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## Noble gas hydrides: theoretical prediction of the first group of anionic species†

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The first group of anionic noble-gas hydrides with the general formula  $\text{HNgBeO}^-$  ( $\text{Ng} = \text{Ar, Kr, Xe, Rn}$ ) is predicted through MP2, Coupled-Cluster, and Density Functional Theory computations employing correlation-consistent atomic basis sets. We derive that these species are stable with respect to the loss of  $\text{H}$ ,  $\text{H}^-$ ,  $\text{BeO}$ , and  $\text{BeO}^-$ , but unstable with respect to  $\text{Ng} + \text{HBeO}^-$ . The energy barriers of the latter process are, however, high enough to suggest the conceivable existence of the heaviest  $\text{HNgBeO}^-$  species as metastable in nature. Their stability arises from the interaction of the  $\text{H}^-$  moiety with the positively-charged  $\text{Ng}$  atoms, particularly with the  $\sigma$ -hole ensuing from their ligation to  $\text{BeO}$ . This actually promotes relatively tight  $\text{Ng}-\text{H}$  bonds featuring a partially-covalent character, whose degree progressively increases when going from  $\text{HArBeO}^-$  to  $\text{HRnBeO}^-$ . The  $\text{HNgBeO}^-$  compounds are also briefly compared with other noble-gas anions observed in the gas phase or isolated in crystal lattices.

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### 1. Introduction

Chemical compounds containing noble gas–hydrogen ( $\text{Ng}-\text{H}$ ) bonds have not yet been prepared using synthetic methods. Numerous cationic and neutral noble-gas hydrides are, however, detected in the gas phase or in cold solid matrices. The first evidence of gaseous cationic species dates back to 1925,<sup>1</sup> when Hogness and Lunn detected the simplest  $\text{HeH}^+$  and  $\text{HeH}_2^+$  from ionized  $\text{He}/\text{H}_2$  mixtures. Over the years, the gas-phase chemistry of the  $\text{Ng}_m\text{H}_n^+$  ( $\text{Ng} = \text{He-Xe}$ ;  $m, n \geq 1$ ) turned out to be rich and varied,<sup>2</sup> and the rejuvenated interest that it is currently enjoying<sup>3–13</sup> is also stimulated by the actual detection of  $\text{ArH}^+$  and  $\text{HeH}^+$  in various galactic and extragalactic regions.<sup>14–18</sup> Neutral compounds with  $\text{Ng}-\text{H}$  bonds emerged first in 1995,<sup>19</sup> when Räsänen and his coworkers identified the strong infrared absorbers originating from the photodissociation of hydrogen halides in  $\text{Kr}$  and  $\text{Xe}$  matrices as the “inserted” compounds  $\text{HXeI}$ ,  $\text{HXeBr}$ ,  $\text{HXeCl}$ , and  $\text{HKrCl}$ . Other  $\text{HNgY}$  species ( $\text{Y} = \text{electronegative group}$ )

were soon prepared using the same method, including the celebrated  $\text{HArF}$ ,<sup>20</sup> a first and still unique neutral covalent argon compound. The family currently includes more than thirty  $\text{HNgY}$  ( $\text{Ng} = \text{Kr, Xe}$ ) and other related species, whose investigation is a major chapter of modern noble-gas chemistry.<sup>21,22</sup> Anionic noble-gas hydrides are, instead, still essentially unknown. The simplest diatomic  $\text{HNg}^-$  ( $\text{Ng} = \text{He-Xe}$ )<sup>23</sup> species are weak van der Waals complexes, but more compact structures featuring  $\text{Ng}-\text{H}$  bonds are still unreported, both experimentally and theoretically. We report here – to the best of our knowledge – a first theoretically-predicted group of such species, having formula  $\text{HNgBeO}^-$ . The complexes of  $\text{Ng}$  atoms with beryllium Lewis acids, including  $\text{BeO}$  and other related species, have attracted, over the years, considerable experimental and theoretical interest.<sup>24–30</sup> The present search was inspired by the computational results that we recently obtained from the study of the complexes of  $\text{ArBeO}$  with simple ligands.<sup>31,32</sup> When the  $\text{Ng}$  atoms, particularly the heaviest  $\text{Ar, Kr, Xe}$ , and  $\text{Rn}$ , interact with the strong electron-withdrawing  $\text{BeO}$ , the only slightly positive electrostatic potential (EP)<sup>33,34</sup> of  $\text{Ng}$  (*ca.* 2 kcal mol<sup>–1</sup> at the 0.0010  $e\text{a}_0^{-3}$  isodensity surface) dramatically increases up to more than 50 kcal mol<sup>–1</sup>. The EP of  $\text{NgBeO}$  features, in particular, a point of maximum on the outer prolongation of the  $\text{Ng}-\text{Be}$  bond axis, and a  $\sigma$ -hole<sup>35,36</sup> at the  $\text{Ng}$  atom that allows the interaction with various ligands  $\text{L}$ . The study of numerous  $\text{L-ArBeO}$ <sup>31,32</sup> unraveled, in particular, that the complexes with  $\text{NH}_3$  and  $\text{HF}$  (featuring a negative EP at the  $\text{N}$  and  $\text{F}$  atom, respectively) have sizable binding energies of 4–5 kcal mol<sup>–1</sup>, whose major attractive component (*ca.* 70%) comes from the electrostatic term. In essence, the formation of these complexes is driven by the interaction of the positive EP of  $\text{Ar}$  with the

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negative EP of N or F. We thus surmised that this favorable electrostatic contact could be further enhanced with anionic ligands, including the simplest  $\text{H}^-$ . This picture was confirmed by the actual location of the four  $\text{HN}\text{gBeO}^-$  species ( $\text{Ng} = \text{Ar}, \text{Kr}, \text{Xe}, \text{Rn}$ ) as true minima on the corresponding potential energy surface (PES). These systems are actually unstable with respect to dissociation into  $\text{Ng}$  and  $\text{HBeO}^-$ , but the protecting barriers are high enough to suggest their conceivable existence as metastable species, at least for the heaviest congeners. The structure, bonding situation, harmonic frequencies, and stability of these anions are discussed in this article. We also briefly compare the bonding motif occurring in the  $\text{HN}\text{gBeO}^-$  species with those occurring in other observed or predicted  $\text{Ng}$  anions.

## 2. Theoretical methods and computational details

The theoretical methods employed in this study were the Møller-Plesset<sup>37</sup> perturbation theory truncated at the second order (MP2), the Coupled Cluster theory<sup>38</sup> with the inclusion of single and double electronic substitutions, CCSD, and an estimate of connected triples, CCSD(T), and the B3LYP density functional.<sup>39,40</sup> The employed basis sets, henceforth denoted as aVnZ ( $n = \text{T}, \text{Q}, 5$ ), were the Dunning's correlation consistent aug-cc-pVnZ<sup>41</sup> for H, Be, O, Ar, and Kr, and aug-cc-pVnZ-PP<sup>41</sup> for Xe and Rn, the latter being treated with the Stuttgart/Cologne small-core, scalar-relativistic effective core potentials (ECP-28 and ECP-60, respectively).<sup>42</sup> The MP2 and CCSD(T) calculations were performed by correlating only the outer valence electrons (*i.e.* frozen-core approximation).

The MP2/aVTZ and B3LYP/aVTZ geometry optimization and harmonic frequency calculations were performed using Gaussian 09 (G09, Revision D1),<sup>43</sup> and the CCSD(T)/aVTZ geometry optimizations and harmonic frequencies calculations were performed using CFOUR (V2.1).<sup>44</sup> Electronic energies at the complete basis set (CBS) limit were obtained by extrapolating the CCSD(T)/aVQZ and CCSD(T)/aV5Z correlation energies using the cubic formula:<sup>45</sup>

$$E^{\text{corr}}(\text{CBS}) = \frac{E_5^{\text{corr}} \times 5^3 - E_4^{\text{corr}} \times 4^3}{5^3 - 4^3} \quad (1)$$

At each computational level, the energy change at 0 K and the energy, enthalpy and free energy changes at 298.15 K of the investigated reactions were calculated using the unscaled harmonic vibrational frequencies and by adding the translational (3/2 RT), rotational (RT or 3/2 RT for linear and non-linear species, respectively) and vibrational contributions at this temperature. The last term was calculated using standard statistical mechanics formulas.<sup>46</sup> The total entropies were calculated using the unscaled harmonic frequencies and moments of inertia.

