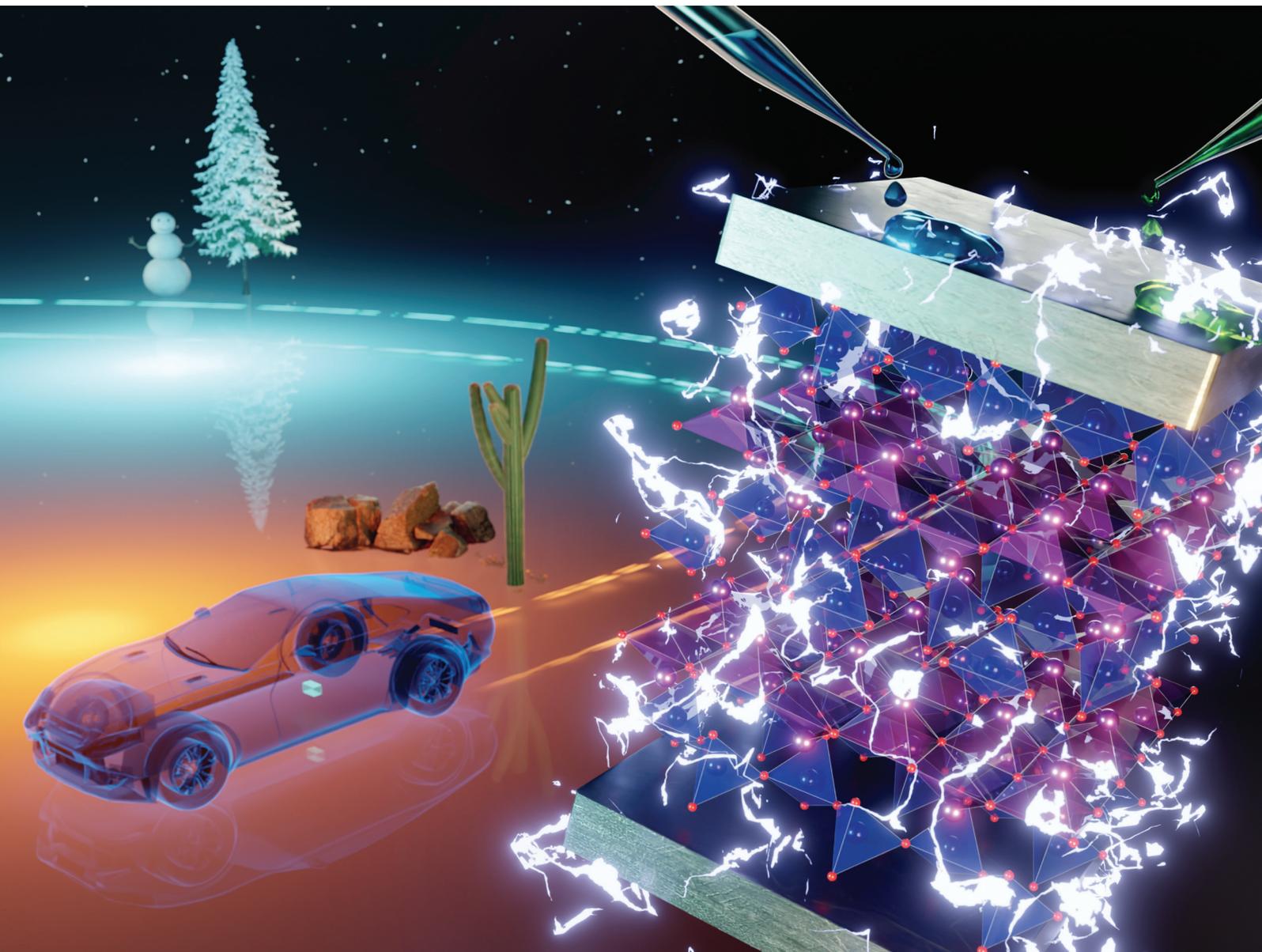


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**PAPER**

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Improving the dielectric temperature stability of  $\text{Bi}_2\text{SiO}_5$ -based ceramics through the spontaneous formation of paraelectric-ferroelectric nanocomposite structures

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# Improving the dielectric temperature stability of Bi<sub>2</sub>SiO<sub>5</sub>-based ceramics through the spontaneous formation of paraelectric–ferroelectric nanocomposite structures

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The substitution of a portion (~3%) of Bi<sup>3+</sup> in ferroelectric Bi<sub>2</sub>SiO<sub>5</sub> ceramics with La<sup>3+</sup> induces a paraelectric phase and stabilizes the dielectric permittivity by eliminating the ferroelectric–paraelectric phase transition. However, the non-negligible negative temperature dependence of the permittivity remains an issue for practical applications in capacitors, resonators, and antennas. Herein, we show that the additional substitution of Si<sup>4+</sup> with Ge<sup>4+</sup> in paraelectric (Bi<sub>0.97</sub>La<sub>0.03</sub>)<sub>2</sub>SiO<sub>5</sub> can substantially improve its dielectric temperature stability. Ceramic samples with compositions of (Bi<sub>0.97</sub>La<sub>0.03</sub>)<sub>2</sub>Si<sub>1-x</sub>Ge<sub>x</sub>O<sub>5</sub> with *x* up to 0.3 were prepared via a sol–gel process and subsequent low-temperature sintering below 720 °C. The incorporation of Ge stabilized the ferroelectric phase with an elevated Curie temperature, leading to the spontaneous formation of a paraelectric–ferroelectric nanocomposite structure. The fraction of the ferroelectric phase increased from 0% at *x* = 0 to 53% at *x* = 0.3. Because of the negative and positive temperature dependence of the paraelectric and ferroelectric phases, respectively, the sample with *x* = 0.2 exhibited a dielectric permittivity over 50 with a small temperature coefficient of  $-70 \pm 50$  ppm °C<sup>-1</sup> in a temperature range from -55 to 125 °C. The ceramics also showed a paraelectric-like linear polarization response under electric fields up to 280 kV cm<sup>-1</sup>.

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## Introduction

Dielectric ceramics with a high temperature stability of the dielectric permittivity ( $\epsilon_r$ ) are essential for a wide range of applications, including Class I (temperature compensating) multilayer ceramic capacitors (MLCCs) for electronics devices as well as resonators and antennas for wireless communication systems.<sup>1,2</sup> In particular, the market for Class I MLCCs used in power electronics systems for electric vehicles is growing rapidly due to their high temperature and high voltage compatibility.<sup>3</sup> Paraelectric CaZrO<sub>3</sub> is commonly used in such MLCCs, but its  $\epsilon_r$  is as low as 30.<sup>1</sup> Thus, the development of dielectric ceramics with higher and temperature-stable  $\epsilon_r$  is required for the downsizing and weight reduction of power electronic circuits, contributing to the reduction of greenhouse gas emissions. Dielectric

ceramics with  $\epsilon_r > 50$  and near-zero temperature dependence of  $\epsilon_r$  are also increasingly demanded for use in resonators for smartphone base stations.<sup>4</sup>

