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Dynamics studies for the multi-well and multi-channel reaction of OH with C₂H₂ on a full-dimensional global potential energy surface†

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The C₂H₂ + OH reaction is an important acetylene oxidation pathway in the combustion process, as well as a typical multi-well and multi-channel reaction. Here, we report an accurate full-dimensional machine learning-based potential energy surface (PES) for the C₂H₂ + OH reaction at the UCCSD(T)-F12b/cc-pVTZ-F12 level, based on about 475 000 *ab initio* points. Extensive quasi-classical trajectory (QCT) calculations were performed on the newly developed PES to obtain detailed dynamic data and analyze reaction mechanisms. Below 1000 K, the C₂H₂ + OH reaction produces H + OCCH₂ and CO + CH₃. With increasing temperature, the product channels H₂O + C₂H and H + HCCOH are accessible and the former dominates above 1900 K. It is found that the formation of H₂O + C₂H is dominated by a direct reaction process, while other channels belong to the indirect mechanism involving long-lived intermediates along the reaction pathways. At low temperatures, the C₂H₂ + OH reaction behaves like an unimolecular reaction due to the unique PES topographic features, of which the dynamic features are similar to the decomposition of energy-rich complexes formed by C₂H₂ + OH collision. The classification of trajectories that undergo different reaction pathways to generate each product and their product energy distributions were also reported in this work. This dynamic information may provide a deep understanding of the C₂H₂ + OH reaction.

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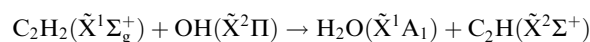
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1. Introduction

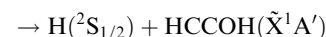
The dynamics investigation of the key elementary reactions in combustion processes can not only provide accurate dynamic data but also help in further exploration of the reaction mechanism, which is of great significance for the in-depth understanding of combustion processes. Acetylene is a major intermediate of most hydrocarbon flames and an important precursor of polycyclic aromatic hydrocarbons (PAHs) and soot.^{1–3} The reaction between C₂H₂ and OH is one of the main degradation pathways of acetylene and plays a key role in the

combustion process. Therefore, it is necessary to study the dynamics of the C₂H₂ + OH reaction in detail.

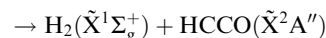
In the last sixty years, many works have focused on product analysis and rate coefficient determination of the C₂H₂ + OH reaction.^{4–34} Up to now, it is accepted that there are five major product channels:



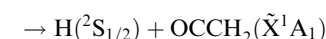
$$\Delta_r H_{298} = 14.1 \text{ kcal mol}^{-1} \quad (\text{P1})$$



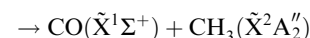
$$\Delta_r H_{298} = 10.9 \text{ kcal mol}^{-1} \quad (\text{P2})$$



$$\Delta_r H_{298} = -21.5 \text{ kcal mol}^{-1} \quad (\text{P3})$$



$$\Delta_r H_{298} = -22.7 \text{ kcal mol}^{-1} \quad (\text{P4})$$



$$\Delta_r H_{298} = -54.9 \text{ kcal mol}^{-1} \quad (\text{P5})$$

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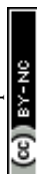
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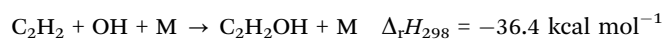
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Experimentally, the $\text{H}_2\text{O} + \text{C}_2\text{H}$ (P1) channel was first proposed in the acetylene–oxygen reaction mechanism and was found to be an important high-temperature direct reaction channel in subsequent other studies.^{5,7} Gehring *et al.* and Kanofsky *et al.* reported the product channels of $\text{CO} + \text{CH}_3$ (P5) and $\text{H} + \text{OCCH}_2$ (P4), respectively, by using the crossed molecular beam technique in combination with mass spectrometry for this reaction.^{6,9} Because hydroxyacetylene (HCCOH) and ketene (OCCH_2) have the same mass-to-charge ratio, the $\text{H} + \text{HCCOH}$ (P2) channel was finally determined with the help of theoretical calculations.²⁹ Currently, the P1, P2, P4, and P5 channels and the association reaction (M is a third body involved in energy transfer)



are commonly used in combustion models to describe the $\text{C}_2\text{H}_2 + \text{OH}$ reaction, without considering the $\text{H}_2 + \text{HCCO}$ (P3) channel. The possibility of $\text{H}_2 + \text{HCCO}$ (P3) production was first suggested by Breen and Glass,⁷ but this has not been found in other product analysis experiments.

In terms of reaction rates, the reactions between acetylene and hydroxyl radicals are dominated by electrophilic addition association reactions at low temperatures, and the reaction rates exhibit a strong pressure dependence.^{8,11–14,17,20,27} The pressure dependence arises mostly from the competition of collisional relaxation of nascent energy-rich complexes against prompt unimolecular reactions such as isomerization or decomposition.³⁵ Smith *et al.* measured the rate coefficient for the $\text{C}_2\text{H}_2 + \text{OH}$ reaction at 900, 1100, and 1300 K over a

pressure range from 10 to 120 torr and found it to be pressure-dependent at 900 K and pressure-independent at 1100 and 1300 K, which is probably due to the contribution of the association reaction decreases at high temperatures.¹⁷ At high temperatures, the rate coefficient typically shows an Arrhenius-type temperature dependence.^{17,20,26,27}

In theory, several theoretical groups have performed *ab initio* calculations of $\text{C}_2\text{H}_2 + \text{OH}$ for several reaction pathways.^{28–31,36–42} Based on the BAC-MP4 (bond-additivity-corrected Möller–Plesset fourth-order perturbation theory) level of theory, Miller and Melius used statistical-theoretical methods to calculate rate coefficients.²⁹ Senosiain *et al.* calculated the *ab initio* energies of reaction pathways in the RQCISD(T) (restricted quadratic configuration-interaction method with single, double, and perturbative triple excitations) method, then used the master equations (ME) to calculate the rate coefficients and product branching ratios.³⁰ Nonetheless, the detailed microscopic dynamics of the $\text{C}_2\text{H}_2 + \text{OH}$ reaction, including the energy transfer process, have not been studied yet.