The CCSD(T)/aVTZ natural bond orbital (NBO) atomic charges were calculated using the NBO program.<sup>47</sup>

The functions examined within the bonding analysis, including the electron density  $\rho(\mathbf{r})$ ,<sup>48</sup> the electron energy density  $H(\mathbf{r})$ ,<sup>49–51</sup> and the reduced density gradient (RDG)

$s(\mathbf{r})$ ,<sup>52,53</sup> are defined as follows. The  $\rho(\mathbf{r})$  is defined by the equation:<sup>48</sup>

$$\rho(\mathbf{r}) = \sum_i \eta_i |\varphi_i(\mathbf{r})|^2 \quad (2)$$

where  $\eta_i$  is the occupation number of the natural orbital  $\varphi_i$ , which is expanded as a linear combination of the basis functions.

The  $H(\mathbf{r})$  is the sum of the kinetic energy density  $G(\mathbf{r})$  and the potential energy density  $V(\mathbf{r})$ . The presently-employed definition<sup>48,54</sup> of the  $G(\mathbf{r})$  is given by the equation:

$$G(\mathbf{r}) = \frac{1}{2} \sum_{i=1} \eta_i |\nabla \varphi_i(\mathbf{r})|^2 \quad (3)$$

where the sum runs over all the occupied natural orbitals  $\varphi_i$  of occupation numbers  $\eta_i$ .

The potential energy density  $V(\mathbf{r})$  is evaluated<sup>48</sup> from the local form of the virial theorem:

$$V(\mathbf{r}) = \frac{1}{4} \nabla^2 \rho(\mathbf{r}) - 2G(\mathbf{r}) \quad (4)$$

At last, the RDG is defined by the equation:<sup>52,53</sup>

$$s(\mathbf{r}) = \frac{|\nabla \rho(\mathbf{r})|}{2(3\pi^2)^{\frac{1}{3}} \times \rho(\mathbf{r})^{\frac{4}{3}}} \quad (5)$$

Low-value  $s(\mathbf{r})$  isosurfaces (typically 0.2–0.6) appear among atoms undergoing any type of interaction. The integral of a given property  $P$  [particularly the  $\rho(\mathbf{r})$  and the  $H(\mathbf{r})$ ] over the volume  $\Omega_s$  enclosed, in particular, by the  $s(\mathbf{r}) = 0.2$  isosurface ( $s$ ) at around the BCP located on any bond path,  $P(\Omega_s)$ , was calculated by producing an orthogonal grid of points that encloses the isosurface and applying the formula:

$$P(\Omega_s) = \sum_{i(\text{RDG} < s)} P(r_i) d_x d_y d_z \quad (6)$$

where  $P(r_i)$  is the value of  $P$  at the grid point  $r_i$ , and  $d_x, d_y$ , and  $d_z$  are the grid step sizes in the  $x, y$ , and  $z$  directions, respectively ( $d_x = d_y = d_z = 0.025 a_0$ ). The summation is then carried out on all grid points  $r_i$  having  $\text{RDG} < s$ .

The Extended Transition State – Natural Orbitals for Chemical Valence (ETS-NOCV) calculations were performed at the B3LYP/aVTZ level of theory using the CCSD(T)/aVTZ optimized geometries. In the ETS scheme,<sup>55</sup> the interaction energy between two fragments A and B in a molecular system AB,  $\Delta E_{\text{int}}$ , is partitioned into five components:

$$\Delta E_{\text{int}} = \Delta E_{\text{prep}} + \Delta E_{\text{elstat}} + \Delta E_{\text{Pauli}} + \Delta E_{\text{disp}} + \Delta E_{\text{orb}} \quad (7)$$

$\Delta E_{\text{prep}}$  (preparation energy) is the energy required to deform the separated fragments from their ground-state equilibrium geometries to the geometries that they acquire in the complex.  $\Delta E_{\text{elstat}}$  is the classical electrostatic interaction between the unperturbed charge distributions of the prepared fragments at their position in the final complex, and is calculated using the frozen electron densities.  $\Delta E_{\text{Pauli}}$  arises when the wave function of the two superimposed fragments is renormalized

and antisymmetrized, and comprises the destabilizing interaction between electrons of the same spin on either fragment.  $\Delta E_{\text{disp}}$  is the dispersion term.  $\Delta E_{\text{orb}}$  arises when the Kohn–Sham orbitals relax to their final optimal form. It accounts for the interactions between the occupied molecular orbitals of one fragment with the unoccupied molecular orbitals of the other fragment as well as for mixing of occupied and virtual orbitals within the same fragment. This term is particularly informative about the bonding situation of a molecular system as it can be further decomposed in the framework of the NOCV theory.<sup>56–58</sup> The NOCV orbitals are the eigenvectors of the chemical valence operator  $V$  of the Nalewajski–Mrozek valence theory:<sup>59</sup>

$$V\varphi_k = v_k \varphi_k \quad (8)$$

The  $\varphi_k$  can be grouped into pairs of complementary orbitals ( $\varphi_k$ ,  $\varphi_{-k}$ ) corresponding to the same eigenvalue with the opposite sign,  $\pm v_k$ . In particular, the NOCV orbitals decompose the deformation density  $\Delta\rho_{\text{orb}}(\mathbf{r})$  (namely, the difference between the density of the complex and that of the separated fragments) into the sum of the various pair contributions:

$$\Delta\rho_{\text{orb}}(\mathbf{r}) = \sum \Delta\rho_{\text{orb}}^k(\mathbf{r}) = \sum_{k=1}^{N/2} v_k [\varphi_k^2(\mathbf{r}) - \varphi_{-k}^2(\mathbf{r})] \quad (9)$$

( $N$  is the number of NOCV orbitals). In the combined ETS–NOCV scheme,<sup>57,58</sup> the  $\Delta E_{\text{orb}}$  term of eqn (7) can be expressed in terms of the NOCV eigenvalues  $v_k$ :

$$\Delta E_{\text{orb}} = \sum \Delta E_{\text{orb}}^k = \sum_{k=1}^{N/2} v_k [F_{k,k}^{\text{TS}} - F_{-k,-k}^{\text{TS}}] \quad (10)$$

where  $F_{k,k}^{\text{TS}}$  and  $F_{-k,-k}^{\text{TS}}$  are the diagonal Kohn–Sham matrix elements defined over the NOCV  $\varphi_k$  and  $\varphi_{-k}$ , respectively, with respect to the transition-state density (at the midpoint between the density of the complex and the sum of fragment densities). Thus, within the ETS–NOCV scheme,<sup>57,58</sup> irrespective of the molecular symmetry, any orbital interaction  $k$  contributing to  $\Delta E_{\text{orb}}$  is assayed quantitatively in terms of  $\Delta E_{\text{orb}}^k$ , and also qualitatively by visual inspection of the shape of the corresponding contribution to the deformation density  $\Delta\rho_{\text{orb}}^k(\mathbf{r})$ .

The  $\Delta E_{\text{orb}}$  term of eqn (7) and the  $\rho(\mathbf{r})$ , the  $H(\mathbf{r})$ , and the  $s(\mathbf{r})$  were evaluated and analyzed with the Multiwfn package (version 3.8.dev).<sup>60</sup> The CCSD(T)/aVTZ wave functions were stored in the molden files generated using CFOUR,<sup>44</sup> and properly formatted using the Molden2AIM utility.<sup>61</sup> The Multiwfn was also employed to produce the two-(2D) plots of the  $\Delta\rho_{\text{orb}}^k(\mathbf{r})$  and of the  $H(\mathbf{r})$ , the latter including the contour lines corresponding to the critical points located for each structure from the topological analysis of the  $H(\mathbf{r})$  and the standard contour lines belonging to the patterns  $\pm k \times 10^n$  ( $k = 1, 2, 4, 8$ ;  $n = -5$  to 6).

### 3. Results and discussion

#### 3.1 Structure and bonding

All the linear  $\text{HN}\text{gBeO}^-$  ( $\text{Ng} = \text{He–Rn}$ ) species were located as stationary points on the MP2/aVTZ PES. However, the lightest  $\text{HHeBeO}^-$  and  $\text{HNeBeO}^-$  species turned out to be second-order

saddle points (unstable to dissociation through the  $\text{H–Ng–Be}$  bending), and were not explored in further detail. The  $\text{HArBeO}^-$ ,  $\text{HKrBeO}^-$ ,  $\text{HXeBeO}^-$ , and  $\text{HRnBeO}^-$  were instead characterized as true energy minima, and as such confirmed also at the B3LYP/aVTZ and CCSD(T)/aVTZ levels of theory. The  $\text{NgBeO}$  species were also investigated for comparison.