The temperature dependence of dielectric materials is often evaluated using the temperature coefficient of capacitance (TCC), which is calculated as follows:<sup>5</sup>

$$\text{TCC} = \frac{C_T - C_{25}}{C_{25} \times (T - 25)} \times 10^6 \text{ (ppm } ^\circ\text{C}^{-1}) \quad (1)$$

where *T* is the temperature in °C, and *C<sub>T</sub>* and *C<sub>25</sub>* are the capacitance values at *T* and 25 °C (base temperature), respectively. For example, the C0G specification for Class I MLCCs, which is the most stringent temperature stability standard, requires zero TCC with a tolerance of  $\pm 30$  ppm °C<sup>-1</sup> over a temperature range from -55 to 125 °C.<sup>1</sup> For application in microwave devices such as resonators and antennas, the temperature coefficient of the resonant frequency (TCF) is also commonly used, which is given as  $\text{TCF} = -(\text{TCC} + \alpha_L)/2$ , where  $\alpha_L$  is the linear thermal expansion coefficient.<sup>2</sup> As dielectric ceramics generally exhibit low  $\alpha_L$  (around +10 ppm °C<sup>-1</sup>), TCC determines the TCF in most dielectric ceramics.<sup>6</sup> The possibility of sintering at low temperatures is also an important factor in many applications because low sintering tempera-

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tures enable the co-firing of ceramics with low-melting metal electrodes such as Ag and Al, thereby reducing the material cost of devices.<sup>7,8</sup>

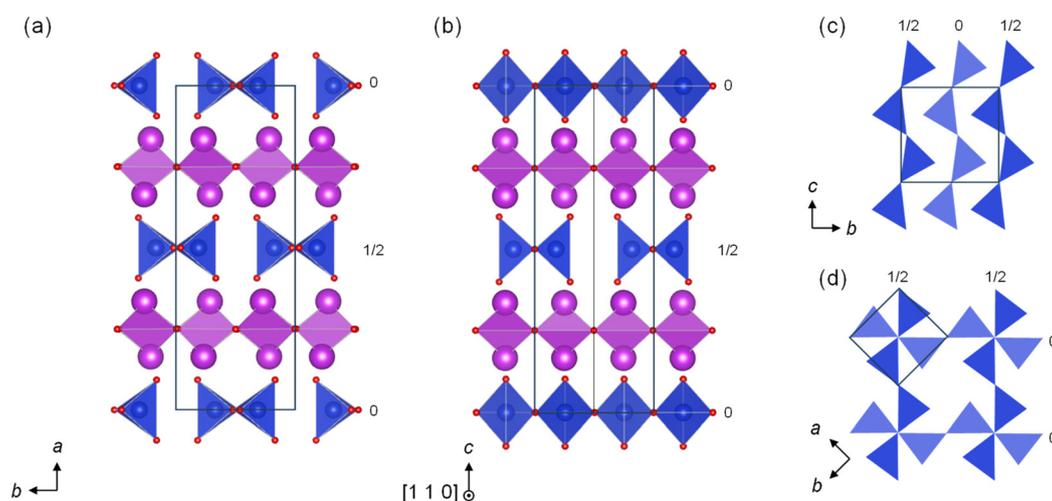
Recently, we reported that La-substituted  $\text{Bi}_2\text{SiO}_5$  synthesized *via* a sol-gel process can be sintered at 700 °C and possesses relatively high and temperature-stable dielectric permittivity ( $\epsilon_r = 59$  at 25 °C).<sup>9</sup>  $\text{Bi}_2\text{SiO}_5$  is a unique and unconventional ferroelectric oxide with spontaneous polarization occurring because of the twisting of one-dimensional chains of corner-sharing  $\text{SiO}_4$  tetrahedra [Fig. 1(a) and (c)].<sup>10</sup> Pristine  $\text{Bi}_2\text{SiO}_5$  transforms from a ferroelectric (monoclinic  $Cc$ ) phase to a paraelectric (orthorhombic  $Cmcm$ ) phase at the Curie temperature ( $T_C$ ) of approximately 400 °C upon heating, resulting in a strong positive temperature dependence of  $\epsilon_r$ .<sup>10,11</sup> The substitution of a portion (~3%) of  $\text{Bi}^{3+}$  in  $\text{Bi}_2\text{SiO}_5$  with  $\text{La}^{3+}$  perturbs the  $\text{SiO}_4$  chains, transforming the ferroelectric phase to another paraelectric phase with the tetragonal  $I4/mmm$  symmetry [Fig. 1(b) and (d)].<sup>12,13</sup> This structural change eliminates the dielectric peak, greatly improving the temperature stability of  $\epsilon_r$  while maintaining a relatively high  $\epsilon_r$ .<sup>9,13</sup> However, La-substituted  $\text{Bi}_2\text{SiO}_5$  ceramics still have negative TCCs (approximately  $-400 \text{ ppm } ^\circ\text{C}^{-1}$ ),<sup>9</sup> so further improvement of the dielectric temperature stability is essential for practical applications.

The general strategy for improving the temperature stability (TCC or TCF) of dielectric ceramics with low to medium  $\epsilon_r$  involves two main approaches: the preparation of composites and the formation of solid solutions.<sup>6</sup> The first approach requires two dielectric materials with temperature coefficients of opposite signs and very different crystal structures. For example, spinel-type  $\text{ZnAl}_2\text{O}_4$  (TCF =  $-79 \text{ ppm } ^\circ\text{C}^{-1}$ ) and rutile-type  $\text{TiO}_2$  (TCF =  $+423 \text{ ppm } ^\circ\text{C}^{-1}$ ) can be sintered into composite ceramics exhibiting  $\epsilon_r = 20$  with TCF close to zero at 30%  $\text{TiO}_2$  content.<sup>14</sup> This approach can only be used when the two

dielectric materials do not react with each other. As  $\text{Bi}_2\text{SiO}_5$  is a metastable phase in the  $\text{Bi}_2\text{O}_3$ - $\text{SiO}_2$  system,<sup>15</sup> the sintering of  $\text{Bi}_2\text{SiO}_5$  in the presence of another dielectric material may easily cause the decomposition of the  $\text{Bi}_2\text{SiO}_5$  phase. Therefore, the conventional composite formation approach is not suitable for  $\text{Bi}_2\text{SiO}_5$ -based dielectric ceramics.

In the second approach (solid solution formation), two or more end members with the same crystal structure but TCC or TCF of opposite signs are employed. For example, solid solution ceramics composed of perovskite-type  $\text{CaTiO}_3$  (TCF =  $800 \text{ ppm } ^\circ\text{C}^{-1}$ ) and  $\text{NdAlO}_3$  (TCF =  $-33 \text{ ppm } ^\circ\text{C}^{-1}$ ), namely  $\text{Ca}_{1-x}\text{Nd}_x\text{Ti}_{1-x}\text{Al}_x\text{O}_3$ , show a near-zero TCF at  $x = 0.3$ .<sup>16</sup> This approach has been widely used with perovskite-type oxides because of the large number of such materials with TCC or TCF of opposite signs. However, no materials with positive TCC are known to form solid solutions with La-substituted  $\text{Bi}_2\text{SiO}_5$ . For this reason, the solid solution approach is also not applicable to  $\text{Bi}_2\text{SiO}_5$ -based ceramics, thus requiring the development of a novel method for controlling the TCC.

