of Ace-SIVSF-NHMe calculated at the B3LYP-D3/6-311(++)G(3df,3pd) level are compared with those obtained by various levels of electronic structure theory (Fig. S24, ESI<sup>†</sup>). Notably, f19375 is the most stable conformer, irrespective of the level of electronic structure calculations. However, the B3LYP/6-31(++)G\*\* level gives the lowest correlation coefficient of 0.75. Incorporating the dispersion correction<sup>53</sup> (B3LYP-D3/6-31(++)G\*\*) dramatically improves the coefficient to 0.99. The relative energy of low-energy conformers obtained by B3LYP and B3LYP-D3, shown in Fig. S25 (ESI<sup>†</sup>), suggests that some conformers agree well within 5 kJ mol<sup>-1</sup>, while others deviate

by more than 20 kJ mol<sup>-1</sup>. The structures of f19375, f389, and f21065 optimized by B3LYP and B3LYP-D3 are superimposed in Fig. S26 (ESI†). In f21065, B3LYP-D3 changes the orientation of the C-terminus and forms new HBs, thereby stabilizing the energy by more than 20 kJ mol<sup>-1</sup>. Therefore, incorporating the dispersion correction is generally crucial. Nevertheless, the structural change is little in the case of f19375 and f389 (RMSD = 0.30 and 0.45 Å, respectively). Since the effect of dispersion on the vibrational frequency is known to be minor,<sup>55,56</sup> the conformer assignment is valid with the use of B3LYP/6-31(++)G\*\* in this study.

Considering the large computational cost of anharmonic calculations, it is interesting to check the performance of similarity scores obtained from scaled harmonic frequencies and intensities, which are shown in Fig. S27 (ESI†). The minimum values of  $S_1$  are given by conformers f26549 ( $S_1(X) = 24.4$  cm<sup>-1</sup>) and f359 ( $S_1(Y) = 34.6$  cm<sup>-1</sup>). The values of  $S_1$  for f19375 and f389 (the assigned conformers) are found to be larger than these values:  $S_1(X) = 42.3$  cm<sup>-1</sup> and  $S_1(Y) = 34.8$  cm<sup>-1</sup>, respectively. Therefore, anharmonic calculations are required for a correct assignment of the conformers. Nevertheless, the similarity score obtained from the harmonic spectrum predicts the trend and thus can be used for selecting the candidate conformers for anharmonic calculations. For example, we checked the peak position of  $\nu(\text{OH}_{\text{ser}})$  by eye and rejected the conformers when they appeared in the wrong region. This step may be automated using the similarity score based on the harmonic results.

The present study demonstrates that the conventional conformational search of polypeptides based on the energetics may be imperfect, particularly, when multiple conformers are observed, because not only the most stable conformer(s) but also conformers that belong to a high energy basin can be produced in the experiment. The proposed scheme remedies the drawback by exploiting the structure-spectrum correlation. The grouping based on RMSD classifies the structural features, and the similarity score quantifies the agreement of theoretical and experimental spectra without a subjective point of view. Combined with enhanced sampling simulations (REMD) and anharmonic vibrational calculations (VQDPT2), these methods provide a general workflow to analyze the IR spectrum of large, complex systems, e.g., longer polypeptides and molecular complexes.

## Methods

### Similarity score

The comparison of experimental and theoretical spectra is crucial in spectroscopic studies to verify the validity of theory and interpret experiments. However, the comparison becomes difficult as the spectrum grows complex. To resolve this issue, Pendry<sup>57</sup> has proposed a factor that quantifies the agreement of two spectra. Pendry's reliability factor is widely used in low-energy electron diffraction (LEED). The factor has also been used to analyze the vibrational spectra of polypeptides.<sup>58,59</sup>

Following these works, we propose a score to evaluate the similarity of the two spectra. The score is obtained as follows.

(1) Obtain a set of frequency and intensity for each peak of the spectrum. We assume that the two spectra to be compared, spectrum-1 and spectrum-2, have  $N_1$  and  $N_2$  peaks, respectively. We can set  $N_1 \leq N_2$  without loss of generality. The intensities are normalized so that the maximum value in each spectrum is equal to one.