In general, as shown in Table S1 of the ESI,<sup>†</sup> compared with the two *ab initio* methods, the B3LYP method tends to underestimate the  $\text{Ng–H}$  and  $\text{Be–O}$  distances, while overestimating the  $\text{Ng–Be}$  distances, with mutual differences arriving up to *ca.* 0.05 Å. The MP2/aVTZ and CCSD(T)/aVTZ values are, instead, quite similar, with the largest difference of only 0.02 Å. The forthcoming discussion will be based on the in principle most accurate CCSD(T)/aVTZ values shown in Fig. 1. At these geometries, the CCSD/aVTZ T1 diagnostic<sup>62</sup> of any  $\text{HN}\text{gBeO}^-$  species resulted close to the accepted threshold of 0.02, thus suggesting the effectiveness of single-determinant methods to describe their electronic structure. The geometries and NBO atomic charges of the  $\text{HN}\text{gBeO}^-$  species suggest their structural assignment as tight complexes between  $\text{H}^-$  and  $\text{NgBeO}$ , best formulated as  $\text{H}^-(\text{NgBeO})$ . As shown in Fig. 1, in any  $\text{HN}\text{gBeO}^-$ , the  $\text{H}$  atom bears a negative charge lower than  $-0.8e$ , arriving at  $-0.943e$  in  $\text{HArBeO}^-$ . The  $\text{Ng–H}$  distances range between 2.5267 Å ( $\text{Ng} = \text{Rn}$ ) and 2.5764 Å ( $\text{Ng} = \text{Kr}$ ). These values are definitely higher than the sum of the covalent radii<sup>63</sup> of  $\text{H}$  (0.32 Å) and of the  $\text{Ng}$  atoms ( $\text{Ar}$ : 1.07 Å,  $\text{Kr}$ : 1.21 Å,  $\text{Xe}$ : 1.35 Å,  $\text{Rn}$ : 1.45 Å), but lower by *ca.* 0.5–1 Å than the sum of the van der Waals radii of  $\text{H}$ <sup>64</sup> (1.06 Å) and of the  $\text{Ng}$  atoms<sup>65</sup> ( $\text{Ar}$ : 1.97 Å,  $\text{Kr}$ : 2.12 Å,  $\text{Xe}$ : 2.32 Å,  $\text{Rn}$ : 2.43 Å). They are also appreciably lower than the distances of the diatomic  $\text{HN}^-$ , predicted<sup>23</sup> between 3.47 Å ( $\text{Ng} = \text{Rn}$ ) and 3.78 Å ( $\text{Ng} = \text{Ar}$ ). This overall suggests that the  $\text{Ng–H}$  bonds of the  $\text{HN}\text{gBeO}^-$ , while certainly rather far from typical covalent interactions, are, however, appreciably tighter than simple van der Waals contacts. This was confirmed by the results of the bonding analysis, performed at the CCSD(T)/aVTZ level of theory using our recently proposed method.<sup>49,66–68</sup> It involves the study of three functions, namely

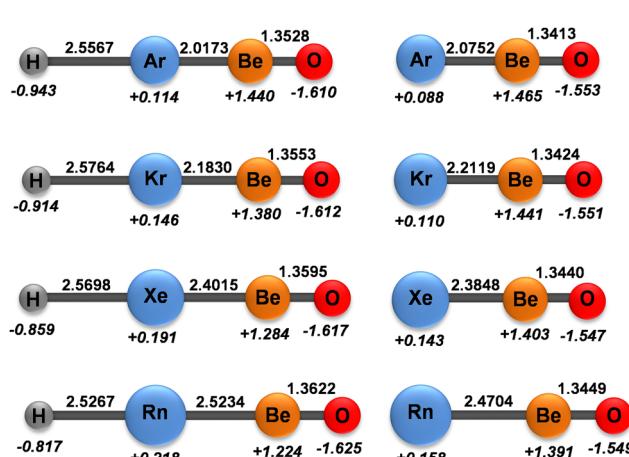


Fig. 1 CCSD(T)/aVTZ optimized bond lengths (Å) and NBO atomic charges (e, in italics) of the  $\text{HN}\text{gBeO}^-$  and  $\text{NgBeO}$  species ( $\text{Ng} = \text{Ar, Kr, Xe, Rn}$ ).

the electron density  $\rho(\mathbf{r})$ ,<sup>48</sup> the electron energy density  $H(\mathbf{r})$ ,<sup>49–51</sup> and the reduced density gradient (RDG)  $s(\mathbf{r})$ .<sup>52,53</sup> Any Ng–X bond (X = binding partner) is assigned following the step-by-step procedure<sup>68</sup> briefly recalled below. Further details are given in ref. 49 and 66–68.

Step 1. The Ng–X contact is ascertained by analyzing the topology of the  $\rho(\mathbf{r})$  and locating the corresponding bond path (BP) and bond critical point (BCP) (the classical AIM analysis).

Step 2. The topology of the  $H(\mathbf{r})$  of the whole molecule is analyzed. This typically produces various critical points (HCPs) of rank 3 and signature  $-3, -1, +1$ , or  $+3$ . The contour lines these points belong to are collected as the HCP lines.

Step 3. The HCP lines are combined with a set of standard (STD)  $H(\mathbf{r})$  lines, typically the patterns  $\pm k \times 10^n$  ( $k = 0, 1, 2, 4, 8$ ;  $n = -5$  to 6).

Step 4. The HCP/STD lines are plotted as 2D or 3D graphs, whose visual inspection allows assignment of the bond as type A, B, or C. As best discussed previously,<sup>49,66–68</sup> the  $H(\mathbf{r})$  generally partitions the atomic space into inner regions of negative values, indicated as  $H^-(\mathbf{r})$ , and outer regions of positive values, indicated as  $H^+(\mathbf{r})$ . When two atoms form a chemical bond, their  $H^-(\mathbf{r})$  and  $H^+(\mathbf{r})$  regions combine in modes that signal the nature of the interaction. Particularly for the Ng–X bonds, it is possible to recognize three major situations. In interactions of type A, the atoms overlap all the contour lines of their  $H^+(\mathbf{r})$  regions, and part of the contour lines of their inner  $H^-(\mathbf{r})$  regions, the bond appearing as a continuous region of negative values of  $H(\mathbf{r})$ , plunged in a zone of positive values. The bond is topologically signed by a (3, +1) HCP falling on the bond axis. Typical examples are covalent bonds, or donor–acceptor interactions with some degree of electron sharing. In interactions of type B, the  $H^-(\mathbf{r})$  region of Ng is, again, overlapped with the  $H^-(\mathbf{r})$  region of the binding partner, but (i) the bond is not signed by a HCP on the axis, and (ii) the Ng–X inter-nuclear region includes a (more or less wide) region of positive  $H(\mathbf{r})$ . Typical examples are the complexes of Ng donors with strongly electropositive Lewis acceptors. In interactions of type C, Ng and X overlap only part of their  $H^+(\mathbf{r})$  regions, their  $H^-(\mathbf{r})$

regions remaining perfectly closed and separated by a region of positive  $H(\mathbf{r})$ . The bond thus appears as two clearly distinguishable  $H^-(\mathbf{r})$  regions, separated by a region of positive values of  $H(\mathbf{r})$ . Typical examples are non-covalent contacts of variable nature.

Step 5. The assignment of the bond is refined by examining the  $H(\mathbf{r})$  along the Ng–X BP, particularly at around the BCP. This serves to confirm the interactions of type A, and to distinguish the interactions of type B and C as B-loose ( $B^l$ ) or B-tight ( $B^t$ ), and C-loose ( $C^l$ ) or C-tight ( $C^t$ ). The adopted criteria are given in Table 1.

Step 6. Once assigned as of type A,  $B^l/B^t$ , or  $C^l/C^t$ , the Ng–X bond is assayed in terms of contribution of covalency. This is accomplished by integrating the  $\rho(\mathbf{r})$  and the  $H(\mathbf{r})$  over the volume  $\Omega_s$  enclosed by the  $s(\mathbf{r})$  isosurface associated with the Ng–X BCP. The value of the  $s(\mathbf{r})$  is chosen by examining, particularly at around the BCP, the  $s(\mathbf{r})$  vs.  $\text{sign}(\lambda_2) \times \rho(\mathbf{r})$  2D plot [ $\lambda_2$  is the second eigenvalue of the Hessian matrix of  $\rho(\mathbf{r})$ , with  $\lambda_1 < \lambda_2 < \lambda_3$ ]. The selected value of  $s(\mathbf{r})$  is the highest one that still avoids the contribution of the tails of the atomic densities, and typically ranges between 0.2 and 0.5. Relevant quantities calculated over  $\Omega_s$  include the average  $\rho(\mathbf{r})$ ,  $\rho_s$  (ave), and the average, maximum, and minimum  $H(\mathbf{r})$ ,  $H_s$  (ave/max/min). Based on the obtained values, and on the sign of  $H(\mathbf{r})$  over  $\Omega_s$ ,  $H(\Omega_s)$ , the bond is therefore assigned as covalent (Cov), partially-covalent (pCov) or non-covalent (nCov) according to the criteria listed in Table 1.