Herein, we propose a unique method to improve the TCC of  $\text{Bi}_2\text{SiO}_5$ -based ceramics: the spontaneous formation of nano-composite structures of ferroelectric and paraelectric phases. As the ferroelectric  $Cc$  phase has a positive TCC whereas the paraelectric  $I4/mmm$  phase has a negative TCC, the composite formation between these phases brings TCC toward zero. To prepare this composite, we simultaneously substituted  $\text{Bi}^{3+}$  and  $\text{Si}^{4+}$  in  $\text{Bi}_2\text{SiO}_5$  with  $\text{La}^{3+}$  and  $\text{Ge}^{4+}$ , respectively.  $\text{Bi}_2\text{GeO}_5$  is a structural analog of  $\text{Bi}_2\text{SiO}_5$ , and *ab initio* calculations suggest that the stability of the ferroelectric phase relative to the high temperature paraelectric phase in  $\text{Bi}_2\text{GeO}_5$  is higher than that in  $\text{Bi}_2\text{SiO}_5$ .<sup>17</sup> Thus, the substitution of  $\text{Si}^{4+}$  with  $\text{Ge}^{4+}$  is expected to stabilize the ferroelectric phase of  $\text{Bi}_2\text{SiO}_5$  and shift  $T_C$  to higher temperatures. At the same time, the doping



**Fig. 1** (a and b) Schematic illustrations of the crystal structures of (a) the monoclinic  $Cc$  phase of  $\text{Bi}_2\text{SiO}_5$ , viewed along the  $c$ -axis, and (b) the tetragonal  $I4/mmm$  phase (local ordered description) of La-substituted  $\text{Bi}_2\text{SiO}_5$ , viewed along the  $[1\ 1\ 0]$  direction.<sup>10,13</sup> Purple, blue, and red spheres represent Bi (and La), Si, and O atoms, respectively. The solid-line squares represent the unit cells. (c and d) Connectivity of  $\text{SiO}_4$  tetrahedra in the (c) monoclinic phase (viewed along the  $a$ -axis) and (d) tetragonal phase (viewed along the  $c$ -axis). Note that the long-range connectivity of the  $\text{SiO}_4$  network in the tetragonal phase is disordered.<sup>13</sup>



of  $\text{La}^{3+}$  into  $\text{Bi}^{3+}$  sites breaks the long-range ferroelectric order, leading to a competition between the stabilities of the ferroelectric and paraelectric states. In this study,  $\text{Bi}_2\text{SiO}_5$  ceramics simultaneously substituted with La (3 mol%) and Ge (0–30 mol%) are prepared *via* a previously developed sol-gel process, and their crystalline phases and microstructures were investigated. The results show that the sintering of co-substituted ceramics results in the spontaneous formation of a nanocomposite structure with a TCC of  $-70 \pm 50 \text{ ppm } ^\circ\text{C}^{-1}$  and  $\epsilon_r > 50$  in the temperature range of from  $-55$  to  $125 \text{ }^\circ\text{C}$ .

## Experimental

### Sample preparation

$\text{Bi}_2\text{SiO}_5$  ceramics co-substituted with La and Ge, with nominal compositions of  $(\text{Bi}_{0.97}\text{La}_{0.03})_2\text{Si}_{1-x}\text{Ge}_x\text{O}_5$  ( $x = 0, 0.1, 0.2, \text{ and } 0.3$ ), were synthesized *via* a sol-gel process reported in our previous works.<sup>9,11</sup> The La content was fixed at 3 mol% because  $\text{Bi}_2\text{SiO}_5$  substituted with only La changes to the paraelectric phase at this La concentration.<sup>9</sup> Tetraethyl orthosilicate  $\text{Si}(\text{OC}_2\text{H}_5)_4$  (TEOS; 99.9%, Kanto Chemical Co., Inc.), tetraethyl orthogermanate  $\text{Ge}(\text{OC}_2\text{H}_5)_4$  (TEOG; 99.999%, Kojundo Chemical Laboratory Co., Ltd), bismuth nitrate pentahydrate  $(\text{Bi}(\text{NO}_3)_3 \cdot 5\text{H}_2\text{O}; 99.9\%$ , FUJIFILM Wako Pure Chemical Corporation), and lanthanum nitrate hexahydrate  $(\text{La}(\text{NO}_3)_3 \cdot 6\text{H}_2\text{O}; 99.9\%$ , FUJIFILM Wako Pure Chemical Corporation) were used as starting materials without further purification.

TEOS [ $6.0 \times (1 - x)$  mmol] was dissolved in a mixture of water (1.0 mL) and ethanol (1.3 mL), followed by the addition of citric acid (0.1 g) as a catalyst for hydrolysis. The solution was stirred at room temperature for 15 min to prehydrolyze TEOS, after which ethanol (4.7 mL) was added to prepare a Si solution. Separately, TEOG ( $6.0 \times x$  mmol) was dissolved in ethanol (6.00 mL) to prepare a Ge solution. In addition,  $\text{Bi}(\text{NO}_3)_3 \cdot 5\text{H}_2\text{O}$  (11.64 mmol) and  $\text{La}(\text{NO}_3)_3 \cdot 6\text{H}_2\text{O}$  (0.36 mmol) were dissolved in a mixture of L-lactic acid (3.2 mL) and water (7.8 mL) at  $60 \text{ }^\circ\text{C}$ . The resulting solution was cooled to room temperature to prepare a Bi-La solution. The Si and Ge solutions were added dropwise to the Bi-La solution under stirring, followed by additional stirring for 30 min at room temperature. The resulting transparent solution was gelatinized and dried at  $65 \text{ }^\circ\text{C}$  to obtain a xerogel. The xerogel was pulverized in a mortar and pyrolyzed at  $300 \text{ }^\circ\text{C}$  for 1 h under airflow, followed by calcination at  $500 \text{ }^\circ\text{C}$  for 30 min in air to obtain  $(\text{Bi}_{0.97}\text{La}_{0.03})_2\text{Si}_{1-x}\text{Ge}_x\text{O}_5$  fine powders.

The obtained powders were ball-milled in ethanol for 24 h, after which poly(vinyl alcohol) (2 wt%) and  $\text{CH}_3\text{COOLi}$  (4 mol%) were added as a binder and a sintering aid, respectively, and the mixture was uniaxially pressed at 100 MPa into 6 mm (diameter) pellets, followed by cold isostatic pressing at 150 MPa. The green bodies were heat-treated at  $400 \text{ }^\circ\text{C}$  for 1 h in air to remove the binder, followed by sintering at  $680\text{--}720 \text{ }^\circ\text{C}$  for 1 h in air to obtain  $(\text{Bi}_{0.97}\text{La}_{0.03})_2\text{Si}_{1-x}\text{Ge}_x\text{O}_5$  ceramics. The short holding time was essential to suppress the decomposition of the  $\text{Bi}_2\text{SiO}_5$ -type phase during sintering.

### Characterization

The density of the ceramic samples was measured using Archimedes' method. The crystal phases of the samples were determined *via* X-ray diffraction (XRD) analysis using a Bruker D8 ADVANCE diffractometer with a  $\text{Cu K}\alpha$  radiation source. The XRD patterns of the ceramic samples were analyzed using the Rietveld refinement software RIETAN-FP<sup>18</sup> to determine the phase contents. The crystallite sizes of the  $\text{Bi}_2\text{SiO}_5$ -type phases were estimated by applying the Halder-Wagner method to the diffraction angle dependence of the profile parameters refined by the Rietveld method, using the algorithm implemented in the RIETAN-FP program. The crystallite sizes obtained by such a method are expected to carry an uncertainty of at least  $\pm 10\text{--}20\%$ .<sup>19</sup> The microstructure of the samples was observed using field-emission scanning electron microscopy (FE-SEM) using a JEOL JSM-7600F microscope. The elemental distribution in sample particles was studied by high-angle annular dark-field scanning transmission electron microscopy-energy dispersive spectroscopy (HAADF-STEM-EDS) using an FEI Tecnai Osiris microscope.

To investigate their dielectric properties, the ceramic samples were polished to a thickness of approximately 0.7 mm, and Au electrodes were sputtered onto both the bottom and top surfaces. The temperature dependence of the capacitance and dielectric loss ( $\tan \delta$ ) were measured in the temperature range from  $-170$  to  $450 \text{ }^\circ\text{C}$  using an Agilent 4284A precision LCR meter equipped with a Linkam THMS600 temperature controller. TCC was calculated based on the measured temperature dependence of capacitance using eqn (1). Capacitance was converted to permittivity using the sample dimensions measured at room temperature. To measure the polarization ( $P$ )-electric field ( $E$ ) loops, the ceramic samples were polished to a thickness of approximately 0.15 mm, after which an Au electrode with a diameter of 1 mm was sputtered onto the top surface and the bottom surface was completely sputter-coated with Au. The  $P$ - $E$  loops were measured using a TOYO Corp. FCE10-B ferroelectric characterization system equipped with a Matsusada Precision Inc. HEOPT-10B10 high-voltage amplifier.