In this work, aimed at a better understanding of the dynamical characterization of this important elementary reaction in combustion, extensive quasi-classical trajectory (QCT) calculations have been performed on a newly developed potential energy surface (PES). The accurate full-dimensional PES for the ground doublet state of the $\text{C}_2\text{H}_2 + \text{OH}$ reaction is constructed using the permutation invariant polynomial-neural network (PIP-NN) method^{43,44} based on approximately 475 000 *ab initio* energies calculated at the UCCSD(T)-F12b/cc-pVTZ-F12 level of theory, covering all possible product channels that can

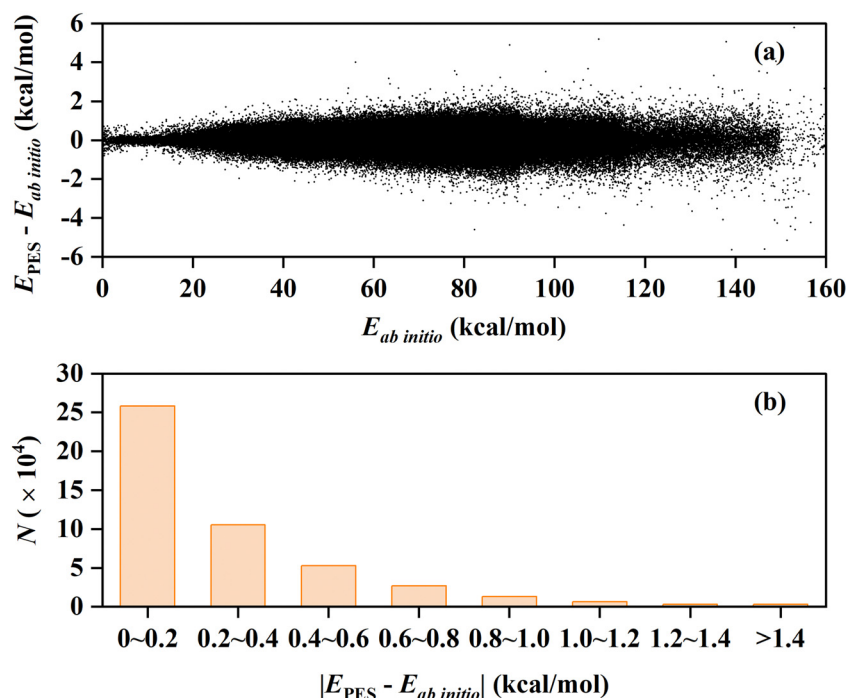


Fig. 1 (a) Fitting errors of all the data points in the PIP-NN PES as a function of their corresponding *ab initio* energies. (b) Distribution of the absolute fitting errors for all the data points.



be reached below 3000 K. The dynamic information and the comprehensive reaction mechanisms would greatly expand our understanding of other multi-well and multi-channel reactions. The paper is organized as follows. Section II presents the details of the PES and QCT calculations. The PES characterization and the dynamical results are shown in Section III. Finally, conclusions are given in Section IV.

II. Methods

A. Potential energy surface

The *ab initio* calculations employed the explicitly correlated unrestricted coupled cluster using the single, double, and perturbative triple excitations (UCCSD(T)-F12b) method^{45,46} here. The specially optimized correlation consistent basis sets (cc-pVnZ-F12 ($n = \text{D, T, and Q}$))⁴⁷ were tested. We compared the *ab initio* energies of different basis sets at various stationary points, as shown in Table S1 (ESI[†]), where the single point calculations for all methods were performed on the optimized geometries obtained from the UCCSD(T)-F12b/cc-pVTZ-F12 method. The energies obtained from the cc-pVTZ-F12 basis set exhibit good consistency with those derived from the larger basis set (aug-cc-pV5Z),⁴⁸ with energy differences less than 0.25 kcal mol⁻¹ for all stationary points. For 6-core parallel computation, a single point calculation using this method takes about 8 minutes, which is 1/5 of the cost of the cc-pVQZ-F12 basis set. Hence, the cc-pVTZ-F12 basis set was chosen to calculate the potential energies for selected points.

In coupled-cluster methods, the T_1 diagnostic is seen as an indication of the importance of nondynamical electron correlations, with a large T_1 value indicating the need for a multi-reference electron correlation treatment.⁴⁹ For this system, the T_1 value for most data points is small (below 0.05) in the entire configuration space. We also examined the shape of the PES in important regions along the minimal energy path (MEP), which is smooth and continuous, as shown in Fig. S1 (ESI[†]). Those very few points with T_1 diagnostic values larger than 0.05 were discarded to get a more reliable *ab initio* data set. All the electronic structure calculations were performed using the MOLPRO 2015.1.0 program package.⁵⁰

An appropriate sampling process is very helpful for constructing a high-dimensional global PES. We first selected an initial set of points by performing Born–Oppenheimer molecular dynamics (BOMD) simulations at the UB3LYP/6-31G level of theory^{51,52} using the Gaussian 16 package.⁵³ Based on these energy points calculated at the UCCSD(T)-F12b/cc-pVTZ-F12 level, a primitive PES was fitted using the PIP-NN approach.^{43,44} Then, a large number of trajectories with different initial conditions were carried out on that PES to further explore the dynamic important configuration space and select more points to improve the PES according to both the distance and energetic criteria. The generalized Euclidean distance was used to describe the similarity degree

of data points in configuration space, which is defined as $\chi =$

$$\sqrt{\sum_{i=1}^{15} |r_i - r'_i|^2}$$

between a new point and a data point in the existing

data set, in which r_i or r'_i is the distance between every two atoms. Those points with $\chi \leq 0.2 \text{ \AA}$ were not selected for the data set. After many iterations of adding points, finally, 477 821 points covering all the dynamical-relevant regions were selected to construct the final PES.

The essence of the PIP-NN method is to use the symmetry functions of internuclear distances instead of the coordinates as the input vector in NN fitting.^{43,44} The PIP symmetric functions can be obtained by monomial symmetrization as the form $X = \hat{S} \prod_{i < j}^6 p_{ij}^{l_{ij}}$, from Morse-like variables of internuclear distances $p_{ij} = \exp(-r_{ij}/\alpha)$ with r_{ij} as the internuclear distances and $\alpha = 2.0$ bohr, where i and j denote atoms and the order is CCHHHO.⁵⁴ l_{ij} is the degree of p_{ij} , and \hat{S} contains all symmetrization operators for the $\text{A}_2\text{B}_3\text{C}$ molecule. In total, 134 symmetrized polynomials under the maximum degree 3 for the $\text{C}_2\text{H}_3\text{O}$ system were used as the input layer of NN.

The standard forward-feed NN functional form can be written as

$$y = b_1^{(3)} + \sum_{k=1}^K w_{1,k}^{(3)} \cdot f_2[b_k^{(2)} + \sum_{j=1}^J w_{k,j}^{(2)} \cdot f_1(b_j^{(1)} + \sum_{i=1}^I w_{j,i}^{(1)} \cdot x_i)], \quad (1)$$

where I is the number of PIPs in the input layer; J and K are the numbers of the neurons of the first and second hidden layers, $w_{j,i}^{(1)}$, $w_{k,j}^{(2)}$, and $w_{1,k}^{(3)}$ are the weights connecting neighboring layers, $b_j^{(1)}$, $b_k^{(2)}$, and $b_1^{(3)}$ are the bias of each layer, and f_1 and f_2 are the transfer functions (hyperbolic tangent function) for the two hidden layers. The architecture of the NN employed for our PES is 134-60-70-1, resulting in 12 441 parameters. In each NN fitting, the database was randomly divided into the training (96%) and validation (4%) sets. The training data were fitted using the Levenberg–Marquardt algorithm,⁵⁵ and the “early stopping” method⁵⁶ was used to avoid overfitting. The root mean square error (RMSE) defined as

$$\text{RMSE} = \sqrt{\sum_{i=1}^{N_{\text{data}}} (E_i^{\text{PES}} - E_i^{\text{ab initio}})^2 / N_{\text{data}}}, \quad (2)$$

was used to evaluate the fitting performance. The complex reaction pathways and large energy range for this hexatomic system make the PES fitting more complicated than that of a simple polyatomic system. To further reduce random errors, the final PES was averaged as the three best PESs with RMSEs of 0.47/0.73, 0.45/0.79, and 0.48/0.89 kcal mol⁻¹ for the training/validation sets, respectively. The final averaged PES yields an overall RMSE of 0.38 kcal mol⁻¹.