Step 7. The bond is finally classified using the notations Cov(Type), pCov[Type/ $H(\Omega_s)$ ], or nCov(Type), for example, Cov(A), pCov( $B^t/H^{l+}$ ), or nCov( $C^l$ ).

In developing the method, we also found it convenient to introduce some additional numerical indices that allow further assay of the degree of the various interactions. Of relevance in the present context is the average bond degree over  $\Omega_s$ ,  $BD_s$  (ave). Borrowing the concept of BD introduced by Espinosa *et al.*,<sup>69</sup> this index is defined as the average over  $\Omega_s$  of the ratio  $-H(\mathbf{r})/\rho(\mathbf{r})$ . Formulated in this way, the index is *de facto* applicable to any type of interaction (A, B, or C).

**Table 1** Criteria to assign the Ng–X chemical bonds in terms of the sign of the  $H(\mathbf{r})$  at around the BCP, and of covalency

$H(\mathbf{r})$ at around the BCP		
Assignment	Ng side	X side
A	Negative	Negative
$B^l$ or $C^l$	Positive	Positive
$B^t$ or $C^t$	Positive	Negative
	Negative	Positive
	Negative	Negative

Covalency			
	$\rho_s$ <sup>a</sup> (ave)	$H(\Omega_s)$	Notation
Cov	$\geq 0.08$	Invariably negative	$H^-$
pCov	$< 0.08$	Invariably negative	$H^-$
	Any value	From negative to positive	$H^{l+}$ (positive on the average) $H^{-/+}$ (negative on the average)
nCov	Any value	Invariably positive	$H^+$

<sup>a</sup>  $e a_0^{-3}$ .

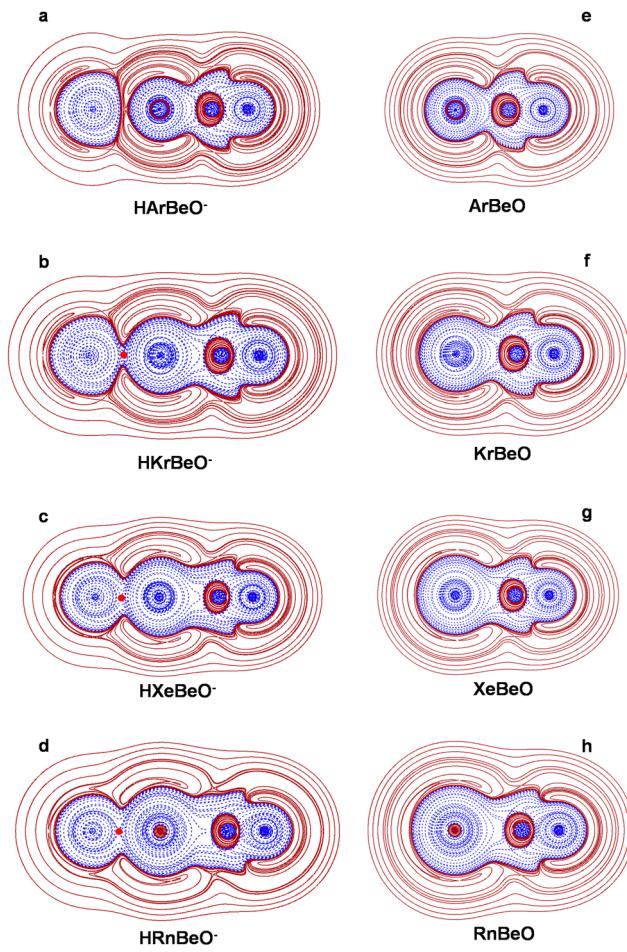


Fig. 2 2D-plots of the CCSD(T)/aVTZ  $H(r)$  in the main plane of  $\text{HNgBeO}^-$  (a–d) and  $\text{NgBeO}$  (e–h) ( $\text{Ng} = \text{Ar}, \text{Kr}, \text{Xe}, \text{Rn}$ ) (solid/brown and dashed/blue lines correspond, respectively, to positive and negative values). The (red) dots indicate the HCP of the interactions of type A.

The results of the bonding analysis of the  $\text{HNgBeO}^-$  are given in Fig. 2 and in Table 2. The  $\text{NgBeO}$  species were also investigated for comparison. As shown in Fig. 2(a), in  $\text{HArBeO}^-$ ,

the  $H^-(\mathbf{r})$  regions of the H atom and of the  $\text{ArBeO}$  moiety are separated by a zone of positive values, and the interaction is, therefore, of type C. In addition, along the BCP, the  $H(\mathbf{r})$  is positive at both the H and the Ar side. Over  $\Omega_s$ , however, although positive on the average, the  $H(\mathbf{r})$  is partially negative (see Table 2). The bond is, therefore, partially covalent and overall assigned as  $\text{pCov}(\text{C}^1/\text{H}^{+/-})$ . It is, indeed, possible from Fig. 2(a) to clearly appreciate the strong deformation of the spherical  $H^-(\mathbf{r})$  region of the H atom due to the interaction with  $\text{ArBeO}$ . When going to the heaviest congeners  $\text{KrArBeO}$ ,  $\text{XeArBeO}$ , and  $\text{RnArBeO}$ , this polarization markedly increases up to promoting the overlapping of the  $H^-(\mathbf{r})$  regions of the H atom and of the  $\text{NgBeO}$  moiety (Fig. 2(b)–(d)). Consequently, the type of the interaction changes from C to A. The  $H(\mathbf{r})$  is also invariably negative over  $\Omega_s$ , but the values of  $\rho_s$  (ave), ranging between 0.0202 and 0.0299  $e \text{a}_0^{-3}$ , are definitely lower than those typical of covalent bonds. All the Ng–H contacts ( $\text{Ng} = \text{Kr}, \text{Xe}, \text{Rn}$ ) are, therefore, assigned as  $\text{pCov}(\text{A}/\text{H}^-)$ . Not unexpectedly, the quantitative indices indicate that the interaction becomes progressively tighter when going from  $\text{HArBeO}^-$  to  $\text{HRnBeO}^-$ . One notes, in particular, the  $\text{BD}_s$  (ave), predicted to be negative for  $\text{Ng} = \text{Ar}$  ( $-0.0104$  hartree  $e^{-1}$ ) and increasingly positive for  $\text{Ng} = \text{Kr}$  ( $0.0492$  hartree  $e^{-1}$ ),  $\text{Ng} = \text{Xe}$  ( $0.0989$  hartree  $e^{-1}$ ), and  $\text{Ng} = \text{Rn}$  ( $0.121$  hartree  $e^{-1}$ ). This suggests that the irregular trend of the Ng–H bond distances (an increase from  $2.5567 \text{ \AA}$  to  $2.5764 \text{ \AA}$  when going from  $\text{HArBeO}^-$  to  $\text{HKrBeO}^-$ , and then a decrease to  $2.5968 \text{ \AA}$  and  $2.5267 \text{ \AA}$  when going to  $\text{HXeBeO}^-$  and  $\text{HRnBeO}^-$ ) is, most likely, a balance of atomic size and degree of interaction.