## Results and discussion

As  $\text{Bi}_2\text{SiO}_5$  is a metastable phase, it readily decomposes into  $\text{Bi}_4\text{Si}_3\text{O}_{12}$  and  $\text{Bi}_{12}\text{SiO}_{20}$  at temperatures above  $600 \text{ }^\circ\text{C}$ .<sup>12,15,20</sup> Although the addition of lithium acetate promotes the densification of  $\text{Bi}_2\text{SiO}_5$  and the incorporation of a small amount of  $\text{La}^{3+}$  at the  $\text{Bi}^{3+}$  site of  $\text{Bi}_2\text{SiO}_5$  retards thermal decomposition, the sintering of  $\text{Bi}_2\text{SiO}_5$ -based materials remains very challenging.<sup>9,11</sup> Thus, herein, the sintering temperature for  $(\text{Bi}_{0.97}\text{La}_{0.03})_2\text{Si}_{1-x}\text{Ge}_x\text{O}_5$  ceramics was optimized for each composition ( $x = 0, 0.1, 0.2, \text{ and } 0.3$ ) to balance the sintered density and the amount of secondary phases. The optimal sintering temperatures and the relative densities of the resulting ceramics are listed in Table 1. Although the samples are not perfectly densified, the relative densities of all samples are above 80%.



**Table 1** The optimal sintering temperature and the relative density of  $(\text{Bi}_{0.97}\text{La}_{0.03})_2\text{Si}_{1-x}\text{Ge}_x\text{O}_5$  ceramics ( $x = 0, 0.1, 0.2, \text{ and } 0.3$ )

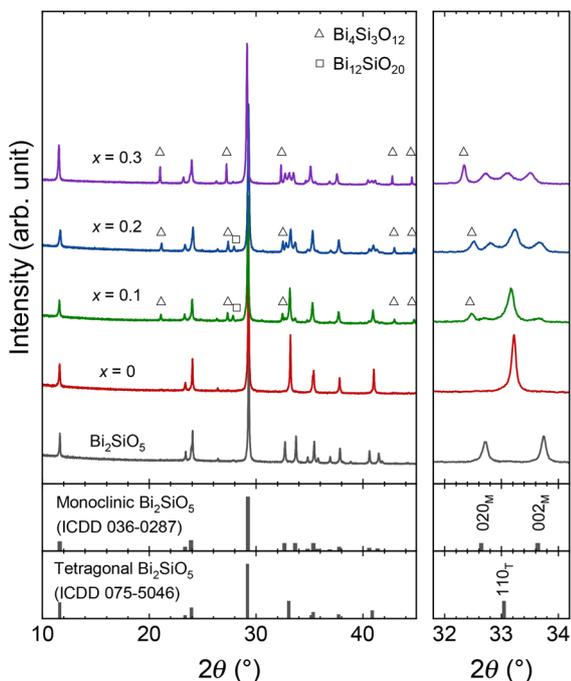
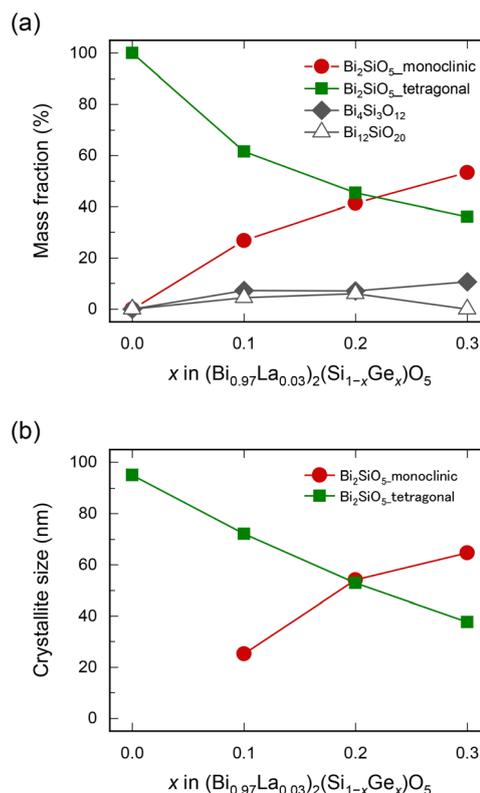
$x$	Sintering temperature ( $^{\circ}\text{C}$ )	Relative density (%)
0	720	91.4
0.1	700	91.0
0.2	680	82.2
0.3	700	84.9

Fig. 2 shows the XRD patterns of the  $(\text{Bi}_{0.97}\text{La}_{0.03})_2\text{Si}_{1-x}\text{Ge}_x\text{O}_5$  ceramics sintered at the optimum temperatures. For comparison, the XRD pattern for pristine  $\text{Bi}_2\text{SiO}_5$  prepared *via* a similar sol-gel process is also shown.<sup>9</sup> The diffraction peaks of pristine  $\text{Bi}_2\text{SiO}_5$  were assigned to the monoclinic ( $Cc$ ) structure, which is the ferroelectric phase with the spontaneous polarization caused by the twisting of  $\text{SiO}_4$  chains.<sup>10</sup> At the same time, the sample doped only with 3 mol% La ( $x = 0$ ) exhibits a paraelectric tetragonal ( $I4/mmm$ ) structure, consistent with previous reports.<sup>9,12,13</sup> This is because the substitution of  $\text{Bi}^{3+}$  with  $\text{La}^{3+}$  induces the disordering of  $\text{SiO}_4$  chains.<sup>13</sup> The diffraction peaks for the  $x = 0.1$  sample were mainly assigned to the tetragonal phase, with weak additional peaks at lower and higher angles relative to the tetragonal 1 1 0 peak assigned to the 0 2 0 and 0 0 2 lattice planes of the ferroelectric monoclinic phase. The intensity of the diffraction peaks of the monoclinic phase increases with Ge content, whereas peaks of the tetragonal phase are observed even at  $x = 0.3$ , indicating that the monoclinic and tetragonal phases coexist in  $(\text{Bi}_{0.97}\text{La}_{0.03})_2\text{Si}_{1-x}\text{Ge}_x\text{O}_5$  over a

wide compositional range,  $x = 0.1\text{--}0.3$ . This result is remarkable because in  $\text{Bi}_2\text{SiO}_5$  ceramics doped only with La, ferroelectric and paraelectric phases coexist in a very narrow compositional range (only around La = 1 mol%).<sup>9</sup> Additionally, the intensity of the diffraction peaks of the  $\text{Bi}_4\text{Si}_3\text{O}_{12}$  secondary phase increases with the Ge content. This indicates that the incorporation of Ge promotes the thermal decomposition of  $\text{Bi}_2\text{SiO}_5$ .

The XRD patterns of the samples were further analyzed *via* Rietveld refinement using a multiphase model consisting of the monoclinic and tetragonal  $\text{Bi}_2\text{SiO}_5$ -type phases of along with the  $\text{Bi}_4\text{Si}_3\text{O}_{12}$  and  $\text{Bi}_{12}\text{SiO}_{20}$  secondary phases. The analysis was conducted to determine the lattice parameters of the  $\text{Bi}_2\text{SiO}_5$  phases and the mass fraction of each phase. Phases with diffraction intensities below the detection limit were excluded from the fitting model. The initial structural parameters of the  $\text{Bi}_2\text{SiO}_5$ -type phases were derived from the relevant crystallographic data in the literature.<sup>10,12</sup> The fitted XRD profiles and the refined parameters for each composition are shown in Fig. S1, Tables S1, and S2 in SI.