B. Quasi-classical trajectory calculations

The dynamic calculations were performed at several temperatures of 298, 500, 1000, 1500, 2000, 2500, and 3000 K, respectively, using the QCT method as implemented in the VENUS code.^{57,58} The maximum impact parameter b_{max} was set as 4.0 Å for all temperatures after testing. The impact parameter b for each trajectory was selected randomly from $b_{\text{max}}\sqrt{r}$, where r is a



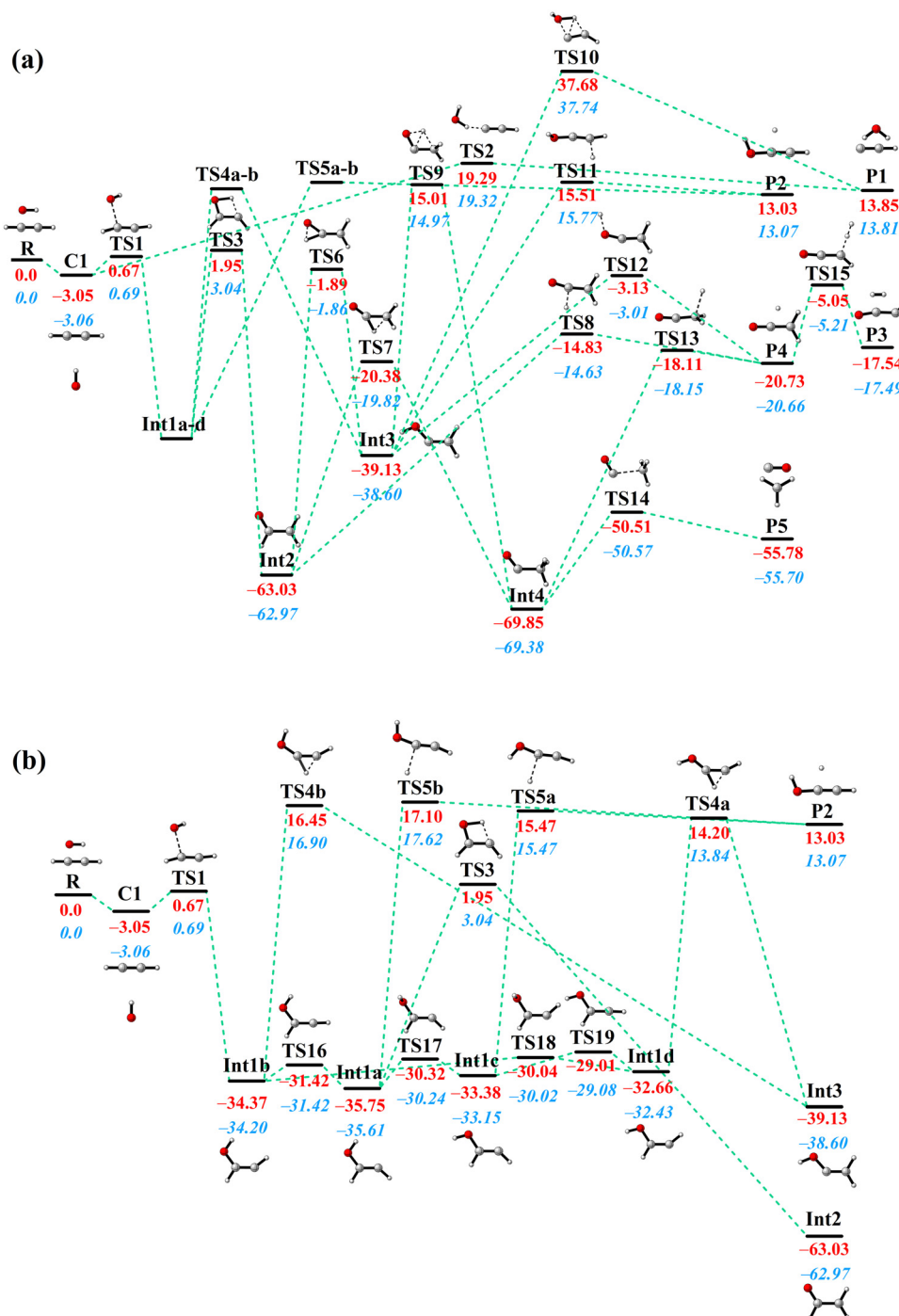


Fig. 2 Schematic illustration of the $\text{C}_2\text{H}_2 + \text{OH}$ reaction including geometries and relative energies of all stationary points on the PIP-NN PES. Panel (b) presents detailed information of the Int1 region in (a). All energies are in kcal mol^{-1} , relative to the reactant asymptote. The values in red and blue italics represent the energies from PIP-NN PES and the corresponding *ab initio* results, respectively.

uniform random number between 0 to 1. At each temperature above, a large number (400 000–4000 000) of trajectories were run on the PIP-NN PES, to make sure that the statistical error $\Delta = [(N_{\text{total}} - N_r)/(N_{\text{total}}N_r)]^{1/2}$ was reasonably small enough. The time step was selected to be 0.1 fs to guarantee convergence of total energy in the propagation. The trajectories were initiated at distances of 10.0 Å between reactants and stopped when the

products reached a separation of 8.0 Å or reactants were separated by 13.5 Å. A few trajectories that failed to converge total energy within 0.01 kcal mol^{-1} or propagated for too long a time (> 5.0 ns) were discarded. It should be noted that in QCT, the molecules involved in the reaction have approximately quantized energies in the initial ro-vibrational state, but not in the final state. To mitigate the zero-point energy (ZPE)