Like those occurring in the  $\text{NgBeO}$  species, the Ng–Be bonds of the  $\text{HNgBeO}^-$  species are invariably assigned as of type B. The bonding analysis unravels, however, that the ligation of  $\text{NgBeO}$  to  $\text{H}^-$  increases the extent of the Ng–Be interaction. This is particularly evident when going from  $\text{ArBeO}$  to  $\text{HArBeO}^-$ : as shown in Table 2, the character of the Ar–Be bond changes from  $\text{pCov}(\text{B}^1/\text{H}^{+/-})$  to  $\text{pCov}(\text{B}^1/\text{H}^-)$ , and the  $\text{BD}_s$  (ave) changes from negative ( $-0.0754$  hartree  $e^{-1}$ ) to positive ( $0.101$  hartree  $e^{-1}$ ). As shown in Fig. 1, this is accompanied by a shortening of the Ar–Be distance from  $2.0752 \text{ \AA}$  to  $2.0173 \text{ \AA}$ . The  $\text{BD}_s$  (ave) of

Table 2 CCSD(T)/aVTZ type and properties of the Ng–X bonds of  $\text{HNgBeO}^-$  and  $\text{NgBeO}$  (see Fig. 1 and 2) calculated over the  $s(\mathbf{r}) = 0.2$  RDG isosurface at around the BCP.  $\Omega_s$  is the volume ( $\text{a}_0^{-3}$ ) enclosed by  $s(\mathbf{r})$ , and  $N(\Omega_s)$ ,  $\rho_s$  (ave),  $H_s$  (ave/max/min) and  $\text{BD}_s$  (ave) are, respectively, the total electronic charge (me), the average electron density ( $e \text{a}_0^{-3}$ ), the average, maximum and minimum value of  $H(\mathbf{r})$  (hartree  $\text{a}_0^{-3}$ ), and the average bond degree (hartree  $e^{-1}$ ) over  $\Omega_s$

Species	Bond	Type	$\Omega_s$	$N(\Omega_s)$	$\rho_s$ (ave)	$H_s$ (ave/max/min)	$H(\Omega_s)^a$	$\text{BD}_s$ (ave)	Assignment
$\text{HArBeO}^-$	Ar–H	$\text{C}^1$	0.0585	0.98	0.0167	0.00017/0.00052/–0.00022	$\text{H}^{+/-}$	–0.0104	$\text{pCov}(\text{C}^1/\text{H}^{+/-})$
	Ar–Be	$\text{B}^t$	0.0135	0.59	0.0435	–0.0044/–0.00087/–0.0089	$\text{H}^-$	0.101	$\text{pCov}(\text{B}^t/\text{H}^-)$
$\text{ArBeO}$	Ar–Be	$\text{B}^1$	0.0104	0.33	0.0319	0.0024/0.0052/–0.00024	$\text{H}^{+/-}$	–0.0754	$\text{pCov}(\text{B}^1/\text{H}^{+/-})$
	Kr–H	A	0.0821	1.66	0.0202	–0.00099/–0.00074/–0.0014	$\text{H}^-$	0.0492	$\text{pCov}(\text{A}/\text{H}^-)$
$\text{HKrBeO}^-$	Kr–Be	$\text{B}^t$	0.0262	1.11	0.0423	–0.0093/–0.0041/–0.0142	$\text{H}^-$	0.221	$\text{pCov}(\text{B}^t/\text{H}^-)$
	Kr–Be	$\text{B}^t$	0.0151	0.48	0.0321	–0.0016/0.0011/–0.0049	$\text{H}^{-/+}$	0.0497	$\text{pCov}(\text{B}^t/\text{H}^{+/-})$
$\text{HXeBeO}^-$	Xe–H	A	0.1203	3.14	0.0261	–0.0026/–0.0022/–0.0032	$\text{H}^-$	0.0989	$\text{pCov}(\text{A}/\text{H}^-)$
	Xe–Be	$\text{B}^t$	0.0595	2.49	0.0418	–0.0152/–0.0092/–0.0198	$\text{H}^-$	0.364	$\text{pCov}(\text{B}^t/\text{H}^-)$
$\text{XeBeO}$	Xe–Be	$\text{B}^t$	0.0267	0.84	0.0325	–0.0055/–0.0011/–0.0094	$\text{H}^-$	0.168	$\text{pCov}(\text{B}^t/\text{H}^-)$
	Rn–H	A	0.1373	4.10	0.0299	–0.0036/–0.0031/–0.0043	$\text{H}^-$	0.121	$\text{pCov}(\text{A}/\text{H}^-)$
$\text{HRnBeO}^-$	Rn–Be	$\text{B}^t$	0.1162	4.67	0.0402	–0.0170/–0.0125/–0.0202	$\text{H}^-$	0.422	$\text{pCov}(\text{B}^t/\text{H}^-)$
	Rn–Be	$\text{B}^t$	0.0350	1.10	0.0314	–0.0066/–0.0028/–0.0101	$\text{H}^-$	0.210	$\text{pCov}(\text{B}^t/\text{H}^-)$

<sup>a</sup> Depending on the sign of  $H_s$  (ave/max/min),  $H(\Omega_s) = \text{H}^{+/-}$ ,  $\text{H}^{-/+}$ , or  $\text{H}^-$ .

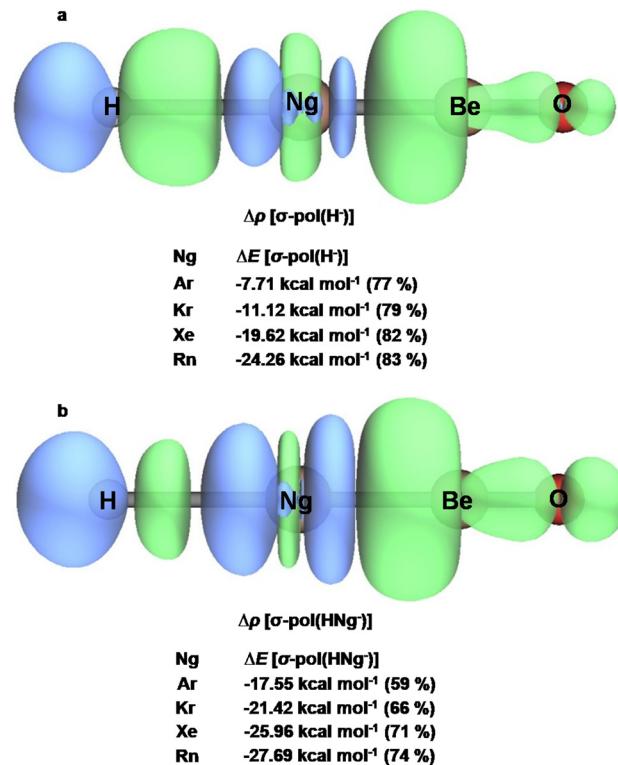
the Ng–Be bond of the other  $\text{HNgBeO}^-$  is also higher by *ca.* 0.2 hartree  $e^{-1}$  than that of the corresponding  $\text{NgBeO}$ . Only for  $\text{HKrBeO}^-$ , however, is this change accompanied by a decrease of the Kr–Be bond length (from 2.1830 Å to 2.2119 Å). The Xe–Be and Rn–Be bond lengths of  $\text{HXeBeO}^-$  and  $\text{HRnBeO}^-$  increase by 0.0167 Å and 0.053 Å, respectively.

Within the classical AIM analysis,<sup>48</sup> a chemical bond is characterized in terms of  $\rho(\text{BCP})$ , of the Laplacian of the electron density at the BCP,  $\nabla^2\rho(\text{BCP})$ , and of  $H(\text{BCP})$ . The values of these quantities calculated for the  $\text{HNgBeO}^-$  and  $\text{NgBeO}$  are given in Table S2 (ESI<sup>†</sup>). When compared with those quoted in Table 2, these data unravel some peculiar features of our employed method of bonding analysis. For example, the Ar–H bond of  $\text{HArBeO}^-$ , presently assigned as pCov, would have been assigned as non-covalent, based on a positive value of both  $\nabla^2\rho(\text{BCP})$  and  $H(\text{BCP})$ . In addition, even though the AIM analysis is sufficient in predicting the partially-covalent character of the Ng–H and Ng–Be bonds of any other  $\text{HNgBeO}^-$  and  $\text{NgBeO}$  ( $\nabla^2\rho(\text{BCP})$  is positive but  $H(\text{BCP})$  is negative), our employed indices, particularly the  $H(\Omega_s)$  and  $\text{BD}_s$  (ave), provide further insights into their quantitative aspects and trends of intrinsic strength.