Fig. 3(a) shows the mass fraction of each phase, including the secondary phases of  $\text{Bi}_4\text{Si}_3\text{O}_{12}$  and  $\text{Bi}_{12}\text{SiO}_{20}$ , at different Ge contents ( $x$ ). With the increase in Ge content ( $x$ ) from 0 to 0.3, the fraction of the tetragonal  $\text{Bi}_2\text{SiO}_5$ -type phase monotonically decreases from 100% to 36%, and that of the monocli-

**Fig. 2** XRD patterns of the  $(\text{Bi}_{0.97}\text{La}_{0.03})_2\text{Si}_{1-x}\text{Ge}_x\text{O}_5$  ceramics with  $x = 0, 0.1, 0.2, \text{ and } 0.3$ , as well as a pristine  $\text{Bi}_2\text{SiO}_5$  ceramic. (Bottom panel) Reference patterns of monoclinic and tetragonal  $\text{Bi}_2\text{SiO}_5$ .**Fig. 3** (a) Mass fractions of  $\text{Bi}_2\text{SiO}_5$ -type (monoclinic and tetragonal),  $\text{Bi}_4\text{Si}_3\text{O}_{12}$ -type, and  $\text{Bi}_{12}\text{SiO}_{20}$ -type phases at different  $x$ ; (b) crystallite size of  $\text{Bi}_2\text{SiO}_5$ -type (monoclinic and tetragonal) phases against  $x$ .

nic  $\text{Bi}_2\text{SiO}_5$ -type phase increases from 0% to 53%. This indicates that the ratio of the tetragonal and monoclinic phases can be easily and widely tuned through the incorporation of Ge into La-substituted  $\text{Bi}_2\text{SiO}_5$ . The Ge-substituted samples ( $x = 0.1$ – $0.3$ ) also contain  $\text{Bi}_4\text{Si}_3\text{O}_{12}$  and  $\text{Bi}_{12}\text{SiO}_{20}$  with a total mass fraction of approximately 10%. Although these secondary phases are difficult to completely remove from the Ge-substituted samples at this stage, their effects on the TCC of the resulting ceramics should be limited because of their small mass fractions and low dielectric permittivities ( $\epsilon_r = 8.8$  for  $\text{Bi}_4\text{Si}_3\text{O}_{12}$  and  $\epsilon_r = 37.6$  for  $\text{Bi}_{12}\text{SiO}_{20}$ ).<sup>21,22</sup> Additionally, as shown in Table S2, the lattice volume of the tetragonal and monoclinic  $\text{Bi}_2\text{SiO}_5$ -type phases tends to increase with the Ge content, confirming the incorporation of Ge into the Si site.

Fig. 3(b) shows the crystallite sizes of the tetragonal and monoclinic phases obtained from Rietveld refinement as functions of the Ge content. The crystallite size of the tetragonal phase is 95 nm at  $x = 0$  and monotonically decreases with increasing  $x$  to 38 nm at  $x = 0.3$ . Conversely, the crystallite size of the monoclinic phase increases with  $x$  from 25 nm at  $x = 0.1$  to 65 nm at  $x = 0.3$ . Interestingly, the sum of the crystallite sizes of the two phases is almost constant, approximately 100 nm. Fig. 4 shows the FE-SEM images of the fracture surfaces of the  $(\text{Bi}_{0.97}\text{La}_{0.03})_2\text{Si}_{1-x}\text{Ge}_x\text{O}_5$  ceramics. Although the grain boundaries are not well defined, grains of several hundred nanometers are observed in the sample with  $x = 0$ . In contrast to the crystallite size, the grain size is less dependent on the Ge content. Thus, the structural characterization results shown above indicate that the samples co-substituted with La and Ge have intragranular-type nanocomposite structures with nanosized crystallites of the monoclinic phase formed in the matrix grains of the tetragonal phase.<sup>23</sup>

Fig. 5(a) shows the temperature dependence of  $\epsilon_r$  for the  $(\text{Bi}_{0.97}\text{La}_{0.03})_2\text{Si}_{1-x}\text{Ge}_x\text{O}_5$  ceramics measured at 1 MHz over a wide temperature range, from  $-170$  to  $450$  °C. As previously

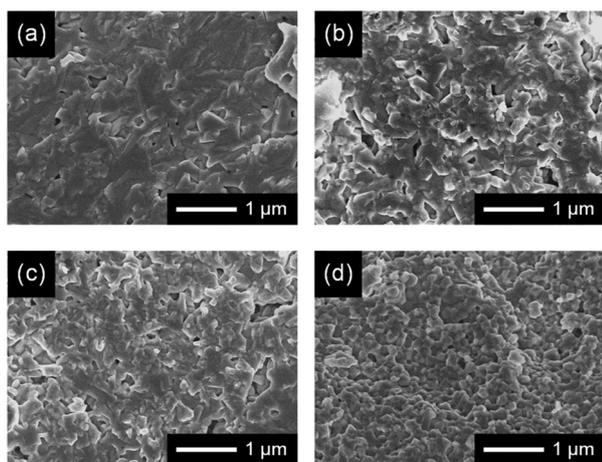


Fig. 4 FE-SEM images of the fracture surface of  $(\text{Bi}_{0.97}\text{La}_{0.03})_2\text{Si}_{1-x}\text{Ge}_x\text{O}_5$  ceramics with  $x$  of (a) 0, (b) 0.1, (c) 0.2, and (d) 0.3.

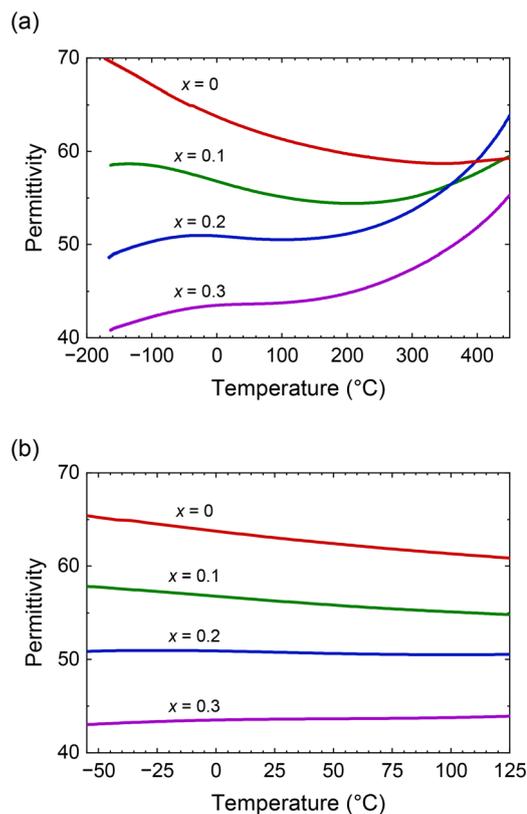
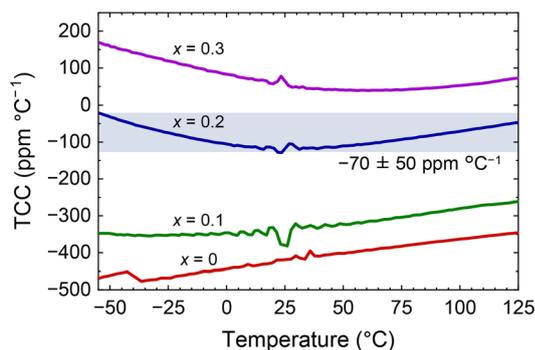


Fig. 5 (a) Temperature dependence of the dielectric permittivity for  $(\text{Bi}_{0.97}\text{La}_{0.03})_2\text{Si}_{1-x}\text{Ge}_x\text{O}_5$  ceramics with  $x = 0, 0.1, 0.2,$  and  $0.3$  in the temperature range of  $-170$  to  $450$  °C. (b) Enlarged view of the dielectric permittivity in the temperature range from  $-55$  to  $125$  °C.