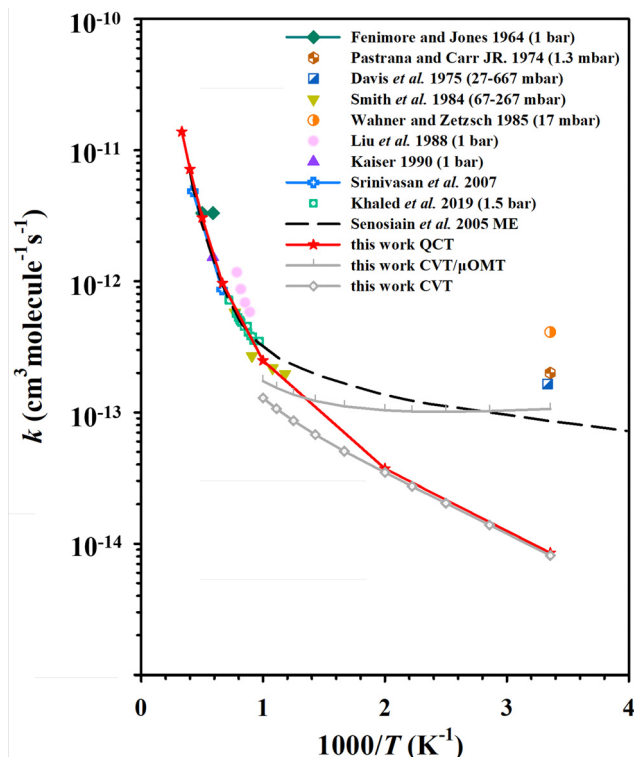


Fig. 3 The rate coefficients for the $C_2H_2 + OH$ reaction, compared with previous experimental^{4,10,11,17,20–22,26,27,33} and theoretical³⁰ results.

leakage problem, we applied a “passive” method⁵⁹ in this work, which is to remove the reactive trajectories where the sum of the vibrational energies is smaller than the total ZPE for all products. In the previous investigation for the $O(^3P) + CH_4$ reaction, QCT results corrected by this approach are closer to the corresponding quantum mechanical cross sections.⁶⁰

The thermal rate coefficients were calculated according to the following formula:

$$k(T) = g_e \left(\frac{8k_B T}{\pi \mu} \right)^{1/2} \pi b_{\max}^2 \frac{N_r}{N_{\text{total}}} \quad (3)$$

in which k_B is the Boltzmann constant and μ is the reduced mass of reactants, namely $\mu = m_{C_2H_2} m_{OH} / (m_{C_2H_2} + m_{OH})$. N_r and N_{total} are the numbers of reactive and total effective trajectories.

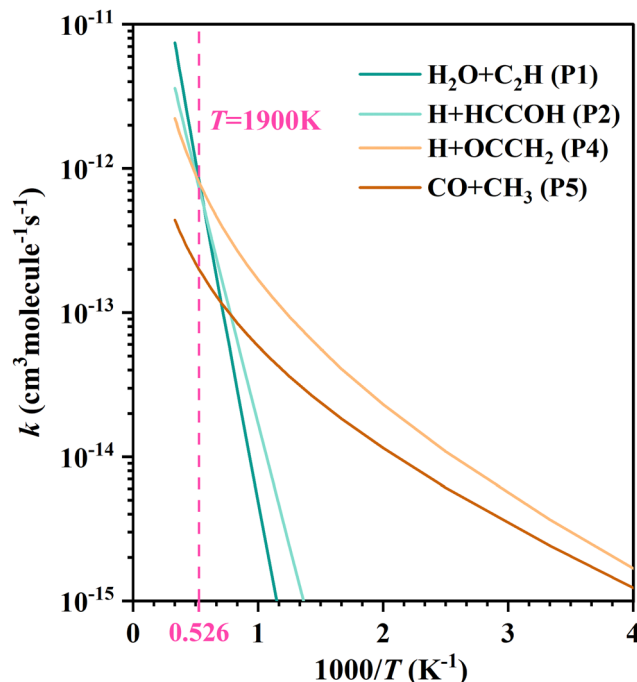


Fig. 4 The fitted curves by the modified Arrhenius expression for each product channel in the $C_2H_2 + OH$ reaction.

The electronic partition function factor for the spin–orbit states of OH^{61} was used to obtain the electronic degeneracy factor, $g_e = 2/[2 + 2\exp(-139.21 \text{ cm}^{-1}/k_B T)]$.

The scattering angle θ was given by $\theta = \cos^{-1} \left(\frac{\vec{v}_i \cdot \vec{v}_f}{|\vec{v}_i| |\vec{v}_f|} \right)$, where \vec{v}_i and \vec{v}_f represent the initial and final relative velocities, respectively, and are denoted as

$$\vec{v}_i = \vec{v}_{C_2H_2} - \vec{v}_{OH}, \quad \vec{v}_{f1} = \vec{v}_{C_2H} - \vec{v}_{H_2O}, \quad \vec{v}_{f2} = \vec{v}_{HCCOH} - \vec{v}_H,$$

$$\vec{v}_{f3} = \vec{v}_{HCCO} - \vec{v}_{H_2}, \quad \vec{v}_{f4} = \vec{v}_{OCCH_2} - \vec{v}_H \quad \text{and} \quad \vec{v}_{f5} = \vec{v}_{CO} - \vec{v}_{CH_3}.$$

III. Results and discussion

A. Potential energy surface

In this work, we constructed a new PES for the $C_2H_2 + OH$ reaction at the UCCSD(T)-F12b/cc-pVTZ-F12 level of theory. The new PES covered the reactant channel, five product channels,

Table 1 The QCT rate coefficients ($\text{cm}^3 \text{ molecule}^{-1} \text{ s}^{-1}$) together with the corresponding modified Arrhenius expressions for each product channel and the product branching ratios (BR) for the $C_2H_2 + OH$ reaction

T (K)	298	500	1000	1500	2000	2500	3000
k_{total}	8.52×10^{-15}	3.72×10^{-14}	2.49×10^{-13}	9.68×10^{-13}	3.06×10^{-12}	7.18×10^{-12}	1.39×10^{-11}
$H_2O + C_2H$ (P1)	BR	0	3.13%	16.28%	35.92%	48.12%	53.64%
	k_{P1}	4.085×10^{-12}	$T^{0.4995} \exp(-10197.5/T)$				
$H + HCCOH$ (P2)	BR	0	7.39%	22.77%	25.16%	27.00%	26.79%
	k_{P2}	4.085×10^{-12}	$T^{0.2997} \exp(-7559.8/T)$				
$H_2 + HCCO$ (P3)	BR	0	0	0	0	0.02%	0.12%
$H + OCCH_2$ (P4)	BR	65.69%	66.54%	62.50%	47.13%	30.95%	20.75%
	k_{P4}	4.085×10^{-19}	$T^{1.9635} \exp(-629.5/T)$				
$CO + CH_3$ (P5)	BR	34.31%	33.46%	26.99%	13.83%	7.97%	4.10%
	k_{P5}	4.085×10^{-18}	$T^{1.4726} \exp(-605.4/T)$				