The assignment of the  $\text{HNgBeO}^-$  as a tight donor–acceptor complex between  $\text{H}^-$  and  $\text{NgBeO}$  is further supported by the results of the ETS–NOCV analysis. In general, the energy decomposition analysis performed according to the ETS scheme may be used to address the question about the choice of the most appropriate fragments that should be used to discuss a chemical bond. It has been, in particular, suggested<sup>70–73</sup> that those fragments, which exhibit the smallest change in the electronic structure that is associated with bond formation, should be used for discussing the nature of the chemical interactions. Thus, the absolute value of the orbital term  $\Delta E_{\text{orb}}$  indicates which fragments should be used for the bonding analysis. The data obtained for the  $\text{HNgBeO}^-$  species are given in Table 3. Irrespective of Ng, the smallest (less negative)  $\Delta E_{\text{orb}}$  is predicted for the  $\text{H}^-/\text{NgBeO}$  interacting fragments, the values ranging between  $-9.99 \text{ kcal mol}^{-1}$  (Ng = Ar) and  $-29.40 \text{ kcal mol}^{-1}$  (Ng = Rn). If the Ng–H bond would be a covalent interaction between H and  $\text{NgBeO}^-$ , the  $\Delta E_{\text{orb}}$  would be definitely more negative, ranging between  $-65.78 \text{ kcal mol}^{-1}$  (Ng = Ar) and  $-77.32 \text{ kcal mol}^{-1}$  (Ng = Rn). As for the Ng–Be bond, the analysis clearly unravels that there is a dative bond between  $\text{HNg}^-$  and BeO rather than a covalent bond between  $\text{HNg}^-$  and BeO<sup>–</sup>. In fact, if one assumes the former pair of interacting fragments, the  $\Delta E_{\text{orb}}$  ranges between  $-29.81 \text{ kcal mol}^{-1}$  (Ng = Ar) and  $-37.41 \text{ kcal mol}^{-1}$  (Ng = Rn), but the values strongly decrease to  $-106.64 \text{ kcal mol}^{-1}$  (Ng = Ar) and  $-122.31 \text{ kcal mol}^{-1}$  (Ng = Xe) for the alternative interacting pair.

**Table 3** B3LYP/aVTZ  $\Delta E_{\text{orb}}$  ( $\text{kcal mol}^{-1}$ ) of  $\text{HNgBeO}^-$  evaluated with respect to different interaction fragments

Ng	$\text{H}^-/\text{NgBeO}$	$\text{H}/\text{NgBeO}^-$	$\text{HNg}^-/\text{BeO}$	$\text{HNg}/\text{BeO}^-$
Ar	–9.99	–65.78	–29.81	–106.64
Kr	–14.00	–68.58	–32.57	–108.94
Xe	–23.81	–75.09	–36.42	–122.31
Rn	–29.40	–77.32	–37.41	–117.83



**Fig. 3** Deformation densities  $\Delta\rho(\mathbf{r})$  (plotted isosurfaces:  $0.0008 \text{ e} \text{a}_0^{-3}$ ) and the corresponding orbital interaction energies  $\Delta E$  associated with the two most important pairwise orbital interactions for: (a)  $\text{H}^-$  interacting with  $\text{NgBeO}$  and (b)  $\text{HNg}^-$  interacting with  $\text{BeO}$ . The values in parentheses are the percentage contributions to the total  $\Delta E_{\text{orb}}$ . Green and blue zones correspond, respectively, to charge accumulation and charge depletion.

(Ng = Ar) and  $-122.31 \text{ kcal mol}^{-1}$  (Ng = Xe) for the alternative interacting pair.

The analysis of the deformation density  $\Delta\rho_{\text{orb}}(\mathbf{r})$  accompanying the formation of  $\text{HNgBeO}^-$  from the two most favourable interacting pairs  $\text{H}^-/\text{NgBeO}$  and  $\text{HNg}^-/\text{BeO}$  unravelled that, in both cases, for any Ng, the by far prevailing contribution is the  $\sigma$  polarization of  $\text{H}^-$  or  $\text{HNg}^-$  toward  $\text{NgBeO}$  or  $\text{BeO}$ . The corresponding isosurfaces are shown in Fig. 3. The interaction of  $\text{H}^-$  with  $\text{NgBeO}$  (Fig. 3(a)) produces the polarization of the electronic cloud of the anion already highlighted by the analysis of the  $H(\mathbf{r})$  (*vide supra*), and a charge accumulation particularly at the BeO moiety. The ensuing stabilization ranges between  $-7.71 \text{ kcal mol}^{-1}$  (Ng = Ar) and  $-24.26 \text{ kcal mol}^{-1}$  (Ng = Rn), and accounts for 77–83% of the total  $\Delta E_{\text{orb}}$ . The interaction of  $\text{HNg}^-$  with  $\text{BeO}$  (Fig. 3(b)) produces the polarization of both Ng and  $\text{H}^-$  toward  $\text{BeO}$ , and the ensuing stabilization, ranging between  $-17.55 \text{ kcal mol}^{-1}$  (Ng = Ar) and  $-27.69 \text{ kcal mol}^{-1}$  (Ng = Rn), is still the prevailing contribution to the total  $\Delta E_{\text{orb}}$ , with percentages ranging between 59% (Ng = Ar) and 74% (Ng = Rn).

### 3.2 Harmonic frequencies

The description of the  $\text{HNgBeO}^-$  species as tight complexes between  $\text{H}^-$  and  $\text{NgBeO}$  emerges also from their vibrational pattern. The latter includes, in fact, the  $\nu(\text{Ng–Be})$  and  $\nu(\text{Be–O})$

stretchings, and the doubly-degenerate  $\delta(\text{Ng}-\text{Be}-\text{O})$  of the  $-\text{NgBeO}$  moiety, and the  $\nu(\text{Ng}-\text{H})$  stretching and the  $\delta(\text{H}-\text{Ng}-\text{Be})$  bending. The MP2/aVTZ, B3LYP/aVTZ and CCSD(T)/aVTZ harmonic frequencies are compared in Table S3 (ESI<sup>†</sup>). With respect to the *ab initio* methods, the B3LYP underestimates the  $\nu(\text{Ng}-\text{Be})$  and overestimates the  $\nu(\text{Be}-\text{O})$ . The forthcoming discussion is based on the CCSD(T)/aVTZ values quoted in Table 4.

Compared with the triatomic  $\text{NgBeO}^-$ , the  $\nu(\text{Be}-\text{O})$  of  $\text{HN}\text{gBeO}^-$ , falling between  $1476 \text{ cm}^{-1}$  ( $\text{Ng} = \text{Rn}$ ) and  $1508 \text{ cm}^{-1}$  ( $\text{Ng} = \text{Ar}$ ), is red-shifted by *ca.*  $30\text{--}40 \text{ cm}^{-1}$ . This mirrors the elongation of the  $\text{Be}-\text{O}$  bond that occurs when going from any  $\text{NgBeO}$  to the corresponding  $\text{HN}\text{gBeO}^-$ . The  $\nu(\text{Ng}-\text{Be})$ , falling between  $224 \text{ cm}^{-1}$  ( $\text{Ng} = \text{Rn}$ ) and  $318 \text{ cm}^{-1}$  ( $\text{Ng} = \text{Ar}$ ), is, instead, blue-shifted by *ca.*  $10\text{--}40 \text{ cm}^{-1}$ . This is consistent with the increase of the strength of the  $\text{Ng}-\text{Be}$  bond when going from any  $\text{NgBeO}$  to the corresponding  $\text{HN}\text{gBeO}^-$  unravelled by the bonding analysis. The  $\delta(\text{Ng}-\text{Be}-\text{O})$ , falling between  $233$  ( $\text{Ng} = \text{Ar}$ ) and  $286 \text{ cm}^{-1}$  ( $\text{Ng} = \text{Rn}$ ), is also blue-shifted with respect to  $\text{NgBeO}$  by *ca.*  $100 \text{ cm}^{-1}$ . The rather tight character of the interaction occurring between  $\text{H}^-$  and  $\text{NgBeO}$  is, however, best signalled by the relatively high value of the  $\nu(\text{Ng}-\text{H})$  stretching, predicted between  $569 \text{ cm}^{-1}$  ( $\text{Ng} = \text{Ar}$ ) and  $641 \text{ cm}^{-1}$  ( $\text{Ng} = \text{Rn}$ ). This absorption is expected to be brilliant. Thus, as shown in Table S3 (ESI<sup>†</sup>), both the MP2/aVTZ and B3LYP/aVTZ predicted intensities are higher than  $1000 \text{ km mol}^{-1}$ , and are up to more than  $2000 \text{ km mol}^{-1}$  for  $\text{HRnBeO}^-$ . The  $\delta(\text{H}-\text{Ng}-\text{Be})$  bending, predicted between  $134 \text{ cm}^{-1}$  ( $\text{Ng} = \text{Ar}$ ) and  $161 \text{ cm}^{-1}$  ( $\text{Ng} = \text{Rn}$ ), is also expected to be brilliant. The intense  $\nu(\text{Ng}-\text{H})$  of the  $\text{HN}\text{gBeO}^-$  could be in principle diagnostic for their experimental detection, for example, in the gas phase or in cold matrices. In this regard, it is decisive to investigate the conceivable stability or metastability of the anions on the corresponding PES. This issue is discussed in the subsequent paragraph.