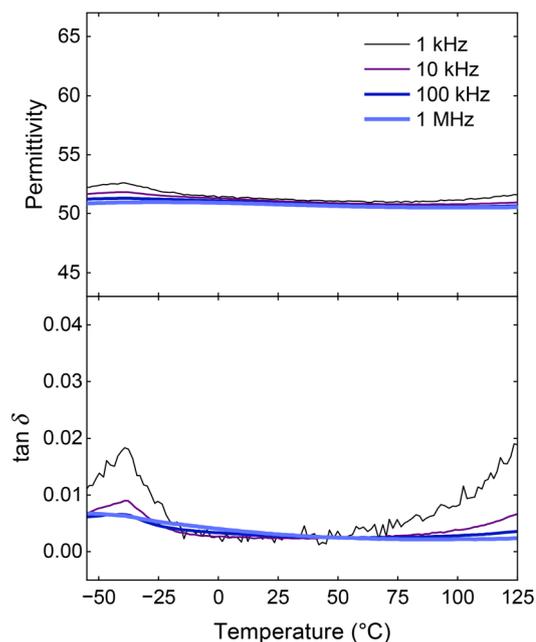
reported, the curve for the sample without Ge ( $x = 0$ ) exhibits a relatively large negative slope.<sup>9</sup> As the Ge content increases, the slope gradually changes from negative to positive at temperatures below  $200$  °C. Additionally,  $\epsilon_r$  of the co-substituted samples ( $x = 0.1, 0.2,$  and  $0.3$ ) rapidly increases with temperature above  $200$  °C. The positive temperature dependence of  $\epsilon_r$  in these samples at elevated temperatures is attributed to the ferroelectric phase transition of the monoclinic phase at  $T_C$ . The absence of a dielectric peak would be ascribed to the shift of the  $T_C$  of the monoclinic phase in these samples to above  $450$  °C because of the stabilization effect of the ferroelectric phase by the Ge substitution.<sup>17</sup> In fact, the permittivity of a  $\text{Bi}_2\text{GeO}_5$  glass-ceramic has also been reported to show no peak at temperatures up to  $450$  °C, suggesting that the  $T_C$  of  $\text{Bi}_2\text{GeO}_5$  is substantially higher than that of  $\text{Bi}_2\text{SiO}_5$ .<sup>24</sup> Fig. 5(b) compares the temperature stability of  $\epsilon_r$  from  $-55$  to  $125$  °C, which is the temperature range used to classify Class I MLCCs.<sup>1</sup> Notably, the samples with  $x = 0.2$  and  $0.3$  show very stable permittivity in this temperature range. In particular, the sample with  $x = 0.2$  exhibits  $\epsilon_r > 50$  and superior temperature stability of  $\epsilon_r$ .

To quantitatively evaluate the temperature stability of the dielectric permittivity, we calculated the TCC from the temperature dependence of capacitance using eqn (1) (Fig. 6). As





**Fig. 6** Temperature dependence of TCC for  $(\text{Bi}_{0.97}\text{La}_{0.03})_2\text{Si}_{1-x}\text{Ge}_x\text{O}_5$  ceramics with  $x = 0, 0.1, 0.2,$  and  $0.3$  in the temperature range from  $-55$  to  $125$  °C. The blue shaded area indicates the range of TCC variation in this temperature range for the  $x = 0.2$  sample. The fluctuations in the TCC near room temperature were attributed to random errors in the measured capacitance.



**Fig. 7** Temperature dependences of the dielectric permittivity (top panel) and dielectric loss (bottom panel) for  $(\text{Bi}_{0.97}\text{La}_{0.03})_2\text{Si}_{0.8}\text{Ge}_{0.2}\text{O}_5$ , measured at 1 kHz–1 MHz.

TCC is the slope of the capacitance *versus* temperature curve, the closer TCC is to 0, the weaker the temperature dependence. The sample without Ge ( $x = 0$ ) exhibits a strongly negative TCC, between  $-350$  ppm and  $-480$  ppm °C $^{-1}$ , over the entire temperature range. The increase in Ge content up to  $x = 0.2$  pushes TCC closer to 0, with TCC becoming positive at  $x = 0.3$ . Among the samples tested herein, the sample with  $x = 0.2$ , which consists of almost equal amounts of the tetragonal and monoclinic phases, exhibits the best temperature stability, with TCC =  $-70 \pm 50$  ppm °C $^{-1}$  in the temperature range from  $-55$  to  $125$  °C. Fig. 7 shows the temperature dependences of  $\epsilon_r$  and  $\tan \delta$  for the  $x = 0.2$  sample (which showed the best dielectric performance) at frequencies of 1 kHz–1 MHz. Data for all samples over the entire temperature range are shown in Fig. S2 in SI. The dielectric loss peak at  $-40$  °C can be attributed to the dielectric relaxation of ice formed from water molecules absorbed in the pores of the samples.<sup>25</sup> Although the dielectric loss tends to increase at temperatures above  $50$  °C, it remains less than 0.02 even at  $125$  °C and the lowest frequency of 1 kHz. The observed dielectric loss is larger than that of  $\text{CaZrO}_3$ -based materials, which is likely attributed to factors such as adsorbed water and oxide ion conduction. Therefore, further improvements in density and doping with aliovalent cations may help to reduce the dielectric loss. Additionally,  $\epsilon_r$  does not considerably depend on the measurement frequency, confirming that the superior dielectric temperature stability of this sample is its intrinsic property than a result of extrinsic contributions such as electrical conduction.

Here, we discuss the formation process of the paraelectric-ferroelectric nanocomposite structure in  $(\text{Bi}_{0.97}\text{La}_{0.03})_2\text{Si}_{1-x}\text{Ge}_x\text{O}_5$  ceramics, as well as the mechanism through which their dielectric temperature stability improves. To gain insight into the nanocomposite structure, we first prepared a powder with the composition of  $x = 0.2$  using the same process as for the ceramic sample, but without pressing. The XRD measurement confirmed that the intensity ratio of the diffraction peaks from the tetragonal and monoclinic phases of the powder sample are similar

to those of the ceramic sample (Fig. S3 in SI). This suggests that the phase separation is not caused by mechanical effects related to the grain structure of ceramics. Then, we performed HAADF-STEM-EDS observations on ten different particles from the powder. Fig. 8 shows the HAADF-STEM-EDS elemental mapping of one representative particle, while the results for all particles are shown in Fig. S4 in SI. Since the crystalline sizes of the two phases, as determined by XRD, are both about 50 nm for this composition, regions of size about 50 nm separated by abrupt changes in composition should be observed if the phase separation occurs due to the nucleation and growth mechanism.<sup>26</sup> However, the results of the observation show that all constituent elements are uniformly distributed in each particle within the resolution range of the instrument, indicating that the nanocomposite structure has not formed through nucleation and growth. We believe that the phase separation in  $(\text{Bi}_{0.97}\text{La}_{0.03})_2\text{Si}_{1-x}\text{Ge}_x\text{O}_5$  occurs *via* the spinodal decomposition mechanism, which is similar to that observed in the  $\text{TiO}_2$ - $\text{SnO}_2$  and  $\text{TiO}_2$ - $\text{VO}_2$  systems.<sup>27–29</sup> However, since the spinodal decomposition is expected to be in its early stage after one hour of firing, the amplitude of the concentration fluctuations is small, making it difficult to detect using HAADF-STEM-EDS. A similar situation has been reported regarding the formation of lamellar-type phase separation structures in  $\text{TiO}_2$ - $\text{VO}_2$  films.<sup>27</sup> To further understand the phase separation mechanism in  $(\text{Bi}_{0.97}\text{La}_{0.03})_2\text{Si}_{1-x}\text{Ge}_x\text{O}_5$ , it is important to observe the time evolution of the two-phase separation structure. However, extending the heat treatment time causes the  $\text{Bi}_2\text{SiO}_5$ -type phases to decompose into the secondary phases, making this difficult at present.