(2) Select  $N_1$  peaks from spectrum-2, which are compared with the  $N_1$  peaks of spectrum-1. The frequencies and intensities of spectrum-1 and 2 can be written as,

$$\left\{ \left( \omega_1^{(1)}, I_1^{(1)} \right), \left( \omega_2^{(1)}, I_2^{(1)} \right), \dots, \left( \omega_{N_1}^{(1)}, I_{N_1}^{(1)} \right) \right\}, \quad (1)$$

$$\left( \omega_1^{(1)} < \omega_2^{(1)} < \dots < \omega_{N_1}^{(1)} \right)$$

$$\left\{ \left( \omega_1^{(2)}, I_1^{(2)} \right), \left( \omega_2^{(2)}, I_2^{(2)} \right), \dots, \left( \omega_{N_1}^{(2)}, I_{N_1}^{(2)} \right) \right\}, \quad (2)$$

$$\left( \omega_1^{(2)} < \omega_2^{(2)} < \dots < \omega_{N_1}^{(2)} \right)$$

where  $\omega_k^{(j)}$  and  $I_k^{(j)}$  are the frequency and normalized intensity of the  $k$ -th peak of spectrum- $j$ .

(3) Calculate a score  $S_1$  defined as,

$$S_1 = \sqrt{\frac{1}{N_1} \sum_{k=1}^{N_1} \left\{ \left( \omega_k^{(2)} - \omega_k^{(1)} \right)^2 + \alpha^2 \left( I_k^{(2)} - I_k^{(1)} \right)^2 \right\}}, \quad (3)$$

where  $\alpha$  is a weight factor of the intensity. Note that  $S_1$  becomes sensitive to the difference in the intensity when  $\alpha$  is large, and *vice versa*. Quantitative prediction of IR intensities is more difficult than that of frequencies,<sup>60,61</sup> so that an optimal choice of  $\alpha$  is important for  $S_1$  to be useful. In this work, we used the spectra of Ace-SIVSF-NH<sub>2</sub> as a test set to validate the optimal value of  $\alpha$ , and found that  $\alpha = 50$  cm<sup>-1</sup> was an optimal choice (Section S1.4, ESI†).

(4) Steps 2 and 3 are iterated over all the combinations to choose  $N_1$  peaks out of  $N_2$  peaks. The number of combinations is equal to  $\binom{N_2}{N_1}$ . The combination with the lowest  $S_1$  is taken as the final value of  $S_1$ .

(5) Using the  $N_1$  peaks of spectrum-2 selected in step 4, we calculate another score  $S_2$  defined as,

$$S_2 = \sqrt{\left\langle \left( \omega^{(2)} - \omega^{(1)} \right)^2 \right\rangle - \left\langle \omega^{(2)} - \omega^{(1)} \right\rangle^2}, \quad (4)$$

which corresponds to a standard deviation of  $\omega_k^{(2)} - \omega_k^{(1)}$ . Note that  $S_2$  indicates the difference in the interval of the peaks rather than the difference in the frequency itself.

Note that the final assignment should be determined not only from the values of the scores  $S_1$  and  $S_2$ , but also with a visual inspection of the spectra. Because  $S_1$  and  $S_2$  are evaluated from a subset of the peaks of spectrum-2, it is important to check how the overall shape look alike.

In this study, we used the peak with the frequency higher than 3100 cm<sup>-1</sup> and intensity larger than 10.0 km mol<sup>-1</sup> to construct the set of peaks for VQDPT2 spectra. Note that VQDPT2 distributes the intensity of fundamental modes to many states that are dark in the harmonic approximation and

thus produces many peaks. As for the experimental spectrum, the frequencies and intensities are obtained by fitting the spectrum to Lorentz functions. Since the scores depend on the quality of the fitting of the experimental spectrum, small and broad bands need to be fitted carefully (Section S2, ESI†).

### Computational programs

The MD and REMD simulations were carried out using the NAMD software (version 2.9).<sup>62</sup> The geometry optimization and the harmonic vibrational analysis at the DFT level were carried out using Gaussian09.<sup>63</sup> The single point energy at the RI-MP2/def2-TZVP(-df) level was calculated using ORCA program package (version 3.0.3).<sup>64</sup> VQDPT2 calculation was carried out with SINDO program.<sup>65</sup> UCSF Chimera (version 1.12)<sup>66</sup> was used for molecular drawing. HB diagrams were drawn using Cytoscape (version 3.8.0).<sup>67</sup>

### Data availability

The data that support the findings of this study are openly available in the ESI† and Zenodo at <https://www.doi.org/10.5281/zenodo.7580818>. The script for evaluating the similarity scores can be found at <https://github.com/hotaki/similarity-score>.

### Author contributions

H. O.: data curation, formal analysis, funding acquisition, investigation, methodology, software, visualization, writing – original draft. S. I.: data curation, formal analysis, funding acquisition, investigation, visualization, writing – original draft. M. F.: conceptualization, funding acquisition, resources, supervision, writing – review & editing. Y. S.: conceptualization, funding acquisition, project administration, resources, supervision, writing – review & editing. K. Y.: funding acquisition, project administration, software, visualization, writing – original draft, review & editing.

### Conflicts of interest

There are no conflicts to declare.

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