### 3.3 Stability

The stability or metastability of the  $\text{HN}\text{gBeO}^-$  species depends on the thermodynamics and the activation barrier ( $E^\ddagger$ ) of their conceivable dissociation processes. These include the two-body (2B) reactions (11) and (12), and the three-body (3B) reactions (13) and (14) summarized by the equations:

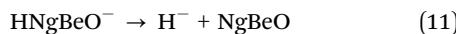


Table 4 CCSD(T)/aVTZ harmonic vibrational frequencies ( $\text{cm}^{-1}$ ) of the linear  $\text{HN}\text{gBeO}^-$ . MP2/aVTZ IR intensities ( $\text{km mol}^{-1}$ ) in parentheses

Species	$\nu(\text{Ng}-\text{Be})$	$\nu(\text{Be}-\text{O})$	$\nu(\text{Ng}-\text{H})$	$\delta(\text{Ng}-\text{Be}-\text{O})^a$	$\delta(\text{H}-\text{Ng}-\text{Be})^a$
$\text{HArBeO}^-$	318 (0.4)	1508 (124)	569 (1284)	233 (15)	134 (713)
$\text{ArBeO}$	272 (2)	1536 (72)		155 (64)	
$\text{HKrBeO}^-$	267 (19)	1495 (117)	591 (1635)	250 (8)	153 (638)
$\text{KrBeO}$	246 (1)	1533 (77)		155 (59)	
$\text{HXeBeO}^-$	267 (69)	1495 (107)	591 (2273)	250 (84)	153 (420)
$\text{XeBeO}$	237 (0.6)	1527 (78)		150 (50)	
$\text{HRnBeO}^-$	234 (94)	1476 (101)	641 (2548)	286 (90)	161 (300)
$\text{RnBeO}$	224 (0.5)	1522 (81)		145 (46)	

<sup>a</sup> Doubly-degenerate bending.



The values of their  $\Delta E_{\text{el}}$ ,  $\Delta E$  (0 K),  $\Delta E$  (298.15 K),  $\Delta H$  (298.15 K), and  $\Delta G$  (298.15 K) computed at the B3LYP/aVTZ, MP2/aVTZ, and CCSD(T)/aVTZ levels of theory are given in Tables S4–S6 (ESI<sup>†</sup>), and the CCSD(T)/CBS data, explicitly discussed in this paragraph, are quoted in Table 5. Both the MP2/aVTZ and CCSD(T)/aVTZ values are quite similar to the benchmark CCSD(T)/CBS values, while the B3LYP/aVTZ method overestimates the energetics by *ca.*  $1\text{--}2 \text{ kcal mol}^{-1}$ .

The 2B channel (11) measures the degree of the interaction between  $\text{H}^-$  and  $\text{NgBeO}$ . When going from  $\text{HArBeO}^-$  to  $\text{HRnBeO}^-$ , the corresponding  $\Delta E_{\text{el}}$  progressively increases from  $28.4$  to  $39.4 \text{ kcal mol}^{-1}$ , and these rather high values confirm the strong character of the interaction between  $\text{H}^-$  and  $\text{NgBeO}$  suggested by the geometries and bonding analysis. The  $\Delta G$  (298.15 K) values are also definitely positive, ranging between  $21.3$  and  $31.6 \text{ kcal mol}^{-1}$ .

The  $\Delta E_{\text{el}}$  and  $\Delta G$  (298.15 K) of the 3B channel (13) are even higher, as they include the dissociation energy of  $\text{NgBeO}$  into  $\text{Ng} + \text{BeO}$ . The  $\Delta E_{\text{el}}$  values range, in particular, between  $11.7$  ( $\text{Ng} = \text{Ar}$ ) and  $16.6 \text{ kcal mol}^{-1}$  ( $\text{Ng} = \text{Rn}$ ), and these estimates perfectly agree with those reported previously.<sup>24</sup>

The electron affinity of  $\text{H}$ ,  $17.4 \text{ kcal mol}^{-1}$ ,<sup>74</sup> is lower than that of  $\text{BeO}$ ,  $49.6 \text{ kcal mol}^{-1}$ ,<sup>75</sup> and, in fact, the thermodynamic values of reaction (14) are lower than those of reaction (13) by *ca.*  $33 \text{ kcal mol}^{-1}$ . The  $\Delta E_{\text{el}}$  of reaction (14) thus ranges between  $7.6$  ( $\text{Ng} = \text{Ar}$ ) and  $23.4 \text{ kcal mol}^{-1}$  ( $\text{Ng} = \text{Rn}$ ). Once the entropy term is included, the dissociation is predicted to be exoergic for  $\text{Ng} = \text{Ar}$  ( $-7.2 \text{ kcal mol}^{-1}$ ) and  $\text{Ng} = \text{Kr}$  ( $-3.6 \text{ kcal mol}^{-1}$ ), but endoergic for  $\text{Ng} = \text{Xe}$  ( $2.8 \text{ kcal mol}^{-1}$ ) and  $\text{Ng} = \text{Rn}$  ( $8.2 \text{ kcal mol}^{-1}$ ).

The 2B channel (12) is largely exothermic, its  $\Delta E_{\text{el}}$  progressively decreasing from  $-83.2$  ( $\text{Ng} = \text{Ar}$ ) to  $-67.4 \text{ kcal mol}^{-1}$  ( $\text{Ng} = \text{Rn}$ ). This reaction occurs through the bent transition structures (TSs) whose CCSD(T)/aVTZ optimized geometries are shown in Fig. 4 (likewise the corresponding minima, their CCSD/aVTZ T1 diagnostics are close to the threshold of 0.02). The MP2/aVTZ and B3LYP/aVTZ optimized geometries are also given in Table S7 (ESI<sup>†</sup>). Compared with the linear  $\text{HN}\text{gBeO}^-$  (see Fig. 1), the  $\text{Ng}-\text{H}$  bonds of these TSs (between  $2.6842 \text{ \AA}$  and  $2.9587 \text{ \AA}$ ) are longer by *ca.*  $0.3\text{--}0.5 \text{ \AA}$ , and the  $\text{H}-\text{Ng}-\text{Be}$  angles (between  $91.6^\circ$  and  $114.4^\circ$ ) are appreciably smaller than  $180^\circ$ . There is also a closing of the  $\text{Ng}-\text{Be}-\text{O}$  angle by *ca.*  $17\text{--}18^\circ$ . The

Table 5 CCSD(T)/CBS dissociation energies (kcal mol<sup>-1</sup>) of  $\text{HN}\text{gBeO}^-$  (reference species)

Species		$\text{H}^- + \text{NgBeO}$	$\text{H}^- + \text{Ng} + \text{BeO}$	$\text{H} + \text{Ng} + \text{BeO}^-$	$\text{Ng} + \text{HBeO}^-$	$E^\#$ <sup>a</sup>
HArBeO <sup>-</sup>	$\Delta E_{\text{el}}$	28.4	40.1	7.6	-83.2	3.0
	$\Delta E$ (0 K)	26.9	37.7	5.1	-81.5	2.5
	$\Delta E$ (298.15 K)	27.0	37.7	5.0	-82.2	2.0
	$\Delta H$ (298.15 K)	27.6	38.9	6.2	-81.6	2.0
	$\Delta G$ (298.15 K)	21.3	25.9	-7.2	-87.4	1.8
HKrBeO <sup>-</sup>	$\Delta E_{\text{el}}$	30.4	43.9	11.4	-79.4	6.0
	$\Delta E$ (0 K)	28.9	41.5	8.8	-77.7	5.4
	$\Delta E$ (298.15 K)	29.1	41.5	8.8	-78.4	5.0
	$\Delta H$ (298.15 K)	29.7	42.7	10.0	-77.8	5.0
	$\Delta G$ (298.15 K)	23.1	29.5	-3.6	-83.8	4.5
HXeBeO <sup>-</sup>	$\Delta E_{\text{el}}$	34.6	50.5	17.9	-72.9	11.1
	$\Delta E$ (0 K)	33.0	47.9	15.3	-71.3	10.3
	$\Delta E$ (298.15 K)	33.2	47.9	15.3	-71.9	10.0
	$\Delta H$ (298.15 K)	33.8	49.1	16.5	-71.3	10.0
	$\Delta G$ (298.15 K)	27.0	35.9	2.8	-77.4	9.1
HRnBeO <sup>-</sup>	$\Delta E_{\text{el}}$	39.4	56.0	23.4	-67.4	14.4
	$\Delta E$ (0 K)	37.6	53.3	20.6	-65.9	13.5
	$\Delta E$ (298.15 K)	37.9	53.4	20.7	-66.5	13.2
	$\Delta H$ (298.15 K)	38.5	54.5	21.9	-65.9	13.2
	$\Delta G$ (298.15 K)	31.6	41.3	8.2	-72.0	12.3

<sup>a</sup> Energy barrier for the reaction  $\text{HN}\text{gBeO}^- \rightarrow \text{Ng} + \text{HBeO}^-$ .