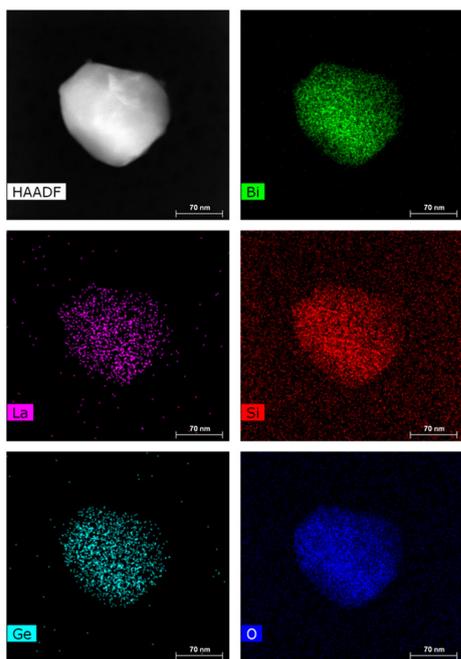


Fig. 8 HAADF-STEM-EDS elemental mapping of a  $(\text{Bi}_{0.97}\text{La}_{0.03})_2\text{Si}_{0.8}\text{Ge}_{0.2}\text{O}_5$  particle.

Fig. 9 shows a schematic illustration of the mechanism for improving the dielectric temperature stability in  $(\text{Bi}_{0.97}\text{La}_{0.03})_2\text{Si}_{1-x}\text{Ge}_x\text{O}_5$  ceramics. The sample without Ge ( $x = 0$ ) consists of the single tetragonal (paraelectric) phase, which

shows a negative temperature dependence of  $\epsilon_r$ . The incorporation of Ge results in the nucleation of the monoclinic (ferroelectric) phase with a positive temperature dependence of  $\epsilon_r$  in the matrix of the tetragonal phase. The crystallite size of the monoclinic phase increases with the Ge content, leading to the spontaneous formation of a paraelectric–ferroelectric composite structure. The incorporation of Ge also shifts the  $T_C$  of the ferroelectric phase toward higher temperatures. The contents of the paraelectric and ferroelectric phases become almost equal at  $x = 0.2$ , resulting in the minimal temperature dependence of TCC  $-70 \pm 50 \text{ ppm } ^\circ\text{C}^{-1}$  because of the opposite contributions of the two phases. As for the microstructures, it is unclear at this stage whether the small grain size or crystallite size of the samples obtained in this study affects the dielectric temperature stability. However, it is generally known that in ferroelectric ceramics, a reduction in grain size suppresses the development of ferroelectric order due to mechanical stress at grain boundaries, thereby broadening the temperature dependence of the dielectric permittivity.<sup>30–32</sup> Therefore, it is possible that the small grain and crystallite sizes in this study also contribute to the improved temperature stability.

Although the achieved TCC of  $-70 \pm 50 \text{ ppm } ^\circ\text{C}^{-1}$  does not meet the requirement for the C0G specification of MLCC, it is substantially smaller than that of conventional paraelectric ceramics such as  $\text{TiO}_2$  ( $-820 \text{ ppm } ^\circ\text{C}^{-1}$ ,  $\epsilon_r = 114$  at  $25^\circ\text{C}$ ) and  $\text{CaTiO}_3$  ( $-1442 \text{ ppm } ^\circ\text{C}^{-1}$ ,  $\epsilon_r = 174$  at  $25^\circ\text{C}$ ).<sup>33,34</sup> In addition, the dielectric permittivity of the  $x = 0.2$  sample ( $\epsilon_r = 52$  at  $25^\circ\text{C}$ ) is higher than that of  $\text{CaZrO}_3$  ( $\epsilon_r = 30$ ), which is used in

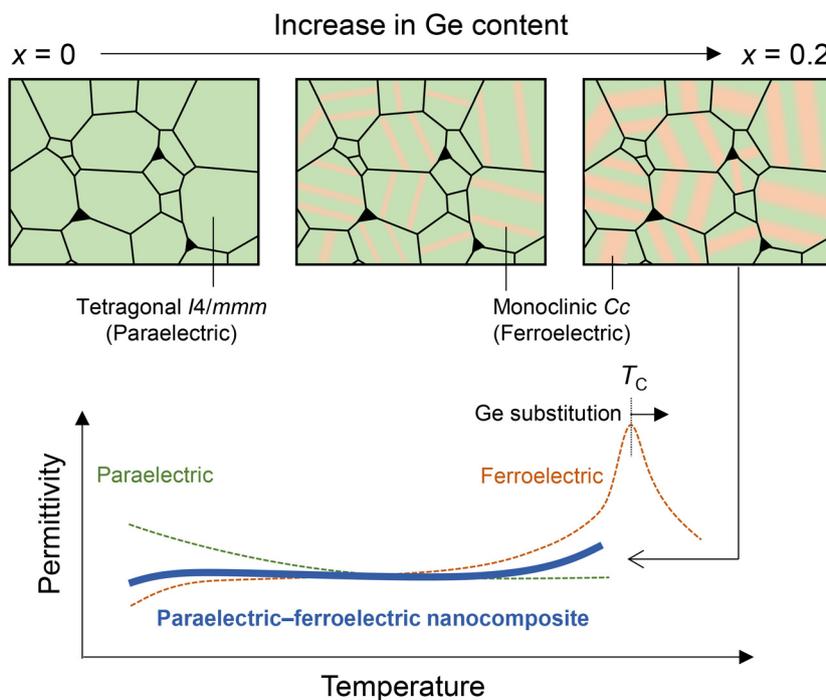


Fig. 9 Schematic of the mechanism for improving the dielectric temperature stability of  $(\text{Bi}_{0.97}\text{La}_{0.03})_2\text{Si}_{1-x}\text{Ge}_x\text{O}_5$  ceramics. Note that the lamellar-type phase separation structure is not based on observed results, and other forms are also possible.