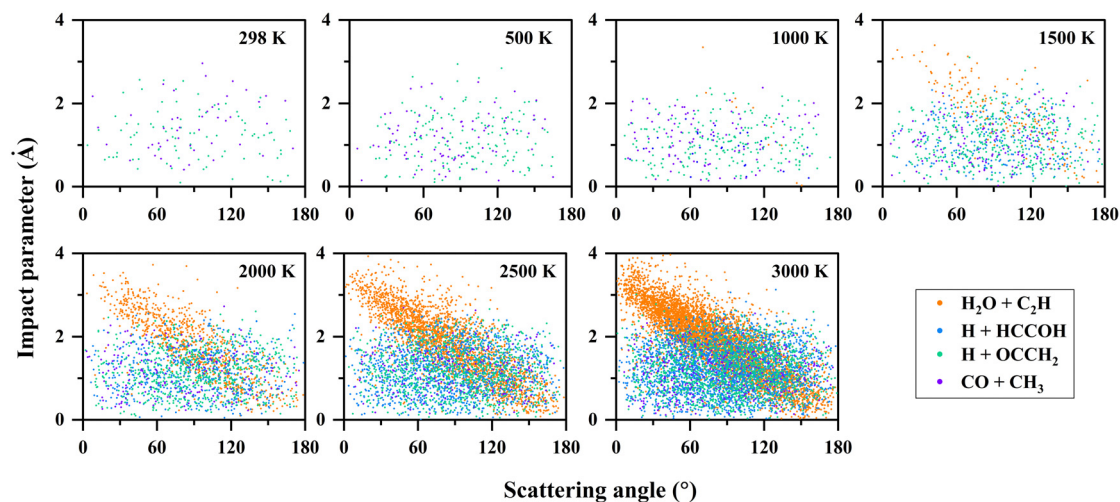


Fig. 5 Correlation diagrams between the scattering angle and the impact parameter for the $\text{C}_2\text{H}_2 + \text{OH}$ reaction at different temperatures.

and the interaction regions with many deep potential wells and transition states, with a total RMSE of $0.38 \text{ kcal mol}^{-1}$. The fitting errors of all the data points and their distribution are presented in Fig. 1(a) and (b). About 55.1% of all points are fitted well with a quite small absolute fitting error of $0\text{--}0.2 \text{ kcal mol}^{-1}$, especially the points with potential energy lower than $100 \text{ kcal mol}^{-1}$. The fitting performance is reasonably

good for such a complex system involving six atoms and covering the quite large energy range of $0\text{--}160 \text{ kcal mol}^{-1}$ with respect to the global minimum.

All stationary points along the MEP on the PIP-NN PES with their energies optimized by using the POLYRATE 17-C software⁶² are shown in Fig. 2. The $\text{C}_2\text{H}_2 + \text{OH}$ reaction consists of seven intermediates, twenty-one transition states, and a van

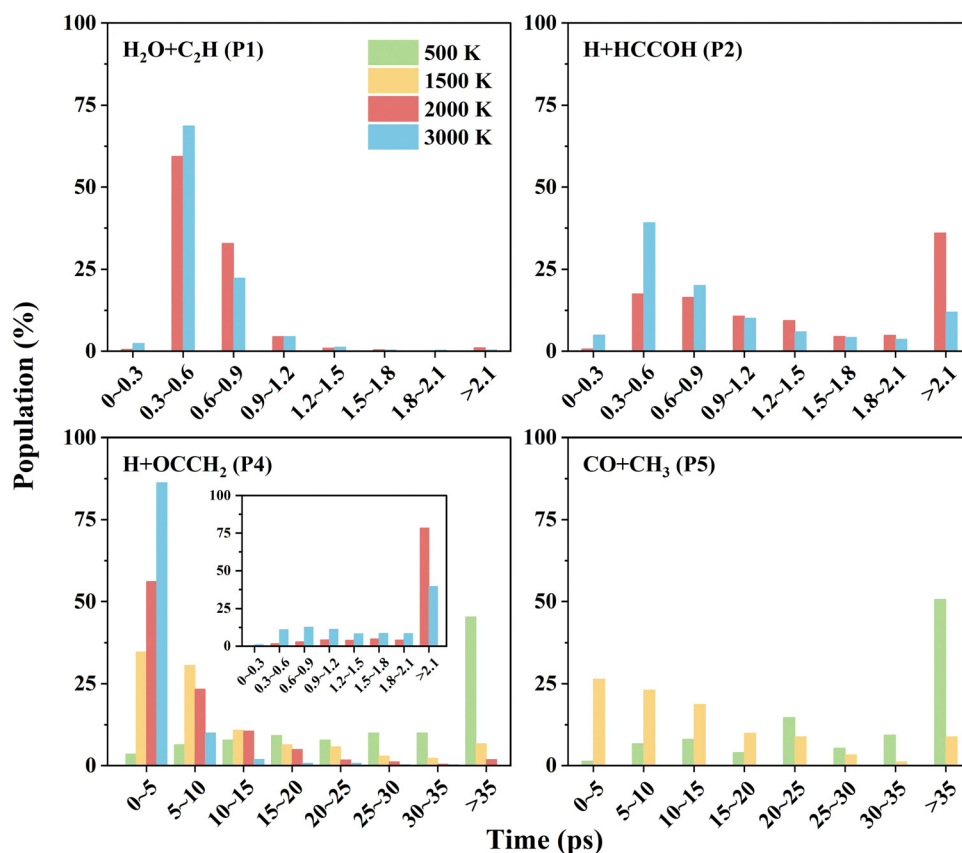


Fig. 6 The propagation time distributions for different product channels of the $\text{C}_2\text{H}_2 + \text{OH}$ reaction.



der Waals complex. The pre-reactive van der Waals complex is T-shaped, in which the hydrogen atom of the hydroxyl radical associates with the middle of the $\text{C}\equiv\text{C}$ triple bond. This configuration has been reported before, where the distance between the hydrogen atom of OH radical and the middle of the $\text{C}\equiv\text{C}$ triple bond is 2.371 Å at the UB3LYP/6-311++G(d,p) level,³⁰ 2.420 Å at the CBS-QB3 level,^{39,42} and 2.347 Å in this work with a slightly deeper depth than before. With the oxygen atom in the OH radical getting closer to one of the C atoms in acetylene, the complex strides TS1 and then forms the most

important intermediate Int1 in this reaction. Int1 has four conformers (Int1a, Int1b, Int1c, and Int1d) which are connected by small isomerization barriers, as shown in Fig. 2(b). In the subsequent process, different kinds of H-migration barriers and dissociation barriers lead to different pathways. It is important to point out that the reactants also have the option of taking a direct pathway, in which they overcome a high energy barrier (TS2) to yield H_2O and C_2H (P1). The high barrier height (19.3 kcal mol⁻¹) makes this direct hydrogen abstraction process possible only at high temperatures. As for