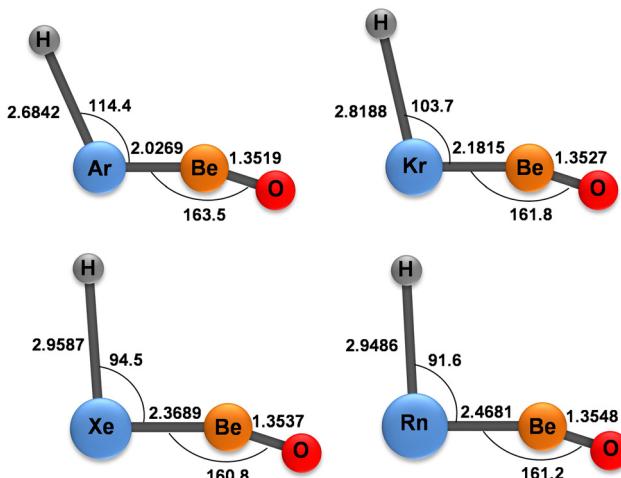


Fig. 4 CCSD(T)/aVTZ optimized bond lengths (Å) and bond angles (°) of the  $\text{HN}\text{gBeO}^-$  transition structures (Ng = Ar, Kr, Xe, Rn).

lengths of the Ng-Be bonds (between 2.0269 Å and 2.4681 Å) feature instead minor shortenings of 0.00015–0.0553 Å. These geometric changes suggest that the activation barriers of reaction (12) mainly arise from the shrinking of the H-Ng-Be angle and the elongation of the Ng-H bond, with an only minor contribution to the reaction coordinate of the dissociation of the Ng atom. The values of  $E^\#$  are, indeed, relatively high and less affected by inclusion of thermal and entropy contributions, with predicted values at 0 K ranging between 2.5 kcal mol<sup>-1</sup> for HArBeO<sup>-</sup> and 13.5 kcal mol<sup>-1</sup> for HRnBeO<sup>-</sup>.

The  $E^\#$  of reaction (12) and the  $\Delta E$  of reaction (14) can be used to assay the conceivable metastability of  $\text{HN}\text{gBeO}^-$ . Thus, in a benchmark study reported so far,<sup>76</sup> it was found that for a HNgY system, in order to have a life-time of *ca.* 100 seconds for spectroscopic studies in the gas phase at 100 K, the 3B channel  $\text{HN}\text{gY} \rightarrow \text{H} + \text{Ng} + \text{Y}$  and the 2B channel  $\text{HN}\text{gY} \rightarrow \text{Ng} + \text{HY}$  must

have barriers, respectively, of 13 and 8 kcal mol<sup>-1</sup>. As shown in Table 5, for HArBeO<sup>-</sup> and HKrBeO<sup>-</sup>, even the  $\Delta E$  (0 K) values (5.1/8.8 kcal mol<sup>-1</sup> and 2.5/5.4 kcal mol<sup>-1</sup>, respectively) are lower than these limits, and put into question the metastability of these species even under the conditions occurring, for example, in a cold matrix at a few kelvin. On the other hand, for HXeBeO<sup>-</sup> and HRnBeO<sup>-</sup>, even the  $\Delta E$  (298.15 K) of reaction (14) (15.3 and 20.7 kcal mol<sup>-1</sup>, respectively) and the  $E^\#$  of reaction (12) (10.0 and 13.2 kcal mol<sup>-1</sup>, respectively) are definitely higher than the thresholds for metastability. This encourages the experimental search, particularly of HXeBeO<sup>-</sup>, overall appearing as a difficult but not impossible task.

### 3.4 Comparison with other noble-gas anions

The  $\text{HN}\text{gBeO}^-$  species are briefly compared here with other observed or predicted noble-gas anions. Based on their geometries, one could first surmise a relationship with the FN $\text{gO}^-$  predicted by Hu and co-workers,<sup>77</sup> and with the other “inserted” Ng anions FN $\text{gX}^-$  (X = S, Se, BN) that emerged after this first report.<sup>78–81</sup> The compact structure of these ions, however, arises from the strong F<sup>-</sup>-induced stabilization of the singlet NgO and NgX that are intrinsically unstable or only marginally stable on their PES. This bonding motif is, indeed, substantially different from that occurring in the  $\text{HN}\text{gBeO}^-$  species, instead best related to that observed in other Ng species, particularly of xenon, that were observed in the gas phase or in synthesized salts. A first one is the XeF<sub>3</sub><sup>-</sup> species. This ion was detected in the gas phase from the collisionally-stabilized addition of F<sup>-</sup> to XeF<sub>2</sub>,<sup>82</sup> and was subsequently established as the intermediate in the exchange between F<sup>-</sup> and XeF<sub>2</sub> in the CH<sub>3</sub>CN solution.<sup>83</sup> No salts of XeF<sub>3</sub><sup>-</sup> could, however, be prepared,<sup>83</sup> and this was explained by the predicted ground-state structure of XeF<sub>3</sub><sup>-</sup>,<sup>83</sup> described as a complex between F<sup>-</sup> and XeF<sub>2</sub>, stabilized by the weak covalent interaction of the fluoride anion with the positively-charged Xe atom of xenon difluoride. This situation is clearly reminiscent of

the weak covalent bond between  $\text{H}^-$  and the  $\sigma$ -hole at the Xe atom of  $\text{XeBeO}$  occurring in the  $\text{HXeBeO}^-$  species. Interestingly, the hydride ion affinity of  $\text{XeBeO}$  as measured by the  $\Delta H$  (298.15 K) of reaction (11), 34.6 kcal mol<sup>-1</sup>, is significantly higher than the fluoride ion affinity of  $\text{XeF}_2$ , experimentally measured as 19.1 kcal mol<sup>-1</sup>.<sup>82</sup> This suggests that species such as  $\text{FNgBeO}^-$ ,  $\text{ClNgBeO}^-$ , and other similar anions could be even more stable than  $\text{HNgBeO}^-$ , thus inviting both their theoretical and experimental investigation in the next future. A bonding motif similar to that occurring in the  $\text{HNgBeO}^-$  species is also behind the stability of the  $[\text{X}_3(\text{XeO}_3)_3]^{3-}$  and  $[\text{X}_4(\text{XeO}_3)_4]^{4-}$  anions (X = Br and Cl) more recently isolated in crystal lattices by Schrobilgen and his co-workers.<sup>84</sup> In these peculiar Xe-cage structures, the halide anions form multiple weak covalent bonds with the  $\sigma$ -hole at the Xe atom of  $\text{XeO}_3$ , and these interactions are sufficient to ensure the overall stability of the cage.

## 4. Conclusions

The linear  $\text{HNgBeO}^-$  (Ng = Ar-Rn) species are the first theoretically-predicted examples of anionic noble-gas hydrides. Their stability is driven essentially by the favourable contact between  $\text{H}^-$  and the  $\sigma$ -hole at the Ng atom of NgBeO, producing partially-covalent Ng-H bonds. These anions possess rather compact structures, and reside in potential wells deep enough to suggest their challenging but not impossible detection in the gas phase or in cold matrices. Other anionic species such as  $\text{FNgBeO}^-$  or  $\text{ClNgBeO}^-$  could be even more stable, as suggested also by the comparison of the  $\text{HNgBeO}^-$  species with the gaseous  $\text{XeF}_3^-$ , and  $[\text{X}_3(\text{XeO}_3)_3]^{3-}$  and  $[\text{X}_4(\text{XeO}_3)_4]^{4-}$  (X = Br and Cl) isolated in crystal lattices. The experimental and theoretical search for  $\text{HNgBeO}^-$  and other related species could further expand our current knowledge about the intriguing chemistry of noble-gas anions.

## Author contributions

Stefano Borocci: methodology, data curation – reviewing and editing. Patrizio Cecchi: reviewing and editing. Felice Grandinetti: conceptualization – methodology – writing – original draft preparation. Nico Sanna: methodology, software – reviewing and editing. Costantino Zazza: methodology, data curation – reviewing and editing.

## Conflicts of interest

There are no conflicts to declare.

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