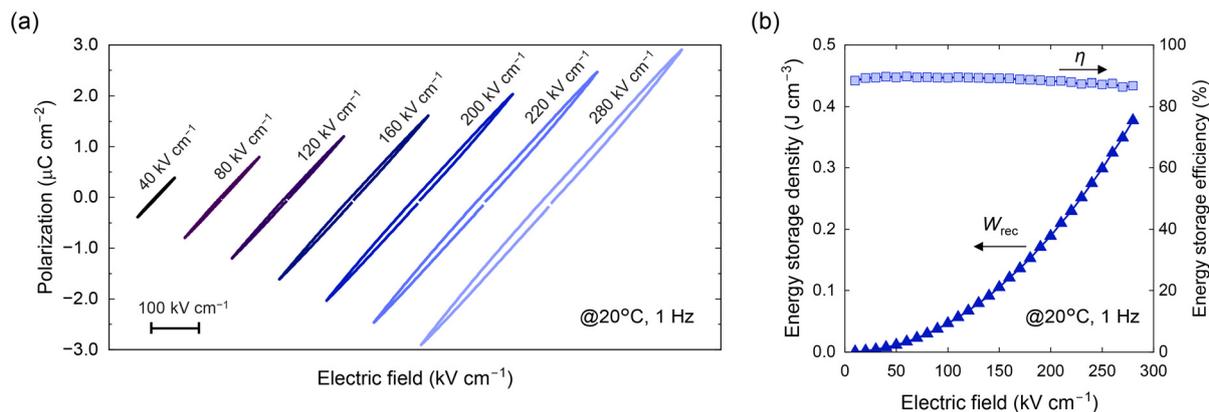


Fig. 10 (a) Bipolar  $P$ - $E$  hysteresis loops and (b) energy storage properties of  $(\text{Bi}_{0.97}\text{La}_{0.03})_2\text{Si}_{0.8}\text{Ge}_{0.2}\text{O}_5$  ceramics measured at different maximum electric fields (20–280  $\text{kV cm}^{-1}$ ).

the commercial C0G MLCCs.<sup>35</sup> It is also important to note that the samples prepared herein are not perfectly densified because of the difficulty of sintering. According to ref. 13,  $\epsilon_r$  values of fully dense ceramics of monoclinic  $\text{Bi}_2\text{SiO}_5$  and tetragonal  $(\text{Bi}_{0.97}\text{La}_{0.03})_2\text{SiO}_5$ , which were crystallized from corresponding glasses, are approximately 200 and 160 at room temperature, respectively—both significantly higher than that of the  $x = 0.2$  sample fabricated in this study. Therefore, although further improvement in density is unlikely to reduce the TCC, it may lead to a significant increase in  $\epsilon_r$ . Thus, we believe that  $\text{Bi}_2\text{SiO}_5$  co-substituted with La and Ge shows great promise for applications in Class I MLCCs.

The direct measurement of the TCF values of the samples prepared in this study has not yet been carried out. However, based on the variable-temperature XRD data shown in ref. 13, the linear thermal expansion coefficients ( $\alpha_L$ ) near room temperature are reported to be 6.8  $\text{ppm } ^\circ\text{C}^{-1}$  for the monoclinic ferroelectric phase (pristine  $\text{Bi}_2\text{SiO}_5$ ) and 9.8  $\text{ppm } ^\circ\text{C}^{-1}$  for the tetragonal paraelectric phase (La-substituted  $\text{Bi}_2\text{SiO}_5$ ). Using these values and the volume fraction of the two phases [Fig. 3(a)], the linear thermal expansion coefficient of the  $x = 0.2$  sample can be roughly estimated to be 8.0  $\text{ppm } ^\circ\text{C}^{-1}$  by applying the rule of mixtures. Accordingly, the temperature coefficient of resonant frequency (TCF) of this sample is estimated to be  $\text{TCF} = -(\text{TCC} + \alpha_L)/2 = 31 \pm 25 \text{ ppm } ^\circ\text{C}^{-1}$ , suggesting that it may also exhibit a favorable TCF as a microwave dielectric material.

Polarization response under high electric fields is also an important factor for MLCC applications. Fig. 10(a) shows the bipolar  $P$ - $E$  curves of the sample with  $x = 0.2$  measured at 20  $^\circ\text{C}$  and varying electric field amplitudes up to dielectric breakdown. Despite incomplete densification, the sample withstands electric fields up to 280  $\text{kV cm}^{-1}$ . All  $P$ - $E$  curves show linear behavior with a small hysteresis, probably because of leakage. In contrast to undoped  $\text{Bi}_2\text{SiO}_5$  ceramics,<sup>10,11</sup> no hysteresis associated with ferroelectric polarization switching is observed, even though this sample contains over 40% of the ferroelectric phase. Given the high  $T_C$  above 450  $^\circ\text{C}$  owing to

the Ge substitution, the absence of ferroelectric switching would be attributed to a high coercive field of the ferroelectric phase. Such a paraelectric-like linear polarization response is suitable for high-voltage applications because the effective  $\epsilon_r$  of normal ferroelectrics is greatly reduced under bias voltages owing to ferroelectric polarization switching.<sup>36,37</sup> We also calculated the recoverable energy storage density ( $W_{\text{rec}}$ ) and energy storage efficiency ( $\eta$ ) of this sample using the following equations:<sup>38</sup>

$$W_{\text{rec}} = \int_{P_r}^{P_m} E dP \quad (2)$$

$$\eta = \frac{W_{\text{rec}}}{W_{\text{rec}} + W_{\text{loss}}} \quad (3)$$

where  $P_m$ ,  $P_r$ , and  $W_{\text{loss}}$  are the maximum polarization, remanent polarization, and hysteresis loss, respectively. Fig. 10(b) shows the electric field dependence of  $W_{\text{rec}}$  and  $\eta$ . Owing to the linear polarization response of the sample,  $W_{\text{rec}}$  quadratically increases with the field strength, reaching 0.38  $\text{J cm}^{-3}$  before the dielectric breakdown, while maintaining  $\eta$  values over 85% even at the maximum electric field. The obtained  $W_{\text{rec}}$  value is higher than those of undoped  $\text{Bi}_2\text{SiO}_5$  ( $W_{\text{rec}} = 0.06 \text{ J cm}^{-3}$ ) and La-substituted  $\text{Bi}_2\text{SiO}_5$  ( $W_{\text{rec}} = 0.29 \text{ J cm}^{-3}$ ).<sup>11</sup> Thus, this result also suggests that the co-substitution with La and Ge is a promising strategy for improving the dielectric properties of  $\text{Bi}_2\text{SiO}_5$  ceramics.

## Conclusions

$\text{Bi}_2\text{SiO}_5$  ceramics co-substituted with La and Ge, with the compositions of  $(\text{Bi}_{0.97}\text{La}_{0.03})_2\text{Si}_{1-x}\text{Ge}_x\text{O}_5$  ( $x = 0-0.3$ ), were prepared *via* the sol-gel process. We found that  $\text{Ge}^{4+}$  ions at the  $\text{Si}^{4+}$  site stabilize the ferroelectric phase and increase its  $T_C$ , whereas  $\text{La}^{3+}$  ions at the  $\text{Bi}^{3+}$  site break the long-range ferroelectric order, leading to the spontaneous formation of ferroelectric-paraelectric composites with a crystallite size below 100 nm at



$x = 0.1$ – $0.3$ . The co-substitution with La and Ge substantially improved the dielectric stability of  $\text{Bi}_2\text{SiO}_5$  ceramics because of the canceling out of the positive and negative temperature dependences of the ferroelectric and paraelectric phases, respectively. The ceramics with  $x = 0.2$  showed the best temperature stability of  $-70 \pm 50$  ppm  $^\circ\text{C}^{-1}$  with  $\epsilon_r > 50$  as well as the high dielectric breakdown strength of  $280$  kV  $\text{cm}^{-1}$  and highly linear polarization response. As we could not attain complete densification of the prepared samples, further investigations of the densification process are needed to pave the way for the transfer of this material into practical applications.

## Author contributions

Yoji Yasumoto: investigation, writing – original draft. Taro Kuwano: investigation. Hiroki Taniguchi: conceptualization, funding acquisition. Shinobu Fujihara: project administration, supervision. Manabu Hagiwara: conceptualization, investigation, funding acquisition, writing – review & editing, project administration, supervision.

## Conflicts of interest

There are no conflicts to declare.

## Data availability

The data that support the findings of this study are available within the article and its SI. Additional raw data are available from the corresponding author, Manabu Hagiwara, upon reasonable request.

Rietveld refinement results; Dielectric properties; XRD patterns; HAADF-STEM-EDS elemental mapping. See DOI: <https://doi.org/10.1039/d5dt01380a>

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