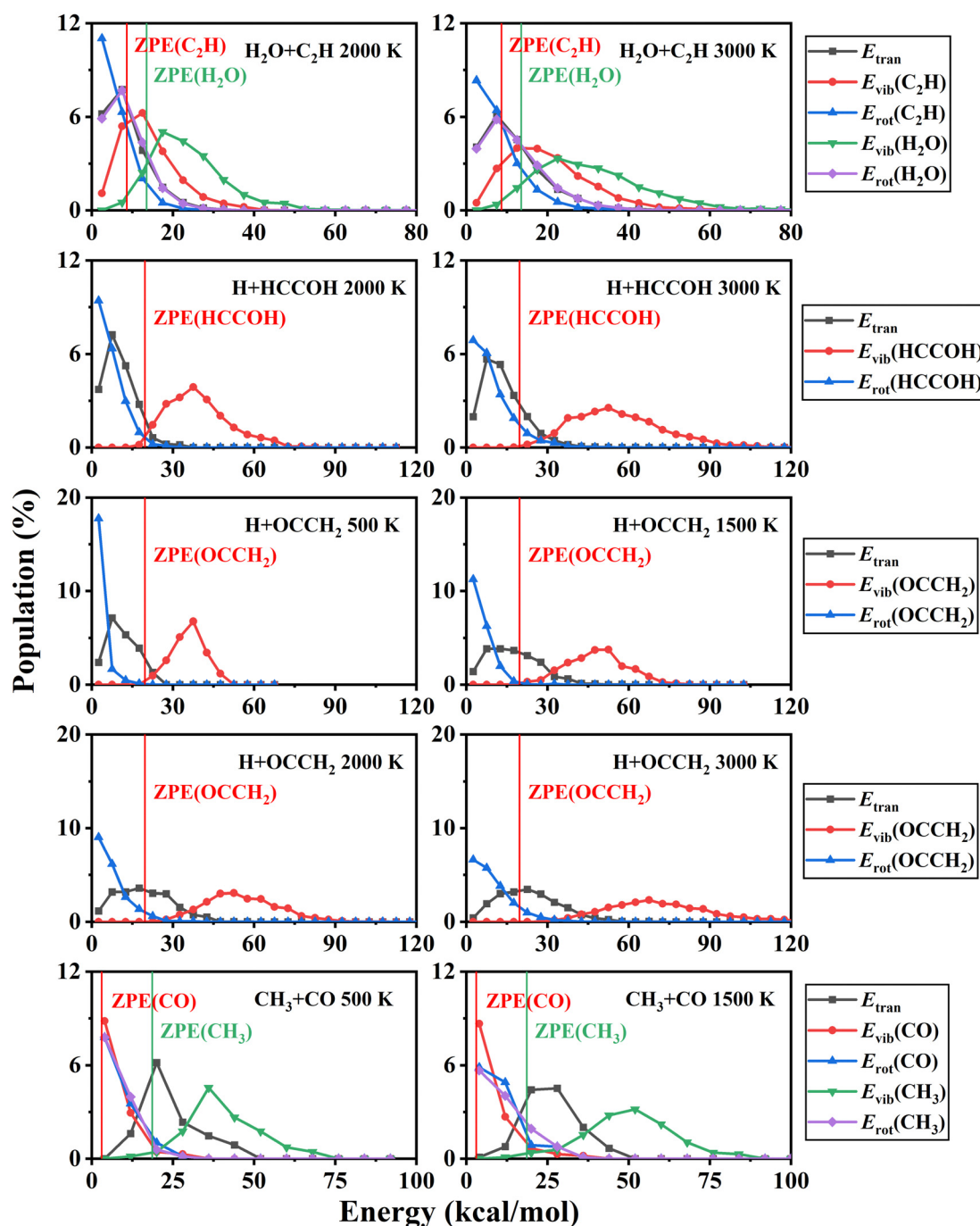


Fig. 7 The product energy distributions for the $\text{C}_2\text{H}_2 + \text{OH}$ reaction at different temperatures.



the formation of $\text{H}_2 + \text{HCCO}$ (P3), there have been discrepancies in previous studies. Senosiain *et al.* reported a $\dots \rightarrow \text{Int3} \rightarrow \text{TS} \rightarrow \text{P3}$ pathway,³⁰ while others reported $\dots \rightarrow \text{P4} \rightarrow \text{TS} \rightarrow \text{P3}$.^{31,36,38} On our PES, the latter mechanism from P4 to P3 was found and connected by TS15 while the former pathway was not found.

Fig. S1 (ESI†) shows a comparison of potential energies between *ab initio* calculations and fitted results from the PES for the MEs. The energies obtained on the PES are in agreement with those from the *ab initio* calculations. The detailed geometrical parameters and harmonic frequencies for each stationary point are presented in Fig. S2 and Table S2 (ESI†), respectively. The small differences in some flexible coordinates such as dihedral angles may be due to the difficulty in fitting the PES. Fortunately, in those regions, the differences between the *ab initio* energies and the PES values are small and would have little effect on the QCT results.

B. Rate coefficients and branching ratios

Standard QCT calculations were carried out on the PIP-NN PES at temperatures ranging from 298 K to 3000 K, and the statistical errors are less than 9% at 298 K and 500 K, and less than 6% above 1000 K. More than 99.8% of trajectories conserved energy within the criterion of $0.01 \text{ kcal mol}^{-1}$, which implied that the PES is smooth and free of discontinuity. Fig. 3 shows the rate coefficients of the QCT calculations for the $\text{C}_2\text{H}_2 + \text{OH}$ reaction compared to experimental data^{4,10,11,17,20–22,26,27,33} and theoretical calculations³⁰ in the literature. Above 1000 K, the QCT results agree well with most experimental measurements, and the rate coefficients exhibit a typical Arrhenius-type temperature dependence. At low temperatures ($< 1000 \text{ K}$), the QCT rate coefficients are lower than the previous low-pressure experimental results. The rate coefficients calculated by Miller and Melius²⁹ were not shown in this work because the *ab initio* accuracy in their work is

relatively low. Another previous theoretical work on this rate coefficient is the ME calculations of Senosiain *et al.*, in which asymmetric Eckart barriers were employed to compute the effect of tunneling through the reaction barriers.³⁰ Their ME data shown in Fig. 3 is the total rate coefficients in the zero-pressure limit, which agreed well with many experiments and our QCT results above 1000 K, and slightly lower than the experimental values but higher than ours at room temperature.

The key feature of the $\text{C}_2\text{H}_2 + \text{OH}$ PES is that, at low temperatures, the MEs for product formation have two roughly isoenergetic barriers (TS1 and TS3), with a deep potential well (Int1a-d) between the barriers $\sim 34 \text{ kcal mol}^{-1}$ below the reactant energy. As a result, the complex will stay in this potential well for a long time, allowing the collisional relaxation of nascent energy-rich complexes to occur, which is similar to the dynamics of the $\text{HO} + \text{CO} \rightarrow \text{H} + \text{CO}_2$ reaction.⁶³ At 298 K, 0.014% QCT trajectories propagate longer than 100 ps (as a footnote, unlike this, most of the direct reaction trajectories ($\text{R} \rightarrow \text{TS2} \rightarrow \text{P1}$) have propagation times less than 1 ps), with values of 0.021% at 500 K and 0.015% at 1000 K. For comparison, the ratios of reactive trajectories to total trajectories at these temperatures are 0.0033% (298 K), 0.012% (500 K) and 0.063% (1000 K). From the difference between these, it can be seen that at 298 K, the fraction of long-time non-reactive trajectories in the total number of trajectories is significantly higher than the fraction of reactive trajectories. The significant fraction of long-time non-reactive trajectories suggests the reason why collisional relaxation processes have a large impact on the reaction rates under different pressure conditions. In experiments, the $\text{C}_2\text{H}_2 + \text{OH}$ rate coefficients are generally determined by measuring the rate of the depletion of reactant, which is the sum of the bimolecular product formation rate and the association reaction rate. Our QCT calculations are simulations of the bimolecular reaction, and

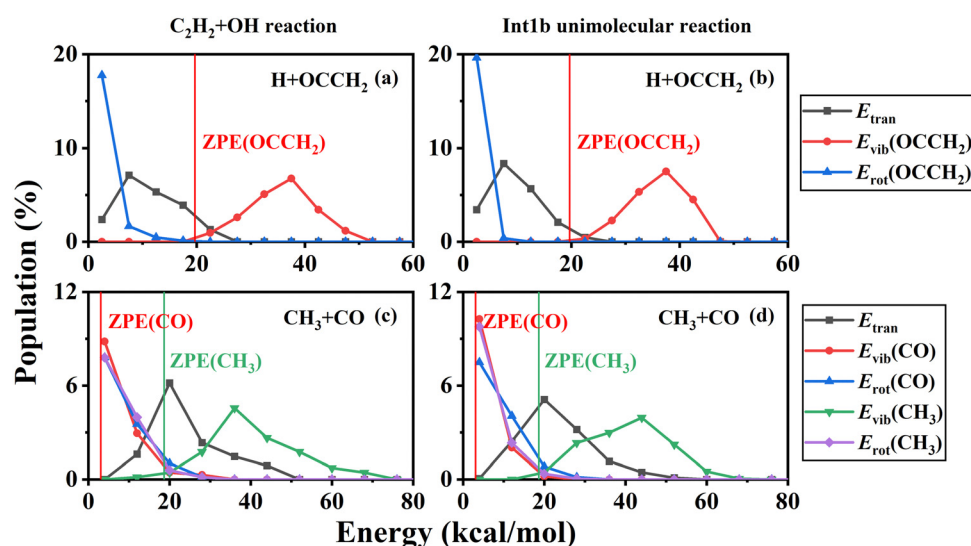


Fig. 8 The product energy distributions of the $\text{H} + \text{OCCH}_2$ (a) and $\text{CO} + \text{CH}_3$ (c) channels for the $\text{C}_2\text{H}_2 + \text{OH}$ reaction at 500 K, compared with the results of the $\text{H} + \text{OCCH}_2$ (b) and $\text{CO} + \text{CH}_3$ (d) channels for unimolecular reactions with fixed total energies at the maximum probability of the total energy distribution at 500 K.



the collisional relaxation process with a third body cannot be taken into account. Thus, in the QCT results, the unconsidered association reaction rates may be one of the reasons for the discrepancy at low temperatures.

Another reason for the underestimation of the rate coefficient is that the QCT method does not consider quantum effects, such as tunneling which can allow the long-lived complexes to penetrate through barriers, thus leading to more products eventually. To estimate the influence of tunneling on the $\text{C}_2\text{H}_2 + \text{OH}$ rate coefficients, we employed the micro-canonical optimized multidimensional tunneling (μOMT) approach.⁶⁴ In the temperature regime 298–1000 K, especially below 500 K, the reaction occurs mainly through the $\text{R}(\rightarrow\text{C1}) \rightarrow \text{TS1} \rightarrow \text{Int1a-d} \rightarrow \text{TS3} \rightarrow \text{Int2} \rightarrow \text{TS8} \rightarrow \text{P4}$ and $\text{R}(\rightarrow\text{C1}) \rightarrow \text{TS1} \rightarrow \text{Int1a-d} \rightarrow \text{TS3} \rightarrow \text{Int2} \rightarrow \text{TS7} \rightarrow \text{Int4} \rightarrow \text{TS14} \rightarrow \text{P5}$ pathways, forming $\text{H} + \text{OCCH}_2$ (P4) and $\text{CO} + \text{CH}_3$ (P5), respectively. In both pathways, TS3 is the highest potential barrier for both pathways and is therefore an important reaction bottleneck at low temperatures. For applying canonical variational transition-state theory (CVT)⁶⁵ combined with the μOMT approach,⁶⁴ we chose this highest TS as the dividing surface, and roughly estimated the overall reaction rate, omitting the recrossing among wells. The CVT/ μOMT and CVT rate coefficients calculated using the POLYRATE 17-C software⁶² are also presented in Fig. 3. The difference between the two results suggests that the hydrogen migration process in TS3 may be affected by significant tunneling effects. Indeed, the tunneling correction given by CVT/ μOMT is as large as over 10 below 300 K. One should note that both the previous ME work³⁰ and current CVT/ μOMT calculations can only treat quantum tunneling effects approximately. A better way to investigate the rate coefficients of the $\text{C}_2\text{H}_2 + \text{OH}$ reaction by including the quantum tunneling is to employ the ring polymer molecular dynamics (RPMD) method.^{66–70}

For each product channel, the product branching ratios and modified Arrhenius expressions are given in Table 1. To see more intuitively the variation of the product branching ratio with temperature, we compared the fitted curves of the rate coefficients for each product channel in Fig. 4. Below 1000 K, the $\text{C}_2\text{H}_2 + \text{OH}$ reaction mainly produces $\text{H} + \text{OCCH}_2$ (P4) and $\text{CO} + \text{CH}_3$ (P5), where the production of ketene (OCCH_2) is the predominant channel. At temperatures above 1000 K, the $\text{H}_2\text{O} + \text{C}_2\text{H}$ (P1) and $\text{H} + \text{HCCOH}$ (P2) channels open up and contribute significantly. Higher than 1900 K, the $\text{H}_2\text{O} + \text{C}_2\text{H}$ (P1) becomes dominant. The production of $\text{H}_2 + \text{HCCO}$ (P3) can be negligible in all the aforementioned temperature regions.

C. Mechanism analysis and product energy distribution

To further understand the reaction mechanism, an analysis of the trajectories and product information was performed. The correlation between the scattering angle and the impact parameter is shown in Fig. 5. In the $\text{H}_2\text{O} + \text{C}_2\text{H}$ (P1) channel, there is a correlation between the scattering angle and the impact parameter. The reaction exhibits a “rebound” mechanism when the impact parameter is small, and a “stripping” mechanism when the impact parameter is large, which is usually seen

in direct reactions. It was found that $\text{H}_2\text{O} + \text{C}_2\text{H}$ (P1) was produced dominantly by the direct hydrogen abstraction pathway ($\text{R} \rightarrow \text{TS2} \rightarrow \text{P1}$) with a ratio of 96% at 2000 K, and 94% at 3000 K. These direct trajectories also present a distinct feature in propagation time (see Fig. 6), namely, the distribution of their propagation time is concentrated, mainly in the range of 0.3–1.2 ps.

For the other channels, there is no clear correlation between the scattering angle and the impact parameter, and they all present a uniform distribution corresponding to a “long-lived complex” mechanism. The propagation time of such reaction trajectories is widely distributed, with very long propagation time at low temperatures (see Fig. 6). By determining whether certain intermediates are formed in the reaction, we can roughly classify the reaction pathways, where the intermediates are identified by the geometric parameters defined in Table S3 (ESI[†]). As for the $\text{H} + \text{HCCOH}$ (P2) channel, the trajectories can be divided into two types of pathways: $\dots \rightarrow \text{Int1a-d} \rightarrow \text{TS5a-b} \rightarrow \text{P2}$ and $\dots \rightarrow \text{Int3} \rightarrow \text{TS11} \rightarrow \text{P2}$. The fractions of trajectories passing through the two pathways are 75% and 25% at 2000 K, and 67% and 33% at 3000 K. The former is slightly more significant on the whole. In the $\text{H} + \text{OCCH}_2$ (P4) channel, the dominant pathway changes with increasing temperature. At 500 K, about 95% of the product is generated by the $\dots \rightarrow \text{Int2} \rightarrow \text{TS8} \rightarrow \text{P4}$ pathway, and it becomes 61% as the temperature increases to 1500 K, with the rest passing through the $\dots \rightarrow \text{Int3} \rightarrow \text{TS12} \rightarrow \text{P4}$ pathway. At 3000 K, the fractions for the $\dots \rightarrow \text{Int2} \rightarrow \text{TS8} \rightarrow \text{P4}$ and $\dots \rightarrow \text{Int3} \rightarrow \text{TS12} \rightarrow \text{P4}$ pathways are 39% and 57%. The $\dots \rightarrow \text{Int4} \rightarrow \text{TS13} \rightarrow \text{P4}$ pathway is an insignificant one for the $\text{H} + \text{OCCH}_2$ (P4) channel, with a contribution of less than 3% at different temperatures. In the $\text{CO} + \text{CH}_3$ (P5) channel, the differences in pathways are mainly reflected in the Int4 formation, where the $\dots \rightarrow \text{Int2} \rightarrow \text{TS7} \rightarrow \text{Int4} \rightarrow \text{TS14} \rightarrow \text{P5}$ pathway dominates with a fraction of more than 85% at temperatures below 2000 K.

In addition, the product energy distributions have also been investigated in this work. We calculated the energy distributions of trajectories whose total vibrational energy of the products is larger than the sum of their ZPEs. The product energy distributions at each temperature are shown in Fig. 7. For the $\text{H} + \text{HCCOH}$ (P2) and $\text{H} + \text{OCCH}_2$ (P4) channels, the ratios of the relative translational, vibrational, and rotational energies of the products are less affected by temperature variations. A large fraction of the energy is deposited in the vibrational modes of the pentatomic products. In the $\text{CO} + \text{CH}_3$ (P5) channel, product energy distributions are similar to that of the $\text{C}_2\text{H}_2 + \text{O}(^3\text{P}) \rightarrow \text{CO} + \text{CH}_2$ reaction we had studied previously.⁷¹ The relative translational energy and the CH_3 vibrational energy account for a relatively large fraction of the total available energy. The CO rotational state is highly excited, while the CO vibrational energy accounts for a small fraction, and the CO vibrational energy distribution is slightly characterized by a thermal equilibrium distribution. For the $\text{H}_2\text{O} + \text{C}_2\text{H}$ (P1) channel, the available energy distributions for the relative translational, vibrational and rotational energies of the



products are relatively close, and the energy flowing into the rovibrational modes of H_2O is slightly larger than that of C_2H .

At low temperatures, long-lived complexes generated by electrophilic addition decompose into products in a process similar to that of unimolecular reactions. Here, we simulated the unimolecular reaction of the energy-rich complex decomposition and compared it with the $\text{C}_2\text{H}_2 + \text{OH}$ reaction. The initial molecule for the unimolecular reaction was set to Int1b and the total energy was fixed at the maximum probability of the total energy distribution at 500 K. The branching ratios for $\text{H} + \text{OCCH}_2$ (P4) and $\text{CO} + \text{CH}_3$ (P5) are 65.50% and 34.50% under these conditions, in general agreement with the product branching ratios for the $\text{C}_2\text{H}_2 + \text{OH}$ reaction. The product energy distributions of the unimolecular reaction are shown in Fig. 8. In terms of comparison of the energy distributions, the overall results are approximately the same, except that the rotational energy of the products is slightly lower for the unimolecular reactions. Thus at low temperatures, especially below 500 K, the decomposition of the energy-rich complexes for the $\text{C}_2\text{H}_2 + \text{OH}$ reaction could be approximated by unimolecular reactions.

IV. Conclusions

In this work, we developed the first full-dimensional chemically accurate PES for the $\text{C}_2\text{H}_2 + \text{OH}$ reaction covering five reachable product channels below 3000 K using the PIP-NN method based on 477 821 UCCSD(T)-F12b/cc-pVTZ-F12 data points. The new PES is accurate and smooth in important dynamical regions, which can be verified by the small fitting RMSE of $0.38 \text{ kcal mol}^{-1}$ and a good representation of the minimum energy paths. Based on the PIP-NN PES, we used the QCT method to calculate the rate coefficients of the $\text{C}_2\text{H}_2 + \text{OH}$ reaction over 298–3000 K and make a comparison with the previous experimental results. Above 1000 K, the QCT rate coefficient is in good agreement with the experimental values, but it is lower than the experimental values at low temperatures. The discrepancy might be mitigated by further considering quantum effects and the effect of the association reaction. At low temperatures, the $\text{C}_2\text{H}_2 + \text{OH}$ reaction produces $\text{H} + \text{OCCH}_2$ (P4) and $\text{CO} + \text{CH}_3$ (P5). At about 1000 K, the $\text{H}_2\text{O} + \text{C}_2\text{H}$ (P1) and $\text{H} + \text{HCCOH}$ (P2) channels are open, and $\text{H}_2\text{O} + \text{C}_2\text{H}$ (P1) mainly formed by a direct hydrogen abstraction pathway becomes the dominant product above 1900 K. While the probability of the $\text{H}_2 + \text{HCCO}$ (P3) channel is negligible in the $\text{C}_2\text{H}_2 + \text{OH}$ reaction. Due to the similarity found in branching ratios and product energy distributions, the decomposition of the energy-rich complexes for the $\text{C}_2\text{H}_2 + \text{OH}$ reaction could be approximated by unimolecular reactions at low temperatures. In addition, the modified Arrhenius expressions and the product energy distribution for the $\text{C}_2\text{H}_2 + \text{OH}$ reaction were also reported in this work. We hope that these results will provide new insights into understanding this complex combustion reaction. This full-dimensional PES can be further used to investigate the mode specificity in the title reaction and the reaction dynamics for this system from other reactant channels.

Data availability

The data and the PES code that support the findings of this study can be obtained by contacting the corresponding author X. Hu (xxhu@nju.edu.cn).

Conflicts of interest

The authors declare no competing financial interest.

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